

#Pr 18.2 (Complex potential)

restart;

F := arcsin(z);

$$F := \arcsin(z) \quad (1)$$

z := x + I·y;

$$z := x + Iy \quad (2)$$

phi := evalc(Re(F));

$$\phi := -\arcsin\left(-\frac{\sqrt{(x+1)^2 + y^2}}{2} + \frac{\sqrt{(x-1)^2 + y^2}}{2}\right) \quad (3)$$

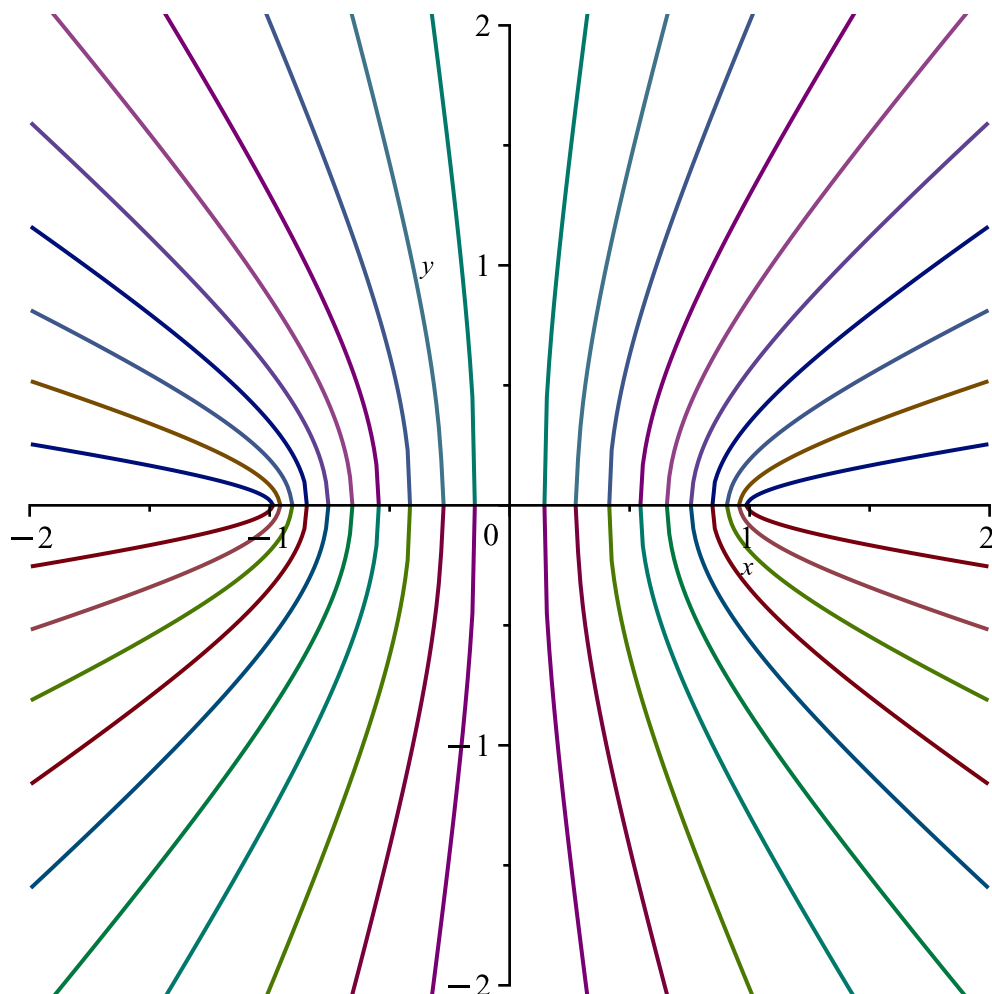
y := solve(phi = k, y);

$$y := -\frac{\sqrt{\cos(k)^2 x^2 + \sin(k)^4 + \cos(k)^2 - 1}}{\sin(k)}, \frac{\sqrt{\cos(k)^2 x^2 + \sin(k)^4 + \cos(k)^2 - 1}}{\sin(k)} \quad (4)$$

S := seq(y, k = 1 .. 10) :

y := 'y':

plot([S], x = -2 .. 2, y = -2 .. 2, scaling = constrained);



#Pr 18.5 (Pair of opposite electrical charges)

restart;

$$F := \ln\left(-\frac{(z+1)}{z-1}\right);$$

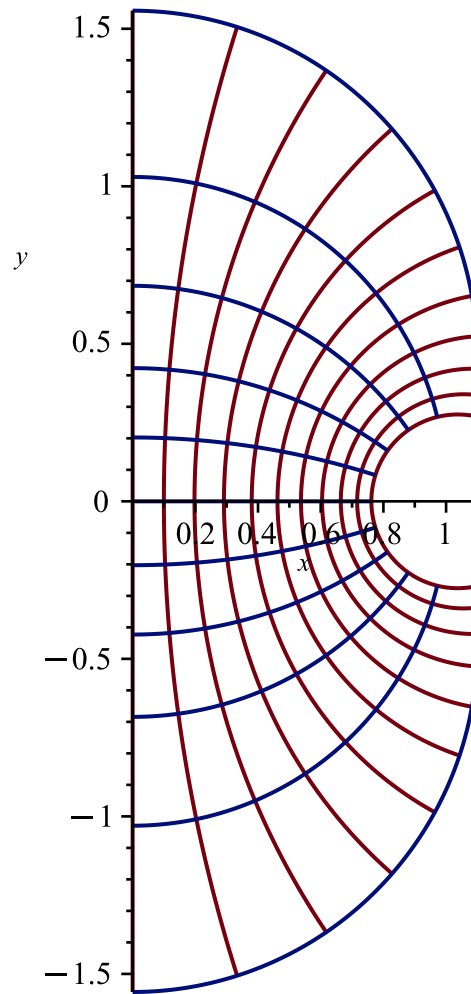
$$F := \ln\left(-\frac{z+1}{z-1}\right) \quad (5)$$

w := solve(F=k, z);

$$w := \frac{e^k - 1}{e^k + 1} \quad (6)$$

with(plots) :

*conformal(w, k=-2..2 + 2*I, scaling=constrained, labels=[x, y]);*



#Pr 18.6 (Arbitrary cylinder

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restart;
z := r·exp(I· theta);
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$$z := r e^{i\theta} \quad (7)$$

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radius := 2
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$$radius := 2 \quad (8)$$

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F := z + (radius)^2 / z;
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$$F := r e^{i\theta} + \frac{4}{r e^{i\theta}} \quad (9)$$

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psi := simplify(evalc(Im(F)));
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$$\psi := \frac{\sin(\theta) (r^2 - 4)}{r} \quad (10)$$

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sol := solve(psi = K/3, r);
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$$sol := \frac{K + \sqrt{K^2 + 144 \sin(\theta)^2}}{6 \sin(\theta)}, \frac{K - \sqrt{K^2 + 144 \sin(\theta)^2}}{6 \sin(\theta)} \quad (11)$$

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S1 := seq([sol[1], theta, theta = 0.001 .. Pi - 0.001], K = 0 .. 20) :
S2 := seq([sol[2], theta, theta = 0.001 .. Pi - 0.001], K = -20 .. 0) :
with(plots) :
P1 := plot([S1], -9 .. 9, -4 .. 4, coords = polar, color = black) :
P2 := plot([S2], -9 .. 9, -4 .. 4, coords = polar, color = black) :
display(P1, P2, scaling = constrained);

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