

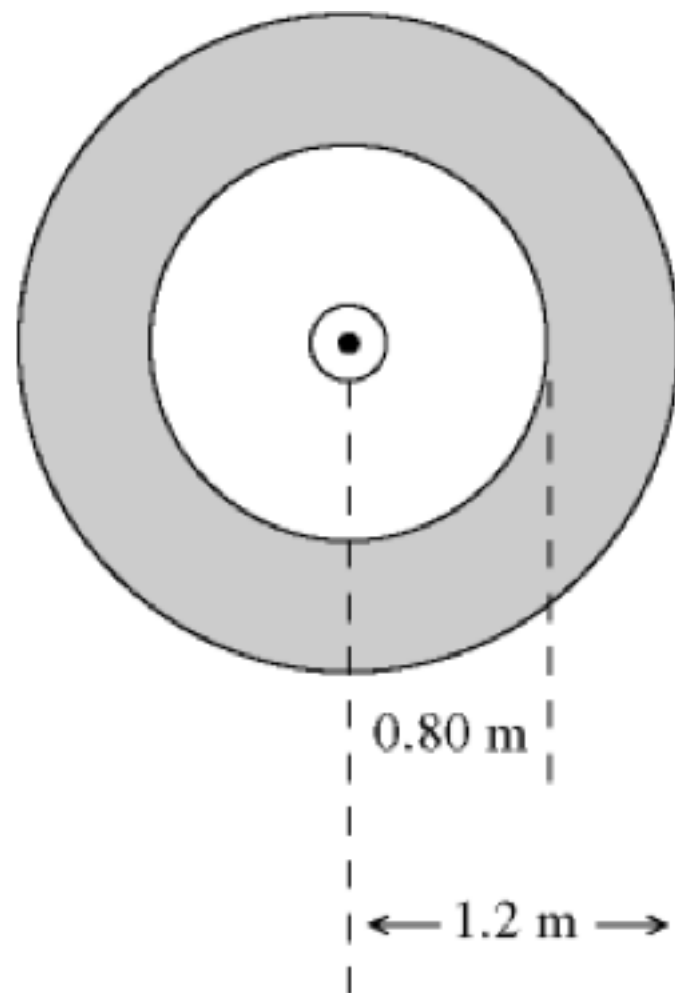


PH 220

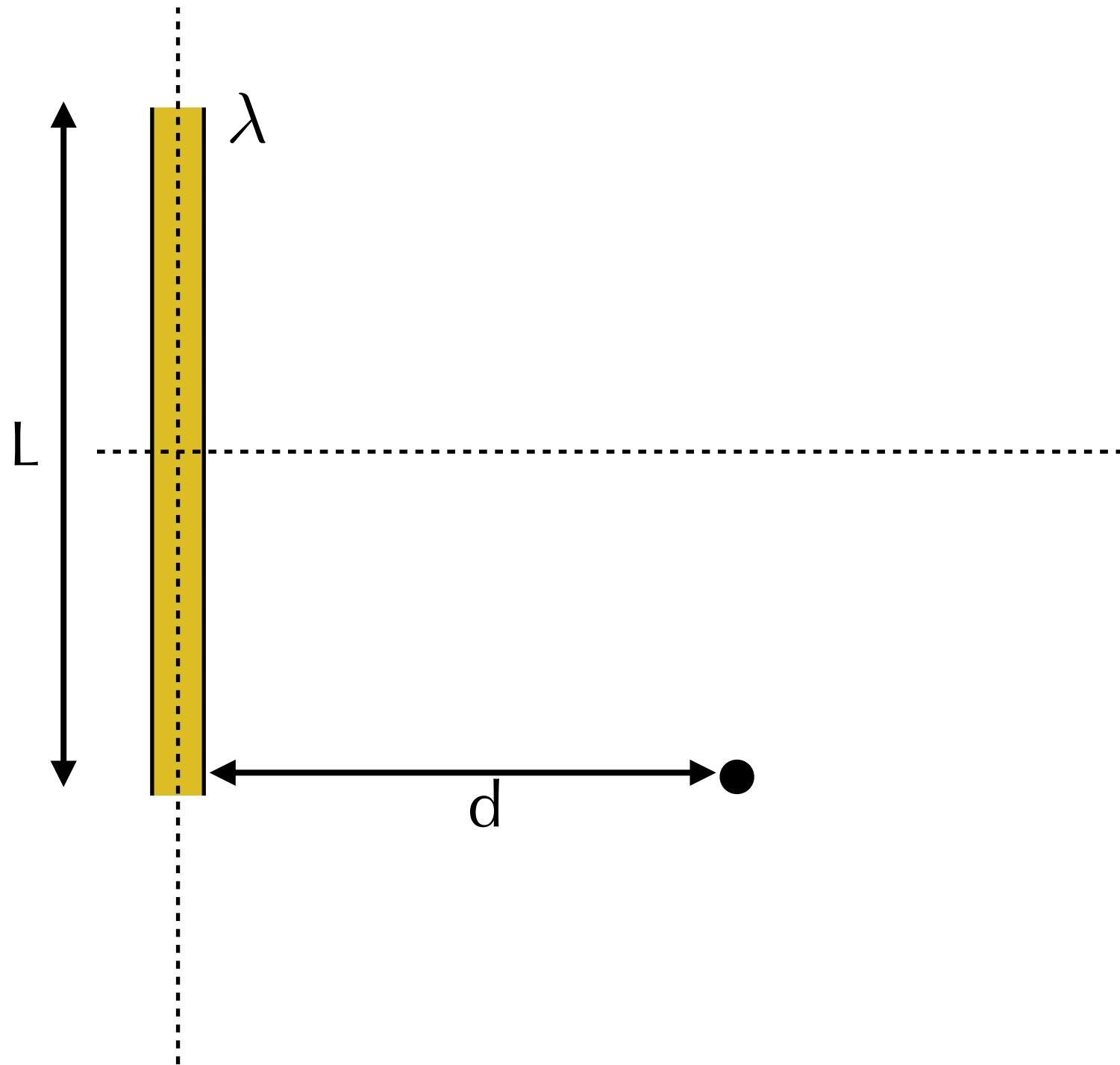
Lance Nelson



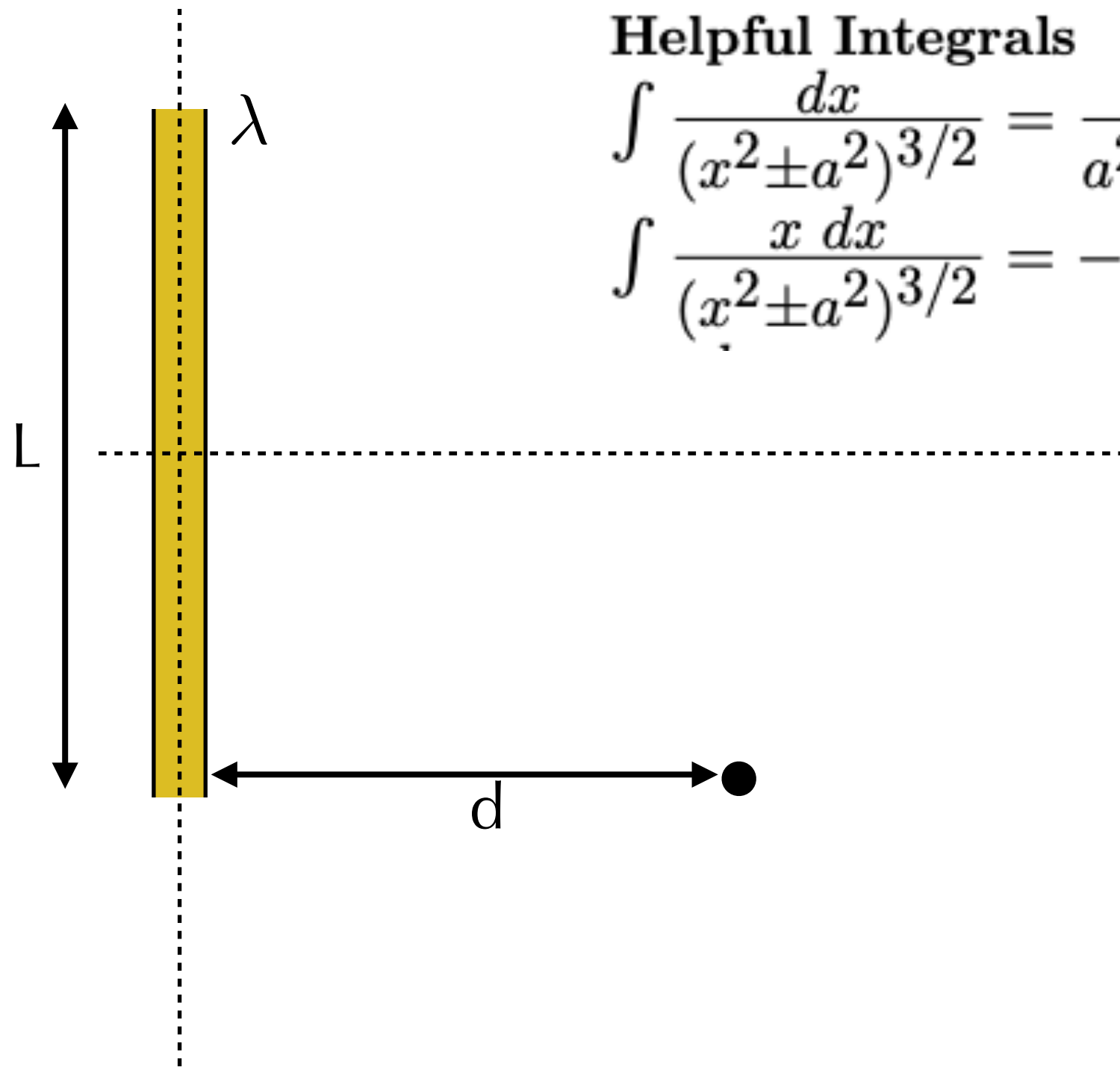
# Gauss's Law Practice



# E-Field Integration Practice



# E-Field Integration Practice



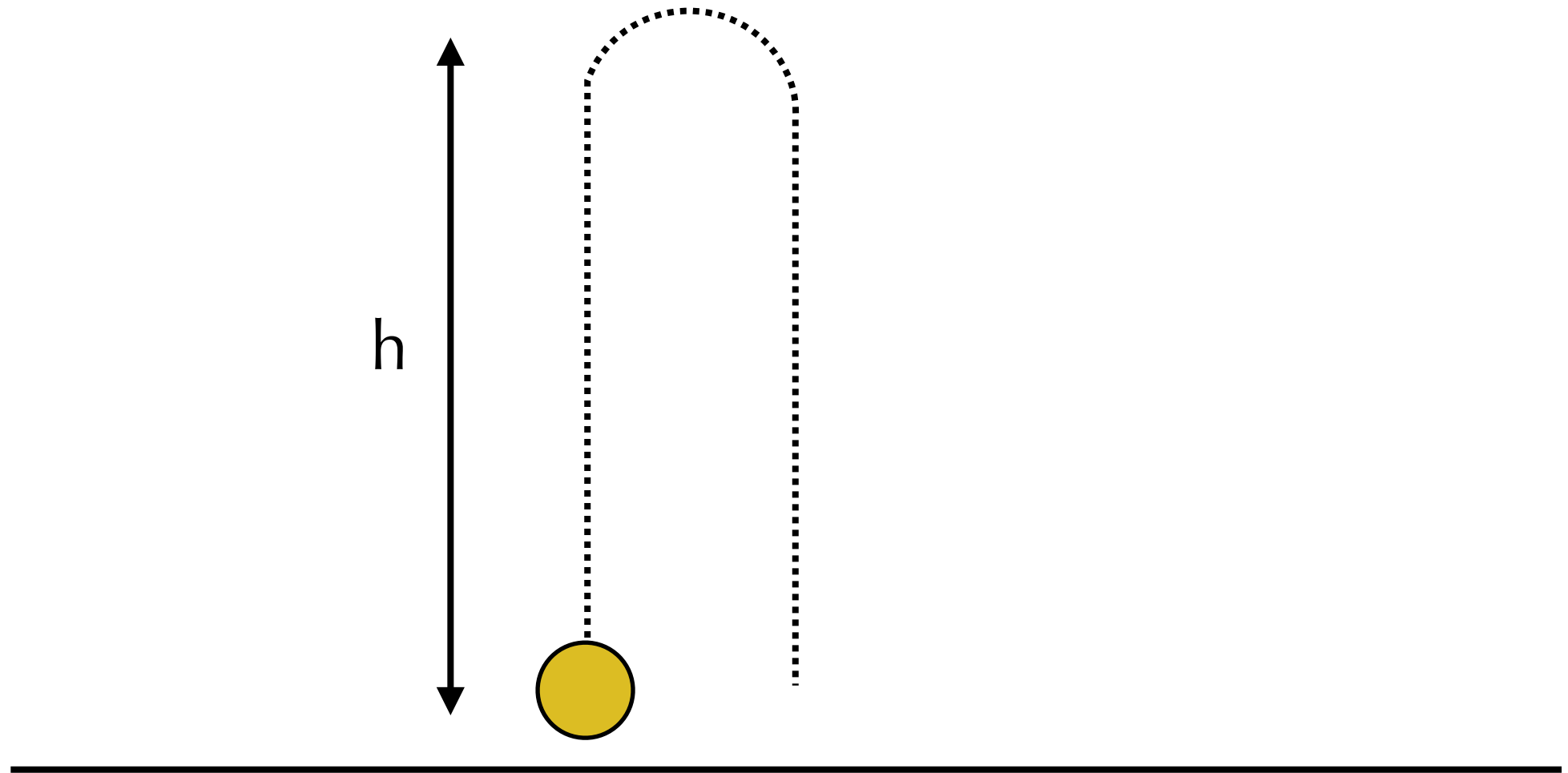
## Helpful Integrals

$$\int \frac{dx}{(x^2 \pm a^2)^{3/2}} = \frac{\pm x}{a^2 \sqrt{a^2 + x^2}}$$

$$\int \frac{x dx}{(x^2 \pm a^2)^{3/2}} = -\frac{1}{\sqrt{x^2 \pm a^2}}$$

