

KROMA: Ontology Matching with Knowledge Retrieval and Large Language Models

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Abstract. Ontology Matching (OM) is a cornerstone task of semantic interoperability, yet existing systems often rely on handcrafted rules or specialized models with limited adaptability. We present KROMA, a novel OM framework that harnesses Large Language Models (LLMs) within a Retrieval-Augmented Generation (RAG) pipeline, to dynamically enrich the semantic context of OM tasks with structural, lexical, and definitional knowledge. To optimize both accuracy and efficiency, KROMA integrates a bisimilarity-based concept matching and a lightweight ontology refinement step, which prune candidate concepts and substantially reduce the communication overhead from invoking LLMs. Using a variety of benchmark datasets, we experimentally verify that knowledge retrieval and context-augmented LLMs effectively improve ontology matching outperforms both traditional OM systems and state-of-the-art LLM-based OM methods, with comparable communication overhead. Our study highlights the feasibility and benefit of the proposed optimization techniques (targeted knowledge retrieval, prompt enrichment, and ontology refinement) for ontology matching at scale. Code is available at: <https://anonymous.4open.science/r/kroma/>

Keywords: Ontology Matching · Large Language Models · Retrieval Augmented Generation

1 Introduction

Ontologies have been routinely developed to unify and standardize knowledge representation to support data-driven applications. They allow researchers to harmonize terminologies and enhance knowledge and sharing in their fields. Ontologies can be classified according to their level of specificity, ranging from more abstract, general-purpose ontologies such as Basic Formal Ontology (BFO)[38] or DOLCE[6] down to more domain-oriented ‘mid-level’ ones, such as CheBi [14] in chemistry, Industrial Ontology Foundry (IOF) [17] or Common Core Ontology (CCO) [27]. Domain ontologies are data-driven, task-specific “low-level” ontologies, containing concepts from domain-specific data, such as Materials Data Science Ontology (MDS-Onto) [46]. To achieve broad usability, ontologies need to be aligned for better interoperability via ontology matching.

Ontology matching has been studied to find correspondence between terms that are semantically equivalent [52]. It is a cornerstone task to ensure semantic interoperability among terms originated from different sources. Ontology

matching methods can be categorized to rule-based or structural-based (graph pattern or path-based) matching [10], matching with semantic similarity, machine learning-based approaches and hybrid methods. Linguistic (terminological) methods are often used for ontology matching tasks, ranging from simple string matching or embedding learning to advance counterparts based on natural language processing (NLP). Nevertheless, conventional rule- or structural-based methods are often restricted to certain use cases and hard to be generalized for new or unseen concepts. Learning-based approaches may on the other hand require high re-training process, for which abundant annotated or training data remains a luxury especially for *e.g.*, data-driven scientific research.

Meanwhile, the emerging Large Language Models (LLMs) have demonstrated remarkable versatility for NL understanding. LLMs are trained on vast and diverse corpora, endowing them with an understanding of language nuances and contextual subtleties. Extensive training enables them to capture semantic relationships and abstract patterns that are critical for aligning concepts across different data sources. A missing yet desirable opportunity is to investigate whether and how LLMs can be engaged to automate and improve ontology matching.

This paper introduces KROMA, a novel framework that exploits LLMs to enhance ontology matching. Unlike existing LLM-based methods that typically “outsource” ontology matching to LLMs with direct prompting (which may have low confidence and risk of hallucination), KROMA maintain a set of conceptually similar groups that are co-determined by concept similarity and LLMs, both guided by their “context” obtained via a runtime knowledge retrieval process. Moreover, the groups are further refined by a global ontological equivalence relation that incorporate structural equivalence.

Contributions. Our main contributions are summarized below.

- (1) We propose a formulation of semantic equivalence relation in terms of a class of bisimilar equivalence relation, and formally define the ontology structure, called concept graph, to be maintained (**Sections 2 and 3**). We justify our formulation by showing the existence of an “optimal” concept graph with minimality and uniqueness guarantee, subject to the bisimilar equivalence.
- (2) We introduce KROMA, an LLM-enhanced ontology matching framework (**Section 4**). KROMA fine-tunes LLMs with prompts over enriched semantic contexts. Such contexts are obtained from knowledge retrieval, referencing high-quality, external knowledge resources.
- (3) KROMA supports both offline and online matching, to “cold-start” from scratch, and to digest terms arriving from a stream of data, respectively. We introduce efficient algorithms to correctly construct and maintain the optimal concept graphs (**Section 5**). (a) The offline refinement performs a fast grouping process guided by the bisimilar equivalence, blending concept equivalence tests co-determined by semantic closeness and LLMs. (b) The online algorithm effectively incrementalizes its offline counterpart with fast delay time for continuous concept streams. Both algorithms are in low polynomial time, with optimality guarantee on the computed concept graphs.

(4) Using benchmarking ontologies and knowledge graphs, we experimentally verify the effectiveness and efficiency of KROMA (**Section 6**). We found that KROMA outperforms existing LLM-based methods by 10.95% on average, and the optimization of knowledge retrieval and refinement improves its accuracy by 6.65% and 2.68%, respectively.

Related Work. We summarize related work below.

Large Language Models. Large language models (LLMs) have advanced NLP by enabling parallel processing and capturing complex dependencies [53,48], which have scaled from GPT-1’s 117M [44], GPT-2’s 1.5B [45] to GPT-3’s 175B [35] and GPT-4’s 1.8T parameters [36]. Open-source models like Llama have grown to 405B [32], with Mistral Large (123B) [33] and DeepSeek V3 (671B) [12] also emerging. Recent advances in specialized reasoning LLMs (RLLMs) such as OpenAI’s O1 and DeepSeek R1 have further propelled Long Chain-of-Thought reasoning—shifting from brief, linear Short CoT to deeper, iterative exploration, and yielded substantial gains in multidisciplinary tasks [37,13,47,50,8,42,56,30].

Ontology Matching with LLMs. Several methods have been developed to exploit LLMs for ontology matching. Early work focused on direct prompting LLMs for ontology matching. For example, [39] frame product matching as a yes/no query, and [34] feed entire source and target ontologies into ChatGPT—both achieving high recall on small OAEI conference-track tasks but suffering from low precision. Beyond these “direct-prompt” approaches, state-of-the-art LLM-OM systems fall into two main categories: (1) retrieval-augmented pipelines, which first retrieve top- k candidates via embedding-based methods and then refine them with LLM prompts (e.g. LLM4OM leverages TF-IDF and SBERT retrievers across concept, concept-parent, and concept-children representations [20], while MILA adds a prioritized depth-first search step to confirm high-confidence matches before any LLM invocation [49]); and (2) prompt-engineering systems, which generate candidates via a high-precision matcher or inverted index and then apply targeted prompt templates to LLMs in a single step (e.g. OLaLa embeds SBERT candidates into MELT’s prompting framework with both independent and multi-choice formulations [25], and LLMMap uses binary yes/no prompts over concept labels plus structural context with Flan-T5-XXL or GPT-3.5 [23]).

2 Ontologies and Ontology Matching

Ontologies. An ontology O is a pair (C, E) , where C is a finite set of concept names, and $E \subset C \times C$ is a set of relations. An ontology has a graph representation with a set of concept nodes C , and a set of edges E . We consider ontologies as directed acyclic graphs (DAGs).

In addition, each concept node (or simply “node”) c in O carries the following auxiliary structure. (1) The *rank* of a node $c \in C$ is defined as: (a) $r(c) = 0$ if c has no child, otherwise, (b) $r(c) = \max(r(c') + 1)$ for any child c' of c in O . (2) A *ground set* $c.\mathcal{I}$, refers to a set of entities from *e.g.*, external ontologies or knowledge bases that can be validated to belong to the concept c .

