
Andrew Lampinen

FriSem, 5/11/2018

**How do humans learn so quickly and
effectively?**

Transfer across domains



[Lampinen, Hsu, and McClelland, 2017, Hansen, Lampinen, Suri, and McClelland, 2017]

Transfer across domains



[Lampinen et al., 2017, Hansen et al., 2017]

Transfer across domains

<u>Category's name :</u>	<u>its objects :</u>	<u>its morphisms :</u>
Set	sets	functions
Group	groups	group homomorphisms
Top	topological spaces	continuous functions
Vect _k	vector spaces over a field, k	linear transformations
Meas	measurable spaces	measurable functions
Poset	partially ordered sets	order-preserving functions
Man	smooth manifolds	smooth maps

[Lampinen et al., 2017, Hansen et al., 2017]

Background

- Not a new idea: transfer has been called a central component of “why we’re so smart” [Gentner, 2003], and an important source of new ideas [Gick and Holyoak, 1980].

Background

- Not a new idea: transfer has been called a central component of “why we’re so smart” [Gentner, 2003], and an important source of new ideas [Gick and Holyoak, 1980].
- However, this perspective has been criticized!

Background

- Not a new idea: transfer has been called a central component of “why we’re so smart” [Gentner, 2003], and an important source of new ideas [Gick and Holyoak, 1980].
- However, this perspective has been criticized!
 - “Significant transfer is probably rare and accounts for very little human behavior. ... We generally do what we have learned to do and no more.” [Detterman, 1993]

Background

- Not a new idea: transfer has been called a central component of “why we’re so smart” [Gentner, 2003], and an important source of new ideas [Gick and Holyoak, 1980].
- However, this perspective has been criticized!
 - “Significant transfer is probably rare and accounts for very little human behavior. ... We generally do what we have learned to do and no more.” [Detterman, 1993]
- How can we reconcile these different viewpoints?

Transfer speed

I think there's a neglected variable: speed of transfer.

[Lampinen et al., 2017]

Transfer speed

I think there's a neglected variable: speed of transfer.

Fast	Slow
<ul style="list-style-type: none">• one (or a few) examples explicitly shown	<ul style="list-style-type: none">• learning gradually through many interactions

[Lampinen et al., 2017]

Transfer speed

I think there's a neglected variable: speed of transfer.

Fast	Slow
<ul style="list-style-type: none">• one (or a few) examples explicitly shown• transfer requires explicit awareness of analogy	<ul style="list-style-type: none">• learning gradually through many interactions• transfer may or may not be explicit

[Lampinen et al., 2017]

Transfer speed and outcomes

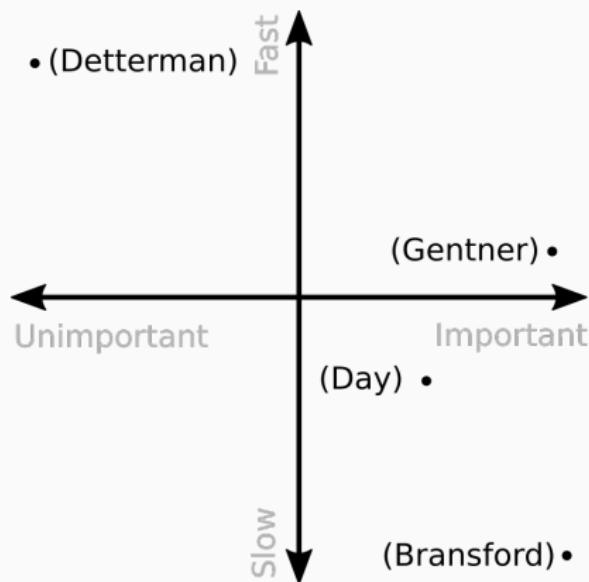
For example, imagine you are about to teach someone to play guitar. Who do you think would likely perform better:

- a person who has just taken their first piano lesson
- a person who has been playing piano for years



Transfer speed and opinions

Transfer speed helps reconcile why some people think transfer is important, while others don't.



Slow transfer between tasks is important.

Is abstraction transfer?

We often progress from procedural to more explicit, abstract, or formal knowledge:

www.worksheetfun.com

Multiplying Three Numbers
3 X 2 X 2 =
2 X 2 X 8 =
3 X 3 X 5 =
2 X 3 X 7 =
1 X 3 X 9 =
2 X 4 X 8 =
1 X 7 X 4 =

Copyright © 2013 www.worksheetfun.com All rights reserved

Is abstraction transfer?

We often progress from procedural to more explicit, abstract, or formal knowledge:

www.worksheetfun.com

Multiplying Three Numbers			
3	X	2	X
2	X	2	X
3	X	3	X
2	X	3	X
1	X	3	X
2	X	4	X
1	X	7	X

Copyright © 2013 www.worksheetfun.com

Factoring Practice
(Continued)

(15) $2x^2 - 7x + 3$	(16) $3x^2 - 8x + 5$
(17) $1x^2 - 15x + 2$	(18) $2x^2 - 5x + 3$
(19) $5x^2 - 12x + 7$	(20) $4x^2 - 12x + 5$
(21) $2x^2 + 6x - 3$	(22) $3x^2 + 2x - 5$
(23) $4x^2 + 4 - 3$	(24) $7x^2 + 11x - 6$
(25) $5x^2 + 8x - 4$	(26) $9x^2 + 6x - 8$
(27) $6x^2 + 31x + 5$	(28) $5x^2 - 6x - 8$
(29) $3x^2 - 11x + 6$	(30) $6x^2 + 15x - 5$

Is abstraction transfer?

We often progress from procedural to more explicit, abstract, or formal knowledge:

www.worksheetfun.com

Multiplying Three Numbers			
3	X	2	X
2	X	2	X
3	X	3	X
2	X	3	X
1	X	3	X
2	X	4	X
1	X	7	X

Copyright © 2013 www.worksheetfun.com

Factoring Practice
(Continued)

(15) $2x^2 - 7x + 3$ (16) $3x^2 - 8x + 5$
(17) $1x^2 - 15x + 2$ (18) $2x^2 - 5x + 3$
(19) $5x^2 - 12x + 7$ (20) $4x^2 - 12x + 5$
(21) $2x^2 + 6x - 3$ (22) $2x^2 - 7x - 5$
(23) $4x^2 - 4$.
(24) $5x^2 + 8x$
(25) $6x^2 + 3x$
(26) $3x^2 - 1$

Theorem 4.11. Let P be a prime ideal in a commutative ring R with identity.

(i) There is a one-to-one correspondence between the set of prime ideals of R which are contained in P and the set of prime ideals of R_P , given by $Q \mapsto Q_P$;
(ii) the ideal P_P in R_P is the unique maximal ideal of R_P .

PROOF. Since the prime ideals of R contained in P are precisely those which are disjoint from $S = R - P$, (i) is an immediate consequence of Theorem 4.10. If M is a maximal ideal of R_P , then M is prime by Theorem 2.19, whence $M = Q_P$ for some prime ideal Q of R with $Q \subset P$. But $Q \subset P$ implies $Q_P \subset P_P$. Since $P_P \neq R_P$ by Theorem 4.8, we must have $Q_P = P_P$. Therefore, P_P is the unique maximal ideal in R_P . ■

Is abstraction transfer?

We often progress from procedural to more explicit, abstract, or formal knowledge:

www.worksheetfun.com

Multiplying Three Numbers			
3	X	2	X
2	X	2	X
3	X	3	X
2	X	3	X
1	X	3	X
2	X	4	X
1	X	7	X

Copyright © 2013 www.worksheetfun.com

Factoring Practice
(Continued)

⑯ $2x^2 - 7x + 3$ ⑰ $3x^2 - 8x + 5$
⑯ $1x^2 - 15x + 2$ ⑰ $2x^2 - 5x + 3$
⑯ $5x^2 - 12x + 7$ ⑰ $4x^2 - 12x + 5$
⑯ $2x^2 + 6x - 3$ ⑰ $2x^2 - 7x - 5$
⑯ $4x^2 - 4$.
⑯ $5x^2 + 8x$
⑯ $6x^2 + 3x$
⑯ $3x^2 - 1$

Theorem 4.11. Let P be a prime ideal in a commutative ring R with identity.

(i) There is a one-to-one correspondence between the set of prime ideals of R which are contained in P and the set of prime ideals of R_P , given by $Q \mapsto Q_P$;
(ii) the ideal P_P in R_P is the unique maximal ideal of R_P .

PROOF. Since the prime ideals of R contained in P are precisely those which are disjoint from $S = R - P$, (i) is an immediate consequence of Theorem 4.10. If M is a maximal ideal of R_P , then M is prime by Theorem 2.19, whence $M = Q_P$ for some prime ideal Q of R with $Q \subset P$. But $Q \subset P$ implies $Q_P \subset P_P$. Since $P_P \neq R_P$ by Theorem 4.8, we must have $Q_P = P_P$. Therefore, P_P is the unique maximal ideal in R_P . ■

These are related tasks that share some structure! Is it useful to think about this from the perspective of transfer?

Is abstraction transfer?

Yet there are also times when procedural and formal knowledge seem partially dissociable:



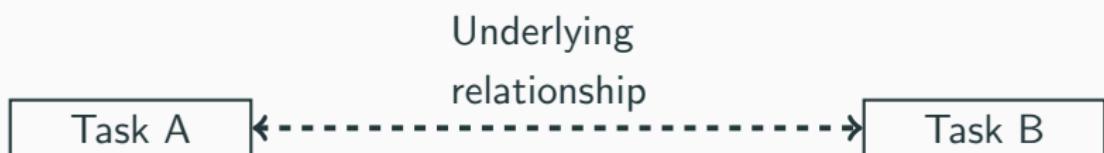
Mixolydian

Musical notation for Mixolydian mode. The key signature has one flat (B-flat). The scale degrees are labeled I, II, III, IV, V, VI, VII. The chords shown are:

Chord	Scale Degree
C ⁷	I
Dm ⁷	II
E [∅]	III
F [△]	IV
Gm ⁷	V
Am ⁷	VI
Bb [△]	VII

When and how does procedural knowledge transfer to more explicit, abstract, or formal knowledge?

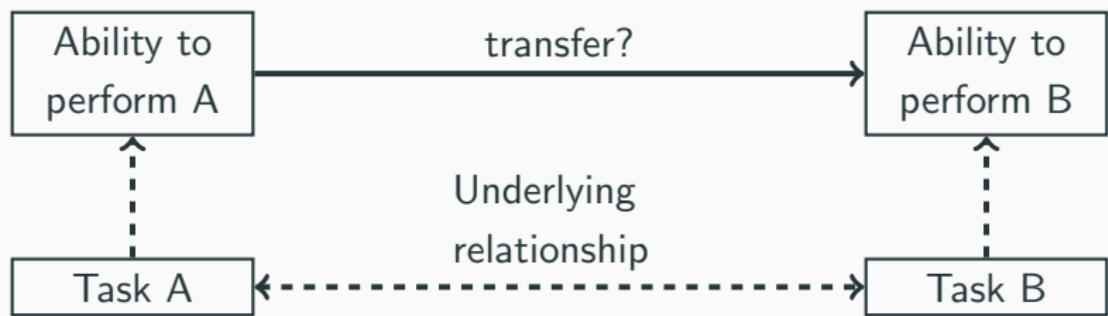
A diagram of potential phenomena of interest



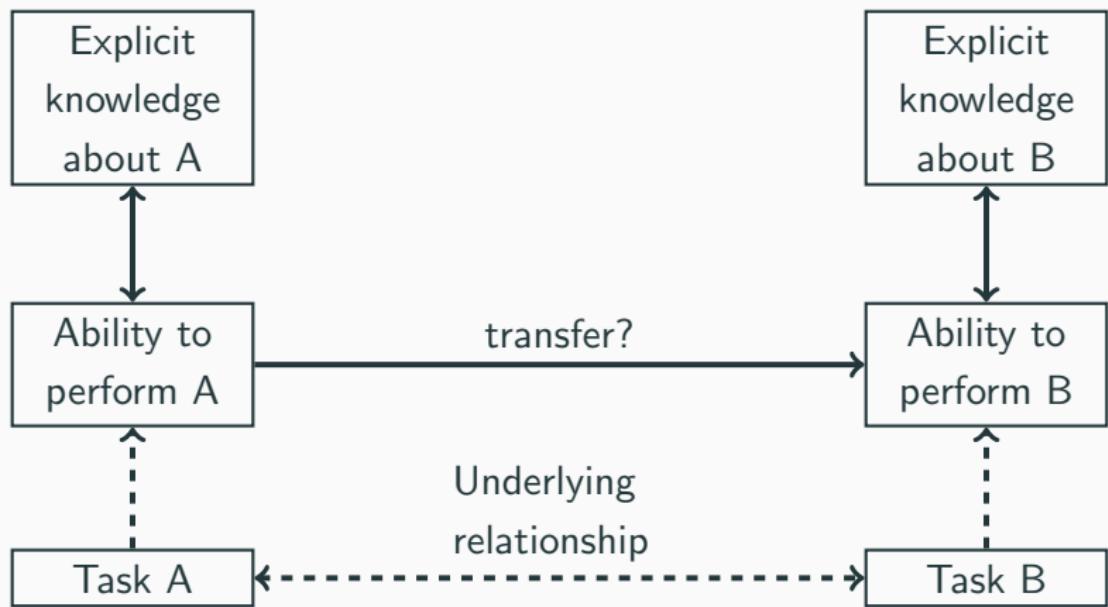
A diagram of potential phenomena of interest



