

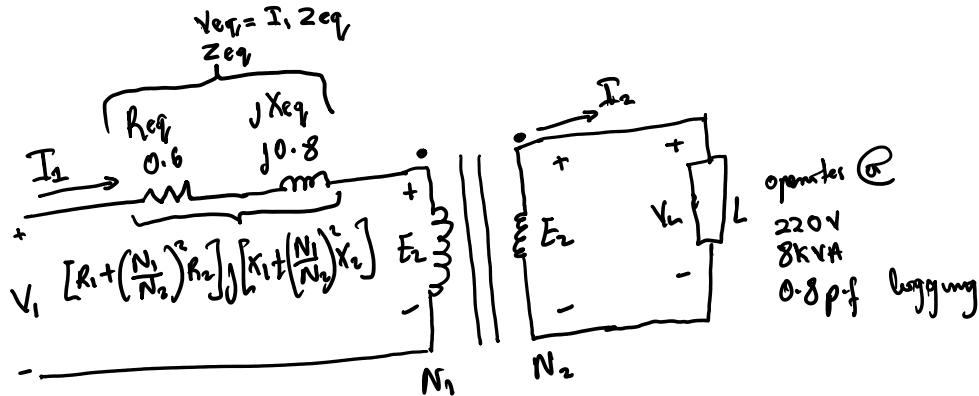
60 Hz step-down transformer [$N_m - 1$ den]

$$E_1 / E_2 = 480V / 240V @ 10kVA$$

Load: $V_L = 220V$
 $S_L = 8kVA @ 0.8 \text{ pf lagging}$

$$Z_{eq} = 0.6 + j0.8 [\Omega]$$

1a



Neglecting exciting Current

1b Load Current = I_L

$$S_L = V_L \times I_L$$

$$I_L = \frac{S_L}{V_L} \quad S_L = 8kVA \angle \cos^{-1}(0.8)$$

$$S_L = 8kVA \angle 36.87^\circ$$

$$V_L = 220V \angle 0^\circ$$

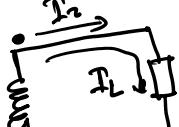
$$I_L = \frac{8kVA}{220V} \angle 36.87^\circ - 0^\circ$$

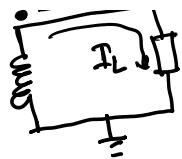
$$I_L = 36.36A \angle -36.87^\circ$$

$$\text{Primary Current } I_1 = \frac{N_2}{N_1} \times I_2 = \frac{1}{a_t} I_2$$

$$a_t = \frac{E_1}{E_2} = \frac{480V}{240V} = 2$$

$I_2 = I_L$ since N_2 winding is in series with Load



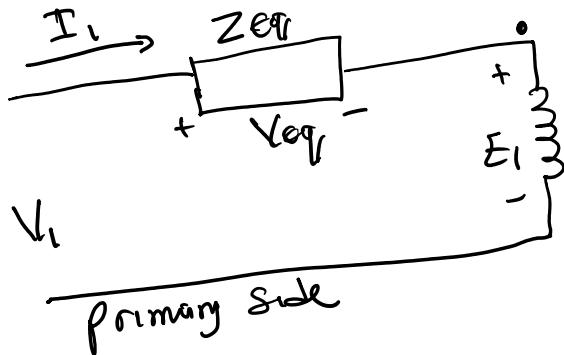


$$I_1 = \frac{1}{\alpha_t} I_L$$

$$I_1 = \frac{1}{2} (36.36 \angle -36.87^\circ [\text{A}])$$

$$I_1 = 18.18 \angle -36.87^\circ [\text{A}]$$

(10)



$$V_1 = V_{eq1} + E_1$$

$$E_1 = 480 \text{ V}$$

$$V_{eq1} = I_1 (Z_{eq1}) = (18.18 \angle -36.87^\circ [\text{A}]) (0.6 + j1.8)$$

