THIS IS A PLACE HOLDER TITLE PAGE (empty page)

Ship motion prediction using IMU and wave images - a deep learning approach

Lance De Waele

2022

(second title page)

# Preface

TODO. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Fusce ultricies, orci et scelerisque volutpat, nibh metus vestibulum ipsum, quis convallis ex orci ut massa. Curabitur felis dolor, tempor eu interdum nec, mattis quis felis. Vestibulum in nibh sit amet quam porta tristique. Fusce eu tortor tempus, tincidunt tortor hendrerit, sollicitudin elit. Cras a tempor urna. Vivamus vel malesuada purus. Sed feugiat egestas dolor, at feugiat lorem. Aliquam erat volutpat. Ut vel suscipit mi, quis vehicula lacus. Duis vitae libero semper, dignissim risus quis, vulputate augue. Praesent libero mauris, pretium id pharetra eget, malesuada et augue. Donec sed tincidunt augue. Nunc condimentum lectus non augue consequat, eget malesuada felis volutpat. Vestibulum ornare ultricies orci. Nulla sit amet dictum justo, non commodo arcu.

# Abstract

(English)

TODO Lorem ipsum dolor sit amet, consectetur adipiscing elit. Fusce ultricies, orci et scelerisque volutpat, nibh metus vestibulum ipsum, quis convallis ex orci ut massa. Curabitur felis dolor, tempor eu interdum nec, mattis quis felis. Vestibulum in nibh sit amet quam porta tristique. Fusce eu tortor tempus, tincidunt tortor hendrerit, sollicitudin elit. Cras a tempor urna. Vivamus vel malesuada purus. Sed feugiat egestas dolor, at feugiat lorem. Aliquam erat volutpat. Ut vel suscipit mi, quis vehicula lacus. Duis vitae libero semper, dignissim risus quis, vulputate augue. Praesent libero mauris, pretium id pharetra eget, malesuada et augue. Donec sed tincidunt augue. Nunc condimentum lectus non augue consequat, eget malesuada felis volutpat. Vestibulum ornare ultricies orci. Nulla sit amet dictum justo, non commodo arcu.

# Extended abstract

(Nederlands)

TODO Lorem ipsum dolor sit amet, consectetur adipiscing elit. Fusce ultricies, orci et scelerisque volutpat, nibh metus vestibulum ipsum, quis convallis ex orci ut massa. Curabitur felis dolor, tempor eu interdum nec, mattis quis felis. Vestibulum in nibh sit amet quam porta tristique. Fusce eu tortor tempus, tincidunt tortor hendrerit, sollicitudin elit. Cras a tempor urna. Vivamus vel malesuada purus. Sed feugiat egestas dolor, at feugiat lorem. Aliquam erat volutpat. Ut vel suscipit mi, quis vehicula lacus. Duis vitae libero semper, dignissim risus quis, vulputate augue. Praesent libero mauris, pretium id pharetra eget, malesuada et augue. Donec sed tincidunt augue. Nunc condimentum lectus non augue consequat, eget malesuada felis volutpat. Vestibulum ornare ultricies orci. Nulla sit amet dictum justo, non commodo arcu.

# Table of contents

[Preface 3](#_Toc105549470)

[Abstract 4](#_Toc105549471)

[Extended abstract 5](#_Toc105549472)

[Table of contents 6](#_Toc105549473)

[List of Figures 9](#_Toc105549474)

[List of Tables 10](#_Toc105549475)

[List of Abbreviations 11](#_Toc105549476)

[1 Introduction 12](#_Toc105549477)

[1.1 Problem definition 12](#_Toc105549478)

[1.2 Objectives 13](#_Toc105549479)

[1.3 Thesis outline 13](#_Toc105549480)

[2 Background and literature review 14](#_Toc105549481)

[2.1 Motion states in six degrees of freedom 14](#_Toc105549482)

[2.2 Ocean wave induced ship motion 15](#_Toc105549483)

[2.3 Ship motion prediction methods 16](#_Toc105549484)

[2.3.1 Dynamic linear modelling 16](#_Toc105549485)

[2.3.2 Deep learning 17](#_Toc105549486)

[2.3.3 Hybrid models 18](#_Toc105549487)

[2.4 Artificial neural networks 18](#_Toc105549488)

[2.4.1 Activation functions 19](#_Toc105549489)

[2.4.2 Auto-encoders 20](#_Toc105549490)

[2.4.3 RNN and LSTM layers 20](#_Toc105549491)

[2.4.4 Convolutional Neural Networks 21](#_Toc105549492)

[2.5 Tools 23](#_Toc105549493)

[2.6 Expected performance 23](#_Toc105549494)

[2.7 Summary 25](#_Toc105549495)

[3 Data collection and preprocessing 26](#_Toc105549496)

[3.1 Simulated data 26](#_Toc105549497)

[3.1.1 Simulation parameters 27](#_Toc105549498)

[3.1.2 Data augmentation 27](#_Toc105549499)

[3.2 Real data 28](#_Toc105549500)

[3.2.1 Sensors onboard the ASV 28](#_Toc105549501)

[3.2.2 Sensory data challenges 29](#_Toc105549502)

[3.3 Data pre-processing 29](#_Toc105549503)

[3.3.1 Data cleaning 30](#_Toc105549504)

[3.3.2 Data formatting 30](#_Toc105549505)

[3.3.3 Data reduction 30](#_Toc105549506)

[3.3.4 Data normalization 30](#_Toc105549507)

[3.4 Data analysis 31](#_Toc105549508)

[3.4.1 Statistical properties 31](#_Toc105549509)

[3.4.2 Correlation and interactions 33](#_Toc105549510)

[3.5 Data loading 33](#_Toc105549511)

[3.5.1 Sequence creation 33](#_Toc105549512)

[3.5.2 Train-test splitting 34](#_Toc105549513)

[3.5.3 PyTorch batching 35](#_Toc105549514)

[3.6 Summary 35](#_Toc105549515)

[4 Model designs 36](#_Toc105549516)

[4.1 Single-step model 36](#_Toc105549517)

[4.2 Multi-step models 37](#_Toc105549518)

[4.2.1 Encoder-Decoder LSTM 37](#_Toc105549519)

[4.2.2 Sequential CNN 39](#_Toc105549520)

[4.2.3 CNN LSTM single input 40](#_Toc105549521)

[4.2.4 CNN LSTM dual input 41](#_Toc105549522)

[4.3 Summary 42](#_Toc105549523)

[5 Testing environment 43](#_Toc105549524)

[5.1 Gradient descent algorithms 43](#_Toc105549525)

[5.1.1 SGD Adam optimizer 43](#_Toc105549526)

[5.2 Hyperparameters 44](#_Toc105549527)

[5.3 Performance metrics 45](#_Toc105549528)

[5.3.1 Loss function 45](#_Toc105549529)

[5.3.2 Inference time 46](#_Toc105549530)

[5.4 Summary 47](#_Toc105549531)

[6 Results 48](#_Toc105549532)

[6.1 Hyperparameter optimization 48](#_Toc105549533)

[6.1.1 Number of epochs 48](#_Toc105549534)

[6.1.2 Learning rate 49](#_Toc105549535)

[6.1.3 LSTM hidden size 49](#_Toc105549536)

[6.1.4 Activation functions 50](#_Toc105549537)

[6.2 Single-step model 51](#_Toc105549538)

[6.3 Multi-step models 53](#_Toc105549539)

[6.3.1 Encoder-Decoder LSTM 53](#_Toc105549540)

[6.3.2 Sequential CNN 56](#_Toc105549541)

[6.3.3 CNN LSTM ensemble models 57](#_Toc105549542)

[6.4 Augmented data 58](#_Toc105549543)

[6.5 Inference time 59](#_Toc105549544)

[6.6 Summary 60](#_Toc105549545)

[7 Conclusion 61](#_Toc105549546)

[7.1 Future work 61](#_Toc105549547)

[References 63](#_Toc105549548)

[Appendix A. Individual predictions and LPF 67](#_Toc105549549)

# List of Figures

[Figure 1: Prototype of Autonomous Surface Vessel (ASV) with on-board computer and sensors (“MarSur,” 2019) 12](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549345)

[Figure 2: Six degrees of freedom in ship motion(de Masi et al., 2011) 14](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549346)

[Figure 3: Heave (m) in function of time (s) (Ham et al., 2017) 15](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549347)

[Figure 4: Neural network structure (left) and a linear neuron (right) 18](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549348)

[Figure 5: Neurons in a recurrent neural network with additional feed-back connections 20](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549349)

[Figure 6: LSTM-cell components (left) and their mathematical notations (right) 21](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549350)

[Figure 7: Convolution over grayscale image with 3x3 kernel 22](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549351)

[Figure 8: Max pooling with 2x2 kernel 22](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549352)

[Figure 9: Generated images of incoming waves (chronologically ordered left to right, top to bottom) 27](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549353)

[Figure 10: Augmented images 28](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549354)

[Figure 11: ZED-mini IMU stereo camera (StereoLabs, Paris, France) 28](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549355)

[Figure 12: Scatterplot of pitch and roll 29](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549356)

[Figure 13: Maximum range of rolling motion for ships 31](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549357)

[Figure 14: Simulated Pitch and Roll distributions 32](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549358)

[Figure 15: Correlation matrix for pitch and roll 33](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549359)

[Figure 16: Sequence creation with moving input and output sequence 34](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549360)

[Figure 17: Single step model architecture variants: single output (left), dual output (right) 37](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549361)

[Figure 18: LSTM encoder decoder architecture 38](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549362)

[Figure 19: sequential CNN neural network architecture 39](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549363)

[Figure 20: CNN LSTM single input architecture 40](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549364)

[Figure 21: CNN LSTM dual input architecture 42](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549365)

[Figure 22: inference time over 10.000 prediction with GPU warm-up effect 46](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549366)

[Figure 23: training losses for different numbers of epochs 48](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549367)

[Figure 24: training loss for different learning rates 49](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549368)

[Figure 25: training loss for different LSTM hidden sizes 50](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549369)

[Figure 26: predicted (orange) vs. real (blue) values for pitch (top) and roll (bottom) 52](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549370)

[Figure 27: MSE loss during training of the single-step models 53](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549371)

[Figure 28: encoder-decoder LSTM training and validation losses for different IO-ratios 54](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549372)

[Figure 29: loss per frame for 10/60 (top) and 120/60 (bottom) IO-ratio with reference line at 3° (grey) 55](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549373)

[Figure 30: loss per frame for 60/120 (top) and 120/120 (bottom) IO-ratio with reference line at 3° (grey) 56](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549374)

[Figure 31: training and validation losses for different IO-ratios of the sequential CNN model 57](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549375)

[Figure 32: training and validation loss for CNN LSTM ensemble models 57](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549376)

[Figure 34a: CNN LSTM **single** input prediction (red) vs. real (blue) on augmented frames: grayscale (left) and colored (right) 59](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549377)

[Figure 34b: CNN LSTM **dual** input prediction (red) vs. real (blue) on augmented frames: grayscale (left) and colored (right) 59](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549378)

[Figure 35: encoder decoder LSTM - 60/60 67](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549379)

[Figure 36: Sequential CNN - 10/60 68](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549380)

[Figure 37: CNN LSTM single input (colored) - 10/60 69](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549381)

[Figure 38: CNN LSTM dual input (colored) - 10/60 70](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549382)

[Figure 39: CNN LSTM dual input (colored) - 10/120 71](https://d.docs.live.net/fa0db4c9d4849523/Documenten/paper.docx#_Toc105549383)

# List of Tables

[Table 1: overview of different activation functions 19](#_Toc105547781)

[Table 2: Kaminskyi's results for different models with worst (red) and best (green) model highlighted (Kaminskyi, 2019a) 24](#_Toc105547782)

[Table 3: prediction error at different future time-steps of Kaminskyi's best model (Kaminskyi, 2019a) 24](#_Toc105547783)

[Table 4: Statistical information for pitch and roll in simulated dataset 32](#_Toc105547784)

[Table 5: newly introduced notations and their explanations 36](#_Toc105547785)

[Table 6: parameter table for single-step models 36](#_Toc105547786)

[Table 7: parameter table for encoder-decoder LSTM 38](#_Toc105547787)

[Table 8: parameter table for sequential CNN model 40](#_Toc105547788)

[Table 9: parameter table for CNN LSTM single input and dual output (red) 41](#_Toc105547789)

[Table 10: average pitch and roll errors for different activation function configurations 50](#_Toc105547790)

[Table 11: denormalized RMSE for single-step LSTM variants at 10/1 and 50/1 IO-ratios 51](#_Toc105547791)

[Table 12: average denormalized RMSE for encoder decoder LSTM per IO-ratio 54](#_Toc105547792)

[Table 13: average denormalized RMSE for CNN LSTM single [img] and dual [img-PR] input model 58](#_Toc105547793)

[Table 15: inference timing, PR error and number of trainable parameters for each model’s optimal configuration 60](#_Toc105547794)

# List of Abbreviations

AI: Artificial Intelligence

ASV: Autonomous Surface Vessel

VTOL: Vertical Take Off and Landing

IMU: Inertial Measurement Unit

PoV: Point of View

ANN: Artificial Neural Network

GPU: Graphics Processing Unit

PR: Pitch and Roll

Img: Images

LSTM: Long Short-Term Memory

CNN: Convolutional Neural Network

NN: Neural Network

ReLU: Rectified Linear Unit

Tanh: Hyperbolic Tangent

PR: Pitch and Roll

FC: Fully Connected

RNN: Recurrent Neural network

GPU: Graphics Processing Unit

CPU: Central Processing Unit

RAM: Random Access Memory

# Introduction

In the last few years, the world has seen an exponential increase in technological advancements. This evolution brought a new influence of autonomous systems controlled by artificial intelligence (AI). Each of these systems being designed with their own unique characteristics, optimized for the desired task. Increasingly more of these systems are being deployed as a direct or indirect replacement for tasks humans could do, but also, for tasks too complex for humans to accomplish. And because these autonomous systems are optimized for specific jobs, they are often more accurate and accomplish them faster than humans.

Because autonomous systems are especially useful in military operations. They can take over the role of a human in dangerous environments such as an active warzone and can therefore eliminate the endangerment of someone’s life. On the other hand, they can also be used as a complimentary asset, providing support and aid in logistics. An increasing amount of these autonomous assets such as drones, surface vessels, tanks and reconnaissance vehicles are being deployed around the world for various objectives. However, with this increasing amount of autonomous assets, there is need for proper communication between them, to allow them to work together and be aware of the state of each other when they need to interact (de Cubber, 2019).

“*Interoperability is the key that acts as the glue among the different units within the team, enabling efficient multi-robot cooperation.”* (“MarSur,” 2019)



Figure 1: Prototype of Autonomous Surface Vessel (ASV) with on-board computer and sensors (“MarSur,” 2019)

## Problem definition

The Robotics & Autonomous Systems lab of the Belgian Royal Military Academy is currently working on two autonomous vehicles in two separate projects named MarSur and MarLand. Project MarSur is developing framework for autonomous systems to easily interact with each other. In short, they are developing a heterogeneous interoperability and collaboration framework which is seamlessly interoperable with existing infrastructure. This framework will, among others, be used to facilitate the communication and interaction of autonomous surface vessels (ASV) (**Fout! Verwijzingsbron niet gevonden.**) and other unmanned aerial systems such as drones (“MarSur,” 2019). Project MarLand focuses on research in one of these interactions, namely vertical take-off and landing (VTOL). The aim of the MarLand project is to provide a proof-of-concept solution and practical implementation for a helicopter-type drone with the capability to land autonomously on the Belgian Navy vessels (“MarLand,” 2020). The capability for these unmanned aerial drones to automatically take off and land on vessels in all kinds of environmental conditions remains a bottleneck for widespread deployment. Landing a relatively small aerial vehicle - that is inherently very receptive to wind gusts - on the pitching and rolling deck of a moving ship is a very difficult control problem that requires the consideration of the kinematics and dynamics of both the unmanned aerial vehicle and the ship. For a smooth landing to be possible, the target vessel must be capable to determine its state in a three-dimensional space and predict its movement in the ocean. This way, the drone can anticipate the movement off the vessel and avoid collision. In addition, the predictions can be used to find a window of landing opportunity in which the vessel remains in a relatively stable state. In conclusion, this thesis proposes to provide a state-of-the-art solution for ship motion prediction to serve as a landing guidance for drones.

## Objectives

The goal of this thesis is to research and develop a method to predict the motion of a surface vessel using the data captured from onboard sensors. This method should be both accurate and have a low latency to allow for real-time deployment on minimal hardware. The prediction models can use a sequence of values describing the state of the vessel such as pitch and roll together with images of incoming waves taken from a stabilized camera pointing to the front of the vessel. The state of the vessel is described by an Inertial Measurement Unit (IMU) sensor that can capture both translational as rotational movement variables. As an output, the model should provide the motion of the vessel in the form of a new sequence of predicted pitch, roll and heave values for every predicted time step. These three parameters are selected as targets due to them being mostly uncontrollable and because they are most impactful to the stability of the landing surface. A more in-depth discussion of these state describing parameters is provided in the next chapter. The duration for these predicted sequences should be at minimum thirty seconds at a 1Hz sample-rate to provide the drone with ample time to prepare for a take-off or landing procedure. Bigger drones will need more time for this procedure so the predicted sequence duration should be maximized within the model’s capabilities.

Since the model will be deployed in real-time scenarios and will be making predictions in real-time based on the continuous data stream of the onboard sensors, it should be lightweight and not require substantial amounts of computational power. This means that the inference time or latency of the different proposed methods should also be considered when comparing different models’ performances. In conclusion, both prediction errors and latency should be minimized.

## Thesis outline

The contents of this thesis are divided over the seven chapters. In this first chapter, a general introduction was given of the problem and the objectives. In the second chapter, the most important and insightful related studies are discussed. An overview is given of the state-of-the-art in ship motion prediction and commonly used methods. All background information needed to fully understand the contents of this paper, is provided here as well. In the third chapter, all aspects related to data are discussed: data collection, processing and analysis. In the fourth chapter, different solutions are proposed in the form of deep learning neural network architectures. The fifth chapter discusses how the different solutions are going to be tested and evaluated. The results are discussed in chapter six followed by a concluding discussion in chapter seven. References and an appendix with complementary documents are added at the end of the paper.

# Background and literature review

A lot of research has been performed in the field of motion prediction. It is a topic that has many different applications and is applied to solve or aid in a broad spectrum of problems. For example, with the upcoming trend of autonomous vehicles and self-driving cars, motion prediction is implemented to avoid collisions and provide a safe experience for the passengers, the vehicles themselves and their surroundings (Ren et al., 2021). Additionally, motion prediction also has applications in for example human motion prediction for robot cooperation (Tang et al., 2018) and ground motion prediction to anticipate seismic activity (Dhanya & Raghukanth, 2018). However, due to its complex and mostly non-deterministic nature, motion prediction remains a very difficult problem to solve. And ship motion prediction is no exception to this. Before looking at some viable solutions however, a general understanding is required on how ship motion is described and how ocean wave dynamics induce these motions on ships. The following two sections gently introduce some basic principles followed by three sections explaining different ship motion prediction methods.

## Motion states in six degrees of freedom

The motion of a ship or any rigid object in a three-dimensional space can be described in six degrees of freedom. These six degrees can further be divided into two categories: translational and rotational movement. Where translational movement is movement along one of the three axes in a three-dimensional space, rotational movement is the rotation of an object around these same three axes. These three reference axes run through the center of mass of the ship and are oriented as follows:

* Vertical Z-axis runs vertically through the vessel
* Transverse Y-axis runs horizontally across the vessel
* Longitudinal X-axis runs horizontally through the length of the ship



Figure 2: Six degrees of freedom in ship motion(de Masi et al., 2011)

Each type of motion, translation or rotation, among each of the three axes has a different impact on the movement of the vessel (Figure 2). The translational movements are expressed in linear units such as meters and are named as followed:

* **Sway**: side to side movement along the transverse Y-axis
* **Surge**: forward and backwards movement along the longitudinal X-axis
* **Heave**: upward and downward movement along the vertical Z-axis

The rotational movements are expressed in angular units and are named as followed:

* **Yaw**: rotational movement around the vertical Z-axis
* **Pitch**: rotational movement around the transverse Y-axis
* **Roll**: rotational movement around the longitudinal X-axis

To predict the motion of a ship, one must differentiate between these different motions. Together they form the complete three-dimensional orientation of a ship. But not all of them need to be predicted. Surge and yaw are controlled by the ASV’s autonomous systems and are respectively controlled by the amount of thrust and the rudder position – steering the ship. Surge and yaw will also not change very drastically during the landing or take-off of a drone since this behavior would directly impede our main goal of providing a smooth landing. On the other hand, the sway of a ship, also referred to as drift, is primarily caused by sideways winds or currents in the water and will have minor impact on the stability of the ship whenever the drone needs to take-off or land. If the drone aims for a GPS-tracker present in the ASV, it will follow the vessels movement no matter the sway.

This leaves three main factors remaining which have the most impact on the stability of the vessel: roll, pitch and heave. These three movements have one thing in common, they are all directly caused by the waves in the ocean and are very hard to control. Different methods exist to dampen these movements and keep the vessel as stable as possible such as bilge keels and antiroll tanks. However, most of them are either infeasible or ineffective or do not provide the required stabilization on smaller vessels (Perez & Blanke, 2017). In this case, predicting these movements instead of trying to dampen them, can be an alternative solution. Although it should be noted that using them together, will most likely yield the best performance. Pitch, roll and heave can be divided in two categories based on the effect they have on the landing and take-off of the drone. Pitch and roll are responsible for the stability of the landing surface and heave is responsible for the impact on the drone when landing.

To provide a stable landing zone for the drone, the pitch and roll of the vessel should remain constant and as close to zero as possible. Depending on the characteristics of the drone, the model should be able to analyze its prediction sequence and find a window where the desired circumstances to land/take-off are met. To determine this window of landing/take-off opportunity, different parameters need to be defined such as the maximum difference in consequent prediction values, the length of the window and the interval in which all predicted values should lie. For example, the roll and pitch values should all remain in a [-3°, 3°] interval, the stable window duration must be at least five seconds and there should be no difference larger than two degrees between consecutive predicted values. Within the objectives chapter, these criteria are discussed in more detail.



Figure 3: Heave (m) in function of time (s) (Ham et al., 2017)

To minimize the impact on the drone when landing, the heave needs to be constant or decreasing. This means that the vessel is either not moving up or down, or it is slowly moving downwards following the motion of the descending drone. In regular waves, the heave of a vessel follows a wave-like function, alternating between upwards and downwards motion (Figure 3). In this case, the window of take-off/landing opportunity can be defined as the points where the vessel transitions from upwards to downwards motion, or vice versa, and thus has an acceleration of zero.

## Ocean wave induced ship motion

Natural ship motions are primarily caused by the motion of ocean waves which are little deterministic. Ocean waves are the result of an accumulation of several types of waves including capillary waves generated from atmospheric pressure, wind waves, and planetary waves (Silva, 2015). The product of this accumulation of waves is the stochastic nature of sea motion, which is often described using a wave energy density spectrum (Abujoub, 2019). According to Perez T., the motion of a ship can be decomposed into three separate motion inducing forces. The superposition or accumulation of these three forces results in the magnitude of the motion.

* **First-order wave-induced forces**. This force is oscillatory. This is commonly modelled as a time series disturbance obtained by combining the wave spectrum with the vessel’s Motion Response Amplitude Operators (Motion RAO), which are transfer functions that map the wave elevation or wave slope into force and motion.
* **Slowly varying disturbance forces**. This force is produced by current, wind and second-order wave effects such as wave mean-drift.
* **Control-induced forces**. This is the force induced by the control system, which is usually designed to counteract only the effect of the slowly varying disturbances.

Each one of these forces has profound and proven mathematical foundation which is well documented in Perez T.’s lecture paper (Perez & Fossen, 2005). Besides these forces, the wave encounter frequency spectrum also plays a role in predicting the motion of a ship. According to Dr. Q. Judge, the motions of a vessel can be seen as a three-part black box structure. The input are the ocean waves and their induced forces as discussed above. The black box are the ship dynamics like its inertia, natural frequency and physical form and the output are the motions of the ship in oceanic waves (Q. Judge, 2019).