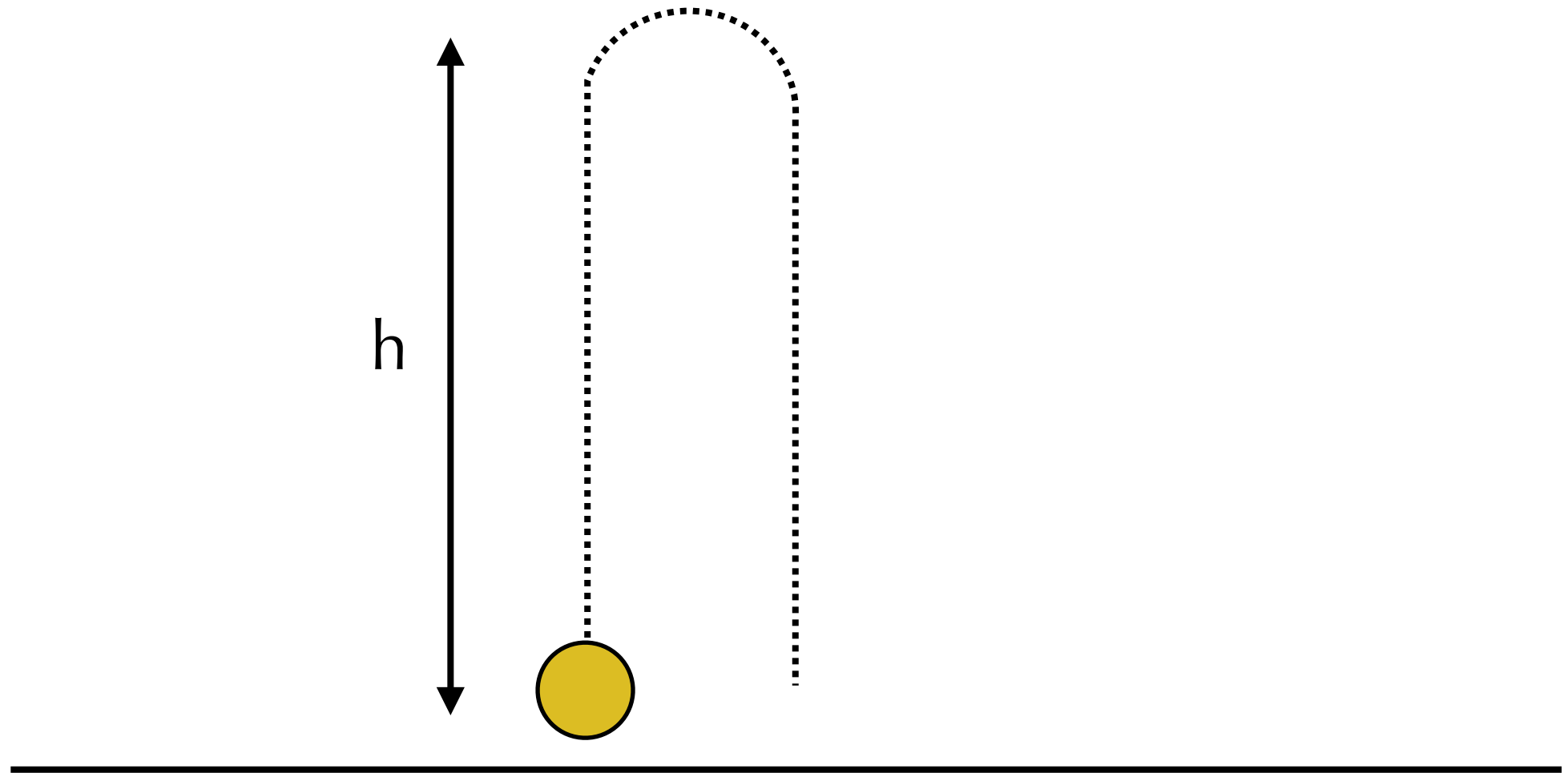
# Refresher on Work-Energy

Calculate the work done by gravity as the ball travels from the ground to the peak of its motion.



# Refresher on Work-Energy

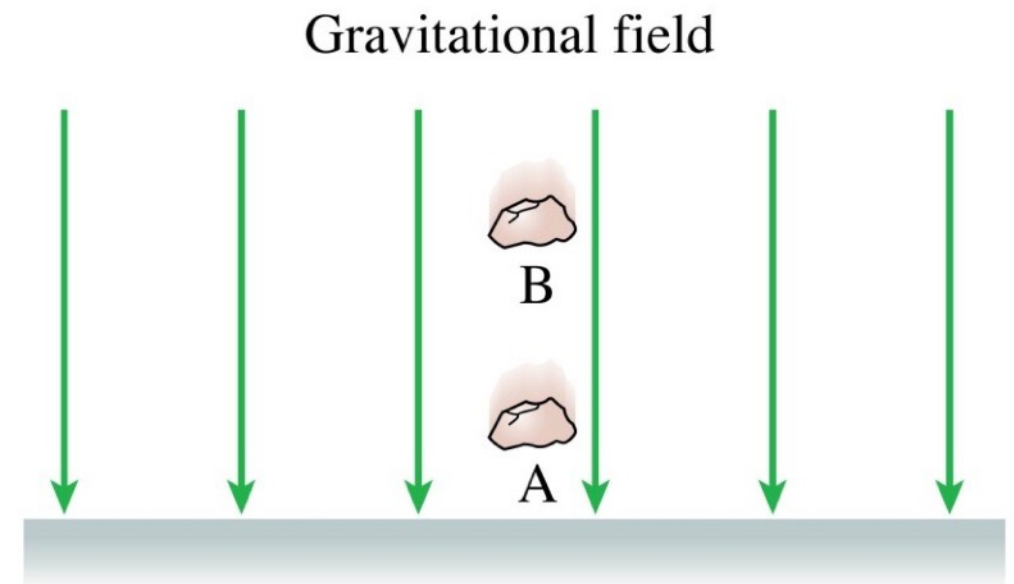
Calculate the work done by gravity as the ball travels from the ground to the peak of its motion.

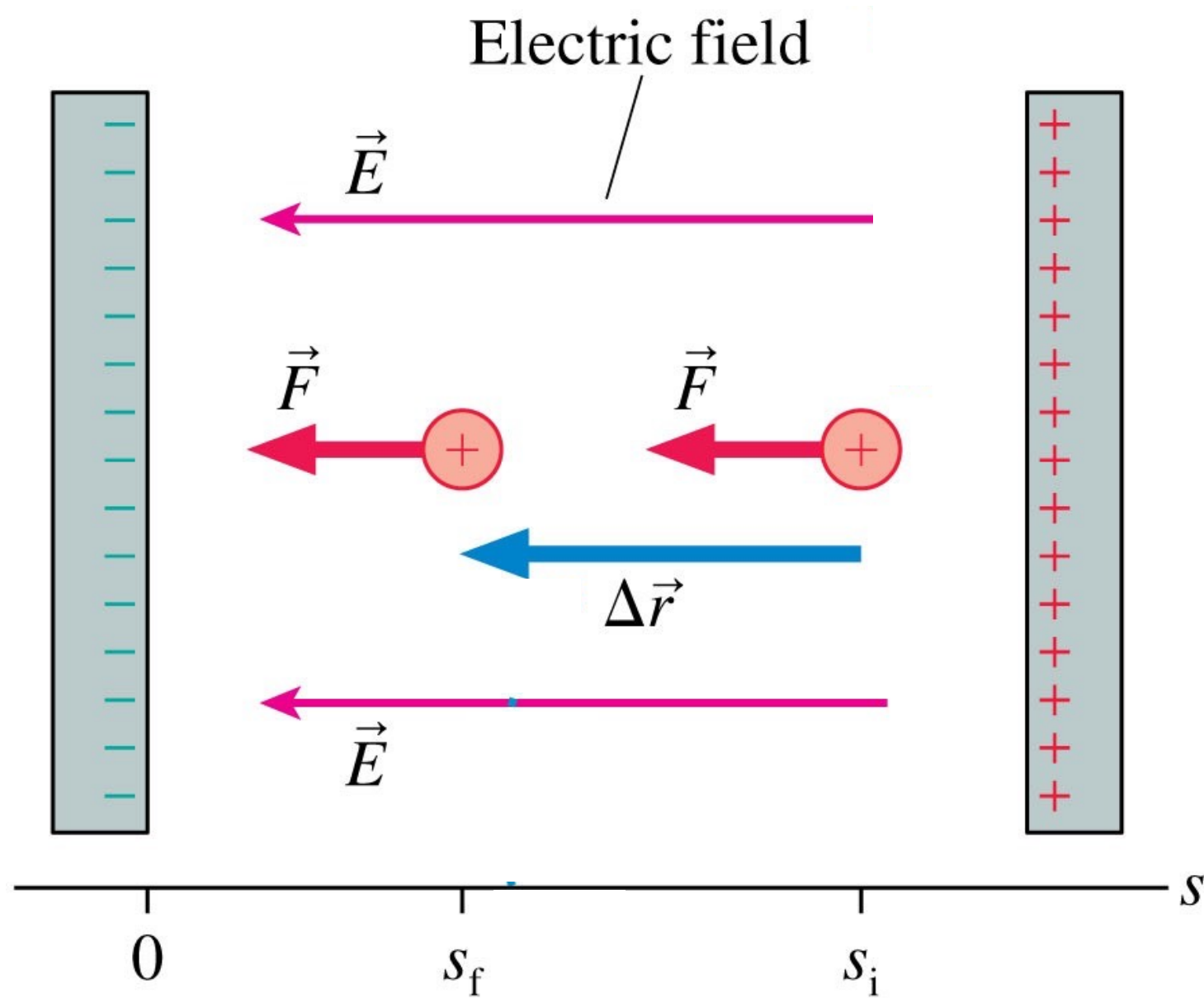


$$\Delta U_g = -W_g$$

Two rocks have equal mass.  
Which has more gravitational  
potential energy?