$$V_{eq1} = (18.18 \angle -36.87^\circ [\text{A}]) (1.897 \angle 71.56^\circ [\text{A}])$$

$$V_{eq1} = 34.49 \angle 34.76^\circ [\text{V}] = 28.33 + j19.66$$

E_1 = Primary voltage of transformer

$$E_1 = 480 \text{ V}$$

$$V_1 = [28.33 + j19.66] \text{ V} + [480 + j0] \text{ V}$$

$$V_1 = 508.33 + j19.66 [\text{V}]$$

(1d)

$$S_1 = I_1 V_1 = (18.18 \angle -36.8^\circ [A]) \times (508.83 + j 19.66 [V])$$

$$S_1 = (18.18 \angle -36.8^\circ [A]) (508.71 \angle 2.2^\circ [V])$$

$$S_1 = 9248.35 \angle -34.59^\circ [\text{VA}]$$

$$S_1 = 9.25 \angle -34.59^\circ [\text{kVA}]$$

$$P_1 = 9.25 \cos(-34.59) [\text{kW}]$$

$$P_1 = 7.62 [\text{kW}]$$

$$Q_1 = j 9.25 \sin(-34.59) [\text{kVAR}]$$

$$Q_1 = -j 5.25 [\text{kVAR}]$$

(1e)

$$S_1 = I_1^2 Z_{in}$$

$$Z_{in} = \frac{S_1}{I_1^2} = \frac{9.25 \angle -34.59^\circ [\text{kVA}]}{(18.18 \angle -36.8^\circ [A])^2}$$

$$Z_{in} = 27.99 \angle -34.59^\circ - 2(-36.8^\circ) [\Omega]$$

$$Z_{in} = 27.99 \angle 39.01^\circ [\Omega]$$

$$Z_{in} = 21.75 + j 17.62 [\Omega]$$

$$Z_{eq} = Z_{in} + Z_L$$

$$Z_L = Z_{eq} - Z_{in} = (21.74 + j 17.62) [\Omega]$$

$$Z_L = Z_{eq} - Z_{in}$$
$$Z_L = (0.6 + j1.8) - (21.74 + j17.62) \quad [\Omega]$$

$$Z_L = 21.14 - j15.82$$

$$R_L = 21.14 \quad X_L = -j15.82 \quad [\Omega]$$

$$P_{in} = 6.47 \text{ kW}$$

(1) Efficiency = $\frac{P_{out}}{P_{in}}$

$$P_{out} = S_L \times P.f$$

$$P_{out} = 8 \text{ kVA} \times 0.8$$

$$P_{out} = 6.4 \text{ kW}$$

$$\text{Efficiency } \eta = \frac{6.4 \text{ kW}}{6.47 \text{ kW}} = 98.9\%$$

$$S_{\text{rated}} = 10 \text{ [kVA]} \quad [V_1 : V_2]_{\text{rated}} = 480V : 240V$$

$$S_{\text{base}} = S_{\text{rated}} = 10 \text{ [kVA]} \quad V_{1\text{base}} = 480V$$

$$V_{2\text{base}} = 240V$$

$$I_{1\text{base}} = \frac{S_{\text{base}}}{V_{1\text{base}}}$$

$$I_{2\text{base}} = \frac{S_{\text{base}}}{V_{2\text{base}}}$$

$$I_{1\text{base}} = \frac{10 \text{ [kVA]}}{480V} = 20.83A$$

$$I_{2\text{base}} = \frac{10 \text{ [kVA]}}{240V} = 41.67A$$

$$Z_{1\text{base}} = \frac{V_{1\text{base}}}{I_{1\text{base}}} = \frac{480V}{20.83A} = 23.04 \Omega$$

$$Z_{2\text{base}} = \frac{V_{2\text{base}}}{I_{2\text{base}}} = \frac{240V}{41.67A} = 5.75 \Omega$$

p.u value using #1b

$$I_L = 36.36A \angle -36.87^\circ$$

$$I_{L\text{p.u.}} = \frac{I_L}{I_{2\text{base}}} = \frac{36.36}{41.67} \angle -36.87^\circ$$