In conclusion, the motion of a vessel in ocean waves is a complex interplay between the dynamics of the ocean and the dynamics of the ship. Due to extensive research in these fields, all of the above-mentioned concepts have been supported with mathematical equations. These mathematical foundations have allowed researchers to accurately model these dynamics in physics simulations (Ran et al., 2021). These models, together with the ever-evolving technological possibilities by the likes of computer vision and artificial intelligence, present a variety of methods that can be considered when trying to predict the motion of a ship.

## Ship motion prediction methods

Ship motion prediction is incredibly useful for several naval operations such as aircraft landing, cargo transfer, off-loading of small boats, and ship "mating" between a big transport ship and some small ships to name a few. With this wide variety of ship motion prediction applications and its long history of research, numerous approaches were developed. However, most of the approaches found in published research studies can be divided in just three categories. They either use a dynamic model based on the above-mentioned principles, artificial neural networks or a hybrid of the first two. In the following sections, each method is discussed.

### Dynamic linear modelling

Dynamic linear models or state space models are a set of equations mapping inputs to outputs of a given system based all parameters that affect the model state. It is an approach that relies on the mathematical foundations of ship and wave dynamics. A common method that is used is **minor component analysis (MCA)** (Luo et al., 1997). MCA has similar mathematics as the Principal Component Analysis, except that MCA utilizes the eigenvectors corresponding to the minor components. The viability of this method is proven by Zhao. He proposed an algorithm using MCA that was able to predict a twenty second sequence from 800 input datapoints with high and consistent accuracy (Zhao et al., 2004). Zhao used a dataset provided by a software simulation from JJMA inc. The data (surge, sway, heave, pitch, roll, yaw) was collected at 8Hz and down sampled to 2Hz. This frequency combined with the simulated data is very similar to the simulated data that will be used for this research. In his work he compared the method to a neural network, vector autoregression (VAR) (Stock & Watson, 2001) and a Wiener filter (Chen et al., 2006). The conclusion was that MCA outperformed all other compared methods and was also suited for real-time implementation. It had the lowest latency based on 500 predictions and the fastest training time. However, only a simple three-layered linear regression neural network was tested for comparison. Newer architectures have since been developed which are better suited for time-series predictions. Additionally, 400 seconds were needed to predict only 20 seconds, this is a very high input-output ratio. Finally, but most importantly, the data of the simulation did not show any form of noise. To compensate this, Zhao tested the models with varying levels of introduced zero-mean Gaussian random noise. This caused the MCA method to quickly lose accuracy with a tenfold decrease in performance at 20% introduced noise. The percentage refers to the peak amplitude percentage or standard deviation of the introduced Gaussian noise.

Another commonly used method is **Kalman filtering,** also known as Linear Quadratic Estimation (LQE) (Kalman, 1960). Initially developed in 1960 and proven effective and reliable by its implementation in the Apollo project (Grewal & Andrews, 2010), Rudolf E. Kalman received the National Medal of Science for Engineering for his research. In theory, the Kalman filter is an algorithm that uses a series of measurements observed over time, including statistical noise and other inaccuracies, and produces estimates of unknown variables. The Kalman filter produces an estimate of the state of the system as a weighted average of the system's predicted state and the new measurement. These estimates tend to be more accurate than those based on a single measurement alone, by estimating a joint probability distribution over the variables for each timeframe (Chen et al., 2006). In the research study of Fossen and Fossen, an exogenous Kalman filter (Johansen & Fossen, 2017) is used for ship trajectory and position estimation based on multiple sensory inputs (Fossen & Fossen, 2018). Another research was done by Peng where Kalman filters are used for estimating the dynamic ship motion states (Peng et al., 2019).

These studies show that the Kalman filter can be a reliable method for estimation problems. However, due to the complex interrelation between ocean waves and ship motions, setting up a dynamic model for the Kalman filter can be quite challenging. It is mostly used for theoretical models and is hard to apply to a real-world scenario where not all state parameters are known. This issue of not knowing all parameters to build an accurate dynamic model caused the need for an alternative. As proposed by Zhong-yi Z., one of the alternatives could be to estimate these parameters (Zhong-yi, 2012). However, the complexity of these dynamic models, still remains. For this reason, dynamic modelling was not selected for the purpose of this thesis. Additionally, incorporating images in these models is not possible.

### Deep learning

Another alternative in trying to determine these parameters was found in artificial intelligence and more specifically, deep learning. The idea is that instead of trying to figure out all necessary parameters to build a dynamic model, a computer is trained to build its own representation which provides the mapping between in- and outputs as accurately as possible. The computer receives a large set of inputs and their corresponding outputs and learns the relation between the two. This completely eliminates the need to know or estimate parameters for a dynamic model. Because of this, the complexity of the problem is also drastically reduced. This is one of the main reasons why this method was chosen.

The idea of enabling computers to train themselves to solve a problem, dates back to 1958 when the US Navy made a first attempt. However, due to the inability of these early neural networks to learn simple linear decision boundaries like the XOR-function, researchers quickly lost interest (Minsky & Papert, 1969). During the following years, small improvements were made over the next decades that slowly expanded the capabilities of these neural networks. Some notable advancements were support for non-linear decision boundaries with multiple layers and the ability to train these multi-layered networks by back-propagating errors (Rumelhart et al., 1986). Nevertheless, they remained inferior to classical methods like Support Vector Machines (SVM) (Boser et al., 1992). It was only around 2010, that they really became popular when deep neural networks started to outperform all other approaches in computer vision tasks. This breakthrough was possible due to the increase in computing power the availability of large datasets. Ever since, deep neural networks quickly evolved beyond computer vision tasks and have been widely adopted for a plethora of different applications. One of these applications is time-series forecasting problems like ship motion prediction.

Extensive research has been performed in search of optimal deep neural network architectures for time-series prediction and image feature extraction. This presents reliable options today when building a network for ship motion prediction based on images and sensor data. In most cases, Long Short-Term Memory (LSTM) networks are used because they excel in time-series forecasting as will be discussed in 2.4.2. In one the of the reviewed studies, a multiscale attention-based LSTM network is proposed to predict ship motion based as an improvement on regular LSTM networks (Zhang et al., 2021). The attention mechanism boosts the sensitivity of the system by paying more attention to significant signals and suppress interference of noise and proves to achieve better performance than other popular methods. In another study, an L1 regularized extreme learning machine is used instead of an LSTM for single-step predictions (predicting only one future value) which resulted in very low near-zero roll prediction errors (°) (Guan et al., 2018). Lastly, in the research of Rashid M., an ensemble model was proposed combining a Convolutional Neural Network (CNN) with an LSTM and with a Gated Recurrent Unit (GRU) (Rashid et al., 2021). The CNN processes two images of incoming waves while the LSTM/GRU processes a sequence of pitch and roll values. Both systems would make a prediction from which the average is taken as result. But once again, this study only provided a solution for single value prediction instead of sequences.

While providing good solutions for ship motion prediction, all above mentioned research fails to meet the requirements for this thesis. They either only predict one future datapoint or they don’t use images. Only one publication was found by **Nazar-Mykola Kaminskyi** where both images and sensor data were used to predict a sequence of data (Kaminskyi, 2019a). Kaminskyi explored different neural networks that can predict the motion of a vessel based on pitch, roll and incoming wave images. The different model designs all used a combination of CNN, LSTM and linear layers with the ones using images and data showing the best performance. He created a dataset that was used for the majority of this thesis and provided research and results that are directly comparable unlike other studies. However, his research lacked a comprehensive evaluation of the used models, and he also did not perform any latency testing. Both will be addressed in this thesis to form a more concise and robust solution that also fully complies with our needs.

In conclusion, deep neural networks provide a state-of-the art solution for ship motion prediction. The fact that they require little knowledge of the underlying physics makes them very accessible. This is clearly visible in the current lay of the land as a majority of found studies on ship motion prediction proposed some form of neural networks. However, due to the virtually unlimited possibilities presented when designing a neural network architecture, finding the optimal one is not unambiguous. This thesis will explore different possibilities in search of finding an optimal architecture for the given simulation data.

### Hybrid models

Hybrid models are models that combine dynamic modelling and deep learning to achieve better performance. In one paper, a neural net is used to correct the prediction made by a dynamic model (Wei et al., 2022). In another study, a hybrid model is applied for ship trajectory prediction based on current, waves and wind (Skulstad et al., 2021). These studies show that these hybrid models can also be highly effective in different ship motion prediction applications. However, this approach was not chosen due to the complexity of both the dynamic model and its integration with deep learning concepts.

## Artificial neural networks

Neural networks, also referred to as artificial neural networks (ANN) are the building blocks of deep learning problems. These problems are a subset of machine learning. They are composed of algorithms that permit software to train itself to perform tasks by exposing a layered neural network to vast amounts of data. Neural networks are structures inspired by the human brain and more specifically the neurons within and how they pass signals from one to another. However, similarities end beyond their connected structure.



Figure 4: Neural network structure (left) and a linear neuron (right)

A neural network consists of different layers which consist of multiple neurons. These neurons are connected to other neurons in adjacent layers and pass data forward over these connections. The input of one neuron is the output of all its preceding neurons it is connected to. Each neuron applies a weight and adds a bias to all its inputs and passes the aggregated resulting value forward. This way data is fed forward through the network and updated in every neuron. At the end of the network, the resulting value is compared to a ground truth value. After which, every neuron updates its weight and bias via backpropagation to improve its predictions.

There are three main parts in a neural network, the input layer, output layer and hidden layers. The input layer has the same number of neurons as the features in the input data. For example, when simulation data is used and only pitch and roll are used, there are two input neurons. The output layer size equals the number of features one wants to predict. In our case – with the real data – the output features will be pitch, roll and heave.

Different architectures exist for different applications, each with their strengths and weaknesses. In this thesis, sequential data will be used which contains numeric data as well as images. Because of this, different architectures are utilized that are designed to perform best with these kinds of data. Since no single model architecture exists that can handle all data well, different architectures will be combined to form hybrid models. In the following sections, all components and network architectures that play a role in this research are explained.

|  |  |  |
| --- | --- | --- |
| **Linear** |  |  |
| **Rectified linear unit (ReLU)** |  |  |
| **Sigmoid** |  | Afbeelding met onscherp  Automatisch gegenereerde beschrijving |
| **Hyperbolic tangent** |  |  |
| **Binary step** |  |  |

Table 1: overview of different activation functions

### Activation functions

In every neuron the weighted sum of all input is taken, and a bias is added. This aggregation results in a new scalar value that is passed through an activation function before moving to the next layer. The activation function, also referred to as the transfer function, applies a linear or nonlinear transformation to this scalar to limit its output to a certain range. This is especially useful for classification problems where an activation function such as the sigmoid function can be used to limit the output of a neuron to a range of zero to one. The output can then be interpreted as the predicted probability of the input belonging to a specific class. For linear regression problems where a numerical value needs to be predicted like pitch or roll, a linear activation is used. In Table 1, some common activation functions are shown together with their graphs. The sigmoid function and hyperbolic tangent are both used in LSTM networks while fold functions are used by pooling layers in CNN networks. Fold functions are special activation functions that perform aggregation over the results to take the mean, minimum or maximum.

In conclusion, different activation functions are used for different use cases. To predict numeric values such as pitch and roll, a linear or tanh (when input is normalized to [-1, 1]) activation is used in the very last layer. However, hidden layers can use different activations to limit the output of their neurons. This way the network can decide whether each hidden neuron’s output is important and should be activated. The choice of the activation function can heavily affect a model’s performance (Sharma et al., 2020). As a future reference, ReLU and the hyperbolic tangent will both be used in some proposed models in chapter 3.

### Auto-encoders

Auto-encoders are a type of neural networks that are designed to efficiently copy its input to its output. More specifically, the input gets encoded into a compressed representation, and then decoded or reconstructed based on this encoding. There are two main parts that make up an auto-encoder: the encoder and the decoder. An auto-encoder also holds two main characteristics: the number of neurons in the input is the same as the output and secondly, the hidden layers serve as bottleneck. This bottleneck forces the model to learn only the most prominent features of its input data that are needed to reconstruct it as accurate as possible (Lopez Pinaya et al., 2020).

The encoder part of an auto-encoder is capable of creating a sparse representation of the input data that holds as much information as possible. This property can be used to train an auto-encoder on the images and use the encoder part as a pretrained feature extractor for the images. This concept is applied in the work of Kaminskyi. He used the encoder part of an auto-encoder as a pre-trained feature extractor. The auto-encoder was trained once on the simulation images and could afterwards be used without the need of retraining. However, in this research, the encoder decoder configuration is used in a more liberal approach where two neural networks work together. One is used to encode the input and a second one is used to decode this encoding and make new predictions based on the encoding. This form of auto-encoders is commonly referred to as variational auto-encoders where input is encoded to decode into new outputs instead of reconstructing the input (Kingma & Welling, 2019).

### RNN and LSTM layers

Recurrent Neural Networks, RNN are special neural networks designed to work with sequential data (Sherstinsky, 2018). Sequential data is data where the order is important, for example time series data, sentences, audio etc. Ship motion data like pitch and roll fall within the time-series data category. The same goes for video footage or consecutive images where frames should be processed in a specific order. The learn this relation between consecutive datapoints, RNNs are introduced.



Figure 5: Neurons in a recurrent neural network with additional feed-back connections

To efficiently learn from ordered data, each neuron passes its output forward to the next layer and back into the next neuron in the same layer. Each neuron in an RNN network uses an output that is fed back and a new input to make a prediction. This is the main concept in RNNs and difference between feed-forward networks. However, as illustrated in Figure 5, RNN network neurons only pass the previous output back into the network, therefore it only “remembers” the short-term history in the sequence. This causes the model to “forget” its long-term history or in other words: the model losses perception on the general trend of the sequence.

LSTM networks provide a solution to this disadvantage by not only using a short-term memory but also saving a long-term memory state (Hochreiter & Schmidhuber, 1997). Each neuron of an LSTM network receives three inputs: the input data, the previous output (short-term memory) and the long-term memory state. The short-term memory and long-term memory are called the hidden state and the cell state respectively. Within the cell, four components are used to update these states and produce new states and an output. These four components are gates, each with their own function: input, forget, update or output. The gates use activation functions to decide whether to let information through, “update”, or block information, “forget”. This way, the LSTM-cells gradually learn what information should be kept for long-term memory and which information can be discarded.

Because of their design and beneficial characteristics, LSTM networks will be the main building blocks for the deep learning models proposed in this thesis. They should be able to learn the trend of the ship’s motion and make accurate predictions based on this trend. However, LSTM architectures are not the only viable option for sequence-to-sequence prediction problems. Different variants exists such as peephole LSTM networks and gated recurrent units, GRU. These will be discussed more in the discussion chapter.



Figure 6: LSTM-cell components (left) and their mathematical notations (right)

### Convolutional Neural Networks

Besides sequential numeric data, there are also images available to aid with the prediction process. However, LSTM networks and standard linear networks are not very efficient when working with image data. Because of the way an image is represented, see below, the number of parameters in these networks ramp up very quickly, even with small images. This causes the networks to train and generalize very slowly. Therefore, a second architecture is introduced: convolutional neural networks, CNN. These networks are highly effective when dealing with images (Wu, 2017).

Images are represented as three-dimensional matrices where every element in the matrix represents the intensity of a channel for a specific pixel. The width and height of this matrix are equal to image and the depth is the number of color channels in the image. When this data structure would be used for a linear neural network, the matrix would have to be flattened into a one-dimensional vector to feed into the first layer. This way all two-dimensional information is lost. CNN networks solve this problem by extracting features from the images with two-dimensional convolution kernels.

A convolution kernel or filter is a square matrix. Each element within this kernel contains a weight value. During a convolution, the kernel is moved over the matrix representation of the image and applies each of its weights to the corresponding pixel value as illustrated in Figure 7. The result is a new value placed at the center of the current kernel position. Because the kernel is a two-dimensional matrix just like the image, no information is lost, unlike when flattening the image. The kernel is moved across the whole image while repeating the same process. After one convolution, the result is a filtered image with more accentuated features. In typical fashion, multiple convolution layers are connected to allow each consecutive layer to extract more precise features such as wheels, eyes, windows etc. During the training process, the network learns the best values for each weight in the kernels to extract the most prominent features. In the case of incoming wave images, the network is expected to extract the form of the waves in the images. Because the wave images are colored, they contain three channels (red, green and blue) and thus three kernels are used – one for each channel. If images are loaded in grayscale however, only one channel is present.

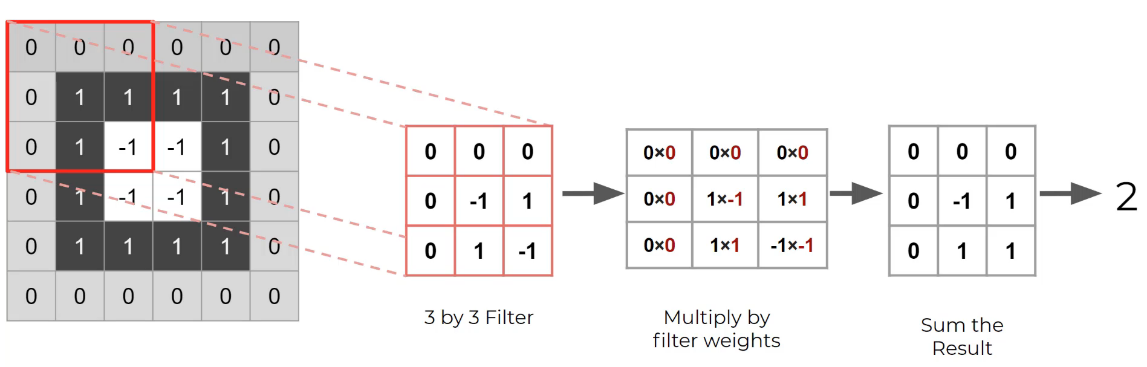


Figure 7: Convolution over grayscale image with 3x3 kernel

Two important parameters are used when dealing with convolutional layers: the kernel size and its stride distance. The first one sets the dimensions for the kernel matrix while the stride determines how many steps forward the kernel moves before calculating a new filter value. Additionally, padding can be added to the border of the image to prevent data loss. This allows the filtered image to remain the same size as the input after a convolution. Otherwise, each convolution would remove one layer of pixels around the border of the image. This is because each resulting value is placed at the center location of the kernel in a new matrix. Padding values are mostly all white or all black pixel values normalized with the method at hand.

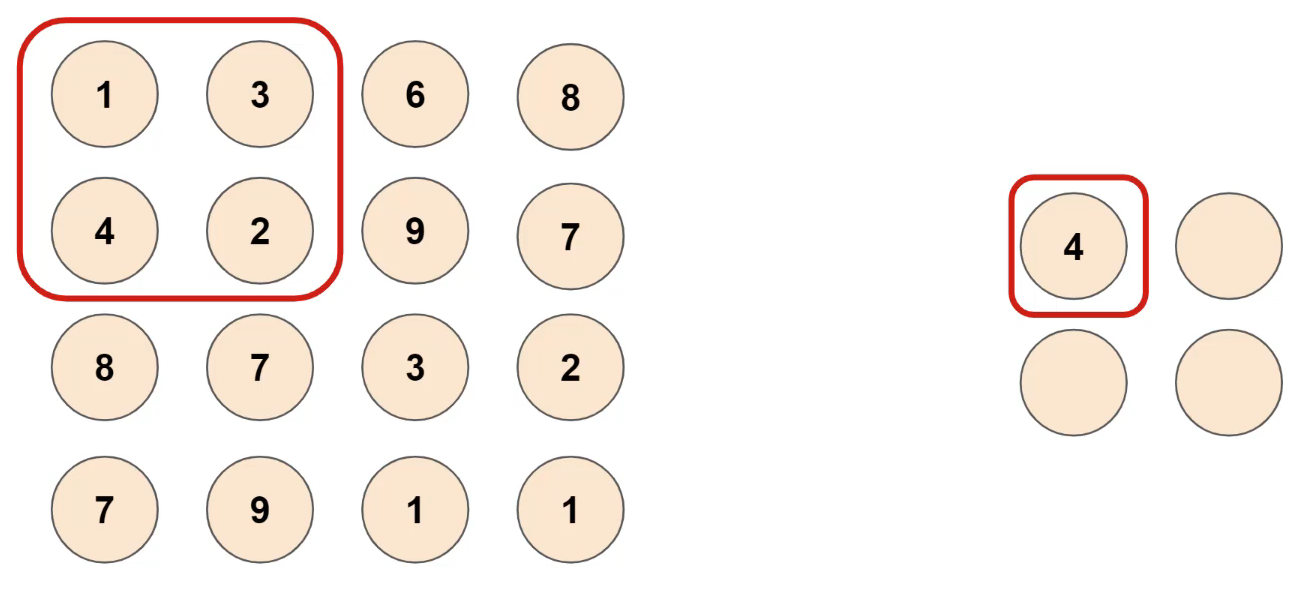


Figure 8: Max pooling with 2x2 kernel

A convolutional neural network still has a very large number of parameters despite being more efficient than linear networks. When dealing with colored images and a lot of filters, tens to hundreds, a method is needed to reduce the number of parameters. Pooling layers can be used to reduce this. A pooling layer samples the filter size down by applying a function to different subsets of data from the filter. The process is very similar to a convolution where a kernel is moved across the filter. However, the kernel has no weights. Instead, it takes the maximum of the values in the filter on a basis. This method is called Max Pooling. For example, if a kernel is used, four data points of the filter will be down sampled to one (Figure 8). If the kernel is moved forward two places on each iteration, this configuration leads to a 75% reduction in data. Another method is called Average Pooling where the average is taken from the kernel-sized subset.

## Tools

To develop the deep learning neural networks, Python 3.8 was used. Python is a high-level, general-purpose programming language that is in - most cases - most suited for machine learning applications. To facilitate the development of the deep learning models, different packages were used. The most important of which are briefly discussed below.

Pandas, Seaborn and NumPy were used to process and manipulate data. NumPy provides functionality to perform mathematical functions on large datasets with multiple dimensions. Pandas provides the functionality to visualize and order the data in its Data frames. Seaborn was mainly used to perform data analysis on the numeric data such as pitch and roll, to assess and visualize statistical information between features. To plot training and test results, Matplotlib was used.

For the implementation of the deep learning models, PyTorch was used. PyTorch is an open-source framework for machine learning applications that allows fast development and ease of use. PyTorch was used together with the cudatoolkit extension. This enabled the models to be trained and tested on a dedicated graphics processing unit (GPU) to increase computing performance.

Blender was used to generate a dataset from an ocean wave simulation. Blender is an open-source three-dimensional creation suite that can be used for many purposes. In this case, it was used to simulate incoming waves on a vessel. The data itself will be discussed more in detail bellow.

All code was written in Jupyter Notebook for its ease of use and simple debugging. Whenever parts of the code in the notebooks were tested thoroughly, they were extracted to standalone Python files and accessed via import statements.

## Expected performance

To evaluate the performance of each model and their viability as possible solution based on the requirements discussed in the objectives, all models are subjected to a set of minimum criteria. These criteria set baselines to which the model will be compared. Note that the criteria defined in this subchapter are set for use only in the simulation environment. A model is fit to be used with real data only when it meets the simulation criteria. These criteria were determined based on related work, primarily on the study by Kaminskyi, and desired expectations. The reason why Kaminskyi’s results were primarily used as a reference is because of the dataset he used. He created and used a simulated dataset of incoming wave images and corresponding pitch and roll measurements that is publicly available. This same dataset was also used for our research which makes his results directly comparable to ours. Additionally, no other research was found where implementations of methods or neural network source code were publicly disclosed. If this would have been the case, results taken from those methods on our dataset could also be used as a comparison.

