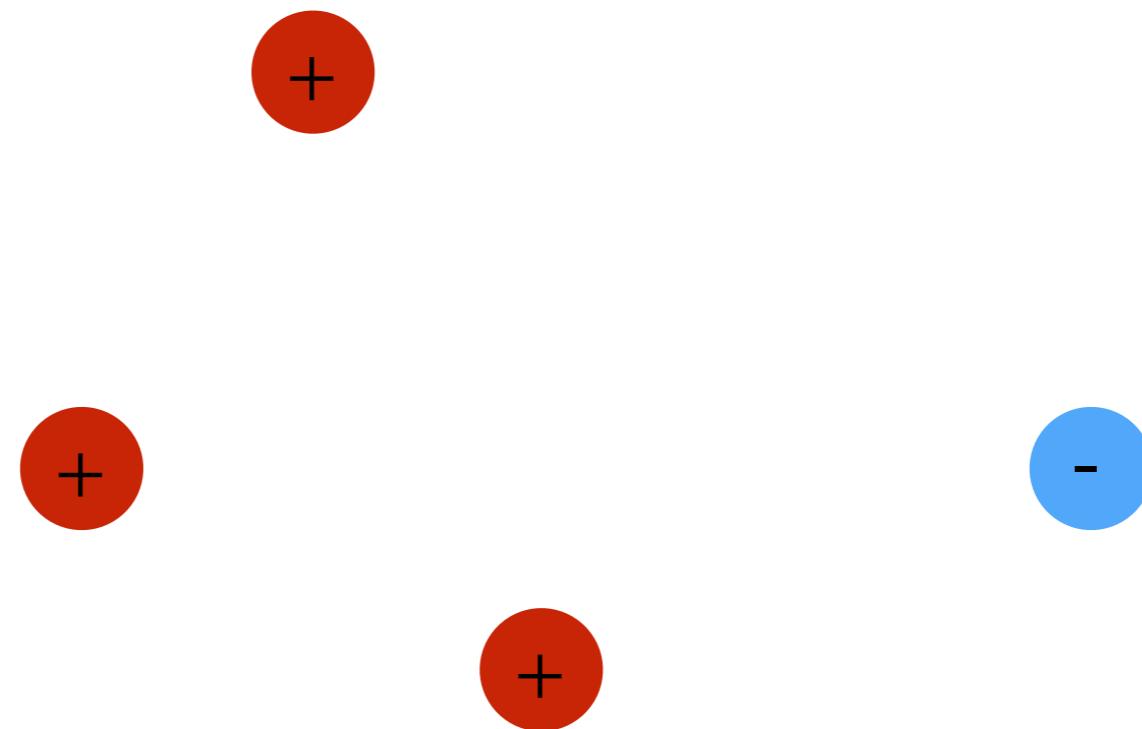




PH 220

Lance Nelson

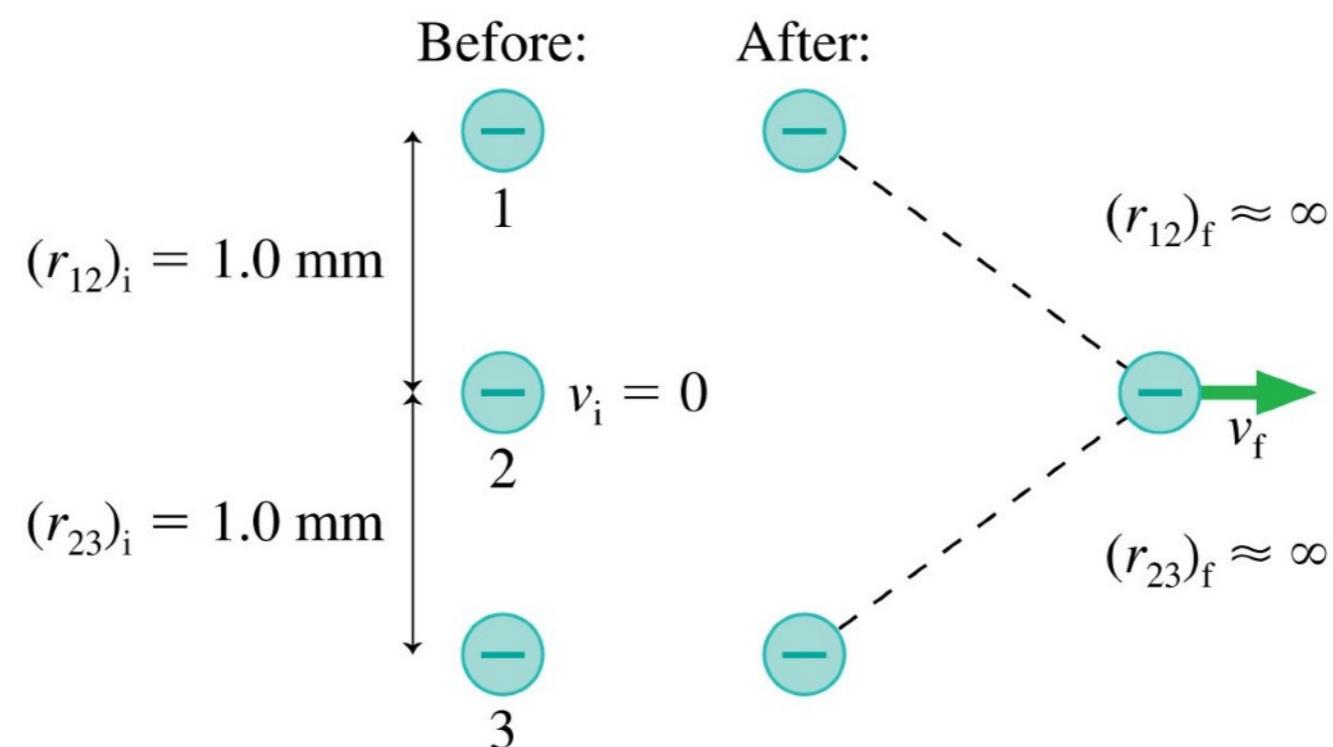
What if there are more than just two charges?



