# **Scientific Computing**

Lance Nelson

7/16/2022

# Table of contents

1	Pyt	hon and Jupyter Notebooks	6
	1.1	Python	6
	1.2	Installing Software	7
	1.3	Jupyter Notebooks	7
		1.3.1 Notebook Structure	7
		1.3.2 Navigating Jupyter Notebooks	8
	1.4	Tips for studying Jupyter notebooks	9
		1.4.1 Print Statements	9
		1.4.2 Comments	9
ı	Ва	asic Python	11
2		iables and Numbers	12
	2.1	Variables	12
		2.1.1 Variable naming convention	12
	2.2	Numbers: Integers and Floats	13
		2.2.1 Augmented Assignment	15
		2.2.2 Large numbers	16
		2.2.3 Very Large Numbers	16
		2.2.4 Python functions	17
	2.3	Flash Cards	18
	2.4	Exercises	19
3	Stri	9	20
	3.1	Creating Strings	20
	3.2	Displaying text and numbers together	21
	3.3	Indexing and Slicing	23
	3.4	String Methods	25
4	Flas	sh Cards	27
5	Exe	rcises	28

6	Bool	olean Variables and Conditionals	29
	6.1	Boolean Variables	
		6.1.1 Boolean Logic	
		6.1.2 Compound Comparisons (Logical Operators)	31
		6.1.3 Tests for Inclusion	
	6.2	Conditions	32
		6.2.1 if statement	
		6.2.2 else Statment	
7	Flasi	sh Cards	35
8	Exer	ercises	36
9	Lists	ts and Tuples	38
	9.1	Creating Lists	38
	9.2	Indexing and Slicing Lists	39
		9.2.1 Tests for Inclusion	
		9.2.2 List Methods	41
		9.2.3 Built-in functions for Lists	41
		9.2.4 The range function	42
	9.3	Tuples	
10	Loop	ops	44
	•	· 1 for loops	44
		10.1.1 Boolean Logic Inside Loops	
		10.1.2 Zipping and Enumerating	
		10.1.3 List Comprehension	
	10.2	$^{2}$ while $\operatorname{Loops}$	49
	10.3	3 continue, break, and pass Commands	
11	Fund	nctions	52
	11.1	1 Native Functions	53
	11.2	2 Imported Functions	53
	11.3	3 User-defined Functions	
		11.3.1 The return statement	
		11.3.2 Local vs Global Variable Scope	
		11.3.3 Positional vs. Keyword Arguments	
		11.3.4 Lambda Functions	
Ш	Int	termediate Python	61
12	The	e numpy module	62
	19 1	1 Numby Arrays	62

	12.2	Array Creation	63
			63
			64
		12.2.3 Arrays from Functions	66
	12.3		67
			67
		12.3.2 Multi-dimensional Arrays	68
			68
	12.4	Slicing Arrays	69
			69
		12.4.2 Boolean Slicing	70
	12.5	Vectorization and Broadcasting	71
		12.5.1 Numpy Functions	72
		12.5.2 Arrays of same Dimensions	72
		12.5.3 Arrays of Different Dimensions	73
		12.5.4 Vectorizing user-defined functions	74
	12.6	Manipulating and Modifying Arrays	76
		12.6.1 Reshaping Arrays	76
		12.6.2 Flattening Arrays	77
		12.6.3 Transposing Arrays	77
		12.6.4 Merging Arrays	78
	12.7	Commonly-used Array Methods and Functions	<b>7</b> 9
13	File	I/O (Input/Output)	81
			81
			81
			83
	13.2		84
			85
		13.2.2 Using NumPy's savetxt function	85
14	Basi	c Plotting	87
		Plotting Functions of a Single Variable	
		9	88
		,	90
		<del>-</del>	91
			93
			94
	14.2	· -	96
			97
		O Company of the comp	98
			99
		14.2.4 Scatter Plots	

	14.2.5	Histograms	$\mathbf{S}$																		101
14.3	Multifi	gure Plots																			103

# 1 Python and Jupyter Notebooks

# 1.1 Python

Python is a computer programming language available on all major platforms (Mac. Windows, Linux). Python is a scripting language which means that the computer interprets and runs your code at the moment you run it. In contrast, with a compiled language like C the code must first be converted into binary before it can run (called "compiling" the code). There are pros and cons to both types of languages. The on-the-fly interpretation of Python makes it quick and easy to write code and provides fast results for simple calculations. When codes become longer and more complex, on-the-fly interpretation becomes less efficient and execution time will be much slower than it would be with a compiled language. The pros and cons flip for a compiled language; writing code in a compiled language can be cumbersome and slow, but the execution time is typically much faster. Out of necessity, most programmers become proficient in both types of languages. Python(or another interpreted language) is used to "toy around" with your problem and build familiarity. As the complexity of the code increases the user is then forced to transition to a compiled language to get the needed speed. This is the famous "two language" problem and there is a new programming language designed to eliminate this problem by combining the pros from both into one language. (The name of the language is Julia)

Python is free, open source software and is maintained by the non-profit Python software foundation. This is great because it means that you will always have free access to the Python language regardless of what organization or university you are affiliated with. You'll never have to worry about not being able to use your Python code without paying for it. Another benefit of open source languages is that all of the codes developed by other people are available for anyone to inspect, modify, and use. This allows anyone to review another's code to ensure that it does what they say it does, or to modify it to do something else. One last benefit that comes with an open source language is the community of Python users available to answer questions and provide instruction to the beginner. Answers to most questions about python are readily available on tutorial or forum websites.

# 1.2 Installing Software

The first step is to install the software (if you haven't already). The most convenient way to install Python and also get many of the commonly-used libraries is to use an installer. I recommend Anaconda. When installing the software be sure to choose Python 3 since this is the current version. By default, Anaconda will install a suit of softwares and libraries that are commonly used. If you want to install other Python libraries, open the Anaconda-Navigator (green circle icon) and select the **Environment** tab on the left. Select **Not Installed** from the pull-down to see all of the libraries that are available to be installed. To install a library, check the box next to it and click **Apply**. Anaconda will take care of the rest.

### To Do:

- 1. Install Anaconda
- 2. Check to see if the library "numpy" is installed. If not, install it.

# 1.3 Jupyter Notebooks

A Jupyter notebook is an electronic document designed to support interactive data processing, analysis, and visualization in an easily shared format. A Jupyter notebook can contain live code, math equations, explanatory text, and the output of codes (numbers, plots, graphics, etc..). To launch a Jupyter notebook, first open Anaconda-Navigator (green circle icon) and click the **Launch** button under JupyterLab. Jupyter can also be launched from the command line by typing jupyter-lab. The jupyter notebook will launch in your default web browser, but it is not a website. From here you can select an already existing Jupyter notebook, denoted by the orange icons and the .ipynb extension, or create a new notebook by clicking **New** from the **File** menu.

## To Do:

- 1. On iLearn, find the module entitled "Jupyter Notebooks" and download the file "Intro.ipvnb".
- 2. Launch JupyterLab as explained above.
- 3. Open "Intro.ipynb" that you downloaded in step 1 and continue reading this book in the jupyter notebook.

# 1.3.1 Notebook Structure

There are two types of "cells" in a Jupyter notebook: code cells and text cells (also called Markdown cell). Code cells contain "live" Python code that can be run inside of the notebook with any output appearing directly below it. Markdown cells are designed to contain

explanatory information about what is happening inside of the code cells. They can contain text, math equations, and images. Markdown cells support markdown, html, and Latex (for generating pretty math equations).

Both markdown and code cells can be executed by either selecting **Run Selected Cells** in the **Run** menu, by clicking the **Play** icon at the top of the notebook, or by using the **Shift-Return** shortcut when your cursor is in the desired cell.

# 1.3.2 Navigating Jupyter Notebooks

Navigating a Jupyter notebook is fairly straightforward but there are a few handy short-cuts/hotkeys that will make navigation quicker and your workflow more efficient. When working in a Jupyter notebook, you are always operating in one of two modes: edit mode or navigate mode. In edit mode you can make modifications to the text or code in a cell and in navigate mode you can add/delete cells and modify the cell type. If you can see a blinking cursor in one of the cells you are in edit mode. Otherwise you are in navigate mode. To exit edit mode, simply press the esc key and you will enter navigate mode. To exit navigate mode, simply press the enter key and you will enter edit mode for the cell you were focused on. (You can also double click on a cell with your mouse to enter edit mode.) The shift + enter key sequence will "execute" a cell and produce the associated output. For text cells, executing just means to render the text in a nicely formatted fashion. "Executing" a code cell will actually execute the code block contained in the cell. You also enter navigate mode every time you execute a cell using the shift + enter key sequence. A summary of these shortcuts is given below:

- Up/down arrows Navigate to different cells in the notebook.
- Y turns a text cell into a code cell.
- M turns a code cell into a text cell.
- A inserts a new cell above the current cell.
- B inserts a new cell below the current cell.
- X deletes the current cell.
- enter enters edit mode.
- shift + enter execute a cell.
- esc enter navigate mode.

You should take some time now to practice these shortcut keys until you become good at navigating a jupyter notebook. Consider attempting the following actions using the shortcuts above:

- 1. Add a cell below this one.
- 2. Turn the cell into a code cell (observe the distinct appearance of code cells).
- 3. Type the following code into the cell:
  - print("I did it!")

- 4. Execute the cell using shift + enter. Observe the output.
- 5. Delete the cell.
- 6. Enter edit mode for this text cell.
- 7. Add a sentence of your choice at the end of the cell.
- 8. "Execute" the cell and observe the new output.
- 9. Remove the sentence to restore the cell to it's previous state.

# 1.4 Tips for studying Jupyter notebooks

### 1.4.1 Print Statements

Jupyter notebooks in this class will be a nice mix of text cells (explanation) and code cells (examples). You will soon learn that code cells produce no output unless you explicitly tell them to using a **print** statement (similar to the one you used above). When you encounter a code cell, you should feel free to make modifications and additions to the cell until you fully understand how the code works.

### 1.4.2 Comments

Comments are a way to describe what each section of code does and makes it easier for you and others to understand the code. It may seem clear what each section of code does as you write it, but after a week, month or longer, it is unlikely to be obvious. Paul Wilson of the University of Wisconsin at Madison is quoted as saying, "Your closest collaborator is you six months ago, but you don't reply to emails." Comment your code now so that you are not confused later.

There are several ways to add comments to your code:

- 1. Use # to start a comment. Everything on that line the follows will be ignored.
- 2. For longer comments that will span several lines, use triple double quotes to begin and end the comment (""")

The cell below illustrates these two ways to make comments:

```
# Speed of light in a vacuum
c = 3e8
v = 300 # Speed of sound in air
"""
The variables below are the initial conditions for a cannon
```

# To Do:

- 1. Execute the code block below and verify that no output is produced.
- 2. Add print statements that help you see the result of the calculation.
- 3. Add simple comments next to each line explaining the code.

```
a = 2
b = 3
c = a**b

import subprocess
import sys

def install(package):
    subprocess.check_call([sys.executable, "-m", "pip", "install", package])
install("numpy")
```

# Part I Basic Python

# 2 Variables and Numbers

# 2.1 Variables

When performing mathematical operations, it is often desirable to store the values in *variables* for later use instead of manually typing them back in each time you need to use them. This will reduce effort because small changes to variables can automatically propagate through your calculations.

Attaching a value to a variable is called *assignment* and is performed using the equal sign (=), as demonstrated in the cell below:

```
a = 5.0
b = 3
c = a + b
```

# 2.1.1 Variable naming convention

There are some rules for allowed variable names in Python. They are as follows:

- 1. Variable names must begin with a letter or an underscore (\_)
- 2. Variables names must only contain letters, numbers, and underscores.
- 3. Variable names cannot contain spaces.
- 4. Variables names cannot be a word reserved by Python for something else. These words are:

	Python	reserved	words	
and continue except global	as def False if	assert del finally import	break elif for in	class else from is
lambda pass why	None raise with	nonlocal return yield	not True	or try

The cell below contains some allowed variable names and some that are not allowed.

#### To Do:

- 1. Determine which variable names are allowed and which are not in the cell below.
- 2. What does Python do if you try to define a variable using a name that is not allowed?

```
my1variable = 3
1stvariables = 2
a big constant = 3
a_big_constant = 1e8
```

It is also a good practice to make variable names meaningful. For example, in the cell below we calculate  $E = mc^2$  using two choices for variable assignments. In one case, it is easy to determine what the calculation is and in the other it isn't.

```
# Good Variable Names
mass_kg = 1.6
light_speed = 3.0e8
E = mass_kg * light_speed**2

# Poor Variable Names
a = 1.6
b = 3.0e8
c = a * b**2
```

# 2.2 Numbers: Integers and Floats

There are two types of numbers in Python - floats and integers. *Floats*, short for "floating point numbers," are values with decimals in them. They may be either whole or non-whole numbers such as 3.0 or 1.2, but there is always a decimal point. *Integers* are whole numbers with no decimal point such as 2 or 53.

Mathematical operations that only use integers and evaluate to a whole number will generate an integers (except for division). All other situations will generate a float. See the example cell below.

```
a = 24
b = 6
d = 0.3
e = a + b # Produces an integer.
f = a + d # Produces a float
g = a * b # Produces a ???
h = a / b # Produces a ???
```

### To Do:

- 1. For each of the mathematical operations above guess what type of number the result will be.
- 2. Use print statements to verify your guesses and formulate a general rule that you can rely on. (Tip, the type() function will tell you what kind of number a variable is.)

Integers and floats can be inter-converted to each other using the int() and float() functions.

```
int(3.0)
float(4)
```

### 4.0

The distinction between floats and ints is often a minor detail. Occasionally, a function will require that an argument be a float or an int but usually you won't have to worry about which one you use.

Below you will find some other common mathematical operations that can be performed on numerical variables.

```
a = 20
b = 10
c = a + b
d = a/b
r = a//b
r = a % b
e = a * b
f = c**4
```

# To Do:

- 1. Use print statements to investigate what each operation does.
- 2. Guess what type of number you expect the result to produce (int or float) and then check yourself?
- 3. Add comments next to each line (Use # to start a comment) explaining that operation.

# 2.2.1 Augmented Assignment

Augmented assignment is a shortened way to make a simple modification to a variable. For example, if we want to increase the value of a variable by 10, one way to do it would be like this.

```
a = 5
a = a + 10
```

This is certainly not difficult, but it does involve typing the variable twice which becomes cumbersome as your variable name gets longer. Alternatively, we can accomplish the same thing with the += operator.

```
a = 5
a += 10
```

Augmented assignment can be used with addition, subtraction, multiplication, and division as shown in the code cell below.

### To Do:

- 1. Predict what the final result of a will be in the code cell below.
- 2. Add an appropriately-place print statement to see if you were correct.
- 3. If you were wrong, pow-wow with your neighbor until you understand.

```
a = 7
a += 3
a -= 1
a *= 4
a /= 3
```

## To Do:

- 1. Predict what the final result of a will be in the code cell above.
- 2. Add an appropriately-place print statement to see if you were correct.

3. If you were wrong, pow-wow with your neighbor until you understand. ### Compound Assignment

At the beginning of a program or calculation, it is often necessary to define a set of variables. Each variable may get it's own line of code, but if there are a lot of variables, this can begin to clutter your code a little. An alternative is to assign multiple variables on a single line. In the code below, we assign the atomic mass of the first three elements.

```
H, He, Li = 1.01, 4.00, 5.39
```

# To Do:

- 1. Use print statements to verify that each variable was assigned it's own value.
- 2. Add assignments for the atomic masses of the next three elements on the periodic table.