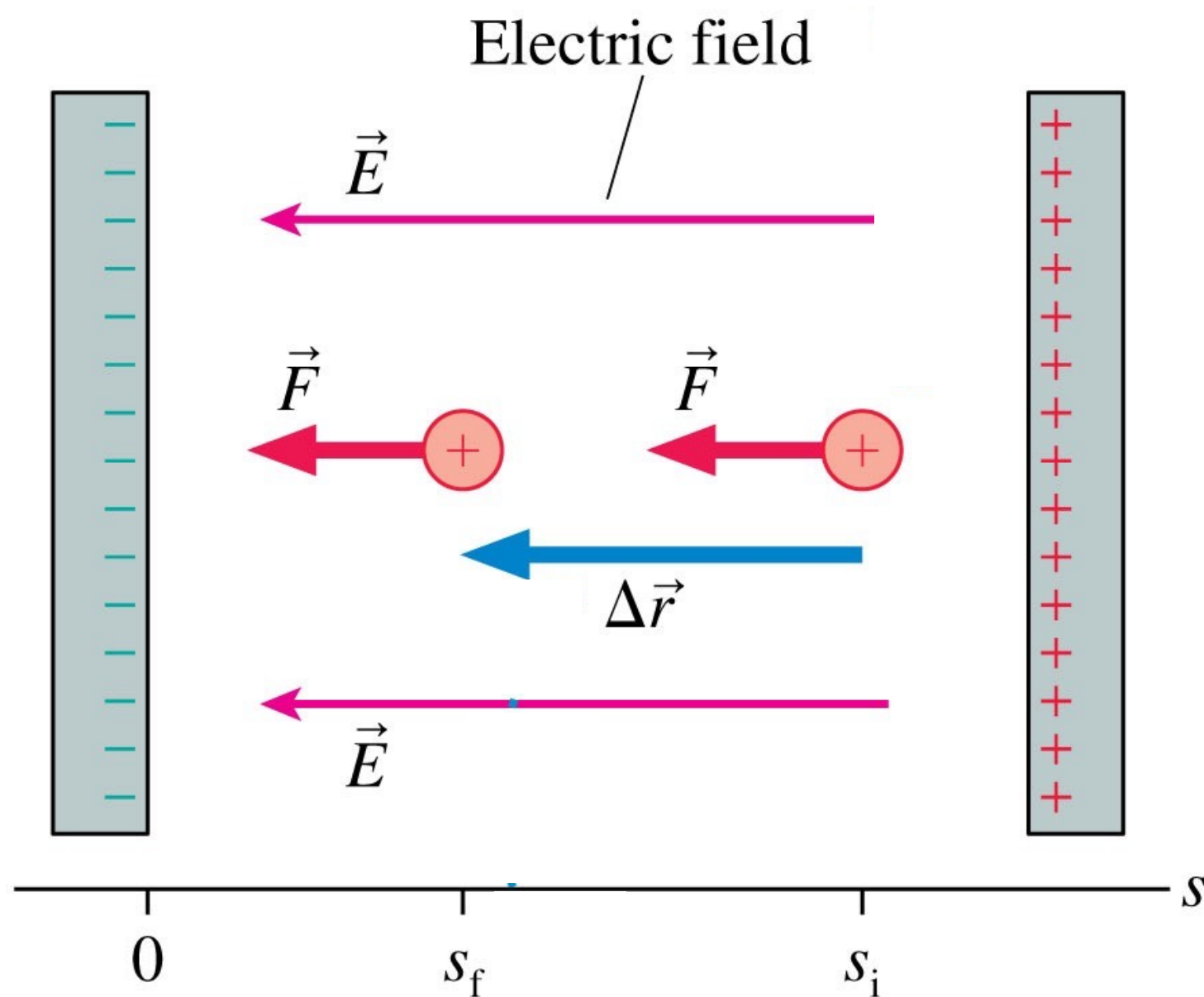
- A. Rock A.
- B. Rock B.
- C. They have the same potential energy.
- D. Both have zero potential energy.





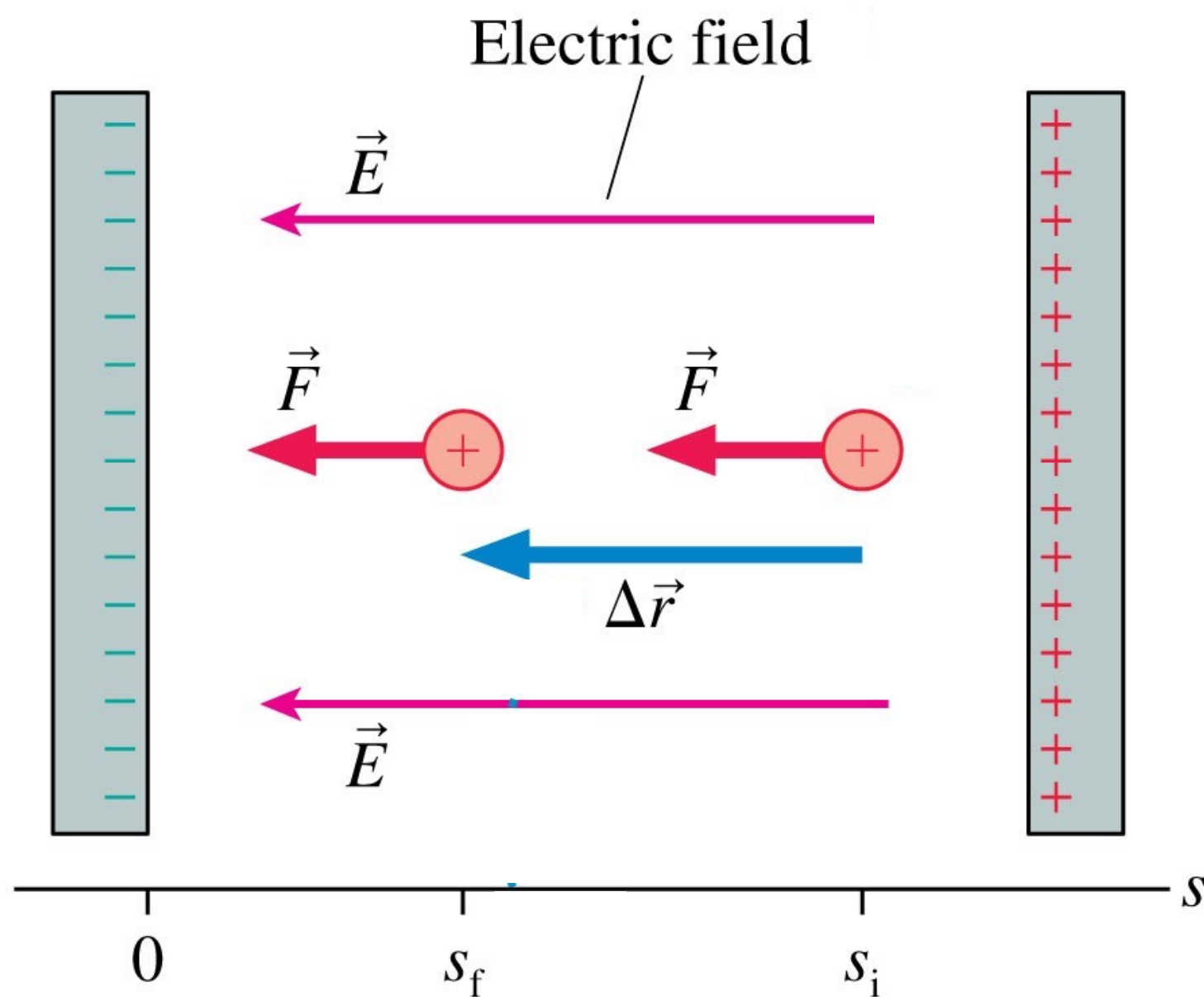
Calculate the work done on the proton!





Calculate the work done on the proton!

$$W = Eq\Delta r$$



Calculate the work done on the proton!

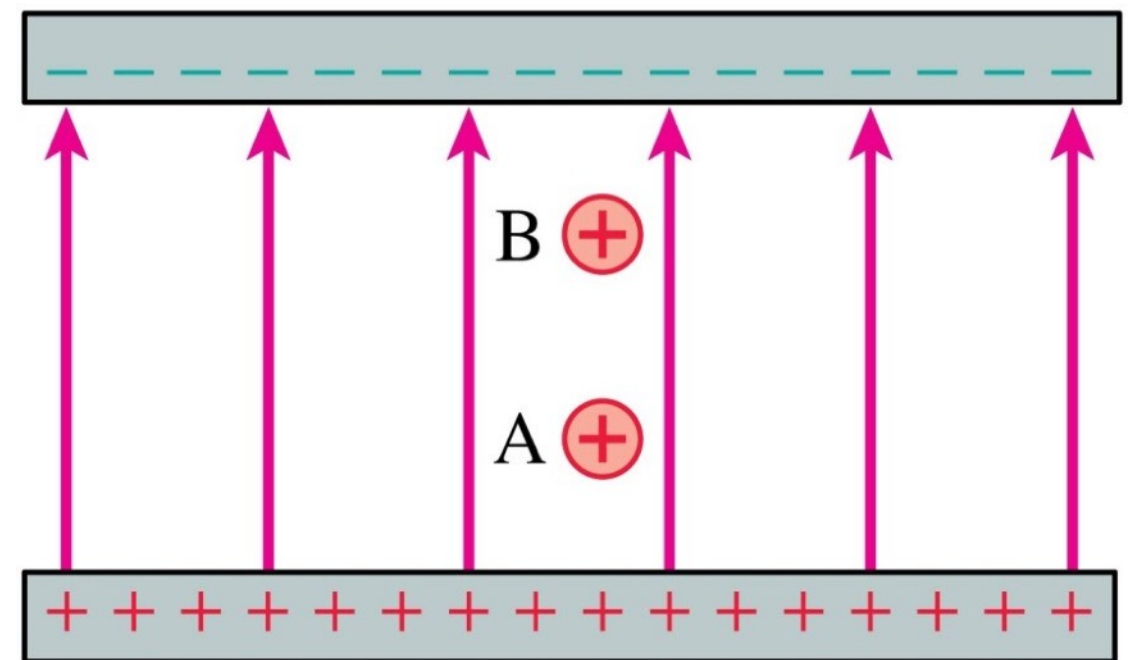
$$W = Eq\Delta r$$

$$\Delta U_{\text{elec}} = -W_{\text{elec}}$$

Two positive charges are equal. Which has more electric potential energy?