$$U = \sum_{i < j} \frac{k q_i q_j}{r_{ij}}$$

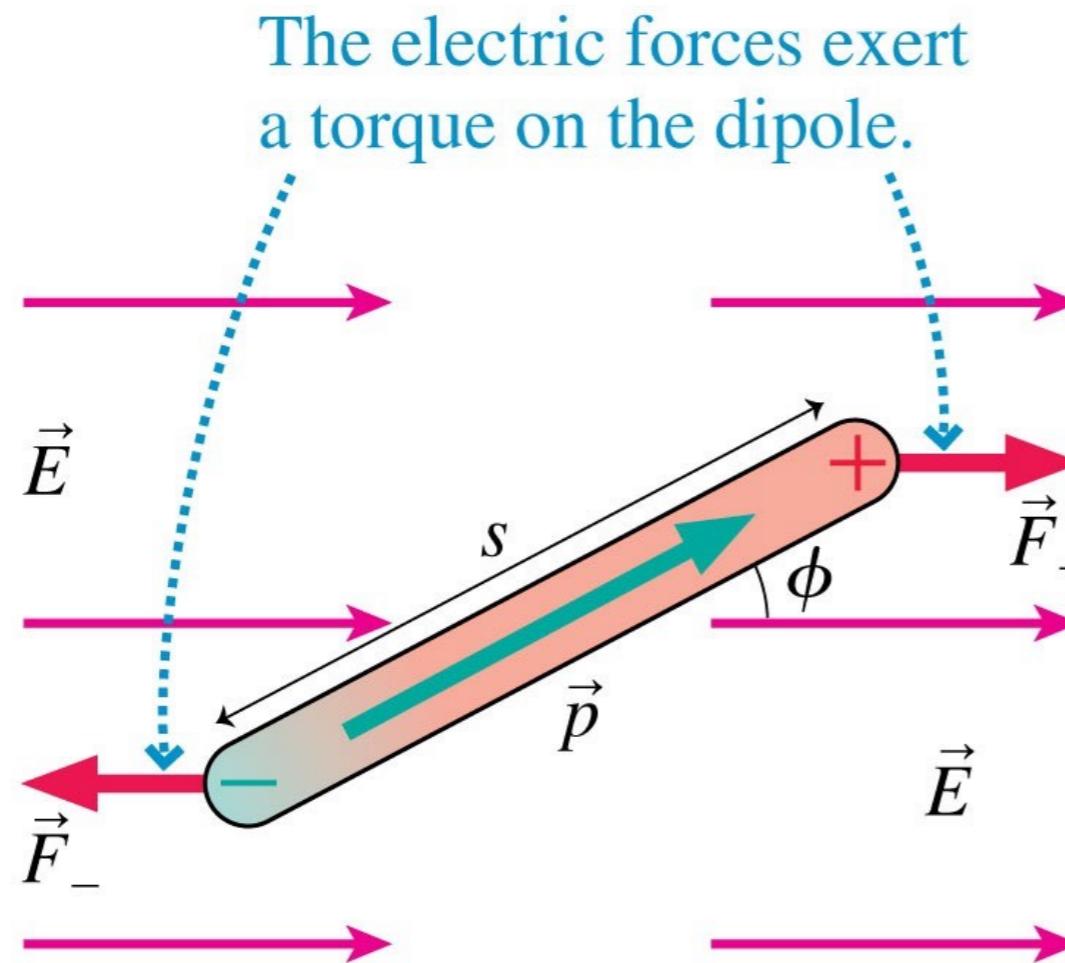
# Example

Three electrons are spaced 1.0 mm apart on a vertical line. If the center electron is nudged horizontally by a very small distance, what will its speed be when it is very far away?