# 2.2.2 Large numbers

Sometimes you find yourself working with large numbers in your calculation. Maybe your calculation involves the use of ten billion, which has 10 zeros in it. It can be difficult to look at all of those zeros with no commas to help break it up. In those cases, you can use an underscore (\_) in place of the comma, as shown below.

```
myLargeNumber = 10000000000 # This is tough to look at.
myLargeNumber = 10_000_000_000 # This is easy to read
myLargeFloat = 5000000.6 # This is tough to read
myLargeFloat = 5_000_000.6 # This is easy to read
```

# 2.2.3 Very Large Numbers

If your number is very large or very small (20-30 zeros), you would probably rather not have to type all of the zeros at all, even if you can break it up with the underscores. For example, the Boltzmann constant, which comes up in thermodynamics, has a value equal to

$$1.38\times10^{-23}$$

We can avoid typing all those zeros by using scientific notation when defining the variable. (see example below) This is super handy for very large and very small number. (Numbers of both variety show up frequently in physics!)

```
kB = 1.38e-23
```

# 2.2.4 Python functions

In addition to basic mathematical functions, python contains several mathematical functions. As in mathematics, a function has a name (e.g. f) and the arguments are places inside of the parenthesis after the name. The *argument* is any value or piece of information fed into the function. In the case below, f requires a single argument x.

f(x)

In the cell below, you will find several useful math equations.

```
abs(-5.5)
float(2)
int(5.6)
print(1.26e-6)
round(-5.51)
str(3.2)

1.26e-06
```

In addition to Python's native collection of mathematical functions, there is also a math module with more mathematical functions. Think of a module as an add-on or tool pack for Python just like a library. The math module comes with every installation of python and can be *imported* (i.e. activated) using the import math command. After the module has been imported, any function in the module is called using math.function() where function is the name of the function. Here is a list of commonly-used function inside the math module:

```
import math
math.sqrt(4)
math.ceil(4.3)
math.cos(1.5)
math.sin(1.5)
math.tan(3.14)
math.asin(1)
math.acos(1/2)
math.atan(2)
```

```
math.degrees(6.28)
math.e
math.exp(5)
math.factorial(4)
math.log(200)
math.log10(1000)
math.radians(360)
math.pi
math.pow(2,8)
```

256.0

#### To Do:

- 1. Use print statements to figure out what each function in the code cell above does. Pay special attention to trigonometric function. Do these functions expect the argument to be in radians or degrees?
- 2. Add comments to remind yourself for later.

There are other ways to import functions from modules. If you only want to use a single function inside the module, you can selectively import it using from, as shown below.

```
from math import radians
radians(4)
```

0.06981317007977318

# 2.3 Flash Cards

- 1. What are the rules for naming variables in Python?
- 2. When will a mathematical calculation produce a float?
- 3. When will a mathematical calculation produce an int?
- 4. What is the best way to increase/decrease the value of a variable by a multiplicative factor (multiply it by a number)?
- 5. What is the best way to increase/decrease the value of a variable by an additive constant (add a number to it)?
- 6. When assigning large numbers to variables, what character can replace the "," to separate the numbers into groups of three?
- 7. How do you use scientific notation to assign a very large number to a variable?
- 8. Explain how to print a sentence with a variable inserted in the middle?

- 9. What format code should be used to display a variable as a float with 8 total spaces and 2 numbers after the decimal?
- 10. What format code should be used to display a variable in scientific notation with 6 total spaces and 2 numbers after the decimal?
- 11. When using a trig function  $(\sin \theta, \cos \theta, \tan \theta)$ , the number that is passed in must have what units?
- 12. What does the math.radians function do?

# 2.4 Exercises

1. Calculate the distance from the point (-48, 56) to the point (23, 81) 1- using the math.hypot() function and then 2- using the following distance equation:

$$d = \sqrt{\Delta x^2 + \Delta y^2}$$

Print out the result and check your answer with your neighbor's answer.

2. Solve the quadratic equation using the quadratic function below for  $a=1,\ b=2,$  and c=1.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Print out the result and check your answer with your neighbor's answer.

3. (Optics Application) When light passes from one material to another, it is redirected from its original path. We call this refraction. The equation for calculating the bending angle is called Snell's law.

$$n_1\sin\theta_1=n_2\sin\theta_2$$

where  $n_1$  ( $n_2$ ) is the index of refraction of the first (second) material and  $\theta_1(\theta_2)$  is the incident (refracted) angle. Calculate the refracted angle for an air-water interface for the following incident angles:

Title	
15°	
$35^{\circ}$	
$45^{\circ}$	
$60^{\circ}$	
$85^{\circ}$	

The index of refraction for air is  $n_1 = 1.0$  and for water is  $n_2 = 1.33$ . Print out your results and check your answer with your neighbor's answer.

# 3 Strings

Another commonly-used type of data is a string of characters known simply as *strings*. Strings can contain a variety of characters including letters, numbers, and symbols.

# 3.1 Creating Strings

Strings are created by placing the sequence of characters in single (or double) quotes.

```
text = "some text"
```

Strings can also be created by converting a float or an integer into a string using the str() function.

```
text = str(4.5)
```

One common error made when working with strings is to attempt to perform math with them. Python will not perform math with strings because it sees them as a series of characters and nothing more. In the cell below, we attempt to perform math with some strings.

```
a = "4"
b = "2"
c = 5

d = a + b
e = a * b
f = b * c
```

# To Do:

- 1. Use print statements in the cell above to determine what happens when you add two strings together. (Ancillary question: Can you subtract strings?)
- 2. Use print statements in the cell above to determine what happens when you multiply two strings.
- 3. Use print statements in the cell above to determine what happens when you multiply a string and an integer.

- 4. What do you think will happen if you multiplied a string and a float? Guess and then see if you're right.
- 5. Add comments for you to refer back to later.

If you want to know the length of a string, you can use the len() function

```
text = "some text"
len(text)
```

9

The length of the string above is 9 because a space is a valid character.

# 3.2 Displaying text and numbers together

You have been using print() statements quite a lot lately (hopefully) but you probably haven't printed text and numbers together. To display both text and numbers in the same message, there are several options. The first is to just put multiple variables into the print() function, separating them with commas.

```
g = 9.8
unit = "m/s^2"
print(g,unit)
```

### $9.8 \text{ m/s}^2$

Another option is to convert the number to a string and then "add" it to the other string. This creates a single string as an argument to the print() function.

```
g = 9.8
unit = "m/s^2"
print(str(g) + unit)
```

## $9.8m/s^2$

Notice the lack of space between the number and the unit. "Adding" the two strings smashed them together exactly as they were, no spaces added. You can insert multiple numbers into a string using something called "f"-strings. (short for formatted strings). To construct an f-string, simply place an "f" in front of the string. Anytime you want to insert a number in your string, enclose it in curly braces.

```
v = 5.0

c = 3e8

print(f"The speed of light is {c} and the speed of my car is {v}")
```

The speed of light is 300000000.0 and the speed of my car is 5.0

That's a clever way to insert a numerical value into a string, but the value of the speed of light is still displaying too many digits. To specify how the number should be formatted place a : after the variable name followed by a formatting tag.

```
v1 = 5.0 v2 = 8.3 c = 2.998e8 n = 2 print(f"There are <math>\{n:d\} cars traveling side by side. One car is traveling at \{v1:4.2f\} m/
```

There are 2 cars traveling side by side. One car is traveling at 5.00 m/s and the other is

The structure of the stuff inside of the curly braces is {variable:formatcode}; variable holds the value to be displayed and formatcode indicates how the variable should be formatted when it is printed. The f in :4.2f indicates that the variable should be displayed as a float and the 4.2 indicates that four spaces should be allocated to display the number and no more than 2 numbers after the decimal should be displayed. A selection of some commonly-used format codes is given below.

Table 3.1: A summary of common format codes.

format code	explanation
{variable}	Use the default format for the data type.
{variable:4d}	Display as an integer, allocating 4 spaces for
	it.
<pre>{variable:.4f}</pre>	Display as a float, with four numbers after
	the decimal being displayed.
<pre>{variable:8.4f}</pre>	Display as a float, allocating 8 total spaces
	and 4 numbers after the decimal place.
{variable:8.4e}	Display using scientific notation, allocating 8
	total spaces and 4 numbers after the decimal
	place.

format code	explanation
{variable:6s}	Display as a string, allocating 6 total spaces for it. If the string is longer than 6 spaces, it will display the entire string with no extra white space. If the string is shorter than 6 spaces, it will pad the string with whitespace until it is 6 spaces long.

### To Do:

- 1. Modify the print statement above so that the float variables are given 8 total spaces with only 1 number after the decimal being displayed.
- 2. Modify the print statement above so that the speed of light is displayed with 3 numbers after the decimal place.

# 3.3 Indexing and Slicing

Accessing a piece (or slice) of a string is a common task in scientific computing. Often you will import data into Python from a text file and need to extract a portion of the file for later use in calculations. Indexing allows the user to extract a single element, or character, from a string. The key detail about indexing in Python is that *indices start from zero*. That means that the first character is index zero, the second character is index 1, and so on. For example, maybe a string contains the following amino acid sequence 'MSLFKIRMPE'. For this example, the indices are as follows:

Characters	M	S	L	F	K	Ι	R	M	Р	Е
Index	0	1	2	3	4	5	6	7	8	9

To access a single character from a string, place the desired index in square brackets after the name of the string.

```
seq = "MSLFKIRMPI"
seq[0]
```

'M'

To access the last character in a string you could do

```
seq = "MSLFKIRMPI"
seq[len(seq) - 1]
```

'I'

But this seems overly cumbersome. An easier approach is to index backwards. The string can be reverse indexed from the last character to the first using negative indices, starting with -1 as the last character.

```
seq = "MSLFKIRMPE"
seq[-1]
```

'E'

# To Do:

- 1. Access the 5th character in the peptide sequence above.
- 2. Access the character that is 3rd from the end in the peptide sequence above.

Indexing only provides a single character, but it is common to want a series of characters from a string. Slicing allows us to grab a section of a string. Slicing is performed by specifying start and stop indices separated by a colon in the square brackets. One important detail worth mentioning: the character at the starting index is included in the slice while the character located at the final index is not included in the slice.

```
seq = "MSLFKIRMPE"
seq[0:5]
```

'MSLFK'

Looking at the string, you notice that the character at location 5 (I) has been excluded from the slice. You can leave off the first number when slicing and the slice will start at the beginning of the string.

```
seq = "MSLFKIRMPE"
seq[:5]
```

'MSLFK'

You can also use negative indices when slicing. This is especially helpful when you want to grab the last few characters in a string.

```
file = "data.txt"
ext = file[-3:]
```

Finally, we can adjust the step size in the slice. That is, we can ask for every other character in the string by setting a step size of 2. The structure of the slice is [start,stop,step].

```
seq = "MSLFKIRMPE"
seq[0:8:2]
```

'MLKR'

'MLKRP'

You can omit the start and stop indices and Python will assume that you are slicing the entire string.

```
seq = "MSLFKIRMPE"
seq[::2]
```

# 3.4 String Methods

A *method* is a function that works only with a specific type of object. String methods only work on strings, and they don't work on other types of objects, like floats or ints. If it helps you, you can just think of a method as a function.

One example of a string method is the capitalize() function which returns a string with the first letter capitalized. To use a method (referred to as *calling* the method), the method name is appended to the variable you want it to operate on. For example, below is an Albert Einstein quote that needs capitalized.

```
quote = "i want to know God's thoughts. The rest are details."
quote.capitalize()
print(quote)
```

i want to know God's thoughts. The rest are details.

Notice that the original variable (quote) remains unchanged. This particular method does not change the value of the original string but rather returns a capitalized version of it. If we want to save the capitalized version, we can assign it to a new variable, or overwrite the original.

```
quote = "i want to know God's thoughts. The rest are details"
quote = quote.capitalize()
print(quote)
```

I want to know god's thoughts. the rest are details

In the cell below you will find a list of commonly-used string methods.

```
a = "spdfgssfpggg"
a.capitalize()
a.center(10)
a.count("s")
a.find("d")
a.isalnum()
a.isalpha()
a.isdigit()
a.lstrip("s")
a.rstrip("g")
a.split("s")
a.startswith("s")
a.endswith("p")
```

# False

# To Do:

- 1. Use well-placed print statements to determine what each string method does.
- 2. Add comments next to each method for future reference.

# 4 Flash Cards

- 1. What is the index value of the sixth character in a string?
- 2. What happens when you "add" two strings together?
- 3. What happens when you multiply two strings together?
- 4. What happens when you multiply a string by an integer?
- 5. What happens when you multiply a string by a float?
- 6. What function will tell you how many characters are in a string?
- 7. Give two ways that you could slice out the first 4 characters in a string.
- 8. Give two ways that you could slice out the last 4 characters in a string.
- 9. What string method would you use to see if a string contains only numbers and characters, but no symbols?
- 10. What does the string method split() do?
- 11. What does the string method find() do?
- 12. Explain how to print a sentence with a variable inserted in the middle?
- 13. What format code should be used to display a variable as a **float with 8 total spaces** and 2 numbers after the decimal?
- 14. What format code should be used to display a variable in **scientific notation with 6** total spaces and 2 numbers after the decimal?

# **5** Exercises

- 1. In the cell below you will find a string containing the name of a PNG file. (i.e. name always ends in ".png").
  - i) Remove the ".png" extension from the string using a string method.
  - ii) Remove the ".png" extension from the string using slicing.

```
file = "physics.png"
```

- 2. (Lightning Strike) The dielectric strength of air determines how likely it is for lightning to strike and this value varies with the humidity (moisture content) of the air. In the cell below, you will find a string that contains the dielectric strength of air for three different humidity levels. Use string methods to extract the three dielectric constant values. Then calculate
  - 1. the difference between the largest and smallest values.
  - 2. The average of the three values.

```
dielectricBreakdownAir = "dry:15847, moderate:8523, wet:7864"
```

- 3. Below you will find a string containing all experimentally known alloys (compounds formed by combining two or more elements on the periodic table) represented using the elements first discovered to exhibit that crystal structure (or "prototypes").
  - 1. Use string methods to find the number of alloys containing Aluminum (symbol: Al).
  - 2. Is there a crystal structure with the designation "CaC2" (Calcium Carbide) in the list? How about "Fe2Ag"?
  - 3. Use string methods to calculate the percentage of the alloys listed that have gold in them (symbol Au).

alloys = "Cu, W, Mg, betaSn, Indium, alphaAs, alphaHg, Cu, AuCu, CuPt, AB2, MoPt2, AB2, AB3, A2B2, AB

# 6 Boolean Variables and Conditionals

# 6.1 Boolean Variables

We have learned about three types of variables in Python: ints, floats, and strings. Another variable type is a boolean, which can be one of two values: True or False. You can assign a boolean variable in the same way that you assign numbers or string, using =

```
myBool = True
```

True must be capitalized so don't try true or it won't be a boolean

```
myBool = true
```

# 6.1.1 Boolean Logic

Often you will want to check to see if some condition is true. For example, maybe you want to know if the radius of a certain satellite's orbit is bigger or smaller than Mercury's orbit. To perform this check, there are several boolean operators that will return True or False. Take note of the boolean operators shown in the cell below along with the comments added to explain what they do.

```
r1 = 3.5e8
r2 = 2.7e6

r1 > r2 # Is r1 greater than r2
r1 < r2 # Is r1 less than r2
r1 >= r2 # Is r1 greater than or equal to r2
r1 <= r2 # Is r1 less than or equal to r2
r1 != r2 # Is r1 not equal to r2
r1 == r2 # Is r1 equal to r2</pre>
```

False

A word of caution about comparing Python floats using == is in order here. Python floats are stored as a 53-digit, base-2 binary number(that's a mouthful). If you're interested in what that means, we can talk more. If you're not that interested, just know that when you define a float in Python, the number that is stored in the computer is not *exactly* the number that you think it is. This can cause problems when you are comparing two numbers that you think should be equal but actually aren't equal in the computer.<sup>1</sup> The code below illustrates this problem.