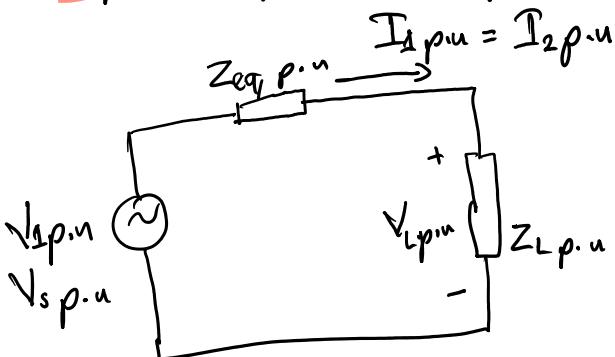
$$I_{L\text{p.u.}} = 0.87 \angle -36.87^\circ$$

$$I_1 = 18.18 \angle -36.87^\circ \text{ [A]}$$

$$I_{1\text{p.u.}} = \frac{18.18}{20.83} \angle -36.87^\circ$$

$$I_{1\text{p.u.}} = 0.87 \angle -36.87^\circ$$

$$I_{L\text{p.u.}} = I_{2\text{p.u.}} \approx I_{1\text{p.u.}} = 0.87 \angle -36.87^\circ$$



p.u value using #1c

$$V_1 = 508.33 + j 19.66 \text{ [V]}$$

$$V_1 = 508.71 \angle 2.21^\circ \text{ [V]}$$

$$V_{1\text{p.u.}} = \frac{V_1}{V_{1\text{base}}} = \frac{508.71}{480} \angle 2.21^\circ$$

$$V_{1\text{p.u.}} = 1.06 \angle 2.21^\circ$$

$$V_1 \text{ p.u} = 1.06 \angle 2.21^\circ$$

p.u value using # 1d

$$S_1 = 9.25 \angle -34.59^\circ [\text{kVA}]$$

$$S_{1 \text{ p.u}} = \frac{S_1}{S_{\text{Base}}} = \frac{9.25 \angle -34.59^\circ [\text{kVA}]}{10 [\text{kVA}]}$$

$$S_{1 \text{ p.u}} = 0.925 \angle -34.59^\circ$$

$$P_{1 \text{ p.u}} = 0.925 \angle -34.59^\circ$$

$$P_{1 \text{ p.u}} = 0.761$$

$$Q_{1 \text{ p.u}} = 0.925 \sin(-34.59^\circ)$$

$$Q_{1 \text{ p.u}} = -0.525$$

p.u value using # 1e

$$Z_{in} = 27.99 \angle -39.01^\circ [\Omega]$$

$$Z_{in \text{ p.u}} = \frac{Z_{in}}{Z_{\text{Base}}} = \frac{27.99 \angle -39.01^\circ}{23.04}$$

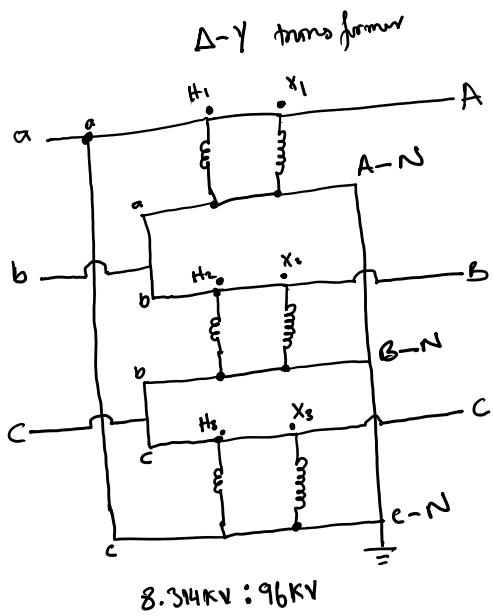
$$Z_{in \text{ p.u}} = 1.21 \angle -39.01^\circ$$