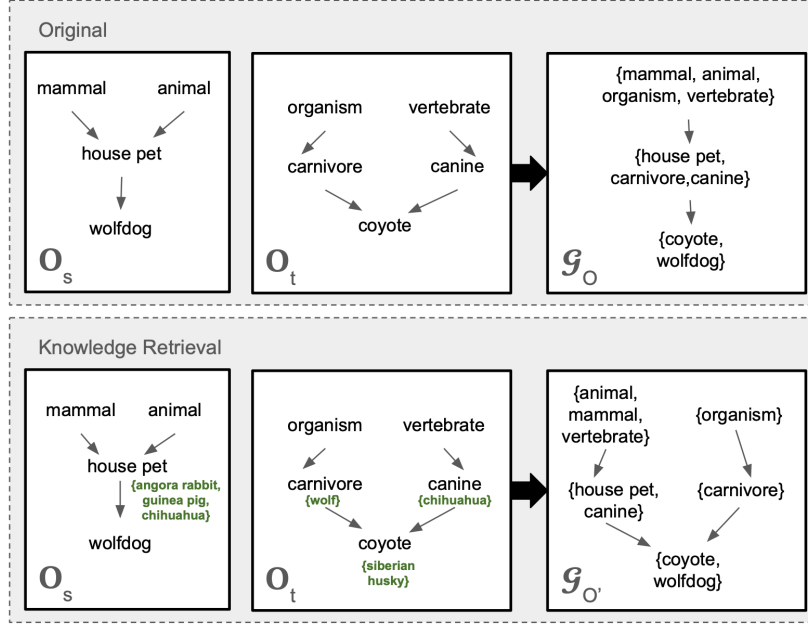


Fig. 1: Ontologies with ground sets, Ontology Matching and Concept Graphs

Ontology Matching. Given a source ontology $O_s = (C_s, E_s)$ and a target ontology $O_t = (C_t, E_t)$, an *ontological equivalence relation* $R_{\sim} \subseteq C_s \times C_t$ is an equivalence relation that contains pairs of nodes (c, c') that are considered to be “semantically equivalent”. The relation R_{\sim} induces an equivalence partition \mathcal{C} of the concept set $C_s \cup C_t$, such that each partition is an equivalence class that contains a set of pairwise equivalent concepts in $C_s \cup C_t$.

Consistently, we define a *concept graph* $\mathcal{G}_O = (V_O, E_O)$ as a DAG with a set of nodes V_O , where each node $[c] \in V_O$ is an equivalence class in \mathcal{C} , and there exists an edge $([c], [c']) \in E_O$ if and only if there exists an edge (c, c') in E_s or in E_t . A concept graph \mathcal{G}_O can be a multigraph: there may exist multiple edges of different relation names between two equivalent classes.

Given O_s and O_t , the task of ontology matching is to properly formulate R_{\sim} and compute \mathcal{C} induced by R_{\sim} over O_s and O_t ; or equivalently, compute the concept graph \mathcal{G}_O induced by R_{\sim} .

Example 1. Figure 1 depicts two ontologies O_s and O_t as DAGs, involving in total 9 concept nodes. An equivalence relation may suggest that “mammal”, “animal”, “organism” and “vertebrate” are pairwise similar; and similarly for the sets {“house pet”, “carnivora” and “canine”}, and {“wolfdog”, “coyote”}. This induces a concept graph \mathcal{G}_o as shown on the top right as a result of ontology matching, with three equivalence classes.

Language Models for Ontology Matching. A language model M takes as input a prompt query q , and generate an answer $q(M)$, typically an NL statement, for downstream processing. Large language models (LLMs) are foundation

models that can effectively learn from a handful of in-context examples, included in a prompt query q , that demonstrate input–output distribution [54].

Prompt query. A prompt query q is in a form of NL statements that specifies (1) a task definition \mathcal{T} with input and output statement; (2) a set of in-context examples \mathcal{D} with annotated data; (3) a statement of query context Q , which describe auxiliary query semantics; and optionally (4) specification on output format, and (5) a self-evaluation of answer quality such as confidence. An evaluation of a prompt query q invokes an LLM M to infer a query result $q(M)$.

We specify a prompt query q and LLMs for ontology matching. A prompt query q is in the form of $q(c, c')$, which asks “are c and c' semantically equivalent?” An LLM M can be queried by $q(c, c')$ and acts as a Boolean “oracle” with “yes/no” answer. An LLM is *deterministic*, if it always generate a same answer for the same prompt query. We consider deterministic LLMs, as in practice, such LLMs are desired for consistent and robust performance.

3 Ontology Matching with LLMs

In this section, we provide a pragmatic characterization for the ontological equivalence relation R_{\simeq} . We then formulate the ontology matching problem.

3.1 Semantic Equivalence: A Characterization

Concept similarity. A variety of methods have been proposed to decide if two *concepts* are equivalent [7]. KROMA by default uses a Boolean function F defined by a weighted combination of a semantic closeness metric sim^1 and the result from a set of LLMs \mathcal{M} (see Section 4).

$$F(c, c') = \gamma \text{sim}(c, c') + (1 - \gamma) q(c, c', \mathcal{M})$$

where q is a prompt query that specifies the context of concept equivalence for LLMs. KROMA supports a built-in library of semantic similarity functions sim , including (a) string similarity, feature and information measure [40], or normalized distances (NGDs) [28]; and (b) a variety of LLMs such as GPT-4o Mini (OpenAI) [36], LLaMA-3.3 (Meta AI) [31], and Qwen-2.5 (Qwen Team) [43].

Ontological Bisimilarity. We next provide a specification of the ontological equivalence relation, notably, *ontological bisimilarity*, denoted by the same symbol R_{\simeq} for simplicity. Given a source ontology $O_s = (C_s, E_s)$, and a target ontology $O_t = (C_t, E_t)$, we say a pair of nodes $c_s \in C_s$ and $c_t \in C_t$ are *ontologically bisimilar*, denoted as $(c_s, c_t) \in R_{\simeq}$, if and only if there exists a non-empty binary relation R_{\simeq} , such that: (1) c_s and c_t are concept similar, *i.e.*, $F(c_s, c_t) \geq \alpha$, for a threshold α ; (2) for every edge $(c'_s, c_s) \in E_s$, there exists an edge $(c'_t, c_t) \in E_t$, such that $(c'_s, c'_t) \in R_{\simeq}$, and vice versa; and (3) for every edge $(c_s, c''_s) \in E_s$, there exists an edge $(c_t, c''_t) \in E_t$, such that $(c''_s, c''_t) \in R_{\simeq}$.

One can verify the following result.

¹ We adopt similarity metrics that satisfy transitivity, *i.e.*, if concept c is similar to c' , and c' is similar to c'' , then c is similar to c'' . This is to ensure transitivity of ontology equivalence, and is practical for representative concept similarity measures.

Lemma 1. *The ontological bisimilar relation R_{\sim} is an equivalence relation.*

We can prove the above results by verifying that R_{\sim} is reflexive, symmetric and transitive over the concept set $C_s \cup C_t$, ensured by the transitivity of concept similarity and by definition. Observe that two nodes that are concept similar may *not* be ontologically bisimilar. On the other hand, two ontologically bisimilar entities must be concept similar, by definition.

3.2 Problem Statement

We now formulate our ontological matching problem. Given a *configuration* $W = (O_s, O_t, F, \mathcal{M}, \alpha)$ that specifies as input a source ontology O_s , a target ontology O_t , a Boolean function F and threshold $\alpha \in (0, 1]$ that asserts concept similarity, and a set of LLMs \mathcal{M} , the problem is to compute a smallest concept graph \mathcal{G}_O induced by the ontologically bisimilar equivalence R_{\sim} .

We justify the above characterization by proving that there exists an “optimal”, invariant solution encoded by a concept graph \mathcal{G}_O . To see this, we provide a *minimality* and *uniqueness* guarantee on \mathcal{G}_O .