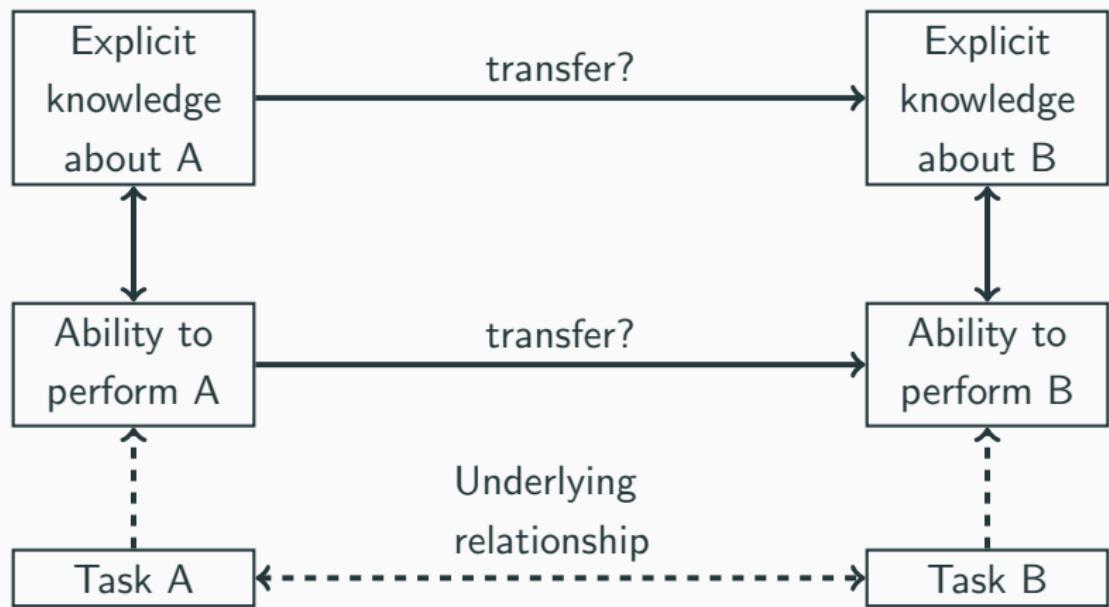
A diagram of potential phenomena of interest



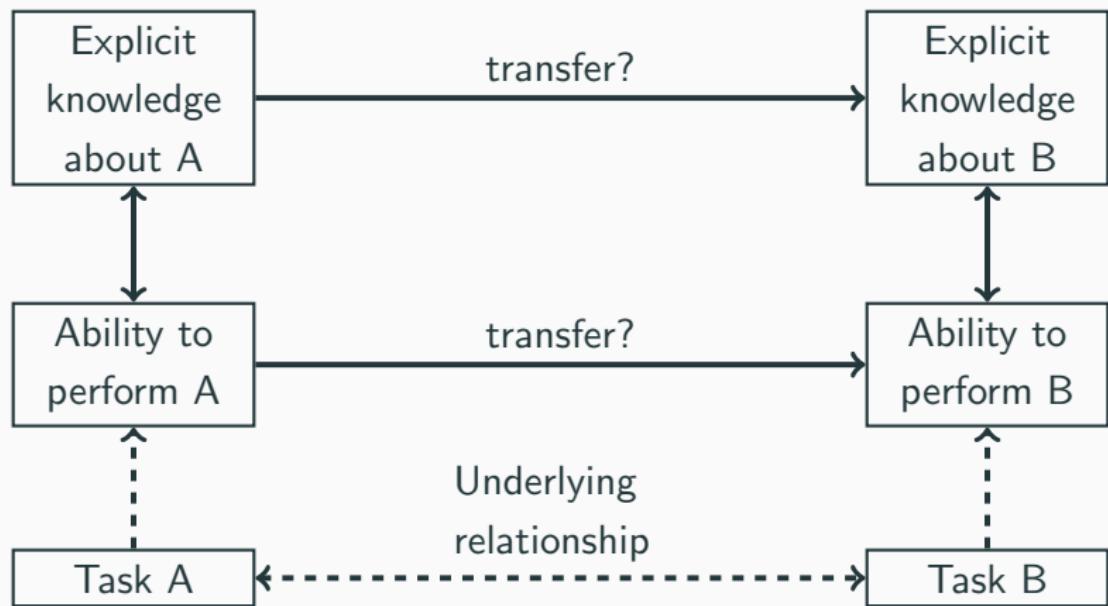
A diagram of potential phenomena of interest



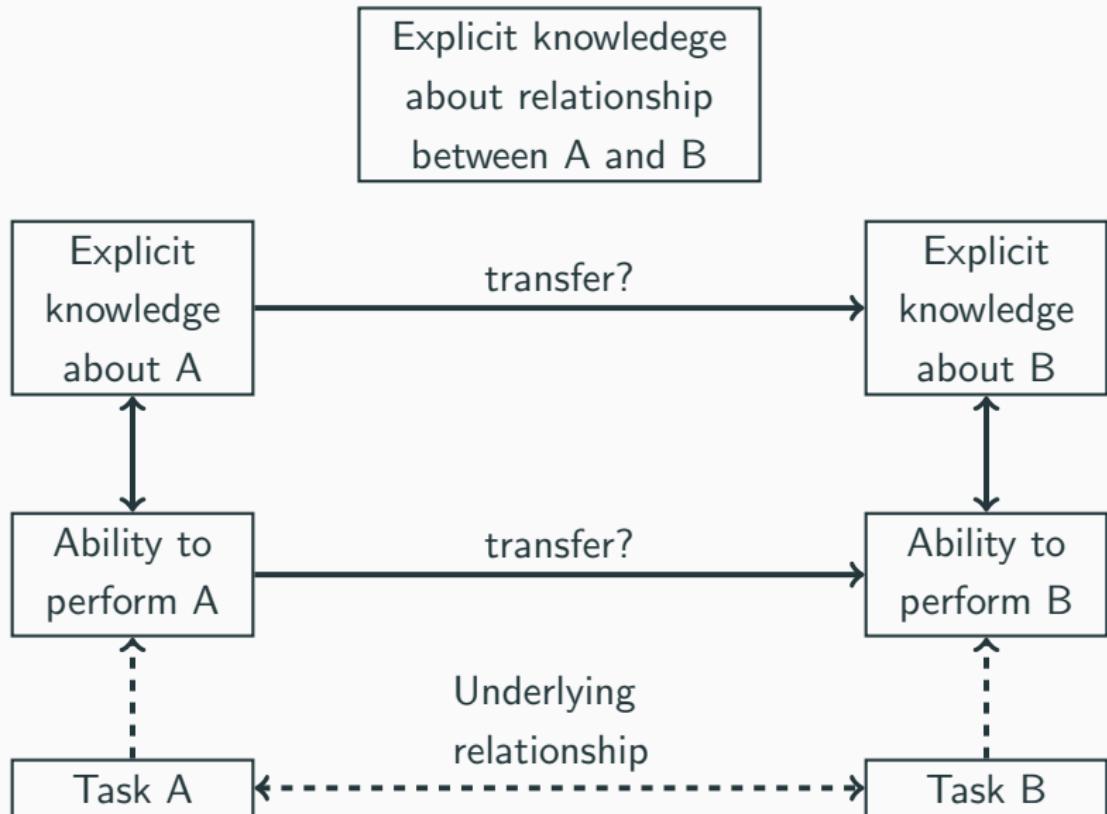
A diagram of potential phenomena of interest



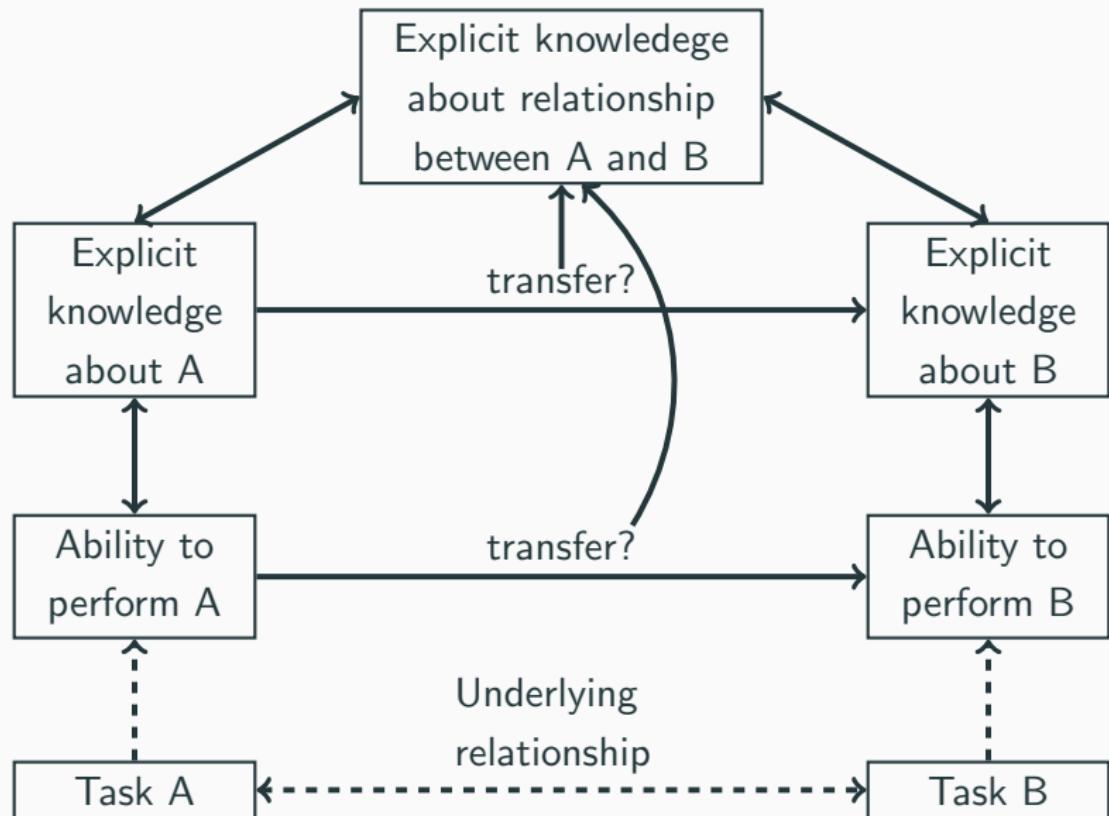
A diagram of potential phenomena of interest



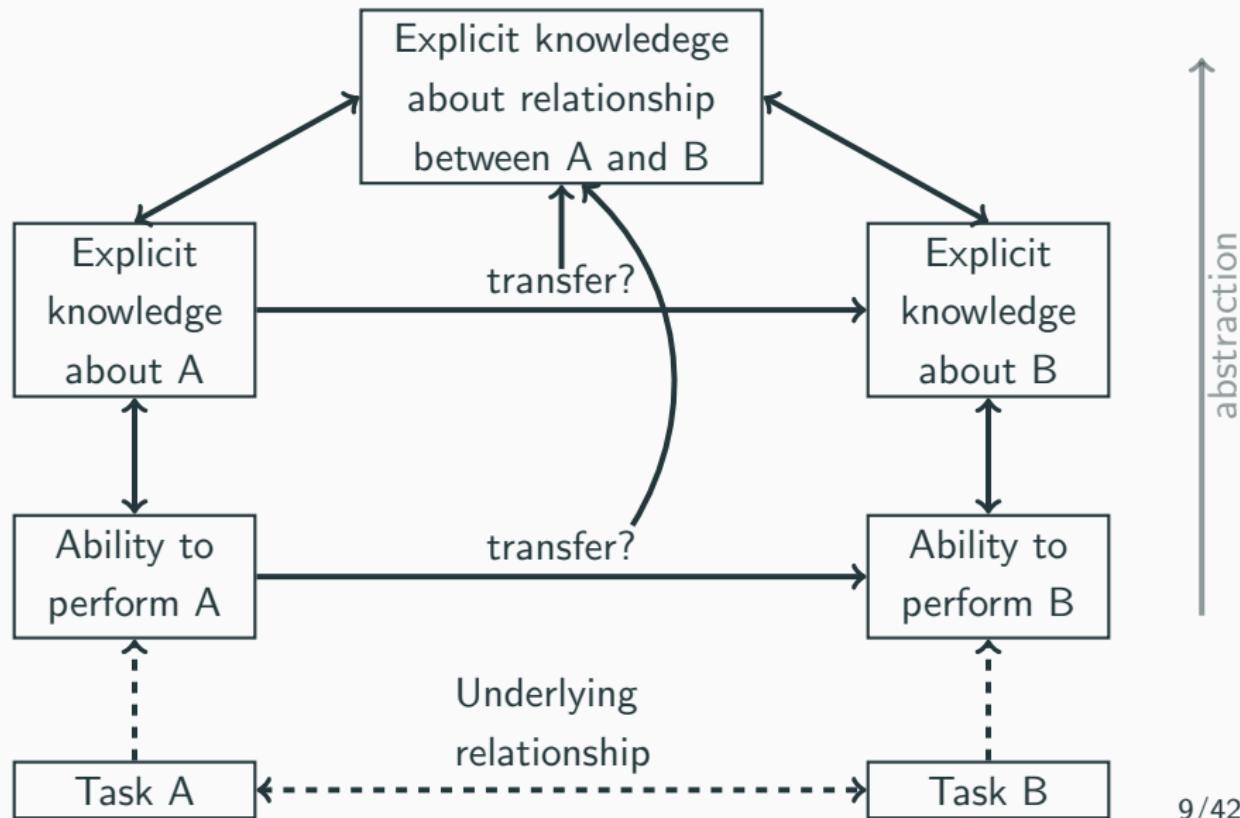
A diagram of potential phenomena of interest