$$m_{\text{electron}} = 9.109 \times 10^{-31} \text{ kg}$$

# Potential Energy of a dipole in a uniform field



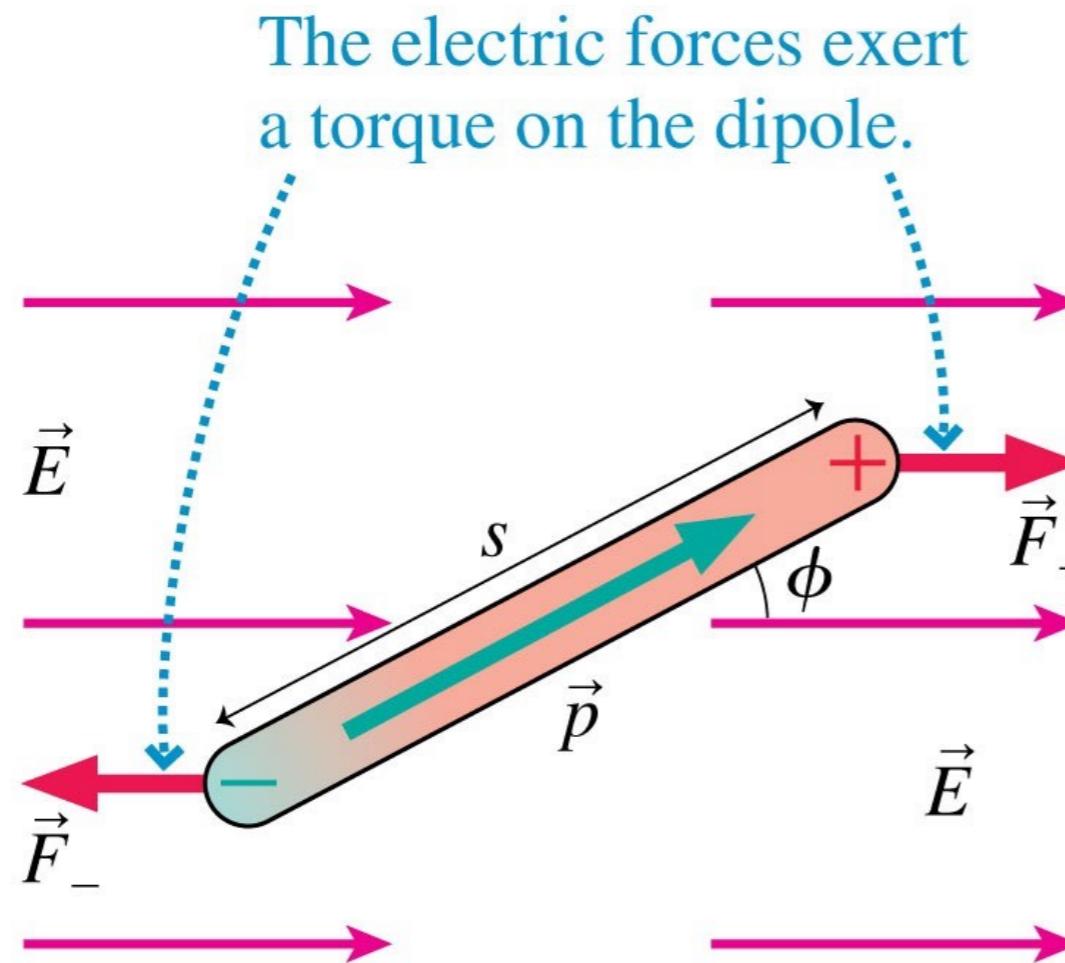
linear motion

$$dW = F_s ds$$

rotational motion

$$dW = \tau d\phi$$

# Potential Energy of a dipole in a uniform field



linear motion

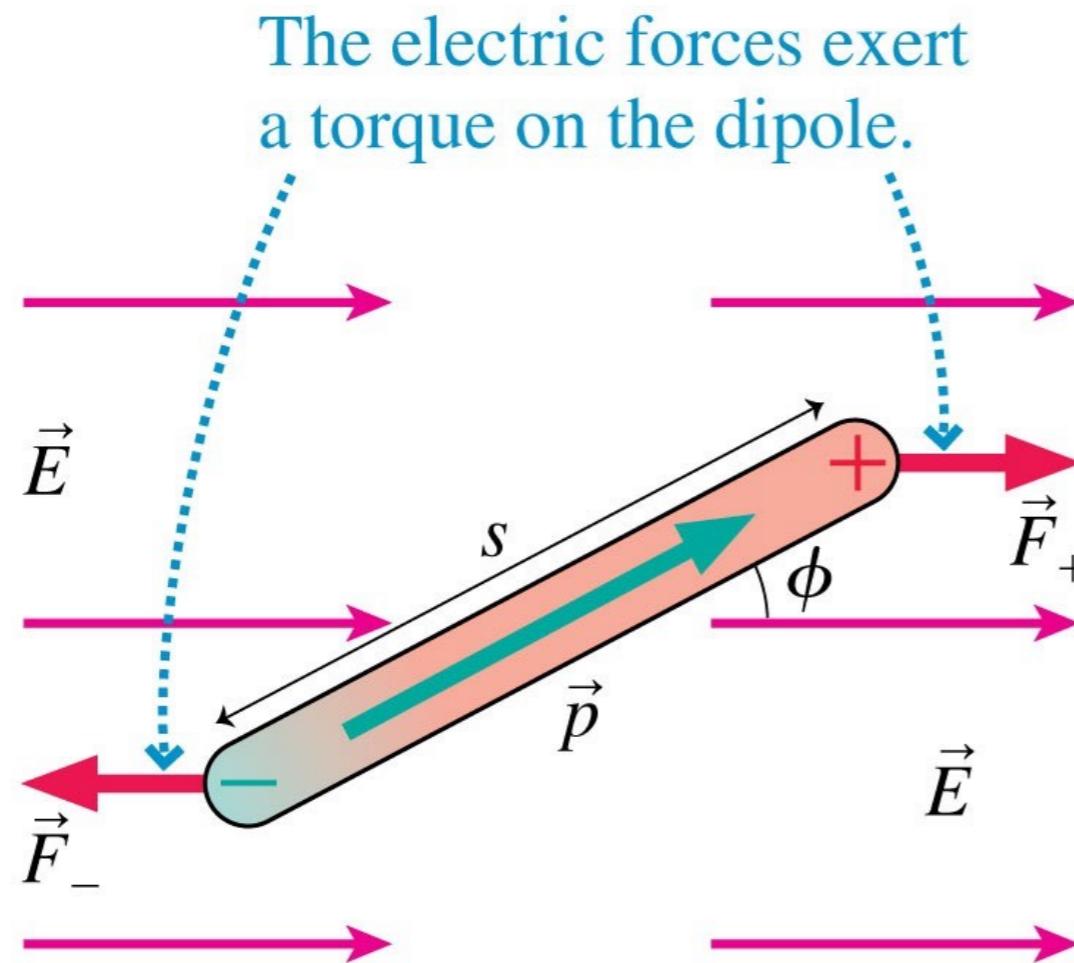
$$dW = F_s ds$$

rotational motion

$$dW = \tau d\phi$$

$$= -pE \sin \phi d\phi$$

# Potential Energy of a dipole in a uniform field



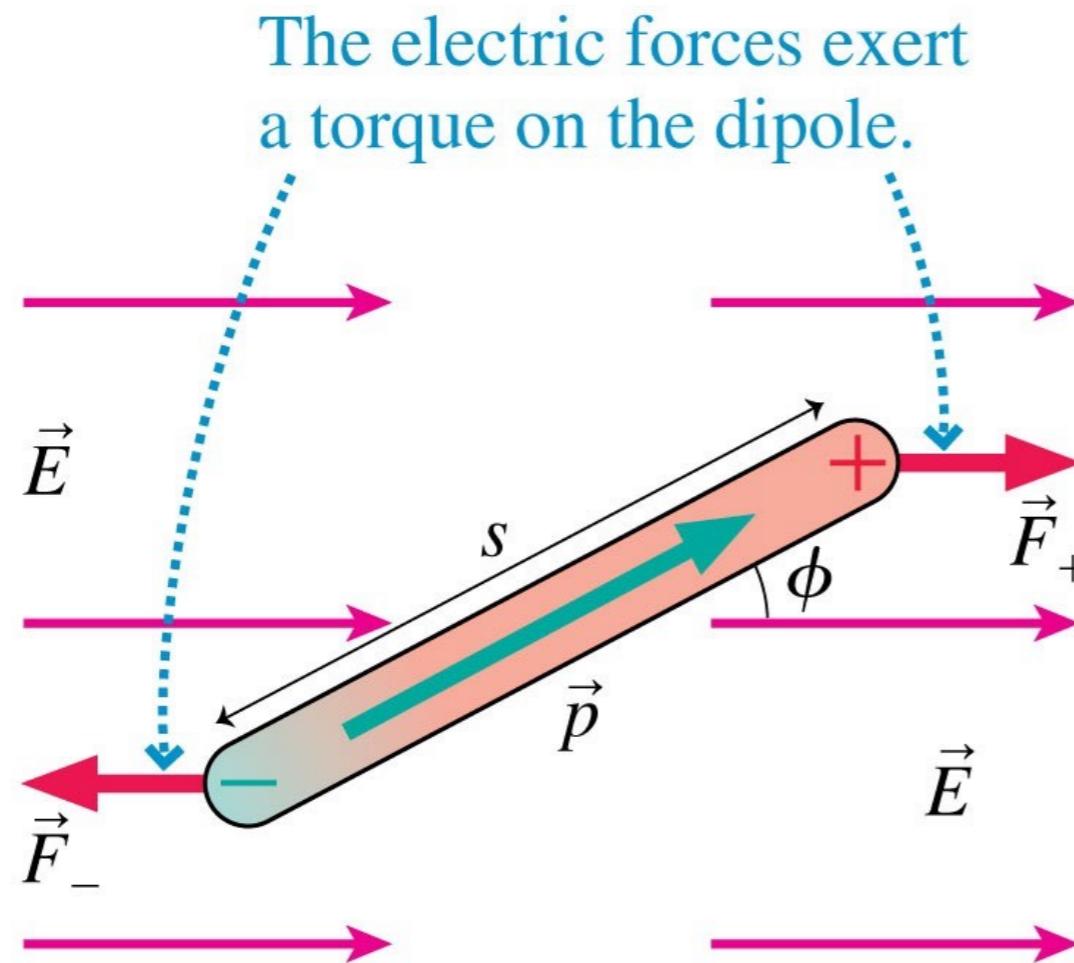
$$W = - \int pE \sin \phi d\phi$$

linear motion  
 $dW = F_s ds$

rotational motion  
 $dW = \tau d\phi$

$$= -pE \sin \phi d\phi$$

# Potential Energy of a dipole in a uniform field



linear motion

$$dW = F_s ds$$

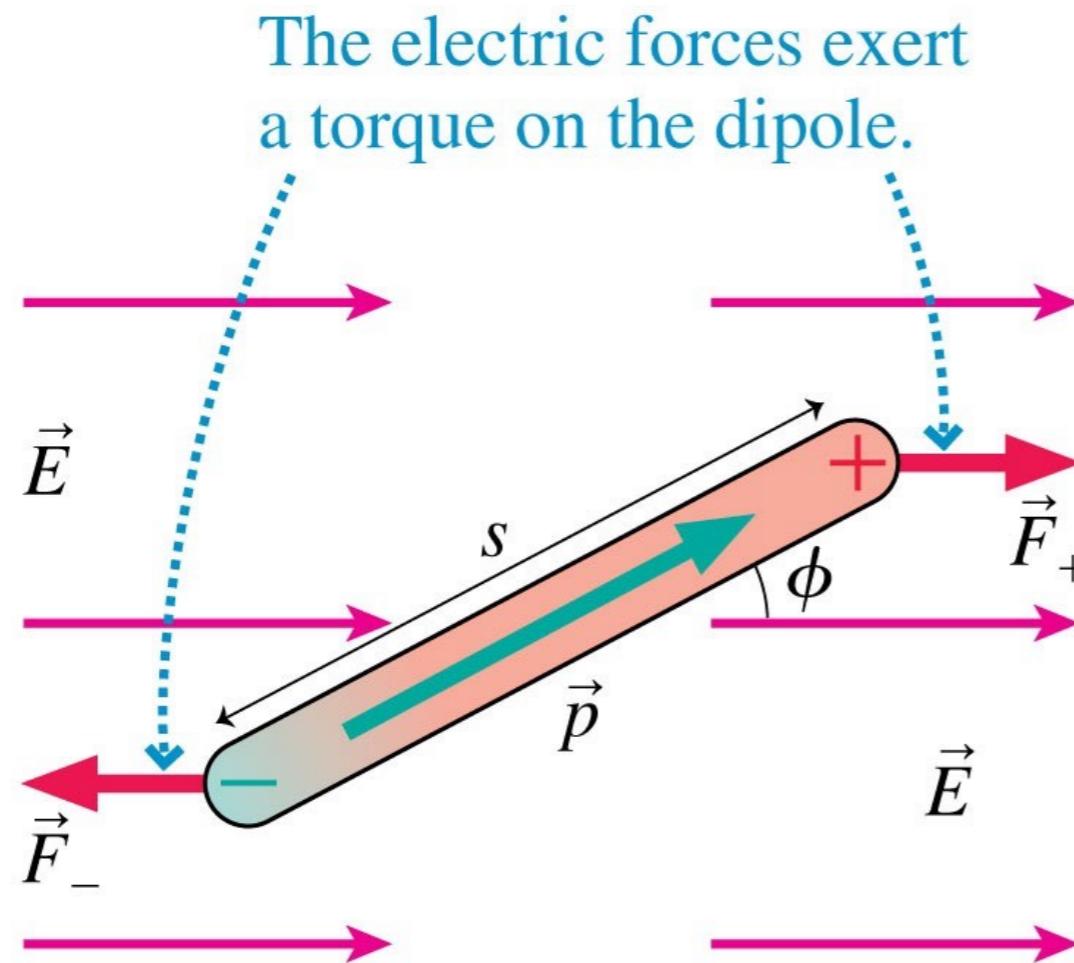
rotational motion

$$dW = \tau d\phi$$

$$= -pE \sin \phi d\phi$$

$$W = - \int pE \sin \phi d\phi = -pE \int_{\phi_i}^{\phi_f} \sin \phi d\phi$$

# Potential Energy of a dipole in a uniform field



linear motion

$$dW = F_s ds$$

rotational motion

