Angular

**Tangential** 

A rads revs degrees

S m cm km

 $\omega = \frac{\text{rads}}{\text{s}} = \frac{\text{revs}}{\text{s}} = \frac{\text{degrees}}{\text{s}}$ 

 $v_t$  m/s cm/s km/s

 $\alpha \frac{\text{rads}}{\text{s}^2} \frac{\text{revs}}{\text{s}^2} \frac{\text{degrees}}{\text{s}^2}$ 

 $a_t$  m/s<sup>2</sup> km/s<sup>2</sup> cm/s<sup>2</sup>

Angular

A rads revs degrees

 $\omega$   $\frac{\text{rads}}{\text{s}}$   $\frac{\text{revs}}{\text{s}}$   $\frac{\text{degrees}}{\text{s}}$ 

 $\alpha \frac{\text{rads}}{\text{s}^2} \frac{\text{revs}}{\text{s}^2} \frac{\text{degrees}}{\text{s}^2}$ 

Tangential

 $S^{4}$  5 6 m cm km

 $v_t$  m/s cm/s km/s

 $a_t$  m/s<sup>2</sup> km/s<sup>2</sup> cm/s<sup>2</sup>

$$\alpha \frac{\text{rads}}{\text{s}^2} \frac{\text{revs}}{\text{s}^2} \frac{\text{degrees}}{\text{s}^2}$$

Tangential

S m cm km

 $v_t^{5}$   $^{6}$  m/s cm/s km/s

 $a_{t}$  m/s<sup>2</sup> km/s<sup>2</sup> cm/s<sup>2</sup>

$$lpha rac{1}{\mathrm{rads}} rac{3}{\mathrm{revs}} rac{2}{\mathrm{degrees}}$$

Tangential

S m cm km

 $v_t^{5}$   $^{6}$  m/s cm/s km/s

 $a_t^{4}$   $_{\text{m/s}^2}^{6}$   $_{\text{cm/s}^2}^{5}$ 

$$egin{array}{cccccc} Herminist & Hermini$$

$$\alpha = \frac{1}{\frac{1}{s^2}} = \frac{3}{\frac{1}{s^2}} = \frac{2}{\frac{1}{s^2}}$$

**Tangential** 

S m cm km

 $v_t^{5}$  4 6 m/s cm/s km/s

 $a_t^{4}$   $_{\text{m/s}^2}^{6}$   $_{\text{cm/s}^2}^{5}$ 

$$s = \theta r$$
$$v_t = \omega r$$
$$a_t = \alpha r$$

How does  $\omega$  compare for points S and R?

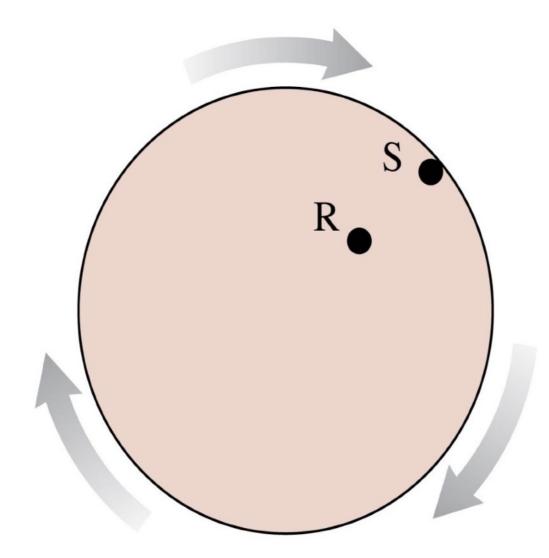
How does compare for points S and R?

How do the accelerations compare for points S and R?

How does  $\omega$  compare for points S and R?

How does v<sub>t</sub> compare for points S and R?

How do the accelerations compare for points S and R?