$$Z_L = 21.14 + j15.82$$

$$Z_L = 26.40 \angle 36.81^\circ (\Omega)$$

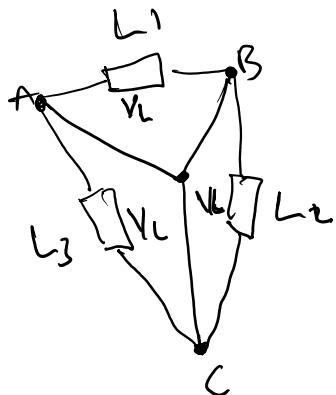
$$Z_{L \text{ p.u}} = \frac{Z_L}{Z_{\text{Base}}} = \frac{26.40}{5.75} \angle 36.81^\circ$$

$$Z_{L \text{ p.u}} = 4.59 \angle 36.81^\circ$$



$$8.34 \text{ kV} : 96 \text{ kV}$$

Secondary side of transformer



(3a) per unit quantities needed $[I_{A \text{ p.u}}, N_{\text{p.u}}]$ Short p.u

$$V_{\text{load p.u.}} = \frac{V_L / \text{phase}}{V_2 \text{ rating / phase}}$$

$$V_{\text{load p.u.}} = \frac{50 \text{ kV}}{96 \text{ kV}}$$

$V_{\text{load p.u.}} = 0.52$

$$I_{\text{load p.u.}} = \frac{I_{\text{load}}}{I_{\text{base}}} \angle -\cos^{-1} \rho \cdot f$$

$$I_{\text{load p.u.}} = \frac{4 \text{ A}}{5.41 \text{ A}} \angle -\cos^{-1}(0.707)$$

$I_{\text{load p.u.}} = 0.74 \angle -45^\circ$

$$I_{\text{base}} = \frac{S_3 \phi \text{ rating}}{V_2 \text{ rating / phase} \times \sqrt{3}} = \frac{900 \text{ kVA}}{96 \times \sqrt{3} \text{ kV}}$$

$$I_{\text{base}} = 5.41 \text{ A}$$

$$I_{\text{load}} = \frac{S_{\text{load 1\phi}}}{V_{\text{load 1\phi}}} = \frac{400 \text{ kVA}}{150 \text{ kV}}$$

$I_{\text{load}} = 4 \text{ A}$

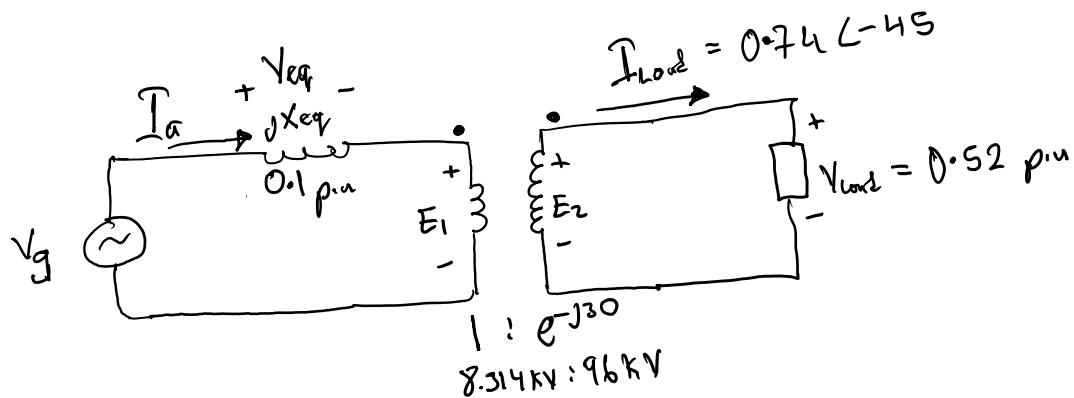
$$I_{load \text{ p.u}} = 0.74 \angle -45^\circ$$