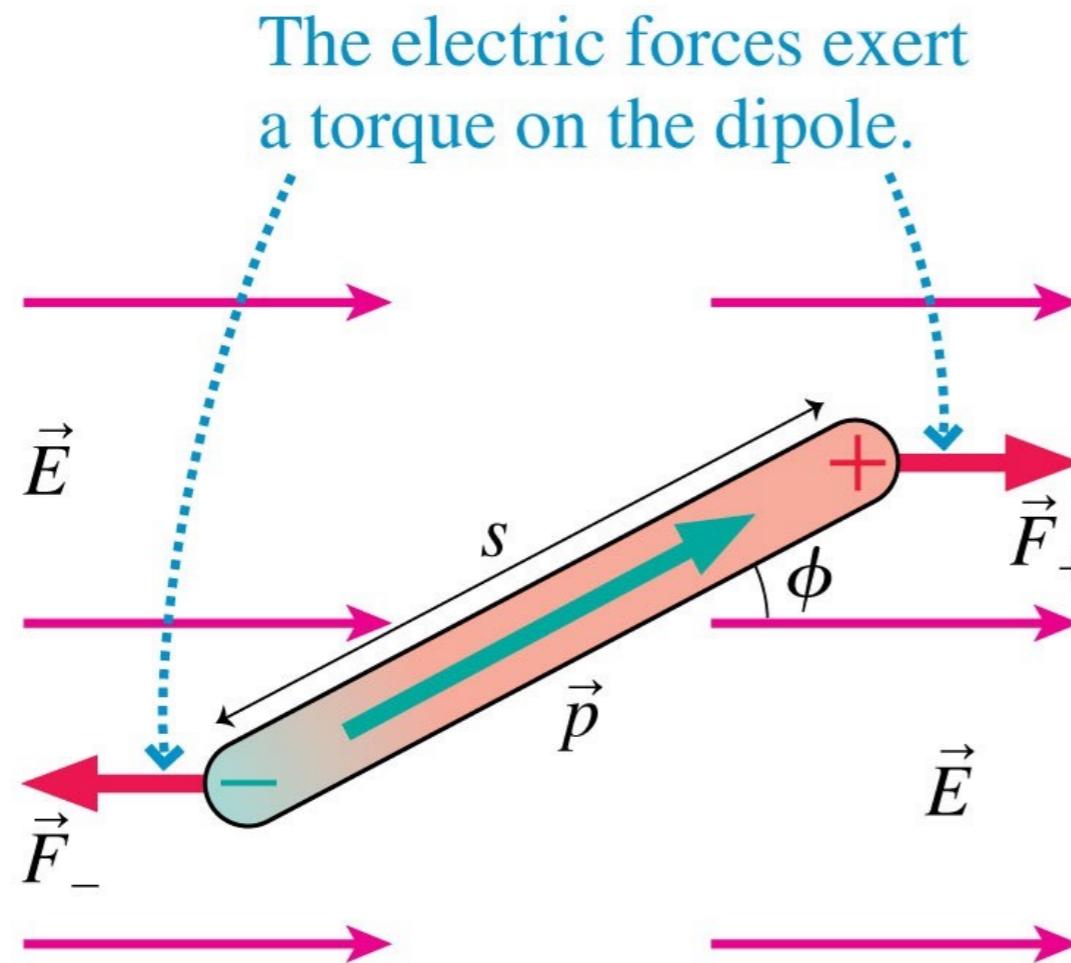
$$dW = \tau d\phi$$

$$= -pE \sin \phi d\phi$$

$$W = - \int pE \sin \phi d\phi = -pE \int_{\phi_i}^{\phi_f} \sin \phi d\phi$$

$$= pE \cos \phi_f - pE \cos \phi_i$$

# Potential Energy of a dipole in a uniform field



linear motion

$$dW = F_s ds$$

rotational motion

$$dW = \tau d\phi$$

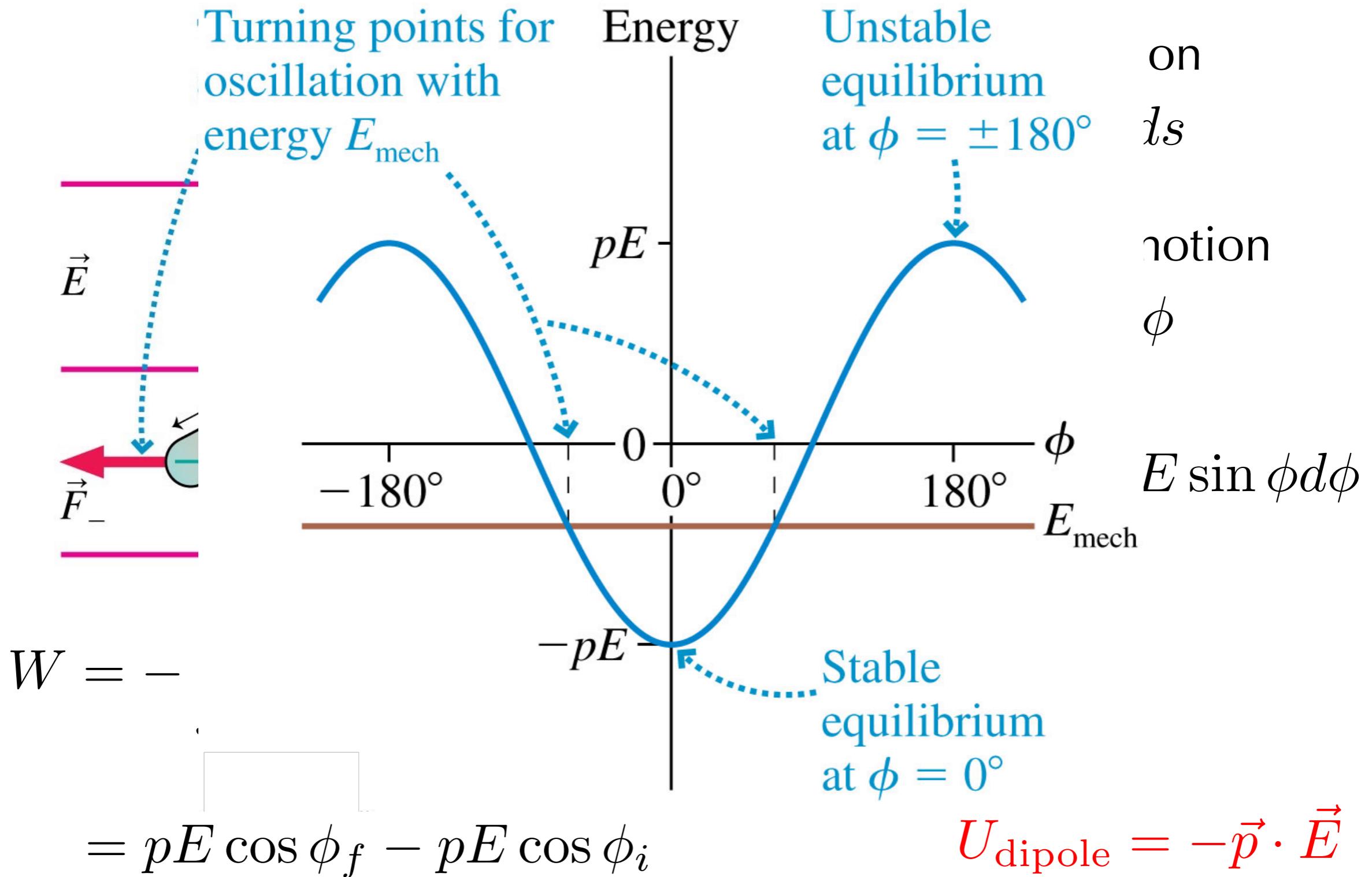
$$= -pE \sin \phi d\phi$$

$$W = - \int pE \sin \phi d\phi = -pE \int_{\phi_i}^{\phi_f} \sin \phi d\phi$$

$$= pE \cos \phi_f - pE \cos \phi_i$$

$$U_{\text{dipole}} = -\vec{p} \cdot \vec{E}$$

# Potential Energy of a dipole in a uniform field



# Potential Energy Potential

Remember when we introduced the electric field?

Force



E - Field

$$\vec{F} = \frac{kq_1q_2}{r^2}\hat{r}$$

$$\vec{E} = \frac{kq_1}{r^2}\hat{r}$$

# Potential Energy Potential

Remember when we introduced the electric field?

Force



E - Field

$$\vec{F} = \frac{kq_1q_2}{r^2}\hat{r}$$

$$\vec{E} = \frac{\vec{F}}{q}$$

$$\vec{E} = \frac{kq_1}{r^2}\hat{r}$$