**Question #43**

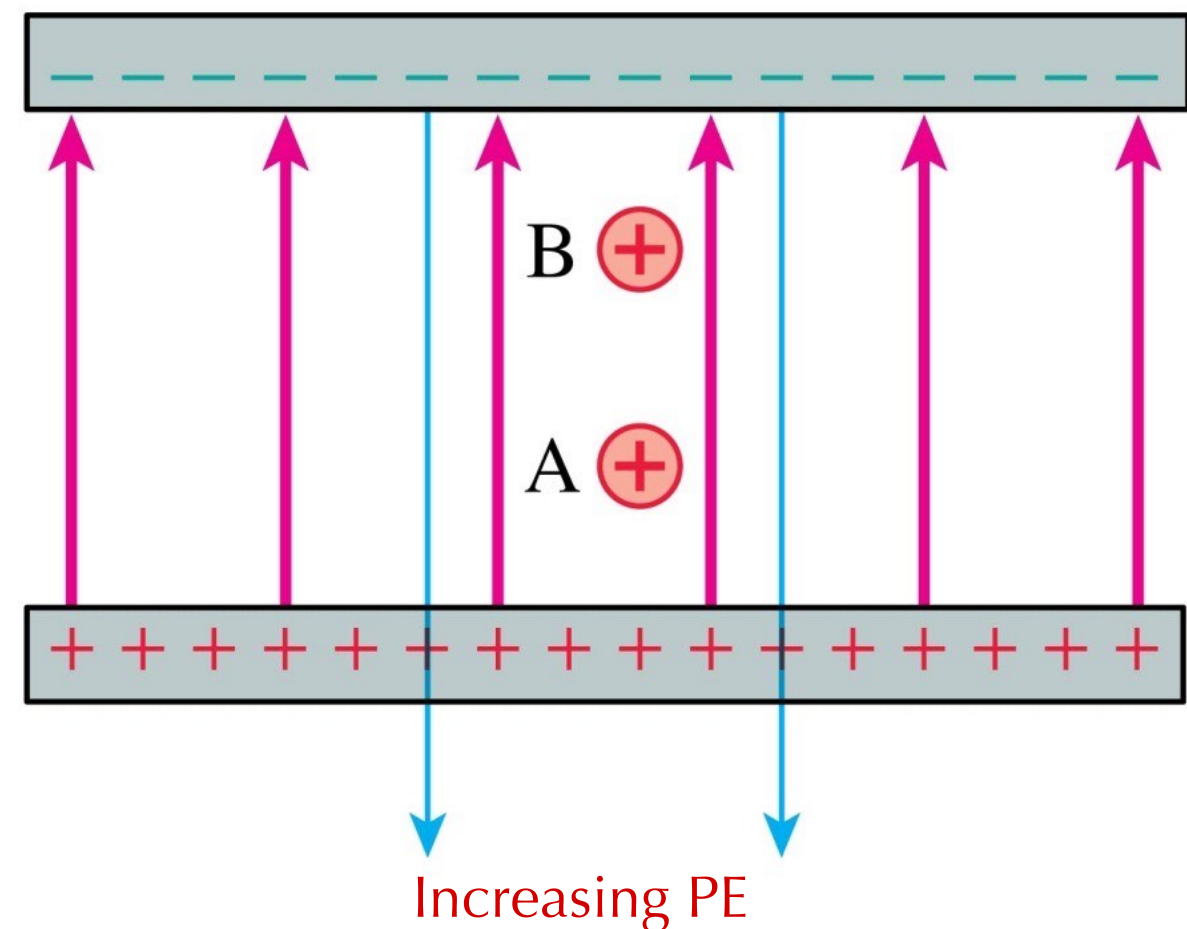
- B. Charge B.
- C. They have the same potential energy.
- D. Both have zero potential energy.
- E. Charge A.



Two positive charges are equal. Which has more electric potential energy?

### Question #43

- B. Charge B.
- C. They have the same potential energy.
- D. Both have zero potential energy.
- E. Charge A.

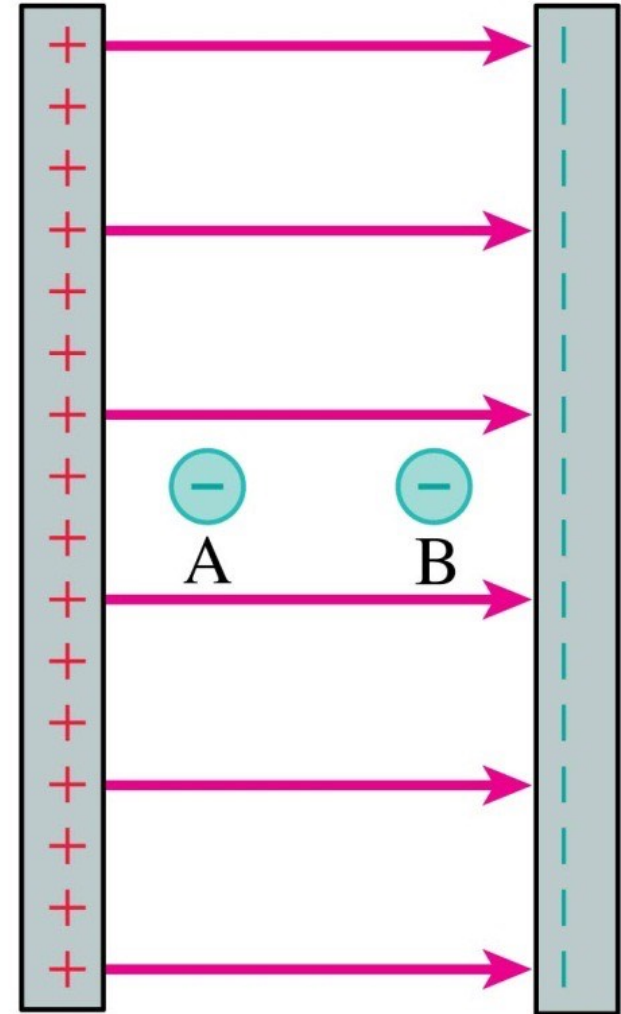




## Question #44

Two negative charges are equal. Which has more electric potential energy?

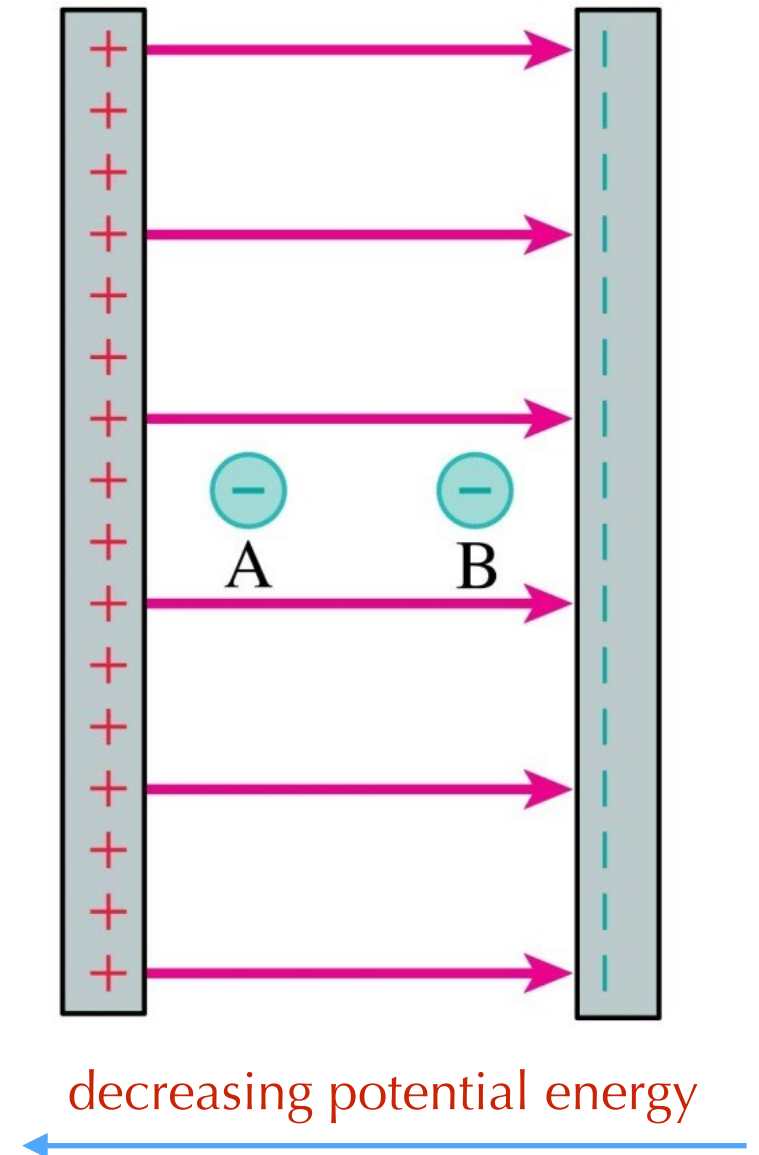
- A. Charge A.
- B. They have the same potential energy.
- D. Both have zero potential energy.
- E. Charge B.



## Question #44

Two negative charges are equal. Which has more electric potential energy?

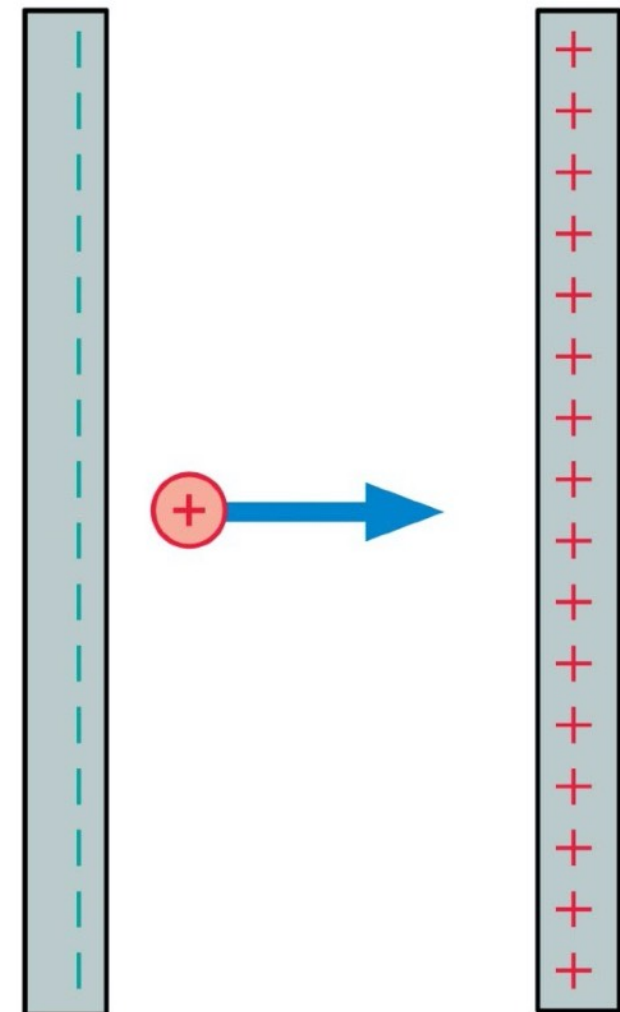
- A. Charge A.
- B. They have the same potential energy.
- D. Both have zero potential energy.
- E. Charge B.



