Introduction to Biostatistics & Descriptive Statistics

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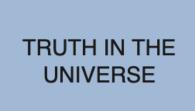
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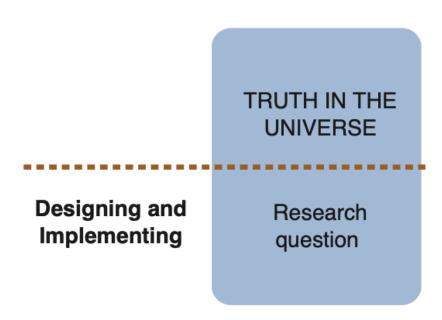
Outline

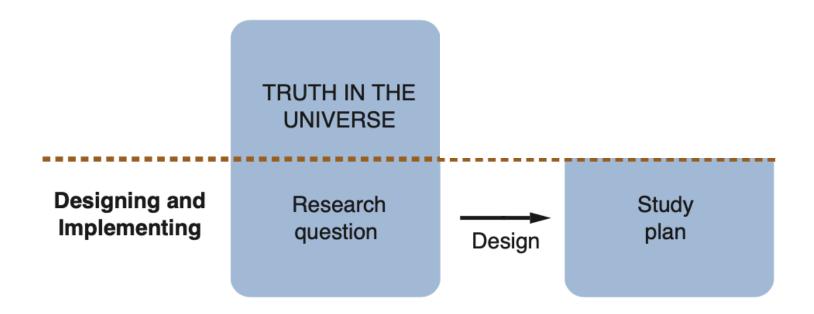
- 1. Introduction to biostatistics
- 2. Descriptive statistics
- 3. Making effective graphs and tables

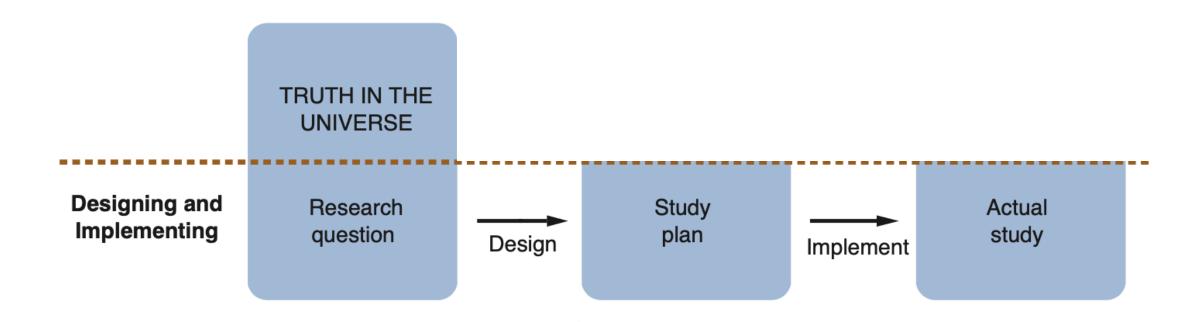
These slides were based on learning materials originally developed by Dr Marcel Wolbers, Prof Ronald Geskus and other members of the Biostatistics group at OUCRU