In Kaminskyi’s research, vastly different performances were measured between different model designs. The LSTM model that processed only pitch and roll as input performed worst, followed by the CNN models that only used images. The best performance was achieved by ensemble models using both pitch and roll and images. The errors of each model are shown in Table 2 with the worst and best performing model highlighted in resp. red and green. These errors were calculated as the average difference between prediction and real values at the tenth predicted second. Models were tested in a configuration where ten seconds were used to predict twelve (resp. 20 and 24 frames at 2Hz). For reference, the model naming convention in his research is a combination of used inputs and architectures. For example, *PR* means that pitch and roll are used as input, *stack* means that a stack of images was used as input and *FC* means that a fully connected linear layer is used. More information on the model design and naming can be found in his report.

|  |  |  |
| --- | --- | --- |
| Model | Pitch at 10th second  [denormalized RMSE] | Roll at 10th second  [denormalized RMSE] |
| LSTM encoder decoder PR | 30.99° | 29.44° |
| CNN stack FC | 28.97° | 28.94° |
| CNN stack FC PR | 21.18° | 22.56° |
| CNN FC PR | 11.36° | 11.28° |
| CNN LSTM image-encoder PR-encoder decoder | 3.56° | 2.83° |
| CNN LSTM encoder decoder images PR | 2.89° | 2.70° |
| CNN LSTM encoder decoder images | 3.42° | 2.32° |
| CNN LSTM decoder images PR | 4.22° | 4.16° |

Table 2: Kaminskyi's results for different models with worst (red) and best (green) model highlighted (Kaminskyi, 2019a)

The red and green rows respectively highlight the worst and best performing model based on prediction errors at the 10th predicted second. These errors are calculated as an average over all predictions made on an unseen dataset. In blue, the absolute lowest measured error value is highlighted. However, the model that resulted in this low roll error was not selected due to its high pitch error in comparison. Both pitch and roll are equally important when estimating the state of the vessel and thus the two similar and low prediction errors of the green model are more optimal than two low yet disproportional errors. The green and red model serve as a reference benchmark to evaluate the models proposed in this research.

Below in Table 3, similarly calculated errors are shown of the best performing model after fully optimizing its parameters with the HyperBand algorithm (Li et al., 2016). The error values show the model’s capabilities to predict longer future sequences and represent the average error over a series of predictions at different time-steps. For reference, when predicting a thirty second window, the model needs to predict sixty future datapoints at 2Hz.

|  |  |  |  |
| --- | --- | --- | --- |
| Parameter | 10th second | 15th second | 30th second |
| Pitch | 2.89° | 2.92° | 3.06° |
| Roll | 2.71° | 3.75° | 4.92° |

Table 3: prediction error at different future time-steps of Kaminskyi's best model (Kaminskyi, 2019a)

Based on these results, a general idea was formed about expected performances on the given dataset and criteria were set accordingly. The following properties of the model must comply with the next requirements. Firstly, the **average error** on the time-series predictions at the 10th second should be no more than three degrees and no more than five degrees at the 30th predicted second. These values are chosen in assumption that the accuracy of any model decreases as it predicts further in the future. The errors should be calculated as the average over all predictions on a large dataset with unseen data (data that was not used for training). Secondly, all models will be compared to a ***zero-predictor***. This is a hypothetical model that predicts a zero for each frame in the output. Models performing worse than the zero-predictor did not learn at all and can be classified as random generators. Finally, the prediction latency or **inference** **time** of the model should be as low as possible. The inference time should be measured as the average over ten thousand predictions with a batch size of one. The batch size is chosen at one as the model will not be able to predict more than one sequence at one time when predicting on live data-streams. There was no research found comparing similar neural network designs compared to ours. But some very popular state-of-the art neural networks like ResNet-18 (He et al., 2015) and GoogLeNet (Szegedy et al., 2014) show inference times between 30 and 150 milliseconds with a batch size of one (Canziani et al., 2016). These values can serve as a reference. If possible, the testing on latency should ideally be expanded towards also testing the model’s hardware usage as resources will be limited when being deployed.

Whenever a prediction sequence is calculated, it should be analyzed by an algorithm. This algorithm will search the sequence for a window of landing/take-off opportunity. During this window, heave, roll and pitch should remain close to constant over a duration of continuous time. However, different drones have different characteristics and requirements to and. For example, the range of motion for pitch and roll of the hovering drone in which it remains stationary. To compensate for this, the parameters of this window should be easily changeable to the needs of the drone at hand. These are just some starting principles as this algorithm falls out of the scope of this thesis

## Summary

In this chapter, the state-of-the-art in motion prediction was briefly discussed. Additionally different methods were introduced to predict wave-induced ship motions. The conclusion was made that for many years, ship motions were predicted based on dynamic modelling of the physics involved. However, due to the non-linear non-deterministic nature of ocean waves and their interaction with ship motions, setting up an agile and accurate quickly becomes extremely complicated. For this reason, deep learning neural networks were chosen as an alternative solution. It is hypothesized that this modern approach can learn the complexity of dynamic models solely based on examples. Their accuracy and effectiveness on an ocean wave simulation will be evaluated in this thesis. The evaluation will be based on criteria that were defined based on results from related studies and expectations. In addition, all used concepts of neural networks were introduced as a reference to future mentioning in the paper. LSTM and CNN networks will be used primarily in the design of proposed neural network architectures due to their efficiency in resp. capturing trends in sequential data and extracting features from images – which are both important given the dataset that will be used.

# Data collection and preprocessing

The first step of any machine learning operation is collecting data. For this thesis, data was collected from two sources as discussed in the introduction. A dataset from simulation and real-world data was used. This poses some challenges as the simulation data is captured in an ideal scenario and contains less motion parameters as the real-world counterpart. This can cause the models to perform differently and have slightly different architectures due to the different inputs and outputs based on the available data. In the following two sections, both datasets will be discussed in more detail. For the remainder of this thesis, the different parameters such as pitch, roll, yaw etc. will be referred to as the *features* of the dataset.

## Simulated data

During most of the development, a simulated dataset was used from an ocean wave simulation made in Blender (Kaminskyi, 2019b). This dataset was made by Nazar-Mykola Kaminskyi and is publicly available through GitHub. It was not made by or in cooperation with the research group of this thesis. Simulation data was needed for training and testing purposes during the initial phases of development when real data from the ASV was not yet collected and available.

For this simulation, a standard model of a vessel was used which is floating on the simulated sea surface and moves along with the waves. This presents the issue that all models trained with this data will be biased to this vessel’s characteristics. A large, heavy vessel will behave vastly different opposed to a small, lightweight vessel. Therefore, all models should be retrained and re-evaluated with real data from the vessel it will be used on, as this vessel will most likely have different characteristics. However, this issue can also form a way to compare how well one model can predict the motion for different vessels. If there are only minor increases in performance when the model is retrained with data from the specific vessel, it might be more useful to use one general purpose model for all vessels with similar characteristics.

Using a simulation also presents a second issue: perfect conditions. The data taken from the simulation is from a perfect scenario, meaning that there are no obstructions or other objects on the images. The images are also perfectly stabilized on the moving vessel. This can cause models that are trained on the simulation data to perform very well in simulation yet fail to meet desired expectations in a real-world scenario. To minimize this effect, data can be augmented to include more variation, or adjustments can be made to the simulation to make it more realistic such as including passing vessels in the images. Finally, since the data is generated by a computer, a computer might be able to capture the trend a lot better than naturally occurring data. A simulation can be very realistic, but behind the scenes there is still just an algorithm with parameters that a neural network might be able to learn very quickly.

The simulated dataset contains images of incoming waves (figure 10) and the pitch and roll values of a vessel floating on these incoming waves. The data was generated in 540 different episodes, each episode containing 400 frames of data. The frames were captured at two frames per second to minimize data overlap in consecutive images. Each frame contains one image together with the state of the vessel at the time of the image in the form of a pitch- and roll-value tuple. In its totality, this dataset contains 216.000 frames, which translates to thirty hours of simulated data at two frames per seconds. All episodes were structured in the same way. Images were named 1 to 400 and pitch and roll data points were included in a *JSON* file. The pitch and roll couples were numbered 1 to 400 as well to easily identify which image corresponds to which tuple.

With this simulated data we only have access to pitch and roll as input data. This means that during testing in the simulation environment, heave cannot be predicted. However, with the neural networks that will be proposed later, this should not be a big issue for two main reasons. First off, heave follows a somewhat predictable pattern in regular conditions as depicted by figure 4. Because of this, it was assumed not necessary to regenerate the full dataset for just one extra output. It was also assumed that if the model performed well on pitch and roll, it should consequently perform well on heave. Secondly, adding extra input and/or output features to a neural network architecture, is not an expensive operation. It is highly likely that all models will have to be retrained when switching from the simulation environment to a real-world environment to adapt to the new vessels’ characteristics and the additional data available from the ZED-mini. The difference in performance of a retrained and non-retrained model remains a topic for future work.



Figure 9: Generated images of incoming waves (chronologically ordered left to right, top to bottom)

### Simulation parameters

To simulate this data, different parameters were used to finetune the simulation environment. The effects of these parameters on the simulation were not tested as the used dataset was already generated with fixed parameters. However, assumptions can be made on how they would affect the simulation. The most important parameters will be discussed briefly.

As mentioned above, the images were taken at two frames per second by a virtual camera. The position of the camera on the simulated vessel was set with the following parameters:

* Height: *5 meters*
* Rotation around x-axis: *76 degrees (slightly tilted downwards)*

The images were captured in a low resolution to decrease the memory requirements to load the dataset. The following resolution parameters were used:

* Height: *54 pixels*
* Width:  *96 pixels*

### Data augmentation

When the ASV is operating in open seas, the images of the incoming waves will be mostly free of obstructions. However, when the ASV is close to land, other objects may be in front of the ship like other vessels, shorelines, etc. To better evaluate performance in these real-life environments, a small subset of the simulated images were edited and added to a different separate dataset. Using an image editing software, ink blots were manually drawn on the images to resemble external objects in front of the ship. The shape, size and colors of these blots were randomly chosen. In some cases, they may be very unrealistic. This was done in assumption that an even worse obstruction in the frames is very unlikely and the performance on these images serve as a baseline for the very worst scenarios. Some of the augmented images are shown in Figure 10. To test the performance on this augmented dataset, models were trained on the normal images. Afterwards, the results of the augmented sequence and normal sequence were compared.

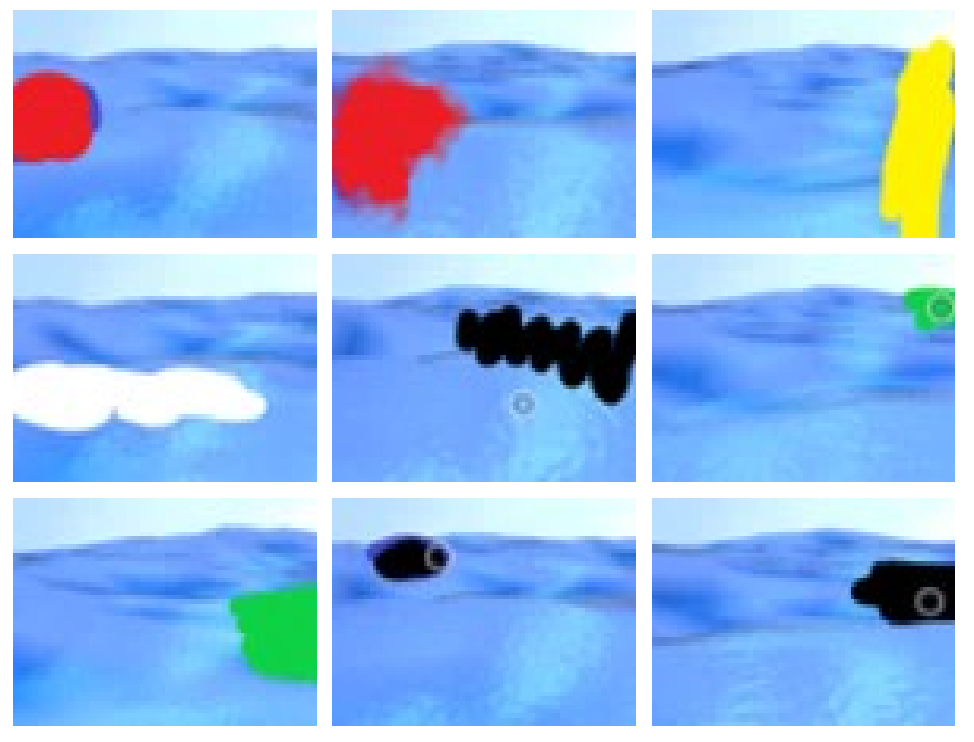


Figure 10: Augmented images

## Real data

Eventually, after evaluation on the simulation set, some prediction models will be selected for deployment on the ASV. This means that they will need to transition from simulation data to real data. To provide the real data, the target vessel is equipped with multiple sensors. However, due to the nature of sensory data, using this real data presents some challenges.

### Sensors onboard the ASV

The ASV is equipped with a ZED-mini stereo IMU camera (Figure 11) (StereoLabs, Paris, France). This is a multipurpose sensor that can capture video from its two cameras and numeric data from its Inertial Measurement Unit (IMU). The combination of these two sensors allows the ZED-mini to accurately describe the state of the sensor and its surroundings. The IMU has two built-in motion sensors: an accelerometer and a gyroscope. These provide a real-time data stream at 800Hz of the movement of the sensor along the rotational and translational axes.



Figure 11: ZED-mini IMU stereo camera (StereoLabs, Paris, France)

The two forward facing lenses on the ZED-mini provide stereo video. This can be used to map the objects in front of the ZED-mini in a three-dimensional space. A stereo image is a combination of two separate images that are captured from two slightly offset point-of-views (PoV) such as the lenses on the ZED-mini. These two PoV’s imitate the left and right human eye and create a perception of depth when the two images are fused together to create one stereo image. This process is called stereoscopy. In computer vision, these two images can be compared to each other to extract three-dimensional information from two dimensional images.

### Sensory data challenges

The real data will be captured and fed into the model at real-time. This means that the data stream will have to be cleaned and filtered to the desired input format according to the prediction model’s requirements. As mentioned above, numeric motion parameters such as pitch and roll, are captured by the ZED-mini at 800Hz. This means that every second 800 data points are measured. At this frequency, consecutive measured values contain a lot of overlapping data where minor change is happening between values. Therefore, the data stream will have to be reduced to minimize this data overlap add avoid overloading the prediction model with noisy data. Since the simulation data was generated at two frames per second, 2Hz should be a good starting frequency to reduce down towards to test the models. Later on, this frequency can be increased or further decreased depending on the model’s performance and inference time.

Similarly, the video framerate from the stereo camera should be reduced to minimize data overlap between consecutive frames and reduce computational requirements. The video footage will also have to be compressed to reduce the memory and computational requirements needed to process a sequence of images.

*(From this point in the thesis and onward, only the simulation data is used due to unavailability of real data)*

## Data pre-processing

Before the images and numerical data can be loaded into the model, they need to be processed. This pre-processing of data is necessary to enhance to performance of the models and ensure that the model operates correctly. Due to a simulation dataset being used, little pre-processing is needed since the data is collected in a predefined format.



Figure 12: Scatterplot of pitch and roll

### Data cleaning

The first step of data pre-processing is data cleansing. In this step, data points are checked for inaccuracies and corrupted values. Odd data points are corrected or removed, and unnecessary features are dropped from the dataset.

In the case of the simulated dataset, this task is rather short as the data was generated following a specific format as discussed in 0. To cleanse the simulated data, all episodes were evaluated to contain 400 images and 400 pitch and roll couples. If this was not the case, there might have occurred and error during simulation at which point the validity of the sequence is infringed. Next, all pitch and roll values were audited to not contain any odd values such as un-numerical values or extreme outliers. This was done with *Pandas.isnull().values.any()* and *Pandas.DataFrame.plot.scatter()*. The scatter plot (Figure 12) shows the two-dimensional layout of pitch and roll. The data is mainly concentrated in the middle with few outliers and no sign of skewing. Further analysis of the distributions will be conducted in 3.4 data analysis.

When real data is used, comprehensive cleaning will be required to filter out noise from the sensors and excessive outliers from inaccurate readings.

### Data formatting

All data features fed into a neural network must be formatted in the same way. This means that all features containing numerical data should be converted into the right datatype and images should be resized to the same resolution. Textual data should also be pre-processed but this falls outside the scope of this thesis as no textual data will be used. This formatting is particularly important as incorrectly formatted data cannot be used to train and test neural networks.

For the simulation data, little formatting had to be done. All images were generated with the same resolution, so image resizing was not necessary. The pitch and roll values were imported from JSON-files as textual string data. They were subsequently casted to 64-bit floating point values for high accuracy.

### Data reduction

Because the data was generated by a simulation, values and images are captured in a desired format. This means that little to no data reduction is necessary. All images were captured with equal dimensions that are small enough to eliminate the need for additional compression or cropping but large enough to keep an adequate level of detail. The small dimensions also allow for lower computational requirements. The data was simulated at two frames per seconds (fps) or 2Hz in assumption that this is a good trade-off between minimizing overlapping data in images without introducing aliasing on the pitch and roll signals. The frequency of the simulated data can be reduced to a lower fps by dropping a certain number of frames between each loaded datapoint, however this was performed in this thesis.

Determining the optimal frequency depends on an accuracy trade-off and environmental parameters. Higher fps increase accuracy but introduces more overlapping data in images, Additionally, it may introduce *landing window noise*. This refers to small changes that have negligible impact on the landing window but may negatively affect the learning process as the model tries to learn this noise. Lower fps decreases the amount processing needed but may introduce aliasing as mentioned above. The inertia of the vessel at hand plays a significant role as well. Large, heavy vessels move a lot slower compared to smaller, lightweight vessels. Because of this inherent law of inertia, the latter will probably benefit from a higher data sampling frequency because it allows faster movement changes due to its lower inertia. This also implies that a neural network trained on data from a small ship might not perform very well for larger ships and should therefore probably be retrained. The period of the waves may also play a part in determining the optimal sampling frequency. According to Stewart H. Robert, ocean waves remain within frequency of approximately 12 to 24 waves per minute – resp. 0.2Hz and 0.4Hz (Stewart, 2008). Using this information, it was concluded that 2Hz is adequate for even the highest wave periods.

### Data normalization

When one feature contains values in a range of [0, 100] and another feature contains values in a range of [0, 5], the first feature will have a much larger impact on the result if they are used together. For this reason, data needs to be normalized.

Pitch and roll are normalized with min-max feature scaling. This method rescales values relative to their absolute maximum and minimum within a [-1, 1] range. Since pitch and roll define the tilting of a ship, the absolute theoretical minimum and maximum were chosen to be -90° and 90° (**Fout! Verwijzingsbron niet gevonden.**). If a ship pitches or rolls beyond these values, it will capsize (Figure 13). It is also not possible to optimize this by defining the minimum and maximum equal to the boundaries of the measured values in the dataset, because these numbers are not known when working in real-time.

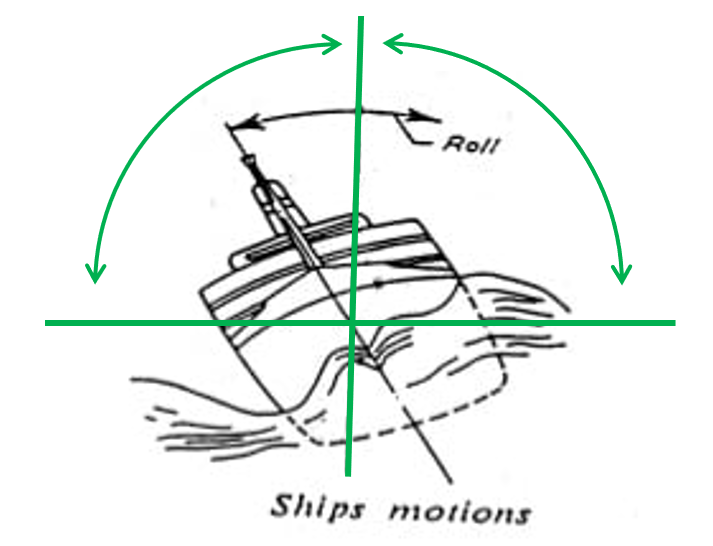


Figure 13: Maximum range of rolling motion for ships

Each images needs to be normalized as well. Each image is three-dimensional matrix containing three values - the red, green and blue channel - for each pixel in the image across the length and width. This means that for every pixel, three values need to be normalized. The three channels indicate the amount of red, green and blue in each pixel. These values are 8-bit integers, meaning that they range from 0 to 255. To normalize them, a similar min-max feature scaling function was used as for the pitch and roll values (**Fout! Verwijzingsbron niet gevonden.**)

## Data analysis

The simulation data was briefly analyzed to have a better understanding of the results. Very in-depth analysis of the input data in not necessary for deep learning applications. Deep learning is a form of unsupervised learning, where the model itself determines the importance of each feature. In comparison, supervised learning problems require thorough data analysis to find out which feature(s) have most impact on the desired output feature(s) and should be included in the models’ input. The goal of the data analysis in this thesis is to firstly better comprehend how they behave and secondly the interactions between pitch and roll.

### Statistical properties

First off, basic statistical information was extracted from all pitch and roll data points from all episodes. With the built-in function of Pandas *pd.DataFrame().describe(),* this is easily achieved. The results are shown in Table 4.

|  |  |  |
| --- | --- | --- |
|  | Pitch | Roll |
| count | 216.000 | 216.000 |
| mean | 0,0678° | 0,303° |
| standard deviation | 6,611° | 7,022° |
| minimum | -53,721° | -58,846° |
| 25% | -2,761° | -2,572° |
| 50% | 0,0262° | 0,230° |
| 75% | 2,876° | 3,187° |
| maximum | 61,328° | 62,217° |

Table 4: Statistical information for pitch and roll in simulated dataset

The count refers to the amount of datapoints analyzed, which is equal to the 540 episodes each containing 400 frames. The quartile percentages at 25% and 75% show a similar interval for both pitch and roll. Additionally, pitch and roll respectively are centered around approximately zero degrees. This is based on their nearly identical mean and median, meaning that 50% of their values are lower and 50% are higher. This is expected behavior of a normal floating vessel that naturally wants to remain upright. Lastly, it was observed that roll had a slightly higher standard deviation, which indicates that its values generally deviate further from the mean than those of pitch. From these properties, it can be concluded that pitch and roll both behave similarly on a numerical basis across all fields. However, this does not necessarily mean that they physically behave similar. The minimum and maximum values give a good estimate of the interval in which the predicted values should remain. They also provide a means to normalize error values relative to these boundaries. When all data occurs in a [-60°, 60°] interval, an error of three degrees is a 5% error relative to the absolute maximum which is really good. If all data lies in a [-10°, 10°] interval, an error of three degrees is a 30% relative error which is very high. However, these minimum and maximum don’t tell the full story.



Figure 14: Simulated Pitch and Roll distributions

The distributions of pitch and roll are shown in Figure 14. Both of them are remarkably similar and show remarkably similar characteristics to a normal Gaussian distribution. Intuitively, it can be assumed that the majority of the datapoints are located in a [-20°, 20°] interval. Compared to the properties of normal distribution, this assumption is justified when the 65%-95%-99.7% rule is applied. This rule determines that given a mean **µ** and a standard deviation **σ** of a normally distributed dataset, respectively 65%, 95% and 99.7% of all datapoints lie within a **µ** ± **σ, µ** ± **2σ** and **µ** ± **3σ** interval. If this rule is applied with the mean and standard deviation from Table 4, the 99.7% interval can be calculated and are the following (values rounded down for readability):

* Pitch: *[-19,74°; 19,86°]*
* Roll: *[-20,70°; 21,30°]*

These intervals confirm that nearly all data points – 99.7% – lie within the above intervals. Because of this, the RMSE should be taken relative to these interval boundaries rather than the maxima and minima of the full dataset. The 99.7% intervals represent almost all data whereas the minima and maxima could be two extreme outliers.

### Correlation and interactions

Secondly, the correlation of pitch and roll was reviewed to assess the influence of roll on the prediction of pitch and vice versa. This was done to decide if having both motion parameters as input is necessary for the predictions on one or the other feature individually.