Lemma 2. *Given a configuration W and semantic equivalence specified by the ontological bisimilar relation R_{\sim} , there is a unique smallest concept graph \mathcal{G}_O that capture all semantically equivalent nodes in terms of R_{\sim} .*

Proof sketch: We show that the above result holds by verifying the following. (1) There is a unique, maximum ontological bisimilar relation R_{\sim} for a given configuration $W = (O_s, O_t, F, \mathcal{M})$, where any LLM in \mathcal{M} is a deterministic model for the same prompt query q generated consistently from W . This readily follows from Lemma 1, which verifies that R_{\sim} is an equivalence relation. (2) Let the union of O_s and O_t be a graph $O_{st} = \{C_s \cup C_t, E_s \cup E_t\}$. By setting \mathcal{G}_O as the quotient graph induced by the largest ontological bisimilar relation R_{\sim} over O_{st} , \mathcal{G}_O contains the smallest number of equivalent classes (nodes) and edges. This can be verified by proof by contradiction. (3) The uniqueness of the solution can be verified by showing that R_{\sim} induces only one unique partition \mathcal{C} and results in a concept graph \mathcal{G}_O up to graph isomorphism. In other words, for any two possible concept graphs induced by R_{\sim} , they are isomorphic to each other. \square

The above analysis suggests that for a configuration W , it is desirable to compute such an optimal concept graph as an invariant, stable result with guarantees on sizes and uniqueness on topological structures. We next introduce KROMA and efficient algorithms to compute such optimal concept graphs.

4 KROMA Framework

4.1 Framework Overview

Given a *configuration* $W = (O_s, O_t, F, \mathcal{M})$ where \mathcal{M} is a set of pre-trained LLMs \mathcal{M} , KROMA has the following major functional modules that enables a multi-session ontology matching process.

Concept Graph Initialization Upon receiving two ontologies $O_s = (C_s, E_s)$ and $O_t = (C_t, E_t)$, KROMA initializes the concept graph $\mathcal{G}_O = (V, E)$ with $V =$

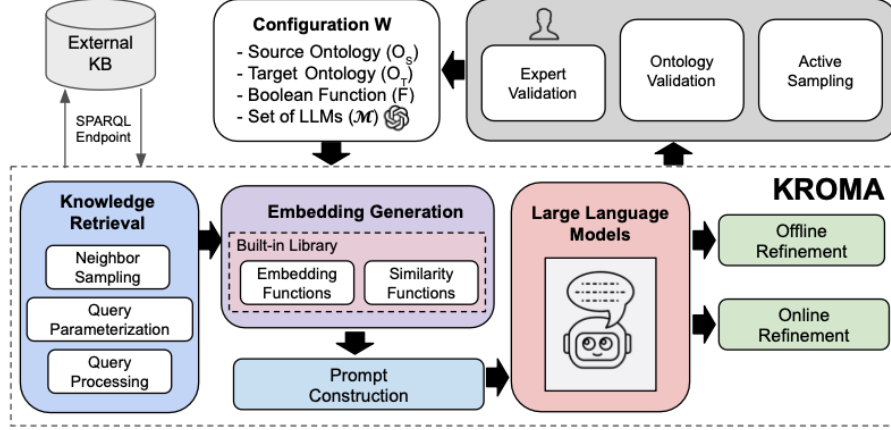


Fig. 2: KROMA Framework Overview: Major Components and Dataflow

$C_S \cup C_T$ and $E = E_S \cup E_T$. For each concept $c \in V$, KROMA computes the *rank* $r(c)$ as described in Section 2.

Knowledge Retrieval. To assemble a rich, yet compact, context for each concept $c \in V$, we perform: (1) *Neighborhood Sampling*: traverse up to its two hops in \mathcal{G}_O to collect parents, children, and “sibling” concepts of c , creating a node induced subgraph centered at c ; (2) *subgraph parameterization*: Sample and substitute constant values from the subgraph with variables to create SPARQL queries S_q ; and (3) *ground set curation*: process S_q onto external knowledge bases to augment its ground set $c.\mathcal{I}$ with auxiliary information (e.g., relevant entities, definition, labels, etc.).

Embedding Generation. In this phase, KROMA consults a built-in library of semantic similarity functions $\text{sim}(\cdot, \cdot)$ and embedding functions $\text{embd}(\cdot)$. For each concept $c \in V$, KROMA computes:

$$z_c = \alpha \text{embd}_{\text{graph}}(c) + (1 - \alpha) \text{embd}_{\text{text}},$$

where $\text{embd}_{\text{graph}}$ (e.g. node2vec [22]) captures the c ’s topology information and $\text{embd}_{\text{text}}$ (e.g. SciBERT [5]) encodes c ’s textual context. After obtaining the necessary embeddings ($z_c \forall c \in V$), KROMA computes pairwise concept similarity between source and target ontologies using sim functions:

$$\mathbb{S} = \{(c_s, c_t, \text{score}_{s,t}) \mid c_s \in C_S, c_t \in C_T, \text{score}_{s,t} = \text{sim}(z_{c_s}, z_{c_t})\}$$

From \mathbb{S} , we select the top- k pairs with the highest similarity scores (i.e. in descending order of $\text{score}_{s,t}$), yielding the candidate list \mathbb{C} .

Example 2. We revisit Example 1. (1) A knowledge retrieval for node “house pet” samples its neighbors and issues a set of “star-shaped” SPARQL queries centered at “house pet” to query an underlying knowledge graph \mathcal{KG} . This enriches its ground set with a majority of herbivore or omnivorous pets that are not “carnivore”. Similarly, the ground set of “carnivore” is enriched by “wolf”, unlikely a

Task Description Given two concepts: source and target . Determine if they are semantically equivalent or not.	Task Description Given two ontology concepts: heatwave and drought . Determine if they are semantically equivalent or not.
Examples <ul style="list-style-type: none"> • Example 1: source1 (+ metadata) is semantically equivalent to target1 (+ metadata) • Example 2: source2 (+ metadata) is not semantically equivalent to target2 (+ metadata) • 3 more examples ... 	Examples <ul style="list-style-type: none"> • Example 1: urban flooding (parents = [hydrological hazard], ...) is semantically equivalent to city flood (parents = [flood event], ...) • Example 2: soil erosion (parents = [land degradation], ...) is not semantically equivalent to landslide (parents = [mass wasting], ...) • 3 more examples ...
Query Context <ul style="list-style-type: none"> • Source context: source (parents = [...], children = [...], synonyms=[...], definition = "...") • Target context: target (parent=[...], children = [...], synonyms=[...], definition = "...") 	Query Context <ul style="list-style-type: none"> • Source context: heatwave (parents = [extreme weather], children = [public health emergency], synonyms=[extreme heat], definition = "...") • Target context: drought (parent=[climatic anomaly], children = [crop failure], synonyms=[prolonged dryness], definition = "...")
Output Format <ans> Yes/No </ans>	Output Format <ans> Yes/No </ans>
Confidence <conf> 0-10 </conf>	Confidence <conf> 0-10 </conf>

Fig. 3: KROMA Prompt Query Template and Query Example

house pet. Despite “coyote” and “wolfdog” (house pet) alone are less similar, the ground set of “coyote” turns out to be a set of canine pets *e.g.*, “husky” that are “coyote-like”, hence similar with “wolfdog”. (2) The embedding generation phase incorporates enriched ground sets and generate embeddings accordingly, which scores that distinguishes “house pet” from “carnivore” due to embedding difference, and assert “coyote” and “wolfdog” to be concept similar, hence a candidate pair to be “double checked” by LLMs in the next phase.

Prompt Querying LLMs. For each candidate pair $(c_s, c_t) \in \mathbb{C}$, KROMA automatically generates an NL prompt that includes: (1) Task description \mathcal{T} (e.g. “*Given two ontology concepts and their contextual metadata, decide if they are related or not.*”), (2) In-context examples \mathcal{D} containing both positive and negative matches, (3) Query context for c_s and c_t including their ground sets, (4) Output format and confidence (e.g., “Answer Yes or No, and provide a confidence score between 0 and 10.”). It then calls (a set of) LLMs \mathcal{M} to obtain a match decision with confidence. Low-confidence or conflicting outputs are routed to validation module. A query template and a generated example is illustrated in Figure 3.