A diagram of potential phenomena of interest



A diagram of potential phenomena of interest

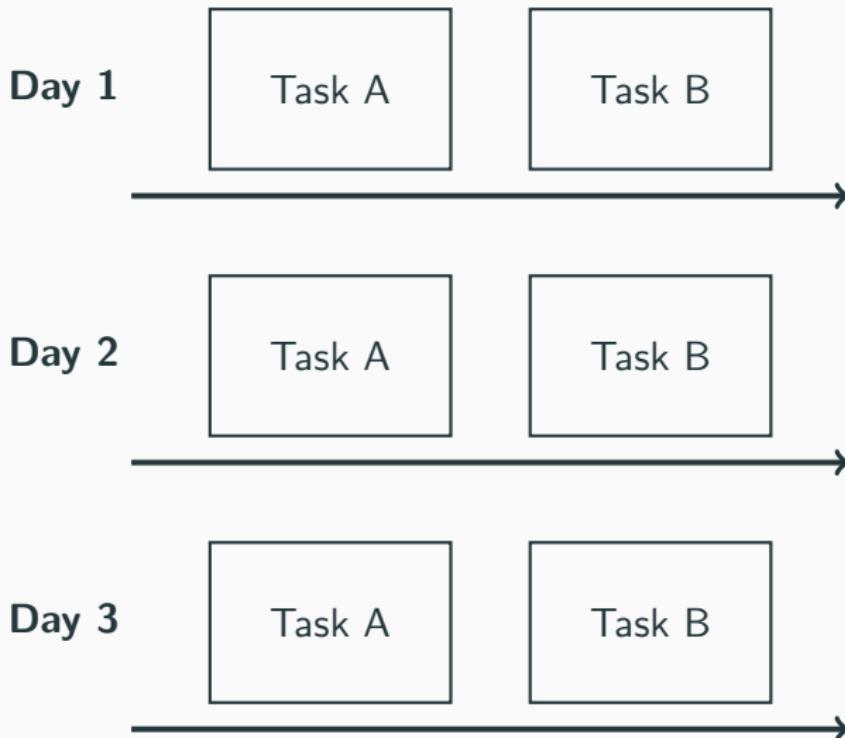


Experiment design

Experiment design



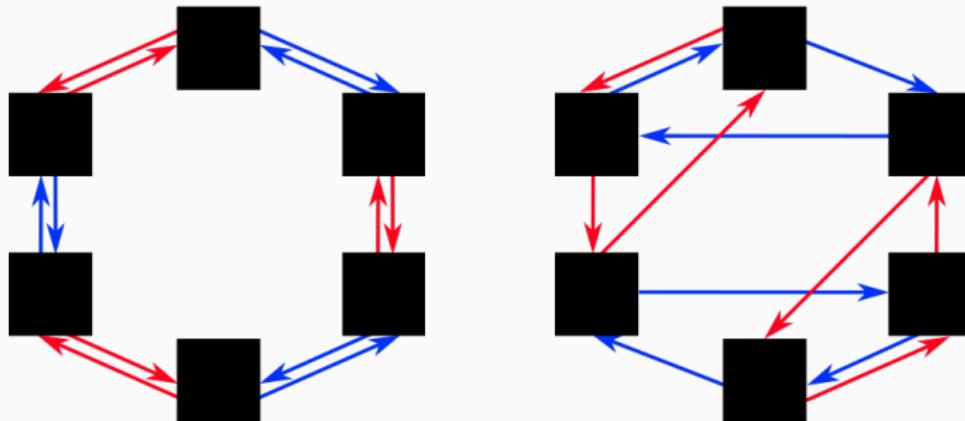
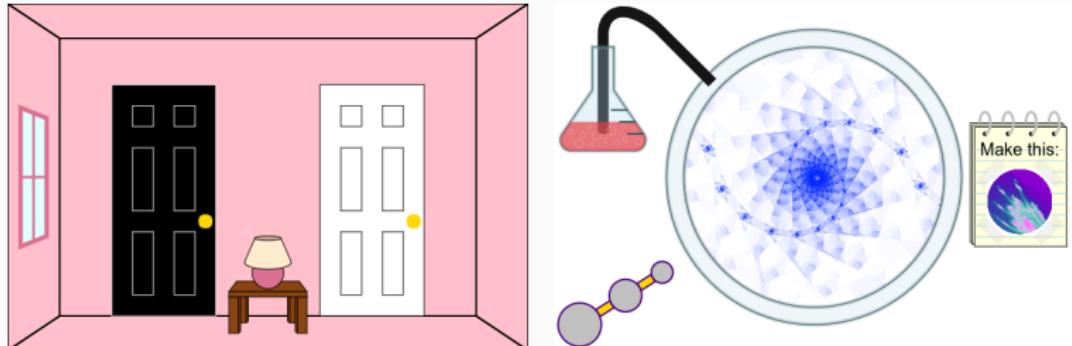
Experiment design



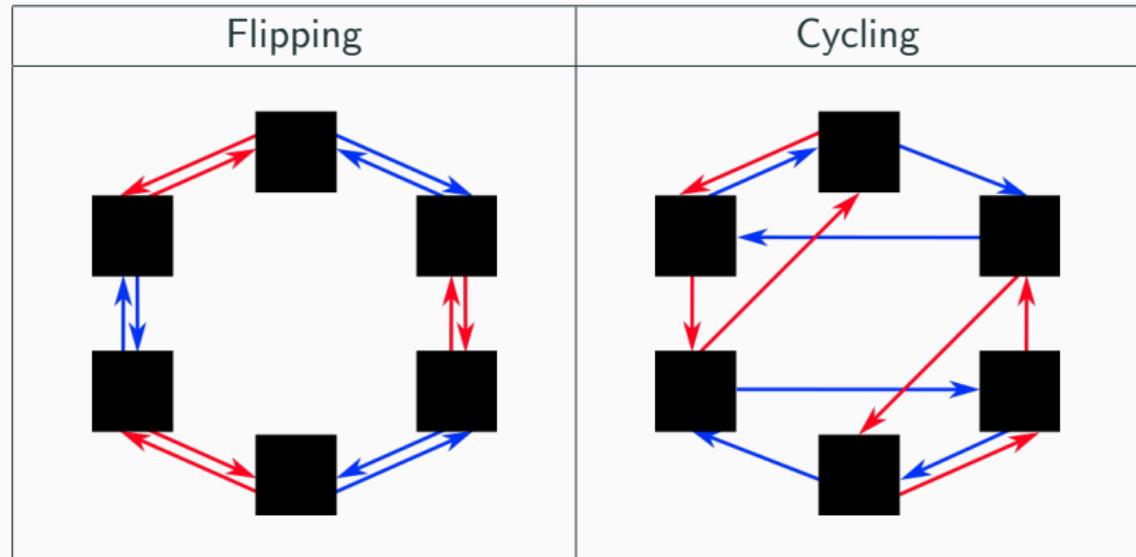
Tasks

https://web.stanford.edu/~lampinen/mturk/il/web/experiment_mockup.html

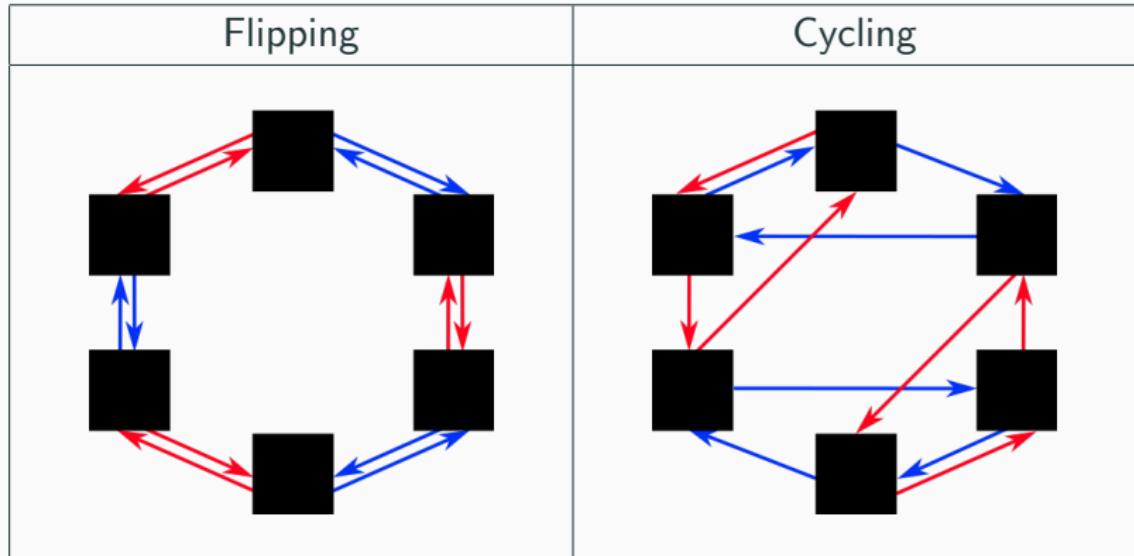
Tasks



Structures



Structures

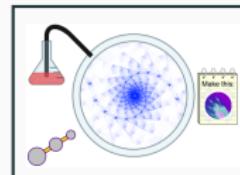
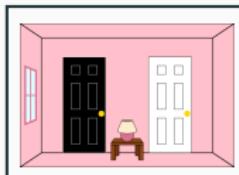


- Balanced for average path length, number of actions entering/exiting a room, etc.

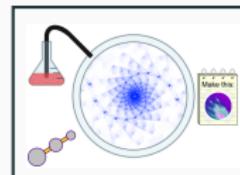
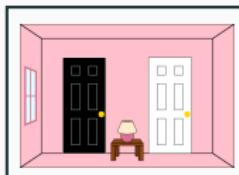
	Fractal structure	
	Flipping	Cycling
Isomorphic		
Non-isomorphic		

Experiment design

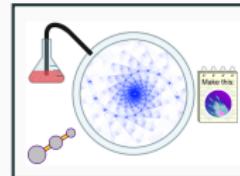
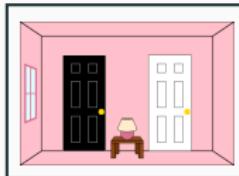
Day 1



Day 2

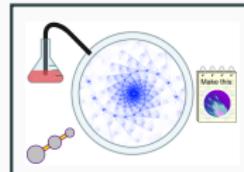
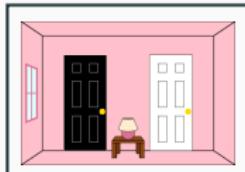


Day 3

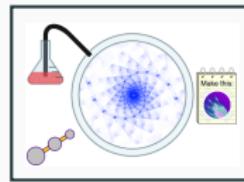
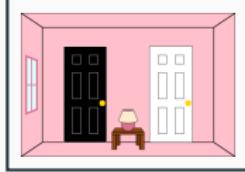


Experiment design

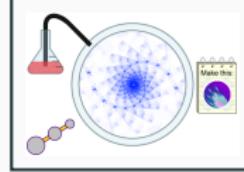
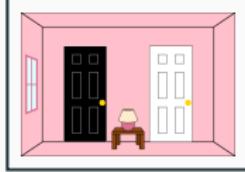
Day 1



Day 2

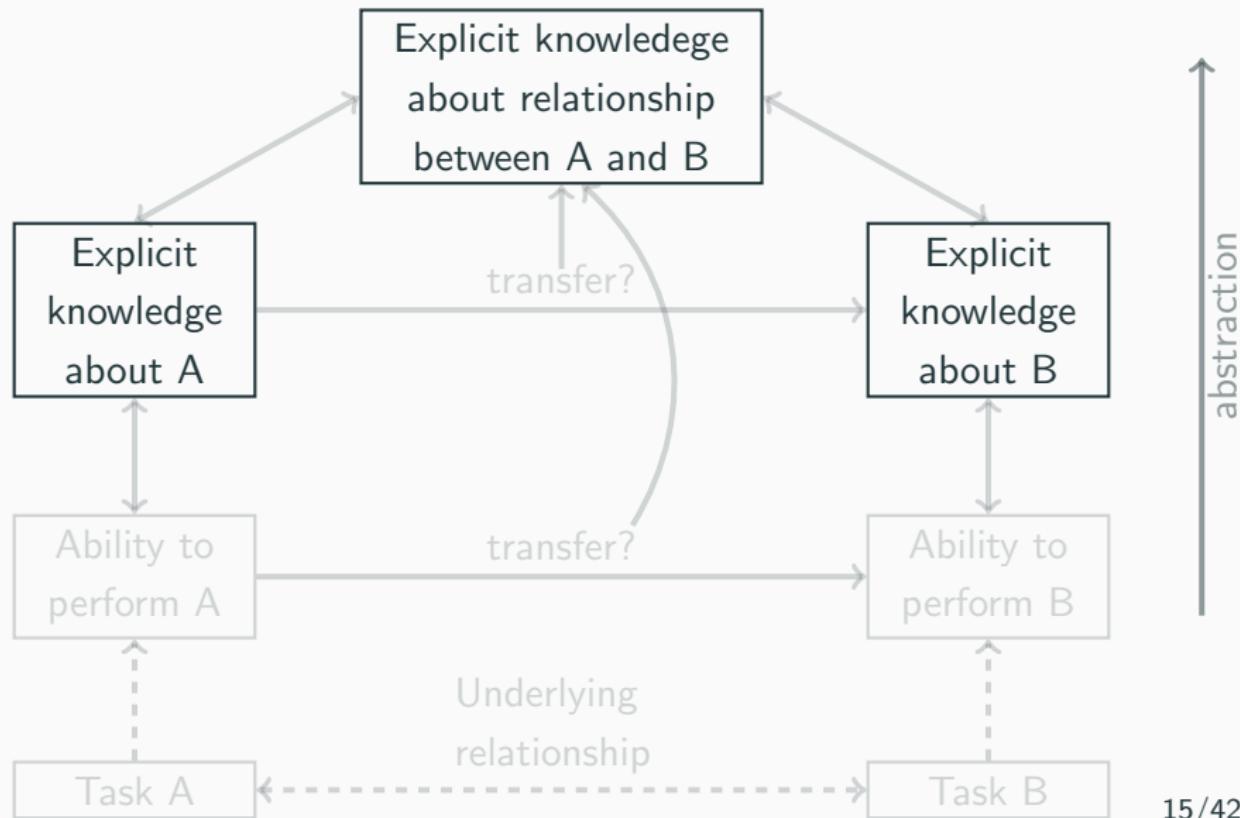


Day 3



Explicit
knowledge?

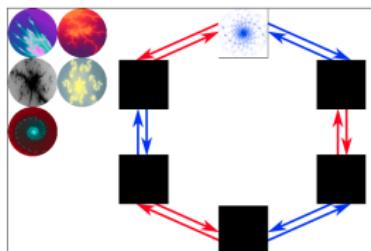
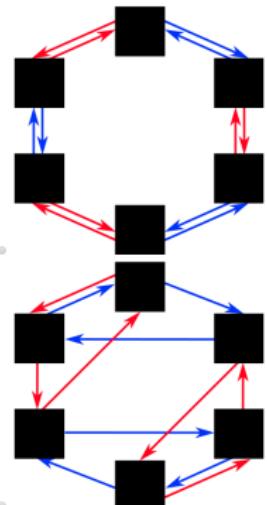
What explicit knowledge?



Explicit knowledge about a single task

Within fractals:

The fractal relationships in your experiment obeyed one of the structures below, where the black squares correspond to fractals, the red arrows correspond to either the gamma ray or the acid, and the blue arrows correspond to the other. Select the structure that you think you had.