Figure 15: Correlation matrix for pitch and roll

A commonly used method for analyzing correlation is a correlation matrix. This is a symmetric matrix where the number of rows and columns equals the number of features. Each cell in the matrix contains a value equal to the correlation of the features of the corresponding row and column. These values range from -1 to 1 where -1 indicates a strong negative correlation, 1 a strong positive correlation and 0 indicates that there is no correlation. From the matrix in Figure 15, pitch and roll have a correlation close to zero, which indicates little to no correlation.

With this result, it can be assumed that one feature has negligible contribution to the prediction of the other feature. Providing additional features besides the predicted feature can therefore be seen as overhead for the model. However, this assumption is only based on numerical values from a simulation containing only pitch and roll. According to this research (Nayfeh et al., 2012), pitch and roll are coupled nonlinearly when their frequencies are in a ratio of two to one. On top of this, more correlated features could be introduced with the additional input features from the ZED-mini sensor.

With this information, it was concluded that standalone feature correlation was not enough evidence to rule out other possible physical interactions. Because of this, all models were designed to ingest all available features instead of dropping some due to low correlation with the predicted target features. In the case of the simulation data, this meant that models were trained and evaluated to predict both pitch and roll from an input sequence also containing both pitch and roll.

## Data loading

Data loading refers to the process of creating input-output sequences, splitting the data and creating batches in the correct format for network training. For each model, the inputs and outputs will be sequences with varying lengths. Next, these generated sequences will be split into three subsets for training, testing and evaluating the model. Finally, the data will be wrapped in PyTorch DataSet and DataLoader objects which will convert the data into Tensors and create batches.

### Sequence creation

The simulated data is generated in episodes. Each episode contains 400 frames that chronologically follow each other as previously shown in 3.1, Figure 9. However, the episodes themselves do not follow each other chronologically. Different episodes are generated in different simulation sessions and should therefore not be seen as continuous. Because of this, the data must be sequenced correctly to not include data from different episodes when used for deep learning models that ingest and predict chronological sequences. In short, all frames in the input and output sequence, should always be from the same episode.

For this reason, a dedicated function was designed to create sequences from a given dataset. One sequence consists of two parts, an input sequence and an output sequence. The input sequence is the data used to predict the output sequence. The length of the input and output sequence can be passed to the function as a parameter to easily create different sequence configurations. This is necessary as the length of the input and output sequences will have a large effect on the performance of the model and will be thoroughly examined. In addition, the function also accepts parameters to define the input and output features when different datasets are being used that contain more features.



Figure 16: Sequence creation with moving input and output sequence

In Figure 16, the sequence creation process is illustrated on an episode with the number of frames being equal to **s** and the input and output sequences having both a length of five. In the first step, the function takes the first five elements which form the input sequence used to predict the next five elements: the output sequence. These two sequences are then coupled together and added to a list with all sequences. In the second step, the starting point for the sequences is moved to the next element and the same procedure is conducted, extracting and coupling an input with an output. This process is repeated until the end of the episode is reached. At this point, a new episode is loaded on which the cycle is repeated. The result is a list of all possible input-output sequences that only contain consecutive datapoints from within a same episode.

### Train-test splitting

After the sequencing is done, the list of all coupled input-output (IO) sequences is split up in two subsets: one for training the model and one for testing the trained model’s performance. This splitting is necessary to properly measure how well a model can generalize what it learned to new data.

When a deep learning neural network is trained on a dataset, it will optimize its performance as much as possible on this training dataset. If all available data is used for the training dataset, the model will have consumed all data at least once, leaving no unseen data for testing. Therefore, in order to evaluate how well the model generalizes to new data, a second dataset is needed. This test dataset contains data that the model has not seen before and is not optimized towards, unlike the training data. As a result, if the model generates predictions on this second dataset, its true performance on new data can be evaluated. After this evaluation, the training parameters can be adjusted, and the model can be retrained to further optimize performance.

To achieve this split, elements from the list of coupled IO-sequences are randomly selected and assigned to one of the two subsets. This randomization has positive effect on the model’s performance because it mitigates possible trends in the initial dataset. For example, due to pure coincidence it is possible that the first ten IO sequences are from calm seas and the next five are from rough seas. If this dataset is split using normal forward iteration over the data - adding the first ten IO-sequences to training and the next five to testing - the model will perform very poorly as it never had the chance to learn the rougher sea’s trends. Thus, the data is split with random selection. Additionally, since sequential data is used, consequent IO-sequences will have some data overlap. Figure 16 shows this more clearly: the sequences from the 1st and 2nd step are very similar. When random selection is used, the effect of this data overlap is minimized and IO-sequences in one batch contain the maximum amount of unrelated data.

### PyTorch batching

Finally, after the pre-processed data is sequenced and split in two subsets, IO-sequences are divided in batches and prepared in the specific format for the neural network. Since all neural networks were implemented with PyTorch, it was most convenient to load the data with PyTorch reusable classes. The two different datasets – training and testing – are each wrapped inside a PyTorch DataSet object. This class stores the IO-sequences in an iterable and indexable data structure that can be used by a PyTorch DataModule. The DataModule stores the two DataSets and makes them accessible via multiple DataLoader objects, one for each DataSet. Each DataLoader divides its DataSet in small batches for batch processing. The size of the batches is an important hyperparameter and determines how much data the model will consume before updating its internal parameters. Batch size and its effects will be discussed more in detail in section 4.2.4.

While only two datasets were used during development, one for training and one for testing, three DataLoader objects were created. One for the training dataset, and two for the test dataset. The latter two used the same dataset but one of them used a batch size of one (test DataLoader) while the other used a batch size equal to the training DataLoader (validation DataLoader). By doing so, the test DataLoader could be used to evaluate the performance of the models on a sequence per sequence basis instead of only having access to batches of multiple sequences. Additionally, the validation DataLoader could be used to measure generalization and overfitting during training.

## Summary

This chapter discussed all subjects related to data collection and processing. The properties of the simulated data and real data were introduced. Both images and ship motion data were collected. However, due to the real data being unavailable for a majority of the project’s duration, there was insufficient time to work with real data and only the simulation data was used in this thesis. Some challenges were discussed when transitioning from simulated data to real data. These will have to be further assessed together with the transition in future work. Besides this, it was concluded that 99.7% of all pitch and roll datapoints lie within an approximate window of [-20°, 20°]. This is important when calculating relative errors based on minima and maxima. In addition, there was no correlation found between pitch and roll. However, studies have shown that pitch and roll can interact with each other and therefore it was concluded that despite the low superficial correlation, pitch and roll should always be used together as input data. Lastly, the data loading process was discussed. Data is first sequenced into corresponding input-output pairs. These sequences are then split into two separate datasets for training and testing. Finally, a PyTorch DataSet and DataLoader object are used to divide the data of these different datasets in batches and feed it to the models in the right format.

# Model designs

In this chapter, all model architectures and parameters will be discussed. An iterative process was used where each model increases in complexity in order to potentially increase performance. As discussed in the introduction, ensemble models combining different neural network architectures will be used to obtain optimal performance on the available data – images and numerical data. To visualize the model designs and input-output dimensions, illustrations were made and are added for each model. In addition, a table is provided with the specific parameters of each model. To identify different models based on their architecture, the following naming conventions are introduced. This nomenclature will also be used in the parameter tables and on the architecture illustrations.

|  |  |
| --- | --- |
| Notation | Explanation |
| P – R – PR | Resp. Pitch – Roll – Pitch AND Roll |
| img | Notes that images are used as input |
| LSTM | An LSTM architecture was used |
| CNN | An CNN architecture was used |
| FC | Fully connected linear layer |
| Single-/Multi-step | Prediction of a single time-step / sequence of time-steps |
| n | Number of frames in the input sequence |
| m | Number of frames in the predicted output sequence |

Table 5: newly introduced notations and their explanations

## Single-step model

The first network that was created was a single-step stacked LSTM architecture. This model uses a sequence of numeric input data for pitch and roll and predicts one future time-step (M = 1) - hence ‘**single-step**’ - of either pitch, roll or both. This model was designed to get familiar with the workflow of designing, training and testing neural networks with PyTorch. For simplicity, image data was omitted to allow for a simple model structure with relatively few parameters that can be trained quickly. Two variants of this model were trained, both having identical architectures with the only difference being that one variant can predict pitch *and* roll at the same time while the other can only predict *either* pitch or roll based on what it was trained for. This is reflected by the number of neurons in the output layer shown in Table 6, where *out\**  is equal to one or two neurons for resp. the single (P or R) or the dual output (PR) variant.

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| **Input** | **Sequence of PR at** | | | | | |
| *Name* | *Layers* | *Number of layers* | *Hidden size* | *Dropout* | *Input* | *Output* |
| LSTM | LSTM | 2 | 128 | 0.2 | 2 x N | 2 x 128 |
| Regressor | Linear | | | | 1 x 128 | 1 x \* |
| **Output** | **Single value for either P, R or PR** | | | | | |

Table 6: parameter table for single-step models

The single-step model consists of an **LSTM architecture** followed by a linear fully connected regressor layer. The general idea behind this design is that the LSTM computes a hidden vector on the sequence which represents the short-term memory of the LSTM. This hidden vector is then used to calculate the predicted output(s). To compute the hidden vector, a two-layered or **stacked** LSTM is used. In this configuration, the output of the first LSTM is passed to the inputs of a second LSTM. This configuration was chosen based on the research of Cui Z. in which the performance of both single layered and stacked LSTMs were compared in a similar forecasting context (Cui et al., 2020). The conclusion was that the stacked LSTM performed better than its single layered counterpart. Both LSTM layers use 128 hidden LSTM cells (neurons) and have a dropout of 0.2. These values were arbitrarily chosen and proved to achieve good performance. Dropout is a function that randomly disables certain neurons in the network. The value for dropout represents the chance of any given neuron to be disabled. Using dropout helps to reduce overfitting during training and thus improve stability and performance (Srivastava et al., 2014). Dropout is applied when data is passed between the two LSTM layers. The concept of overfitting is discussed later on in 5.1. The last layer is a linear fully connected layer, aggregating all the hidden features into a single output feature. Notice that the hidden output of a layered LSTM is a three-dimensional tensor with the following shape: (number of layers, the batch size, number of hidden neurons). It is built by appending the two-dimensional hidden vector of each layer one after the other in chronological order, numbered by their index. For the aggregation in the linear layer, only the hidden state from the last layer is used, hence the notation *hidden[-1]*. The single-step stacked LSTM model architecture is illustrated in Figure 17 with the single output variant on the left.

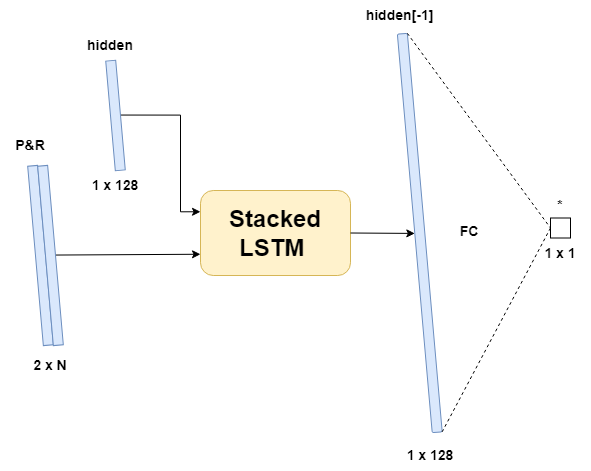
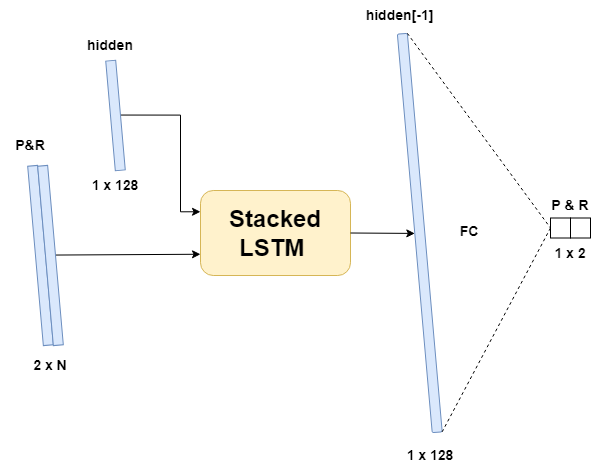


Figure 17: Single step model architecture variants: single output (left), dual output (right)

Due to its simplicity, this model also served as a testing ground to find good values for some important recurring parameters such as the size of the hidden layer and learning rate as well as for different configurations of activation functions. The model was trained with different values for these parameters to form a conclusion on what values worked well. From the results of this testing, later model designs could use similar hidden sizes and learning rates in assumption that they will behave similarly. This way, more efforts could be put in testing other parameters such as input and output sequence lengths. A more detailed discussion on these parameters is provided in 5.1.

## Multi-step models

The next step in development was to design models capable of predicting a sequence of pitch and roll. In addition, images are also introduced as additional input. The combination of these two expansions results in more complex model architectures. In the next sections, four new multi-step model architectures are introduced.

### Encoder-Decoder LSTM

The first model designed for multi-step predictions was an expanded version of the single-step model. The two-layered LSTM was replaced with **two single-layered LSTMs** in an encoder-decoder configuration. This design was inspired by a similar model of Kaminskyi, and by a model designed by Brownlee for power usage time series forecasting (Brownlee, 2018). This architecture was chosen to be implemented first because of its relatively simple design and because of its low expected performance. It performed worst out of all tested models in Kaminskyi’s research, therefore it should be a good starting point to iteratively improve upon.

When tasked with multi-step prediction, the idea is that the first LSTM encodes a latent vector together with a hidden short-term memory vector which are then decoded by the second LSTM to generate an output sequence. With this model, it was possible to evaluate how well a neural network could predict pitch and roll without having the images of incoming waves. If this model would perform similarly to one that uses images as an additional input, the conclusion could be made that, if necessary, the images could be omitted. In this case, this model would provide a more lightweight solution, requiring only numeric data.

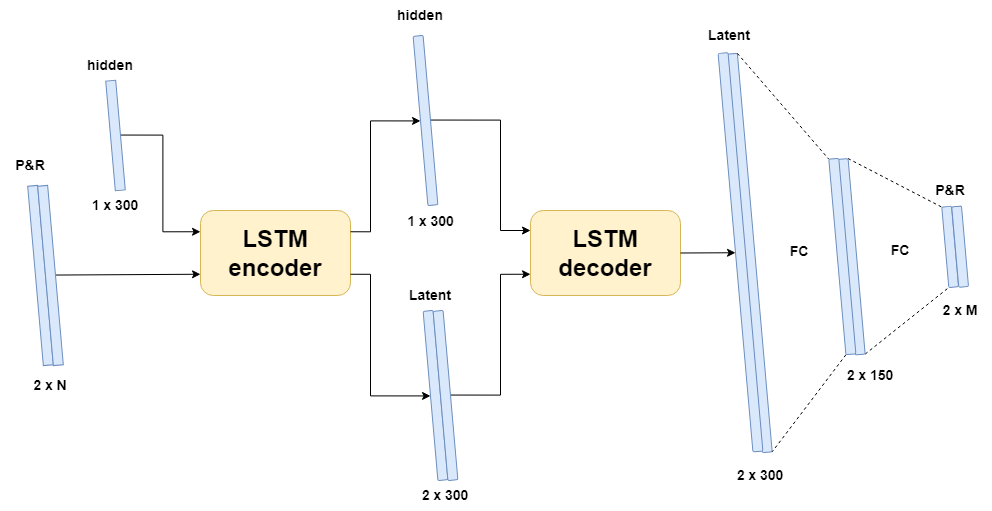


Figure 18: LSTM encoder decoder architecture

Figure 18 shows the architecture of the implemented model. As mentioned above, two LSTMs are used together where the first one acts as an encoder followed by a second decoder LSTM. The first LSTM receives the input sequence of pitch and roll values and has a hidden size of three hundred. When the data is passed through this network, an encoded latent vector is output together with the hidden state of this first LSTM layer. The second LSTM layer uses this hidden and latent vector and decodes it into a new latent vector. Finally, the latent vector from the decoder is passed through two linear layers that aggregate the vectors into a sequence for pitch and roll.

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| **Input** | **Sequence of PR at** | | | | | |
| *Name* | *Layers* | *Number of layers* | *Hidden size* | *Dropout* | *Input* | *Output* |
| **LSTM component** | | | | | | |
| Encoder | LSTM | 1 | 300 | - | 2 x N | 2 x 300 |
| Decoder | LSTM | 1 | 300 | - | 2 x 300 | 2 x 300 |
| **Linear component** | | | | | | |
| FC 2 | Linear | | | | 2 x 300 | 2 x 150 |
| FC 2 | Linear + tanh | | | | 2 x 150 | 2 x |
| **Output** | **Sequence of PR at** | | | | | |

Table 7: parameter table for encoder-decoder LSTM

The parameters for the encoder-decoder LSTM network are shown in Table 7. The LSTM hidden vector sizes are increased to three hundred. This increase was based on test results from the single step model, showing better performance when a larger than 128 hidden size is used. Additionally, the specific value of three hundred was chosen equal to Kaminskyi’s model in order to get a more equal comparison between both designs. Lastly, a second linear layer was added to the end of the model to allow for depth when aggregating the hidden vector down to the predicted output. The predicted output is activated by a tanh to limit the models output to the normalized domains for pitch and roll, i.e., [-1, 1].

### Sequential CNN

After the single- and multi-step LSTM oriented models - that only use pitch and roll inputs - convolutional neural networks (CNN) were introduced. With their introduction, images could also be efficiently processed and used to make predictions. Three models were designed using CNN architectures with the first one being a sequential **CNN architecture**. On one hand, this simple model was created to familiarize with the new CNN network architecture, its parameters and the image data loading process. On the other hand, this model was created to evaluate performances when using solely convolutional and linear layers and **no LSTM module**. Without an LSTM module, performance of this model is expected to be lower than other models. But it might still be better than previous LSTM models that only use numeric data. Additionally, generally speaking, LSTM networks have a high inference time due to their complexity (Mealey & Taha, 2018). Because of its absence in this model, lower inference time is expected which might make up for possible loss in performance.

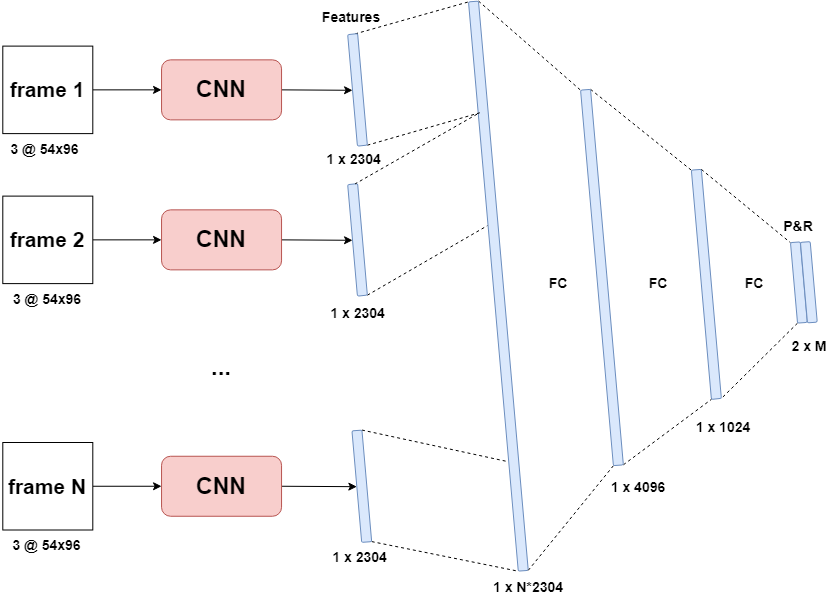


Figure 19: sequential CNN neural network architecture

Each image of an input sequence is processed individually by a CNN. The resulting tensors are then flattened into a one-dimensional vector. These feature vectors are then concatenated into one single large vector which serves as the input layer for the first linear layer. Because the vectors are appended in order, the sequence order is kept. Three consecutive linear layers then aggregate this larger vector into smaller vectors and eventually into an output sequence of pitch and roll. The architecture for this model is illustrated above in Figure 19 together with its parameter table in Table 8.

Three consecutive convolutional layers are used to extract features from the images. The first convolutional layer uses a 5x5 kernel while the next two layers use a 3x3 kernel. The channels follow a doubling pattern where each layer doubles the number of channels by a factor of two. Each layer is followed by a rectified linear unit activation and max pooling. This was done following the conventions of CNN network structures. The kernel sizes were based on the CNN encoder architecture from Kaminskyi’s work as it showed good feature extraction performance and was used in his best model. The size of the linear layers follow a decreasing trend to slowly aggregate the large vector into predicted outputs which are activated by a tanh. The tanh was especially necessary for this model as it would otherwise predict extreme values on the first couple of training batches. This is normal behavior as the model is still learning but without the tanh, these extreme values render the training loss graphs into a single high peak on the first epoch followed by a flat line.

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| **Input** | **Sequence of N images at** | | | | | | |
| **CNN component** | | | | | | | |
| *Name* | *Layers* | *Out channels* | *Kernel Size* | *Stride* | *Padding* | *Input* | *Output* |
| Conv 1 | Convolution  ReLu | 8  - | 5x5  - | 1  - | 2  - | 3 x 54 x 96 | 8 x 54 x 96 |
| Pooling 1 | Max Pooling | 1 | 2x2 | 2 | 1 | 8 x 54 x 96 | 8 x 27 x 48 |
| Conv 2 | Convolution  ReLu | 16  - | 3x3  - | 1  - | 1  - | 8 x 27 x 48 | 16 x 27 x 48 |
| Pooling 2 | Max Pooling | 1 | 2x2 | 2 | 1 | 16 x 27 x 48 | 16 x 13 x 24 |
| Conv 3 | Convolution  ReLu | 32  - | 3x3  - | 1  - | 1  - | 16 x 13 x 24 | 32 x 13 x 24 |
| Pooling 3 | Max Pooling | 1 | 2x2 | 2 | 1 | 32 x 13 x 24 | 32 x 6 x12 |
| **Linear component** | | | | | | | |
| FC 1 | Linear | | | | | 1 x N\*2304 | 1 x 4096 |
| FC 2 | Linear | | | | | 1 x 4096 | 1 x 1024 |
| FC 3 | Linear + tanh | | | | | 1 x 1024 | 1 x M\*2 |
| **Output** | **2 x M** | | | | | | |

Table 8: parameter table for sequential CNN model

### CNN LSTM single input

Now that the two main proposed neural network architectures – CNN and LSTM – were both individually implemented in different models, an **ensemble model** was made composed of both architectures. Many of the design concepts of the previous **sequential CNN** model were kept the same for this model. The consecutive input images are processed individually by a CNN into feature vectors. These different feature vectors are then concatenated into a large single vector. However, this vector is then used as input for an LSTM encoder instead of a linear layer. Since the sequence of the images is kept intact during the concatenation as previously mentioned, the **LSTM** can use its long- and short-term memory properties and should achieve higher performance than linear layers.