Ontology Refinement & Expert Validation. KROMA next invokes a refinement process, OfflineRefine (Algorithm 1), to “cold-start” the construction of \mathcal{G}_O , or OnlineRefine (Algorithm 2), to incrementally refine \mathcal{G}_O for any unseen, newly arrived concept nodes or edges. Any pair of nodes whose structural ranks remain in “conflict” is routed into a set of queries for expert validation (see Algorithm 2, Section 4); once approved, are integrated back into \mathcal{G}_O . An active sampling strategy is applied, to select pairs of nodes that have low confidence from LLMs for expert validation, to reduce the manual effort.

Algorithm 1: Offline Refinement

Input: Source ontology $O_S = (C_S, E_S)$, target ontology $O_T = (C_T, E_T)$
Output: Concept graph \mathcal{G}_O .

```

1 set  $V \leftarrow C_S \cup C_T$ ; set  $E \leftarrow E_S \cup E_T$ ;
2 Initialize concept graph  $\mathcal{G}_O = (V, E)$ ;
3 foreach  $c \in V$  do
4    $\lfloor$  compute rank  $r(c)$  as in Section 2;
5  $\rho \leftarrow \max_{c \in V} r(c)$ ;
6 for  $i \leftarrow 0$  to  $\rho$  do
7    $B_i \leftarrow \{c : r(c) = i\}$ ;
8  $P \leftarrow \{B_0, \dots, B_\rho\}$ ;
9 for  $i \leftarrow 0$  to  $\rho$  do
10   $D_i \leftarrow \{X \in P : X \subseteq B_i\}$ ;
11  foreach  $X \in D_i$  do
12     $\lfloor G \leftarrow \text{collapse}(G, X)$ ;
13  foreach  $c \in B_i$  do
14    foreach  $C \in P$  with  $C \subseteq \bigcup_{j>i} B_j$  do
15      Split  $C$  into  $C_1, C_2$  by adjacency to  $c$ ;
16       $P \leftarrow (P \setminus \{C\}) \cup \{C_1, C_2\}$ ;
17 return  $\mathcal{G}_O$ ;
```

Example 3. Continuing with Example 2, as “golden retriever” and “coyote” are asserted by the function F that combines the descision of semantic similarity function sim and LLMs, an equivalence class is created in \mathcal{G}'_O . As “house pet” and “carnivore” has quite different embedding considering the features from themselves and their ground sets, “carnivore” is separated from the group of “house pet”. This suggests further that “organism” now has a different context that distinguish it from the group $\{\text{mammal}, \text{animal}, \text{vertebrate}\}$, by the definition of bisimilarity equivalence. This leads to a finer-grained concept graph \mathcal{G}'_O .

5 Ontology Refinement

We next describe our ontology refinement algorithms. KROMA supports ontology refinement in two modes. The offline mode assumes that the source ontology O_s and the target ontology O_t are known, and performs a batch processing to compute the concept graph \mathcal{G}_O from scratch. The online refinement incrementally maintains \mathcal{G}_O upon a sequence of (unseen) triples (edges) from external resources.

The offline refinement algorithm is outlined as Algorithm 1. (1) It starts by initializing \mathcal{G}_O (lines 1-6) as the union of O_s and O_t , followed by computing the node ranks. At each rank, it initializes a “bucket” B_i (as a single node set) that simply include all the concept nodes at rank i (lines 7-8), and initialize a partition \mathcal{P} with all the buckets (line 9). It then follows a “bottom-up” process to refine the buckets iteratively, by checking if two concepts c and c' in a same bucket B_i are concept similar (as asserted by LLM and embedding similarity), and have all the neighbors that satisfy the requirement of ontological bisimilar relation by definition (lines 10-13). If not, a procedure `collapse` is invoked, to (1) split

the bucket B_i into three fragments: $B_i^1 = B_i \setminus \{c, c'\}$, $B_i^2 = \{c\}$, and $B_i^3 = \{c'\}$, followed by a “merge” check to test if c and c' can be merged to B_i^1 ; and (2) propagate this change to further “split-merge” operators to affected buckets at higher ranks (lines 14-17). This process continues until no change can be made.

Correctness. Algorithm 1 correctly terminates at obtaining a maximum bisimilar ontological equivalence relation R_{\sim} , with two variants. (1) As ontologies are DAGs, it suffices to perform a one-pass, bottom-up splitting of equivalence classes following the topological ranks; (2) the `collapse` operator ensures the “mergable” cases to reduce unnecessary buckets whenever a new bucket is separated. This process simulates the correct computation of maximum bisimulation relation in Kripke structures (a DAG) [15], optimized for deriving ontology matching determined by LLM-based concept similarity and bisimilar equivalence.

Time Cost. The initialization of concept graph \mathcal{G}_O is in $O(|O_s| + |O_t|)$. Here $|O_s| = |V_s| + |E_s|$; and $|O_t|$ is defined similarly. The iterative collapse (lines 10-17) takes in $O(|O_s| + |O_t|)$ time as the number of buckets (resp. edges) is at most $|C_s| + |C_T|$ (resp. $|E_s| + |E_t|$). The overall cost is in $O(|O_s| + |O_t|)$.

Overall Cost. We consider the cost of the entire workflow of KROMA. (1) The knowledge checking takes $O((|C_s| + |C_T|)|KG|)$ time, where $|KG|$ refers to the size of the external ontology or knowledge graph that is referred to by the knowledge retrieval via *e.g.*, SPARQL access. Note here we consider SPARQL queries with “star” patterns, hence the cost of query processing (to curate ground sets) is in quadratic time. (2) The total cost of LLM inference is in $O(|C_s||C_T|T_I)$, for a worst case that any pair of nodes in $C_s \times C_t$ are concept similar in terms of \sim . Here T_I is the unit cost of processing a prompt query. Putting these together, the total cost is in $O(|C_s||C_T|T_I + (|C_s| + |C_T|)|KG| + (|O_s| + |O_t|))$ time.

Online Refinement. We next outline the online matching process. In this setting, KROMA receives new ontology components as an (infinite) sequence of triples (edges), and incrementally maintain a concept graph \mathcal{G}_O by processing the sequence input in small batched updates $\Delta\mathcal{G}$. For each newly arrived concept (node) c in $\Delta\mathcal{G}$, KROMA conducts knowledge retrieval to curate $c.\mathcal{I}$; and consult LLMs to decide if c is concept similar to any node in \mathcal{G}_O . It then invokes online refinement algorithm to enforce the ontological bisimilar equivalence.

The algorithm (with pseudoscope reported in [1]) first updates the buckets in \mathcal{G}_O by incorporating the nodes from $\Delta\mathcal{G}$ that are verified to be concept similar, as well as their ranks. It then incrementally update the buckets to maintain the bisimilar equivalence consistently via a “bottom-up” split-merge process as in Algorithm 1 (lines 6-15). Due to the unpredictability of the “unseen” concepts, the online refinement defers the processing of two “inconsistent” cases for experts’ validation: (1) When a concept c is determined to be concept similar by function \sim but not LLMs with high confidence; or (2) whenever for a new edge $(c, c') \in \Delta\mathcal{G}$, $(c, [c_1]) \in R_{\sim}$, $(c', [c_2]) \in R_{\sim}$, yet $r(c_1) < r(c_2)$ in \mathcal{G}_O . Both require domain experts’ feedback to resolve. These cases are cached into a query set \mathcal{Q} to be further resolved in the validation phase (see Section 4).

Analysis. The correctness of online refinement carries over from its offline counterpart, and that it correctly incrementalize the split-merge operator for each newly arrived edges. For time cost, for each batch, it takes a delay time to update \mathcal{G}_O in $O(|\mathcal{G}_O| + |\Delta G| \log |\Delta G| + |\Delta G| \log |V_O|)$ time. This result verifies that online refinement is able to response faster than offline maintenance that recomputes the concept graph from scratch. We present the detaled analysis in [1].