# Potential Energy Potential

Remember when we introduced the electric field?

Force



E - Field

$$\vec{F} = \frac{kq_1q_2}{r^2}\hat{r}$$

$$\vec{E} = \frac{\vec{F}}{q}$$

$$\vec{E} = \frac{kq_1}{r^2}\hat{r}$$

$$U = \frac{kq_1q_2}{r}$$

$$V = \frac{U}{q}$$

$$V = \frac{kq_1}{r}$$

Potential Energy



Potential

# Potential Energy $\longrightarrow$ Potential

Remember when we introduced the electric field?

Force



E - Field

$$\vec{F} = \frac{kq_1q_2}{r^2}\hat{r}$$

$$\vec{E} = \frac{\vec{F}}{q}$$

$$\vec{E} = \frac{kq_1}{r^2}\hat{r}$$

$$U = \frac{kq_1q_2}{r}$$

$$V = \frac{U}{q}$$

$$V = \frac{kq_1}{r}$$

Potential Energy



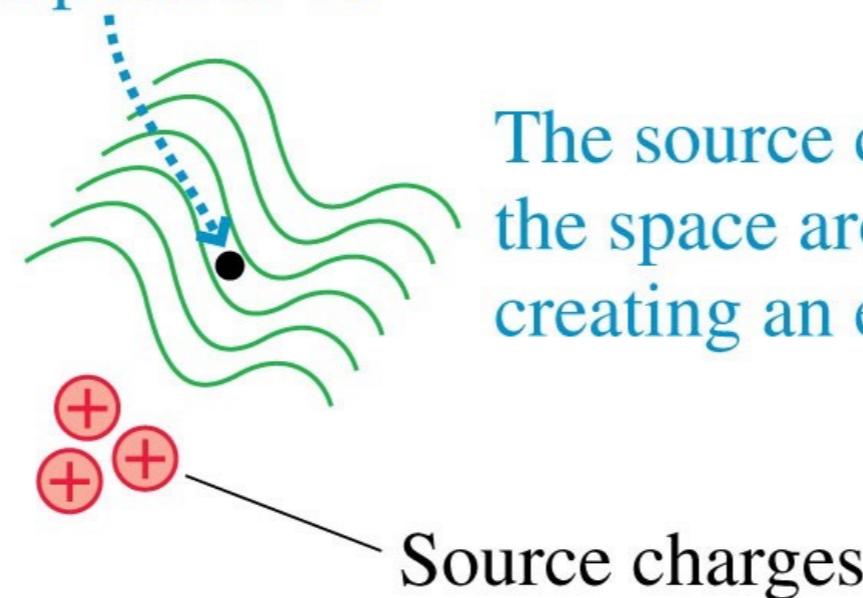
Potential

units??

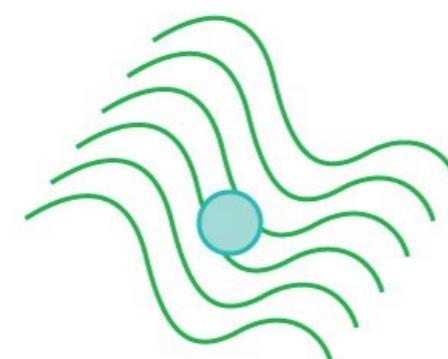
1 volt = 1 V  $\equiv$  1 J/C

- Test charge  $q$  is used as a probe to determine the electric potential, but the value of  $V$  is *independent of  $q$* .
- **The electric potential, like the electric field, is a property of the source charges.**

The potential at  
this point is  $V$ .