$$I_{load} = 4 \text{ A}$$

$$S_{load \text{ p.u}} = \frac{S_{load} + \phi}{S_3 \phi / 3}$$

$$S_{load \text{ p.u}} = \frac{200 \text{ kV}}{\underline{9100 \text{ kV}} / 3}$$

$$S_{load \text{ p.u}} = 0.67$$



$$(3b) V_g = V_{eq} + E_1$$

$$V_{eq} = I_a \times jX_{eq}$$

$$I_a = \frac{N_2}{N_1} \times I_L \angle (\theta - 30^\circ)$$

$$I_a = \frac{96 \text{ kV}}{8.314 \text{ kV}} \times 0.74 \angle (-45 - 30)^\circ$$

$$I_a = 8.54 \angle -75^\circ [\text{A}]$$

$$V_{eq} = (8.54 \angle -75^\circ)(j0.1)$$

$$V_{eq} = 0.825 + j0.221 \text{ p.u}$$

$$E_1 = V_L \angle \theta_L - 30^\circ = 0.52 \angle -30^\circ$$

$$E_1 = 0.45 - j0.26$$

$$\text{V}_g = \text{V}_{eq} + E_1$$
$$\text{V}_g = (0.825 + j0.221) + (0.45 - j0.26)$$

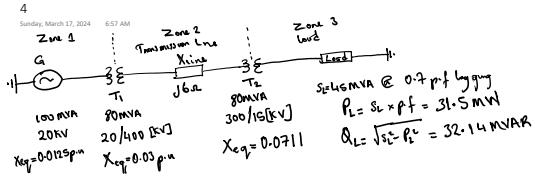
$$\text{V}_g = 1.275 - j0.039 \text{ p.u}$$

$$\text{V}_g = 1.28 \angle -1.75^\circ \text{ p.u}$$

$$\text{V}_{g_{\text{magnitude}}} = \text{V}_g \text{ p.u} \times \text{V}_{g_{\text{base}}}$$

$$\text{V}_{g_{\text{magnitude}}} = (1.28 \angle -1.75^\circ \text{ p.u}) (8.314 \text{ kV})$$

$$\text{V}_{g_{\text{magnitude}}} = 10.64 \angle -1.75^\circ [\text{kV}]$$



(4b) Using system base of 100 MVA of Voltage @ T_1 primary = 10 kV
 " " " T_1 secondary = 10 kV

Determine Base Values of each Zone

Zone 1

$$V_{g_{base}} = \frac{10 \text{ kV}}{20 \text{ kV}} = 0.5 \angle 0^\circ \text{ p.u.}$$

$$S_{base} = 100 \text{ MVA}$$

$$Z_{1base} = \frac{(V_{g_{base}})^2}{S_{base}}$$

$$V_{1base} = 20 \text{ kV}$$

$$Z_{1base} = \frac{(20 \text{ kV})^2}{100 \text{ MVA}} = 4 \Omega$$

$$I_{1base} = \frac{V_{1base}}{Z_{1base}} = 5 \text{ kA}$$

$$I_{1base} = 5 \text{ kA}$$

Zone 2

$$V_{2base} = \left(\frac{400}{20} \right) (20) = 400 \text{ kV}$$

$$Z_{2base} = \frac{(400 \text{ kV})^2}{100 \text{ MVA}} = 1.6 \text{ k}\Omega$$

$$I_{2base} = \frac{V_{2base}}{Z_{2base}} = \frac{400 \text{ kV}}{1.6 \text{ k}\Omega} = 250 \text{ A}$$