#### False

- 0.30000
- 0.30000
- 0.30000000000000044408920985006261616945266724
- 0.2999999999999988897769753748434595763683319

The first two print statements display the value of b and c to five decimal places. The second two print statements force Python to display the value of b and c out to 45 decimal places. Notice that the true value of b is not *exactly* equal to 0.3. This is why the statement print(b==c) returns False. The take home message here is that comparing two floats to see if they are equal is always a bad idea. A better way to check to see if two floats are equal (or close enough that we can say they are equal) is to check if the absolute value of their difference is very small, like this:

```
a = 0.1
b = 3 * a
c = 0.3
print(abs(b - c) < 1e-10)</pre>
```

True

<sup>&</sup>lt;sup>1</sup>There is a library called Decimal that will fix a lot of these problems.

# 6.1.2 Compound Comparisons (Logical Operators)

Comparisons like those shown above can be chained together to make compound comparisons using the and, or, and not operators.

Operator	Description
and or not	Tests for both being True Tests for either being True Tests for False

The and operator requires both inputs to be True in order to return True while the or operator requires only one input to be True in order to evaluate at True. The not operator is different in that it only takes a single input value and returns True if and only if the input is False. It is a test for False.

Truth tables are a good way to visualize the output from compound comparisons.

p	q	p and q	p or q
True	True	True	True
True	False	False	True
False	True	False	True
False	False	False	False

As a simple example, suppose you know the density  $(\rho)$  and speed of light (c) for two materials and you'd like to know if both values are bigger for material 1 or material 2.

### To Do:

- 1. Predict the output for each compound comparison given below. Add your guess as a comment.
- 2. Now add appropriately-placed print statements to check your guesses.
- 3. Modify your guess as needed and discuss any questions with a neighbor.

```
c1 = 2.5e8

c2 = 2.48e8

1 = 450

2 = 580

c1 > c2 and 1 > 2

c1 < c2 and 1 < 2

c1 > c2 and 1 < 2
```

```
c1 < c2 and 1 > 2

c1 > c2 and not 1 > 2

c1 < c2 and not 1 > 2

c1 < c2 and not 1 < 2

c1 > c2 or 1 > 2

c1 < c2 or 1 < 2
```

True

## 6.1.3 Tests for Inclusion

You can check for inclusion using the Python in operator. This provides an easy way to see if a character (or word) is present in a long string. Let's say you have a long string that contains the names of Jupyter's moons (there are 79 of them!!) and you want to see if a certain moon is included in the list. The in statement let's us quickly test to see if it is in the list. (see example below)

```
jupytermoons = "Metis,Adrastea,Amalthea,Thebe,Io,Europa,Ganymede,Callisto,Themisto,Leda,Hi
"Cyllene" in jupytermoons
```

True

# 6.2 Conditions

Conditions allow the user to specify if and when certain lines or blocks of code are executed. Specifically, when a condition is true, the block of *indented* code directly below it will run.

### 6.2.1 if statement

The if statement is used to control when a block of code runs. It's usage is shown below ending in a colon and the block of code below indented with *four spaces*. Using the **Tab** key will also produce four spaces.

```
jupytermoons = "Metis, Adrastea, Amalthea, Thebe, Io, Europa, Ganymede, Callisto, Themisto, Leda, Hi
if "Cyllene" in jupytermoons:
```

```
found = True
  print("Found Cyllene in the list")

if "Matis" in jupytermoons:
  found = True
  print("Found Matis in the list")
```

Found Cyllene in the list

If the boolean statement after if is true, the indented code below it will run. If the statement is false, Python just skips the indented lines below.

#### 6.2.2 else Statment

Sometimes there will be an alternate block of code that you want to run if the if statement evaluates to False. The else statement is used to specify this block of code, as shown below.

```
jupytermoons = "Metis,Adrastea,Amalthea,Thebe,Io,Europa,Ganymede,Callisto,Themisto,Leda,Hi

if "Cyllene" in jupytermoons:
    found = True
    print("Found Cyllene in the string")

else:
    found = False
    print("Did not find Cyllene in the string")

if "Matis" in jupytermoons:
    found = True
    print("Found Matis in the string")

else:
    found = False
    print("Did not find Matis in the string")
```

Found Cyllene in the string
Did not find Matis in the string

Notice that the else statement must be followed by a colon and the block of code to be executed is indented, just as in the if block.

There is an additional statement called the elif statement, short for "else if", which is used to add extra conditions below the initial if statement. The block of code below the elif statement only runs if the if statement is false and the elif statement is true. An example is given below.

```
jupytermoons = "Metis,Adrastea,Amalthea,Thebe,Io,Europa,Ganymede,Callisto,Themisto,Leda,Hi

if "Matis" in jupytermoons:
    foundMatis = True
    print("Found Matis in the string")

elif "Cyllene" in jupytermoons:
    foundCyllene = True
    print("Found Cyllene in the string.")

else:
    foundCyl = False
    foundMatis = False
    print("Did not find Cyllene or Matis in the string")
```

Found Cyllene in the string.

It is worth noting that else statements are not required. If you leave the else statement off and the if statement is false, no code block will execute.

# 7 Flash Cards

- 1. How do you check to see if one value is **greater than or equal to** another one?
- 2. Which boolean operators should **never** be used to compare floats?
- 3. What is the correct way to determine if two floats are equal to each other (or very close)?
- 4. When will the statement p and q evaluate to True?
- 5. When will the statement p or q evaluate to True?
- 6. How do you check to see if a certain sequence of characters is present in a string?
- 7. When constructing an if block how does Python know what code to execute if the condition is True?

# 8 Exercises

1. (Escape Velocity) The escape velocity is the speed needed for an object to completely escape the gravitational pull of a planet. The expression for escape velocity is

$$v_{\rm escape} = \sqrt{\frac{GM_p}{r}}$$

where  $G=6.67\times 10^{-11},\, M_p$  is the mass of the planet you are trying to escape from, and r is the radius of the planet.

- 1. Construct an **if-else** code block that checks to see if a guessed speed is bigger or smaller than the escape velocity of Jupiter. The code block should print an appropriate message about the guessed velocity. Jupiter has a mass of  $M = 1.90 \times 10^{27}$  kg and a radius of  $r = 6.99 \times 10^{7}$  meters.
- 2. Modify your guess until both branches of your if-else trigger.
- 3. Repeat for Earth. Earth has a mass of  $M=5.98\times 10^{24}$  kg and a radius of  $r=6.37\times 10^6$  meters.

```
G = 6.67e - 11
```

2. (Thermoelectrics) A thermoelectric is a material that converts thermal energy into electrical energy and much research is devoted to finding new materials that exhibit this behavior. Good thermoelectrics tend to be materials with high electrical conductivity ( $\sigma > 7 \times 10^5~\Omega^{-1} \mathrm{m}^{-1}$ ) and low thermal conductivity ( $\kappa < 2.0~\mathrm{W/m~K}$ ). Write an if-else code block that checks to see if a material's electrical conductivity is above the threshold and its thermal conductivity is below the threshold. Then choose some values for the conductivities and test your if-else block.

```
sigma = 0  # Electrical Conductivity
kappa = 0  # Thermal Conductivity
```

3. Alloys are often represented by a string containing the elements in the alloy and the relative number of atoms for each element. For example, "Cu2Au" (Copper-2-Gold) means that the alloy is made of copper and gold and there are two copper atoms for every gold atom. Write some python code that calculates the total number of atoms in an alloy. The code should include a print statement to display the result. Then check your code on the alloys in the table below. You can assume that all elements have

two-character symbols even though that isn't true; we won't consider any one-character symbols in this problem.

## Hints:

- 1. The possible lengths for the strings are 4 (one atom per element), 5 (one atom for one element and more for the other), or 6 (more than one atom for both elements).
- 2. My code for this problem was about 15 lines long and it required a nested if-else block (an if-else inside of an if block).
- 3. You may find the isdigit() function to be helpful. Do you remember how to use it and what it does?

		Alloy		
"Cr3Si"	"Al2Cu"	"NbPd3"	"CaIn2"	"Al3Zr4"

alloy = "CaIn2"

# 9 Lists and Tuples

Up to this point, we have only worked with single numerical values or strings (multiple characters). Often we will want to work with collections of values (perhaps the orbital period of all of the planets in our solar system.) and it will be quite inconvenient to store each value into its own variable. Instead, the values can be stored in a list or tuple. Lists and tuples are both collections of *elements*, like numbers or strings. The key difference between them is that tuples are *immutable*, which means they cannot be modified after their initial creation. On the other hand, lists are *mutable*, or able to be modified.

# 9.1 Creating Lists

The easiest way to create a list is by putting the list elements inside of square brackets. Below, we create a list containing the masses of all of the planets in our solar system.

```
mass = [1.8986e27,5.6846e26,10.243e25,8.6810e25,5.9736e24,4.8685e24,6.4185e23,3.3022e23]
```

Note that square brackets ([]) must be used when creating the list. If you accidentally use parenthesis  $(())^1$  or curly brackets  $(\{\})^2$  you'll end up creating something other than a list.

Lists can contain any type of data and the type of data doesn't have to be the same for all of the elements. Below, we create a list of the electron configurations for the first 10 elements on the periodic table.

```
electrons = ["1s1","1s2", "1s2-2s1","1s2-2s2","1s2-2s2-2p1","1s2-2s2-2p2","1s2-2s2-2p3","1
```

Lists can contain mixed data types. Below we construct a list of the electrical conductivities of three metals.

```
conductivity = ["Gold",4.10e7,"Copper",5.96e7,"Aluminum",3.5e7]
```

If the elements of a list are also lists, we call it a *nested* list.

<sup>&</sup>lt;sup>1</sup>Use parenthesis to create a tuple, which is just like a list but cannot be modified.

<sup>&</sup>lt;sup>2</sup>Use curly brackets to create a dictionary, which is like a list but can be indexed on any data type, not just integers.

```
conductivity = [[1,2,3],[4,5,6],[7,8,9]]
```

# 9.2 Indexing and Slicing Lists

Indexing is used to access individual elements of a list, and it is similar to indexing strings. The index is the position of the desired element in the list and the *index numbering starts at zero*. Accessing an element of a list is done by placing the numerical index of the element we want in square brackets behind the list name. For example, if we want the electron configuration of the first element in our list from above, we use electrons[0] and the electron configuration for the second element would be electrons[1] and so on. Just as with string, negative indices can be used to access list elements counting from the back of the list forward.

```
electrons = ["1s1","1s2", "1s2-2s1","1s2-2s2","1s2-2s2-2p1","1s2-2s2-2p2","1s2-2s2-2p3","1
electrons[1]
electrons[-2]
electrons[5]
```

#### To Do:

- 1. Predict the output for each of the indexes performed in the cell above.
- 2. Use print statements to check your answers.
- 3. Discuss any misunderstandings with a peer.

Since lists are mutable, we can modify the value of an element in a list using the = operator.

```
conductivity = ["Gold",4.10e7,"Copper",5.96e7,"Aluminum",3.5e7]
conductivity[1] = 4.15e7
conductivity
['Gold', 41500000.0, 'Copper', 59600000.0, 'Aluminum', 35000000.0]
```

#### To Do:

Use a print statement to verify that the **conductivity** list was indeed modified as expected.

Multiple list elements can be retrieved at once (called *slicing*) by including the start and stop indices separated by a colon: [start:stop:step]. A convention that occurs throughout python is that the first index is included in the slice but the second is *not*. (i.e. [included:

excluded: step]) Default values for the start location, stop location, and step sizes will be used if these values are omitted. Below we give some examples of slicing.

```
electrons = ["1s1","1s2", "1s2-2s1","1s2-2s2","1s2-2s2-2p1","1s2-2s2-2p2","1s2-2s2-2p3","1
electrons[1:]
electrons[1:3]
electrons[1:8:2]
electrons[5:2:-1]
```

#### To Do:

- 1. Predict the output for the five slices in the cell above.
- 2. Use print statements to check your answers.
- 3. Discuss any misunderstandings with a peer.

### 9.2.1 Tests for Inclusion

Just as with strings, the in operator can be used with lists to determine if a list element is present. Suppose you have a list of all the known radioactive elements on the periodic table and you'd like to know if Iridium is in the list. The in statement let's us quickly test to see if it is in the list. (see example below)

```
radioactiveElements = ["Technetium", "Promethium", "Polonium", "Astatine", "Radon", "Francium",
"Iridium" in radioactiveElements
```

#### False

The in operator will work with numerical data as well.

```
numbers = [5,6,3,1,2]
4 in numbers
```

False

## 9.2.2 List Methods

Lists have a collection of methods (or functions) for accomplishing routine tasks. Some of the more common list methods are given below. All of the methods given will modify the original list (except copy()). As a reminder, methods only work on the object type that they were designed for (lists in this case) and they are called by appending the method name to the variable you want it to operate on. (i.e. myList.clear())

Method	Description	
append(element)	Adds a single element to the end of the list.	
clear()	Removes all elements from a list.	
copy()	Creates an independent copy of the list.	
count(element)	Counts the number of occurrences of element in the	
	list.	
extend(elements)	Adds multiple elements to the end of the list.	
<pre>index(element)</pre>	Returns the index of the first occurrence of element.	
<pre>insert(index,element)</pre>	Inserts the given element at the specified index.	
<pre>pop(index)</pre>	Removes and returns the element given at index. If	
	no index is provided, it defaults to the last element.	
remove(element)	Removes the first occurrence of element in the list.	
reverse()	Reverses the order of the entire list.	
sort()	Sorts the list in place. <sup>3</sup>	

```
a = [5,6,23,2,2,6]
a.sort()
```

#### To Do:

1. In the cell below, you will find a list of ...

## 9.2.3 Built-in functions for Lists

Python has several built-in functions that will work with lists. Functions are called by placing the arguments to the function in parenthesis and prepending the name of the function to the parenthesis. Here are a few common functions that are used with lists:

Method	Description
len(list)	Returns the number of elements in the list.

<sup>&</sup>lt;sup>3</sup>It modifies the original list. In contrast, the function sorted() will leave the original list unchanged.