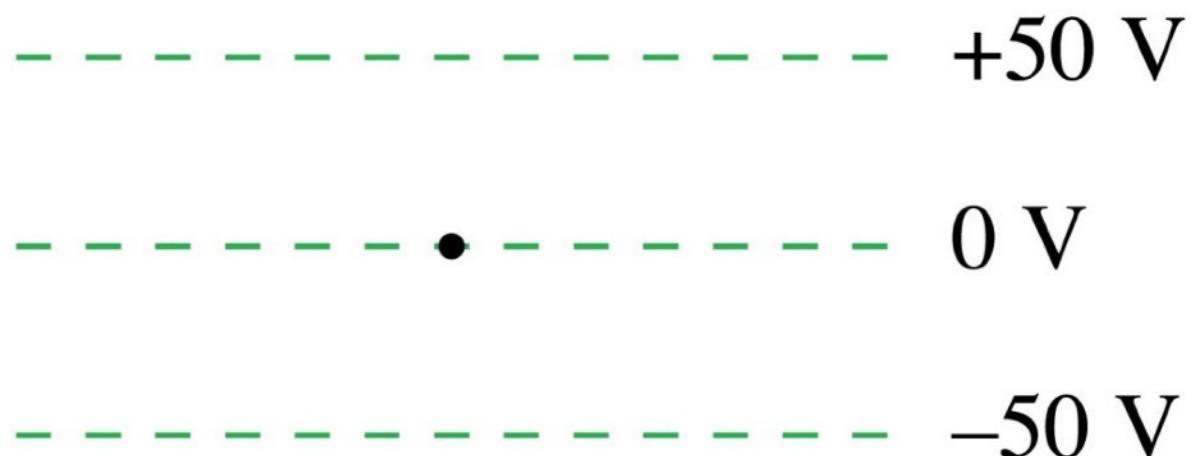
The source charges alter  
the space around them by  
creating an electric potential.



If charge  $q$  is in the potential,  
the electric potential energy is  
 $U_{q+\text{sources}} = qV$ .

## Question #15

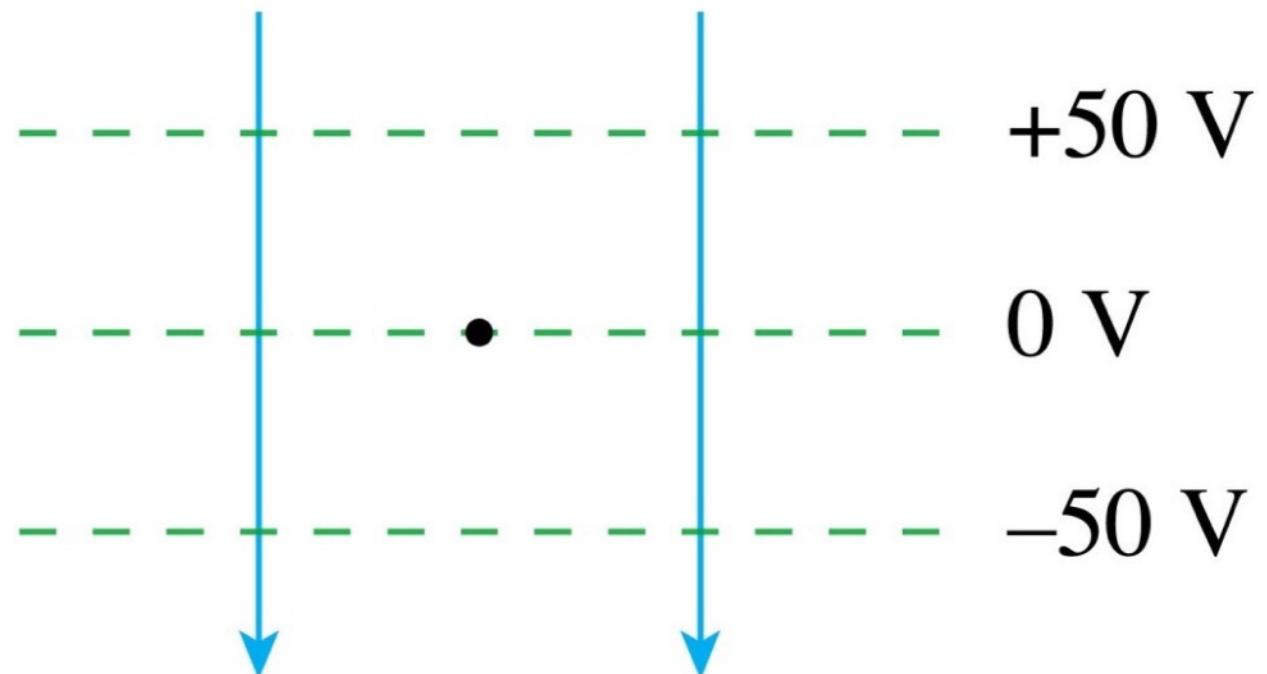
A proton is released from rest at the dot. Afterward, the proton



- A. Moves downward with an increasing speed.
- B. Moves upward with steady speed.
- C. Moves upward with an increasing speed.
- D. Moves downward with a steady speed.
- E. Remains at the dot.

## Question #15

A proton is released from rest at the dot. Afterward, the proton



- A. Moves downward with an increasing speed.
- B. Moves upward with steady speed.
- C. Moves upward with an increasing speed.
- D. Moves downward with a steady speed.
- E. Remains at the dot.