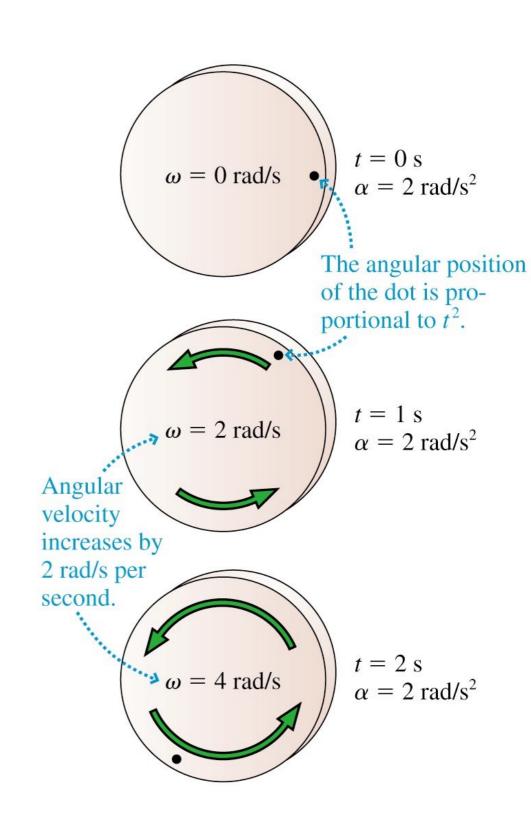
### Angular Acceleration

#### Nonuniform circular motion

$$\alpha \equiv \frac{d\omega}{dt}$$
 (angular acceleration)

units of 
$$\frac{\text{rad}}{\text{s}^2}$$

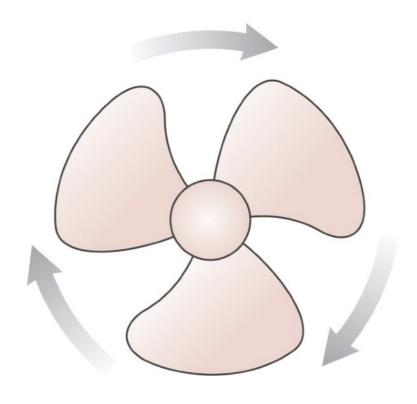
$$a_t = \alpha r$$



### Question #

The fan blade is slowing down. What are the signs of  $\omega$  and  $\alpha$ ?

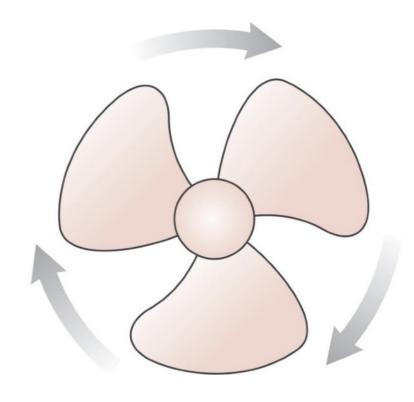
- A.  $\omega$  is positive and  $\alpha$  is positive.
- B.  $\omega$  is positive and  $\alpha$  is negative.
- C.  $\omega$  is negative and  $\alpha$  is positive.
- D.  $\omega$  is negative and  $\alpha$  is negative.
- E.  $\omega$  is positive and  $\alpha$  is zero.



### Quiz

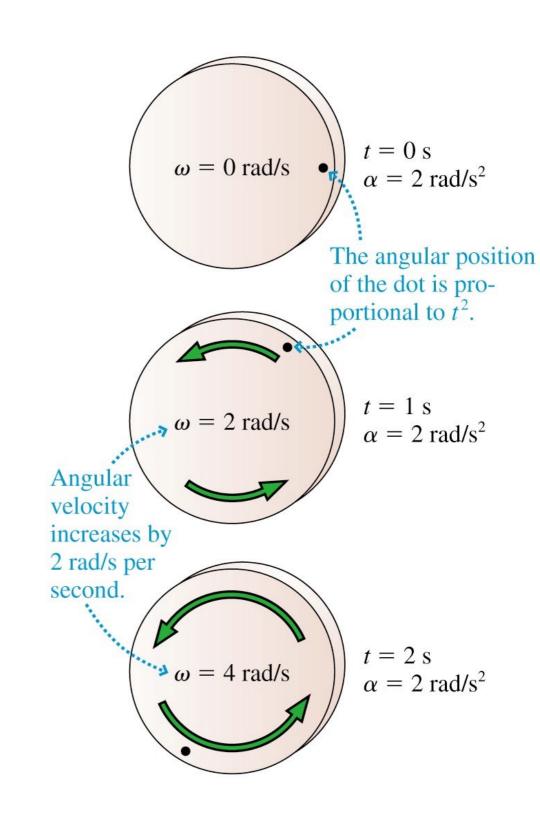
The fan blade is slowing down. What are the signs of  $\omega$  and  $\alpha$ ?