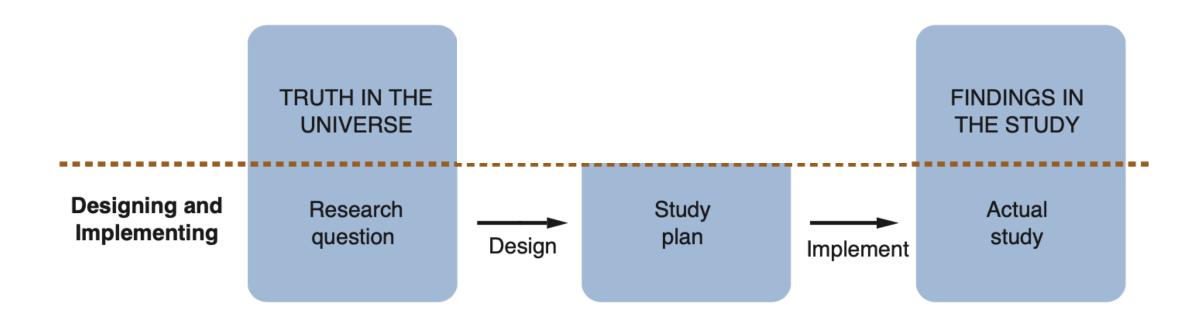
Introduction to biostatistics

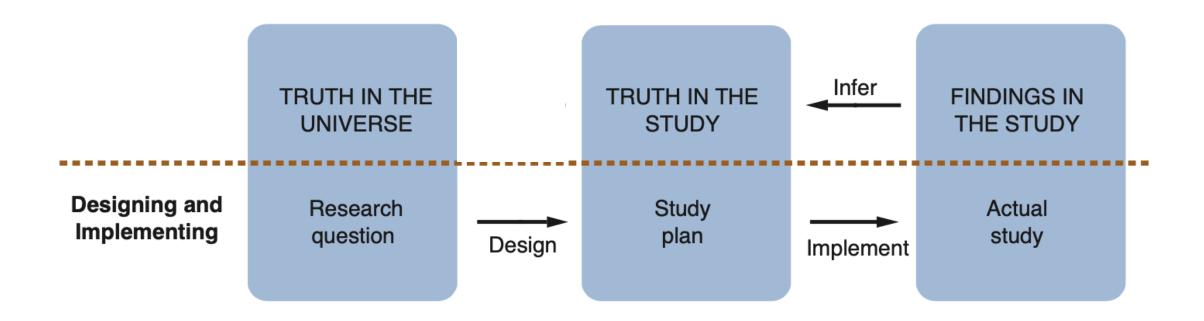


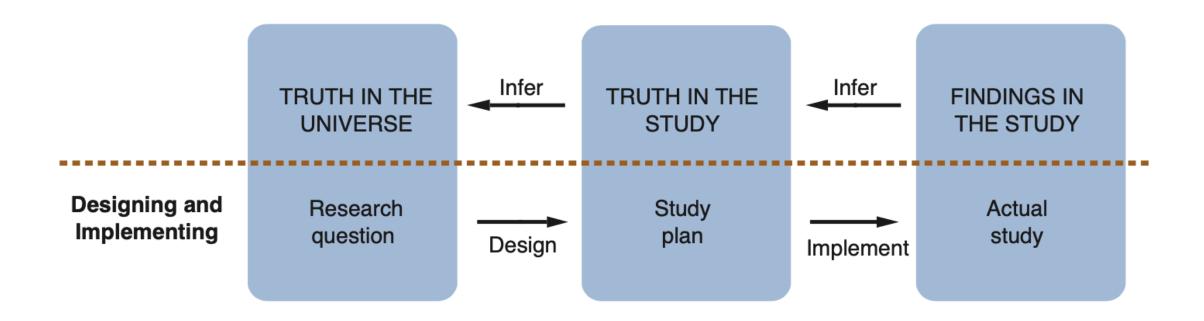


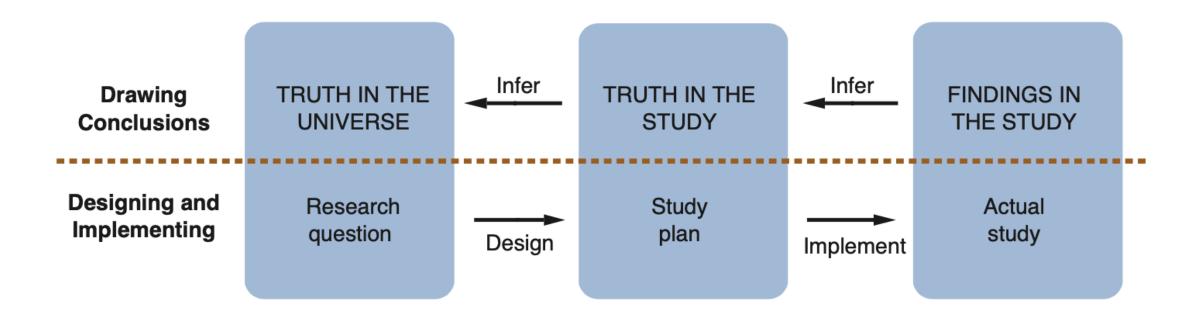


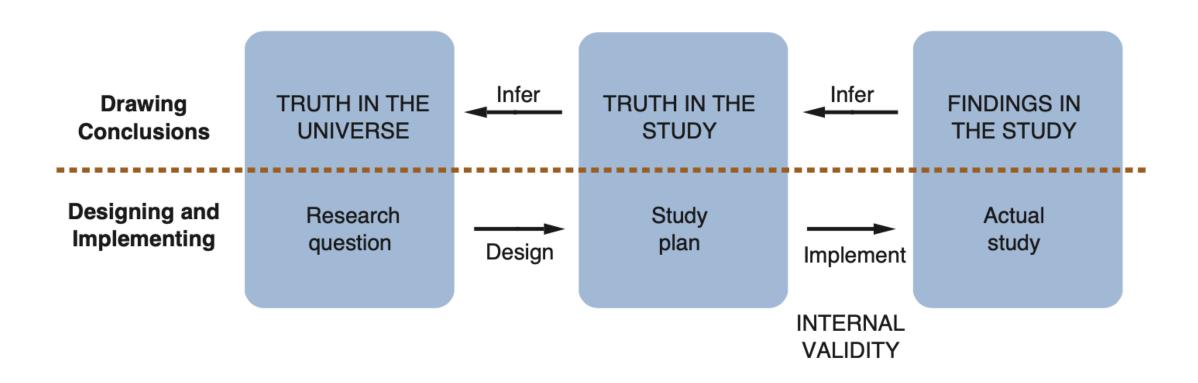


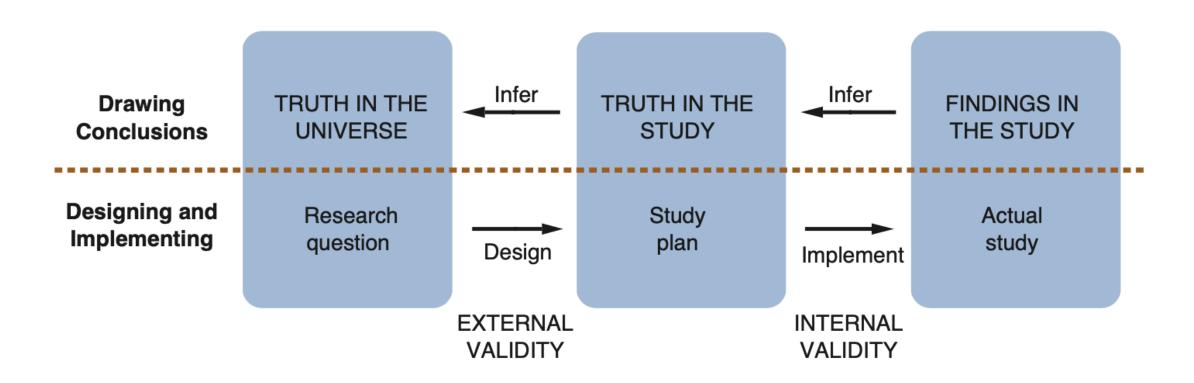






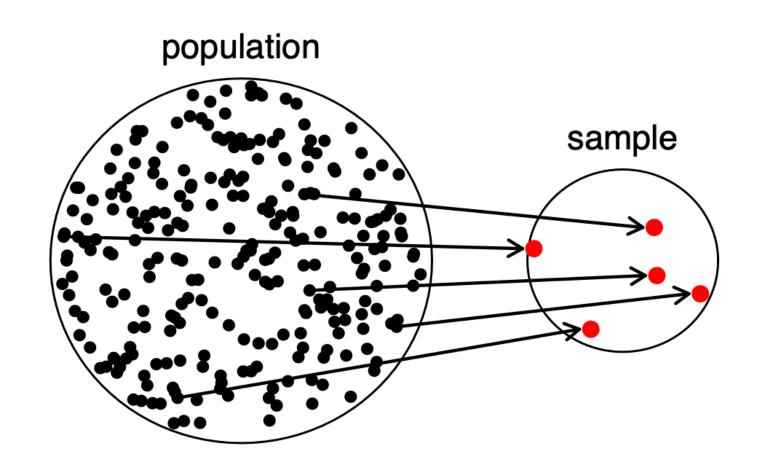


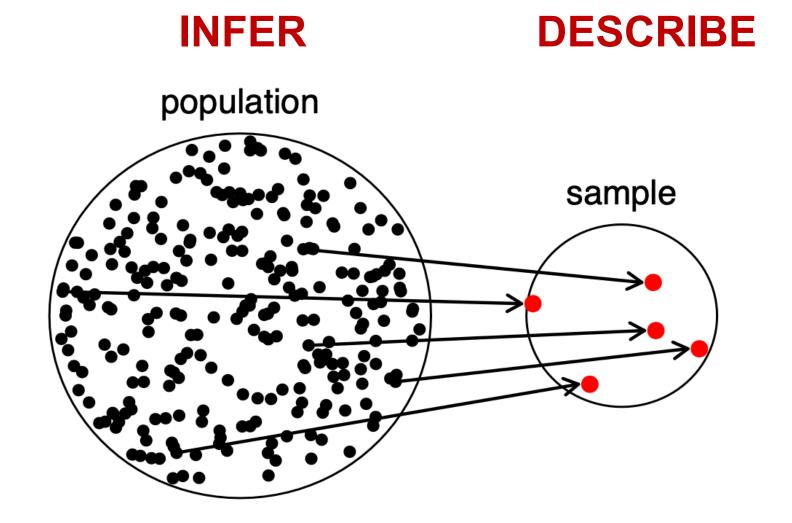




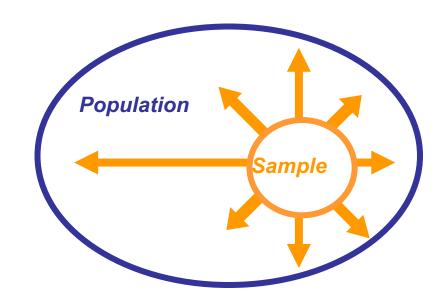
Data as sample from population

Data as sample from population



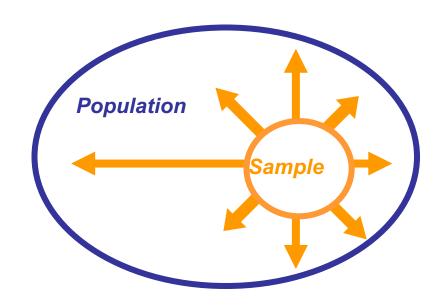


• Descriptive statistics & Inferential statistics



Descriptive statistics & Inferential statistics

- Descriptive statistics
 - Description/ exploration of dataset ... and beyond
 - First step in data analysis



Descriptive statistics & Inferential statistics

Population Sample

- Descriptive statistics
 - Description/ exploration of dataset ... and beyond
 - First step in data analysis
- Inferential statistics
 - Draw conclusions about a population using a sample

Descriptive statistics

Describe data from sample

Descriptive statistics

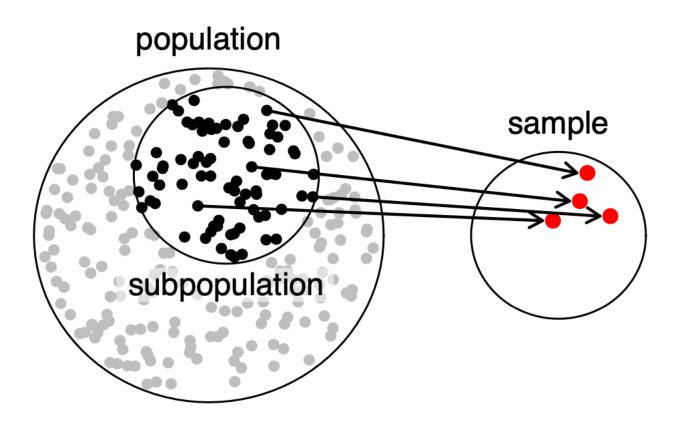
- Describe data from sample
- Use numbers and graphs

Inferential statistics

From sample to population

Inferential statistics

- From sample to population
- But which population???