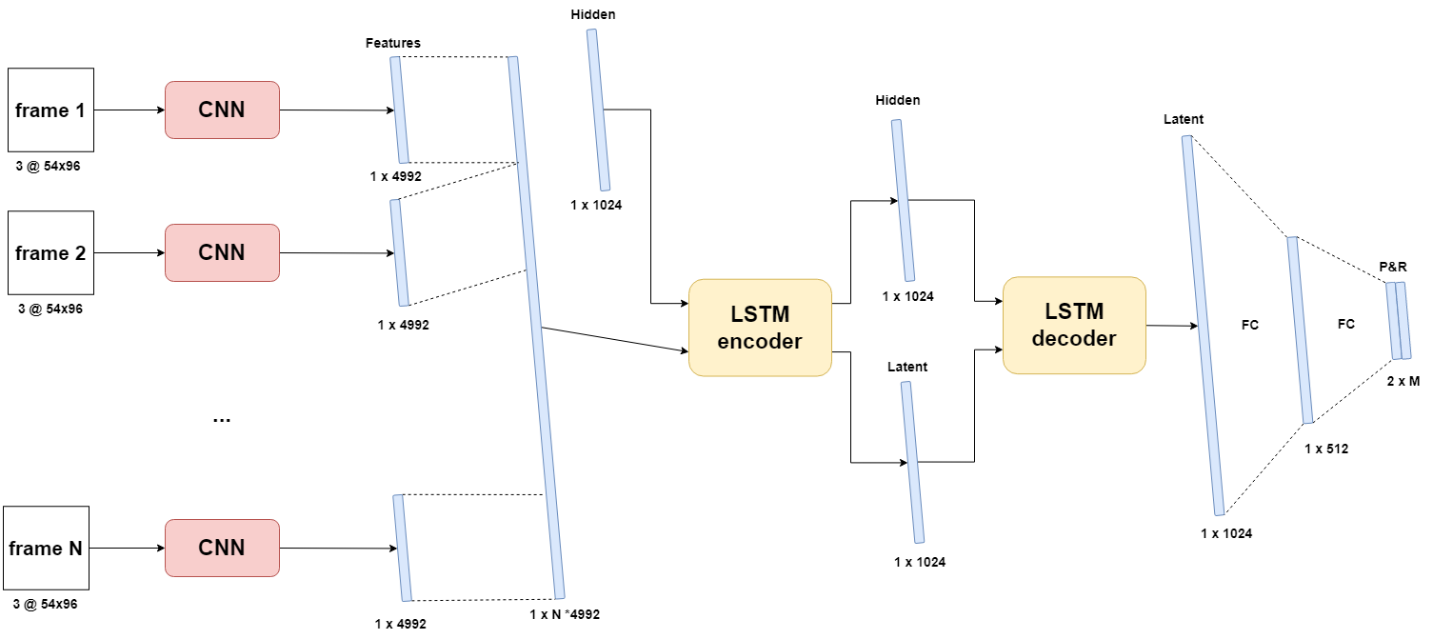


Figure 20: CNN LSTM single input architecture

The first LSTM encodes the large feature vector into a latent and hidden vector. These vectors are then passed to a second decoder LSTM which produces the output. The output of this decoder is then aggregated into a sequence off pitch and roll output by two linear layers. Note the ***single input*** in the model’s name to indicate that **only images are used as input** for this model. A second model was designed as well that allows for dual input. This way, the performance of all three input configurations could be measured: pitch and roll only, images only and both inputs.

The parameters for the single output CNN LSTM model are shown in Table 9. The CNN component is identical to the one from previous model. However, the last convolutional, ReLU and Max Pooling layers were removed. This was done in order to reduce the complexity and the number of parameters of the model to provide a more lightweight solution. The LSTM component is set up equal to the encoder-decoder model from 4.2.1, aside from its increased hidden size. This was done to compensate for the much larger input vector of the encoder LSTM.

|  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| **Input** | **Sequence of N images at** | | | | | | | | | |
| **CNN component** | | | | | | | | | | |
| *Name* | *Layers* | *Out channels* | *Kernel Size* | | *Stride* | | *Padding* | | *Input* | *Output* |
| Conv 1 | Convolution  ReLu | 8  - | 5x5  - | | 1  - | | 2  - | | 3 x 54 x 96 | 8 x 54 x 96 |
| Pooling 1 | Max Pooling | 1 | 2x2 | | 2 | | 1 | | 8 x 54 x 96 | 8 x 27 x 48 |
| Conv 2 | Convolution  ReLu | 16  - | 3x3  - | | 1  - | | 1  - | | 8 x 27 x 48 | 16 x 27 x 48 |
| Pooling 2 | Max Pooling | 1 | 2x2 | | 2 | | 1 | | 16 x 27 x 48 | 16 x 13 x 24 |
| **LSTM component** | | | | | | | | | | |
| *Name* | *Layers* | *Number of layers* | | *Hidden size* | | *Dropout* | | *Input* | | *Output* |
| encoder | LSTM | 1 | | 1024 | | - | | 1 x N x 4992 (+2) | | 1 x 1024 |
| decoder | LSTM | 1 | | 1024 | | - | | 1 x 1024 | | 1 x 1024 |
| **Linear components** | | | | | | | | | | |
| FC 1 | Linear | | | | | | | | 1 x 1024 | 1 x 512 |
| FC 2 | Linear + tanh | | | | | | | | 1 x 512 | 1 x M\*2 |
| **Output** | **2 x M** | | | | | | | | | |

Table 9: parameter table for CNN LSTM single input and dual output (red)

### CNN LSTM dual input

The final model was a slight variation on the previous model which allows it to use both **numeric data and images as input**. It was built based on the concept of the previous CNN LSTM single input model. The main difference is that pitch and roll values for each frame – a frame being an image and its corresponding PR values – are appended at the end of each image’s feature vector before they are concatenated into one large vector. This way, both the image and PR sequence order are preserved for the LSTM. Correct normalization is of utmost importance with this model as one type of data may overshadow the other if they are not normalized to the same window.

Expectations for this model are high as it has all available data at its disposal to make as accurate of predictions as possible. However, this model requires the most amount of processing, so inference time will probably be higher than other models. This is mainly due to the process of building the feature vectors and append the pitch and roll tuples to them. This is an expensive operation in terms of computing resources and might cause this model’s inference time to be too high. The illustrated architecture is shown in Figure 21. Since the model’s only difference is found within its internal functionality for the feature vector concatenation phase, the parameters of Table 9 still apply with the only change being the extra two datapoints added to each feature vector. This change is marked in red. Additionally, the values of the image feature vector are activated with a tanh. This is done to project them back into the domain of the PR-values that are appended. If this was not the case, the values of the appended PR-pairs might be overshadowed by the potentially larger values in the feature vector.

## Summary

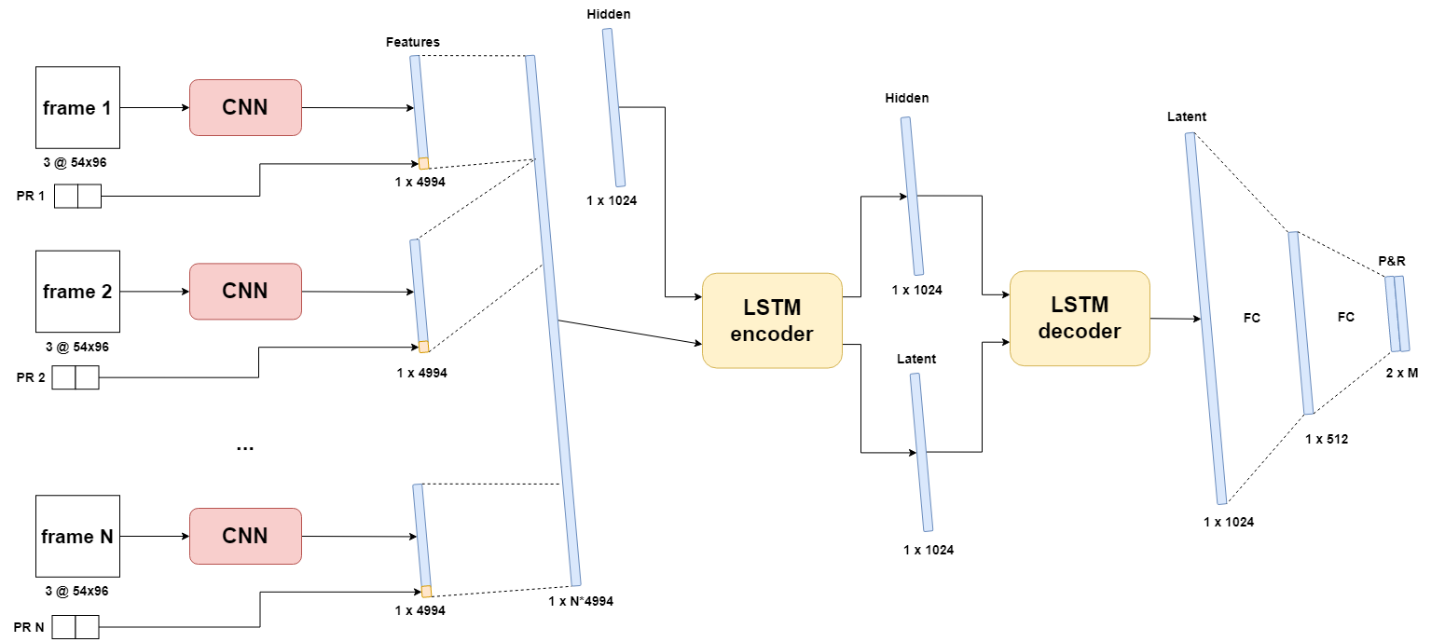


Figure 21: CNN LSTM dual input architecture

In this chapter, all proposed models and their parameters were discussed. An iterative process was followed where each next model increases in complexity and capabilities in hope of receiving better results. First off, a single step model was implemented to acquire experience with PyTorch and deep learning. This model is limited to predicting only one future time-step. Two variants were trained, one for predicting either pitch or roll and one to predict both. Due to its simplicity and low parameter count, this single step model also served as a platform to quickly test different configurations of recurring parameters such as learning rate and hidden size, to find optimal values for future models. Next, four multi-step models were implemented. These are models that are able to predict ordered multi-value sequences of pitch and roll. Each model was designed with a different approach based on what data is used as input and which architectures are used. One model only uses pitch and roll data, two models only use images, and one uses both. Both CNN and LSTM architectures are used either separately or in combination with each other in ensemble models.

# Testing environment

To fairly evaluate each model’s performance and match it to the criteria, a testing environment is needed. This environment determines what parameters will be used to train the models and which metrics will be used to measure performance. In the following sections, all components that make up the testing environment are discussed.

## Gradient descent algorithms

In supervised deep learning problems, each neuron in the network updates its optimal weight and bias by comparing the predicted output with the ground truth. The model receives input-output sequences and tries to learn the relation between the two. A metric is used to compare predicted output and ground truth. This metric – commonly referred to as the cost or loss function – is chosen based on the nature of the problem. Some examples are the mean square error (MSE) for regression problems or cross-entropy loss for classification problems (Wang et al., 2022a). During training, the goal is to minimize this error. Each iteration, the model updates its parameters to move, *descent* in the direction of this minimum. The direction in which the minimum lies, is found by calculating the partial derivatives of the loss function for each neuron. However, since the impact of both weight and bias need to be considered, both partial derivatives are calculated. This is done for all weights and biases. The result is a gradient that can be thought of as a multi-dimensional hyperplane with multiple local minima and one global minimum. To solve for the gradient, the model iterates through all data and computes the gradient in the current configuration of weights and biases. It then utilizes this gradient to find the slope of the cost function and the direction the weights and biases should move towards. Once this direction is known, the parameters of each neuron are updated accordingly starting at the last layer and moving towards the first layer. This process is called backpropagation as the model propagates the errors backwards over its layers (Rumelhart E. et al., 1986).

Different implementations exist for gradient descent with three of them being the most prominent. The main difference between them is how the gradient is calculated. The first is batch gradient descent. This algorithm uses all training data to calculate the gradient before taking a step. This means that the model is updated once per training iteration. The second one is mini-batch gradient descent. Here, the algorithm uses only a subset – a mini batch – of all training data. This allows the model to be updated more throughout training, however some mini batches might not always provide the most optimal gradient. The last one is **stochastic gradient descent (SGD)**. With this implementation, instead of calculating the actual gradient based on all data, an estimate thereof is used (Ruder, 2016). This estimate is calculated through stochastic approximation based on a random subset of the data. Different variants and optimizations exist for each method. For this research, SGD was used with the Adam optimizer.

### SGD Adam optimizer

As discussed above, different algorithms exist to calculate the gradient, namely batch, mini-batch and stochastic gradient descent. These algorithms are used to calculate the weights and biases for the neurons in the network by iteratively taking steps in the direction of the minimum on the gradient. The size of this step is determined by the learning rate which is fixed for the standard implementation of the above three methods. However, variants or optimizers exist to dynamically change the value of the learning rate and optimize the training process. In general, the learning rate should start high and decrease as the model gets closer to the local minimum on the gradient. This way, the model will converge quickly without overshooting or diverging from its optimal state.

Adam is an optimization algorithm for stochastic gradient descent (SGD). While normal stochastic gradient descent maintains a single learning rate for all weight updates which does not change during training, Adam applies an adaptive learning rate that is computed for each network based on estimates for the first and second moments of the gradient. It combines the advantages of two other optimization techniques: AdaGrad and RMSProp. Instead of adapting the parameter learning rates based on the average first moment (the mean) as in RMSProp, Adam also makes use of the average of the second moments of the gradients (the uncentered variance) (Brownlee, 2017). According to (Kingma & Ba, 2014), Adam is computationally efficient, requires little memory and is invariant to diagonal rescale of the gradients.

The choice of the optimizer is based on which gradient descent algorithm will be used. Within PyTorch, selection of an algorithm is very easy and therefore, the best optimizer was chosen based on the current state-of-the-art. Adam is currently one of the best optimizers and a very popular option. The method is really efficient when working with problems involving a lot of data or parameters (Doshi Sanket, 2019). For this reason and because of its easy implementation in PyTorch, Adam was used as optimizer for all models.

## Hyperparameters

An important part to any deep learning problem is defining the hyperparameters and finetuning them for optimal performance. A hyperparameter is a parameter that can be manually set by the programmer. They affect the behavior of the model during training and thus have a direct influence on how well the model will perform afterwards. They are different from the internal parameters of the network such as a neuron’s weights and bias, whose values are derived during the training process. Many different hyperparameters exist, each having their own function but not all of them need to be used in every model. Below, each hyperparameter that was used in this research is discussed.

* **Train-test ratio** is used to control how much of the original data is allocated to each subset of the main dataset as discussed in 3.5.2. The proportion of each subset is relative to all available data points, i.e., IO-sequences. For this research, an **80% - 20%** split was used for respectively the train and test dataset.
* **Learning rate** refers to the rate that an algorithm converges to a solution. For a deep learning neural network, it determines the size of each step during the gradient descent. High learning rates cause the model to converge very quickly to the local minimum but come with the risk of overshooting the minimum. On the other hand, low rates may cause to model to not reach convergence by the end of training. An initial learning rate of **0.001\*** was used for the Adam optimizer.
* **Batch size** determines how many datapoints are processed at one forward pass during training. A large batch size means that a lot of training data is considered at once. This increases memory usage and lowers the number of mini-batch gradient descent backpropagation steps (Shen Kevin, 2018). Therefore, a higher learning rate should be applied to assure that the local minimum is reached within these fewer steps. A small batch size has the opposite effects. A batch size of **64** was used across all models. This is a relatively low batch size, but it was chosen because of memory limitations when working with images.
* **Number of epochs** or the number of training iterations, determines how many times the model can process all training data. During one epoch, all batches of the training data are processed once to update internal parameters. When the model is trained for more epochs, it has more chances to find the best internal parameters. However, training the network for too many cycles can lead to overfitting where the network starts to learn the detail and noise in the training data to such an extent that it start to negatively impact the performance on new data. By using an unseen validation dataset, overfitting can be measured. When the prediction errors on validation data start to increase while those of the training data are still decreasing, the model is overfitting and training should be stopped. All models were trained for **50\*** epochs.
* **Data frequency** defines at which frequency data is fed as input and at which frequency data is predicted by the model. The simulation data was generated at **2Hz** or 2 frames per second as a good balance between having enough detail without having consecutive frames containing too similar data. With up sampling being impossible, the assumption was made that down sampling to a lower frequency was also not beneficial as this would reduce the detail in the predictions and could introduce aliasing effects.
* **Input sequence length** sets the number of frames used as input to make a prediction upon. This hyperparameter had no fixed value and was **chosen on a per model basis**.
* **Output sequence length** sets the number of datapoints the model needs to predict. An output length of **60** **frames** at two frames per second was chosen as the minimum. This way, performance of each model could be measured over a 30 second prediction window as discussed in the objectives and criteria.

The last two hyperparameters, input and output sequence length, will have the most impact on the performance of the model. They will be tested the most to find the best configuration for each model. Ideally, only a short input sequence is needed to make an accurate prediction over a long sequence length. Due to its importance and for readability, the ratio of input to output sequence length will be defined as the **IO-ratio** (input/output-ratio). The notation of the IO ratio will always be in non-simplified non-fractional form, i.e., a 30/60 IO-ratio will never be written as ½ or 0.5 to avoid losing sight in the effective sequence lengths at hand.

As a final note on the hyperparameters, finding the optimal value for each hyperparameter is called hyperparameter optimization. Different algorithms exist to perform this optimization (Claesen & de Moor, 2015). However, they are very expensive and time-consuming operations, especially when many different models are at hand. Optimizing all models would be even more time-consuming. An alternative approach was used in this thesis where only some parameters were tested to find optimal values. These parameters were tested on the simple single-step model. Once an optimal value was found, it was then used for all models in assumption that they would behave similarly. This way all models could be compared equally with roughly estimated optimal hyperparameters. The experimentally found values are marked with an asterisk (\*). Complete testing with results will be discussed in the next chapter.

## Performance metrics

### Loss function

To compare the ground truth with the predictions made by the model, a metric is used to calculate the error, i.e., the loss function. Many distinct functions exists to define this loss, each with their own appliances. For continuous data and predictions, the Mean Squared Error (MSE) is a popular option (Wang et al., 2022b). The MSE of two sets of points of *n* elements (read number of predicted frames), is defined as the average of the squared errors, where the error corresponds to the difference between ground truth and prediction .

During training, the MSE was used as loss function for gradient descent. It calculates the average error over the whole predicted sequence. For example, if sixty values are predicted, the MSE will return one value: the average error over these sixty points. MSE will also be used to compare different models’ permances to each other. However, this is quite a general comparison because some interesting information is lost when the difference between two sequences is averaged into one value. For a more detailed comparison and evaluation of the predictions, an extra metric was introduced: loss per frame (LPF). The LPF of two sequences of length *n* is defined as a sequence of *n* errors where each error is the difference between the two sequences at the corresponding index. Returning to the first example, if sixty values are predicted, the LPF will return an array of sixty elements containing the error between each pair of predicted and real values individually. When this metric is averaged over all predictions made on an unseen test dataset, the result can be used to analyse how the error changes on average throughout the predicted sequence. Additionally, if the root of the MSE is taken – the RMSE – the errors are projected back to the units of the original data and can be de-normalised into their original domain. Using this principle, all MSE values can be translated back into their corresponding pitch and roll angles – which provides a more sensible metric for comparison than MSE.

### Inference time

In the cases were a deep learning model needs to be deployed in real world scenarios to make predictions on completely new data, the speed at which it can make those predictions can be of significant importance. For example, self-driving cars with limited computational resources need fast, low-latency models. This can be a challenging metric to fully optimize when high demand architectures are used such as LSTM networks (Kouris et al., 2019). The target vessel will similarly to the self-driving cars have a limited number of computational resources. Because of this, each model will be subjected to a measurement of its inference time – the time it takes to make one forward pass prediction. Besides having a low error across predictions, having a low inference time is equally important. To measure true inference time, all outside influences should be eliminated. When executing on a GPU, factors like GPU warm-up, asynchronous execution and system hardware specification all need to be considered. As discussed in 1.6, inference time will be measured as the average prediction time over ten thousand single batch predictions.

**GPU warm-up** is a process in which the GPU is initializing. Modern GPUs have multiple power states to reduce their power usage. When the GPU is not used, it will go into a power saving state and potentially completely turn off. In lower power state, the GPU shuts down different pieces of hardware, including memory subsystems, internal subsystems, or even compute cores and caches. A program attempting to interact with the GPU will cause the driver to load and initialize the GPU. It is this driver load that can influence the measurement of inference time. According to (Geifman, 2020), programs that cause the GPU to initialize can be subject to up to three seconds of latency due to the scrubbing behavior of the bit error correcting code (ECC). Memory scrubbing is the process of reading data from each memory location, correcting faulty bits with an ECC, and writing the data back to its original place. Below in Figure 22 the effects of GPU warm-up are clearly visible. A big spike in execution time is measured on the predictions when the GPU is still initializing. When the GPU is initialized, the timings decrease and remain constant. It is important that this initialization period is not included in the inference time calculation because it is inaccurate and does not reflect a production environment where the model is continuously making real-time predictions on an initialized GPU. To compensate for GPU warm-up, a broad estimate of one thousand predictions are executed without time measurements.

**Asynchronous execution** is mechanism that occurs on multi-threaded or multi-device programming. Different tasks are scheduled to different execution units which execute them asynchronously. This can cause a block of code to be executed before the previous one is finished and therefore speeds up execution. However, if a neural network is executed on the GPU – which is asynchronous by default – and inference time is measured on the CPU, the timer will stop before the model is done with its execution. This needs to be taking into consideration when certain popular Python libraries are used like *time* for example, which is executed on the CPU. PyTorch provides a very similar version of the popular *time* library designed for measuring and synchronizing events on a cuda-enabled device.

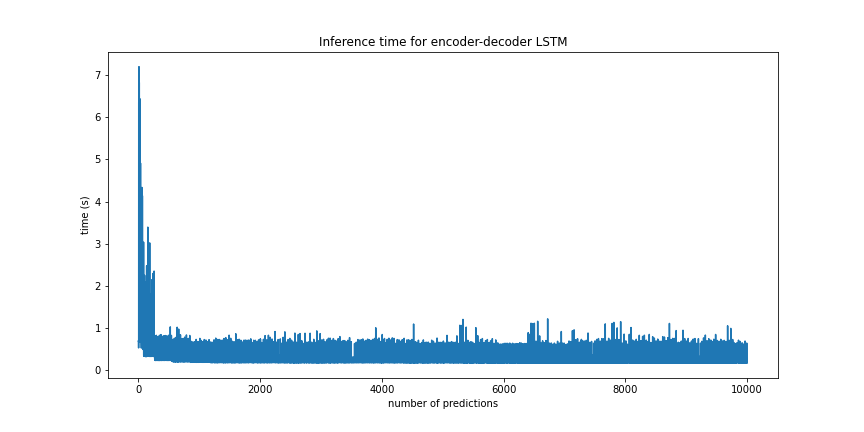


Figure 22: inference time over 10.000 prediction with GPU warm-up effect

|  |
| --- |
| **def** inference\_time**(**model**,** dummy\_input**,** repetitions**=**10000**):**  device **=** torch**.**device**(**"cuda"**)**  model**.**to**(**device**)**  dummy\_input**.**to**(**device**)**    # INIT LOGGERS  starter **=** torch**.**cuda**.**Event**(**enable\_timing**=True)**  ender **=** torch**.**cuda**.**Event**(**enable\_timing**=True)**  timings **=** np**.**zeros**((**repetitions**,** 1**))**    # GPU WARM-UP  **for** \_ **in** **range(**1000**):**  \_ **=** model**(**dummy\_input**)**    # MEASURE PERFORMANCE  **with** torch**.**no\_grad**():**  **for** rep **in** **range(**repetitions**):**  starter**.**record**()**  \_ **=** model**(**dummy\_input**)**  ender**.**record**()**  # WAIT FOR GPU SYNC  torch**.**cuda**.**synchronize**()**  curr\_time **=** starter**.**elapsed\_time**(**ender**)**  timings**[**rep**]** **=** curr\_time  mean\_syn **=** np**.sum(**timings**)** **/** repetitions  std\_syn **=** np**.**std**(**timings**)**  **return** timings**,** mean\_syn |

Listing 1: function definition for inference time measuring

Lastly, the **system** **hardware specifications** on which the measurements were recorded are mentioned for reference. All measurements were taken on a workstation with the following specifications:

* CPU: Intel Core i7 10700k at 3.8GHz base clock and 4.6GHz boost clock
* GPU: Nvidia GeForce RTX 3080 with 8704 cuda cores at 1800MHz boost clock
* RAM: 3200MHz

## Summary

In this chapter, the testing environment was discussed. This environment encompasses all relevant variables and methods which have direct influence on the performance and evaluation of the models. By fixing most of these variables and methods across all models, the effect of specific parameters can be accurately measured, and models can be compared fair and equally. In the first section all hyperparameters are discussed in combination with their value. Some of these hyperparameters where one-and-done choices, others were determined based on experimentation on the single-step model. In the second section, the training optimizer was discussed. To optimize the gradient descent process during training, Adam was used. Adam is an optimizer for the stochastic gradient descent algorithm that has high performance compared to other optimizers. It dynamically changes the learning rate to achieve faster and better convergence. Adam is also very easy to implement on PyTorch. Lastly, the error metrics were discussed. To measure performance, MSE loss, LPF and inference time are used. The first two are functions to calculate and visualize errors and their trend across a predicted sequence. The inference time is used to evaluate the latency that occurs between input and prediction. GPU warm-up, asynchronous execution and system hardware specification all play a role when measuring inference time.