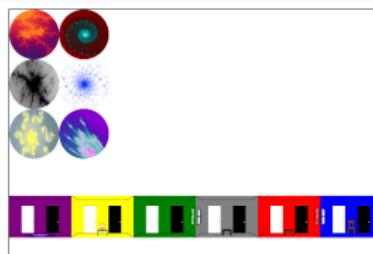
The fractal relationships in your experiment obeyed the structure above (black squares = fractals, red arrows = acid, blue arrows = gamma ray). Drag the fractals onto the black squares that you think they map onto (one has been placed to get you started).

Explicit knowledge about the relationship between tasks

Between tasks:

If the experiments were teaching you the same structure, one of the doors in the spatial navigation experiment would have corresponded to the gamma ray in the fractal experiment, and the other door would have corresponded to the acid. What would be your best guess about the correspondence between the doors and the gamma rays?

- left (black) door = acid, right (white) door = ray
- left (black) door = ray, right (white) door = acid

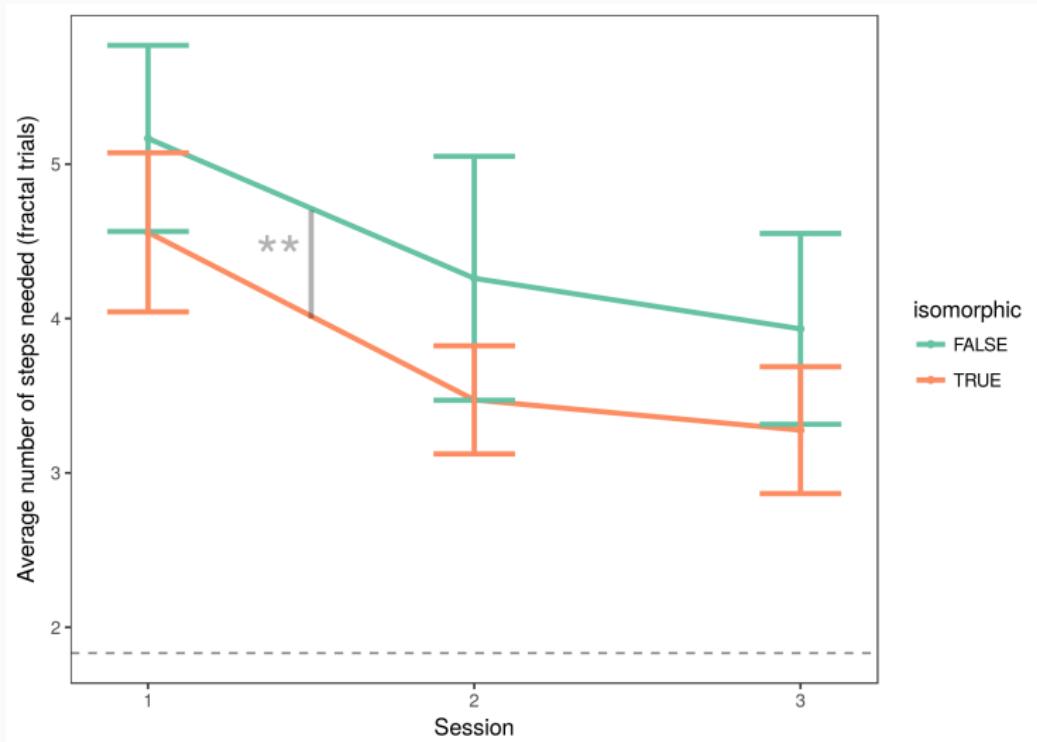


Assuming the experiments were teaching you the same structure, each room in the navigation experiment corresponded to a fractal in the visual patterns experiment. Drag the fractals onto the rooms you think they corresponded to.

[Submit answers](#)

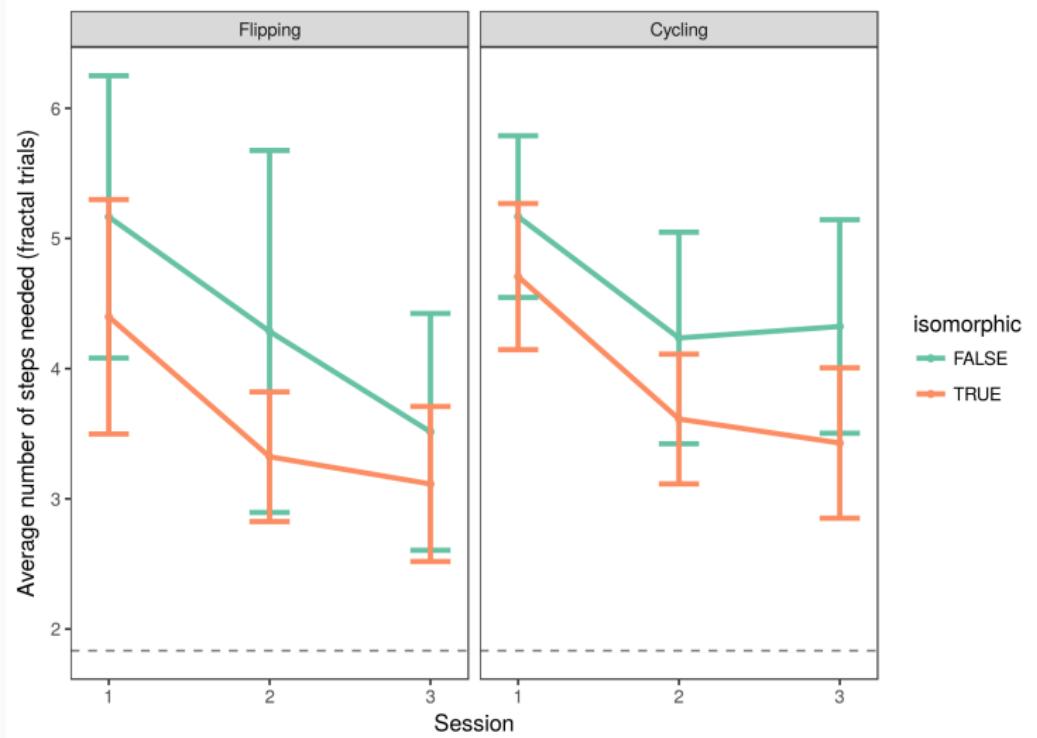
Results

Subjects in isomorphic condition perform better at fractals



Error bars represent 95%-confidence intervals

Subjects in isomorphic condition perform better at fractals



Error bars represent 95%-confidence intervals

Subjects in isomorphic condition perform better at fractals

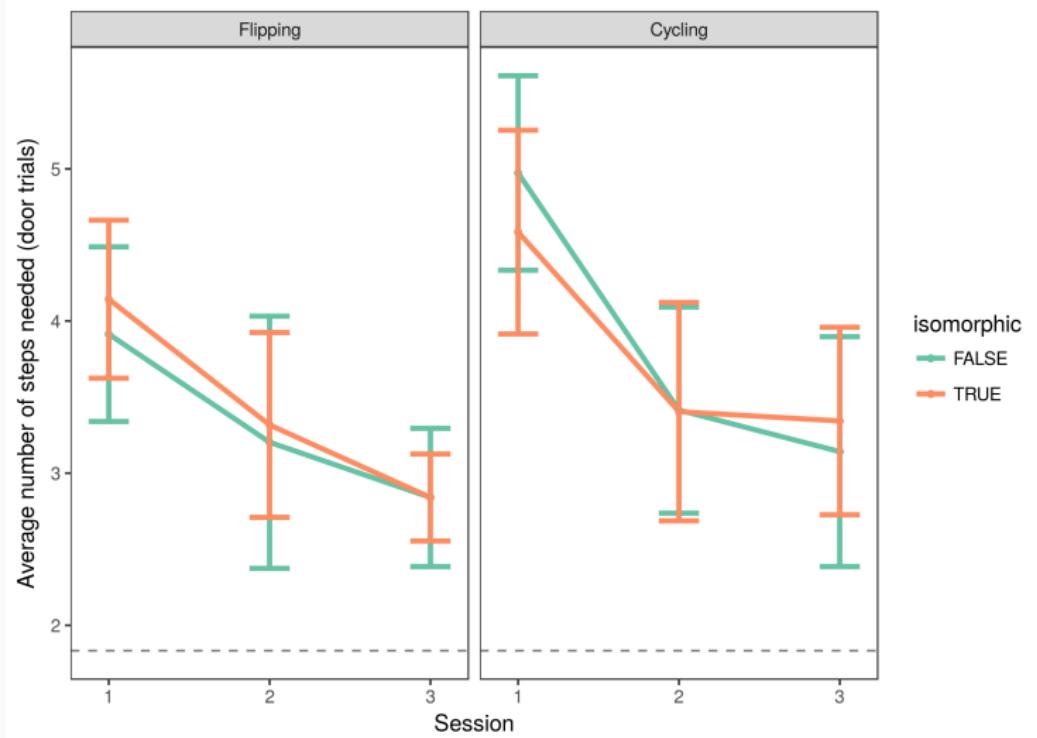
```
Linear mixed model fit by REML
t-tests use Satterthwaite approximations to degrees of freedom ['lmerMod']
Formula: num_steps_needed ~ isomorphic + session_c + I(session_c^2) +
          structure + trial_index_by_type_z +
          I(trial_index_by_type_z^2) + avg_rt_on_trial + (1 + session_c | subject_id)
Data: num_steps_per_trial_data %>% filter(trial_type == "fractal")
REML criterion at convergence: 46673.1

Scaled residuals:
    Min      Q1     Median      Q3     Max 
-2.4192 -0.5138 -0.1547  0.2466 14.9688 

Random effects:
Groups   Name        Variance Std.Dev. Corr
subject_id (Intercept) 1.3336  1.1548
           session_c   0.2308  0.4805  0.06
Residual            15.2730  3.9081
Number of obs: 8350, groups: subject_id, 56

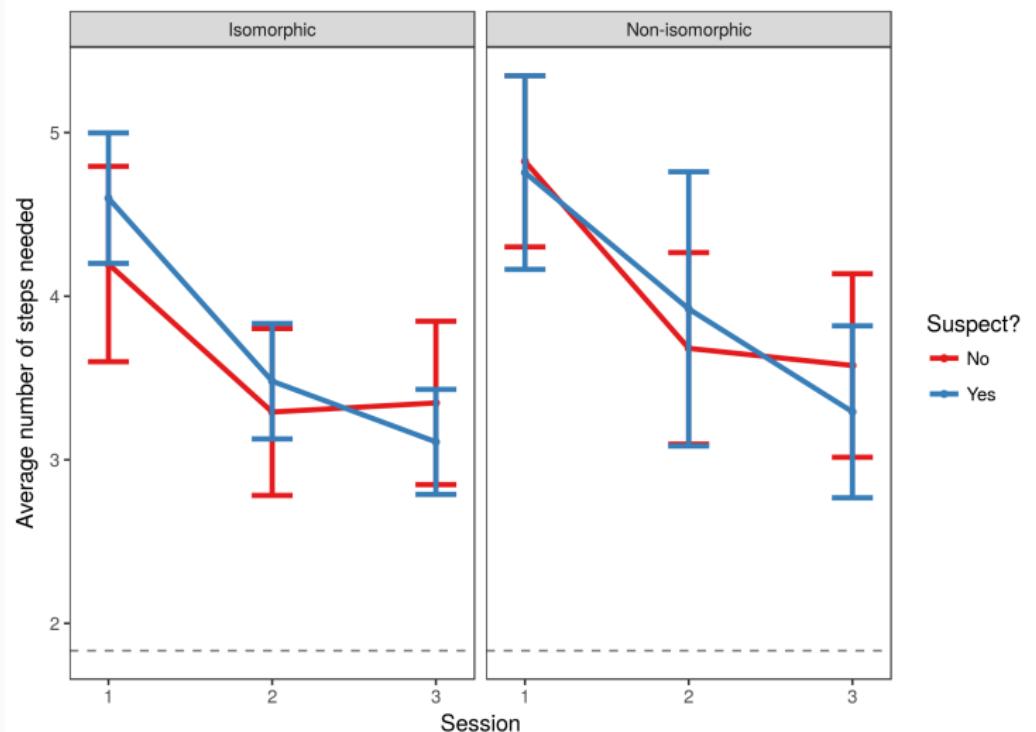
Fixed effects:
            Estimate Std. Error       df t value Pr(>|t|)    
(Intercept)  4.99586  0.29402  67.00000 16.992 < 2e-16 ***
isomorphicTRUE -0.87140  0.32063  53.00000 -2.718  0.00886 ** 
session_c      -0.55866  0.08284  55.00000 -6.744 9.96e-09 *** 
I(session_c^2)  0.21058  0.09152 8250.00000  2.301  0.02142 *  
structureCycling  0.36442  0.32052  53.00000  1.137  0.26067    
trial_Index_by_type_z -0.35697  0.04444 8259.00000 -8.033 1.11e-15 *** 
I(trial_Index_by_type_z^2)  0.27053  0.04964 8238.00000  5.450 5.18e-08 *** 
avg_rt_on_trial -0.56729  0.02996 5704.00000 -18.937 < 2e-16 *** 
...
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

No effect on door performance



Error bars represent 95%-confidence intervals

This may not be conscious



Error bars represent 95%-confidence intervals

This may not be conscious

```
Linear mixed model fit by REML
t-tests use Satterthwaite approximations to degrees of freedom ['lmerMod']
Formula: num_steps_needed ~ isomorphic * (correspondence_suspect) + session_c +
Data: es_joined_ns_data %>% filter(trial_type == "fractal")
                                         I(session_c^2) + structure + trial_index_by_type_z + I(trial_index_by_type_z^2) +
REML criterion at convergence: 46675
avg_rt_on_trial + (1 + session_c | subject_id)

Scaled residuals:
    Min      1Q  Median      3Q     Max 
-2.4227 -0.5136 -0.1547  0.2470 14.9688 

Random effects:
Groups   Name        Variance Std.Dev. Corr
subject_id (Intercept) 1.3898  1.1789
           session_c   0.2308  0.4805  0.00
Residual            15.2730  3.9081
Number of obs: 8350, groups: subject_id, 56

Fixed effects:
                Estimate Std. Error      df t value Pr(>|t|)    
(Intercept)      4.99688  0.30253  63.00000 16.517 < 2e-16 ***
isomorphicTRUE  -0.87178  0.34184  51.00000 -2.556  0.0136 *  
correspondence_suspectYes 0.01273  0.23669  51.00000  0.054  0.9573  
session_c        -0.55867  0.08284  55.00000 -6.744 9.95e-09 ***
I(session_c^2)   0.21056  0.09152  8258.00000  2.301  0.0214 *  
structureCycling 0.36663  0.34714  51.00000  1.056  0.2959  
trial_index_by_type_z -0.35696  0.04444  8259.00000 -8.032 1.11e-15 *** 
I(trial_index_by_type_z^2) 0.27053  0.04964  8238.00000  5.450 5.19e-08 *** 
avg_rt_on_trial  -0.56724  0.02999  5753.00000 -18.914 < 2e-16 *** 
isomorphicTRUE:correspondence_suspectYes -0.01833  0.33967  51.00000 -0.054  0.9572  
...
Signif. codes:  0 '****' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

This may not be conscious

- Consciousness is tricky to assess [Newell and Shanks, 2014].