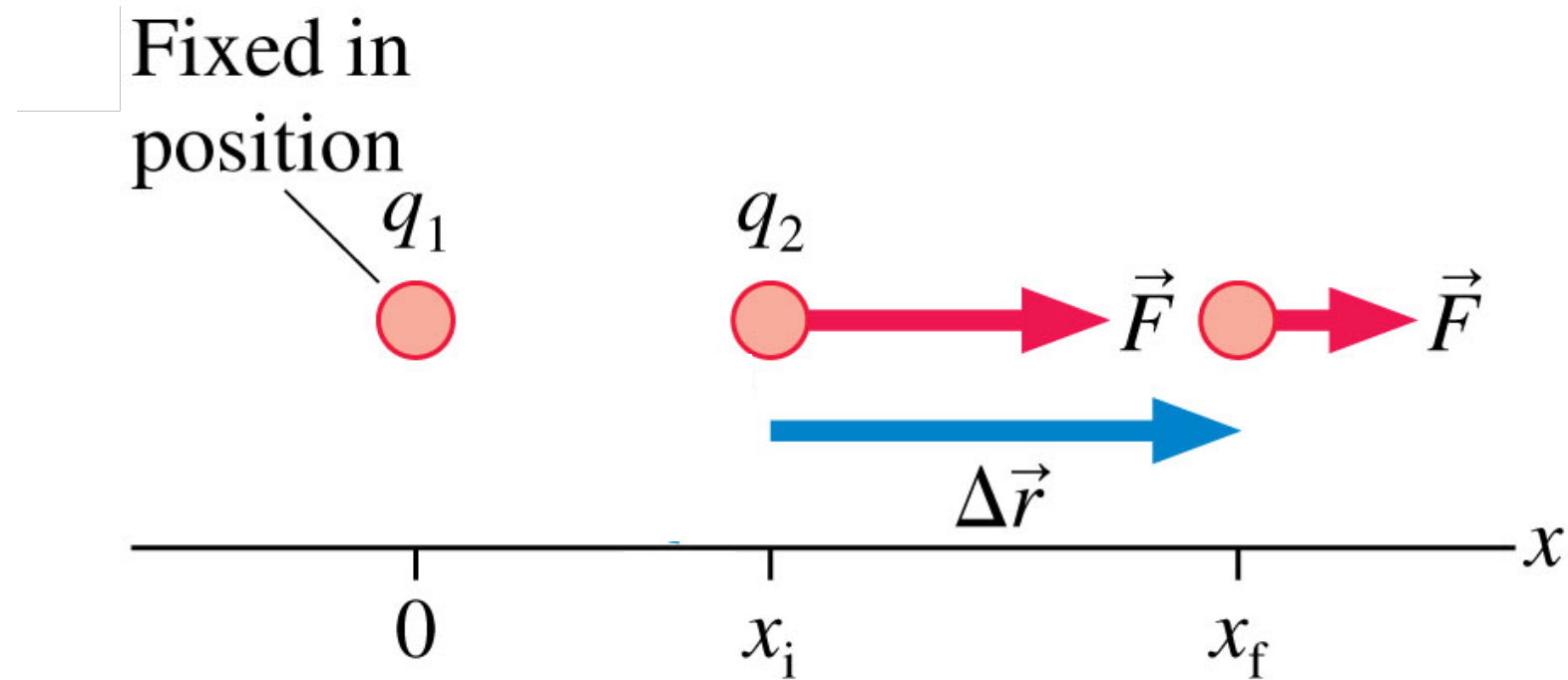
## Question #45

A positive charge moves as shown. Its kinetic energy

- A. Increases.
- B. Decreases.
- C. Remains constant.

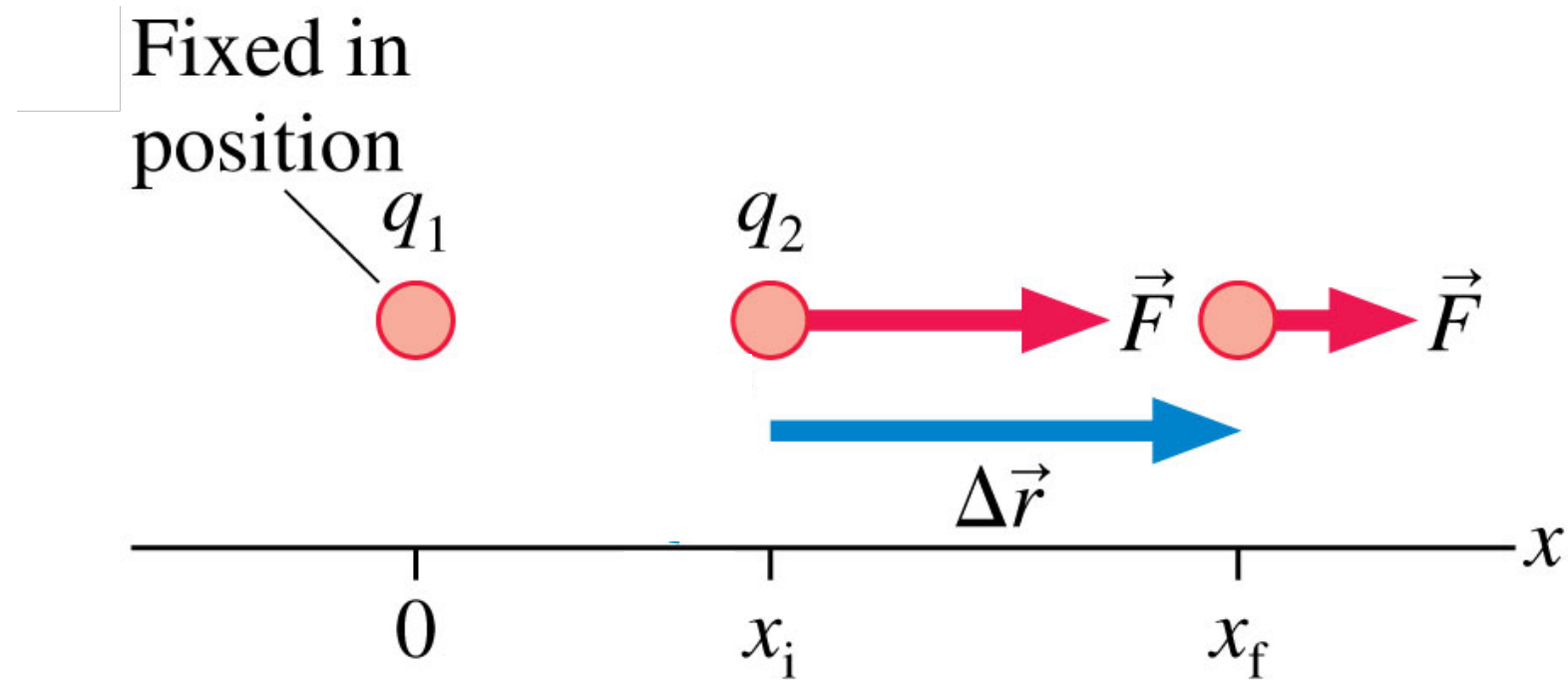


Calculate the work that  $q_1$  does on  $q_2$  as it moves from  $x_i$  to  $x_f$



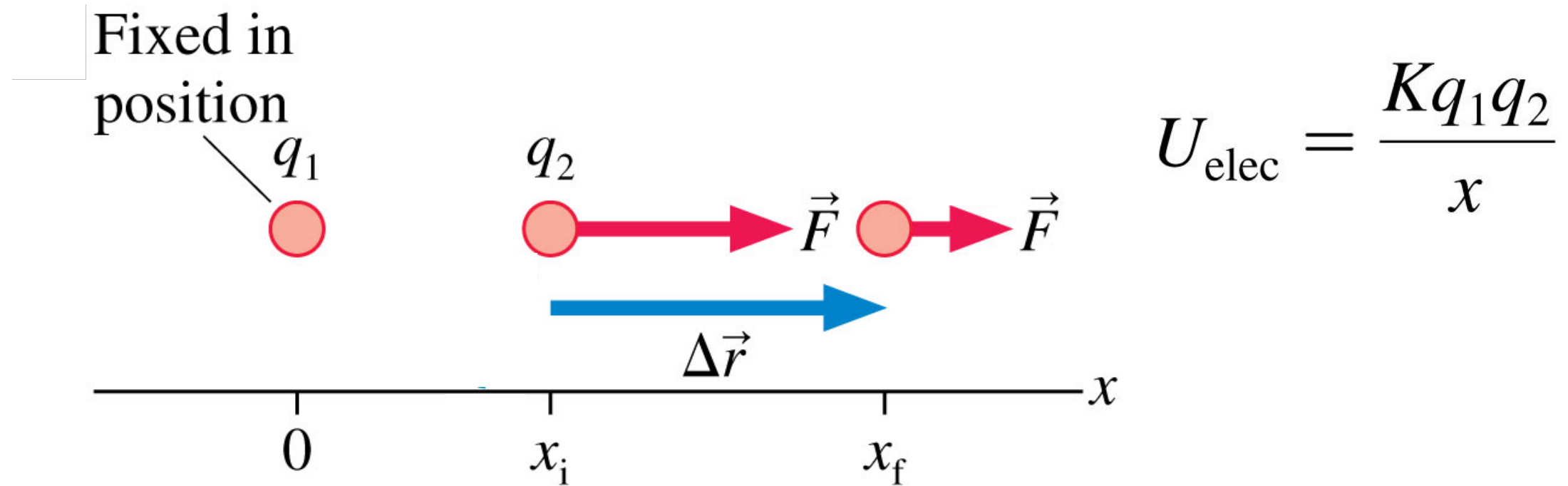


Calculate the work that  $q_1$  does on  $q_2$  as it moves from  $x_i$  to  $x_f$



$$W_{\text{elec}} = \int_{x_i}^{x_f} F_{1 \text{ on } 2} dx = \int_{x_i}^{x_f} \frac{Kq_1q_2}{x^2} dx = Kq_1q_2 \left. \frac{-1}{x} \right|_{x_i}^{x_f} = -\frac{Kq_1q_2}{x_f} + \frac{Kq_1q_2}{x_i}$$

Calculate the work that  $q_1$  does on  $q_2$  as it moves from  $x_i$  to  $x_f$