6 Experimental Study

We investigated the following research questions. [RQ1]: *How well KROMA improves state-of-the-art baselines with different LLMs?* [RQ2]: *How can knowledge retrieval and ontology refinement enhance matching accuracy?* and [RQ3]: *What are the impact of alternative LLM reasoning strategies?*

6.1 Experimental Setting

Benchmark Datasets. We selected five tracks from the OAEI campaign [41], covering various domain tracks. For each track, we selected two representative ontologies as a source ontology O_s and a target ontology O_t . The selected tracks include Anatomy [16] (Mouse-Human), Bio-LLM [24] (NCIT-DOID), CommonKG (CKG) [19] (Nell-DBpedia, YAGO-Wikidata), BioDiv [29] (ENVO-SWEET), and MSE [26] (MI-MatOnto).

LLMs selection. To underscore KROMA’s ability to achieve strong matching performance even with smaller or lower-accuracy LLMs, we selected models with relatively modest Chatbot Arena MMLU scores [9]: Gemma-2B (51.3%) and Llama-3.2-3B (63.4%), compared to the baseline systems Flan-T5-XXL (55.1%) and MPT- 7B (60.1%). We have selected a diverse set of LLMs, ranging from ultra-lightweight to large-scale—to demonstrate KROMA’s compatibility with models that can be deployed on modest hardware without sacrificing matching quality. Our core evaluations use DeepSeek-R1-Distill-Qwen-1.5B [51] (1.5B), GPT-4o-mini [36] (8B), and Llama-3.3 [31] (70B), each chosen in a variant smaller than those employed by prior OM-LLM baselines. To further benchmark our framework, we include Gemma-2B [11] (2B), Llama-3.2-3B [3] (3B), Mistral-7B [4] (7B), and Llama-2-7B [2] (7B) in our ablation studies.

Confidence Calibration. Our selection of LLMs is justified by a calibration test with their confidence over ground truth answers. The self-evaluated confidence by LLMs align well with accuracy: over 80% of correct matches fall in the top confidence bins (9–10), while fewer than 5% of errors are reported. Gemma-2B shows almost no errors above confidence 8, and both Llama-3.2-3B and Llama-3.3-70B maintain $\geq 95\%$ precision at confidence thresholds of 9 or greater. We thus choose a confidence threshold to be 8.5 for all LLMs to accept their output.

Test sets generation. Following [23,21], for each dataset, we randomly sample 20 matched concept pairs from the ground truth mappings. For each source ontology concept, we select an additional 24 unmatched target ontology concepts based on their cosine similarity scores, thereby creating a total of 25 candidate mappings (including the ground truth mapping). Finally, we randomly choose 20

source concepts that lack a corresponding target concept in the ground truth and generate 25 candidate mappings for each. Each subset consists of 20 source ontology concepts with a match and 20 without matches, with each concept paired with 25 candidate mappings, totaling 1000 concept pairs per configuration.

Concepts and entities not selected as test sets are treated as external knowledge base for **knowledge retrieval**. All models operate with SciBERT [5] for **Embedding Generation**, leveraging its strength in scientific data embedding.

Baselines. Our evaluation considers **four** state-of-the-art LLM-based ontology matching methods: LLM4OM [20], MILA [49], OLaLa [25], and LLMMap [23]. For RQ2, we also developed KROMA-NR, which skip knowledge retrieval, and KROMA-NB, which disables the bisimilarity-based clustering (hence clusters are determined by concept similarity alone).

Naming Convention. Each configuration uses a pattern [Method] [Optional Suffix] [LLM Version], where the initials (K, M, O, L) specify the method (KROMA, MILA, OLaLa, LLM4OM). Suffixes “NKR” and “NR” denote “no knowledge retrieval” and “no ontology refinement”, respectively, and the trailing version number (e.g., 3.3, 2.0, 4mini) specifies the underlying LLM release.

6.2 Experimental Results

Exp-1: Effectiveness (RQ1). In this set of tests, we evaluate the accuracy of KROMA compared with baselines, and the impact of factors such as test sizes.

Table 1: KROMA Performance vs. Baselines.

Model	MH	ND	NDB	YW	ES	MM
KL3.3	94.94	98.63	97.08	95.54	—	61.25
KNR3.3	91.25	95.01	94.26	91.98	—	59.95
KNB3.3	86.59	90.91	93.58	89.74	—	55.00
KL3.1	94.50	98.24	—	—	91.43	—
KL2.0	93.24	—	96.02	—	85.06	—
KG2	—	85.53	—	—	—	—
KM7	—	—	—	—	92.98	—
ML3.1	92.20	94.80	—	—	83.70	32.97
OL2.0	90.20	—	96.00	—	51.10	—
L4G3.5	89.11	83.01	94.26	—	—	—
K4mini	—	—	—	—	93.18	—
KNR4mini	—	—	—	—	92.12	—
KNB4mini	—	—	—	—	84.89	—
LLFT	—	72.10	—	—	—	—
L4L2	—	—	—	92.19	—	—
L4M7	—	—	—	—	55.09	—
L4MPT	—	—	—	—	—	32.97

KROMA vs. Baselines: Overall Accuracy. Across all six datasets in Table 1 (abbreviated by their first capitalized letters), the full KROMA configuration (KL3.3) achieves the highest F_1 on every task, substantially outperforming competing baselines. For Mouse–Human, KL3.3 delivers 94.94 F_1 , eclipsing MILA’s best (ML3.1) at 92.20, OLaLa (OL2.0) at 90.20, and LLM4OM (L4G3.5) at 89.11. On NCIT–DOID, KL3.3 reaches 98.63 versus 94.80 for MILA, 83.01 for LLM4OM, and 72.10 for Flan-T5-XXL. Similar gaps appear on Nell–DBpedia (97.08 vs.

96.00/94.26), YAGO–Wikidata (95.54 vs. 92.19/93.33), ENVO–SWEET (93.18 vs. 92.98/85.06), and MI–MatOnto (61.25 vs. 59.05/32.97). These verify the effectiveness of KROMA over representative benchmark datasets. More details (*e.g.*, Precision and Recall) are reported in [1].

Impact of different LLMs. Across six ontology-matching tracks, KROMA equipped with Qwen2.5-1.5B outperforms the best existing baseline on five out of the six datasets (see Table 2). In the Anatomy’s Mouse–Human track, Qwen2.5-1.5B achieves $F_1 = 83.58$ (versus 92.20 for the OM-LLM baseline), while GPT-4o-mini reaches $F_1 = 91.96$. On NCIT–DOID both models surpass the baseline with F_1 of 97.44 and 97.56 (baseline: 94.80), and similar gains appear on Nell–DBpedia (95.02, 95.67 vs. 96.00), YAGO–Wikidata (95.45, 95.44 vs. 92.19), and MI–MatOnto (61.25, 60.88 vs. 32.97). Only on ENVO–SWEET does the smallest model dip below the baseline (79.80 vs. 83.70), whereas GPT-4o-mini (93.18) and Llama-3.3-70B (91.95) still lead. These results confirm that KROMA with knowledge retrieval and ontology refinement can well exploit even relatively “smaller” LLMs with desirable accuracy, and further benefit from larger LLMs.

Table 2: KROMA Performance with different LLMs.

Dataset	Qwen2.5	GPT-4o-mini	Llama-3.3
Mouse–Human	83.6	92.0	94.9
NCIT–DOID	97.4	97.6	98.6
Nell–DBpedia	95.0	95.7	97.1
YAGO–Wikidata	95.5	95.4	95.5
ENVO–SWEET	79.8	93.2	92.0
MI–MatOnto	61.3	60.9	62.2

Impact of Test sizes. We next report the impact of ontology sizes to the performance of KROMA in accuracy (detailed results reported in [1]). For each dataset, we varied test sizes from 200 (xsmall) to 1,000 (full) pairs. KROMA’s accuracy is in general insensitive to the change of test sizes. For example, its F_1 stays within a 1.90 variance on NCIT–DOID and a 1.10-point range on YAGO–Wikidata. This verifies the robustness of KROMA in maintaining desirable accuracy for large-scale ontology matching tasks.

Exp-2: Ablation Analysis (RQ2). In this test, we perform ablation analysis, comparing KROMA with its two variants, KROMA-NKR and KROMA-NR, removing knowledge retrieval and ontology refinement, respectively.