Method	Description
max(list)	Finds the largest element in the list.
min(list)	Finds the smallest element in the list.
<pre>sum(list)</pre>	Returns the sum of the elements in the list. <sup>4</sup>
listOne + listTwo	Joins listOne with listTwo to form one list.
2 * list	Repeat list and concatenate to itself, making the list
	twice as long.
<pre>zip(listOne,listTwo)</pre>	Zips two lists together. (Creates [a1,b1,a2,b2]
	from [a1,a2,a3] and [b1,b2,b3]

```
a = ["1","j","n"]
b = ["r","s","t"]
a + b
#a=[5,6,2]
#min(a)
#print("1" + "j"+"n")
['1', 'j', 'n', 'r', 's', 't']
```

# 9.2.4 The range function

Often it will be necessary to generate a (possibly very long) list of integers. Instead of constructing the list by typing these numbers one by one, Python has a built-in function called range() that will do it for you. The range() function requires at least one argument to tell it how high the range should be.

```
a = range(10) # Generate a list of integers up to 10
a
```

range(0, 10)

This output probably wasn't what you expected. Instead of generating the full list of numbers, Python generates a range object that stands in place of it because it requires less memory. (Consider what might happen to your memory if you did range(100000000000).) To force Python to generate the list, you can convert the range object using the list() function.

<sup>&</sup>lt;sup>4</sup>Only works if the list contains only ints and floats

```
a = range(10) # Generate a list of integers up to 10
list(a)
```

The range function can be called with up to three arguments: range(start,end,stepsize). Consistent with indexing, the range includes the start value and excludes the end value. Below we generate a list of integers starting at 5, ending at 100 with a step size of 5.

```
myList = range(5,100,5)
list(myList)
```

[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]

[5, 10, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60, 65, 70, 75, 80, 85, 90, 95]

# 9.3 Tuples

Tuples are another object type similar to lists except that they are *immutable*... that is to say, they cannot be modified once created. They look similar to lists except that they are created using parenthesis instead of brackets. Because you can't change the elements of a tuple, they are often used so that you don't inadvertently modify (and lose) critical data. You can think of it as locking a file on your computer to avoid inadvertently modifying it and losing the original content.

Below is a tuple containing... Since there will be no need to change these values, it makes sense to store them in a tuple. Indexing and slicing work exactly the same as with lists and strings, so we can still use the values inside of a tuple to perform simple calculations. There are only two methods associated with tuples: count(element) and index(element). Their usage is identical to the list methods.

```
energies = (5,7,2,4,3,2,3)
energies.index(7)
len(energies)
```

7

# 10 Loops

Loops allow programs to rerun the same block of code multiple times. This is important because there are often

# 10.1 for loops

The for loop is probably the most common loop you will encounter and is a good choice when you know beforehand exactly what things you want to loop over. Here is an example of of for loop that is used to add up the elements of a list.

```
thesum = 0
for i in [3,2,1,9.9]:
    thesum = thesum + i
```

This would be equivalent to the following code:

```
thesum = 0

thesum = thesum + 3
thesum = thesum + 2
thesum = thesum + 1
thesum = thesum + 9.9
```

which isn't that much longer than using a loop. However, as the list gets longer and/or the mathematical operations being performed get more complex the second method would get unreasonably long. The correct language is to say that we are *iterating* over the list [3,2,1,9.9]. This means that the loop variable (i in this case but you can choose it to be whatever you want) gets assigned the values of the list elements, one by one, until it reaches the end of the list. You can use for loops to iterate over any multi-element object like lists or tuples. Python uses indentation to indicate where the loop ends. In this case there was only one statement inside to loop, but if you wanted more than one each line should be indented.

You can iterate over range objects and strings using for loops.

```
for i in ['Physics', 'is', 'so', 'fun']: # Iterate over a list of strings
      print(i)
Physics
is
so
fun
  for i in range(5,50,3): #Generates a list from 5 -> 50 with a step size of 3
      print(i)
5
8
11
14
17
20
23
26
29
32
35
38
41
44
47
```

These examples are so simple that you might wonder when a loop might actually be useful to you. Let's see if we can build a loop to calculate the following sum

$$\sum_{n=1}^{1000} \frac{1}{n^2} \tag{10.1}$$

```
theSum = 0
for n in range(1,1000):
    theSum = theSum + 1/n**2
print(theSum)
```

#### 1.6439335666815615

Here, n is being assigned the values 1,2,3,4....1000, one by one, until it gets all the way to 1000. Each time through the loop, n is different and the expression 1/n\*\*2 evaluates to a new value. The variable theSum is updated each time through to be the running total of all calculations performed thus far. Here's another example of a loop used to calculate the value of 20!:

```
theProduct = 1
for n in range(1,21):
    theProduct = theProduct * n #Multiply theProduct by n
print(theProduct)
```

#### 2432902008176640000

Remember that the range function creates a list starting at 1, going up to 21 but not including it. The math library has a function called factorial that does the same thing. Let's use it to check our answer:

```
from math import factorial
factorial(20)
```

2432902008176640000

## 10.1.1 Boolean Logic Inside Loops

Often when using loops, we only want a block of code to execute when some condition is satisfied. We can use boolean logic inside of the loop to accomplish this. For example, let's write a loop to compute the following sum:

$$\sum_{\frac{n}{5} \in \text{Int and } \frac{n}{3} \in \text{Int}} \frac{1}{n^2}$$

which is similar to the one we did above, but this time we only want to include terms where n is a perfect multiple of both 5 and 3. To check to see if  $\mathbf{n}$  is a perfect multiple of a number we can calculate the modulo (remainder after division) using the % operator and check that it is equal to zero.

```
theSum = 0
for n in range(1,1000):
    if n % 5 == 0 and n % 3 == 0:
        theSum = theSum + 1/n**2
print(theSum)
```

0.007243985583159138

## 10.1.2 Zipping and Enumerating

There are times when it is necessary to iterate over two lists simultaneously. For example, let us say that we have a list of atomic numbers (AN) and a list of approximate atomic masses (mass) of the most abundant isotopes for the first six elements on the periodic table.

```
AN = [1,2,3,4,5,6]
mass = [1,4,7,9,11,12]
```

If we want to calculate the number of neutrons in each isotope, we need to subtract each atomic number from the atomic mass. To accomplish this, it would be nice to iterate over both lists simultaneously

## 10.1.2.1 **Zipping**

The simplest way to iterate over two lists simultaneously is to combine both lists into a single, iterable object and iterate over it once. The zip function does just that by merging two lists or tuples into a nested list

```
AN = [1,2,3,4,5,6]
mass = [1,4,7,9,11,12]

zipped = zip(AN,mass)

for pair in zipped:
    print(pair[1] - pair[0])

0
2
4
5
```

6 6

The zip objects are "single use" so you can't reuse zipped in a later loop. If the two lists being zipped are not the same length, zip stops zipping when it reaches the end of the shorter list.

#### 10.1.2.2 Enumeration

A close relative to zip is enumerate which zips a list to the index value for that list (read that last statement again). It also returns a "single use" object that can be iterated over.

```
AN = [1,2,3,4,5,6]
mass = [1,4,7,9,11,12]
enum = enumerate(mass)
for idx,val in enum:
    print(val - AN[idx])

0
2
4
5
6
6
6
```

## 10.1.3 List Comprehension

It is fairly common to use a for loop to populate a list with a sequence of numbers.

```
myList = []

for i in range(10):
    myList.append(i**2)

print(myList)

[0, 1, 4, 9, 16, 25, 36, 49, 64, 81]
```

This entire process can be compressed down into a single line by expressing the for loop in square brackets. This is known as *list comprehension*. The code below will generate the list as above.

```
myList = [i**2 for i in range(10)]
print(myList)

[0, 1, 4, 9, 16, 25, 36, 49, 64, 81]
```

List comprehension can take a little time to get used to but it is well worth it. It saves both time and space and makes code less cluttered. You can even add boolean expressions to your conditionals for further control of the final result.

```
myList = [i**2 for i in range(10) if i %2 == 0] # Include only the evens.
print(myList)
```

[0, 4, 16, 36, 64]

# 10.2 while Loops

Logic can be combined with loops using something called a while loop. A while loop is a good choice when you don't know beforehand exactly how many iterations of the loop will be executed but rather want the loop to continue to execute until some condition is met. As an example, notice that in Equation 10.1, the terms in the sum get progressively smaller as n gets bigger. It doesn't make sense to continue adding to the sum once the terms get very small. Let's compute this sum by looping until the fraction  $\frac{1}{n^2}$  become smaller than  $1 \times 10^{-10}$ .

```
term = 1  # Load the first term in the sum
s = term  # Initialize the sum
n = 1  # Set a counter
while term > 1e-10:  # Loop while term is bigger than 1e-10
n = n + 1  # Add 1 to n so that it will count: 2,3,4,5
term = 1./n**2  # Calculate the next term to add
s = s + term  # Add 1/n^2 to the running total
```

This loop will continue to execute until term<1e-10. Note that unlike the for loop, here you have to do your own counting if you need to know how many iterations have been performed. Be careful about what value n starts at and when it is incremented (n = n + 1). Also notice that term must be assigned prior to the start of the loop. If it wasn't the loop's first logical test would fail and the loop wouldn't execute at all.

while loops should be used with caution because you can easily write a *faulty termination condition* and inadvertently write a loop that runs forever. This happens because your termination condition was never met. An example of this is given below.

Warning: Do not execute the code block below!!

```
x = 0
while x != 10:
    x = x + 3
print("Done")
```

The loop above is intended to end after a few iterations when the value of x is equal to 10. However, closer inspection reveals that the value of x will never be equal to 10. After the first iteration x is equal to 3, then 6.9.12.15 and so on... but never 10. This loop will run forever because the termination condition is never met (x != 10 never produces a False)!! If you choose to use a while loop, triple check your termination condition to make sure you haven't made a mental error. Avoiding the use of != or == in your termination condition will help too. Use <= or >= instead.

# 10.3 continue, break, and pass Commands

The continue, break, and pass commands are used to control the flow of code execution in loops. Here is a description of their usage:

Operator	Description
break	Exits a for/while loop.
continue	Skips the remaining loop block and begins the next
	iteration.
pass	No action; code contiues on

The break statement is useful when you want to completely stop a loop early. Here is our sum loop rewritten with a break statement added to stop the loop after 1000 iterations.

```
term = 1  # Load the first term in the sum
s = term  # Initialize the sum
n = 1  # Set a counter
while term > 1e-10:  # Loop while term is bigger than 1e-10
n += 1  #Add 1 to n so that it will count: 2,3,4,5
term = 1./n**2  # Calculate the next term to add
```

```
s += term  # Add 1/n^2 to the running total
if n > 1000:
    print('This is taking too long. I''m outta here...')
    break
```

This is taking too long. Im outta here...

The continue statement is similar to break except that instead of stopping the loop, it only stops the current iteration of the loop. All code below the continue statement will be skipped and the next iteration will begin. For example, if you wanted to do the sum from equation ?? but only include those terms for which n is a multiple of 3, it could be done like this:

Now, when the value of n is not a multiple of 3, the sum will not be updated and the associated terms are effectively skipped.

Finally, the pass statement does nothing. Seriously!! It is merely a place holder for code that has not bee written yet. Usually, you'll use the pass statement to run and test code without errors due to missing code.

# 11 Functions

We have already been using functions here and there but in this chapter we will introduce them formally and get into the details. A function encapsulates a block of code designed to perform a specific task or set of tasks. To perform the task correctly, most functions require that you provide some information (called arguments) when you call them. To call a function you type the name of the function followed by the needed arguments enclosed in parenthesis (()).

```
functionName(argument1, argument2, argument3...)
```

The **number and type** of arguments allowed is different for every function. As a first example, let's consider the **print** function, which is the simplest (and most familiar) function that we have used so far.

```
print("print is a function") #Single string argument
print("print", "is", "a", "function") # Multiple string arguments
print(5) # Single integer argument
print(5,4) # Multiple integer argument
print([5,4,2,5]) # Single list argument
print() # No arguments
print is a function
print is a function
5
5
4
[5, 4, 2, 5]
```

The print function is pretty flexible in what it allows for arguments; the arguments can be any type of data (strings, ints, floats, booleans, and even lists) and the number of arguments can be as large as you want. Most functions are a little more strict on what they allow their arguments to be. For example, the factorial function only allows one argument and that argument must be an integer. If you attempt to call the factorial function with a float argument or with more than one argument, the result will be an error.

<sup>&</sup>lt;sup>1</sup>The factorial of a float can be calculated, but the math library is not equipped to handle it.

```
from math import factorial
a = factorial(5.54)
b = factorial(5,3)
```

#### To Do:

- 1. Run the code above and take note of the error message that results.
- 2. Comment out the definition of a so you can also see the error message for the definition of b.

Python functions generally fall into three groups: functions that come standard with Python (called native functions), functions that you can import into Python, and functions that you write yourself.

## 11.1 Native Functions

There are a few functions that are always ready to go whenever you run Python. They are included with the programming language. We call these functions native functions. You have already been using some of them, like these

```
myList = [5,6,2,1]
a = len(myList) # 'len' function is native.

b = float(5) # 'float' function is native.

c = str(67.3) # 'str' function is native.
```

The len, float and str functions are all native and they all take a single argument. Other native function have been mentioned in previous chapters and others will be mentioned in the future.

# 11.2 Imported Functions

Many times, you will need to go beyond what Python can do by itself<sup>2</sup>. However, that doesn't mean you have to create everything you need to do from scratch. Most likely, the function that you need has already been coded. Somebody else created the function and made it available to anyone who wants it. Groups of functions that perform similar tasks are typically bundled

<sup>&</sup>lt;sup>2</sup>For example, Python does not include sin() or cos() as Native functions.

together into libraries ready to be imported so that the functions that they contain can be used.

In order to use use a function correctly, you'll need to know what information (arguments) the function expects you to give it and what information the function intends to return to you as a result. This information can be found in the library's documentation. Most libraries have great documentation with lists of the included functions, what the functions do, the expected arguments, and examples on how to use the most common ones. You can usually find the library documentation by searching the internet for the library's name plus "Python documentation".

Providing a complete list of all available libraries and function is not really the purpose of this book. Instead, we'll illustrate how to import functions and use them. As you use Python more and more you should get in the habit of searching out the appropriate library to accomplish the task at hand. When faced with a task to accomplish, your first thought should be, "I'll bet somebody has already done that. I'm going to try to find that library."

Functions are imported using the import statement. You've already seen how to perform very simple mathematical calculations (5/6,84, etc..), but for more complex mathematical calculations like  $\sin(\frac{\pi}{2})$  or  $e^{2.5}$ , you'll need to import these functions from a library.

```
import math

a = math.sqrt(5.2)
b = math.sin(math.pi)
c = math.e**2.5
```

The math. before each function is equivalent to telling Python "Use the sqrt() function that you will find in the math book I told you to grab." If you just type

```
sqrt(5.2)
```

Python won't know where to find the sqrt function and an error message will result. Sometimes the name of the module can be long and typing module. every time you want to use one of it's functions can be cumbersome. One way around this is to rename the module to a shorter name using the as statement.

```
import math as mt
a = mt.sqrt(5.2)
b = mt.sin(mt.pi)
c = mt.e**2.5
```

Instead of importing an entire module, you can import only a selection of functions from that module using the from statement. This can make your code even more succinct by eliminating the module. prefix altogether. The trade-off is that it won't be as clear which function belongs to which module.

```
from math import sqrt, sin, pi, e
a = sqrt(5.2)
b = sin(pi)
c = e**2.5
```

All of the functions belonging to a module can be imported at once using \*.

```
from math import *
a = sqrt(5.2)
b = sin(pi)
c = e**2.5
```

## 11.3 User-defined Functions

After having programmed for a while, you will notice that certain tasks get repeated frequently. For example, maybe in your research project you need to calculate the force exerted on an atom due to many other nearby atoms. You could copy and paste your force-calculation code every time it was needed, but that would likely result in lots of extra code and become very cumbersome to work with. You can avoid this by creating your own function to calculate the force between any two atoms. Then, every time you need another force calculation, you simple call the function again. You only write the force-calculation part of the code once and then you execute it as many times as you need to.