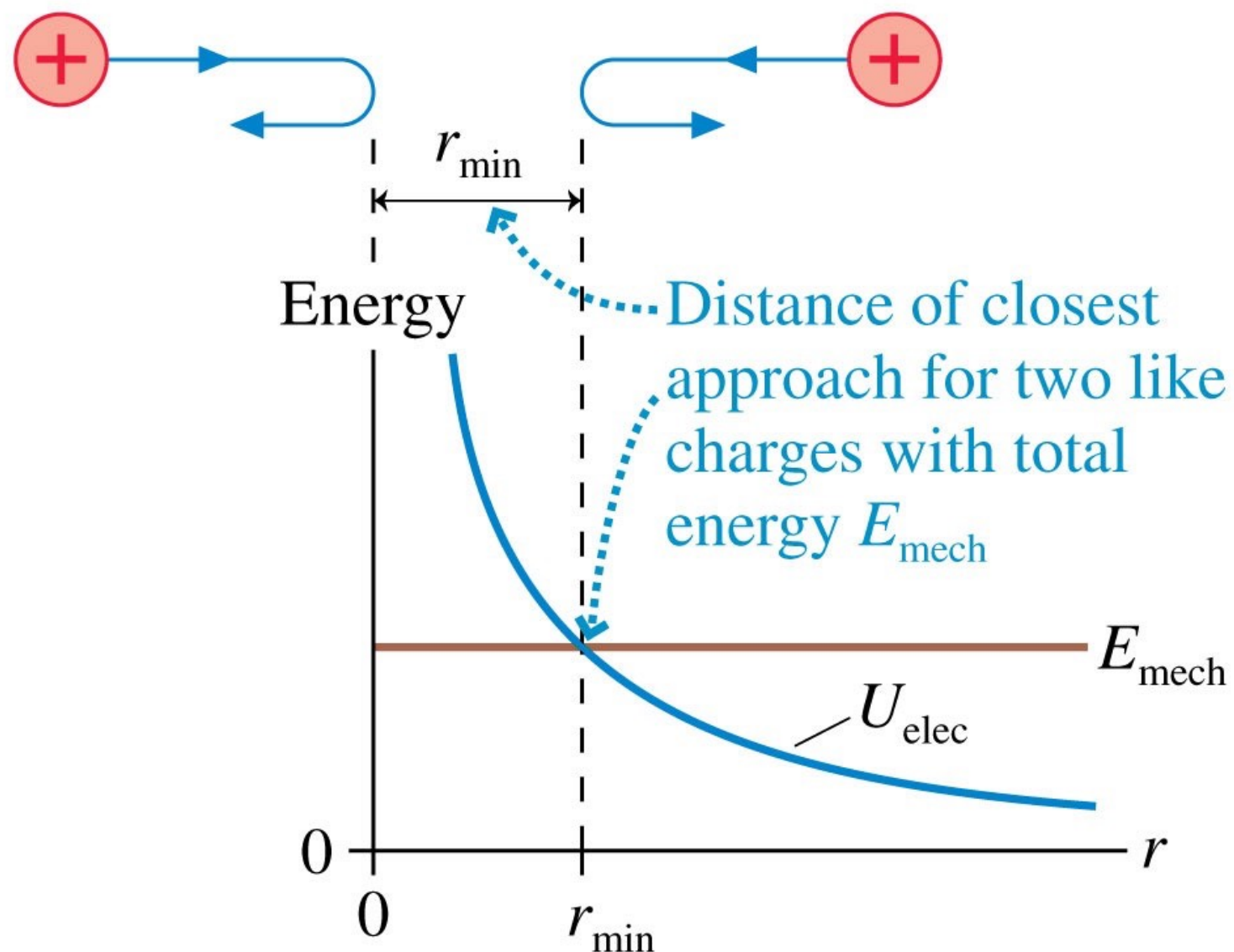


$$W_{\text{elec}} = \int_{x_i}^{x_f} F_{1 \text{ on } 2} dx = \int_{x_i}^{x_f} \frac{Kq_1q_2}{x^2} dx = Kq_1q_2 \left. \frac{-1}{x} \right|_{x_i}^{x_f} = -\frac{Kq_1q_2}{x_f} + \frac{Kq_1q_2}{x_i}$$

Two protons are given initial velocities towards each other. In terms of energy, describe the motion.



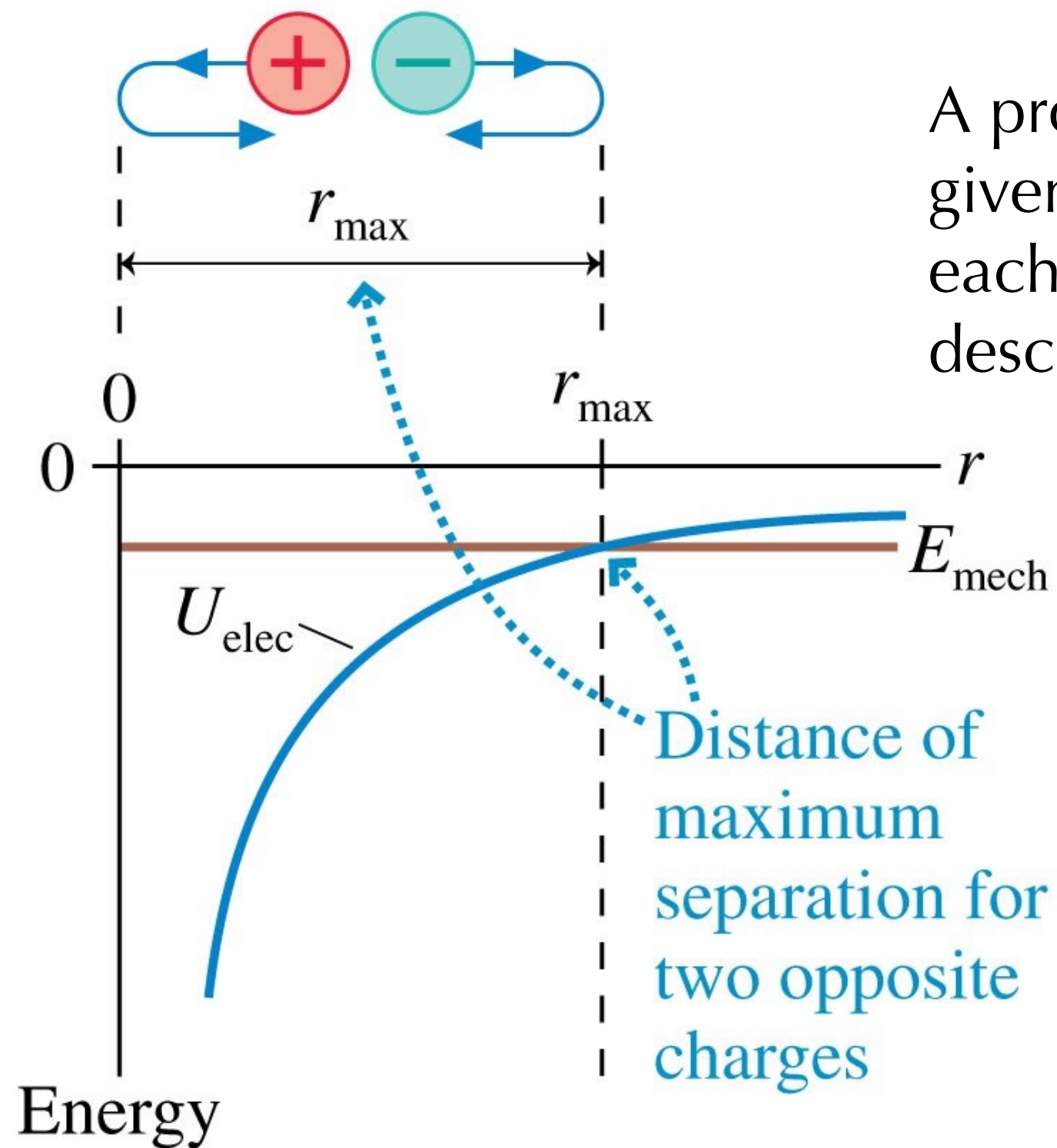
Two protons are given initial velocities towards each other. In terms of energy, describe the motion.







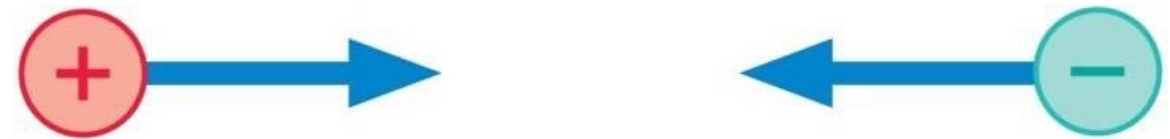
A proton and an electron are given initial velocities away from each other. In terms of energy, describe their motion.



A proton and an electron are given initial velocities away from each other. In terms of energy, describe their motion.

## Question #46

A positive and a negative charge are released from rest in vacuum. They move toward each other. As they do:



- A. A positive potential energy becomes more positive.
- B. A positive potential energy becomes less positive.
- C. A negative potential energy becomes more negative.
- D. A negative potential energy becomes less negative.
- E. A positive potential energy becomes a negative potential energy.

## Question #46

$$U_{\text{elec}} = \frac{Kq_1q_2}{r}$$

Opposite signs, so  $U$  is Negative.

$U$  increases in magnitude as  $r$  decreases.

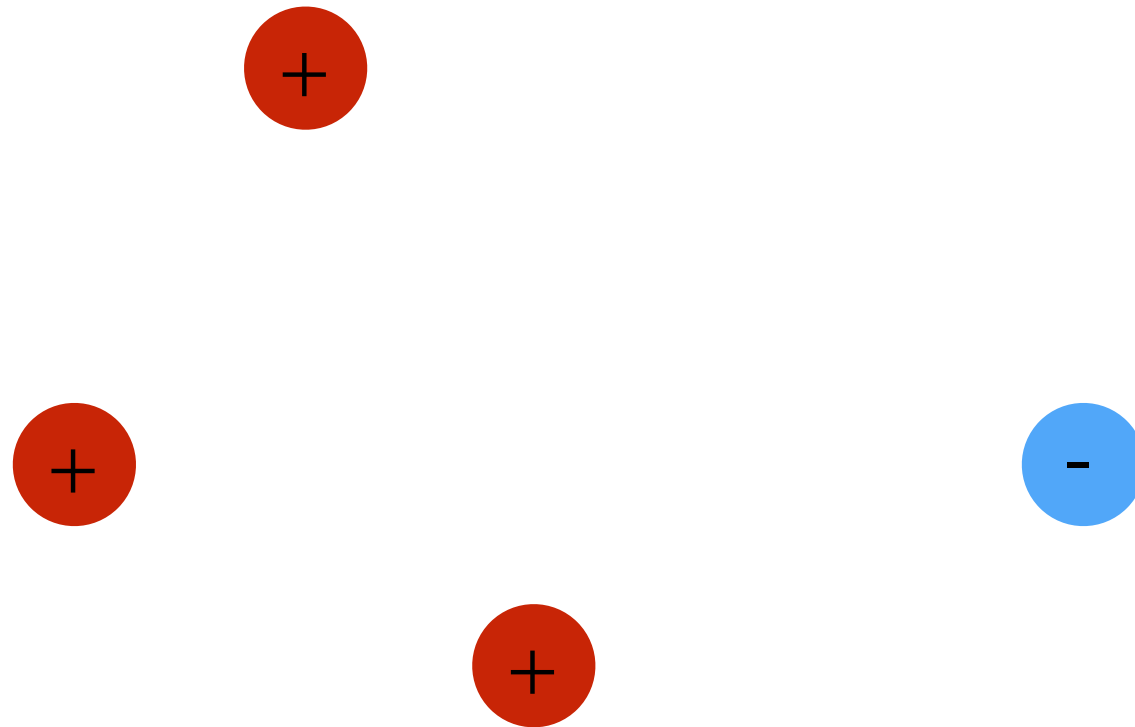
A positive and a negative charge are released from rest in vacuum. They move toward each other. As they do:



- A. A positive potential energy becomes more positive.
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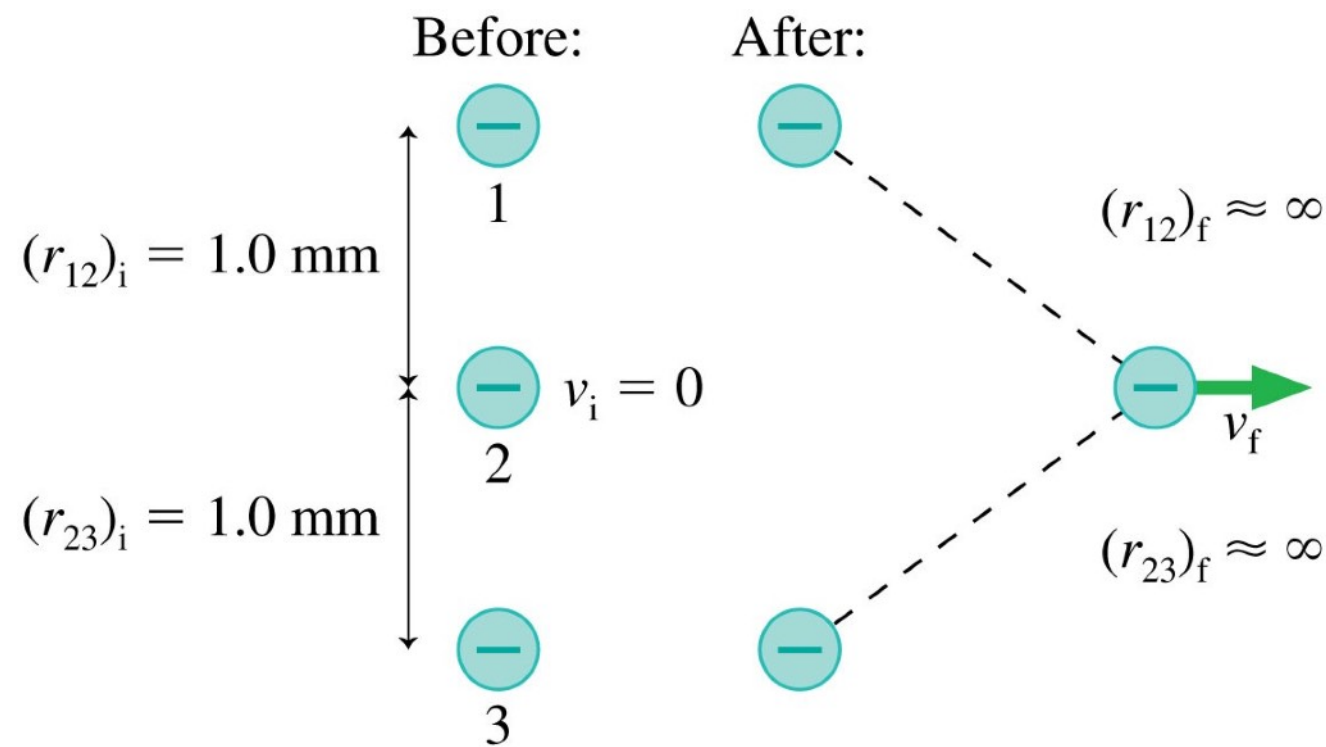
What if there are more than just two charges?