Data randomly selected from some (much) larger population

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- Representative sample: observations (summary, relations between variables) can be transferred to population

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- Data randomly selected from some (much) larger population
- Representative sample: observations (summary, relations between variables) can be transferred to population
 - Data summaries ≈ population summaries
 - Some uncertainty: only (small) sample from population
 - Result slightly different if study repeated (new sample)

Patients with dengue shock treated at HTD during 2014-17

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- Which population do the data represent?

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 - all patients with dengue shock treated at HTD, in past and (near) future
 - all patients with dengue shock in Viet Nam all patients with dengue shock

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 Always ask yourself the question which population the sample represents

Inferential statistics What do we want to say about the population?

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 - Does dexamethasone decrease risk of dying?
 - Role of HIV coinfection in TBM disease process?
 - Exploration
 - What are the risk factors for mortality in TBM patients?

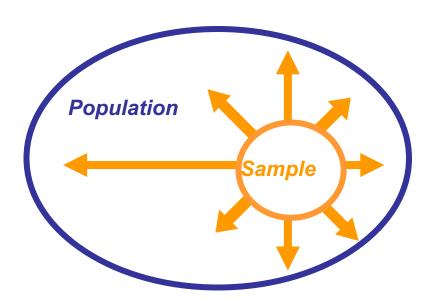
Summary

Summary

- Biostatistics
 - The development and application of statistical methods to a wide range of topics in biology and medicine

Summary

- Biostatistics
 - The development and application of statistical methods to a wide range of topics in biology and medicine
- Two main branches
 - Descriptive statistics
 - Inferential statistics



Descriptive statistics

• Study: sample from population

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Study: sample from population

Dataset: contains observations from a study

 Observation: values of variables that are measured on a unit (patients, animals, farms) at one specific time

Variable: characteristic that may vary over units

Data structure

Data structure

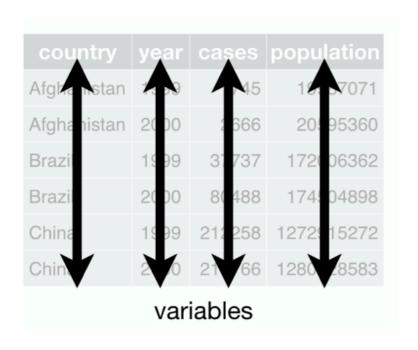
 80% of analysis time spent on data cleaning and preparation, especially when data are "messy"

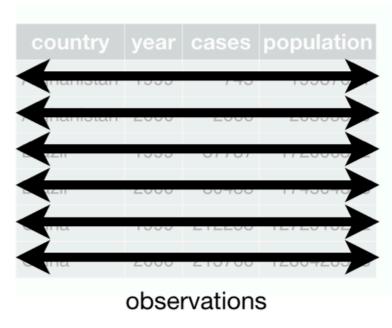
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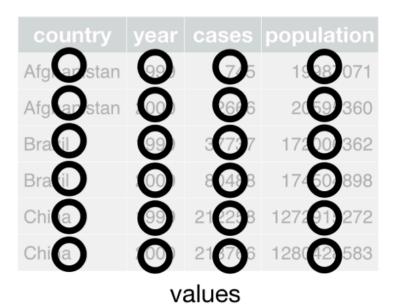
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- "Tidy" data: link structure with semantics
 - Each observation forms a row
 - Each variable forms a column
 - One table for each type of observations
 - If you have multiple tables, they should include a column in the table that allows them to be linked

Tidy data







Tidy data: example

studyno	Fluid	age	sex	hct1	plat1	hospdays	clinical_overload
400	Dextran	9	male	42	80000	4	no
401	Dextran	13	female	48	100000	4	no
402	Starch	10	female	50	47000	4	no
407	Starch	8	male	40	NA	5	no
410	Lactate Hartman	6	male	45	28000	6	yes
412	Dextran	10	female	52	33000	10	yes

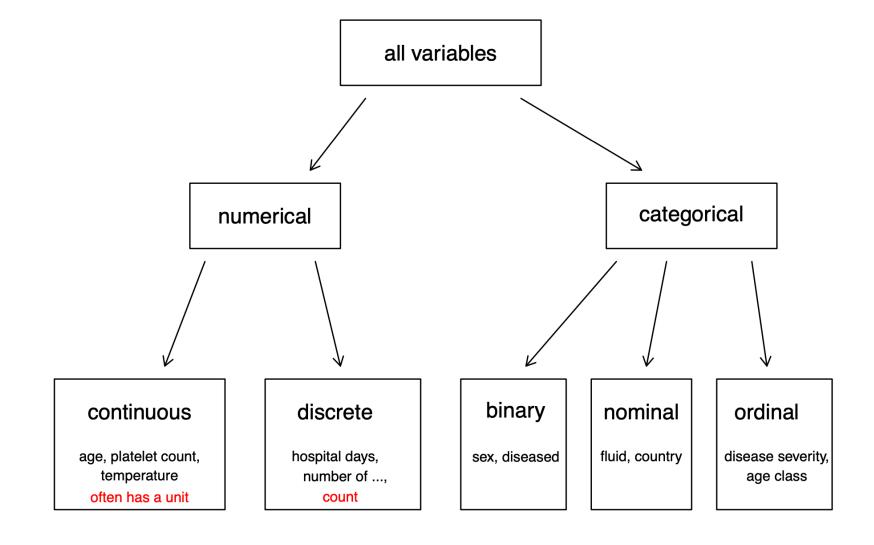
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- Rows: units (subjects, patients at a single time point)
- Columns: variables (outcome, response; covariates, covariables, predictors)
- Cells: values

Types of variables

Types of variables



Types of variables

- 1) Categorical (binary, nominal, ordinal) and
- 2) Numeric (count, continuous):

Binary / Dichotomous - 2 levels: sex, diseased

Nominal – more than 2 levels: fluid, country

Ordinal – ordered levels: severity of disease, disability score, age class

Count – integer: number of ..., calendar year, age year, hospital days

Continuous –often has a unit: temperature, platelet count, age

Quiz: Types of variables in this table?

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- Binary: sex, clinical_overload
- Nominal: Fluid, studyno
- Count: hospdays, age (if rounded, "life years" without unit)
- Continuous: age, hct1, plat1

- Categorical variables often coded numerically
 - e.g. 1=male, 2=female
 - 1=Vietnam, 2=Thailand, 3=Laos
- BUT: This does not make them numerical!