To create your own function, you first need to name the function. The name should be descriptive of what it does and makes sense to you and anyone else who might use it. The first line of a function definition starts with the def statement (short for definition) followed by the name of the function with whatever information, called *arguments*, that needs to be fed into the function enclosed in parenthesis. The last character in this line must be a colon. Everything inside the function is indented four spaces and placed directly below the first line.

```
def functionName(arg1,arg2,arg3):
    # Body of Function
# Body of Function
```

```
# Body of Function
```

As an example, let's construct a function that calculates the distance between two atoms. The function will need to know the location of each atom, which means that there should be two arguments: the xyz coordinates of both atoms passed as a pair of lists or tuples.

```
import math

def distance(coords1,coords2):

    dx = coords1[0] - coords2[0]
    dy = coords1[1] - coords2[1]
    dz = coords1[2] - coords2[2]
    d = math.sqrt(dx**2 + dy**2 + dz**2)
    print(f"The distance is {d:5.4f}.")

distance([1,2,3],[4,5,6])

distance([4.2,9.6,4.8],[2.9,2.6,3.4])
The distance is 5 1962
```

The distance is 5.1962. The distance is 7.2560.

This function works just fine with integers or floats for the coordinates.

#### 11.3.1 The return statement

The distance function prints out the value for the distance, but what if we want to use this distance in a subsequent calculation? Maybe we want to calculate the average distance between several pairs of atoms. We can instruct the function to return the final distance using the return statement. If the arguments to the function are the inputs, the return statement specifies what the output is. Let's modify the function above to include a return statement.

```
import math
def distance(coords1,coords2):
    dx = coords1[0] - coords2[0]
    dy = coords1[1] - coords2[1]
    dz = coords1[2] - coords2[2]
    d = math.sqrt(dx**2 + dy**2 + dz**2)
    return d
```

```
distOne = distance([1,2,3],[4,5,6])

distTwo = distance([4.2,9.6,4.8],[2.9,2.6,3.4])

averageDistance = (distOne + distTwo)/2

print(f"The average distance is {averageDistance:5.4f}.")
```

The average distance is 6.2261.

## 11.3.2 Local vs Global Variable Scope

Variables created inside of a function have *local scope*. This means that they are not accessible outside of the function. In our distance function the variables dx,dy,dz, and d were all local variables that are used inside the function but have no value outside of it. This is convenient because we don't have to worry about overwriting a variable or using it twice. If someone sends you a function and you want to use it in your code, you don't have to worry about what variable he/she chose to use inside his function; they won't affect your code at all.

```
def distance(coords1,coords2):
    dx = coords1[0] - coords2[0]
    dy = coords1[1] - coords2[1]
    dz = coords1[2] - coords2[2]
    d = math.sqrt(dx**2 + dy**2 + dz**2)
    return d

distOne = distance([1,2,3],[4,5,6])

print(dx) # There is no value associated with this variable outside of the function.
```

The down side to all of this is that you don't have access to function variables unless you pass them out of the function using the **return** statement.

Any variables defined outside of a function is called a global variable, which means that Python remembers these assignments from anywhere in your code including inside of functions. Using global variables with the intention to use them inside of functions is usually considered bad form and confusing and is discouraged. One notable exception to this rule are physical constants like  $g = 9.8 \text{ m/s}^2$  (acceleration due to gravity on Earth) or  $k_B = 1.38 \times 10^{-23}$  (Boltzmann's constant which is used heavily in thermodynamics) because these values will never change and may be used repeatedly. Generally speaking every variable that is used in a function ought to

be either i) passed in as an argument or ii) defined inside of the function. Below is an example of an appropriate use of a global variable.

```
def myFunction(a,b):
    c=a+g # <--- Notice the reference to 'g' here
    d = 3.0 * c
    f = 5.0 * d**4
    return f

#The variable below are global variables.
r = 10
t = 15
g = 9.8  #<--- g defined to be a global variable
result = myFunction(r,t)</pre>
```

## 11.3.3 Positional vs. Keyword Arguments

The function arguments we have been using so far are called *positional arguments* because they are required to be in a specific position inside the parenthesis. To see what I mean consider the example below.

```
def example(a,b):
    return a**b

resultOne = example(5,2)
resultTwo = example(2,5)

print(resultOne, resultTwo)
```

25 32

In the first call to example the local variable a gets assigned to be 5 and the local variable b gets assigned 2. In the second call the order of the arguments is switched and the subsequent assignments to a and b switch with it. This produces a different result from the function. Positional arguments are very common but the user must know what information goes where when calling the function.<sup>3</sup>

The other type of argument is the *keyword argument*. These arguments are attached to a keyword inside of the parenthesis. The advantage of a keyword argument is that the user does

<sup>&</sup>lt;sup>3</sup>This is another reason why you want to choose meaningful variable names for your arguments.

not need to be concerned about the location of the argument as long as it has the proper label.

```
def example(a=1,b=2):
    return a**b

resultOne = example(a=5,b=2)
resultTwo = example(b=2,a=5)

print(resultOne, resultTwo)
```

25 25

Another advantage to using keyword arguments is that a default value can be coded into the function. This means that we can call the function with some arguments missing and default values will be used for them. In the example above, the default value of b is 2 and if the function is called without specifying a value for that argument, the function will proceed as usual using the default value for b.

```
def example(a=1,b=2):
    return a**b

result = example(a=5)
print(result)
```

25

## 11.3.4 Lambda Functions

When the function you want to construct is very simple (one line), there is a shortcut code for making it called a *lambda function*. The benefit is that they occupy less lines of code than the standard def functions. A lambda function is defined as shown below with the variable immediately after the lambda statement as the independent variable in the function.

```
f = lambda x: x**2
print(f(5))
```

As a simple application of lambda functions let's consider a function from the scipy.integrate library called quad which will perform a numerical integration of a function. The quad function takes three arguments: the function to be integrated, and the upper and lower bound on the integral. We can use a lambda function for the first argument rather than using several lines of code to build one in the traditional fashion.

```
from scipy.integrate import quad
from math import sin, pi

quad(lambda x: sin(pi * x)**2,0,0.4 )
```

(0.15322553581056808, 1.7011451781741914e-15)

# Part II Intermediate Python

# 12 The numpy module

Numpy (pronounced "num"-"pie") is a popular Python library that is heavily used in the scientific/mathematical community. So much so that numpy is typically included as part of the standard bundle of libraries that comes with your Python installation. The functions inside numpy will allow you to solve problems with less effort and will produce faster-executing code.

# 12.1 Numpy Arrays

You are already familiar with Python lists but may not have noticed that they are not suitable for mathematical calculations. For example, attempting to multiply a list by a scalar or evaluate a mathematical function like  $\sin()$  on a list will *not* produce a mathematical result or may produce an error. For example, consider the following code.

```
myList = [4,5,7]
newList = 2 * myList
print(newList)
```

```
[4, 5, 7, 4, 5, 7]
```

You probably expected newList to be [8,10,14] but multiplying a list by a number doesn't do that. Instead it repeats the list and concatenates it to itself. To multiply each element of a list by a number you must use a for loop.

```
myList = [4,5,7]

newList = []
for i in myList:
    newList.append(i* 2)

print(newList)
```

```
[8, 10, 14]
```

but this seems overly cumbersome for such a simple task. Numpy *ndarrays* (short for n-dimensional arrays) or just *arrays* make this task much simpler. Arrays are similar to lists or nested lists except that mathematical operations and numpy functions (but not math functions) automatically propagate to each element instead of requiring a for loop to iterate over it. Because of their power and convenience, arrays are the default object type for any operation performed with NumPy.

# 12.2 Array Creation

# 12.2.1 Type Conversion from List

You can create an array from a list using numpy's array function. The list that is to be converted is the argument to the array function. Mathematical operations can then be performed on the array and that operation will propagate through to all of the elements.

```
from numpy import array
myArray = array([4,5,7])
newArray = 2 * myArray
print(newArray)
```

[ 8 10 14]

Nested lists, or lists that contain lists as their elements, can be converted to multi-dimensional arrays using the array function.

```
from numpy import array
  myArray = array([[1,2,3],[4,5,6]])
  print(myArray)

[[1 2 3]
  [4 5 6]]
```

## 12.2.2 The arange and linspace Functions

Numpy has some sequence-generating functions that generate arrays by specifying start, stop, and step size values similar to the way range generates a list. The two most common ones are arange and linspace. The arange function behaves very similar to the native Python range function with a few notable exceptions:

- 1. arange produces an array whereas range produces a list.
- 2. The step size for arange does not need to be an integer.
- 3. range produces an iterator and arange generates a sequence of values immediately.

The arguments to arange are similar to range

```
arange(start,stop,step)
```

The linspace function is related to the arange function except that instead of specifying the step size of the sequence, the sequence is generated based on the number of equally-spaced points in the given span of numbers. Additionally, arange excludes the stop value while linspace includes it. The difference between these two functions is subtle and the use of one over the other often comes down to user preference or convenience.

linspace(start,stop,number of points)

Below is an example that shows the usage of linspace and arange.

When using linspace you may still want to know what the sequence spacing is. You can request that linspace provide this information by adding the optional argument retstep = True to the argument list. With this addition, linspace not only returns the sequence to you, but also the stepsize.

Two other useful functions for generating arrays are zeros and ones which generate arrays populated with exclusively ones or zeros. The functions require shape arguments as a tuple or list to specify the shape of the array.

```
zeros((rows,columns))
```

If the array to be created is only one dimensional, the argument can be a single number instead of a tuple.

## zeros(n)

```
from numpy import zeros, ones

myArray = zeros([3,4])
myArray2 = ones(5)
print(myArray)
print(myArray2)

[[0. 0. 0. 0.]
[0. 0. 0. 0.]
[0. 0. 0. 0.]]
[1. 1. 1. 1. 1.]
```

Arrays of any constant (not just one or zero) can then be easily generated by performing the needed math on the original array.

```
from numpy import zeros,ones

myArray = zeros([3,4]) + 5
myArray2 = ones(5) * 12
print(myArray)
print(myArray2)

[[5. 5. 5. 5.]
[5. 5. 5. 5.]
[5. 5. 5. 5.]
[12. 12. 12. 12. 12.]
```

# 12.2.3 Arrays from Functions

A third approach is to generate an array from a function using the fromfunction function which generates an array of values using the array indices as the inputs. The function requires two arguments: the name of the function being used and the shape of the array being generated.

fromfunction(function, shape)

Let's make a 3 x 3 array where each element is the product of the row and column indices:

```
from numpy import fromfunction

def prod(x,y):
    return x * y

myArray = fromfunction(prod,(3,3))
print(myArray)

[[0. 0. 0.]
  [0. 1. 2.]
  [0. 2. 4.]]
```

The table below gives a summary of useful functions for creating numpy arrays. The required arguments are also described.

Table 12.1: Common functions for generating arrays

Method	Description
linspace(start,stop,n)	Returns an array of n evenly-spaced points begining at start and ending at stop.
arange(start,stop,dx)	Returns an array beginning at start, ending at stop with a step size of dx.
empty(dims)	Returns an empty array with dimensions dim.
zeros(dims)	Returns an array of zeros with dimensions dim.
ones(dims)	Returns an array of ones with dimensions dim.
zeros_like(arr)	Returns an array of zeros with dimensions that match the dimensions of arr.
<pre>fromfunction(function,dims)</pre>	Returns an array of numbers generated by evaluating function on the indices of an array with dimensions dims.
copy(arr)	Creates a copy of array arr.
genfromtext(file)	Reads file and loads the text into an array (file must only contain numbers).

# 12.3 Accessing and Slicing Arrays

Accessing and slicing arrays can be done in exactly the same way as is done with lists. However, there is some additional functionality for accessing and slicing arrays that do not apply to lists.

# 12.3.1 One-dimensional Arrays

Elements from a one-dimensional array can be extracted using square brackets ([]) just like we have done with lists.

```
from numpy import array

myArray = array([3,4,7,8])
print(myArray[2])
```

7

## 12.3.2 Multi-dimensional Arrays

Multi-dimensional array can be indexed in a similar fashion to nested lists, but because we often encounter multi-dimensional arrays there is a shortcut that makes the syntax simpler and more convenient. Let's consider a two-dimensional array as an example. To access the entire second row of the array, provide the row index in square brackets just as with one-dimensional arrays.

```
from numpy import array
myArray = array([[1,2,3],[4,5,6], [7,8,9]])
print(myArray[1])

[4 5 6]
```

To access the second element *in the second row*, we can add another set of square brackets with the appropriate index inside, just as we did with nested lists. However, for convenience the second set of square brackets can be omitted and the row and column indices can be placed next to each other and separated by a comma.

array\_name[row,column]

```
from numpy import array
myArray = array([[1,2,3],[4,5,6], [7,8,9]])

print(myArray[1][1]) # This works, but is a bit hard on the eyes
print(myArray[1,1]) # This works also and is easier to look at.
5
5
```

# 12.3.3 Accessing Multiple Elements

Multiple elements of an array can be accessed using a list for the index instead of a single number.

```
from numpy import array

myArray = array([1,2,3,4,5,6,7,8,9,10])
```

```
print(myArray[2]) # Extract element 2
print(myArray[ [3,6,9] ]) # Extract elements 3, 6, and 9.
3
[ 4 7 10]
```

This can even be done with multi-dimensional arrays. If the index is a single list, the corresponding rows will be extract. If the corresponding list of columns is added to the index list, individual elements will be extracted.

```
array_name[[rows]]  # Access set of rows

array_name[[rows], [columns]]  # Access set of elements

from numpy import array
  myArray = array([[1,2,3],[4,5,6], [7,8,9]])

print(myArray[[0,1]])  # Extract rows 0 and 1.

print(myArray[[1,2,0],[0,2,2]])  # Extract elements (1,0), (2,2), and (0,2)

[[1 2 3]
  [4 5 6]]
[4 9 3]
```

# 12.4 Slicing Arrays

## 12.4.1 Multi-dimensional Arrays

We've already shown you how to slice a list using the : operator. The same can be done with arrays. However, for 2D (and higher) arrays the slicing is more powerful (intuitive). It can be helpful to visualize an array as a matrix, even if it is not being treated that way Mathematically. For example, let's say that you define the following array:

```
from numpy import array
myArray = array([[1,2,3],[4,5,6], [7,8,9]])
```

which can be visualized as the following matrix:

$$\begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$$

To slice out the following 2 x 2 sub matrix:

$$\begin{pmatrix} 5 & 6 \\ 8 & 9 \end{pmatrix}$$

we could do

```
from numpy import array
  myArray = array([[1,2,3],[4,5,6], [7,8,9]])
  print(myArray[1:3,1:3])

[[5 6]
  [8 9]]
```

To include all of the elements in a given dimension, use the : alone with no numbers surrounding it.

```
from numpy import array
  myArray = array([[1,2,3],[4,5,6], [7,8,9]])

print(myArray[:,1:3]) # Extract all rows with columns 1 and 2

[[2 3]
  [5 6]
  [8 9]]
```

# 12.4.2 Boolean Slicing

Boolean operations can be evaluated on arrays to produce corresponding arrays of booleans. The boolean array can then be used to index the original array and extract elements that meet some criteria.

```
from numpy import array
a = array([1,2,3,4,5,6])
boolArray = a > 2
print(boolArray)
print(a[boolArray])

[False False True True True]
[3 4 5 6]
```

This also works on multi-dimensional arrays although the result is always one-dimensional regardless of the shape of the original array.

```
from numpy import array
myArray = array([[1,2,3],[4,5,6], [7,8,9]])
print(myArray[myArray>2]) # Extract elements that are greater than 2.
[3 4 5 6 7 8 9]
```

# 12.5 Vectorization and Broadcasting

A major advantage of numpy arrays over lists is that operations *vectorize* across the arrays. This means that mathematical operations propagate through the array instead of requiring a for loop. This speeds up the calculation and makes code easier to write and read. Simple mathematical operations like adding, subtracting, etc can be performed on arrays as you would expect and the operation propagates through to all elements.

```
from numpy import array
a = array([1,2,3])
b = array([4,5,6])
c = a + b
```

All of the common mathematical operations that you learned for numbers now apply to arrays. Cool!