- A.  $\omega$  is positive and  $\alpha$  is positive.
- B.  $\omega$  is positive and  $\alpha$  is negative.
- C.  $\omega$  is negative and  $\alpha$  is positive.
- D.  $\omega$  is negative and  $\alpha$  is negative.
- E.  $\omega$  is positive and  $\alpha$  is zero.



## Angular Acceleration

- $\alpha$  is positive if  $|\omega|$  is increasing and  $\omega$  is counter-clockwise.
- $\alpha$  is positive if  $|\omega|$  is decreasing and  $\omega$  is clockwise.
- $\alpha$  is negative if  $|\omega|$  is increasing and  $\omega$  is clockwise.
- $\alpha$  is negative if  $|\omega|$  is decreasing and  $\omega$  is counter-clockwise.

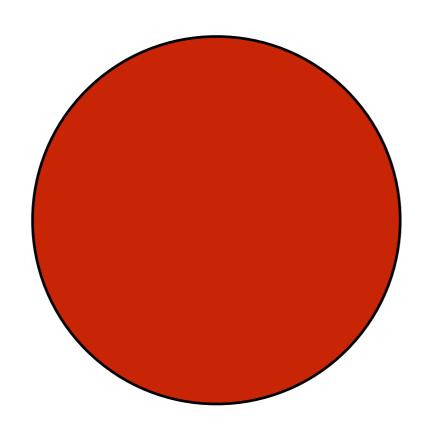


# Angular Kinematics

Rotational kinematics	Linear kinematics
$\omega_{\rm f} = \omega_{\rm i} + \alpha  \Delta t$	$v_{\rm fs} = v_{\rm is} + a_{\rm s} \Delta t$
$\theta_{\rm f} = \theta_{\rm i} + \omega_{\rm i}  \Delta t + \frac{1}{2} \alpha (\Delta t)^2$	$s_{\rm f} = s_{\rm i} + v_{\rm is} \Delta t + \frac{1}{2} a_{\rm s} (\Delta t)^2$
$\omega_{\rm f}^2 = \omega_{\rm i}^2 + 2\alpha\Delta\theta$	$v_{\rm fs}^2 = v_{\rm is}^2 + 2a_s \Delta s$

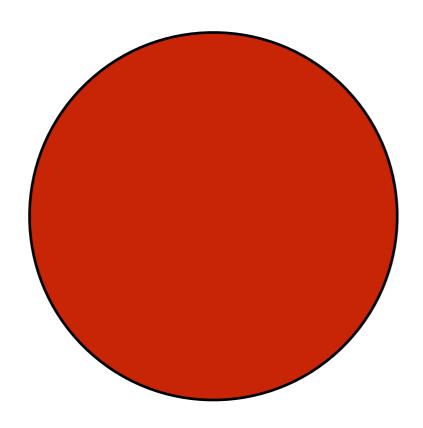
## Conceptualizing Circular Motion

A merry-go-round is spinning at a rate of 0.5 revs/s and is slowing at a rate of 0.034 rad/s<sup>2</sup>. Through how many radians will the merry-go-round turn through as it comes to rest.



## Conceptualizing Circular Motion

A merry-go-round is initially at rest. You begin pushing on it and cause it to speed up. After pushing for 2 minutes you measure the speed of the merry-go-round to be 1.5 revs/second. What was the acceleration of the wheel?



#### Turbine Problem

A turbine is spinning at 3800 rpm. Friction in the bearings is so low that it takes 10 min to coast to a stop. How many revolutions does the turbine make while stopping?