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 Remember during the analyses (or better code them as character from the start)

- Categorical variables often coded numerically
 - e.g. 1=male, 2=female
 - 1=Vietnam, 2=Thailand, 3=Laos
- BUT: This does not make them numerical!
- Remember during the analyses (or better code them as character from the start)
- Missing data
 - use special code; NA ("not available") in R
 - always report amount of missingness per variable
 - usually excluded in analysis (but may introduce bias)

Write on a sheet of paper: 20 numbers from 0 to 9

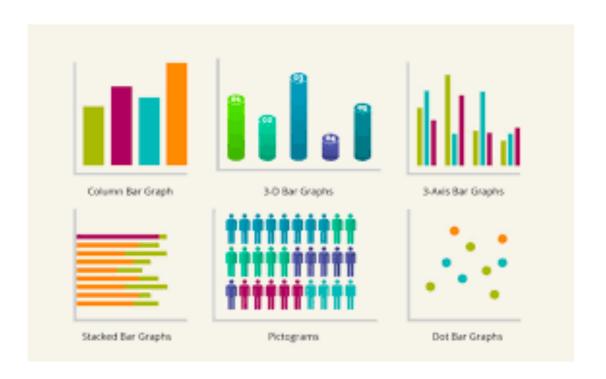
- Write on a sheet of paper: 20 numbers from 0 to 9
- Work in pair: verbally describe your numbers to partner

Numerical

Numerical

12345679

Graphical



Numerical summary

Numerical summary

Categorical variables

Numerical summary

- Categorical variables
 - Frequency: how many subjects in each level/category

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 - Frequency: how many subjects in each level/category
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- Numerical variables
 - Location: mean, median
 - Dispersion: standard deviation, quartiles, range

Adding up all values and dividing this sum by the number of values

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 - e.g.: 5 patients age: 20, 22, 25, 63, 75
 - mean age = 205/5 =41 yrs

General formula

$$\overline{x} := \frac{1}{n} \cdot \sum_{i=1}^{n} x_i$$

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 - e.g.: 5 patients age: 20, 22, 25, 63, 75
 - median age = 25 yrs

Location: mean vs. median

Mean

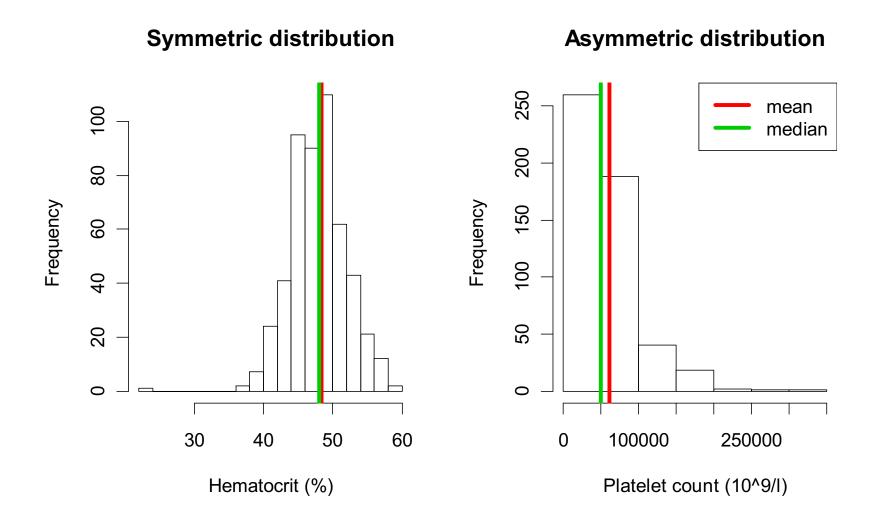
Optimal if data distribution

- ~ symmetric
- No too long tails or outliers
- e.g. data from normal distribution
- Basis of most statistical models and tests

Median

- Close to sample mean if data has symmetric distribution
- Smaller than mean if distribution skewed to the right
- Still meaningful if data has extreme values

Location: mean vs. median - example



Quiz: Sample mean vs. median

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 Length of hospital stay after being admitted to hospital with communityacquired pneumonia

• Distribution is skewed to the right: median ~ 8 days, mean ~ 10 days

Quiz: Sample mean vs. median

- Length of hospital stay after being admitted to hospital with communityacquired pneumonia
- Distribution is skewed to the right: median ~ 8 days, mean ~ 10 days
- Mean or the median more relevant for you if
 - you are a prospective patient?
 - you are a hospital administrator interested in costs?

Dispersion

Dispersion

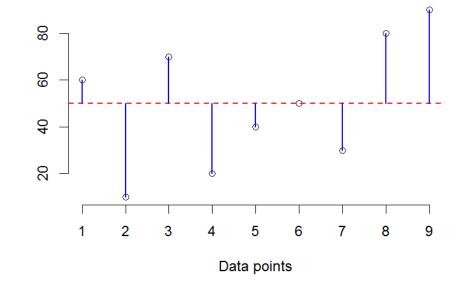
• Age: 60, 10, 70, 20, 40, 50, 30, 80, 90

• Age: 52, 51, 47, 49, 54, 46, 52, 46, 53

Dispersion

• Age: 60, 10, 70, 20, 40, 50, 30, 80, 90

• Age: 52, 51, 47, 49, 54, 46, 52, 46, 53



• Mean 50, but dispersion around mean is different

• Variance: square each deviation and average

variance :=
$$\frac{1}{n-1} \cdot \sum_{i=1}^{n} (x_i - \bar{x})^2$$

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Standard deviation: Square root of variance

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• Rule: If data has approximately normal distribution then

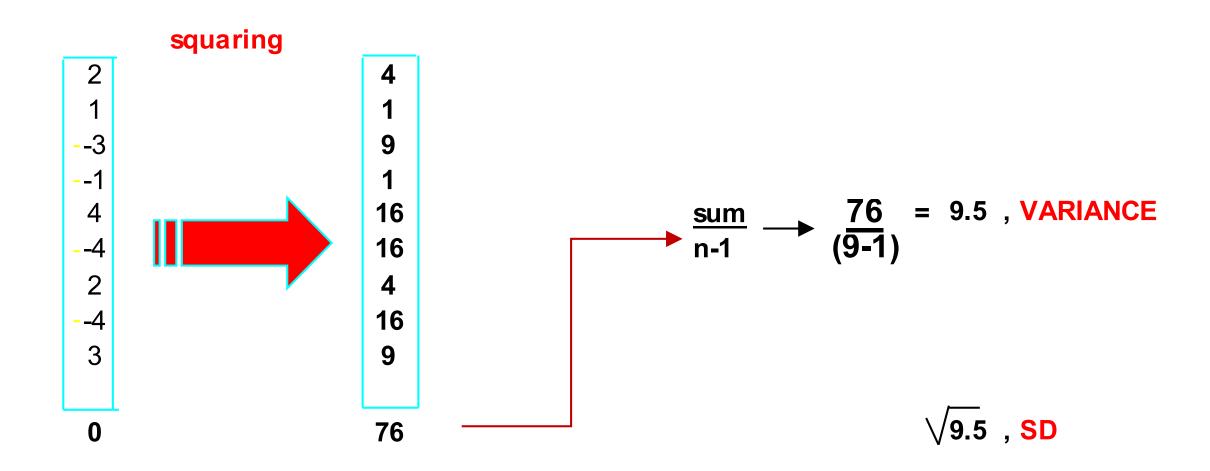
- ~68% of observations lie between $\bar{x} \pm sd$
- ~95% of observation lie between $\bar{x} \pm 2 \cdot sd$

Deviation

• By definition: mean of the deviation is zero

•	value	mean	deviation	
	52	50	2	
	51	50	1	
	47	50	3	The positive differences exactly cancel out the negative differences
	49	50	⁻ -1	
	54	50	4	
	46	50	-4	
	52	50	2	
	46	50	-4	
	53	50	3	
mean	50		0	

Squared deviation



Range: minimum to maximum

Quartiles

Range: minimum to maximum

- Quartiles
 - First quartile q1: cuts off lowest 25% of data

•

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 - Second quartile q2: cuts off lowest 50% of data (median)

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 - First quartile q1: cuts off lowest 25% of data
 - Second quartile q2: cuts off lowest 50% of data (median)
 - Third quartile q3: cuts off lowest 75% of data