## 12.5.1 Numpy Functions

The numpy library has a massive collection of vectorized mathematical functions and these functions should be used instead of similar functions from other libraries that are not vectorized (like math).

```
from numpy import array
from numpy import sqrt as nsqrt
from math import sqrt as mathsqrt

squares = array([1,4,9,16,25])

print(nsqrt(squares))
#print(mathsqrt(squares)) #This will fail because it wasn't a numpy function.
```

[1. 2. 3. 4. 5.]

## 12.5.2 Arrays of same Dimensions

If a mathematical operation is performed between two arrays of the same dimensions, the mathematical operation is performed between corresponding elements in the two arrays. For example, if two  $2 \times 2$  arrays are added together, element (0,0) of the first array gets added to the corresponding element in the second and so forth for all elements:

$$\begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} + \begin{pmatrix} 5 & 6 \\ 7 & 8 \end{pmatrix} = \begin{pmatrix} 6 & 8 \\ 10 & 12 \end{pmatrix}$$

```
from numpy import array

a = array([[1,2],[3,4]])
b = array([[5,6],[7,8]])

c = a + b  # Add the elements of the arrays together.
d = a * b  # Multiply the elements of the arrays together.

print(c)
print(d)

[[ 6   8]
[10  12]]
[[ 5  12]
[21  32]]
```

### 12.5.3 Arrays of Different Dimensions

When a mathematical operation between two arrays of different dimensions is attempted, Python has to figure out how to make them have the same shape before performing the operation. *Broadcasting* refers to the set of rules used for operations like this. To handled arrays with different dimensions, NumPy pads or clones the array with fewer dimensions to make it have the same dimensions as the larger array. For example, what would happen if you attempted this operation:

$$\begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} + \begin{pmatrix} 2 & 2 \end{pmatrix}$$

One array is 2 x 2 and the other is 1 x 2. Before the addition can take place, NumPy clones the smaller array and repeats it until it has the same size as the bigger array.

$$\begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} + \begin{pmatrix} 2 & 2 \\ 2 & 2 \end{pmatrix}$$

```
from numpy import array
a = array([[1,2],[3,4]])
b = array([2,2])
c = a + b
```

```
print(c)
[[3 4]
```

[5 6]]

There are some cases where NumPy simply cannot figure out how to broadcast one of the arrays appropriately and an error results. When broadcasting, NumPy must verify that all dimensions are compatible with each other. Two dimensions are compatible when i) they are equal or ii) one of the dimensions is 1. For example, if we tried to perform the following mathematical operation, broadcasting would fail because the first dimension of the first array is 2 and the first dimension of the second array is 3.

$$\begin{pmatrix} 1 & 2 & 3 \\ 3 & 4 & 5 \end{pmatrix} + \begin{pmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 3 & 3 \end{pmatrix}$$

```
from numpy import array

a = array([[1,2,3],[4,5,6]])
b = array([[1,1,1],[2,2,2],[3,3,3]])
c = a + b
```

but if we attempted

$$\begin{pmatrix} 1 & 2 & 3 \end{pmatrix} + \begin{pmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 3 & 3 \end{pmatrix}$$

the operation would succeed because the first dimension of the first array is 1 and the second dimension of both arrays are 3.

### 12.5.4 Vectorizing user-defined functions

Standard Python functions are often designed to perform a single calculation rather than iterate over a list to perform many calculations. For example, here is a function to calculate the average acceleration of an object given its final velocity and time of travel.

```
def accel(velocity, time):
    return velocity / time
```

```
print(accel(52.6,5.6))
```

#### 9.392857142857144

Now what if I have a list of many times that I'd like to feed into this function and get an acceleration value for each one.

```
def accel(velocity, time):
    return velocity / time

times = [4.6,7.9,3.2,8.5,9.2,4.7]
print(accel(52.6,times)) # Produces an error because you can't divide by a list
```

An error results here because Python does not know how to divide by a list. We can NumPy-ify this function using a function called **vectorize**. The resulting function will behave just like the other functions from the NumPy library, vectorizing across the list of times.

```
from numpy import vectorize
def accel(velocity, time):
    return velocity / time

times = [4.6,7.9,3.2,8.5,9.2,4.7]
vaccel = vectorize(accel)  # Vectorize the function!
print(vaccel(52.6,times))  # Succeeds because NumPy knows how to vectorize.
```

```
[11.43478261 6.65822785 16.4375 6.18823529 5.7173913 11.19148936]
```

Of course, we also could have just converted our times list into an array and used the original function.

```
from numpy import array
def accel(velocity, time):
    return velocity / time

times = array([4.6,7.9,3.2,8.5,9.2,4.7])
print(accel(52.6,times)) # Succeeds because times is an array not a list.

[11.43478261 6.65822785 16.4375 6.18823529 5.7173913 11.19148936]
```

### 12.6 Manipulating and Modifying Arrays

A wealth of functions exist to perform routine manipulation tasks on arrays once they are created. Often these tasks will involve changing the number of rows or columns or merging two arrays into one. The *size* and *shape* of an array are the number of elements and dimensions, respectively. These can be determined using the **shape** and **size** methods.

```
from numpy import array

a = array([[1,2,3],[4,5,6]])
  print(a.size)
  print(a.shape)

6
(2, 3)
```

### 12.6.1 Reshaping Arrays

The dimensions of an array can be modified using the reshape function. This methods maintains the number of elements and the order of elements but repacks them into a different number of rows and columns. Because the number of elements is maintained, the size of the new array has to be the same as the original. Let's see an example.

```
from numpy import array, reshape
a = array([[1,2,3],[4,5,6]])
b = reshape(a,[3,2])
print(a)
print(b)

[[1 2 3]
[4 5 6]]
[[1 2]
[3 4]
[5 6]]
```

The original array (a) was a  $2 \times 3$  and had 6 elements and the reshaped array also has 6 elements but is a  $3 \times 2$ . You can start with a one-dimensional array and reshape it to a higher dimensional array.

### 12.6.2 Flattening Arrays

Flattening an array takes a higher-dimensional array and squishes it into a one-dimensional array. You can "flatten" an array with the flatten method, but note that flatten doesn't actually modify the original array.

```
from numpy import array
a = array([[1,2,3],[4,5,6]])
a.flatten()

print(a) # 'a' remains unchanged

a = a.flatten() # If you want to change the definition of a, redifine it.
print(a)

[[1 2 3]
[4 5 6]]
[1 2 3 4 5 6]
```

### 12.6.3 Transposing Arrays

Transposing an array rotates it across the diagonal and can be accomplished with the transpose function. There is also a shortcut method for this of array. T to accomplish the

same thing but just as with flatten it does not modify the original array. (neither does transpose)

```
from numpy import array,transpose
a = array([[1,2,3],[4,5,6]])
transpose(a)

print(a) # 'a' remains unchanged
a = a.T # If you want to change the definition of a, redefine it.
print(a)

[[1 2 3]
[4 5 6]]
[[1 4]
[2 5]
[3 6]]
```

### 12.6.4 Merging Arrays

Several function exist for combining multiple arrays into a single array. We'll give examples for a couple and mention the others in reference tables. The most commonly used functions for this task are vstack (vertical stacking) and hstack (horizontal stacking). vstack will stack the original arrays vertically to create the new array and hstack will stack them horizontally. Here are some examples.

```
6.6666667 7.77777778 8.88888889 10.
 [ 0.
                                     1.66666667
                                                2.2222222
              0.5555556
                        1.11111111
                                                            2.7777778
  3.3333333 3.88888889
                         4.4444444
                                    5.
                                              ]]
[ 0.
             1.1111111
                        2.2222222 3.3333333 4.4444444
                                                           5.5555556
                        8.8888889 10.
 6.6666667
             7.7777778
                                             ]
[ 0.
             1.11111111
                        2.2222222
                                    3.33333333
                                               4.4444444
                                                           5.5555556
 6.6666667
             7.7777778
                        8.8888889 10.
                                                           0.5555556
                        2.2222222
 1.11111111
             1.66666667
                                   2.77777778 3.33333333
                                                          3.8888889
 4.4444444
                      ]
```

### 12.7 Commonly-used Array Methods and Functions

NumPy contains an extensive listing of array methods and functions and it would be impractical to list them all here. However, below you will find some tables of some of the commonly used ones that can serve as a reference.

Table 12.2: Array Attribute Methods and Functions

Method	Description
shape(array) or array.shape	Returns the dimensions of the array.
ndim(array) or array.ndim	Returns the number of dimensions (i.e. a 2D array is
	2).
size(array) or $array.size$	Returns the number of elements in an array.

Table 12.3: Array Modification Methods and Functions

Method	Description
array.flatten()	Returns a flattened view of array.
reshape(array,dims) or	Returns a view of array reshaped into an array with
array.reshape(dims)	dimensions given by dims.
array.resize(dims)	Modifies array to be a resized array with dimensions
•	dims.
transpose(array) or array.T	Returns a view of the transpose of array.
sort(array)	Returns a view of a sorted version of array.
array.sort()	Modifies array to be sorted.
argsort(array)	Returns index values that will sort array.
array.fill(x)	Modifies array so that all elements are equal to x.
vstack(a,b)	Vertically stack arrays <b>a</b> and <b>b</b> to form the new array.
hstack(a,b)	Horizontally stack arrays a and b to form the new
	array.

Method	Description
<pre>vsplit(array,n)</pre>	Splits array vertically into n equal parts.
hsplit(array,n)	Splits array horizontally into n equal parts.
append(array,x)	Returns a view of array with x added to the end of
	the array.
<pre>insert(array,n,x)</pre>	Returns a view of array with x inserted at location n.
delete(array,n)	Returns a view of array with element at location n
	removed.
unique(array)	Returns a view of the unique elements of array.

Table 12.4: Array Measurement Methods and Functions

Method	Description
min(array) or array.min()	Returns the minimum value in an array.
<pre>max(array) or array.max()</pre>	Returns the maximum value in an array.
<pre>argmin(array) or array.argmin()</pre>	Returns the location of the minimum value in an array.
<pre>argmax(array) or array.argmax()</pre>	Returns the location of the maximum value in an array.
fmin(array1,array2)	Returns the minimum between two arrays of the same size. (Arrays are compared element wise.)
<pre>fmax(array1,array2)</pre>	Returns the maximum between two arrays of the same size. (Arrays are compared element wise.)
<pre>mean(array) or array.mean()</pre>	Returns the mean of array.
<pre>median(array) or array.median()</pre>	Returns the median of array.
<pre>std(array) or array.std()</pre>	Returns the standard deviation of array.
cumprod(array) or	Returns the cumulative product of array.
array.cumprod()	
<pre>cumsum(array) or array.cumsum()</pre>	Returns the cumulative sum of array.
<pre>sum(array) or array.sum()</pre>	Returns the sum of all elements in array.
<pre>prod(array) or array.prod()</pre>	Returns the product of all elements in array.
floor(array)	Returns the floor (i.e., rounds down) of all elements in
	array.
ceil(array)	Returns the ceiling (i.e., rounds up) of all elements in
	array.

# 13 File I/O (Input/Output)

Up to now, we have been working with computer-generated or manually typed data sets. Often in a scientific setting your data will be stored in a file and you will need to read the contents of the file into Python so you can perform an analysis. Most data files are *text* files, but there is a large variety of these that differ mostly in the way the information is formatted. The file extension (i.e., the 3 or 4 letters after the period at the end of a file name) specifies the formatting of the file. For example, a *.csv* file (short for comma-separated values) has commas to separate the information.

### 13.1 Reading Files

### 13.1.1 Reading Line by Line

The first way to read a file is using a for loop to iterate over the file line by line. Admittedly, this is not the most elegant or efficient way to read a file but we present it first because it always works. First, the file is opened using the open command. The file should be attached to a variable for later use. Next, the data is read one line at a time using the readlines() method. We should use a for loop for this. Finally, it is a good idea to close the file when you're finished. Let's see an example for reading in the following file, which will be named squares.csv

```
1, 1
2, 4
3, 9
4, 16
5, 25
6, 36
7, 49

file = open("squares.csv")
  for line in file.readlines():
        print(line)
```

```
file.close()

1,1

2,4

3,9

4,16

5,25

6,36

7,49

8,64

9,81

10,100
```

You can see how each line gets read separately and printed off. But this isn't super useful yet because we'd probably like to have the numbers stored in lists for our forthcoming analysis. We can fix this by creating some empty lists and appending the appropriate values as they are read in.

```
numbers = []
squares = []

file = open("squares.csv")
for line in file.readlines():
    numbers.append( int(line.split(',')[0]) )
    squares.append( int(line.split(',')[1]) )

file.close()

print(numbers)
print(squares)
[1, 2, 3, 4, 5, 6, 7, 8, 9, 10]
```

```
[1, 4, 9, 16, 25, 36, 49, 64, 81, 100]
```

Now the data from the file is saved in Python lists and our analysis can proceed.

One final note: if all you want to do is read your file in as a list of strings (one string for each line), that can be done without a for loop using the readlines function (rather than readline).

```
file = open("squares.csv")
data = file.readlines()
file.close()

print(data)
```

### 13.1.2 Using NumPy's genfromtxt function

If the data file is highly structured (every line looks the same, separated character is consistent across the file, etc) then NumPy's genfromtxt function can read the data very efficiently into an array. The genfromtxt function requires only one argument (the file name) with another optional argument (delimiter) that is typically included to specify the character used to separate the data. Below is an example for using this function to read in the .csv data we have been working with.

```
from numpy import genfromtxt
  data = genfromtxt('squares.csv',delimiter = ",")
  print(data)
[[ 1.
         1.]
 2.
         4.]
 9.]
   3.
 4.
        16.]
 Γ
   5.
        25.1
 6.
        36.]
 Γ
   7.
       49.]
 [ 8.
        64.]
   9.
        81.]
 [ 10. 100.]]
```

Notice that the data was read into a NumPy array (2D in this case because there were two columns of data), which means that we can easily slice off the individual columns if needed.

Other optional arguments that can be used with the **genfromtxt** function are given in the table below:

Argument	Description
delimiter	The string used to separate value. By default,
	whitespace acts as the delimiter.
skip_header	The number of lines to skip at the beginning of a file.
skip_footer	The number of lines to skip at the end of a file.
usecols	Specify which columns to read with 0 being the first.
	For example, usecols = (0,2,5) will read the 1st,
	3rd, and 6th columns.
comments	The character used to indicate the start of a comment.
	Lines beginning with this character will be discarded.