This may not be conscious

- Consciousness is tricky to assess [Newell and Shanks, 2014].
 - Can be altered by the exact wording of question or type of probe.

This may not be conscious

- Consciousness is tricky to assess [Newell and Shanks, 2014].
 - Can be altered by the exact wording of question or type of probe.
- For what it's worth, regressors other than suspecting correspondence give similar results, e.g.:

This may not be conscious

- Consciousness is tricky to assess [Newell and Shanks, 2014].
 - Can be altered by the exact wording of question or type of probe.
- For what it's worth, regressors other than suspecting correspondence give similar results, e.g.:
 - Likert ratings of perception that one task was helpful for the other.

This may not be conscious

- Consciousness is tricky to assess [Newell and Shanks, 2014].
 - Can be altered by the exact wording of question or type of probe.
- For what it's worth, regressors other than suspecting correspondence give similar results, e.g.:
 - Likert ratings of perception that one task was helpful for the other.
 - Likert ratings of similarity between the experiments.

This may not be conscious

- Consciousness is tricky to assess [Newell and Shanks, 2014].
 - Can be altered by the exact wording of question or type of probe.
- For what it's worth, regressors other than suspecting correspondence give similar results, e.g.:
 - Likert ratings of perception that one task was helpful for the other.
 - Likert ratings of similarity between the experiments.
 - Binary split of reports of when they noticed any relationship between the experiments (ever noticed/never noticed).

Evidence of transfer to second task.

Evidence of transfer to second task.

May not require consciousness.

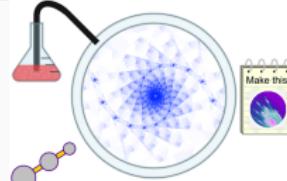
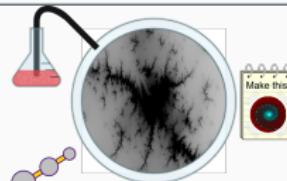
Results: Policies

Policies

- A number of my remaining analyses rely on the idea of a *policy* from reinforcement learning.

Policies

- A number of my remaining analyses rely on the idea of a *policy* from reinforcement learning.
- A policy is a function that maps states to action probabilities:

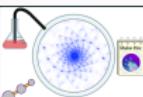
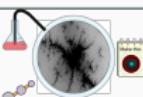
	$P(\text{Acid})$	$P(\text{Ray})$
	0.75	0.25
	0.5	0.5

Policy alignment

- How similar is participants behavior between the tasks?

Policy alignment

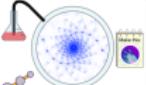
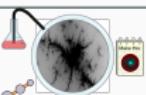
- How similar is participants behavior between the tasks?
- We'll quantify this by looking at similarity between their policies.

	$P(\text{Acid})$	$P(\text{Ray})$
	0.75	0.25
	0.5	0.5
:	:	:

	$P(\text{Right})$	$P(\text{Left})$
	0.5	0.5
	0.75	0.25
:	:	:

Policy alignment

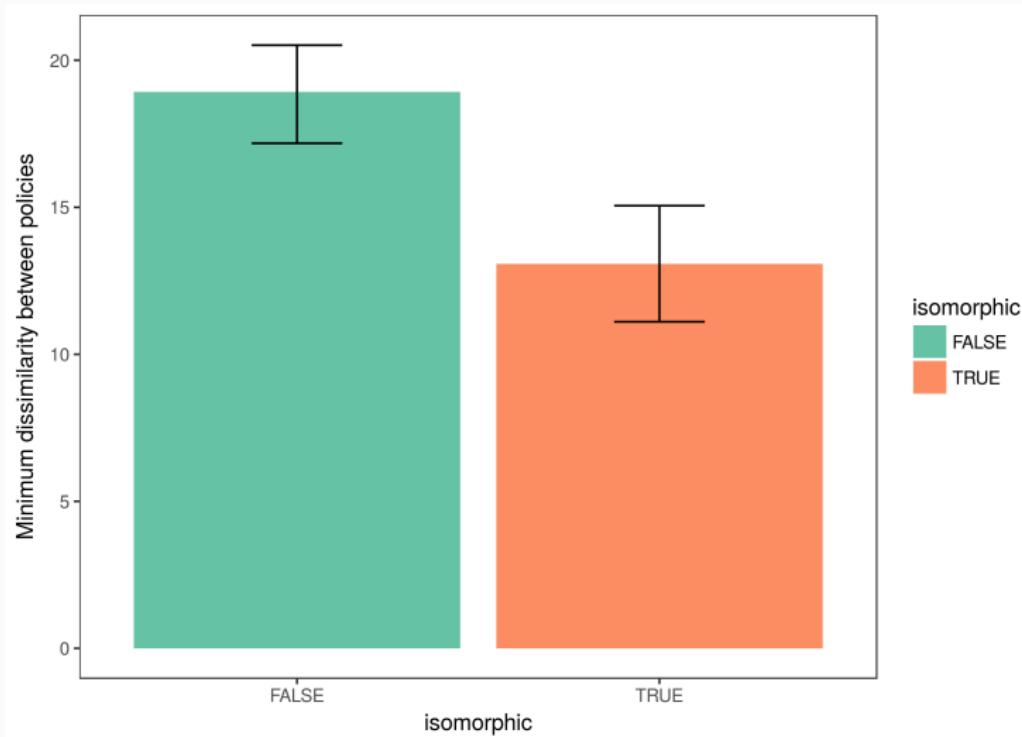
- How similar is participants behavior between the tasks?
- We'll quantify this by looking at similarity between their policies.

	$P(\text{Acid})$	$P(\text{Ray})$
	0.75	0.25
	0.5	0.5
⋮	⋮	⋮

	$P(\text{Right})$	$P(\text{Left})$
	0.5	0.5
	0.75	0.25
⋮	⋮	⋮

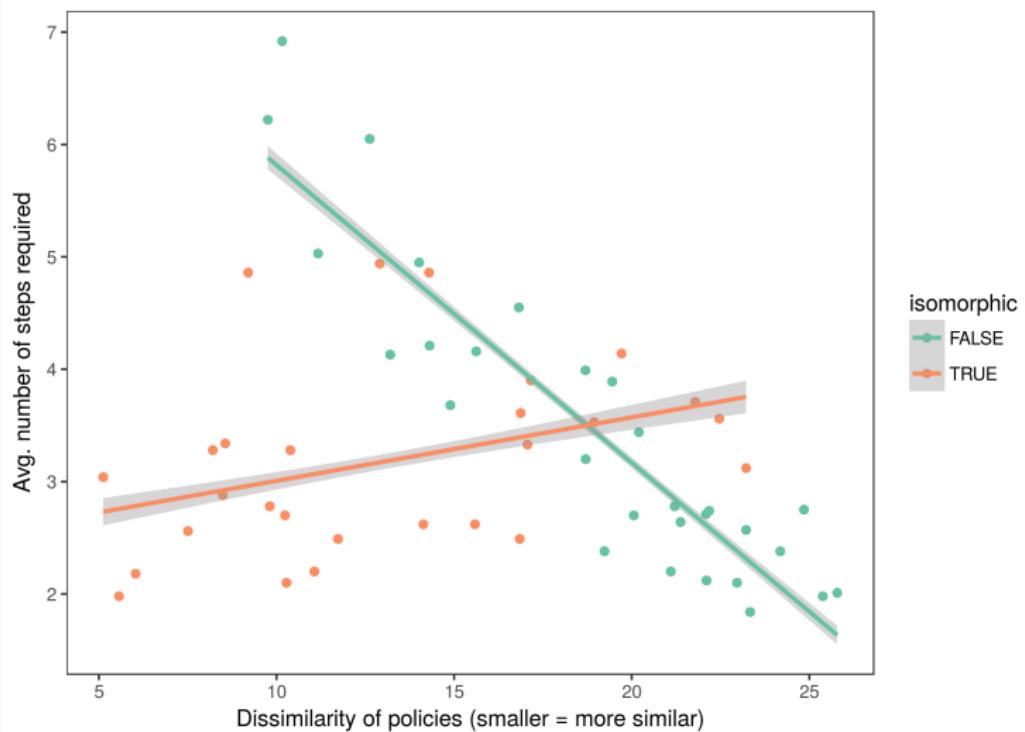
- We'll consider all the structure-preserving mappings between the doors and fractal policies, and see how well the participants' policies align across tasks.

Policy alignment is greater in isomorphic condition



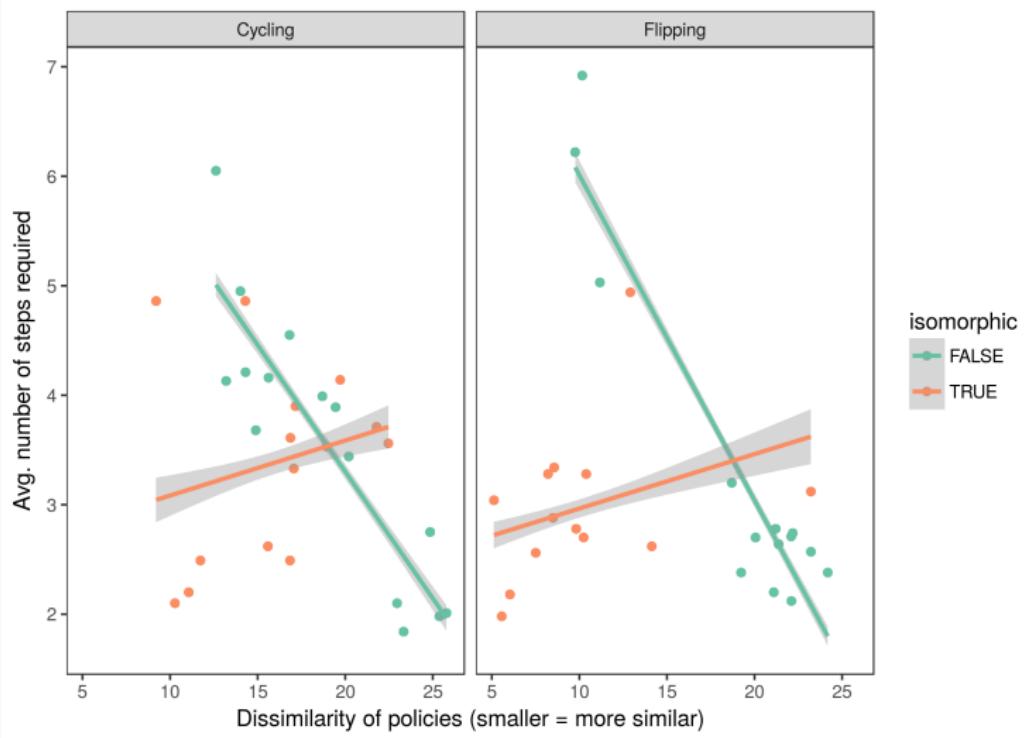
Error bars represent bootstrap 95%-confidence intervals

Policy alignment is related to performance



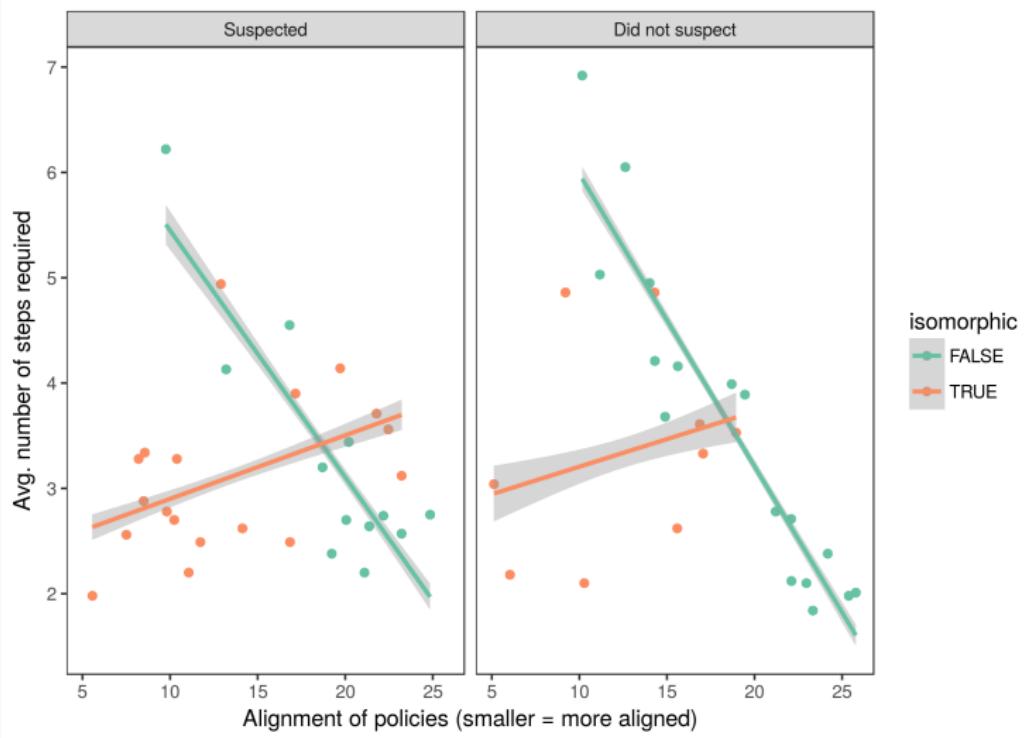
Error bars represent 95%-confidence intervals

Policy alignment is related to performance



Error bars represent 95%-confidence intervals

Not a consciousness effect?



Error bars represent 95%-confidence intervals

Policy alignment strongly affects performance.