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 - First quartile q1: cuts off lowest 25% of data
 - Second quartile q2: cuts off lowest 50% of data (median)
 - Third quartile q3: cuts off lowest 75% of data
 - IQR: q3 q1 (often reported as [q1, q3])

Quiz: medians and IQRs

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Compare distributions (1) and (2) based on their medians and IQRs

Dispersion: comparison

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Standard deviation

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Range

- Useful for very small sample size
- Depends on sample size (increases with sample size)

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IQR, quartiles

- Always interpretable
- Also allows to infer the skewness of the distribution (if median is also given)

Location and dispersion – Recommendations

Location and dispersion – Recommendations

- Report median (quartiles, IQR) for descriptive statistics
 - Reason: Simple and meaningful regardless whether data is symmetric or not
 - Wording: "Median (IQR) hematocrit value was 48 (46 to 51)."
- Mean and sd may be more informative for count data with many ties
 - "median (IQR) = 3 (2-3)" not very informative
- Always give location and dispersion measure

Graphical summary

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Categorical variables

- Pie chart (usually not recommended)
- Bar chart
- Dotplot (often preferred over bar chart)

Graphical summary

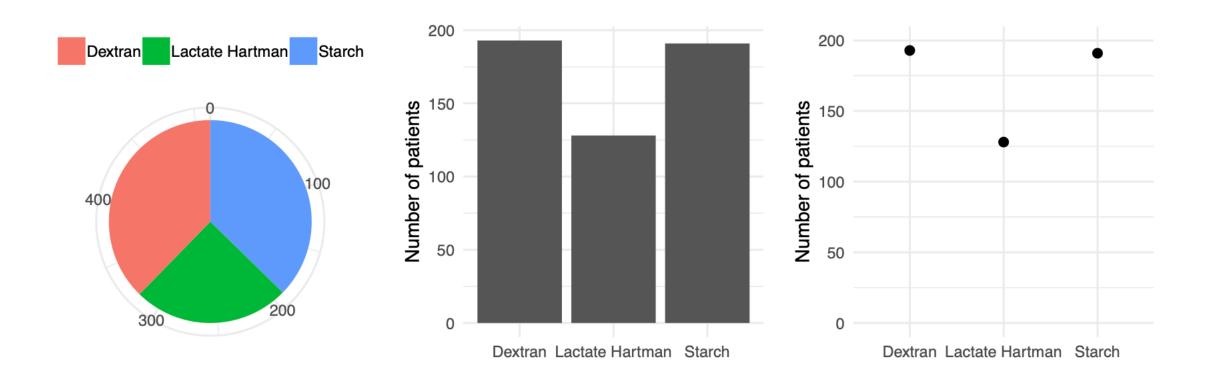
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Continuous variables

- Histogram/density plot
- Boxplot

Pie, bar and dot



Histogram

Histogram

 Group values of a variable into bins of equal width; plot the number (or relative frequency) as a barchart

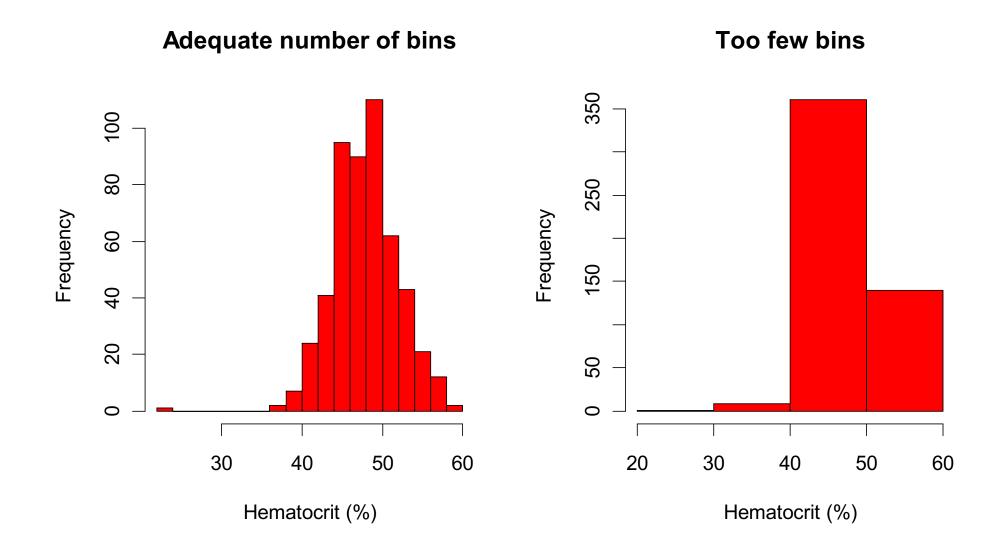
Histogram

 Group values of a variable into bins of equal width; plot the number (or relative frequency) as a barchart

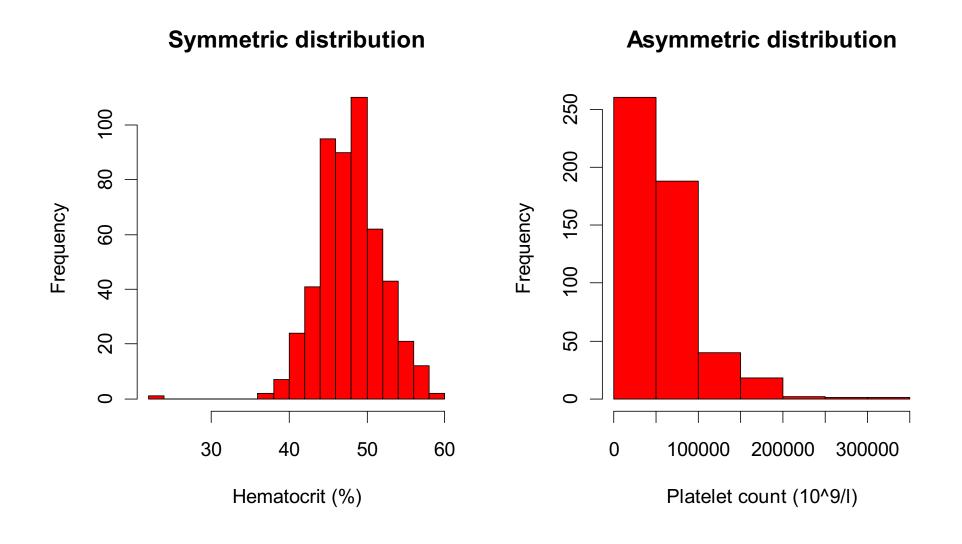
 Caveat: visual appearance may depend on the chosen number and location of bins