Impact of Ontology Refinement. Table 3 (Left) shows that by incorporating Ontology Refinement (KROMA vs. KROMA-NR), KROMA improves F_1 score across 6 datasets: Mouse–Human (+3.69), NCIT–DOID (+3.62), Nell–DBpedia (+2.82), YAGO–Wikidata (+3.56), ENVO–SWEET (+1.06), MI–MatOnto (+1.30). By pruning false candidate pairs via offline and online refinement strategies on the concept graph, ontology refinement retains true semantic connections, by filtering out noise while preserving true alignments.

Impact of Knowledge Retrieval. Table 3 (Right) shows that ablating Knowledge Retrieval (KROMA-KNR vs. KROMA) results in significant F_1 drop across all six

Table 3: KROMA Performance with/without Ontology Refinement (Left); and with/without Knowledge Retrieval (Right).

Dataset	Model	P	R	F ₁	Dataset	Model	P	R	F ₁
Mouse-Human	KL3.3	90.78	99.50	94.94	Mouse-Human	KL3.3	90.78	99.50	94.94
	KNR3.3	92.34	90.16	91.25		KNKR3.3	100.00	76.36	86.59
NCIT-DOID	KL3.3	97.59	99.69	98.63	NCIT-DOID	KL3.3	97.59	99.69	98.63
	KNR3.3	93.20	96.90	95.01		KNKR3.3	83.33	100.00	90.91
Nell-DBpedia	KL3.3	94.32	100.00	97.08	Nell-DBpedia	KL3.3	94.32	100.00	97.08
	KNR3.3	97.46	91.27	94.26		KNKR3.3	91.17	96.12	93.58
YAGO-Wikidata	KL3.3	91.80	99.60	95.54	YAGO-Wikidata	KL3.3	91.80	99.60	95.54
	KNR3.3	93.50	90.50	91.98		KNKR3.3	90.50	89.00	89.74
ENVO-SWEET	K4mini	87.23	100.00	93.18	ENVO-SWEET	K4mini	87.23	100.00	93.18
	KNR4mini	86.90	98.00	92.12		KNKR4mini	82.00	88.00	84.89
MI-MatOnto	KL3.3	45.74	92.69	61.25	MI-MatOnto	KL3.3	45.74	92.69	61.25
	KNR3.3	44.80	91.40	59.95		KNKR3.3	42.00	85.00	55.00

benchmark datasets: Mouse-Human (-8.35), NCIT-DOID (-7.72), Nell-DBpedia (-3.50), YAGO-Wikidata (-5.80), ENVO-SWEET (-8.29), MI-MatOnto (-6.25). By enriching concepts with external, useful semantic context that are overlooked by other baselines, knowledge retrieval helps improving the accuracy.

We have also evaluated the efficiency of KROMA in terms of communication cost and performance gain from online processing. We found that KROMA is feasible for large-scale ontology matching, and the online refinement response fast to continuous matching tasks. Due to limited space, we report details in [1].

Exp-4: Alternative LLM Reasoning Strategies. We evaluate KROMA’s performance with two alternative LLM reasoning strategies: “Debating” and “Deep reasoning” to understand their impact to ontology matching.

Table 4: KROMA Performance with/without “Debating” (Left); and with/without “Deep reasoning” (Right).

Dataset	Model	P	R	F ₁	Dataset	Model	P	R	F ₁
Mouse-Human	D2A3R	100	70	82.35	NCIT-DOID	L3.3Short	97.59	99.69	98.63
	D2A5R	100	74	85.06		L3.3Long	97.66	96.31	96.98
	D4A3R	100	66	79.52	Nell-DBpedia	L3.3Short	94.32	100.00	97.08
	D4A5R	100	68	80.95		L3.3Long	94.67	95.48	95.07
Nell-DBpedia	D2A3R	97.83	90	93.75	YAGO-Wikidata	L3.3Short	91.80	99.60	95.54
	D2A5R	95.91	94	94.95		L3.3Long	92.31	94.80	93.53
	D4A3R	95.55	86	90.53					
	D4A5R	93.88	92	92.93					
YAGO-Wikidata	D2A3R	100	92	95.83					
	D2A5R	100	96.9	98.41					
	D4A3R	100	86	92.47					
	D4A5R	100	90	94.73					

Can “Debating” help? We implemented an LLM Debate ensemble [18], where multiple agents propose alignments with their chain-of-thought and then iteratively critique one another. To bound context size, we drop 50% of historic turns and keep only each agent’s latest reply. Due to its expense, we tested this on Mouse-Human, Nell-DBpedia, and YAGO-Wikidata using four permutation of configurations: 2 or 4 agents over 3 or 5 debate rounds, denoted as D [Number

Of Agent]A[Number Of Round]R. From Table 4 (Left), on Mouse–Human dataset, extending rounds in the 2-agent setup raised F1 from 82.35 to 85.06, whereas adding agents degraded performance (4 agents: 79.52 at 3 rounds, 80.95 at 5). Similar trends follow for Nell-DBpedia and YAGO-Wikidata. This interestingly indicates that “longer debates” help small ensembles converge to accurate matches, but larger groups introduce too much conflicting reasoning. In contrast, a single-agent, single-round KROMA pass attains $F1 = 90.78$, underscoring that a well-tuned solo model remains the most efficient and reliable choice.

Can “Deep reasoning” help? Building on DeepSeek-R1’s “Aha Moment” [13], we extended KROMA to include a forced long chain-of-thought for self-revision. Noting that vanilla DeepSeek-R1 often emits empty “<think>\n” tags (i.e. “<think>\n\n</think>”), we altered our prompt so every response must start with “<think>\n”, ensuring the model spells out its reasoning. We then compared standard Llama-3.3 (70B) (“short” reasoning, noted as L3.3Short) to DeepSeek-R1-Distill-Llama-3.3 (70B) (“long” reasoning, noted as L3.3Long), finding that the added “<think>\n” tag inflated inputs by 20% and outputs by 600% but delivered only tiny precision gains (e.g., NCIT–DOID: 97.59% \rightarrow 97.66%) while slashing recall (99.69% \rightarrow 96.31%), dropping F1 by 1.65–2.01 points, based on Table 4 (Right). This suggests that verbose self-reflection may improve transparency but consumes crucial context and can overly filter valid matches—especially in binary tasks, where lengthy chains of thought have been shown to harm recall, which has been consistently observed in [55].

7 Conclusion

We have presented KROMA, an ontology matching framework that exploits the semantic capabilities of LLMs within a bisimilar-based ontology refinement process. We show that KROMA computes a provably unique minimized structure that captures semantic equivalence relations, with efficient algorithms that can significantly reduce LLMs communication overhead, while achieving state-of-the-art accuracy across multiple OAEI benchmarks. Our evaluation has verified that LLMs, when guided by context and optimized prompting, can rival or surpass much larger models in accuracy. A future topic is to extend KROMA with more LLM reasoning strategies and ontology engineering tasks.

Supplemental Material Statement. Our code and experimental data has been made available at <https://anonymous.4open.science/r/kroma/>, including an extended version of the paper [1].

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Appendix

A Proofs of Theorems and Lemmas

Proof of Lemma 1. The relation R_{\sim} is an equivalence relation.

Proof. Let the set $C = C_s \cup C_t$. It suffices to show that the relation R_{\sim} is reflexive, symmetric, and transitive for a concept equivalence function F that is transitive, *i.e.*, for any three concepts c_1, c_2, c_3 in C , if $F(c_1, c_2) = \text{true}$, $F(c_2, c_3) = \text{true}$, then $F(c_1, c_3)$ is true.

(1) For any node $c \in C$, (c, c) is a trivial case as a concept is the same (hence bisimilar) to itself.