# Results

In this chapter, an extensive overview is given of all tests that were performed and their results. In first section, the results from the hyperparameter optimization are discussed. Afterward, each model will be discussed in detail, followed by a section on inference time results. In the last section, a final overview and comparison is provided of the best performing models. To analyze the accuracy of the models, mainly the MSE, LPF and graphs showing the real vs. predicted values were used. As a baseline, each model is also compared to the *zero-predictor*  as discussed in the criteria.

## Hyperparameter optimization

Three hyperparameters were optimized to estimated optimal values: **LSTM hidden layer size**, **number of epochs** and **learning rate**. It was hypothesized that these three parameters would have the most influence on the performance of the models and thus a simple method was applied to optimize them. To find the best parameters, three values for each parameter were evaluated: one low, one high and one in-between value. With the results of these three tests, the optimal value is chosen based on the trend they form. The resulting value is then used for all other models in assumption that they will show a similar behavior. All tests were executed on the dual output variant of the single-step model due to its low complexity and thus fast training time.

### Number of epochs

The number of epochs determines how many times the model can process the full training dataset to optimize its internal parameters. Low training epochs allow for fast training but might lead to the model not reaching its optimum. High epochs cause longer training times but give the model more time to converge. To define the optimal value, the test model was trained for 8, 25 and 50 epochs and the training loss graphs were compared (Figure 23).

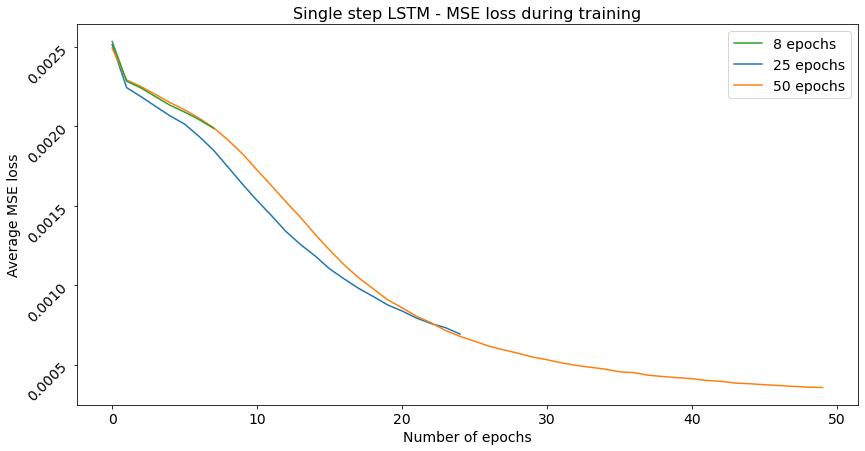


Figure 23: training losses for different numbers of epochs

During training, this loss should rapidly decrease on the first couple of epochs and ease out to a point after which the loss remains constant. At that point, the model has learned the mapping between input and output to the best of its abilities and receives no more benefits from additional epochs. It is clear that the model needs at least 50 epochs to properly train itself and achieve the lowest MSE. Even more, the model is still marginally decreasing during the final epochs indicating that it hasn’t reached optimal convergence yet. Because of this, an even higher number of epochs could possible lead to slightly better results. Nevertheless, the number of epochs was chosen to be 50 for all future training in assumption that this was a good trade-off between optimal performance and minimal training time. Especially when training the more complex models.

### Learning rate

Learning rate was the second parameter that was optimized. Learning is a very hard to conceptualize hyperparameter. It is defined as the size of the step that is taken during one iteration of moving down the gradient towards the minimum. During research of this parameter’s value in other deep learning applications, most cases used a learning rate of 0.01, 0.001 or 0.0001. Learning rate is very much dependent on the complexity of the problem. Simple problems may get away with high learning rates resulting in very fast conversion, but on complex problems such as this one, a smaller learning rate is recommended (Wilson & Martinez, 2001). The three above mentioned values were tested in order to find the optimal value. Once again, the training loss graph is used to discuss the results (Figure 24). It is important to note that these tested values were used as initial learning rates with the Adam optimizer. As discussed in previous chapter, Adam will dynamically change the learning rates. However this does not mean that the initial value is less important.

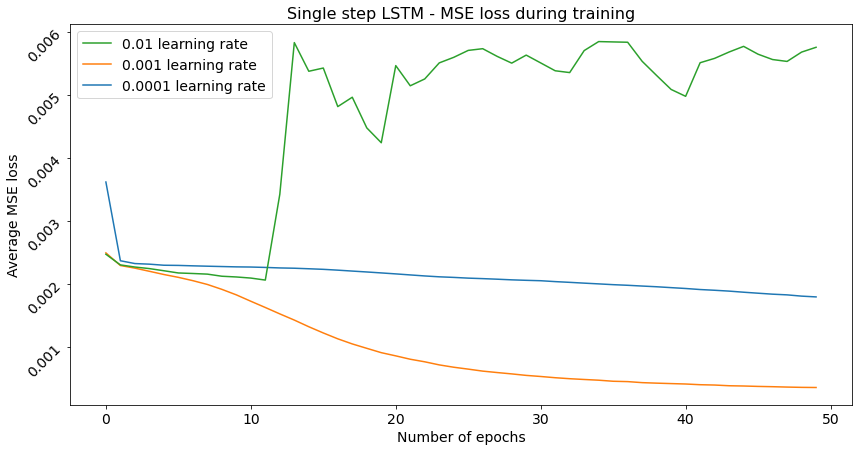


Figure 24: training loss for different learning rates

The model shows very interesting but not unexpected behavior. Based on the mathematical theory for learning rate, a learning rate that is too high will result in very drastic changes to the internal parameters, causing divergent behavior. This is clearly what is happening with the model on the green line of with 0.01 learning rate. The model is basically bouncing around on the gradient without really converging to the minimum at all. The opposite is visible on the blue line. In this case the learning rate is smaller than ideal as the model is converging very slowly compared to the orange line. Due to the smaller steps, the model needs more iterations to reach the minimum. If the current rate is projected forward, convergence will require somewhere between five to ten times more epochs. The model on the orange line and the model on the blue line will probably reach similar performance in the end. However, the orange one will be much more efficient which is why a learning rate of 0.001 was selected as the value for all future models.

### LSTM hidden size

After determining the learning rate and number of epochs, the hidden size for LSTM modules was assessed. Judging based on the nature of our problem: sequence prediction and the efficiency of the LSTM module for this type of problem, it was concluded that the hidden size of the LSTM modules would be the most important parameter to optimize. The size of linear layers, and parameters of the CNN modules were assumed to be less impactful on performance. In addition, the parameters for the CNN were already tested and proven effective in Kaminskyi’s research. Initially, a hidden size of 128 was chosen for the single step LSTM model. To find the direction of the optimal hidden size, a lower 32 and higher 256 hidden size were tested. The results are shown in Figure 25.

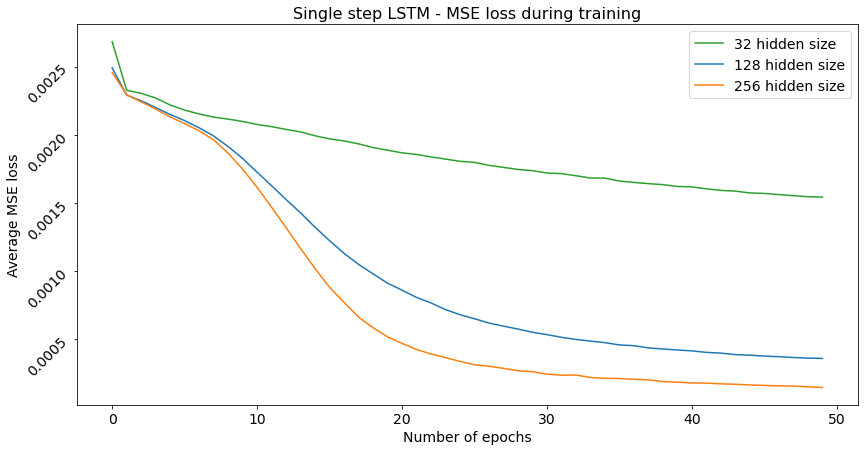


Figure 25: training loss for different LSTM hidden sizes

Once again, the model shows expected behavior. Generally speaking, when increasing the nodes of hidden nodes, the network is able to learn a more powerful function between input and output. In the case of LSTM networks where memory cells are used as hidden nodes, increasing their number allows the model to better remember long term dependencies simply because there are more parameters to represent them. This visible on the graph where the model converges to the lowest MSE with the highest number of hidden nodes. From this trend, the conclusion was made that larger hidden sizes should be used. For the encoder-decoder LSTM, the hidden size was increased to 300 following this trend. For the CNN LSTM ensemble models, the hidden size was increased even further to remain in line with the much larger input vector.

### Activation functions

As a final general-purpose optimization, the effect of activation functions was assessed on the single-step model. The single step model has three logical points in its architecture where activation functions can be placed: one to activate the input before the LSTM module **(1)**, one after the LSTM **(2)** and one after the linear layer **(3)** which activates the predicted output. Since the model trains with normalized data between [-1, 1] and is expected to return values in this domain, a tanh is the only possible activation usable on the output layer. The activation on the input should consider this domain as well. A ReLU here would be ineffective as it nullifies all datapoints lower than zero. Due to the angular units of pitch and roll where negative and positive values are equally important, adding a ReLU here leads to 50% reduction of information in the input. This leaves the second option as the most interesting point for an activation function.

|  |  |  |
| --- | --- | --- |
| Configuration | Average Pitch error  [denormalized RMSE] | Average Roll error  [denormalized RMSE] |
| Barebones model | 2.18° | 2.06° |
| ReLU (2) | 2.36° | 2.20° |
| Tanh (3) | 2.19° | 2.04° |
| ReLU (2) + Tanh (3) | 2.26° | 2.15° |

Table 10: average pitch and roll errors for different activation function configurations

Three configurations were tested on the single step model: one with a ReLU at (2), one with a tanh at (3) and one with a ReLU at (2) and a tanh at (3). The ReLU activation is used in almost every model of Kaminskyi after an LSTM module. However, as discussed in the previous paragraph, the use of the ReLU is expected to negatively impact the results. The goal of this experiment was thus to mainly evaluate the impact of a ReLU activation on the output of the LSTM module. A secondary objective was to evaluate the impact of a tanh activation on the output.

The results are shown in Table 10. Each configuration was trained for 50 epochs with a 0.001 learning rate. The test resulted in very similar performance for each configuration. The introduction of the ReLU activation functions resulted in no measured benefit, rather a slight deterioration. From this experiment, expectations were confirmed and it was concluded that ReLU activation functions were not beneficial to the performance. The tanh on the other hand, showed no immediate impact on performance. However, it was later on proven beneficial due to its ability to transform extremely high predictions into -1 or 1. This solved the issue of training loss graphs turning into one high peak at epoch one followed by a flat line due to the small differences in MSE losses being out-scaled by the single large peak value.

## Single-step model

In this subchapter, the two single-step model will be analyzed on prediction accuracy. Three different variants were trained: one single-output variant for each pitch and roll and one dual-output variant for simultaneous pitch and roll predictions. These models should perform very well as they only need to predict one value. The three models were trained with an input sequence length of both fifty and ten PR-values to identify their optimal IO-ratio. Below in Table 11, the results are shown for each model in each configuration. Note that error values in the table are calculated as the denormalized RMSE averages over all predictions made on the unseen test data set.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Variant | IO-ratio | Average Pitch error [denormalized RMSE] | | | Average Roll error [denormalized RMSE] |
| Pitch | 50/1 | 1.85° | | | / |
| Roll | 50/1 | / | | | 1.91° |
| Dual | 50/1 | 2.17° | | | 2.03° |
| Pitch | 10/1 | 2.28 | | | / |
| Roll | 10/1 | / | | | 2.25° |
| Dual | 10/1 | 2.34° | | | 2.09° |
| **Zero prediction** | | | **6.43°** | **7.30°** | |

Table 11: denormalized RMSE for single-step LSTM variants at 10/1 and 50/1 IO-ratios

On the first three grey rows, the results are shown for the models that were trained with an input of fifty frames. Overall, the performance is very good. The dual-output variant performs slightly worse compared to the single-output ones shown on row one and two. This could be due to the network only having to optimize to one parameter. The bottom row in red shows the average error for the hypothetical zero-predictor model. As expected, these values are significantly worse than the trained models, meaning that the models have indeed captured most of the underlying trend in the simulation data and are making logical predictions. The same variants were also tested with a lower number of frames in the input sequence. This was done to find out whether or not it is necessary to provide fifty frames for just a single prediction. With an input sequence length of ten, the single step models still perform very well, even though the model only has a fifth of the input of the previous configuration. Only a marginal decrease in performance is shown compared to the 50/1 IO-ratio models.

A recurring trend was noticed among all these results. Roll prediction errors are overall lower than pitch prediction errors. Kaminskyi made the same observation and according to his results shown in 2.6, this behavior returned for almost all models. The difference could be explained by roll having a somewhat more predictable behavior than pitch. For example, pitch could inherently have a quirkier behavior which causes it to have a lot more micro changes that are hard to learn and consistently predict. In contrast, the results from the zero predictor are the opposite, the roll prediction error is higher than the pitch prediction’s error. Based on the data analysis which showed that pitch and roll have very similar distributions, this difference means that roll in general has a higher deviation from zero than pitch. Yet, even with this wider spread, roll must have a more predictable trend.

To further analyze the results from the single-step model, only the dual output variant will be considered. The table above provides a general idea of prediction accuracy; however, some information is lost when averaging results. In Figure 26 the prediction results are shown for pitch (top) and roll (bottom) across the whole test dataset. The predicted values are shown in orange on top the real values which are shown in blue. The dark sand-colored area represents overlapping values between predictions and real values while orange or blue areas mean that predictions respectively exceed or underrun the real values. For readability, the dark sand-colored area will be referred to as the *dessert.*  The top graph for pitch shows a constant blue area around its dessert. Judging by the shape of the blue outline and the shape of the dessert, the predicted pitch values seem to follow the trend well but consistently fall short of the real values by a couple of degrees. When comparing this to the roll graph, the effect is much less present which indicates that roll is being predicted with greater accuracy. This confirms the hypothesis made above - that was solely based on the RMSE averages of Table 11 - that pitch must be more random and thus harder to predict.



Figure 26: predicted (orange) vs. real (blue) values for pitch (top) and roll (bottom)

Lastly, the training generalization of the three single-step models is analyzed in the 10 input 50 epoch configuration. This is done by plotting the average MSE per epoch of the models for both the training and test dataset. This is shown in Figure 24. Each full line represents the training dataset loss while the dotted line represents the validation dataset loss. Generally speaking, the training curve should be lower than the validation loss curve because the model always tries to optimize towards the training data and does not know the validation data.

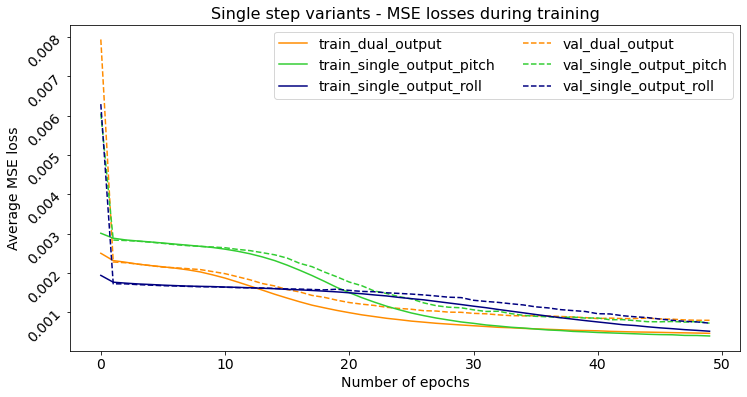


Figure 27: MSE loss during training of the single-step models

With this representation, generalization and overfitting can be visualized and assessed. The first of which is the rate at which the losses minimize and reach a state of very low change per epoch. The roll prediction model has by far the worst convergence out of the three, followed by the dual-output model. This means that it needs to most time to find its optimal internal state. Eventually, all models converge to a similar average error. However, the roll prediction model’s losses are still marginally decreased, indicating that it might benefit from a few more training epochs. The same constellation as above can be made here once again, being that roll has the most accurate predictions. Its validation loss (blue dotted line) is lowest in class on the last epoch even though its training loss (blue solid line) is the highest. Overfitting occurs when the validation loss starts to increase again after reaching a certain point. Based on these graphs, little to no overfitting has happened during training.

In conclusion, even with roll having more spread-out values, it is still easier to predict than pitch. All models performed really well and produced results that can be later used as an additional benchmark. This model and its variants prove that pitch and roll can be predicted with average error of approximately 2°. However, they are not capable of sequence predictions.

## Multi-step models

### Encoder-Decoder LSTM

The LSTM numeric data model is expected to perform the worst out of all proposed models according to Kaminskyi’s research. However, based on the results below, it becomes clear that this is not the case, and this model actually performs very well. The encoder-decoder LSTM was extensively trained for a multitude of different input sequence lengths and a fixed length output of 60. This was done to discover the optimal IO ratio for accurate predictions without creating too much overhead of unnecessary long input sequences. Based on the results from the single-step models, the number of epochs for all training was fixed at 50. The training results are shown in Figure 28 for the first six evaluated IO-ratios. The same layout as above is used where each color represents a different configuration, and the training and validation losses are respectively solid and dotted lines.

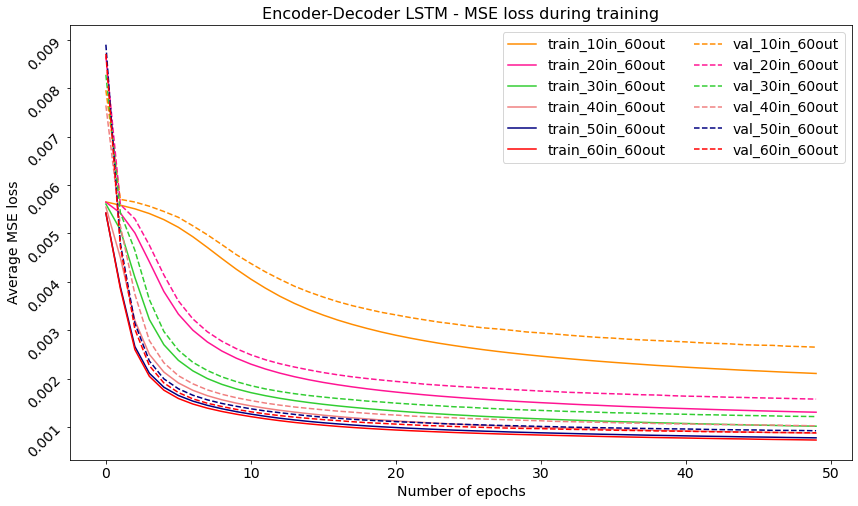


Figure 28: encoder-decoder LSTM training and validation losses for different IO-ratios

A general trend is present among the configurations: the loss and convergence gets better the more input frames are used. Intuitively, this behavior is to be expected. The 10/60 IO-ratio (orange) performs the very worst and shows poor convergence. As the input sequence length increases however, so does convergence. Overall, no overfitting was observed for any of the configurations. Additionally, fifty epochs proved to be a good amount for this model as the higher IO-ratios reach near optimal convergence during the final epochs with their loss remaining almost constant.

|  |  |  |  |
| --- | --- | --- | --- |
|  | IO-ratio | Average Pitch error [denormalized RMSE] | Average Roll error [denormalized RMSE] |
| 10/60 | 4,43° | 4,02° |
| 20/60 | 3,34° | 2,98° |
| 30/60 | 2,92° | 2,59° |
| 40/60 | 2,68° | 2,38° |
| 50/60 | 2,58° | 2,3° |
| 60/60 | 2,46° | 2,2° |
| 90/60 | 2,2° | 2,09° |
| 120/60 | 2,02° | 1,98° |
| zero-prediction | 6.43° | 7.30° |
| **Kaminskyi** | 30,9° | 29.4° |

Table 12: average denormalized RMSE for encoder decoder LSTM per IO-ratio

In order to further evaluate the optimal input sequence length for a thirty second prediction, two more IO-ratios were tested: 90/60 and 120/60. Table 12 shows the average error for pitch and roll for each IO-ratio in combination with a visual representation. These errors are denormalized RMSE averages of all predictions made on the test dataset. Once again, the zero-predictor results are appended for comparison. The trend found in the single step model’s results is noticed once again: pitch prediction errors are consistently higher than those of roll. This further affirms that predicting pitch is harder than predicting roll. Although it is observed that this effect decreases as the input sequence length increase. The error margin for both pitch and roll decrease with an exponential rate. Note that on the graph, the last three points appear to be linearly decreasing, however this is due to their x-labels being disproportionate compared to the first six. From these results, it was concluded that the encoder-decoder LSTM could predict a thirty second with high accuracy for both pitch and roll at a 120/60 ratio. Lower ratios like 90/60 or 60/60 retain high accuracy as well, however, they are not able to predict pitch with the same accuracy as roll.

These results are **very contradictory to Kaminskyi’s results**. Kaminskyi’s tested a similar model for 50 epochs at a 20/24 IO-ratio. His network resulted in an average error of approximately 30° for both pitch and roll on the 10th predicted second (20th frame at 2Hz). In our case, even the worst IO-ratio configuration for this model does not reach an error of this magnitude at 30th predicted second, let alone at the 10th second. Kaminskyi’s result is also far worse than even zero-predictor (Table 12). This is an extreme difference as a similar model trained on the same data should - in theory - perform similar. Based on the distribution of the data discussed in 3.4.2, a 30° error is almost impossible when 99.7% of all datapoints lies within a [-20°, 20°] interval. Therefore, it was concluded that Kaminskyi had made an error during the calculations or de-normalization of his results, or that the model had a too low learning rate (0.0001) which caused it to not have converged by the end of training.

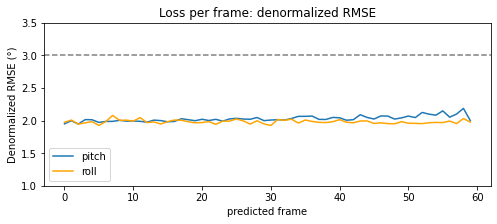
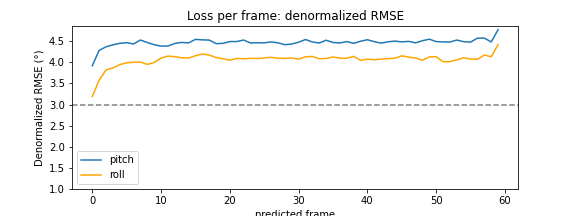


Figure 29: loss per frame for 10/60 (top) and 120/60 (bottom) IO-ratio with reference line at 3° (grey)

For each of the different configurations, the average loss per frame was calculated to observe error evolution over the predictions. In Figure 26, the two graphs are shown for resp. the worst and best IO-ratio. In the 10/60 LPF plot (top), the difference in pitch and roll prediction difficulty is very apparent. All LPF plots for this model resulted in a blue pitch line that is higher than the orange roll line in its entirety. Besides this, a remarkable and counterintuitive property of this model was observed. Only a **minor increase in prediction error** happens when predicting further into the future. It was expected that on average, the error would increase over the predicted sequence. However, the models predict with a close to constant error across the whole sequence and the magnitude of the error is mainly affected by the length of the input sequence. This behavior is similar to Zhao’s results, where a consistent error was found as well: prediction errors at the 5th second and 20th second had equal magnitudes (Zhao et al., 2004).