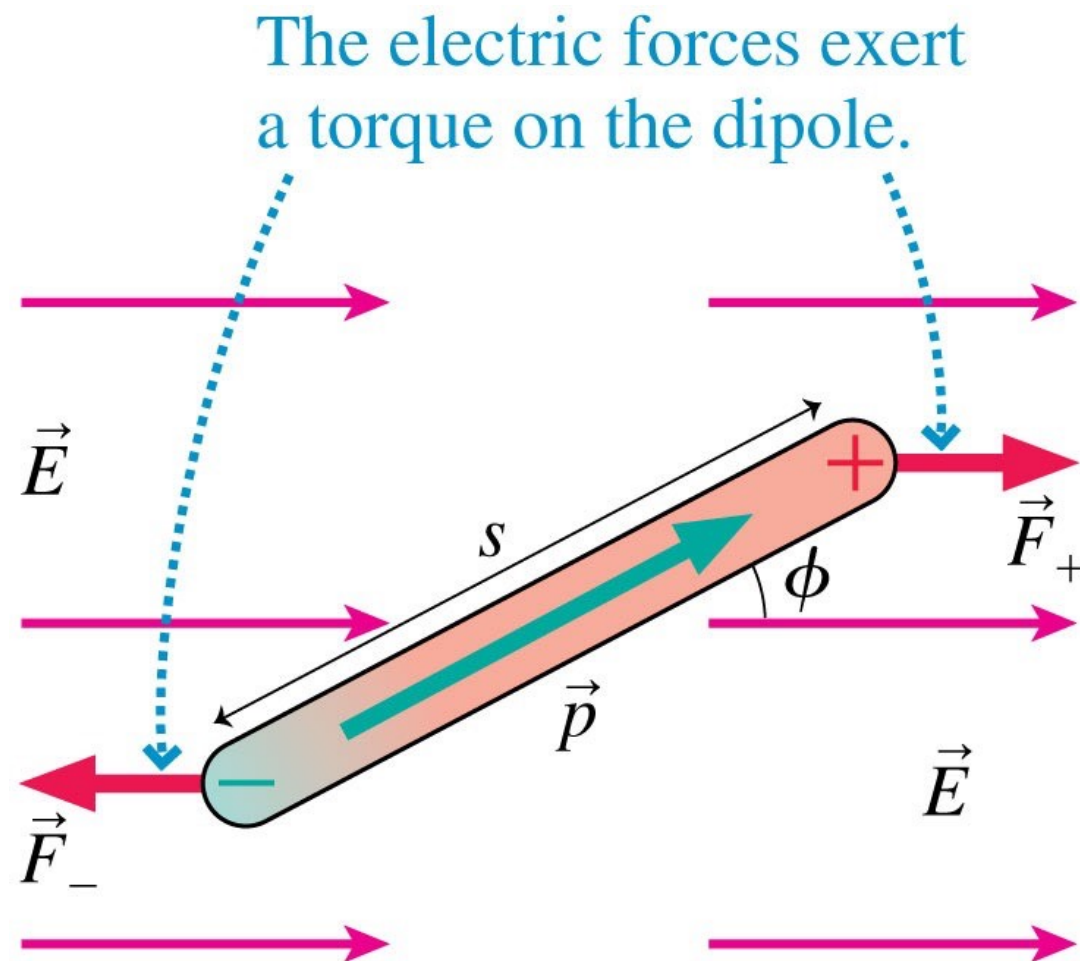
$$U = \sum_{i \neq j} \frac{kq_i q_j}{r_{ij}}$$

# Example

Three electrons are spaced 1.0 mm apart on a vertical line. If the center electron is nudged horizontally by a very small distance, what will its speed be when it is very far away?