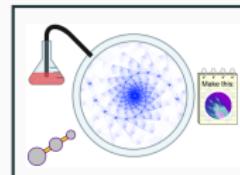
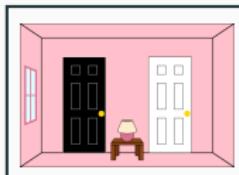
Policy alignment strongly affects performance.

**Some subjects may be “trying” to transfer in
the non-isomorphic condition, and actually be
harmed by it!**

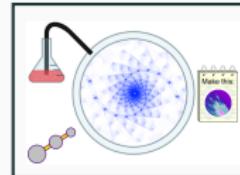
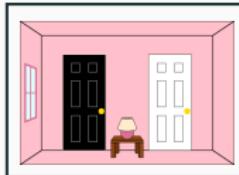
Results: Explicit knowledge

Experiment design

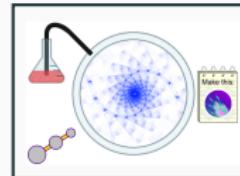
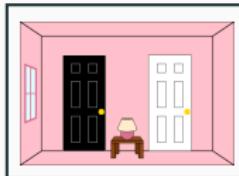
Day 1



Day 2

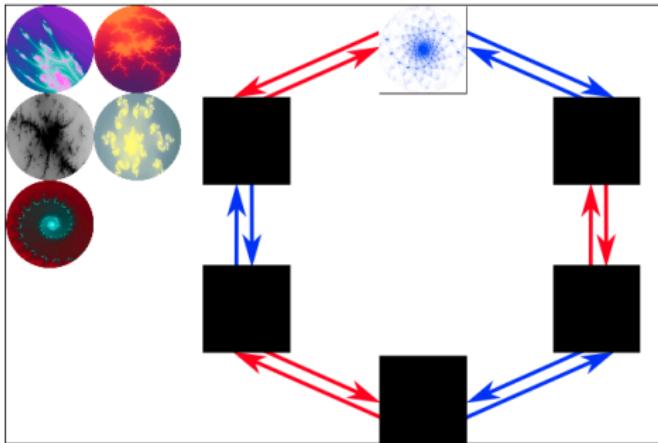


Day 3



Note: we have much less power to detect these effects, because they're generally based off of one answer per question per subject in only the final session.

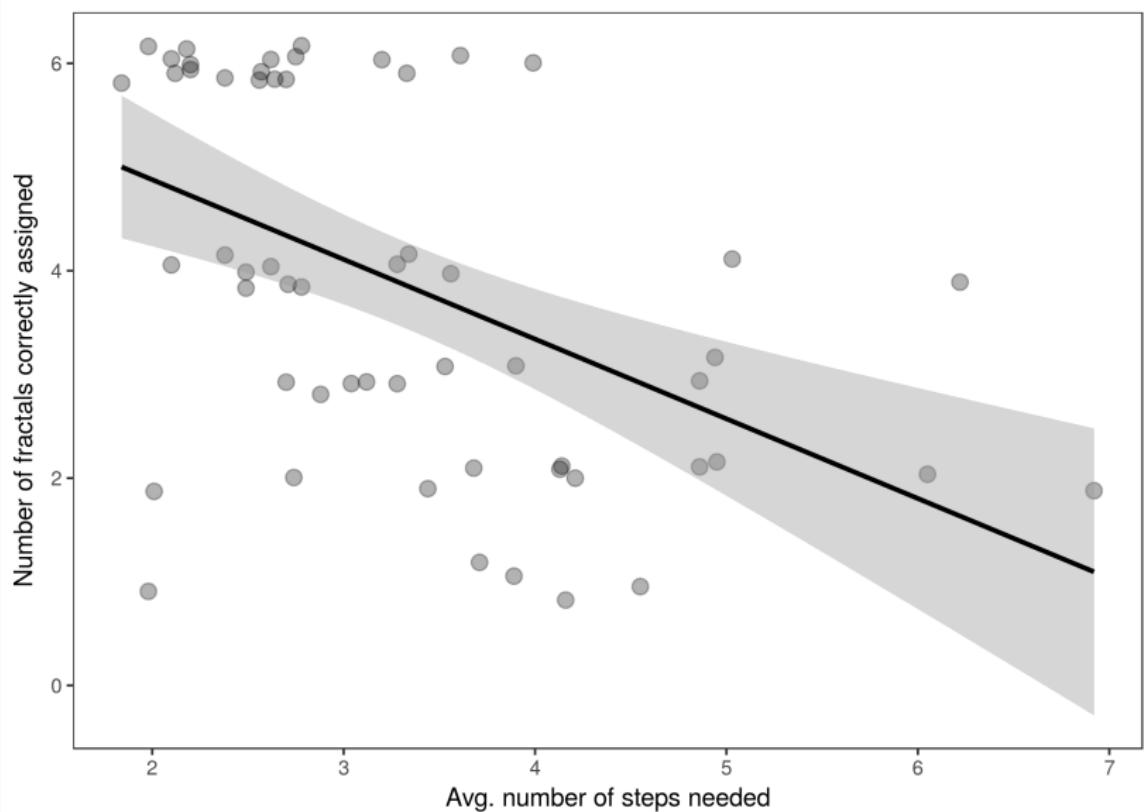
Better performance on task predicts better explicit answers



The fractal relationships in your experiment obeyed the structure above (black squares = fractals, red arrows = acid, blue arrows = gamma ray). Drag the fractals onto the black squares that you think they map onto (one has been placed to get you started).

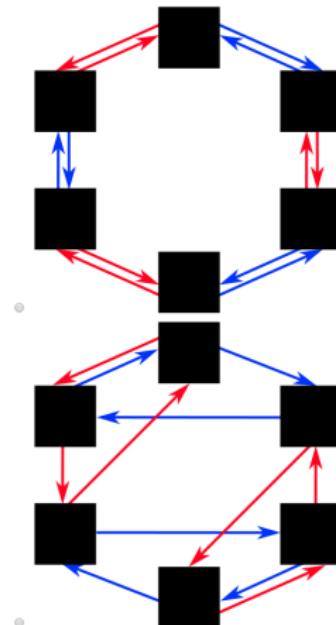
Submit answers

Better performance on task predicts better explicit answers



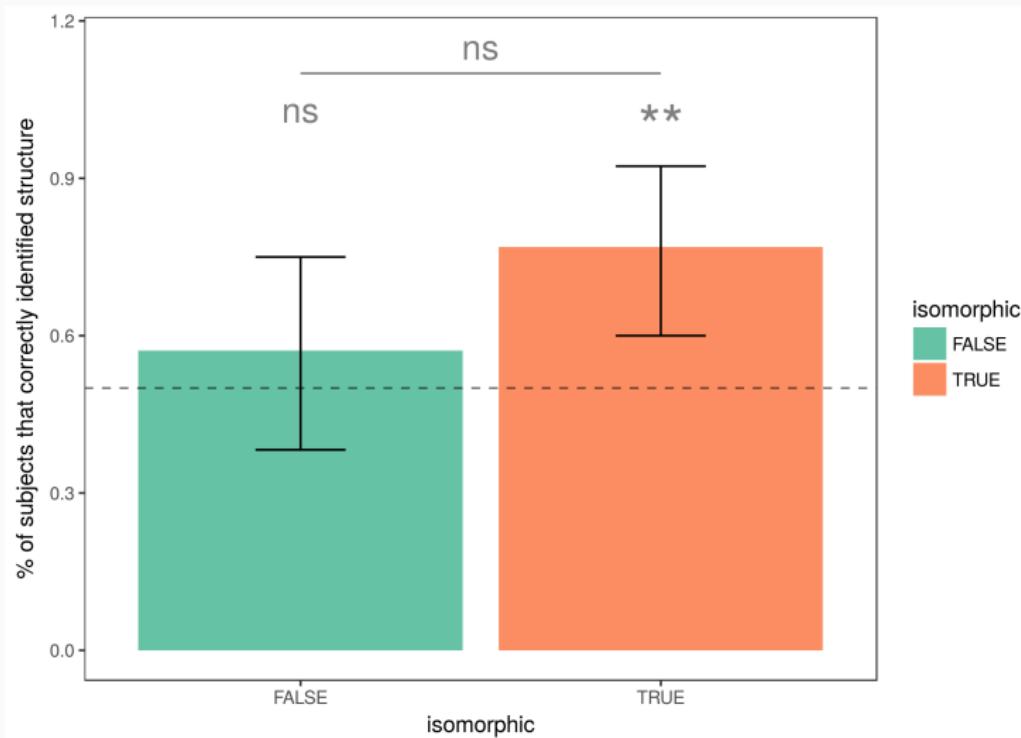
Isomorphism may influence within-task abstraction

The fractal relationships in your experiment obeyed one of the structures below, where the black squares correspond to fractals, the red arrows correspond to either the gamma ray or the acid, and the blue arrows correspond to the other. Select the structure that you think you had.



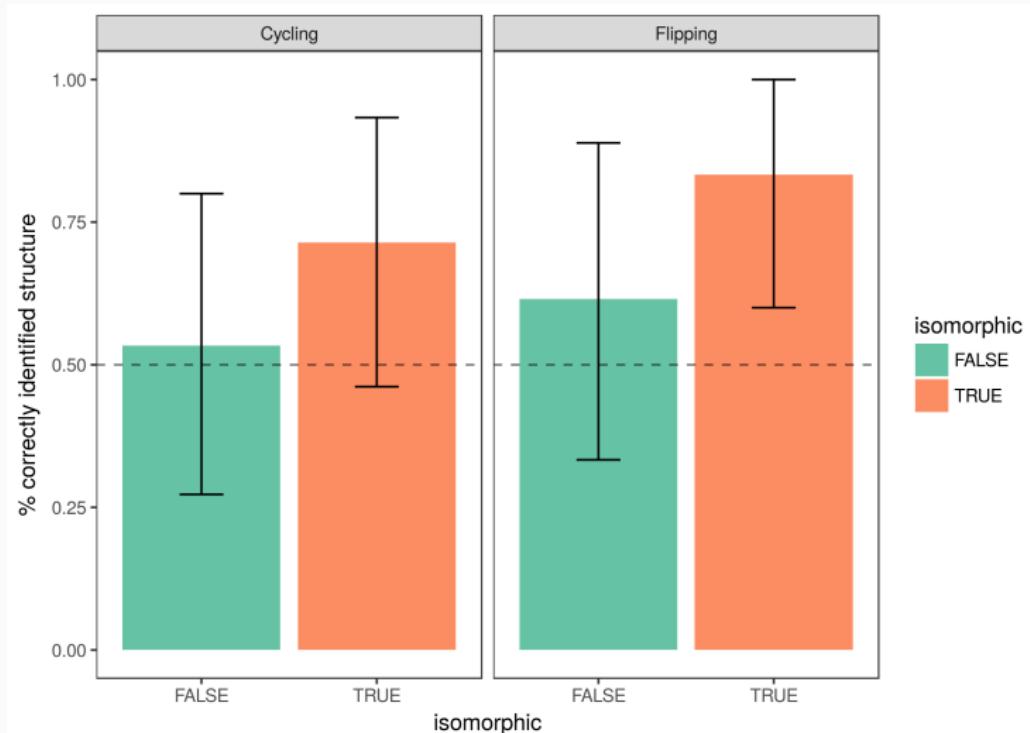
Submit Answers

Isomorphism may influence within-task abstraction



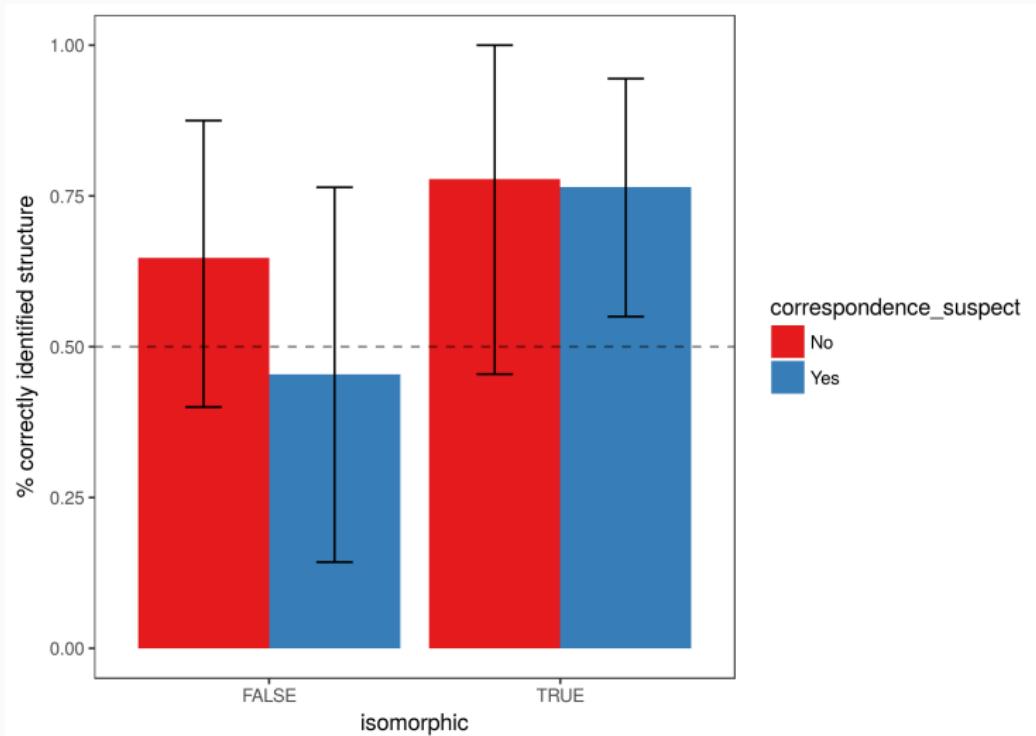
Error bars represent bootstrap 95%-confidence intervals