As a final test for this model, a higher **output sequence length of 120** was tested to evaluate if errors would start to increase over a longer predicted sequence. At two frames per second or 2 Hz, this model predicts a one minute window. A prediction of this duration provides a lot of agility to find the optimal window for take-off/landing. In assumption that the ideal input sequence length for this model is independent of the output length, 60/120 and 120/120 IO-ratios were chosen based on previous results. The loss per frame measures for these configurations are shown in Figure 30. In both cases an increase in pitch error is observed after the 60th frame whilst roll remains relatively constant. With **average PR error** of **2,52°** and **2,22°** for resp. 60/120 and 120/120, errors are similar to the 60/60 and 120/60 models, meaning that the increase in prediction length did not lead to a substantial decrease in accuracy. In conclusion, the encoder decoder LSTM was found to be a very reliable and accurate prediction model that outclassed Kaminskyi’s best model and best overall prediction. It was able to predict up to one minute for both pitch and roll with equal, consistent accuracy.

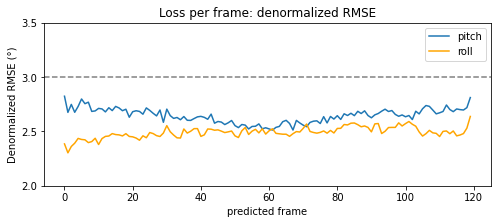
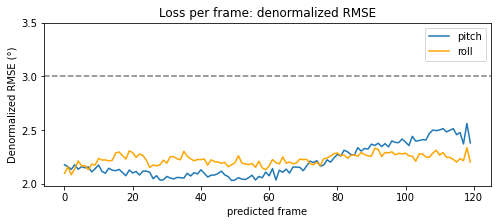


Figure 30: loss per frame for 60/120 (top) and 120/120 (bottom) IO-ratio with reference line at 3° (grey)



### Sequential CNN

The sequential CNN model is the only model to not use an LSTM architecture. For this reason, it was expected to have the highest difficulty learning the trend of the time series data causing it to perform worse than other models. However, the performance trade-off might be made up for by the expected lower inference time due to the absence of the LSTM module. The model was trained twice for two IO-ratios, each with only ten frames in the input sequence. The lower input sequence length was chosen in assumption that less images would be necessary to predict with the same level of accuracy as the encoder-decoder LSTM model. Additionally, the size of the concatenated image feature vector grows linearly with the number of input images. Processing more images in the input sequence quickly leads to high memory requirements which should be kept at a minimum as discussed in the objectives.

In Figure 31, the training and validation losses are shown for a 10/60 (blue) and 10/30 (orange) IO-ratio. As hypothesized, the model indeed shows very **poor convergence**. The 10/60 validation loss (dotted line) during training decreased as expected during the first ten epochs. However, from this point onward, validation loss did not continue to further decrease and instead followed a slight increasing trend. Training loss (solid line) on the other side, did proceed to further decrease across all training epochs. This indicates that the model suffered from slight overfitting after only a few epochs. Further testing was done with a higher IO-ratio of 10/30 to assess whether this poor convergence originated from a suboptimal IO-ratio. However, even with a shorter prediction window, only marginal improvement in convergence was measured . The validation loss once again reaches a minimum in the first ten epochs after which overfitting starts to occur where validation loss increases while training loss keeps decreasing. In both configurations, the **average errors** on the test dataset for both pitch and roll ranged around **five degrees**.

After observing these poor results, training had been done on the CNN LSTM hybrid models. These in contrast, did show very good performance at the same IO-ratios without significant increase in inference time compared to the sequential CNN. For these reasons, it was concluded that without an LSTM module, the sequential CNN could not achieve desired performance and was not further optimized nor evaluated.

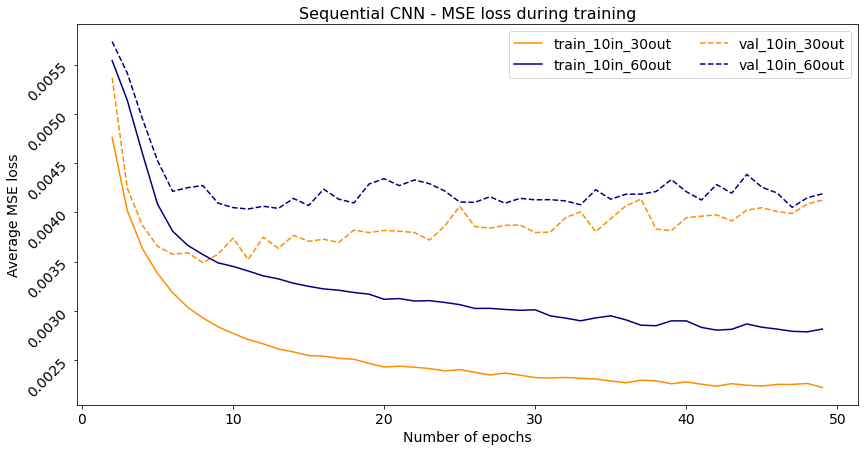


Figure 31: training and validation losses for different IO-ratios of the sequential CNN model

### CNN LSTM ensemble models

Compared to the sequential CNN model, the CNN LSTM ensemble models use an LSTM module to process the image feature vectors. Because of this, they are expected to perform best out of all models. Additionally, Kaminskyi’s models with both a CNN and LSTM module performed best as well. However, due to their complexity, they are also expected to suffer from the highest inference timings. Both CNN LSTM ensemble models will be compared in this section as their architecture is very similar with the only difference being the inputs they process, either only images (single input) or images and PR (dual input). Each model was trained and evaluated for a **10/60** and a **10/120 IO-ratio**. These ratios were chosen in order to compare prediction accuracy against the decoder encoder LSTM. The low input sequence length was once again chosen in assumption that less images are needed and to keep down memory requirements. The two models were also trained on **grayscale** images to lower computational demand and improve inference time.

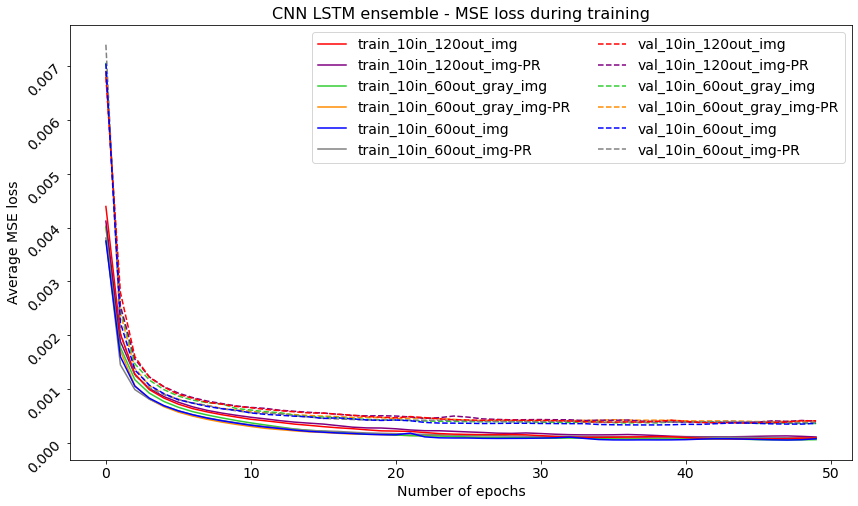
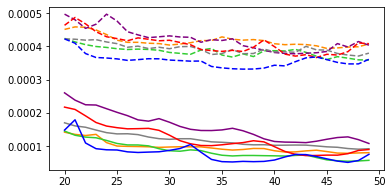


Figure 32: training and validation loss for CNN LSTM ensemble models



Out of all proposed architectures, the ensemble models were the most resource demanding models to train, each taking around three hours to complete fifty epochs on a cuda device. In Figure 32, the training and validation losses are shown for the **single (img)** and **dual (img-PR) input** model. Each configuration follows an almost identical path, even the grayscale ones. They improve rapidly during the first epochs after which the convergence rate decreases drastically. In the small window on the right, a more detailed view is provided of the last thirty epochs. All configurations of the CNN LSTM model reach a validation loss of around 0,0004 with only marginal difference between them. Overall, fifty epochs proved to be a good estimate for optimal training for any configuration of the CNN LSTM ensemble models.

In Table 13 the average denormalized errors are shown for both ensemble models. Four observations were made based on these results for the CNN LSTM ensemble model. **Firstly**, with the introduction of images, the previously observed recurring trend of pitch having higher errors than roll is not present. This indicates that the introduction of images leads to more equally accurate predictions of PR. **Secondly**, no significant increase or decrease in accuracy occurs when grayscale images are processed. Based on this observation, it can be safely assumed that this will hold true for any IO-ratio and can therefore be used as a means to lower computational requirements without compromise. **Thirdly,** no benefit was found in using both images and PR as input. Prediction errors for both input types – img and img-PR – are within a margin of insignificance. As a result, it was concluded that the computationally expensive addition of PR served no benefit towards accuracy. **Lastly,** based on LPF measurements, each configuration showed the same prediction bevahior as the encoder decoder LSTM where prediction accuracy remains consistent across the whole sequence.

|  |  |  |  |
| --- | --- | --- | --- |
| Input type(s) | IO-ratio | Average Pitch error [denormalized RMSE] | Average Roll error [denormalized RMSE] |
| img | 10/60 | 1,74° | 1,65° |
| img-PR | 10/60 | 1,67° | 1,76° |
| (gray) img | 10/60 | 1,77° | 1,66° |
| (gray) img-PR | 10/60 | 1,86° | 1,76° |
| img | 10/120 | 1,81° | 1,81° |
| img-PR | 10/120 | 1,76° | 1,78° |

Table 13: average denormalized RMSE for CNN LSTM single [img] and dual [img-PR] input model

In conclusion, the average prediction errors are near identical for each configuration of input types and IO-ratio. From the LPF metrics, it was observed that the accuracy remains consistent across the whole sequence. Compared to the encoder decoder LSTM, which already outperformed Kaminskyi’s best model and best result, the CNN LSTM ensemble models achieve even better performance by a significant margin (approx. 15%-25% PR error reduction).

## Augmented data

As discussed in 3.1.2, one sequence of augmented data was created by adding random ink blots to the images. These blots represent scenarios in which other objects are in the front of the vessel. Only the ensemble models were tested on this augmented sequence due to their excellent performance on images. It is expected that the dual input model might obtain better performance due to it not being solely dependent on images as input. To evaluate performance, only one heavily augmented sequence was created in assumption that results would be similar for other sequences and can only improve if a worst-case scenario is used.

Above in **Fout! Verwijzingsbron niet gevonden.** and **Fout! Verwijzingsbron niet gevonden.**, results are shown for resp. the single (img) and dual (img-PR) input ensemble model. Pitch predictions are shown in red on top of the real values in blue for both grayscale (left) and colored (right) images. For reference, predictions of the ensemble model on the non-augmented sequence have almost perfect overlap with the real values. These are added in the Appendix. When visually comparing both models, the single input model (top) shows significantly more divergence from the blue line than the dual input model (bottom). As hypothesized, this could be caused by the lack of PR as input. Having PR as additional input, the dual input model is less dependent on the clarity of the images. Additionally, processing greyscale images tends to negatively impact peak prediction ability. In both cases, the peaks in the second halve of the prediction window are more accurately predicted. Anticipating large movements is critical for safe landing of the drone and thus accurate peak prediction is of utmost importance. For this reason, it was concluded that the dual input model with colored images has the highest reliability and accuracy in obstruction dense environments.

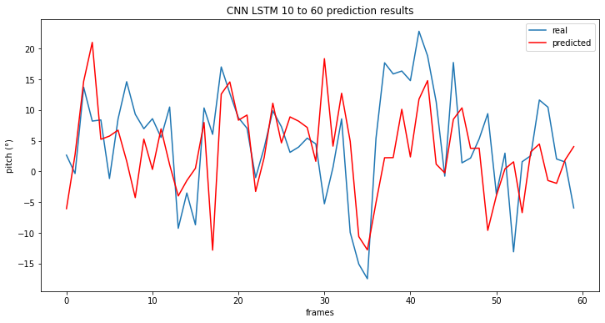
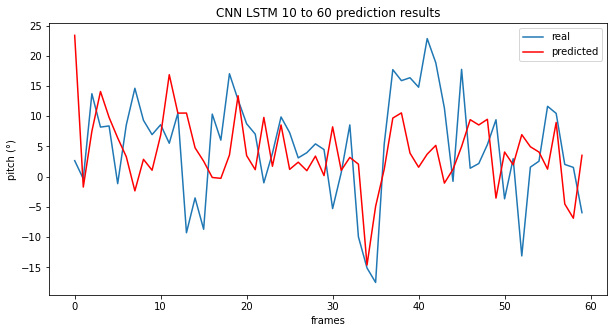


Figure 34a: CNN LSTM **single** input prediction (red) vs. real (blue) on augmented frames: grayscale (left) and colored (right)

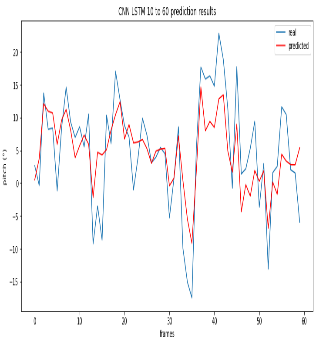
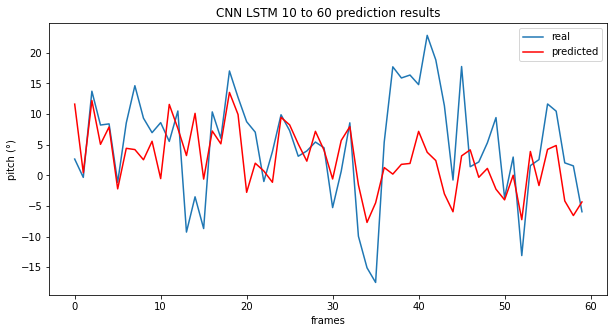


Figure 34b: CNN LSTM **dual** input prediction (red) vs. real (blue) on augmented frames: grayscale (left) and colored (right)

## Inference time

As discussed in the objectives, computational demand and inference time are equally important compared to prediction accuracy. In this section, all proposed models are compared in their optimal form. This optimal form is based on the results discussed in the previous sections: both prediction length and prediction accuracy should be optimized. In this fully optimized form, inference time or latency is used to make a final conclusion on which model is best overall. As discussed in 5.3.22.6, inference time is measured as the average over ten thousand predictions. The single step model is not evaluated as it cannot predict sequences.

Table 14 provides a summary of the results from each multi step model. Error values for each model are included in order to compare inference time and accuracy. These errors are calculated as the average of both pitch and roll over all predictions across all test dataset sequences. As expected, all image processing models have a drastically higher latency. The use of grayscale images improves latency by around 20%. However, this is not enough to make them viable options compared to the encoder decoder LSTM which is around twenty times faster and only marginally less accurate compared to the best performing image processing models.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Model name | IO-ratio | Inference time | Avg. PR error | Trainable parameters |
| Encoder-Decoder LSTM | 120/60 | 155ms | 2° | 1.211.010 |
| Sequential CNN | 10/30 | 4.203ms | 5,79° | 98.639.180 |
| CNN LSTM [img] | 10/120 | 4.042ms | 1,73° | 217.659.752 |
| CNN LSTM [img] (gray) | 10/120 | 3.545ms | 1,71° | 217.659.352 |
| CNN LSTM [img-PR] | 10/120 | 4.453ms | 1,72° | 217.741.672 |
| CNN LSTM [img-PR] (gray) | 10/120 | 3.797ms | 1,81° | 217.741.272 |

Table 14: inference timing, PR error and number of trainable parameters for each model’s optimal configuration

As a final note, inference time measurements were taken on various IO-ratios for each model. This was done in order to evaluate whether this had effect on the inference time. It was concluded that no meaningful change in latency occurs when changing the IO-ratio. However, image processing models were only trained for different output sequence lengths. It is expected that inference time of these models will change linearly with change in the number of input frames.

## Summary

In this chapter, each model proposed in Chapter 4 was rigorously evaluated to form a final conclusion on one optimal architecture. In thefirst section, three hyperparameters were optimized: number of epochs, learning rate and LSTM hidden size. As an alternative to HyperBand optimization, three values were evaluated for each parameter in order to find a trend in performance and determine an optimal value. These three parameters were chosen as they were expected to have the highest impact on model performance. It was concluded that for the number of epochs and the learning rate resp. fifty and 0,001 were near optimal values. As for hidden size, no concrete number was chosen, however it was found that higher hidden sizes, resulted in better performance. Additionally, the effect of activation functions was assessed. In related work, ReLU activations are used to activate LSTM outputs. However, it was found that model performance decreases, although by a small margin, if ReLU activations are used. Tanh activations on the final output proved to be non-influential towards performance.

In the following sections, each model was evaluated individually based on prediction accuracy, convergence, error consistency and inference time. The encoder decoder LSTM was able to accurately predict at least one minute of future pitch and roll values with consistent error of approximately 2°. The sequential CNN did not perform very well as it lacked an LSTM module. It showed poor convergence and suffered from overfitting. The CNN LSTM ensemble models on the contrary did perform exceedingly well, only needing five seconds to predict a one-minute window with consistent errors of around 1,7°. However, they had an extremely high inference time. As an attempt to lower inference time, they were also trained with grayscale images, but this only resulted in marginally lower inference time and even decreased accuracy on augmented data. In conclusion, the CNN LSTM ensemble models achieved most accurate predictions. However, they have high latency and quickly lose accuracy when objects are in frame of the camera. For these reasons, the **encoder decoder LSTM** is proposed as final and optimal model architecture.

# Conclusion

The objective of this thesis was to research and implement a method for ship motion prediction using an on-board IMU motion sensor and a front facing camera. The predictions should be optimally designed to aid in take off and landing for drones on a vessel. The drone should be able to anticipate movements of the vessel based on these predictions to reduce landing impact. Finally, the method should be capable of real-time low latency predictions on a continuous data stream with minimal hardware requirements.

To define ship motion, six degrees of freedom were used: pitch, roll, yaw, heave, sway and surge. Due to the nature of the problem, pitch and roll were chosen as primary prediction target as they are most influential towards ship stability and cannot be controlled. With these targets, ship motion was defined as a sequence of pitch and roll values. In order to predict these sequences, five deep learning neural network architectures were designed and evaluated on a simulated dataset. Empirical results show that models with an LSTM module achieve higher accuracy and that it is possible to achieve low prediction error with any of the available input types – pitch and roll and/or images. However, including images in the input of the model resulted in an increase in latency. Additionally, the use of images introduces problems when visibility is low or when objects like other vessels are in frame. Based on these results, the encoder decoder LSTM was selected as the optimal neural network architecture. It achieves high accuracy, low latency and has no dependency on image clarity.

The objective of the thesis was reached but not to the full extent. Ship motion prediction was achieved in an accurate and low latency manner. However, real-time predictions were not tested. In addition, due to the late availability of real data only a simulated dataset was used. The proposed models show promising results, but further research is necessary to fully develop the system for deployment.

The key contribution of this thesis were:

* Design and implementation of five deep neural network architectures for ship motion prediction using a simulated dataset of images, pitch signals and roll signals
* Optimization of the following hyperparameters: number of epochs, learning rate, LSTM hidden size, input sequence length and output sequence length
* Thorough evaluation of performance of each model architecture based on convergence and prediction accuracy, consistency and latency
* Experimentation with augmented data to close the gap between simulated and real environments

## Future work

For future work, the main goal is to transition to real data. In the first place, a very generous dataset would have to be collected on the vessel of deployment. In order for the model to generalize well to the vessel’s behavior, substantial amounts of data of many different sea conditions are needed. This data will have to be cleaned and sampled to an optimal rate. Additionally, more motion parameters could be added to the predicted features to further aid in impact reduction and anticipation. In this thesis, only pitch and roll were predicted. However, heave – the upward and downwards motion along a vertical axis – also plays a key role in smoothening the drone landing. Other metrics such as linear and angular acceleration could also prove to be useful for better predictions. All these metrics are captured by the on-board IMU sensor.

Besides the transition to real, more optimizations can be done on the model architectures. The models using both a CNN and LSTM module achieved overall highest prediction accuracy. However, they suffered from high inference times which made them less appealing. Further optimizing could be performed to lower their computational demand and decrease their latency. For example, the slow concatenation of the PR values and the image feature vectors could be replaced by a more efficient operation. As of right now, this operation is on average four times slower on a cuda device compared to a CPU due a bug in the PyTorch tensor concatenation function. With a lower inference time, the CNN LSTM models could potentially outperform the encoder decoder LSTM. Additionally, hyperparameter optimization could be performed with specially designed algorithms such as HyperBand (Li et al., 2018) to fully optimize hyperparameters for each model individually. As a final suggestion for future work, the real-time prediction behavior of each architecture could be evaluated. If predictions are accurate enough, it could be possible that the model only needs to predict at for example a five or ten second interval rather than at the frequency of the data stream (2Hz for simulated data). Ideally, a model would only have to make a prediction at the end of the previous prediction’s duration to achieve minimal computations.

# References

Abujoub, S. (2019). *Development of a Landing Period Indicator and the use of Signal Prediction to Improve Landing Methodologies of Autonomous Unmanned Aerial Vehicles on Maritime Vessels*. Carleton University.

Boser, B. E., Guyon, I. M., & Vapnik, V. N. (1992). Training algorithm for optimal margin classifiers. *Proceedings of the Fifth Annual ACM Workshop on Computational Learning Theory*, 144–152. https://doi.org/10.1145/130385.130401

Brownlee, J. (2017). *Gentle Introduction to the Adam Optimization Algorithm for Deep Learning*. Machinelearningmastery. https://machinelearningmastery.com/adam-optimization-algorithm-for-deep-learning/

Brownlee, J. (2018). *Multi-Step LSTM Time Series Forecasting Models for Power Usage*. Deep Learning for Time Series. https://machinelearningmastery.com/how-to-develop-lstm-models-for-multi-step-time-series-forecasting-of-household-power-consumption/

Canziani, A., Paszke, A., & Culurciello, E. (2016). *An Analysis of Deep Neural Network Models for Practical Applications*. https://doi.org/10.48550/arxiv.1605.07678

Chen, J., Benesty, J., Huang, Y., & Doclo, S. (2006). New insights into the noise reduction Wiener filter. *IEEE Transactions on Audio, Speech and Language Processing*, *14*(4), 1218–1233. https://doi.org/10.1109/TSA.2005.860851

Claesen, M., & de Moor, B. (2015). *Hyperparameter Search in Machine Learning*. https://doi.org/10.48550/arxiv.1502.02127

Cui, Z., Ke, R., Pu, Z., & Wang, Y. (2020). Stacked bidirectional and unidirectional LSTM recurrent neural network for forecasting network-wide traffic state with missing values. *Transportation Research Part C: Emerging Technologies*, *118*. https://doi.org/10.1016/J.TRC.2020.102674

de Cubber, G. (2019). *OPPORTUNITIES AND SECURITY THREATS POSED BY NEW TECHNOLOGIES*.

de Masi, G., Gaggiotti, F., Bruschi, R., & Venturi, M. (2011). Ship motion prediction by radial basis neural networks. *IEEE SSCI 2011 - Symposium Series on Computational Intelligence - HIMA 2011: 2011 IEEE Workshop on Hybrid Intelligent Models and Applications*, 28–32. https://doi.org/10.1109/HIMA.2011.5953967

Dhanya, J., & Raghukanth, S. T. G. (2018). Ground Motion Prediction Model Using Artificial Neural Network. *Pure and Applied Geophysics*, *175*(3), 1035–1064. https://doi.org/10.1007/S00024-017-1751-3/FIGURES/22

Doshi Sanket. (2019). *Various Optimization Algorithms For Training Neural Network*. Towards Data Science. https://towardsdatascience.com/optimizers-for-training-neural-network-59450d71caf6

Fossen, S., & Fossen, T. I. (2018). EXogenous Kalman filter (XKF) for Visualization and Motion Prediction of Ships using Live Automatic Identification System (AIS) Data. *Modeling, Identification and Control*, *39*(4), 233–244. https://doi.org/10.4173/MIC.2018.4.1

Geifman, A. (2020). *How to Measure Inference Time of Deep Neural Networks | Deci*. Deci.Ai. https://deci.ai/blog/measure-inference-time-deep-neural-networks/

Grewal, M. S., & Andrews, A. P. (2010). Applications of Kalman Filtering in Aerospace 1960 to the Present. *IEEE Control Systems*, *30*(3), 69–78. https://doi.org/10.1109/MCS.2010.936465

Guan, B., Yang, W., Wang, Z., & Tang, Y. (2018). Ship roll motion prediction based on ℓ1 regularized extreme learning machine. *PLoS ONE*, *13*(10). https://doi.org/10.1371/JOURNAL.PONE.0206476

Ham, S.-H., Roh, M.-I., & Zhao, L. (2017). *Integrated method of analysis, visualization, and hardware for ship motion simulation*. https://doi.org/10.1016/j.jcde.2017.12.005

He, K., Zhang, X., Ren, S., & Sun, J. (2015). Deep Residual Learning for Image Recognition. *Proceedings of the IEEE Computer Society Conference on Computer Vision and Pattern Recognition*, *2016-December*, 770–778. https://doi.org/10.48550/arxiv.1512.03385

Hochreiter, S., & Schmidhuber, J. (1997). Long Short-Term Memory. *Neural Computation*, *9*(8), 1735–1780. https://doi.org/10.1162/NECO.1997.9.8.1735

Johansen, T. A., & Fossen, T. I. (2017). The eXogenous Kalman Filter (XKF). *International Journal of Control*, *90*(2), 177–183. https://doi.org/10.1080/00207179.2016.1172390

Kalman, R. E. (1960). A New Approach to Linear Filtering and Prediction Problems. *Transactions of the ASME--Journal of Basic Engineering*, *82*(Series D), 35–45.