Try several groupings of the data

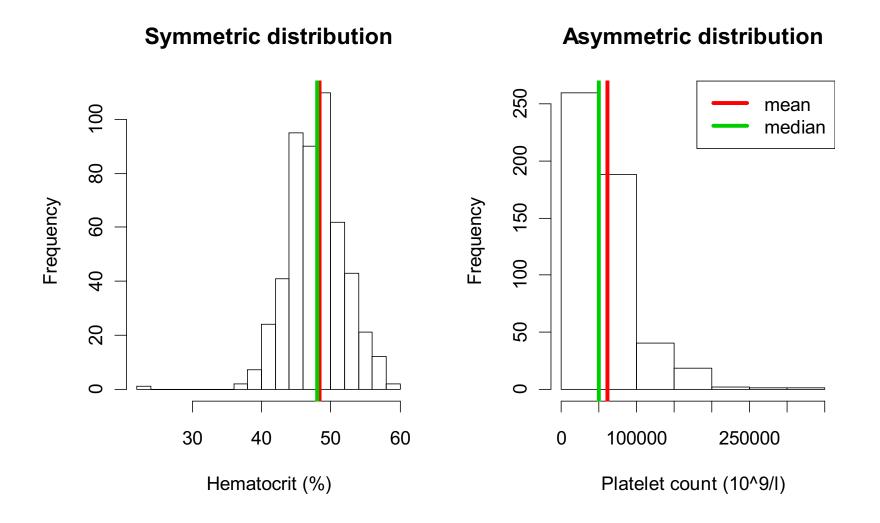
Histogram: examples



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Histogram: examples

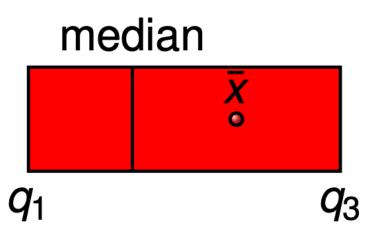


Boxplot

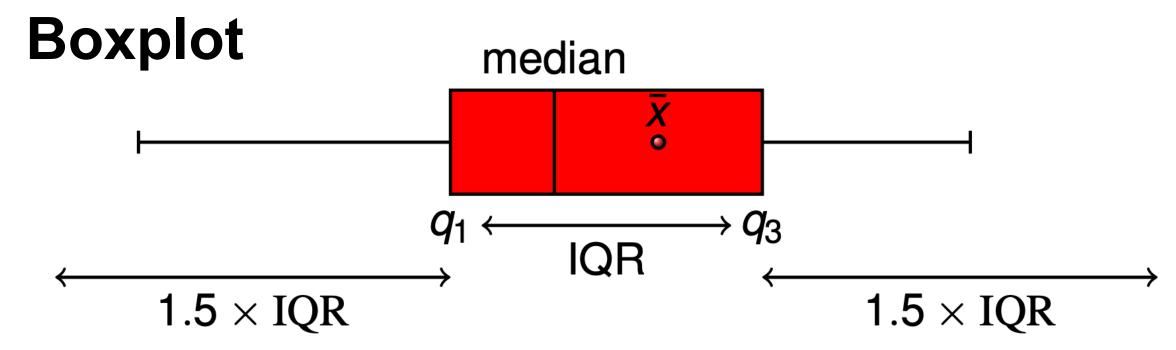
Boxplot

Formal name: box-and-whisker plot

Boxplot

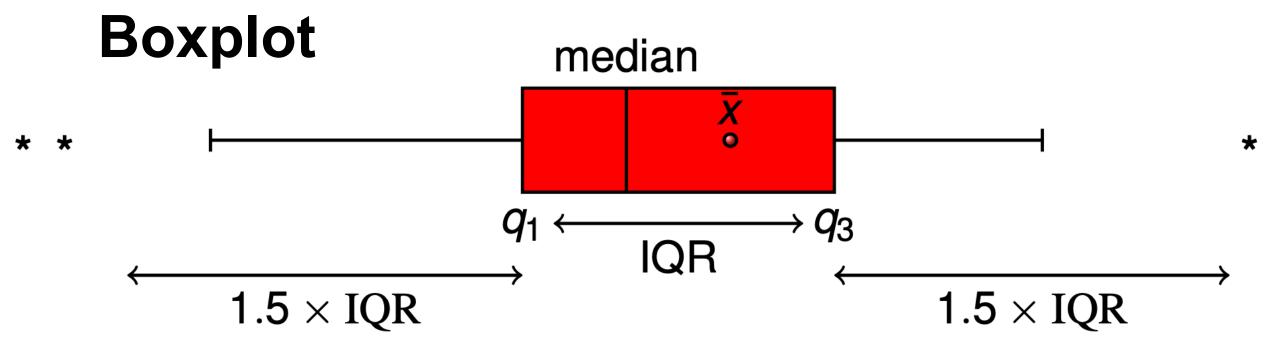


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- Box: most common observations
- Whiskers: less common but still typical
 - From quartiles to the furthest away observation:

$$\geq$$
 q1 -1.5 × IQR and \leq q3 +1.5 × IQR

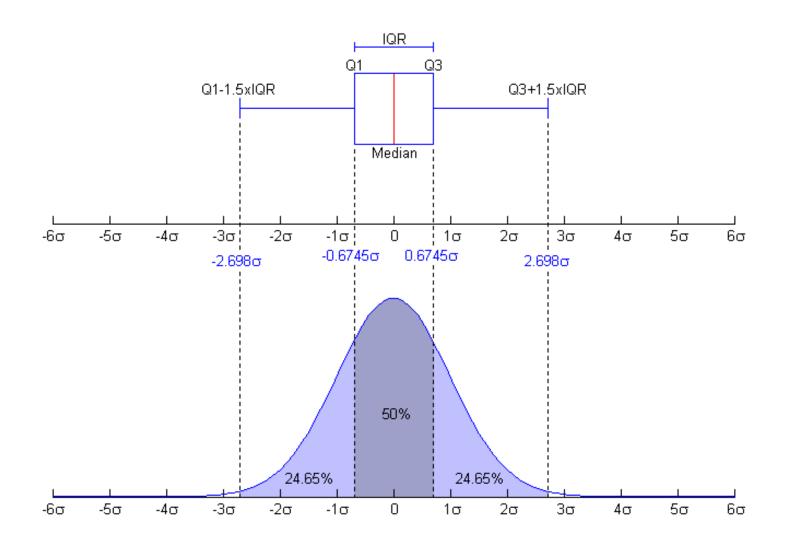


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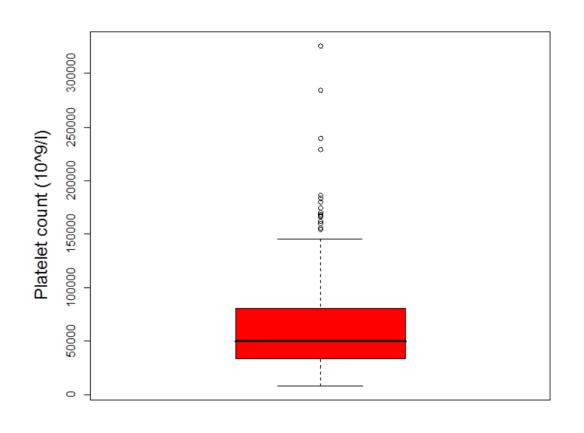
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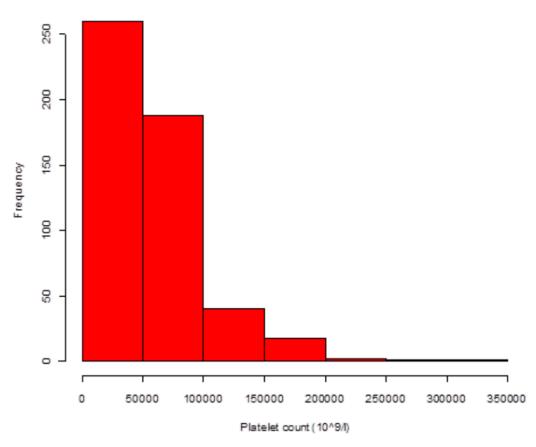
Outliers: All points outside of the whiskers