### New Equations

$$\vec{v}_t = \omega r$$

$$v_t = \frac{ds}{dt}$$

$$\vec{a}_c = \frac{v_t^2}{r}$$

$$s = r\theta$$

$$\omega = \frac{d\theta}{dt}$$

$$a_t = \alpha r$$

$$\alpha = \frac{d\omega}{dt}$$

$$\omega_f = \omega_i + \alpha \Delta t$$

$$\theta_f = \theta_i + \omega_i \Delta t + \frac{1}{2} \alpha \Delta t^2$$

$$\omega_f^2 = \omega_i^2 + 2\alpha\Delta\theta$$

### New Equations

$$\vec{v}_t = \omega r \left[ 5 \right]$$

$$\vec{a}_c = \frac{v_t^2}{r} \left[ 8 \right]$$

$$v_t = \frac{ds}{dt} \left[ 7 \right] \qquad s = r\theta \left[ 3 \right]$$

$$s = r\theta$$
 3

$$\omega = \frac{d\theta}{dt} \left[ 2 \right]$$

$$a_t = \alpha r \left[ 9 \right]$$

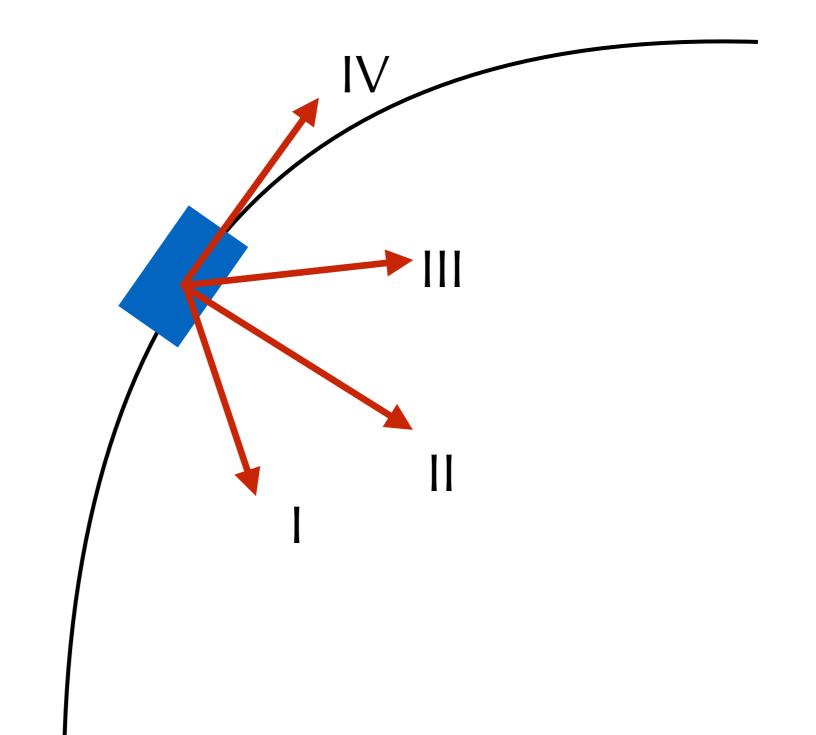
$$\omega_f = \omega_i + \alpha \Delta t \quad \boxed{1}$$

$$\alpha = \frac{d\omega}{dt} \left[ 4 \right]$$

$$\theta_f = \theta_i + \omega_i \Delta t + \frac{1}{2} \alpha \Delta t^2 \ \boxed{6}$$

$$\omega_f^2 = \omega_i^2 + 2\alpha\Delta\theta \ \ \boxed{10}$$

A car is speeding up as it goes around a curve. What is the acceleration vector at this moment in time?



### Acceleration in Nonuniform Circular Motion

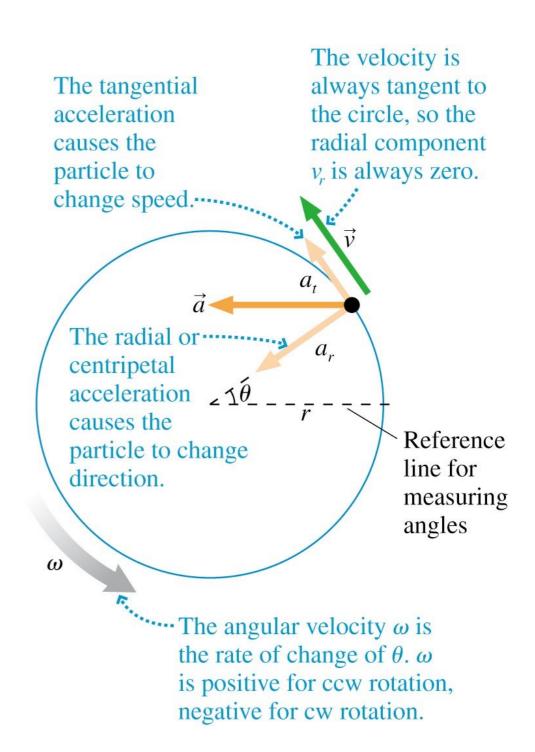
#### Centripetal acceleration

$$a_r = \frac{v^2}{r}$$

#### Tangential acceleration

$$a_t = \frac{ds}{dt}$$

$$a = \sqrt{a_r^2 + a_t^2}$$



#### Car on a curve

A car starts from rest on a curve of radius 50 m and accelerates at a rate of 4.0 m/s<sup>2</sup>. After 2.0 s what is the **total** acceleration of the car?