## 13.2 Writing Files

Writing Python data to file is as simple as is reading a file. Just like when you are reading a file, determining which method to use will be determined by the type of data that you are writing. If your data is strictly numerical information stored in an array, Numpy has a function that will quickly save the data to a file. If your data is rife with inconsistencies, non-numerical data, etc, you'll have to use Python's native write function.

### 13.2.1 Writing Line by Line

Sometimes the data file that you want to write includes some text or other non-numerical data. For example, what if you wanted to write the following data to file:

Planet	Acceleration due to gravity $(m/s^2)$
Earth	9.8
Moon	1.6
Mars	3.7
Venus	8.83
Saturn	11.2
Uranus	10.5
Neptune	13.3
Pluto	0.61
Jupiter	24.5
Sun	275

```
planets = ["Earth","Moon","Mars","Venus","Saturn","Uranus","Neptune","Pluto","Jupiter","Su
g=[9.8,1.6,3.7,8.83,11.2,10.5,13.3,0.61,24.5,275]

f= open("planets.txt","w")

f.write("Planet g (m/s^2)\n")
f.write("----\n")

for idx,planet in enumerate(planets):
    f.write(f"{planet:10s} {g[idx]:5.2f} \n")

f.close()
```

### 13.2.2 Using NumPy's savetxt function

If the data is strictly numerical and contains no text, the savetxt function is a fast and efficient way to write the data to file. For example, maybe you have a two dimensional array containing various columns of planetary data.

Radius ( $\times 10^6$ meters )	Mass ( $\times 10^{23} \text{ kg}$ )	Acceleration due to gravity (m/s <sup>2</sup> )
6.37	59.8	9.8
1.74	0.736	1.6
3.38	6.42	3.7

Radius ( $\times 10^6$ meters )	Mass ( $\times 10^{23} \text{ kg}$ )	Acceleration due to gravity (m/s <sup>2</sup> )
6.07	48.8	8.83
58.2	5680	11.2
23.5	868	10.5
22.7	1030	13.3
1.15	0.131	0.61
69.8	19000	24.5
696	19890000	275

```
from numpy import savetxt

data =[[6.37,59.8,9.8],[1.74,0.736,1.6],[3.38,6.42,3.7],[6.07,48.8,8.83],[58.2,5680,11.2],

savetxt("planetsData.txt",data,fmt = "%5.2e")
```

The fmt keyword argument can be be added to specify how to format the data. If the data is stored in separate one-dimensional arrays, you can pack them into a single list(tuple) when using the savetxt function and it will write each data set to it's own line in the file.

```
radius = [6.37,1.74,3.38,6.07,58.2,23.5,22.7,1.15,69.8,696]
mass = [59.8,0.736,6.42,48.8,5680,868,1030,0.131,19000,19890000]
g = [9.8,1.6,3.7,8.83,11.2,10.5,13.3,0.61,24.5,275]
savetxt("planetsDataTwo.txt",(radius,mass,g),fmt = "%5.2e")
```

Other optional arguments that can be used with the savetxt function are given in the table below:

Argument	Description
delimiter	String or character to separate columns.
newline	String or character to separate lines.
header	String to be written at the beginning of the file.
footer	String to be written at the end of the file.
comments	String that will be prepended to the header and footer string to mark them as comments.

# 14 Basic Plotting

Creating plots is an important task in science and engineering. The old adage "A picture is worth a thousand words!" is wrong.... it's worth way more than that if you do it right. When making plots on a computer it is important to remember that computers don't plot functions, rather they plot individual points. Only when you connect those points does the image look like the function you are so used to seeing. In this chapter we will use a library called matplotlib for plotting. More specifically, we will import the pyplot function inside of matplotlib. It is customary to use plt as an alias for pyplot.

```
from matplotlib import pyplot as plt
%matplotlib inline
```

The %matplotlib inline statement is a Jupyter notebook command. It tells Jupyter to display any plots generated directly in the notebook instead of in a separate window. If you use matplotlib in another environment, you should remove this line and instead place plt.show() af the plot commands.

### 14.1 Plotting Functions of a Single Variable

In order to make a plot, matplotlib needs lists of the x and y coordinates for the points that are going to be plotted. A good choice for generating the x-coordinates is either linspace or arange from NumPy. The following equation is called the Lennard-Jones equation and it gives the energy of two atoms interacting as a function of separation distance

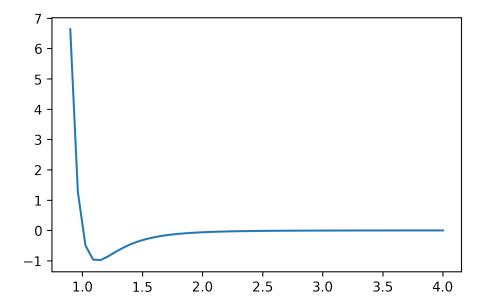
$$E = 4\sigma \left[ \left( \frac{\epsilon}{r} \right)^{12} - \left( \frac{\epsilon}{r} \right)^{6} \right]$$

Let's plot this function from 0.9 to 4.0.

```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace,sqrt
sigma = 1
```

```
epsilon = 1
r = linspace(0.9,4,50)
energy = 4 * sigma* ((epsilon/r)**12 - (epsilon/r)**6)

plt.figure()
plt.plot(r,energy)
```



By default, matplotlib connects the points to form a line (albeit a bit jagged because we didn't plot that many points).

### 14.1.1 Linestyles, Markers, and Colors

Three optional arguments can help you control the look of the plot: marker, linestyle, and color. All of these arguments take strings. The linestyle argument determines if the line is solid or dashed and what type of dashing to use. The marker argument specifies the shape of the plot marker to be used. Below are tables listing possible options for these arguments.

Table 14.1: Common Marker Styles

Argument	Description
0	circle
*	star
р	pentagon

Argument	Description
^	triangle
S	square

Table 14.2: Common Line Styles

Argument	Description
_	solid
	dashed
	dash-dot
:	dotted

Table 14.3: Common Colors

Argument	Description
b	blue
r	$\operatorname{red}$
k	black
g	green
m	magenta
С	cyan
У	yellow

Several other keyword arguments exist for helping you customize the look of your plots. They are summarized in the table below.

Table 14.4: A Few Common plot keyword arguments

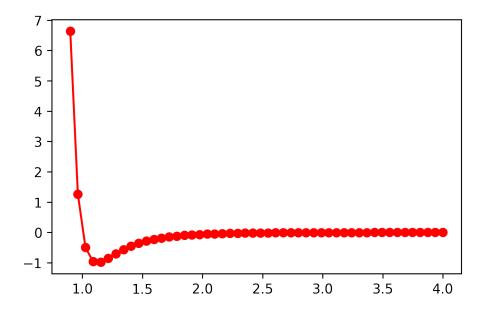
Argument	Description
linestyle or ls	line style
marker	marker shape
linewidth or lw	line width
color or c	line color
markersize or ms	marker size

Here is the plot from above with some of these keyword arguments added.

```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace,sqrt

r = linspace(0.9,4,50)
energy = 4 * ((1/r)**12 - (1/r)**6)

plt.figure()
plt.plot(r,energy,linestyle = '-', marker = 'o', color = 'r')
```



### 14.1.2 Labeling Plots

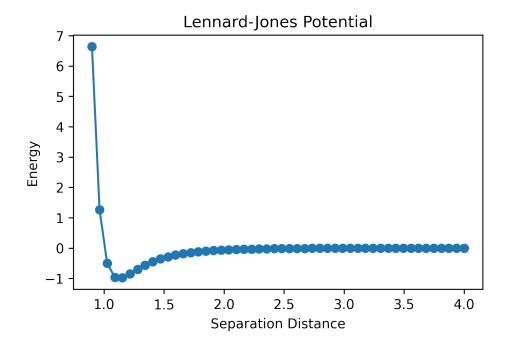
All good plots have axes labels and a title and you can add them to a matplotlib plot using the xlabel(), ylabel(), and title() functions which are placed on their own line after the plot command.

```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace,sqrt

r = linspace(0.9,4,50)
energy = 4 * ((1/r)**12 - (1/r)**6)
```

```
plt.figure()
plt.plot(r,energy,marker = 'o')
plt.xlabel("Separation Distance")
plt.ylabel("Energy")
plt.title("Lennard-Jones Potential")
```

Text(0.5, 1.0, 'Lennard-Jones Potential')



#### 14.1.3 Greek Letters

In physics, Greek letters get used all the time and you may find yourself wanting to use one in a plot title or axes label. This can be accomplished by placing an **r** in front of the title string and then placing the name of the greek variable inside of \$ with a backslash in front of it. This is better illustrated with an example.

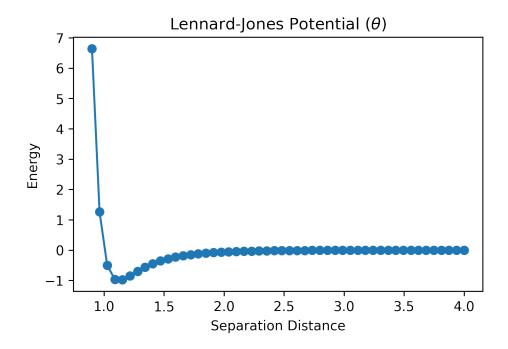
```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace,sqrt

r = linspace(0.9,4,50)
```

```
energy = 4 * ((1/r)**12 - (1/r)**6)

plt.figure()
plt.plot(r,energy,marker = 'o')
plt.xlabel("Separation Distance")
plt.ylabel("Energy")
plt.title(r"Lennard-Jones Potential ($\theta$)")
```

Text(0.5, 1.0, 'Lennard-Jones Potential (\$\\theta\$)')



You can subscript any character using the \_ character followed by the subscript.  $\theta_1$  can be written as \theta\_1. If the subscript is more than one character, you'll need to enclose it in curly braces.  $\theta_{12}$  is written as \theta\_{12}\. Superscripts work the same way only using the ^ character instead of the underscore.

Table 14.5: Lowercase greek letters

Argument	Description
$\alpha$	\alpha
$\beta$	\beta
$\gamma$	\gamma

Argument	Description
$\delta$	\delta
$\epsilon$	\epsilon
$\phi$	\phi
$\theta$	\theta
$\kappa$	\kappa
$\lambda$	\lambda
$\mu$	\mu
$\nu$	\nu
$\pi$	\pi
ho	\rho
$\sigma$	\sigma
au	\tau
ξ ζ	\xi
ζ	\zeta

### 14.1.4 Controlling the Axes

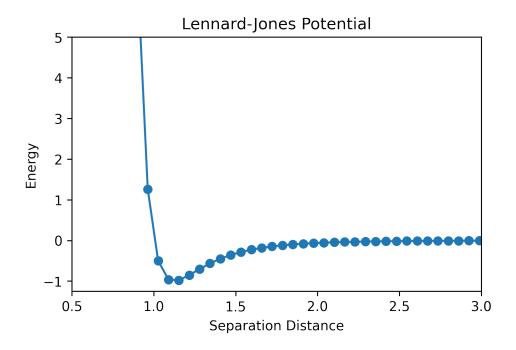
By default, matplotlib will size the plot window to include all of the points. If you want to zoom in our out, you can do so with the xlim and ylim functions. These functions should be placed after the plot command on their own line just like the label commands.

```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace,sqrt

r = linspace(0.9,4,50)
energy = 4 * ((1/r)**12 - (1/r)**6)

plt.figure()
plt.plot(r,energy,marker = 'o')
plt.xlim(0.5,3)
plt.ylim(-1.25,5)
plt.xlabel("Separation Distance")
plt.ylabel("Energy")
plt.title("Lennard-Jones Potential")
```

Text(0.5, 1.0, 'Lennard-Jones Potential')



### 14.1.5 Overlaying Plots

Often you will want to plot more than one set of data on the same set of axes. This can be accomplished two ways. The first way is to call the plot function twice in the same Jupyter notebook cell. Matplotlib will automatically place the plots on the same figure and scale it appropriately. Below you will find a plot of the Lennard-Jones potential for two choices of the parameters  $\sigma$  and  $\epsilon$ .

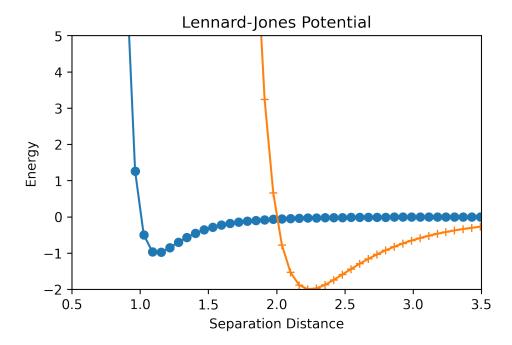
```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace,sqrt

r = linspace(0.9,4,50)

sigmaOne = 1
epsilonOne = 1
sigmaTwo = 2
epsilonTwo = 2
energyOne = 4 * sigmaOne* ((epsilonOne/r)**12 - (epsilonOne/r)**6)
energyTwo = 4 * sigmaTwo * ((epsilonTwo/r)**12 - (epsilonTwo/r)**6)
```

```
plt.figure()
plt.plot(r,energyOne,marker = 'o')
plt.plot(r,energyTwo,marker = '+')
plt.xlim(0.5,3.5)
plt.ylim(-2,5)
plt.xlabel("Separation Distance")
plt.ylabel("Energy")
plt.title("Lennard-Jones Potential")
```

Text(0.5, 1.0, 'Lennard-Jones Potential')



The other way to overlay plots is to include both sets of data into a single plot command.

```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace,sqrt

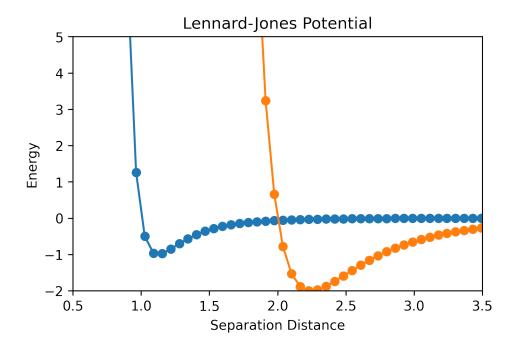
r = linspace(0.9,4,50)

sigmaOne = 1
epsilonOne = 1
```

```
sigmaTwo = 2
epsilonTwo = 2
energyOne = 4 * sigmaOne* ((epsilonOne/r)**12 - (epsilonOne/r)**6)
energyTwo = 4 * sigmaTwo * ((epsilonTwo/r)**12 - (epsilonTwo/r)**6)

plt.figure()
plt.plot(r,energyOne,r,energyTwo,marker = 'o')
plt.xlim(0.5,3.5)
plt.ylim(-2,5)
plt.xlabel("Separation Distance")
plt.ylabel("Energy")
plt.title("Lennard-Jones Potential")
```

Text(0.5, 1.0, 'Lennard-Jones Potential')



# 14.2 Other Plot Types

Beyond the line plot that we learned about in the previous section, matplotlib can generate many other types of plots that are very useful in a scientific setting. We'll explore some of them here.