# Potential Energy of a dipole in a uniform field



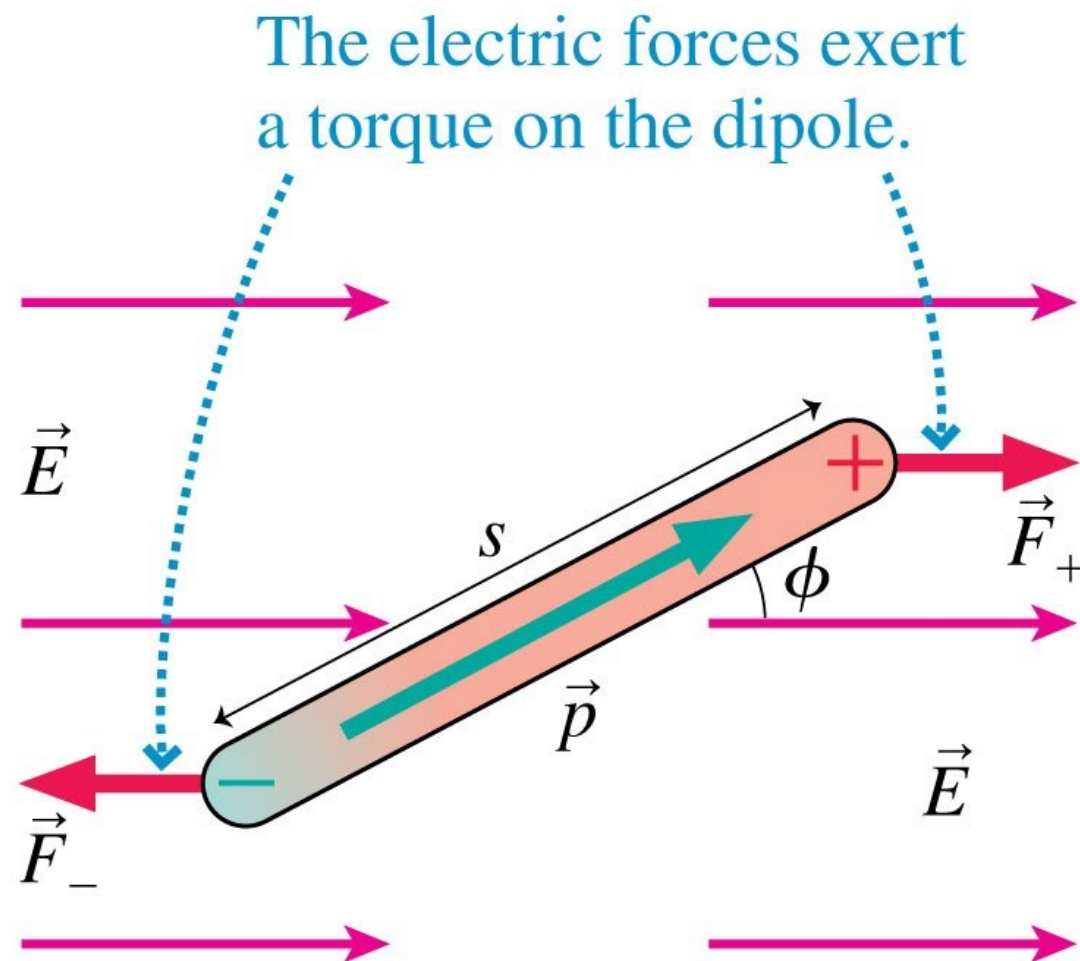
linear motion

$$dW = F_s ds$$

rotational motion

$$dW = \tau d\phi$$

# Potential Energy of a dipole in a uniform field



linear motion

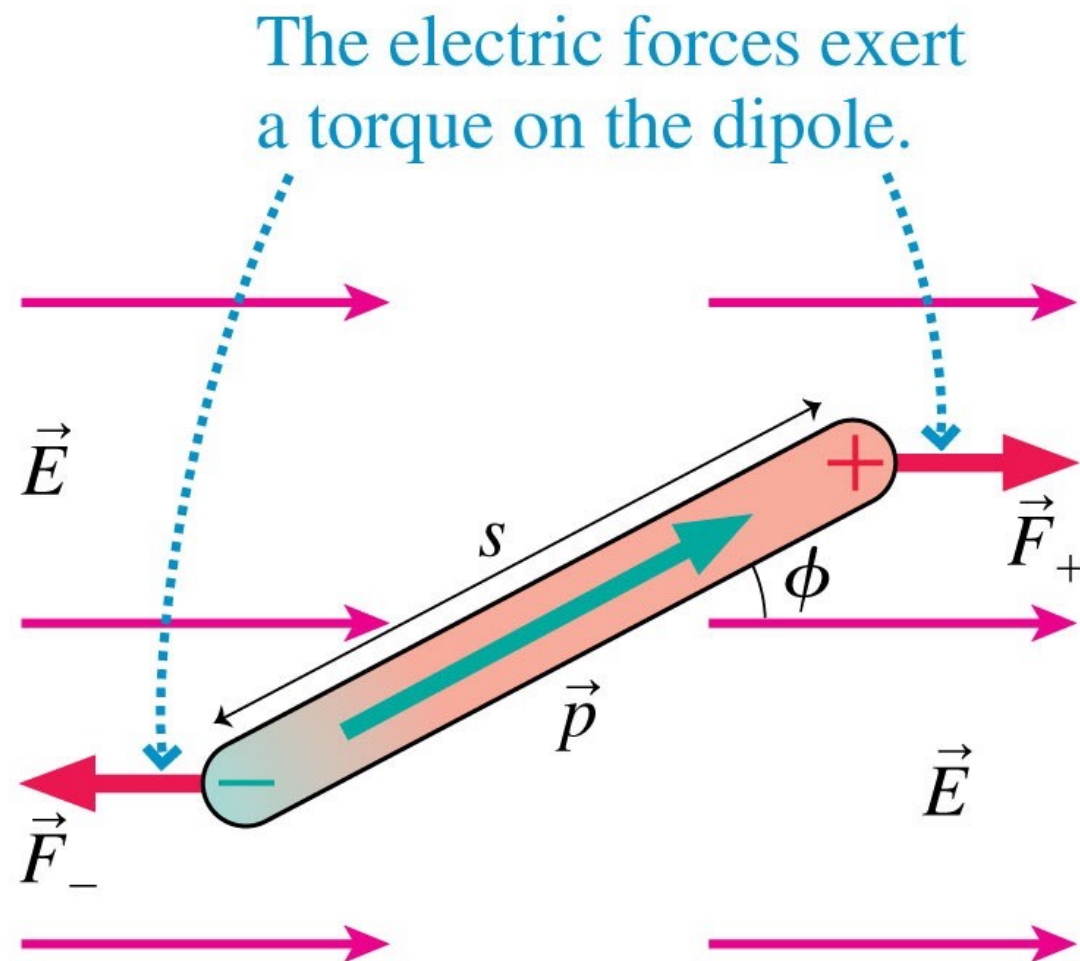
$$dW = F_s ds$$

rotational motion

$$dW = \tau d\phi$$

$$= -pE \sin \phi d\phi$$

# Potential Energy of a dipole in a uniform field



linear motion

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rotational motion

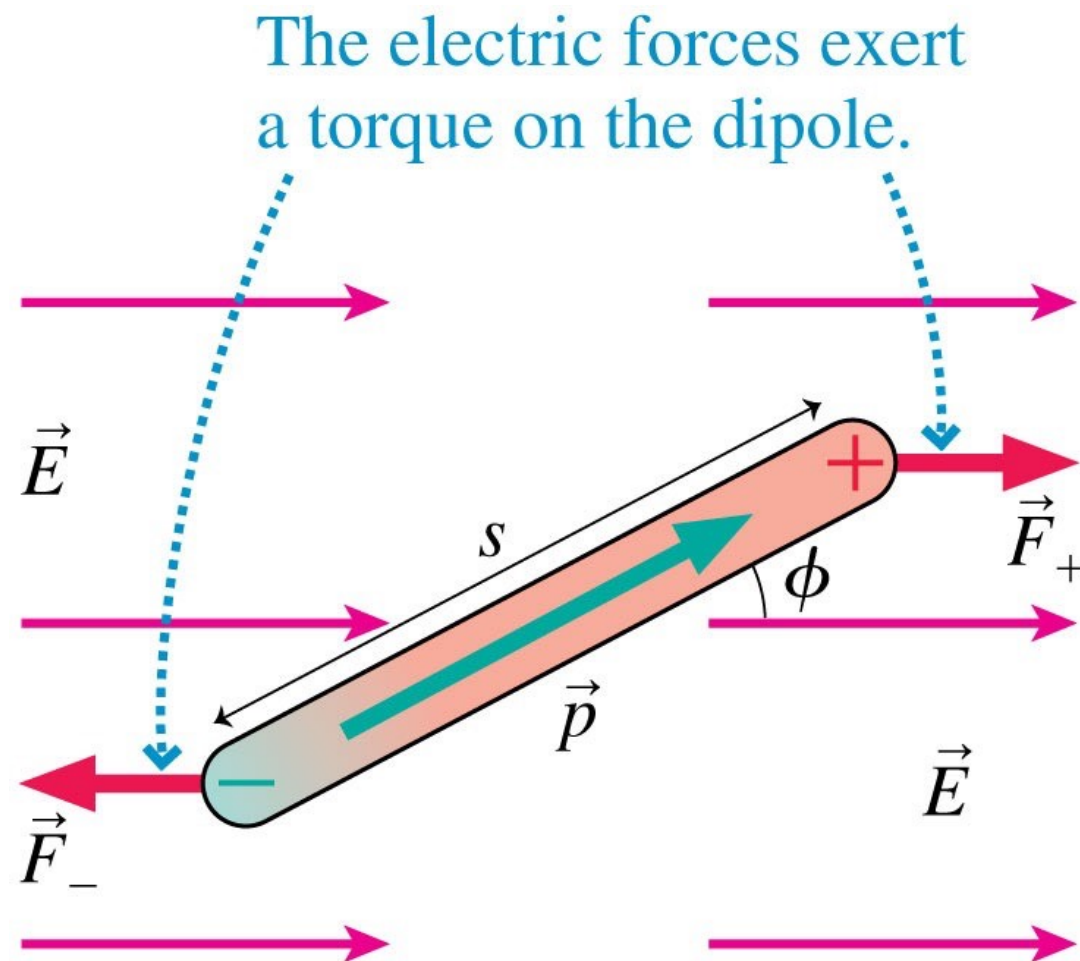
$$dW = \tau d\phi$$

$$= -pE \sin \phi d\phi$$

$$W = - \int pE \sin \phi d\phi$$



# Potential Energy of a dipole in a uniform field



linear motion

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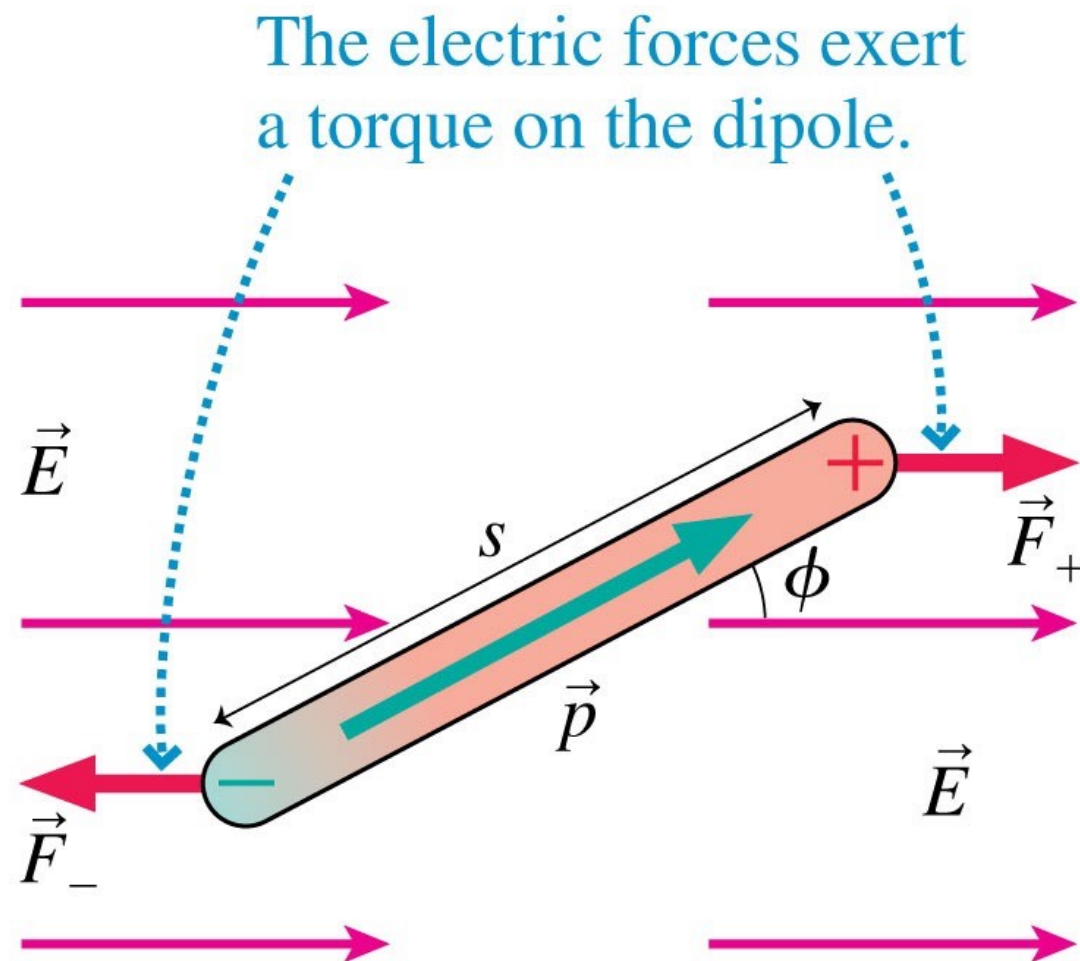
rotational motion

$$dW = \tau d\phi$$

$$= -pE \sin \phi d\phi$$

$$W = - \int pE \sin \phi d\phi = -pE \int_{\phi_i}^{\phi_f} \sin \phi d\phi$$

# Potential Energy of a dipole in a uniform field



linear motion

$$dW = F_s ds$$

rotational motion

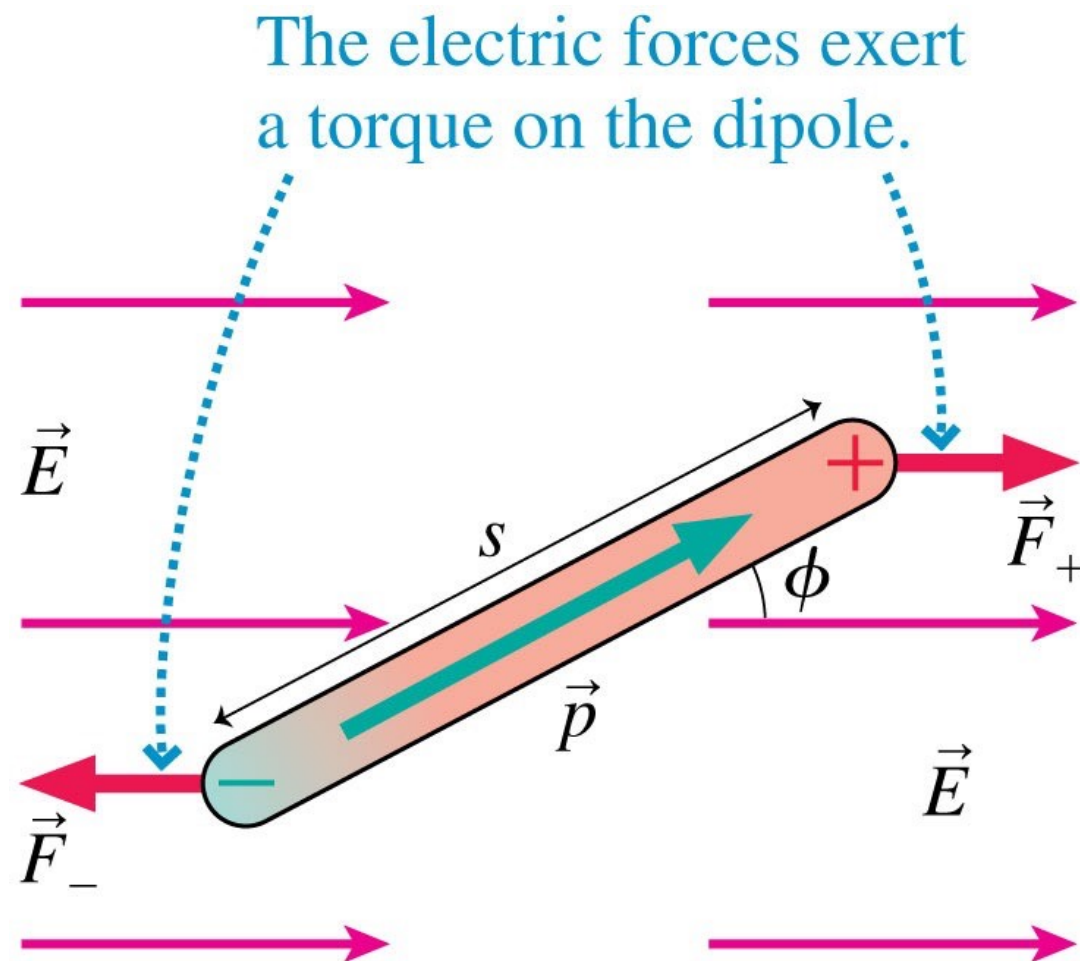
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$$= pE \cos \phi_f - pE \cos \phi_i$$

# Potential Energy of a dipole in a uniform field



linear motion

$$dW = F_s ds$$

rotational motion

$$dW = \tau d\phi$$

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$$W = - \int pE \sin \phi d\phi = -pE \int_{\phi_i}^{\phi_f} \sin \phi d\phi$$

$$= pE \cos \phi_f - pE \cos \phi_i$$

$$U_{\text{dipole}} = -\vec{p} \cdot \vec{E}$$

# Potential Energy of a dipole in a uniform field