Kaminskyi, N.-M. (2019a). *Deep learning models for ship motion prediction from images*.

Kaminskyi, N.-M. (2019b). *Ship Ocean Simulation in Blender*. GitHub.Com. https://github.com/Nazotron1923/ship-ocean\_simulation\_BLENDER

Kingma, D. P., & Ba, J. L. (2014). Adam: A Method for Stochastic Optimization. *3rd International Conference on Learning Representations, ICLR 2015 - Conference Track Proceedings*. https://doi.org/10.48550/arxiv.1412.6980

Kingma, D. P., & Welling, M. (2019). An Introduction to Variational Autoencoders. *Foundations and Trends in Machine Learning*, *12*(4), 307–392. https://doi.org/10.1561/2200000056

Kouris, A., Venieris, S. I., Rizakis, M., & Bouganis, C.-S. (2019). *Approximate LSTMs for Time-Constrained Inference: Enabling Fast Reaction in Self-Driving Cars*. www.imperial.ac.uk/intelligent-digital-systems/approx-lstms/

le Guen, V., & Thome, N. (2022). *Deep Time Series Forecasting with Shape and Temporal Criteria*.

Li, L., Jamieson, K., DeSalvo, G., Rostamizadeh, A., & Talwalkar, A. (2016). Hyperband: A Novel Bandit-Based Approach to Hyperparameter Optimization. *Journal of Machine Learning Research*, *18*, 1–52. https://arxiv.org/abs/1603.06560v4

Li, L., Jamieson, K., Rostamizadeh, A., & Talwalkar, A. (2018). Hyperband: A Novel Bandit-Based Approach to Hyperparameter Optimization. *Journal of Machine Learning Research*, *18*, 1–52. http://jmlr.org/papers/v18/16-558.html.

Lopez Pinaya, W. H., Vieira, S., Garcia-Dias, R., & Mechelli, A. (2020). Autoencoders. *Machine Learning: Methods and Applications to Brain Disorders*, 193–208. https://doi.org/10.48550/arxiv.2003.05991

Luo, F. L., Unbehauen, R., & Cichocki, A. (1997). A Minor Component Analysis Algorithm. *Neural Networks*, *10*(2), 291–297. https://doi.org/10.1016/S0893-6080(96)00063-9

“MarLand.” (2020). *MarLand – Robotics & Autonomous Systems*. https://mecatron.rma.ac.be/index.php/projects/marland/

“MarSur.” (2019). *MarSur – Robotics & Autonomous Systems*. https://mecatron.rma.ac.be/index.php/projects/marsur/

Mealey, T., & Taha, T. M. (2018). Accelerating Inference in Long Short-Term Memory Neural Networks. *Proceedings of the IEEE National Aerospace Electronics Conference, NAECON*, *2018-July*, 382–390. https://doi.org/10.1109/NAECON.2018.8556674

Minsky, M., & Papert, S. A. (1969). Perceptrons: An Introduction to Computational Geometry. In *Perceptrons*. The MIT Press. https://doi.org/10.7551/MITPRESS/11301.001.0001

Nayfeh, A. H., Mook, D. T., & Marshall, L. R. (2012). Nonlinear Coupling of Pitch and Roll Modes in Ship Motions. *Https://Doi.Org/10.2514/3.62949*, *7*(4), 145–152. https://doi.org/10.2514/3.62949

Peng, X., Zhang, B., & Rong, L. (2019). A robust unscented Kalman filter and its application in estimating dynamic positioning ship motion states. *Journal of Marine Science and Technology (Japan)*, *24*(4), 1265–1279. https://doi.org/10.1007/S00773-019-00624-5

Perez, T. ;, & Blanke, M. (2017). Ship Roll Damping Control. *Annual Reviews in Control*, *36*(1), 129–147. https://doi.org/10.1016/j.arcontrol.2012.03.010

Perez, T., & Fossen, T. I. (2005). Kinematics of ship motion. *Advances in Industrial Control*, *9781852339593*, 45–58. https://doi.org/10.1007/1-84628-157-1\_3

Q. Judge, C. (2019). Ship motion in waves. In *Seakeeping and Maneuvering*. https://www.usna.edu/NAOE/\_files/documents/Courses/EN455/AY20\_Notes/EN455CourseNotesAY20\_FrontMaterial.pdf

Ran, T., Tong, S., Yang, Y., & Zhang, H. (2021). Research and Application on Mathematical Model of Ship Manoeuvring Motion under Shallow water effect. *IOP Conference Series: Earth and Environmental Science*, *643*(1). https://doi.org/10.1088/1755-1315/643/1/012127

Rashid, M. H., Zhang, J., & Minghao, Z. (2021). Real-Time Ship Motion Forecasting Using Deep Learning. *The 2nd International Conference on Computing and Data Science*, *5*(2021). https://doi.org/10.1145/3448734

Ren, X., Yang, T., Erran Li, L., Alahi, A., & Chen, Q. (2021). Safety-aware Motion Prediction with Unseen Vehicles for Autonomous Driving. *IEEE Explore*. https://github.com/

Ruder, S. (2016). *An overview of gradient descent optimization algorithms*. http://caffe.berkeleyvision.org/tutorial/solver.html

Rumelhart, D. E., Hinton, G. E., & Williams, R. J. (1986). Learning representations by back-propagating errors. *Nature 1986 323:6088*, *323*(6088), 533–536. https://doi.org/10.1038/323533a0

Rumelhart E., D., Hinton E., G., & Williams J., R. (1986). Learning representations by back-propagating errors. *Letters To Nature*.

Sharma, S., Sharma, S., & Athaiya, A. (2020). ACTIVATION FUNCTIONS IN NEURAL NETWORKS. *International Journal of Engineering Applied Sciences and Technology*, *4*, 310–316. http://www.ijeast.com

Shen Kevin. (2018). *Effect of batch size on training dynamics*. Medium. https://medium.com/mini-distill/effect-of-batch-size-on-training-dynamics-21c14f7a716e

Sherstinsky, A. (2018). Fundamentals of Recurrent Neural Network (RNN) and Long Short-Term Memory (LSTM) Network. *Physica D: Nonlinear Phenomena*, *404*. https://doi.org/10.1016/j.physd.2019.132306

Silva, M. (2015). Ocean Surface Wave Spectrum. In *Physical Oceanography*. https://www.researchgate.net/publication/283722827\_Ocean\_Surface\_Wave\_Spectrum

Skulstad, R., Li, G., Fossen, T. I., Wang, T., & Zhang, H. (2021). A Co-Operative hybrid model for ship motion prediction. *Modeling, Identification and Control*, *42*(1), 17–26. https://doi.org/10.4173/MIC.2021.1.2

Srivastava, N., Hinton, G., Krizhevsky, A., Sutskever, I., & Salakhutdinov, R. (2014). Dropout: A Simple Way to Prevent Neural Networks from Overfitting. *Journal of Machine Learning Research*, *15*(56), 1929–1958. http://jmlr.org/papers/v15/srivastava14a.html

Stewart, R. H. (2008). *Introduction to Physical Oceanography*. http://www.madsci.org/posts/archives/2004-11/1101806651.Es.r.html

Stock, J. H., & Watson, M. W. (2001). Vector Autoregressions. *Journal of Economic Perspectives*, *15*(4), 101–115. https://doi.org/10.1257/JEP.15.4.101

Szegedy, C., Liu, W., Jia, Y., Sermanet, P., Reed, S., Anguelov, D., Erhan, D., Vanhoucke, V., & Rabinovich, A. (2014). Going Deeper with Convolutions. *Proceedings of the IEEE Computer Society Conference on Computer Vision and Pattern Recognition*, *07-12-June-2015*, 1–9. https://doi.org/10.48550/arxiv.1409.4842

Tang, Y., Ma, L., Liu, W., & Zheng, W. S. (2018). Long-Term Human Motion Prediction by Modeling Motion Context and Enhancing Motion Dynamic. *IJCAI International Joint Conference on Artificial Intelligence*, *2018-July*, 935–941. https://doi.org/10.48550/arxiv.1805.02513

Wang, Q., Ma, Y., Zhao, K., & Tian, Y. (2022a). A Comprehensive Survey of Loss Functions in Machine Learning. *Annals of Data Science*, *9*(2), 187–212. https://doi.org/10.1007/s40745-020-00253-5

Wang, Q., Ma, Y., Zhao, K., & Tian, Y. (2022b). A Comprehensive Survey of Loss Functions in Machine Learning. *Annals of Data Science*, *9*(2), 187–212. https://doi.org/10.1007/S40745-020-00253-5/TABLES/8

Wei, Y., Chen, Z., Zhao, C., Chen, X., Tu, Y., & Zhang, C. (2022). Big multi-step ship motion forecasting using a novel hybrid model based on real-time decomposition, boosting algorithm and error correction framework. *Ocean Engineering*, *256*, 111471. https://doi.org/10.1016/J.OCEANENG.2022.111471

Wilson, D. R., & Martinez, T. R. (2001). The need for small learning rates on large problems. *Proceedings of the International Joint Conference on Neural Networks*, *1*, 115–119. https://doi.org/10.1109/IJCNN.2001.939002

Wu, J. (2017). *Introduction to Convolutional Neural Networks*.

Zhang, T., Zheng, X. Q., & Liu, M. X. (2021). Multiscale attention-based LSTM for ship motion prediction. *Ocean Engineering*, *230*. https://doi.org/10.1016/J.OCEANENG.2021.109066

Zhao, X., Xu, R., & Kwan, C. (2004). Ship-motion prediction: Algorithms and simulation results. *ICASSP, IEEE International Conference on Acoustics, Speech and Signal Processing - Proceedings*, *5*. https://doi.org/10.1109/ICASSP.2004.1327063

Zhong-yi, Z. (2012). An adaptive ship motion prediction method based on parameter estimation. *Journal of Ship Mechanics*.

###### Individual predictions and LPF

For each multi step model, a prediction was plotted for one IO-sequence. The results of these predictions are added in this appendix because they provide a good visual representation of how accurate a model is. The predicted sequence is always shown in red on top of the real sequence in blue. The specific IO-ratio and model that was used is mentioned in the caption. **Pitch** will always be shown in the **top** graph and **roll** in the **middle** graph. At the **bottom**, the LPF graph is shown.

Figure 35: encoder decoder LSTM - 60/60

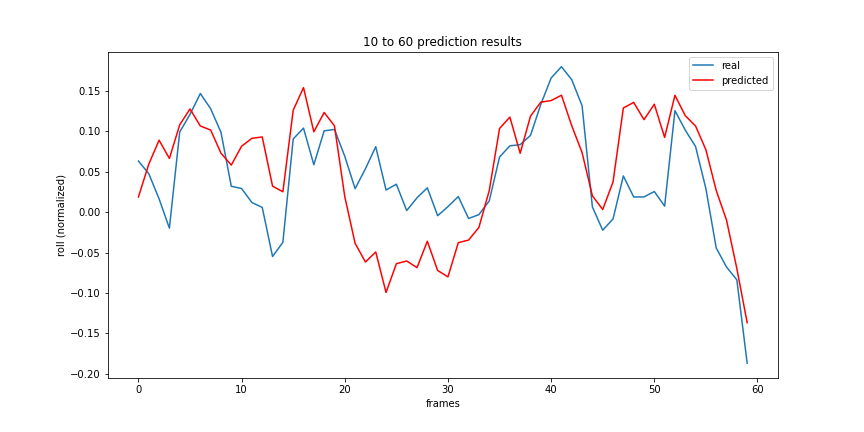
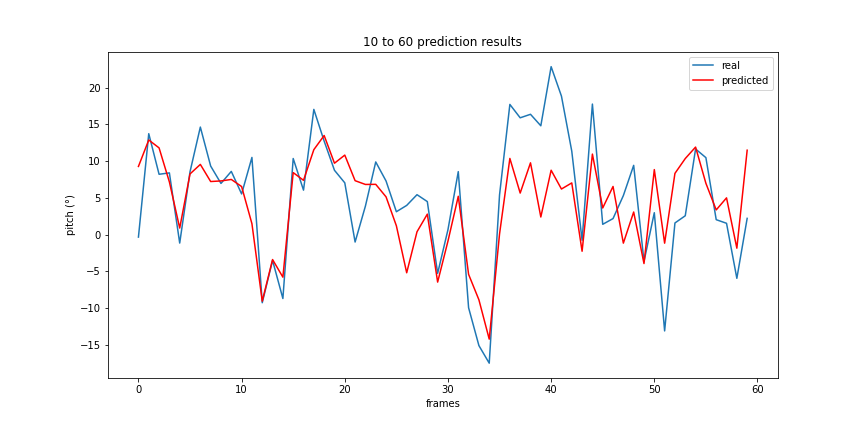
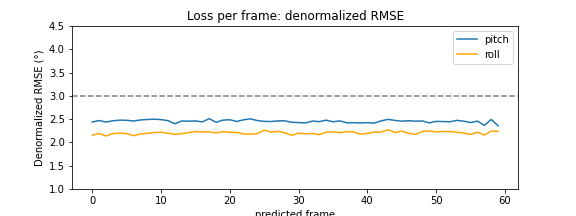
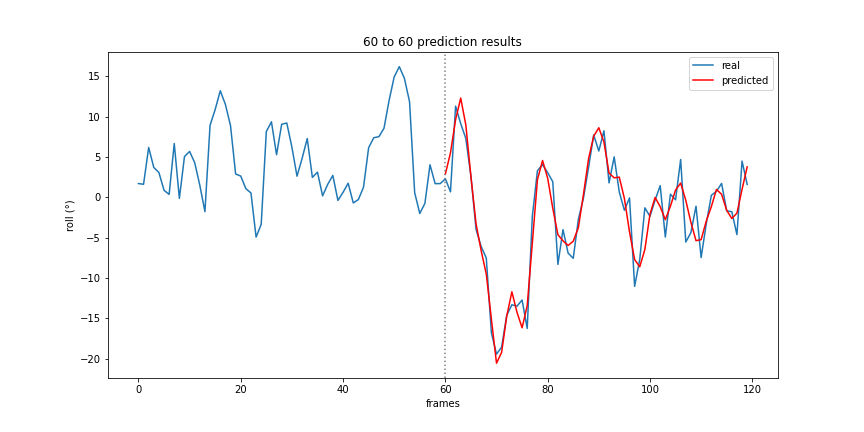
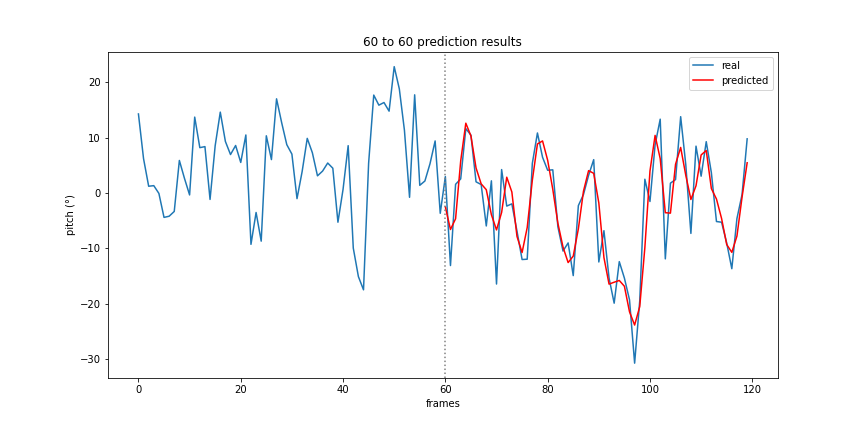


Figure 36: Sequential CNN - 10/60

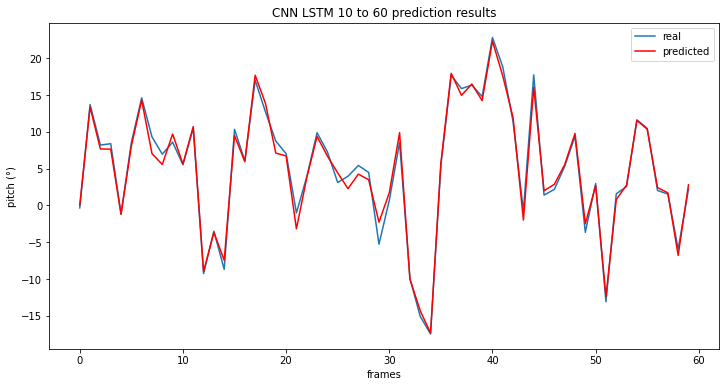
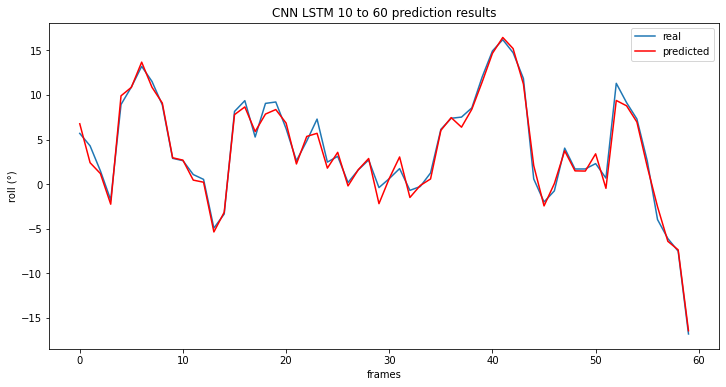
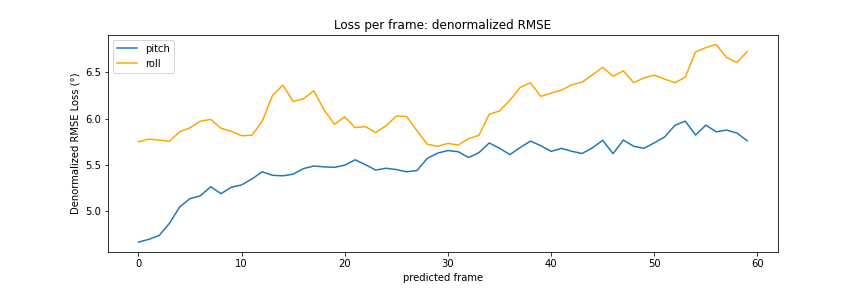


Figure 37: CNN LSTM single input (colored) - 10/60

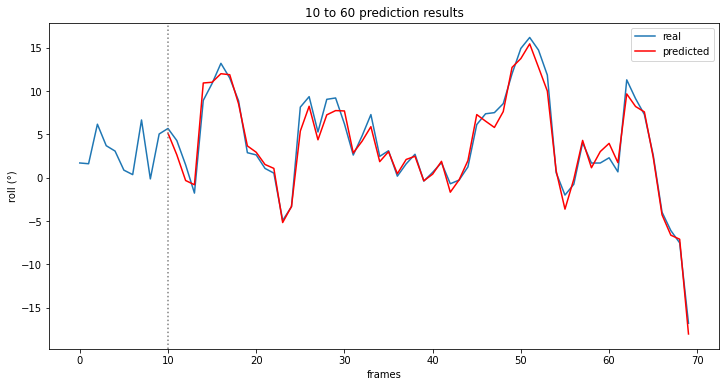
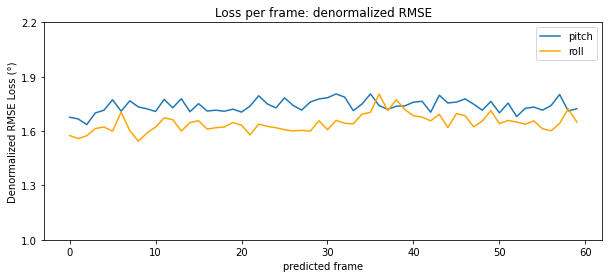


Figure 38: CNN LSTM dual input (colored) - 10/60

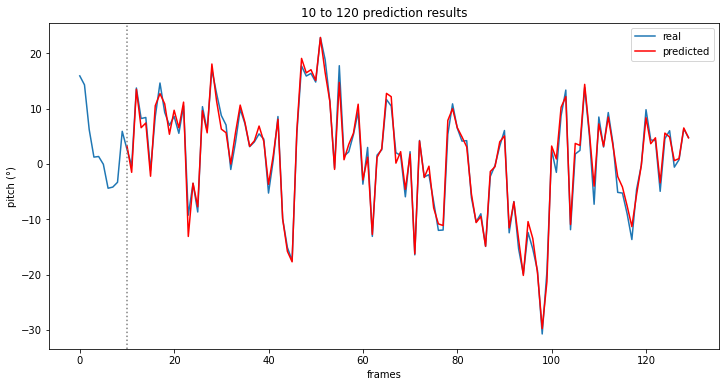
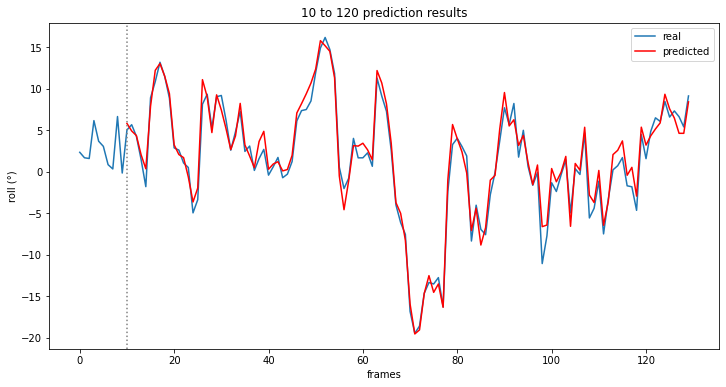
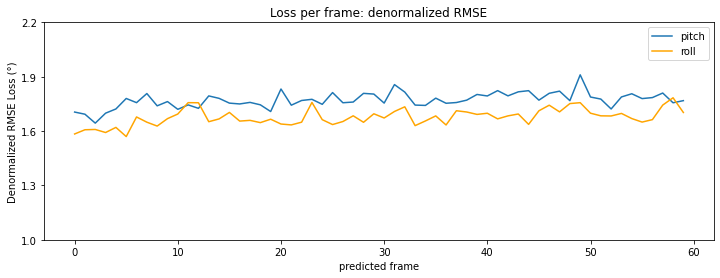


Figure 39: CNN LSTM dual input (colored) - 10/120