(2) We next show that R_{\sim} is symmetric, *i.e.*, for any node pair $(c_1, c_2) \in R_{\sim}$, $(c_2, c_1) \in R_{\sim}$. To see this, assume that $(c_2, c_1) \notin R_{\sim}$. Then there exists a neighbor c'_2 of c_2 such that no neighbor of c_1 can be found to match any neighbor of c'_2 . This violates the condition that for every edge $(c'_2, c_2) \in E_s$, one can find a corresponding edge with the “matched” end nodes in R_{\sim} , indicating that R_{\sim} is not an ontological bisimilarity function. This leads to the contradiction. Hence $(c_1, c_2) \in R_{\sim}$ indicates $(c_2, c_1) \in R_{\sim}$, *i.e.*, R_{\sim} is symmetric.

(3) We next show that if $(c, c') \in R_{\sim}$ and $(c', c'') \in R_{\sim}$, then $(c, c'') \in R_{\sim}$. Assume $(c, c'') \notin R_{\sim}$. Then either there exists a neighbor c_u of c , such that no equivalent “match” can be found in the neighbor of c'' , or vice versa. We consider w.l.o.g the first case. As $(c', c'') \in R_{\sim}$, then $(c'', c') \in R_{\sim}$ given the symmetric property. Then for any neighbor c''_u of c'' , one can find an equivalent match c'_u of c' , such that $(c''_u, c'_u) \in R_{\sim}$. As $(c, c') \in R_{\sim}$, then $(c', c) \in R_{\sim}$. Hence for the neighbor c'_u , there must exist a neighbor c_u of c , such that $(c'_u, c_u) \in R_{\sim}$. Given the transitivity of the concept similarity determined by F function, c''_u and c'_u are concept similar, and c'_u and c_u are concept similar; hence c''_u and c_u are concept similar. This suggests $(c''_u, c_u) \in R_{\sim}$. Hence $(c_u, c''_u) \in R_{\sim}$ given the symmetric property. This contradicts to the assumption that c_u has no equivalent counterpart in R_{\sim} . Hence the transitivity of R_{\sim} holds.

Putting these together, R_{\sim} is an equivalence relation.

Proof of Lemma 2. Given a configuration W and semantic equivalence specified by the ontological bisimilar relation R_{\sim} , there is a unique smallest concept graph \mathcal{G}_O that capture all semantically equivalent nodes in terms of R_{\sim} .

Proof. To see this, we let R^* to be the largest ontological bisimilar relation that holds on $C = C_s \cup C_t$. That is, there is no other relation R such that $R^* \subset R$ and R is an ontological bisimilar relation. Let a graph \mathcal{G}^* be the quotient graph of the ontology graphs $O_s \cup O_t$ induced by the concept set C . It suffices to show that \mathcal{G}^* is the smallest concept graph over C , and is unique up to all smallest concept graphs one may construct in terms of ontological equivalence relations.

(1) We first show that \mathcal{G}^* is the smallest concept graph. To see this, assume there exists another concept graph \mathcal{G}' that contains fewer nodes or edges than \mathcal{G}^* , induced by another ontological equivalence relation R' . Assume w.l.o.g that

it contains fewer nodes. Then there must exist two concept nodes c and c' in C , such that c and c' are in the same equivalence class (node) in \mathcal{G}' but not in \mathcal{G}^* . In other words, $(c, c') \in R'$ but not in R^* . This suggests that $|R^*| \leq |R'|$, violating the fact that \mathcal{G}^* is induced by a largest ontological equivalence relation R^* . The above analysis also holds for the case that \mathcal{G}^* contains more edges than \mathcal{G}' . Hence, \mathcal{G}^* contains the least number of nodes and edges, and is the smallest concept graph.

(2) We next show the uniqueness of \mathcal{G}^* . Let there be another smallest concept graph \mathcal{G}' induced by another ontological equivalence relation R' . Moreover, \mathcal{G}^* and \mathcal{G}' are different in terms of graph isomorphism. Then there are three cases. (i) \mathcal{G}^* and \mathcal{G}' have different number of nodes or edges. For either case, an analysis similar to (1) leads to a contradiction that R^* is the maximum ontological equivalence relation. (ii) $|\mathcal{G}'| = |\mathcal{G}^*|$, and there exists a node $c \in C$ such that its equivalence classes $[c]'$ and $[c]^*$ are different in \mathcal{G}' and \mathcal{G}^* . Then there must exist a pair of nodes (c, c') , such that $(c, c') \in [c]'$ and $(c, c') \notin [c]^*$. This case reduces to the analysis in (1), leading to a contradiction that R^* is the largest ontological equivalence relation. Hence \mathcal{G}^* is structurally unique up to graph isomorphism, *i.e.*, if there exists a second smallest concept graph \mathcal{G}' , then \mathcal{G}^* and \mathcal{G}' are identical in terms of graph isomorphism.

B Additional Experiments & Discussion

KROMA vs Baselines Table 5 shows that the full KROMA configuration (KL3.3) consistently achieves the highest F_1 -score on all six benchmarks. For Mouse–Human, KL3.3 reaches 94.94%, outperforming the next best model (KL3.1) by 0.44 points. On NCIT–DOID, KL3.3 posts 98.63%, edging out KL3.1 (98.24%) and far surpassing other baselines. In Nell–DBpedia, YAGO–Wikidata, and ENVO–SWEET, KL3.3 attains 97.08%, 95.54%, and 93.18% F_1 , respectively—each more than 1.5 points above any alternative. Even on the challenging MI–MatOnto track, KL3.3’s 61.25% F_1 clearly beats KL3.2 (59.05%) and other methods. These results confirm that, across diverse domains, KROMA’s retrieval-augmented, refinement-driven pipeline with Llama-3.3 yields the best precision–recall balance compared to existing LLM-based and traditional baselines.

Confidence Calibration Figure 4 illustrates how well each model’s self-reported confidence aligns with its actual accuracy across six diverse ontology-matching datasets (Mouse–Human, NCI Thesaurus–DOID, NELL–DBpedia, YAGO–Wikidata, ENVO–SWEET, and MI–MatOnto). In each subplot, the horizontal axis is divided into eleven “confidence bins” (e.g., 1–2, 2–3, ..., 10–11), and the vertical axis separates correct versus incorrect predictions. The heatmap’s color intensity corresponds to the number of predictions falling into each cell (correct/wrong \times confidence bin).

A clear pattern emerges across all six datasets: the vast majority of correct matches are concentrated in the highest confidence bins—particularly 9–10 and 10–11—while almost no wrong answers appear at those high confidence levels. Conversely, whenever an error does occur, it is overwhelmingly reported with

Table 5: KROMA vs Baselines.

Dataset	Model	P	R	F_1
Mouse-Human	KL3.3	90.78	99.50	94.94
	KNR3.3	92.34	90.16	91.25
	KNB3.3	100.00	76.36	86.59
	KL3.1	90.42	99.00	94.50
	KL2.0	100.00	87.34	93.24
	ML3.1	100.00	87.50	92.20
	OL2.0	91.40	89.10	90.20
	L4G3.5	90.82	87.46	89.11
NCIT-DOID	KL3.3	97.59	99.69	98.63
	KNR3.3	93.20	96.90	95.01
	KNB3.3	83.33	100.00	90.91
	KL3.1	97.43	99.08	98.24
	KG2	84.76	86.32	85.53
	ML3.1	96.40	93.20	94.80
	LLFT	86.10	62.00	72.10
	L4G3.5	86.19	80.06	83.01
Nell-DBpedia	KL3.3	94.32	100.00	97.08
	KNR3.3	97.46	91.27	94.26
	KNB3.3	91.17	96.12	93.58
	KL2.0	95.50	96.55	96.02
	OL2.0	100.00	92.20	96.00
	L4G3.5	100.00	89.14	94.26
YAGO-Wikidata	KL3.3	91.80	99.60	95.54
	KNR3.3	93.50	90.50	91.98
	KNB3.3	90.50	89.00	89.74
	KL3.2	89.09	98.00	93.33
	L4L2	100.00	85.52	92.19
ENVO-SWEET	K4mini	87.23	100.00	93.18
	KNR4mini	86.90	98.00	92.12
	KNB4mini	82.00	88.00	84.89
	KL3.1	87.11	96.19	91.43
	KL2.0	92.50	78.72	85.06
	KM7	87.19	99.59	92.98
	ML3.1	80.30	59.50	83.70
	OL2.0	43.10	61.30	51.10
MI-MatOnto	L4M7	59.00	51.67	55.09
	KL3.3	45.74	92.69	61.25
	KNR3.3	44.80	91.40	59.95
	KNB3.3	42.00	85.00	55.00
	KL3.2	56.36	62.00	59.05
	L4MPT	89.70	20.19	32.97

lower self-evaluated confidence (bins < 8). For example, in the Mouse–Human subplot, more than 80 percent of correct alignments lie in the 9–10 and 10–11 bins

(bright yellow and light green shading), whereas the “Wrong” row is nearly empty in those same bins. Similarly, the NCI Thesaurus–DOID and NELL–DBpedia plots show that over 80 percent of all correct alignments land in the top two confidence buckets, with fewer than 5 percent of errors ever reported above a confidence of 8.