## **Question #16**

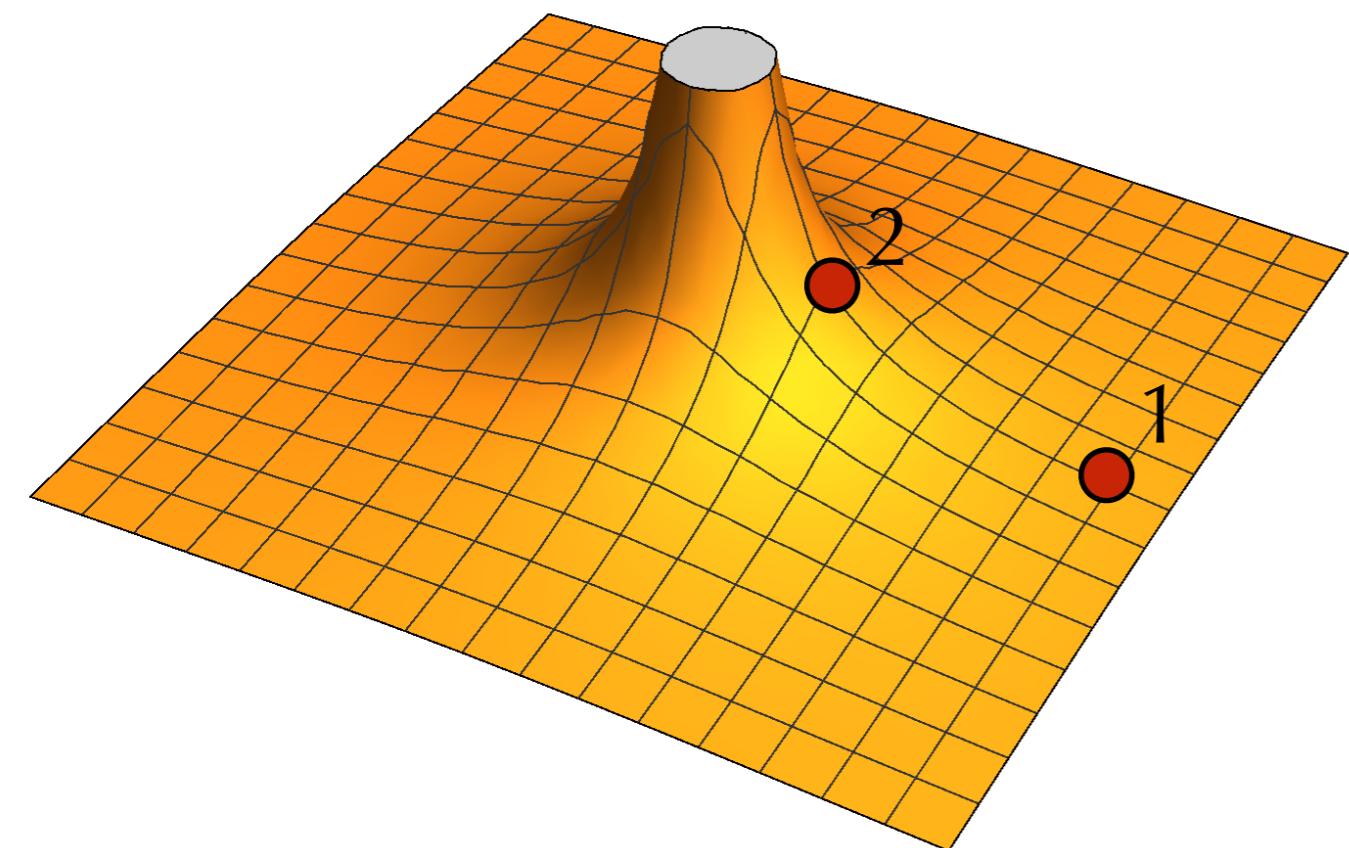
If a positive charge is released from rest, it moves in the direction of

- A. A stronger electric field.
- B. Lower electric potential.
- C. Higher electric potential.
- D. A weaker electric field.
- E. Both B and D.

# Electric potential due to a point charge

$$V = \frac{kq}{r}$$

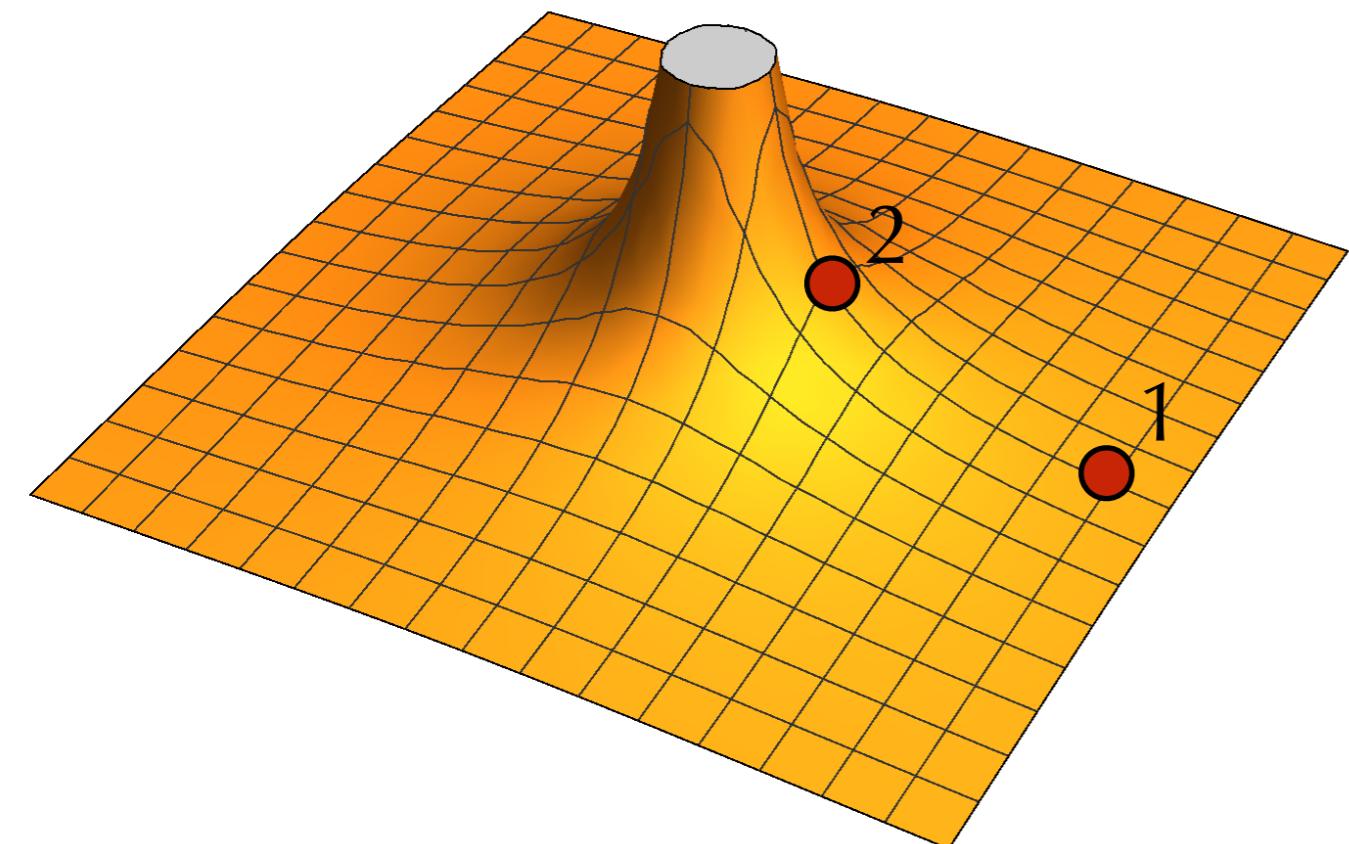
If an electron/proton were to move from point 1 to point 2, would its energy increase or decrease.