Determine per unit values

$$Z_{p.u. new} = Z_{p.u. old} \left(\frac{V_{base old}}{V_{base new}} \right)^2 \left(\frac{S_{base new}}{S_{base old}} \right)$$

At Zone 1

$$Z_{1p.u. new} = 0.03 \left(\frac{20 \text{ kV}}{300 \text{ kV}} \right)^2 \left(\frac{100 \text{ MVA}}{80 \text{ MVA}} \right)$$

$$Z_{1p.u. new} = 0.0375 \text{ p.u.}$$

$$V_{1p.u.} = \frac{10 \text{ kV}}{20 \text{ kV}} = 0.5 \text{ p.u.}$$

$$Z_{2p.u.} = \frac{(V_{1p.u.})^2}{Z_{1base}}$$

$$Z_{2p.u.} = \frac{(10 \text{ kV})^2}{4 \Omega} = 25 \text{ p.u.}$$

$$Z_{2p.u.} = 0.25 \text{ p.u.}$$

$$V_{2base} = \left(\frac{400}{20} \right) (20) = 400 \text{ kV}$$

$$Z_{2base} = \frac{(400 \text{ kV})^2}{100 \text{ MVA}} = 1.6 \text{ k}\Omega$$

$$I_{2base} = \frac{400 \text{ kV}}{1.6 \text{ k}\Omega} = 250 \text{ A}$$

At Zone 2

$$Z_{2p.u. new} = 0.0711 \left(\frac{300 \text{ kV}}{400 \text{ kV}} \right)^2 \left(\frac{100 \text{ MVA}}{80 \text{ MVA}} \right)$$

$$Z_{2p.u. new} = 0.05 \text{ p.u.}$$

At the Transmission Line

$$X_{line p.u.} = \frac{X_{line}}{Z_{2base}} = \frac{6 \Omega}{1.6 \Omega} = 0.00375 \text{ p.u.}$$

At zone 3

$$Z_{load} = \frac{S_{load}}{V_{load}} \quad S_{load} = 45 \text{ MVA} @ 0.7 \text{ pf lagging}$$

$$V_{load} = 10 \text{ KV}$$

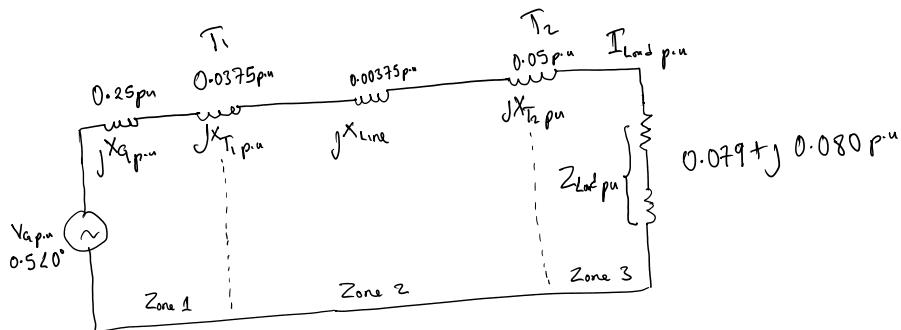
$$Z_{load} = \frac{45 \text{ MVA}}{(10 \text{ KV})^2} \angle -60^\circ 0.7$$

$$Z_{load} = 0.45 \angle -45.57^\circ$$

$$Z_{load} = 0.315 + j 0.321 \text{ [a]}$$

$$Z_{load \text{ pu}} = \frac{0.315 + j 0.321}{4 \text{ a}}$$

$$Z_{load \text{ pu}} = 0.079 + j 0.080 \text{ p.u}$$



(4c)

