

\Rightarrow eigenvector x is given by

$$x = \begin{pmatrix} x_1 = c \\ x_2 = 0 \\ x_3 \end{pmatrix} = x_3 \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

\Rightarrow any real number until $x_3 \neq 0 \rightarrow$
eigenvectors of C until.
Eigen value = 2.

$\therefore \lambda = 3 + 2\sqrt{2}$

+ current matrix $C - \lambda I$

$$[R_1 + R_2] \Leftrightarrow \begin{pmatrix} -1 & -2 & 0 \\ -2 & 5 & 0 \\ 0 & 0 & 1 \end{pmatrix} - \begin{pmatrix} 3+2\sqrt{2} & 0 & 0 \\ 0 & 3+2\sqrt{2} & 0 \\ 0 & 0 & 3+2\sqrt{2} \end{pmatrix}$$

$$\Leftrightarrow \begin{pmatrix} -2\sqrt{2}-2 & 0 & 0 \\ -2 & 5-2\sqrt{2} & 0 \\ 0 & 0 & -1-2\sqrt{2} \end{pmatrix} \quad \left| \begin{array}{l} R_1 \rightarrow R_1 - (-2-2\sqrt{2})R_3 \\ R_2 \rightarrow R_2 - (-2)R_1 \\ R_3 \rightarrow R_3 \end{array} \right.$$

$$\downarrow \quad \left[\begin{array}{l} R_1 \rightarrow R_1 - (-2-2\sqrt{2})R_3 \\ R_2 \rightarrow R_2 - (-2)R_1 \end{array} \right]$$

$$\begin{pmatrix} 1 & 1+\sqrt{2} & 0 \\ -2 & 2-2\sqrt{2} & 0 \\ 0 & 0 & -1-2\sqrt{2} \end{pmatrix}$$

$$\downarrow \quad \left[R_2 \rightarrow R_2 - 4R_1 \right]$$

$$\begin{pmatrix} 1 & 1+\sqrt{2} & 0 \\ 0 & 4 & 0 \\ 0 & 0 & -1-2\sqrt{2} \end{pmatrix}$$

$$\left(\begin{array}{ccc} 1 & 1+\sqrt{2} & 0 \\ 0 & 4 & 0 \\ 0 & 0 & 1 \end{array} \right) \quad \not\rightarrow \quad \left[R_3 \rightarrow R_3 / (1-2\sqrt{2}) \right]$$