Boxplot for normal distribution



Boxplot vs. Histogram





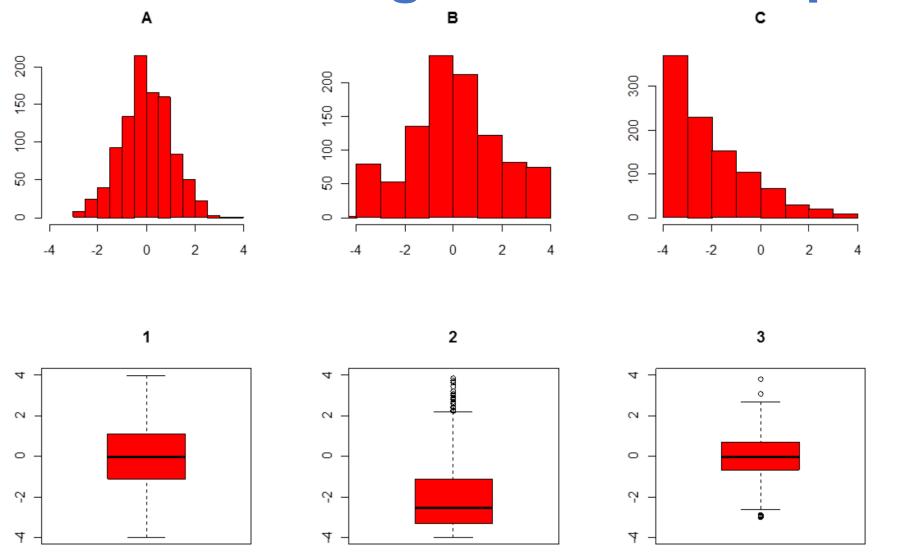
Boxplot: usage

Useful and concise summaries of the data

Particularly useful for visual comparisons of multiple groups

Small data sets: add individual values as dots

Quiz: Match histograms and boxplots

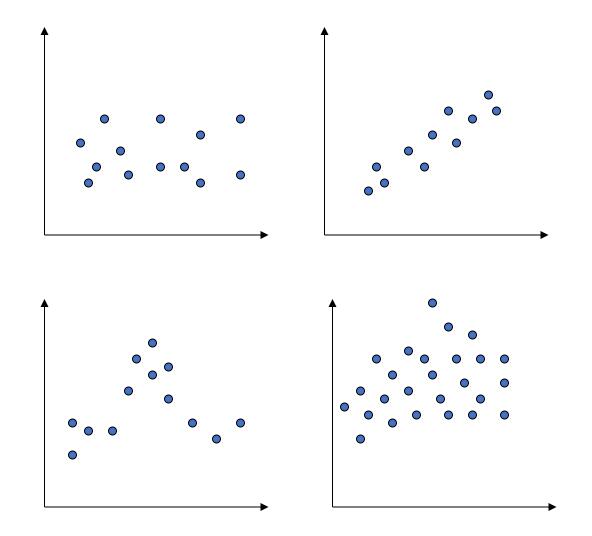


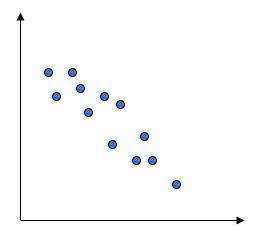
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- Scatterplot
- x independent variable (predictor, covariable)
- y dependent variable (outcome, response)
- Sometimes not clear which variable is x or y
- Each observation is represented by one point
- Pattern of the points → relationship between variables

Scatterplot





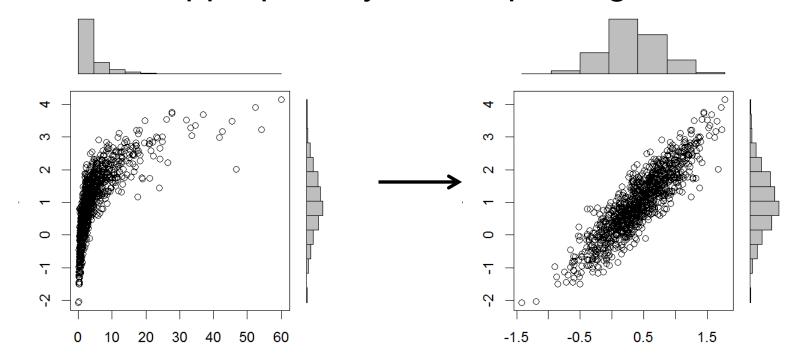
No relationship
Positive correlation
Negative correlation
Linear relationship
Non-linear relationship

Scatterplot

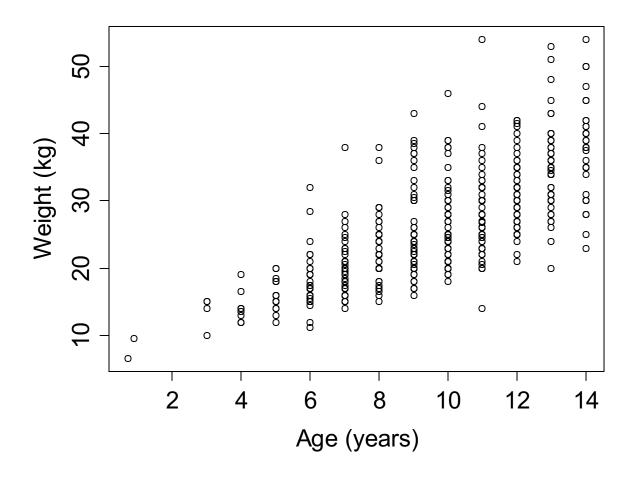
- Scatter plots are easier to interpret if variables are approximately normally distributed
- Transform data appropriately before plotting

Scatterplot

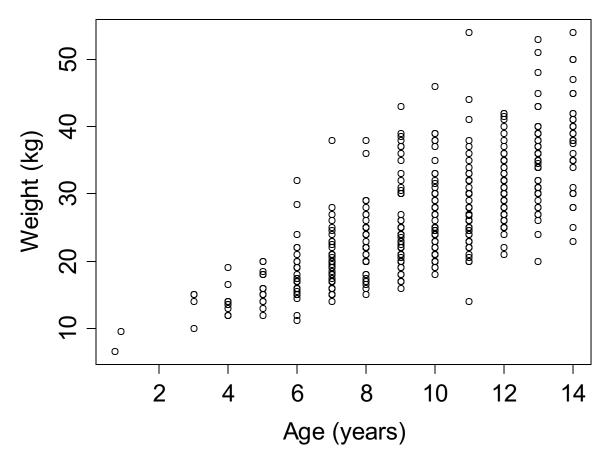
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Quiz: age vs. weight for dengue shock dataset



Quiz: age vs. weight for dengue shock dataset



- Roughly linear increase of weight with age
- · A lot of variability, especially for higher age

Summary

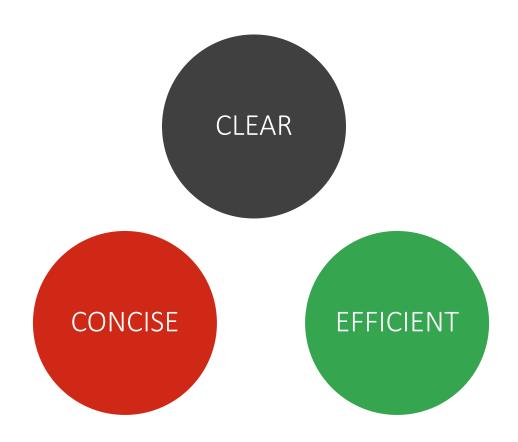
- Data structure
- Data types: categorical/continuous
- Data summary
 - Numbers
 - Frequency, percentage, proportion
 - Location: mean, median
 - Dispersion: standard deviation, range, IQR
 - Graphs
 - Pie chart, bar chart, dotplots
 - Histogram, boxplot
 - Scatterplot