$$I_{load \text{ p.u.}} = \frac{V_{apu} \text{ p.u.}}{Z_{Total}}$$

$$Z_{Total} = j(0.25 + 0.0375 + 0.00375 + 0.05) + (787.5 + j802.5)$$

$$Z_{Total} = 0.079 + j 0.4213 \text{ from matlab}$$

$$I_{load \text{ p.u.}} = \frac{0.5 \angle 0^\circ}{0.079 + j 0.4213}$$

$$I_{load \text{ p.u.}} = 0.215 - j 1.147 \text{ from matlab}$$

$$I_{base} = 5 \text{ KA from above}$$

$$I_{actual} = I_{base} \times I_{load \text{ p.u.}}$$

$$I_{actual} = 5 \text{ KA} (0.215 - j 1.147)$$

$$I_{actual} = 1.0752 - j 5.733 \text{ [KA]}$$

$$= 5.83 \angle -79.38^\circ \text{ [KA]}$$

$$\sqrt{3} p.u = \frac{10\text{kV}}{\sqrt{3} \text{kV}_{base}} = \frac{10\text{kV}}{20\text{kV}} = 0.5 \angle 0^\circ \text{ p.u} \quad \text{from above}$$

$$\sqrt{3} p.u = V_{g.p.u} = 0.5 \angle 0^\circ \text{ p.u}$$

$$S_{Line \text{ p.u.}} = (I_{p.u.})^2 (jX_{Line \text{ p.u.}})$$

$$S_{Line \text{ p.u.}} = (0.215 - j1.147)^2 (j0.00375)$$

$$S_{Line \text{ p.u.}} = 0.0018 - j0.0048 \text{ p.u}$$

$$S_{Line} = I_{actual}^2 \times jX_{Line}$$

$$S_{Line} = (1.0752 - j5.733 \text{ [kA]})^2 \times j6 \Omega$$

$$S_{Line} = 73.97 + j190.27 \text{ [MVA]}$$

$$S_{Line} = 204.14 \angle 68.76^\circ \text{ [MVA]}$$

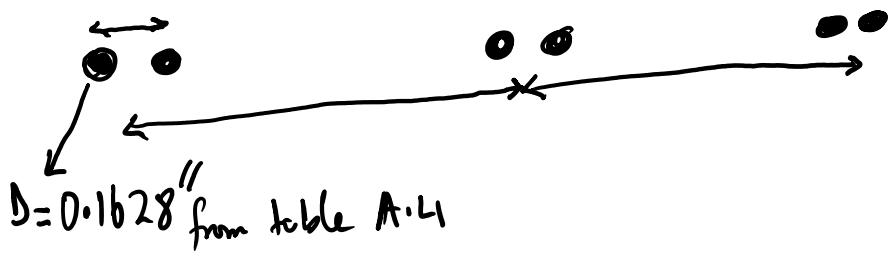
Yes S_{Line} rating exceed all the [MVA] ratings

3φ transmission line with 2 lines/bundle

$$f = 60 \text{ Hz} \quad V = 345 \text{ kV} \quad \# \text{ Strands} = 30$$

$$T = 50^\circ\text{C} \quad f = 2.7 \times 10^{-8} \text{ m}^{-m} @ 20^\circ\text{C} \quad \text{for Aluminum}$$

Phase 1 Phase 2 Phase 3



Resistance

$$R_{DC} = \frac{\rho_{50^\circ\text{C}} L}{A \times \# \text{ lines/bundle}}$$

$$\rho_{50^\circ\text{C}} = 2.7 \times 10^{-8} \text{ m}^{-m} \left(1 + 0.0039 (50^\circ\text{C} - 20^\circ\text{C}) \right)$$

$$\rho_{50^\circ\text{C}} = 3.0159 \times 10^{-8} \text{ m}^{-m}$$

$$L = 1 \text{ m}$$

$$A = \pi \left(\frac{D}{2} \right)^2 \quad \text{for Mallard } D = 0.1628 \text{ inches}$$

$$A = 30 \pi \left(\frac{(0.1628)}{2} \left(0.0254 \frac{\text{m}}{\text{inch}} \right) \right)^2$$