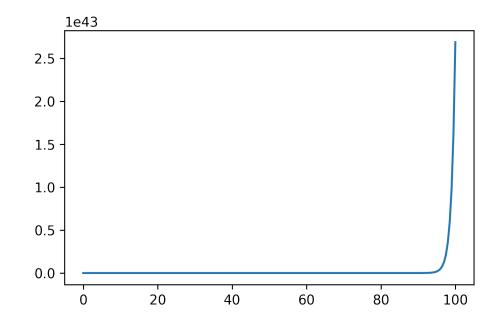
### 14.2.1 Logarithmic Plots

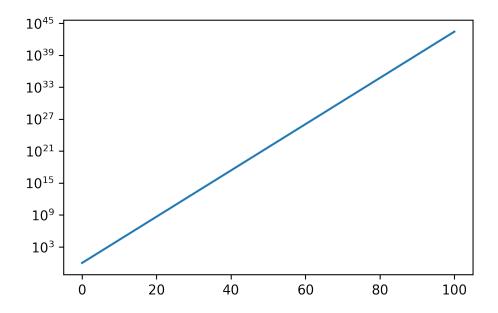
Sometimes the function being plotted increases or decreases by many orders of magnitude and a normal linear plot would not be particularly useful. Logarithmic plots can be made with the use of the semilogx, semilogy, or loglog functions depending on which axes you want to be on a logarithmic scale. Consider the first plot produced below. Notice that it rises from 0 at x = 0 to  $10^{45}$  at x = 100. Plotting this function with the y-axis scaled logarithmically will smooth out the plot and make it easier to analyze.

```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace,exp

x = linspace(0,100,200)
y = exp(x)

plt.figure()
plt.plot(x,y)
plt.figure()
plt.semilogy(x,y)
```





### 14.2.2 Bar Plots

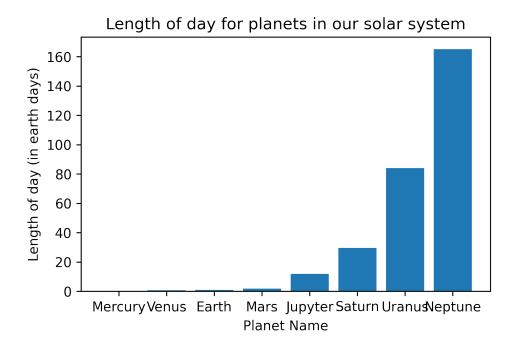
A bar plot and a scatter plot are quite similar except that instead of a plot marker indicating the associated value, the height of the bar represents the value. You can make a bar plot using the bar function inside of pyplot.

```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace,sqrt

#d = [5.8e10,1.9e11,1.5e11,2.3e11,7.8e11,1.4e12,2.9e12,4.5e12]
d = [1,2,3,4,5,6,7,8]
T = [0.241,0.615,1,1.88,11.9,29.5,84,165]

plt.figure()
plt.bar(d,T,tick_label = ["Mercury","Venus","Earth","Mars","Jupyter","Saturn","Uranus","Neplt.xlabel("Planet Name")
plt.ylabel("Length of day (in earth days)")
plt.title("Length of day for planets in our solar system")
```

Text(0.5, 1.0, 'Length of day for planets in our solar system')



Notice the optional argument tick\_labels used to add labels to the bars. If that were left off, the bars would be labeled using the numbers supplied. Other optional arguments that are available for the bar command are given below.

Table 14.6: A Few Common bar keyword arguments

Argument	Description
width	bar width
color	bar color
xerr	X error bar
yerr	Y error bar
capsize	size of caps on error bars

### 14.2.3 Errorbar Plots

To make plots with error bars use matplotlilb's errorbar function. You can choose to add error bars on the x or y axis using the keyword arguments xerr and yerr.

from matplotlib import pyplot as plt

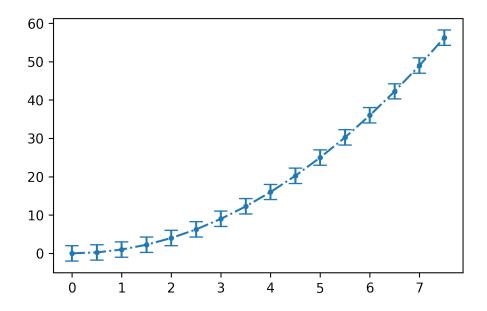
```
from numpy import arange

x = arange(0,8,0.5)
y = x**2

x_err = 0.05 # Same error for all points
y_error = 2 # Different error for each point

plt.errorbar(x,y,linestyle = '-.', marker = 'o',markersize = 3,yerr=y_error,capsize = 5)
```

<ErrorbarContainer object of 3 artists>



The linestyle, marker, and markersize arguments work with this plot type also.

#### 14.2.4 Scatter Plots

We have already generated scatter plots using the plot function but you can also use the scatter command to do the same thing. The only other additional functionality with scatter is the ability to specify the color, shape, and size of each plot marker individually.

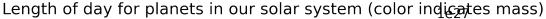
```
from matplotlib import pyplot as plt
%matplotlib inline
```

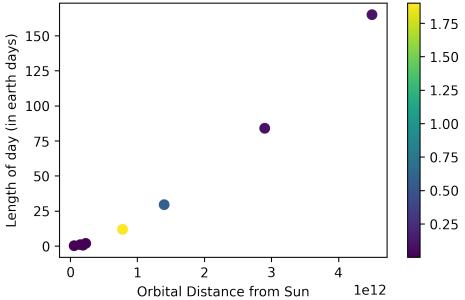
```
from numpy import linspace,log

d = [5.8e10,1.9e11,1.5e11,2.3e11,7.8e11,1.4e12,2.9e12,4.5e12]
#d = [1,2,3,4,5,6,7,8]
T = [0.241,0.615,1,1.88,11.9,29.5,84,165]
mass = [3.2e23,4.9e24,6e24,6.4e23,1.9e27,5.7e26,8.7e25,1e26]

plt.figure()
plt.scatter(d,T,c = mass,s= 50)
plt.xlabel("Orbital Distance from Sun")
plt.ylabel("Length of day (in earth days)")
plt.title("Length of day for planets in our solar system (color indicates mass)")
plt.colorbar()
```

<matplotlib.colorbar.Colorbar at 0x111d74c10>





### 14.2.5 Histograms

Histograms display bars representing the frequency of values in a given data set. Unlike bar plots, the width of the bar is meaningful since the each bar represents the number of x-values

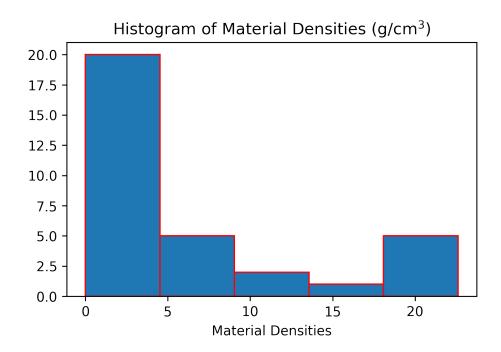
that fall within a range given by the width of the bar. A histogram can be constructed using the hist function. There is only one required argument, which is the data set. Some commonly used keyword arguments are bins which specifies how many equally-spaced groups (called *bins*) to generate and edgecolor which can be used to specify the color of the bar's edges.

```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace,log

densities = [0.00009,0.000178,0.00125,0.001251,0.001293,0.001977,0.534,0.810,0.900,0.920,0

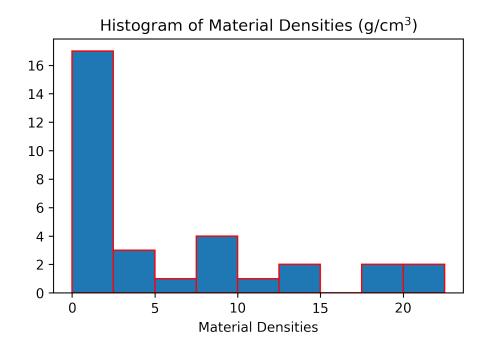
plt.figure()
plt.hist(densities,bins = 5,edgecolor = 'r')
plt.xlabel("Material Densities")
plt.title(r"Histogram of Material Densities (g/cm$^3$)")
```

Text(0.5, 1.0, 'Histogram of Material Densities (g/cm\$^3\$)')



Here we have used bins = 5 which will produce a histogram with 5 equal-size bins. Alternatively, we can specify the exact locations of all the bin edges by placing them in a list.

Text(0.5, 1.0, 'Histogram of Material Densities (g/cm\$^3\$)')



## 14.3 Multifigure Plots

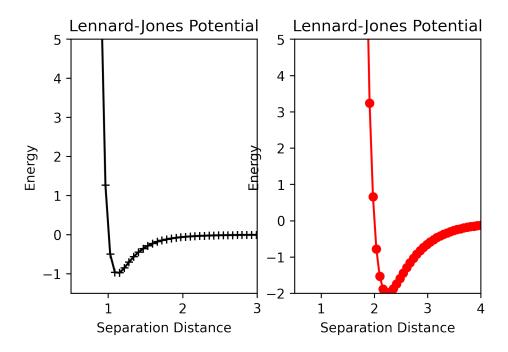
To generate multiple, independent plots in the same figure a few more lines of code are necessary to specify how you want the plots arranged. There are two general methods for doing that and we will demonstrate both of them. In the first method, you'll first use the figure() command to generate a figure and the subplot() function to generate the individual plots in the figure. The subplot function take three arguments.

```
subplot(rows,columns,plot_number)
```

As an example, to generate a figure of two plots side by side.

```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace, sqrt
r = linspace(0.9,4,50)
sigmaOne = 1
epsilonOne = 1
sigmaTwo = 2
epsilonTwo = 2
energyOne = 4 * sigmaOne* ((epsilonOne/r)**12 - (epsilonOne/r)**6)
energyTwo = 4 * sigmaTwo * ((epsilonTwo/r)**12 - (epsilonTwo/r)**6)
plt.figure()
plt.subplot(1,2,1)
plt.plot(r,energyOne,marker = '+',color = 'k')
plt.xlim(0.5,3.0)
plt.ylim(-1.5,5)
plt.xlabel("Separation Distance")
plt.ylabel("Energy")
plt.title("Lennard-Jones Potential")
plt.subplot(1,2,2)
plt.plot(r,energyTwo,marker = 'o',color = 'r')
plt.xlim(0.5,4.0)
plt.ylim(-2,5)
plt.xlabel("Separation Distance")
plt.ylabel("Energy")
plt.title("Lennard-Jones Potential")
```

Text(0.5, 1.0, 'Lennard-Jones Potential')



Pay close attention to the subplot function. subplot(1,2,1) will generate a 1 x 2 grid of plots and place the next plot generated at the 1st location. Below is an example of a more advanced array of plots. Pay close attention to the subplot functions until you understand.

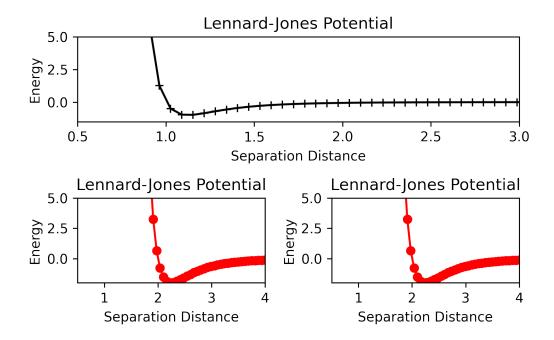
```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace,sqrt

r = linspace(0.9,4,50)

sigmaOne = 1
epsilonOne = 1
sigmaTwo = 2
epsilonTwo = 2
energyOne = 4 * sigmaOne* ((epsilonOne/r)**12 - (epsilonOne/r)**6)
energyTwo = 4 * sigmaTwo * ((epsilonTwo/r)**12 - (epsilonTwo/r)**6)

plt.figure()
plt.subplot(2,1,1)
plt.plot(r,energyOne,marker = '+',color = 'k')
plt.xlim(0.5,3.0)
plt.ylim(-1.5,5)
```

```
plt.xlabel("Separation Distance")
plt.ylabel("Energy")
plt.title("Lennard-Jones Potential")
plt.subplot(2,2,3)
plt.plot(r,energyTwo,marker = 'o',color = 'r')
plt.xlim(0.5,4.0)
plt.ylim(-2,5)
plt.xlabel("Separation Distance")
plt.ylabel("Energy")
plt.title("Lennard-Jones Potential")
plt.subplot(2,2,4)
plt.plot(r,energyTwo,marker = 'o',color = 'r')
plt.xlim(0.5,4.0)
plt.ylim(-2,5)
plt.xlabel("Separation Distance")
plt.ylabel("Energy")
plt.title("Lennard-Jones Potential")
plt.tight_layout()
```

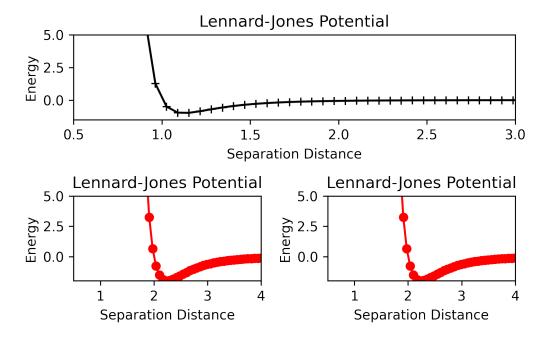


The other method for generating an array of plots is similar to the first but different functions are used and a little more control over the plots is gained. In this approach, functions to explicitly creates and links subplots, called *axes* are used. Just as before, the figure function is

used to generate the overall figure. The create each subplot, the add\_subplot(rows,columns, plot\_number) function is used. The arguments to this function are the same as for subplot in the previous method. After the plot object has been created, we can call the plot function again, but this time preceded by the axes object that you just created. Here is an example.

```
from matplotlib import pyplot as plt
%matplotlib inline
from numpy import linspace, sqrt
r = linspace(0.9, 4, 50)
sigmaOne = 1
epsilonOne = 1
sigmaTwo = 2
epsilonTwo = 2
energyOne = \frac{4}{3} * sigmaOne* ((epsilonOne/r)**12 - (epsilonOne/r)**6)
energyTwo = 4 * sigmaTwo * ((epsilonTwo/r)**12 - (epsilonTwo/r)**6)
fig = plt.figure()
ax1 = fig.add_subplot(2,1,1)
ax1.plot(r,energyOne,marker = '+',color = 'k')
ax1.set_xlim(0.5,3.0)
ax1.set_ylim(-1.5,5)
ax1.set_xlabel("Separation Distance")
ax1.set_ylabel("Energy")
ax1.set_title("Lennard-Jones Potential")
ax2= fig.add_subplot(2,2,3)
ax2.plot(r,energyTwo,marker = 'o',color = 'r')
ax2.set_xlim(0.5,4.0)
ax2.set ylim(-2,5)
ax2.set_xlabel("Separation Distance")
ax2.set_ylabel("Energy")
ax2.set_title("Lennard-Jones Potential")
ax3 = fig.add_subplot(2,2,4)
ax3.plot(r,energyTwo,marker = 'o',color = 'r')
ax3.set_xlim(0.5,4.0)
ax3.set_ylim(-2,5)
ax3.set xlabel("Separation Distance")
ax3.set_ylabel("Energy")
ax3.set_title("Lennard-Jones Potential")
```

### plt.tight\_layout()



Notice the set\_xlim, set\_ylim, set\_xlabel etc methods that were used to customize each individual plot. There are a host of other methods available for further customization. This website has a comprehensive list of them.