Isomorphism may influence within-task abstraction



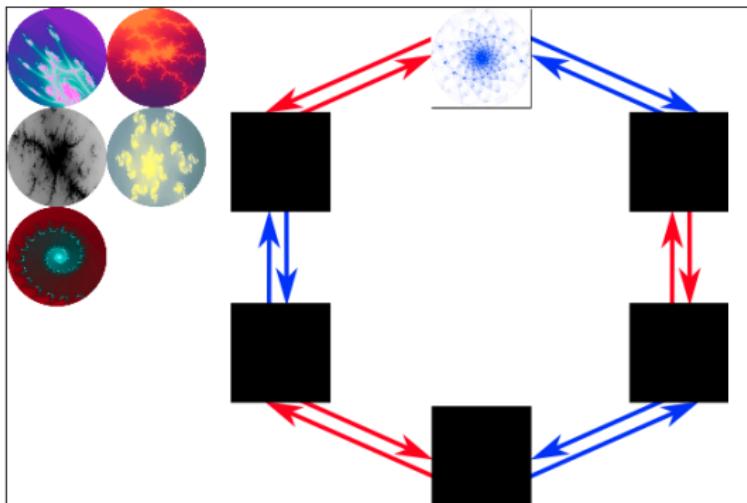
Error bars represent bootstrap 95%-confidence intervals

Isomorphism may influence within-task abstraction



Error bars represent bootstrap 95%-confidence intervals

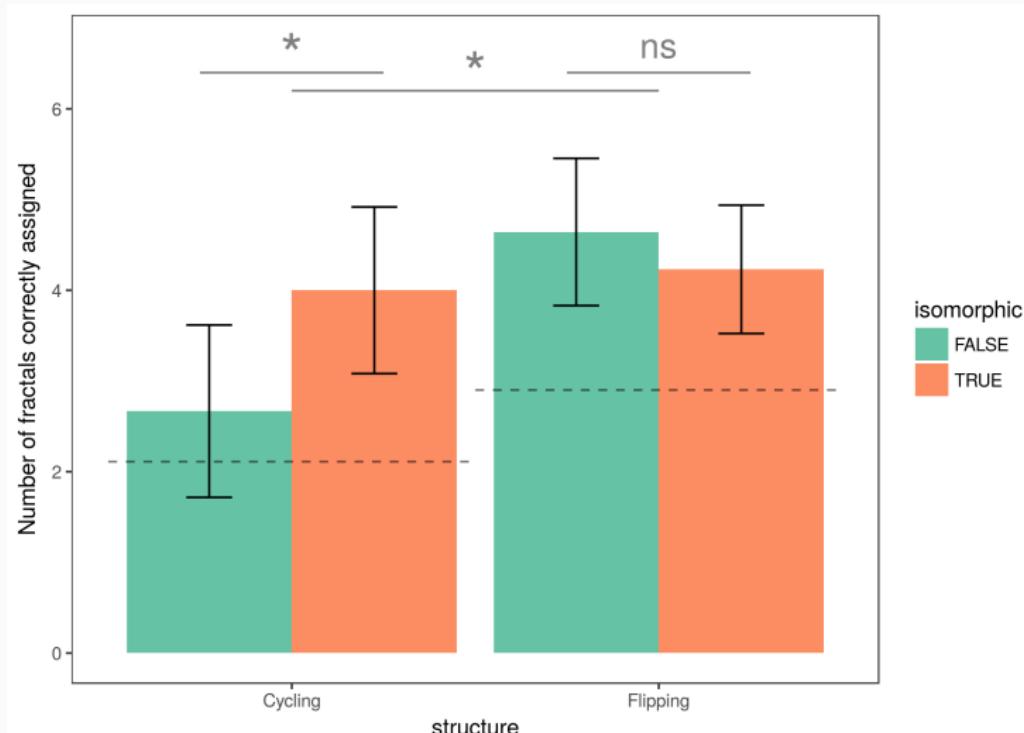
Isomorphism may influence within-task abstraction



The fractal relationships in your experiment obeyed the structure above (black squares = fractals, red arrows = acid, blue arrows = gamma ray). Drag the fractals onto the black squares that you think they map onto (one has been placed to get you started).

[Submit answers](#)

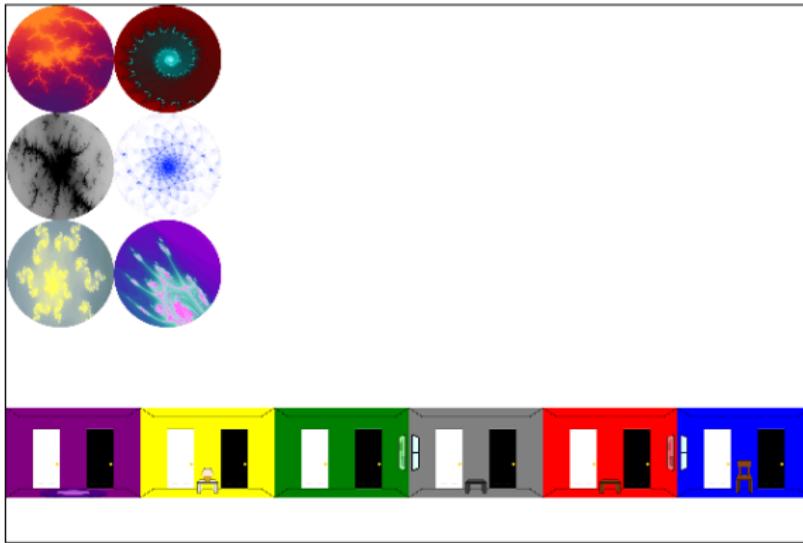
Isomorphism may influence within-task abstraction



Error bars represent bootstrap 95%-confidence intervals

Results: Explicit knowledge about relationship

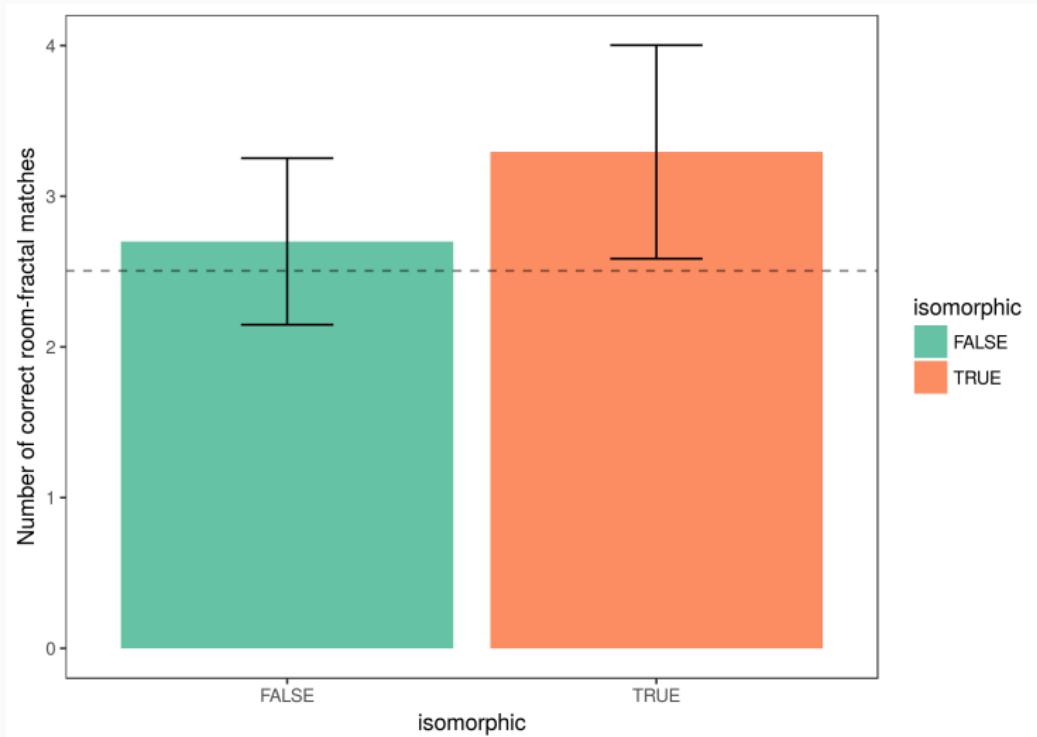
Subjects can explicitly identify analogy better than chance



Assuming the experiments were teaching you the same structure, each room in the navigation experiment corresponded to a fractal in the visual patterns experiment. Drag the fractals onto the rooms you think they corresponded to.

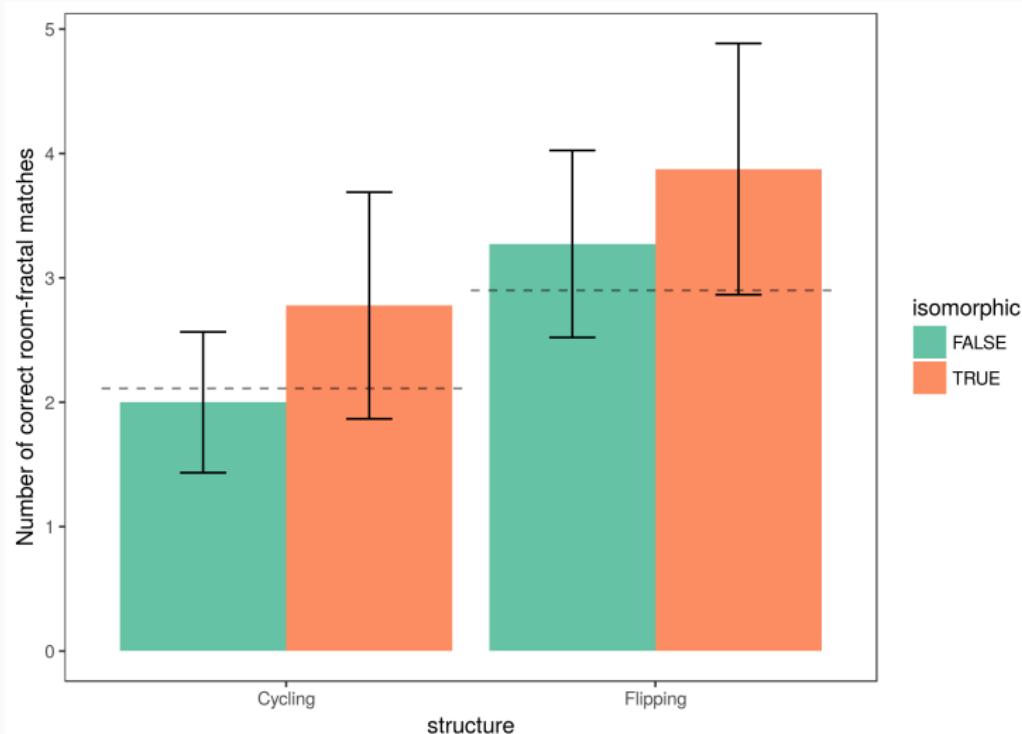
[Submit answers](#)

Subjects can explicitly identify analogy better than chance



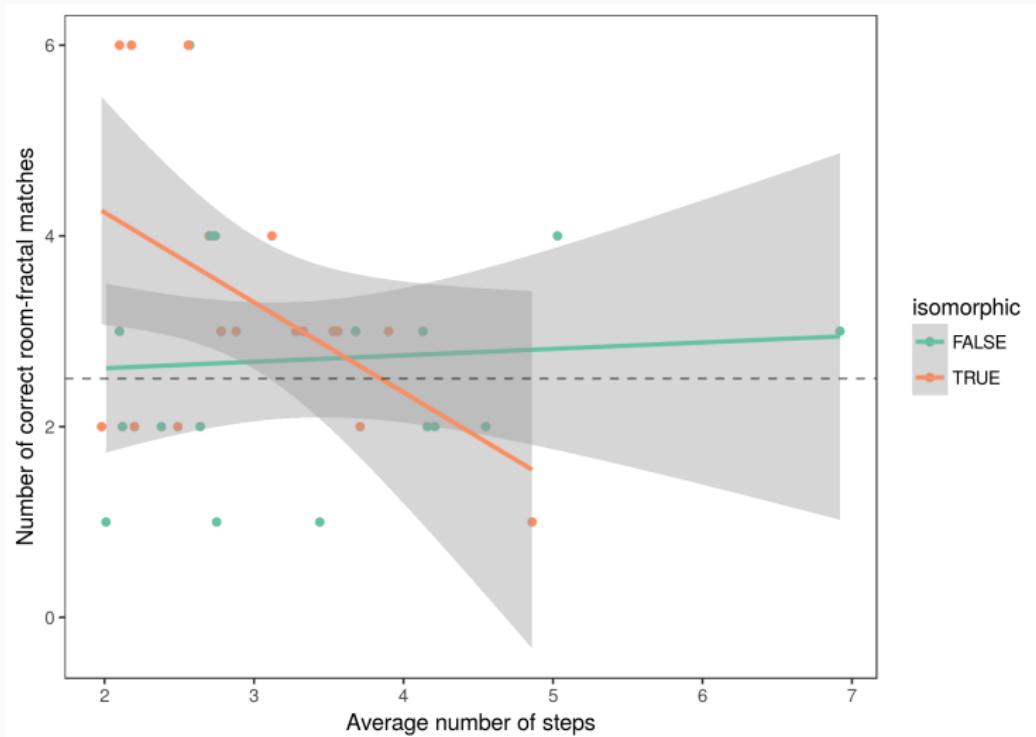
Error bars represent parametric 95%-confidence intervals