$$A = 4.029 \times 10^{-4} \text{ m}^2$$

$$R_{DC} = \frac{(3.0159 \times 10^{-8} \Omega \cdot \text{m}) (1 \text{ m})}{2 \times 4.029 \times 10^{-4} \text{ m}^2}$$

$$R_{DC} = 3.742 \times 10^{-5} \frac{\Omega}{\text{m}}$$

$$R_{DC/\text{km}} = (1.07) \left(3.742 \times 10^{-5} \frac{\Omega}{\text{m}} \right) \left(\frac{1000 \text{ m}}{\text{km}} \right)$$

$$R_{DC/\text{km}} = 40.04 \text{ m } [\Omega/\text{km}]$$

from Table A.4

$$ra = 0.1288 \Omega/\text{mile} \text{ @ } 50^\circ\text{C \& } 60\text{ Hz}$$

$$ra_{\text{1/2 bundle}} = \frac{0.1288 \Omega/\text{mile}}{2} \left(\frac{1}{1.609} \frac{\text{miles}}{\text{km}} \right)$$

$$= 40.02 \text{ m } [\Omega/\text{km}]$$

Line spacing $d = 2.5\text{m}$
 $f = 50\text{ Hz}$

$$1\phi \quad L = 20\text{ miles}$$

Conductor Type Finch $\Rightarrow D = 0.1436''$

$$L_a = (4 \times 10^{-7}) \ln \left(\frac{d}{0.7788 \sqrt{\left(\frac{D}{w}\right)^2}} \right) \text{ H/m}$$

$$L_a = (4 \times 10^{-7}) \ln \left(\frac{2.5\text{m}}{0.7788 \left(\frac{0.1436 \times 0.0254}{2} \right)} \right)$$

$$L_a = 2.99 \mu \text{H/m}$$

$$L_{a/20\text{miles}} = 2.99 \mu \text{H/m} \quad (20 \times 1609 \text{ m/mile})$$

$$L_{a/20\text{miles}} = 0.09619 \text{ H/mile}$$

$$L_{a/20\text{miles}} = 96.19 \text{ m[H/mile]}$$

$$X_{L_{a/20\text{miles}}} = \omega L_{a/20\text{miles}} \quad \omega = 2\pi f$$

$$X_{L_{a/20\text{miles}}} = 2\pi (50\text{ Hz}) (96.19 \text{ m H/mile})$$

$$X_{L_{a/20\text{miles}}} = 30.22 [\Omega/\text{mile}]$$

Line spacing $d = 0.41 \text{ m}$ $f = 60 \text{ Hz}$ ACRS Type Mallard
 phase spacing $D = 6 \text{ m}$ $T = 50^\circ \text{C}$

$$Z_{\text{line}} = R_{\text{Line}} + jX_{\text{Line}}$$

r_a from Table A-41 = $0.1288 \Omega/\text{mile}$ @ 50°C 60 Hz

$$R_{\text{Line}/\text{km}} = \left(0.1288 \frac{\Omega}{\text{mile}}\right) \left(\frac{1}{1.609 \frac{\text{miles}}{\text{km}}}\right)$$

$$R_{\text{Line}/\text{km}} = 0.0800 [\Omega/\text{km}]$$

$$R_{\text{Line}/\text{km}} = 80.0 \text{ m} [\Omega/\text{km}]$$

X_a from table A-41 = 0.393 m/feet

$$X_{\text{Line}/\text{km}} = \left(0.393 \frac{\Omega}{\text{feet}}\right) \left(3.048 \times 10^{-4} \frac{\text{feet}}{\text{km}}\right)$$

$$X_{\text{Line}/\text{km}} = 2.4399 \times 10^{-5} \Omega/\text{km}$$

$$X_{\text{Line}/\text{km}} = 243.99 \text{ m} [\Omega/\text{km}]$$

$$Z_{\text{Line}} = 80 + j243.99 [\text{m}\Omega/\text{km}]$$