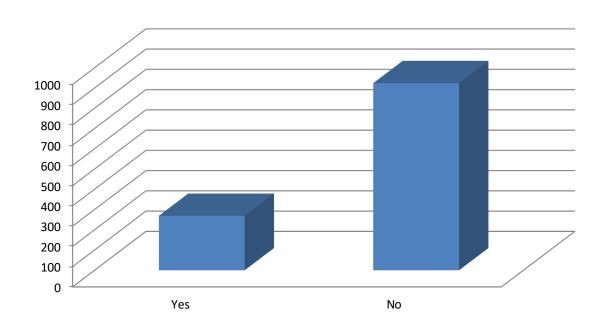
Making effective graphs and tables

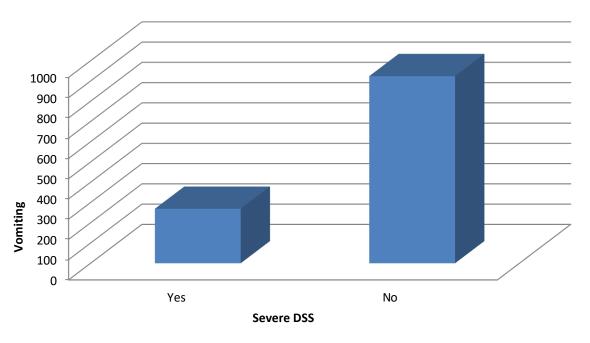
Graphs and tables can be

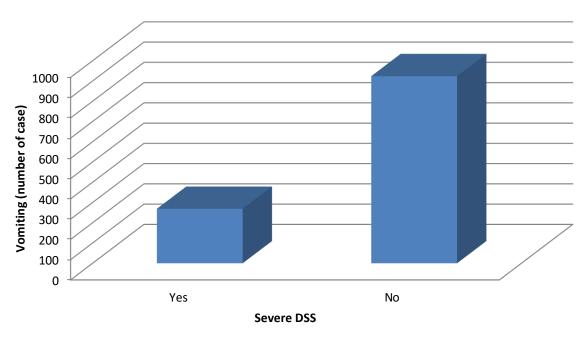


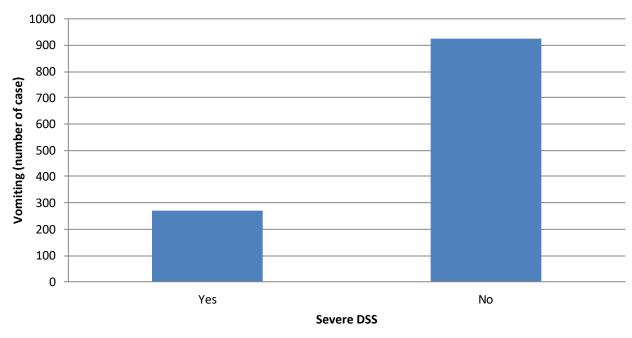
Graphs and tables should be

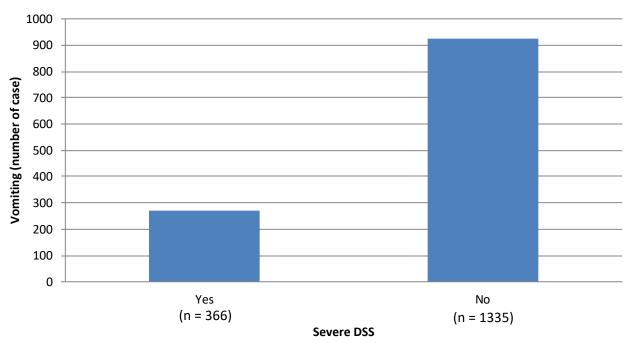


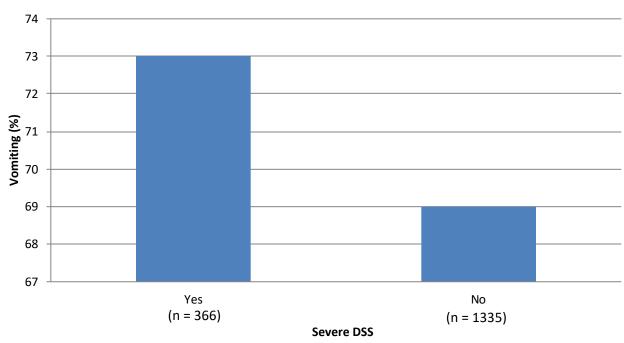


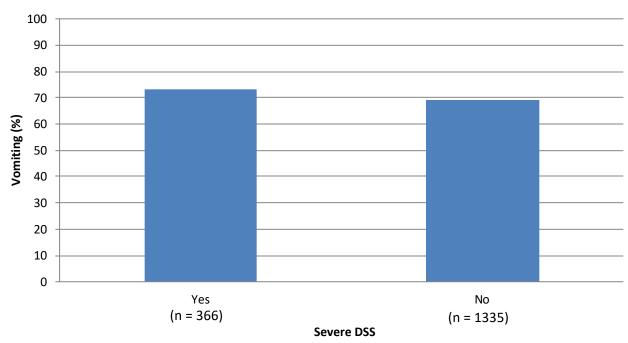












Characteristics	Summary statistics		
Age	9.753	(7.012 – 12.18)	
Weight	27.2	(20.14 – 35.26)	
Hemorrhage			
None	493	(29.1)	
Skin only	1153	(67.35)	
Mucosal	73	(3.55)	

Table 1. Baseline characteristics of the study participants

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Age	9.753	(7.012 – 12.18)	
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Table 1. Baseline characteristics of the study participants at enrolment

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Table 1. Baseline characteristics of the study participants at enrolment (N = 1719)

Characteristics	Summary statistics		
Age	9.753	(7.012 – 12.18)	
Weight	27.2	(20.14 – 35.26)	
Hemorrhage			
None	493	(29.1)	
Skin only	1153	(67.35)	
Mucosal	73	(3.55)	

Table 1. Baseline characteristics of the study participants at enrolment (N = 1719)

Characteristics	Summary statistics		
Age	9.753	(7.012 – 12.18)	
Weight	27.2	(20.14 – 35.26)	
Hemorrhage			
None	493	(29.1)	
Skin only	1153	(67.35)	
Mucosal	73	(3.55)	

Table 1. Baseline characteristics of the study participants at enrolment (N = 1719)

Characteristics	Summary statistics		
Age [year]	9.753	(7.012 – 12.18)	
Weight [kg]	27.2	(20.14 – 35.26)	
Hemorrhage			
None	493	(29.1)	
Skin only	1153	(67.35)	
Mucosal	73	(3.55)	

Table 1. Baseline characteristics of the study participants at enrolment (N = 1719)

Characteristics	Summary statistics		
Age [year]	9.75	(7.01 – 12.18)	
Weight [kg]	27.20	(20.14 – 35.26)	
Hemorrhage			
None	493	(29.10)	
Skin only	1153	(67.35)	
Mucosal	73	(3.55)	

Table 1. Baseline characteristics of the study participants at enrolment (N = 1719)

Characteristics	Summary statistics		
Age [year]	10	(7 – 12)	
Weight [kg]	27	(20 – 35)	
Hemorrhage			
None	493	(29)	
Skin only	1153	(67)	
Mucosal	73	(4)	

Table 1. Baseline characteristics of the study participants at enrolment (N = 1719)

Characteristics	n	Summary statistics	
Age [year]	1710	10	(7 – 12)
Weight [kg]	1600	27	(20 – 35)
Hemorrhage	1719		
None		493	(29)
Skin only		1153	(67)
Mucosal		73	(4)

Table 1. Baseline characteristics of the study participants at enrolment (N = 1719)

Characteristics	n	Summary statistics	
Age [year]	1710	10	(7 – 12)
Weight [kg]	1600	27	(20 – 35)
Hemorrhage	1719		
None		493	(29)
Skin only		1153	(67)
Mucosal		73	(4)

Summary

- How to make an effective graph or table?
 - Ensure its CLARITY, PRECISION, and EFFICIENCY
 - Would you like to receive a KISS? Keep It Short and Simple

RECAP

Recap

- Biostatistics
 - Descriptive and inferential statistics
- Descriptive statistics
 - Data structure: tidy data
 - Data types: categorical/continuous
 - Data summary
 - Numbers
 - Frequency, percentage, proportion
 - Location: mean, median
 - Dispersion: standard deviation, range, IQR
 - Graphs
 - Pie chart, bar chart, dotplots
 - Histogram, boxplot
 - Scatterplot
- Making effective graphs and tables
 - Clarity, precision, efficiency