Subjects can explicitly identify analogy better than chance

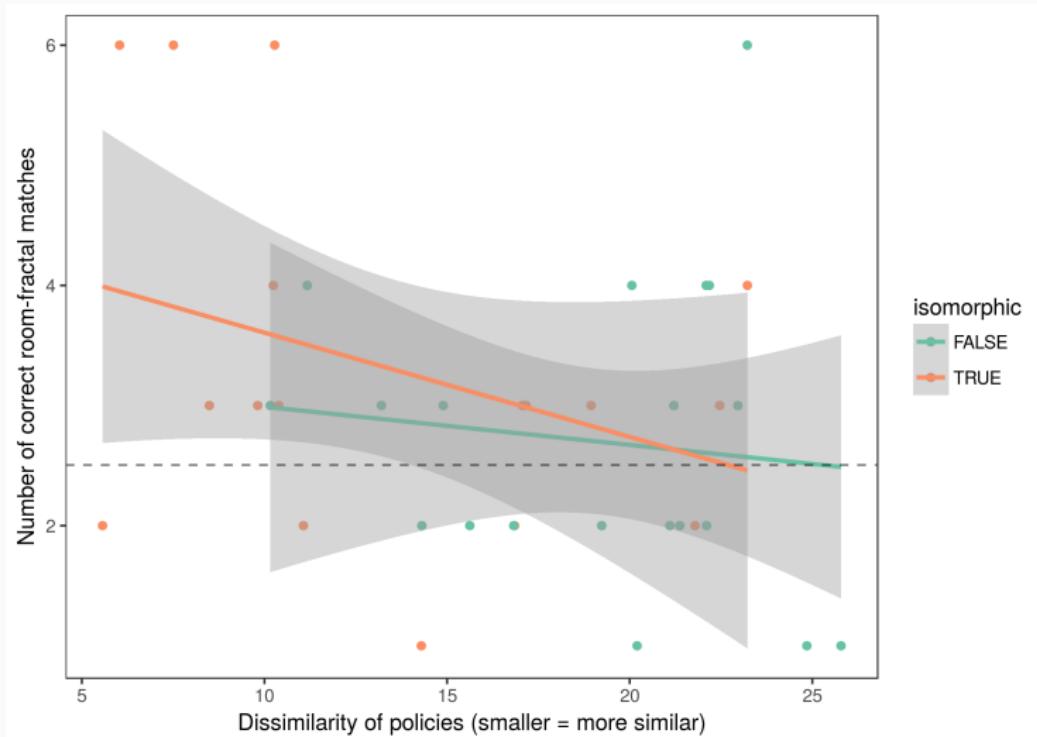


Error bars represent parametric 95%-confidence intervals

Only weakly related to performance and policy alignment

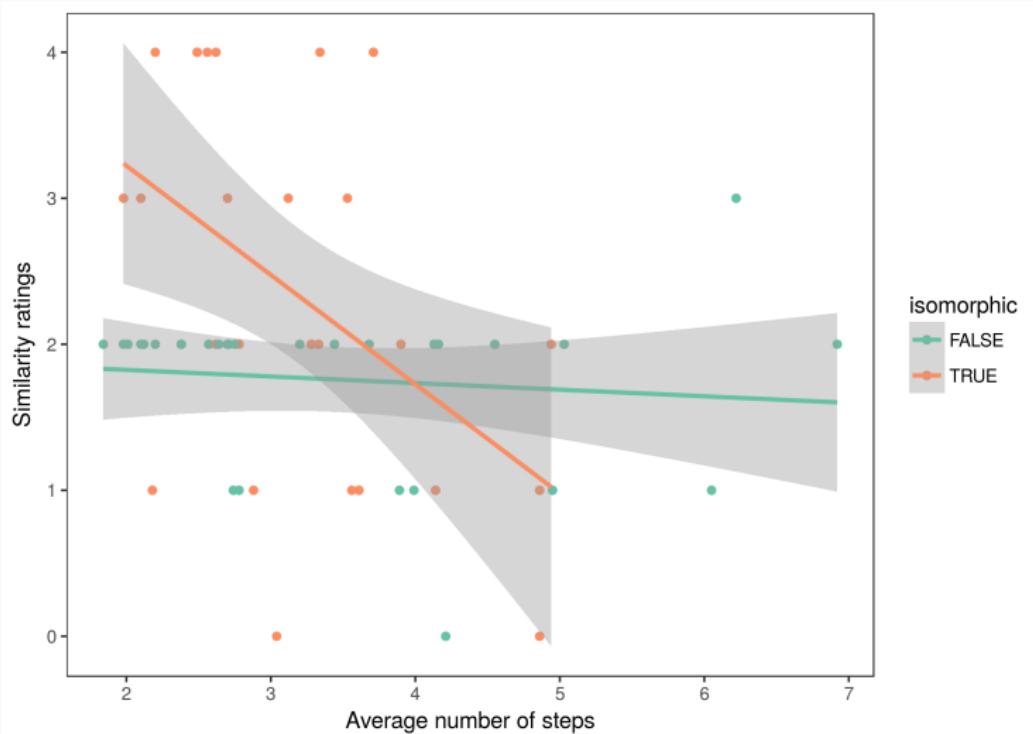


Only weakly related to performance and policy alignment



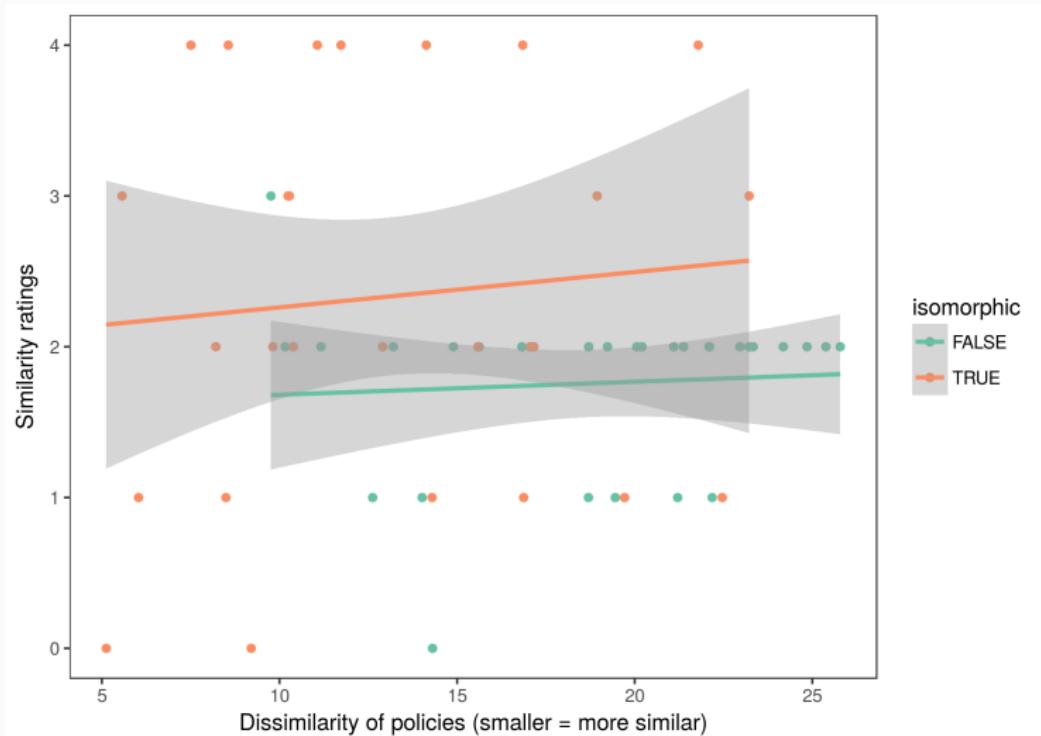
Error bars represent parametric 95%-confidence intervals

Similarity ratings



Error bars represent parametric 95%-confidence intervals

Similarity ratings



Error bars represent parametric 95%-confidence intervals

Slides TODO: but policy alignment does not seem to predict anything explicit very strongly.

Conclusions

- We see evidence of slow transfer between tasks.

Conclusions

- We see evidence of slow transfer between tasks.
- This slow transfer may be independent of consciousness.

Conclusions

- We see evidence of slow transfer between tasks.
- This slow transfer may be independent of consciousness.
- This slow transfer of knowledge affects within-task explicit knowledge.

Conclusions

- We see evidence of slow transfer between tasks.
- This slow transfer may be independent of consciousness.
- This slow transfer of knowledge affects within-task explicit knowledge.
- However, the processes for implicit and explicit mapping between tasks may be at least partially dissociable.

Next steps & possible future directions

- See whether these results hold/replicate

Next steps & possible future directions

- See whether these results hold/replicate
- Verify that direction of transfer is caused by order and not e.g. grounding

Next steps & possible future directions

- See whether these results hold/replicate
- Verify that direction of transfer is caused by order and not e.g. grounding
- Distractor tasks between

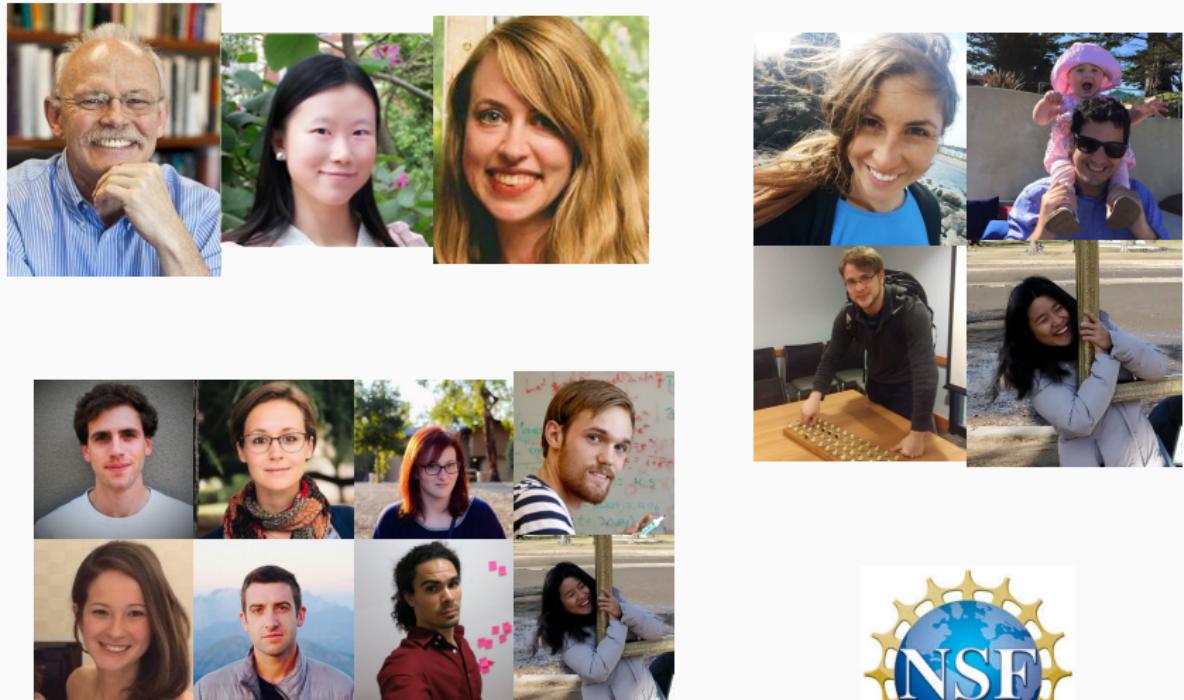
Next steps & possible future directions

- See whether these results hold/replicate
- Verify that direction of transfer is caused by order and not e.g. grounding
- Distractor tasks between
- Integrating abstractions (either taught or interrogated) earlier on one or both tasks

Next steps & possible future directions

- See whether these results hold/replicate
- Verify that direction of transfer is caused by order and not e.g. grounding
- Distractor tasks between
- Integrating abstractions (either taught or interrogated) earlier on one or both tasks
- Role of sleep in abstraction

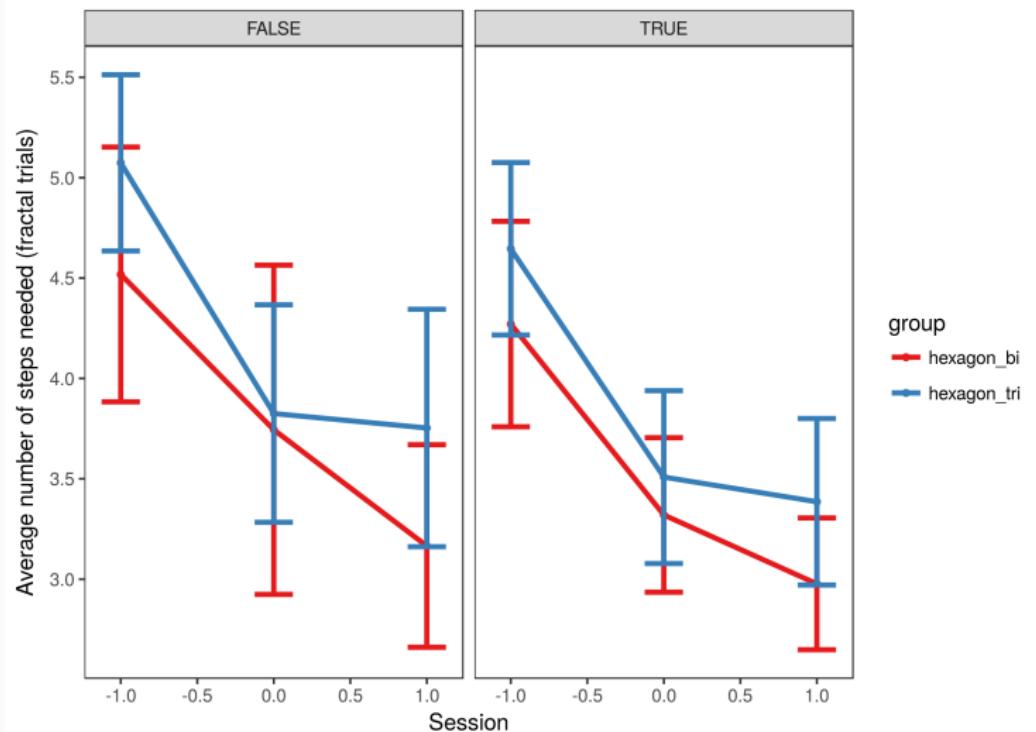
Acknowledgements



References

- Douglas K. Detterman. The Case for the Prosecution: Transfer as an Epiphenomenon. In *Transfer on Trial: Intelligence, Cognition, and Instruction*, pages 1–24. 1993.
- Dedre Gentner. Why We're So Smart. In *Language in mind: Advances in the study of language and thought.*, pages 195–235. 2003.
- Mary L Gick and Keith J. Holyoak. Analogical Problem Solving. *Cognitive P*, 12:306–355, 1980.
- Steven S. Hansen, Andrew Lampinen, Gaurav Suri, and James L. McClelland. Building on prior knowledge without building it in. *Behavioral and Brain Sciences*, 40, 2017.
- Andrew Lampinen, Shaw Hsu, and James L McClelland. Analogies Emerge from Learning Dynamics in Neural Networks. *Proceedings of the 39th Annual Conference of the Cognitive Science Society*, pages 2512–2517, 2017.
- Ben R. Newell and David R. Shanks. Unconscious influences on decision making: A critical review. *Behavioral and Brain Sciences*, 38(01):1–19, 2014. ISSN 0140-525X. doi: 10.1017/S0140525X12003214. URL http://www.journals.cambridge.org/abstract_S0140525X12003214.

Flipping is easier



Error bars represent 95%-confidence intervals