Taken together, these calibration curves give us strong evidence that a confidence cutoff around 8.5 will safely distinguish nearly all true positives from false positives. By accepting only those matches where the model’s own confidence exceeds 8.5, we preserve the vast majority of correct alignments (since 80–90 percent of them sit in bins 9–10 and 10–11) and reject almost all of the few remaining errors. Consequently, for our downstream ontology-matching pipeline, we adopt a uniform confidence threshold of 8.5 for every LLM, striking a balance between recall (capturing most correct alignments) and precision (avoiding high-confidence mistakes).

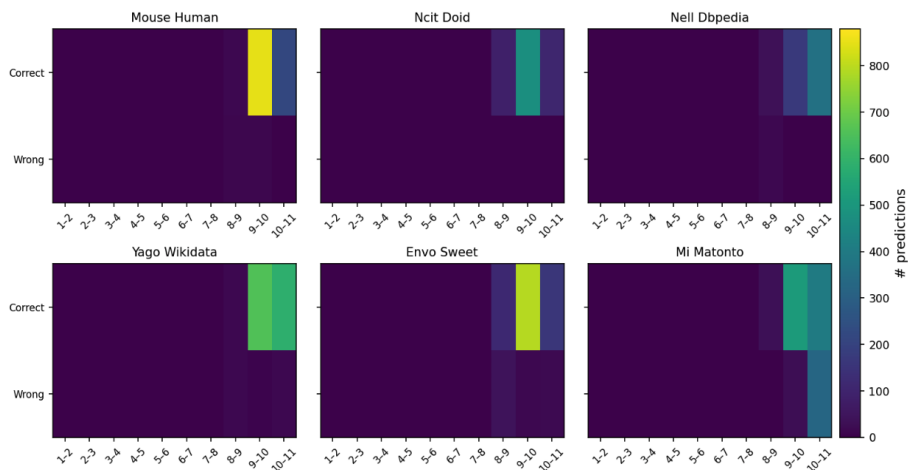


Fig. 4: LLMs Confidence Calibration

KROMA Performance on different ontology sizes Table 6 demonstrates that KROMA’s precision, recall, and F_1 -scores remain remarkably stable as we move from very small (xsmall) to full-sized ontologies. For NCIT–DOID, F_1 fluctuates only between 97.50% (xsmall) and 98.63% (full), with recall slightly increasing on larger splits and precision peaking at 98.00% on the large subset. Similarly, on NELL–DBpedia, F_1 rises steadily from 95.83% (xsmall) to 97.58% (large) before a minor dip to 97.08% at full scale, reflecting high recall (>99%) even as more candidate classes are introduced. YAGO–Wikidata shows the same trend: recall climbs from 98.00% to 99.60% as the ontology grows, while precision decreases only marginally (92.00% to 91.80%), resulting in consistent F_1 values in the mid-90s. These results indicate that KROMA’s retrieval-augmented pipeline can accommodate ontologies of increasing size without sacrificing matching quality, suggesting strong scalability for real-world, large-scale entity-matching tasks.

KROMA’s robustness to growing ontology size stems from its two-stage retrieval-augmented design, which keeps the LLM’s decision space both focused and consistent as more classes are added. First, instead of asking the model to compare every source–target pair globally, KROMA uses a semantic-search index to pull in only the top- k most relevant candidates for each source concept; as the ontology grows, irrelevant classes are filtered out early, so the LLM is still evaluating a bounded, high-precision shortlist. Second, once a small set of likely matches is identified, KROMA applies a fixed-length prompting and refinement step—complete with a confidence-based acceptance threshold—so that the LLM sees a similar amount of contextual information regardless of the overall ontology’s full size. In other words, expanding the classifier’s universe does not force the model to process vastly more text at inference time; it simply broadens the retrieval pool, but the same narrow, top- k candidates are forwarded to the matching prompt. Finally, because the confidence filter rejects low-certainty pairs consistently across all scales, noisy or spurious candidates introduced by a larger ontology rarely make it through to final alignment.

Table 6: KROMA Performance on different ontology sizes.

Dataset	Metric	xsmall	small	medium	large	full
NCIT-DOID	P	97.50	97.88	97.92	98.00	97.59
	R	97.50	98.12	97.50	98.13	99.69
	F_1	97.50	98.00	97.71	98.06	98.63
Nell-DBpedia	P	95.00	95.19	95.24	95.63	94.32
	R	96.67	98.33	99.17	99.58	100.00
	F_1	95.83	96.74	97.18	97.58	97.08
YAGO-Wikidata	P	92.00	92.50	92.67	92.75	91.80
	R	98.00	98.75	99.17	99.38	99.60
	F_1	94.90	95.58	95.89	96.04	95.54

KROMA Efficiency on Communication Cost and Offline/Online Refinement Delay speedup Across all six benchmark datasets, KROMA cuts the average communication cost to roughly a quarter of what a naïve full-pairwise matching approach would require: Qwen2.5, GPT-4o-mini, and Llama-3.3 each achieve overall token-exchange rates of about 25.9%, 25.6%, and 26.4%, respectively. On smaller ontologies like Mouse–Human and ENVO–SWEET, the cost dips below 7%, while even the largest schemas (NCIT–DOID and MI–MatOnto) stay in the 40–54% range. This reduction arises because KROMA’s retrieval stage pre-filters each source concept to a compact shortlist of candidates, so the LLM only receives a fraction of the total class descriptions instead of the entire ontology. As a result, fewer tokens are sent in both the query prompts and the LLM’s responses, directly lowering per-dataset communication without sacrificing matching quality.

When comparing end-to-end latency, performing KROMA’s refinement offline yields a consistent speedup of over $9\times$ on average (with individual dataset factors ranging from $2.33\times$ on NCIT–DOID to $18.76\times$ on YAGO–Wikidata). In the offline scenario, all heavy LLM calls—such as deep refinement of candidate pairs—are run ahead of time, leaving only lightweight lookups and confidence

checks to occur at inference. Online, that means the service can respond almost instantly with precomputed results instead of re-invoking the model for every request. Because each source term has already been matched and filtered offline, the system avoids redundant LLM invocations, dramatically cutting delay and delivering real-time throughput in applications.

Table 7: KROMA Efficiency on Communication Cost (Left); and Offline vs. Online Refinement Delay speedup (Right).

Dataset	Qwen2.5	GPT-4o-mini	Llama-3.3	Dataset	Offline \div Online
Mouse-Human	3.06%	2.88%	6.76%	Mouse-Human	7.17 \times
NCIT-DOID	54.48%	54.63%	54.48%	NCIT-DOID	2.33 \times
Nell-DBpedia	26.09%	25.76%	26.09%	Nell-DBpedia	5.63 \times
YAGO-Wikidata	21.86%	21.93%	22.01%	YAGO-Wikidata	18.76 \times
ENVO-SWEET	6.99%	6.82%	6.99%	ENVO-SWEET	7.00 \times
MI-MatOnto	43.04%	41.66%	41.81%	MI-MatOnto	13.31 \times
Overall	25.92%	25.61%	26.36%	Overall	9.03\times