# Electric potential due to a point charge

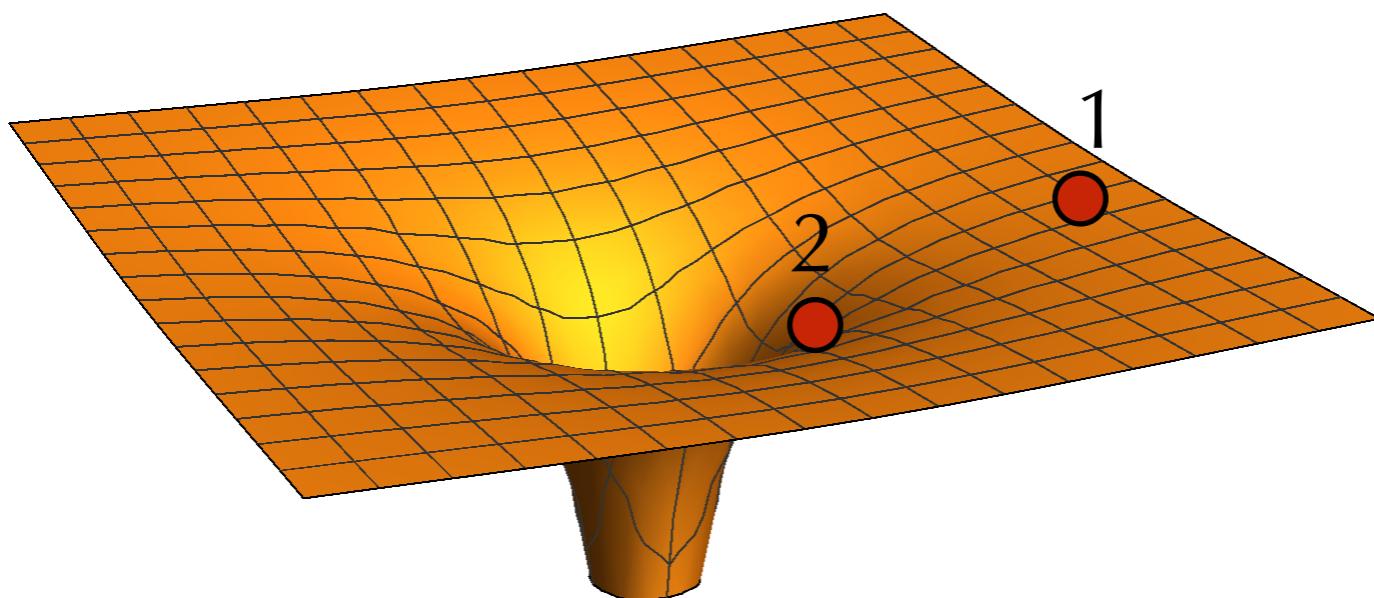
$$V = \frac{kq}{r}$$

If an electron/proton were to move from point 1 to point 2, would its energy increase or decrease.



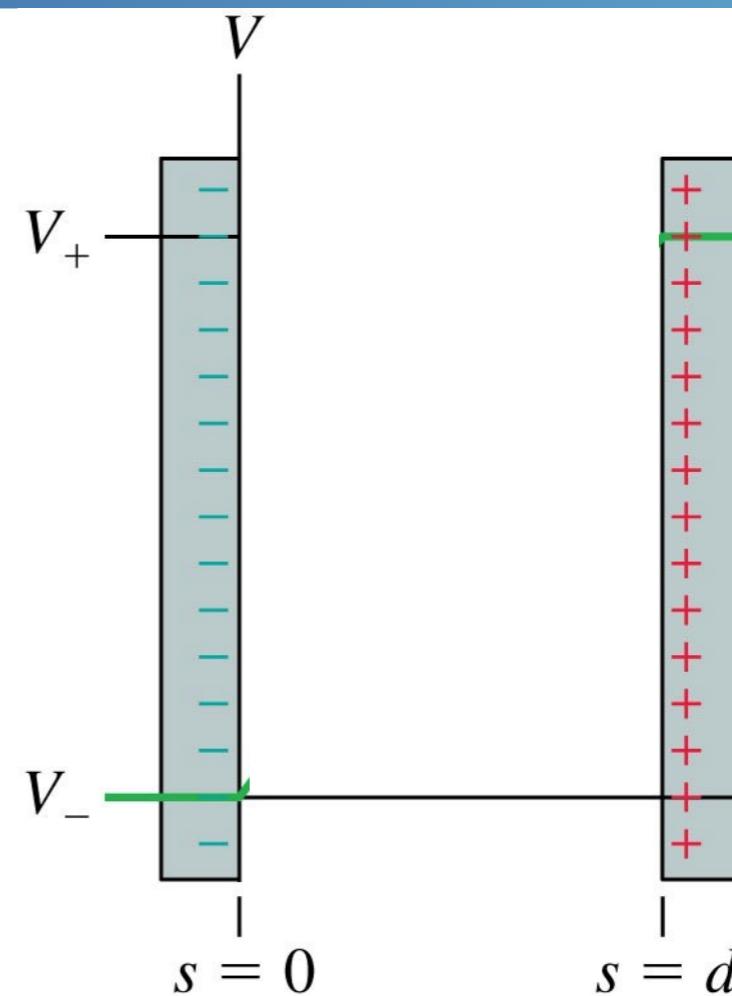
$$U = qV$$

$$V = \frac{kq}{r}$$



If an electron/proton were to move from point 1 to point 2, would its energy increase or decrease.

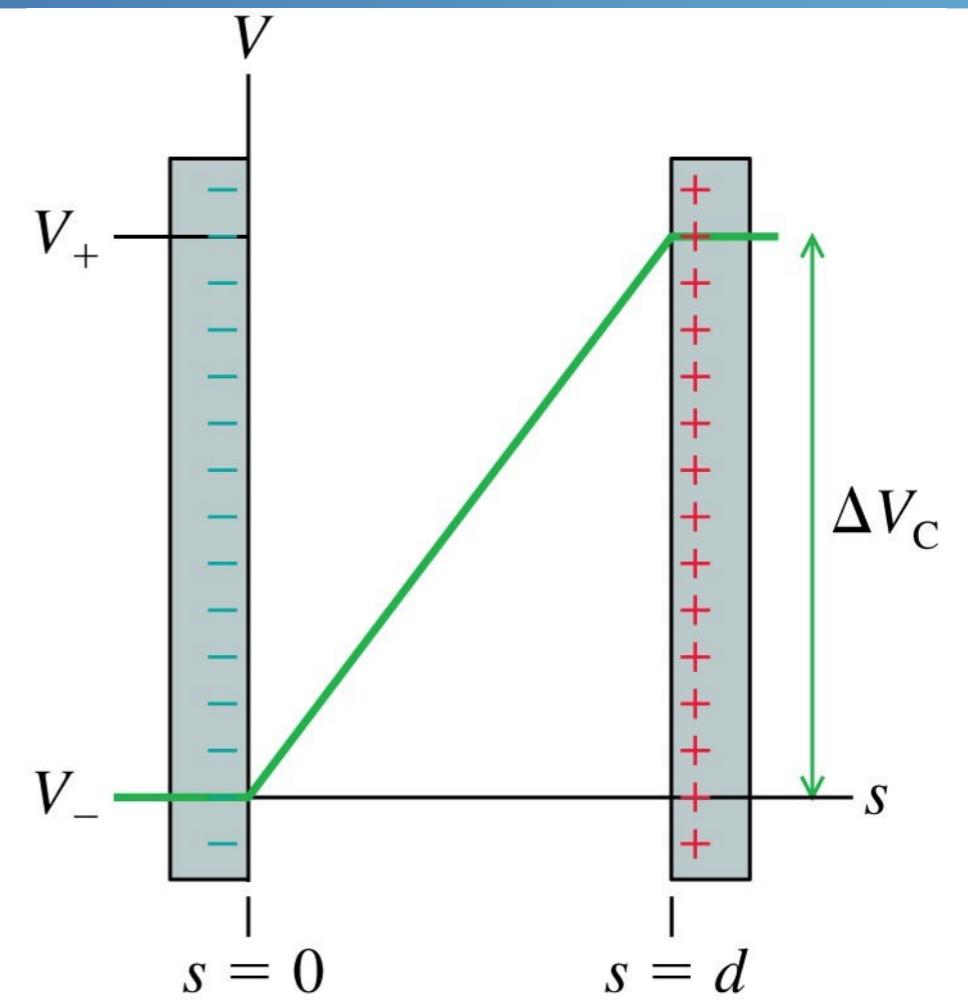
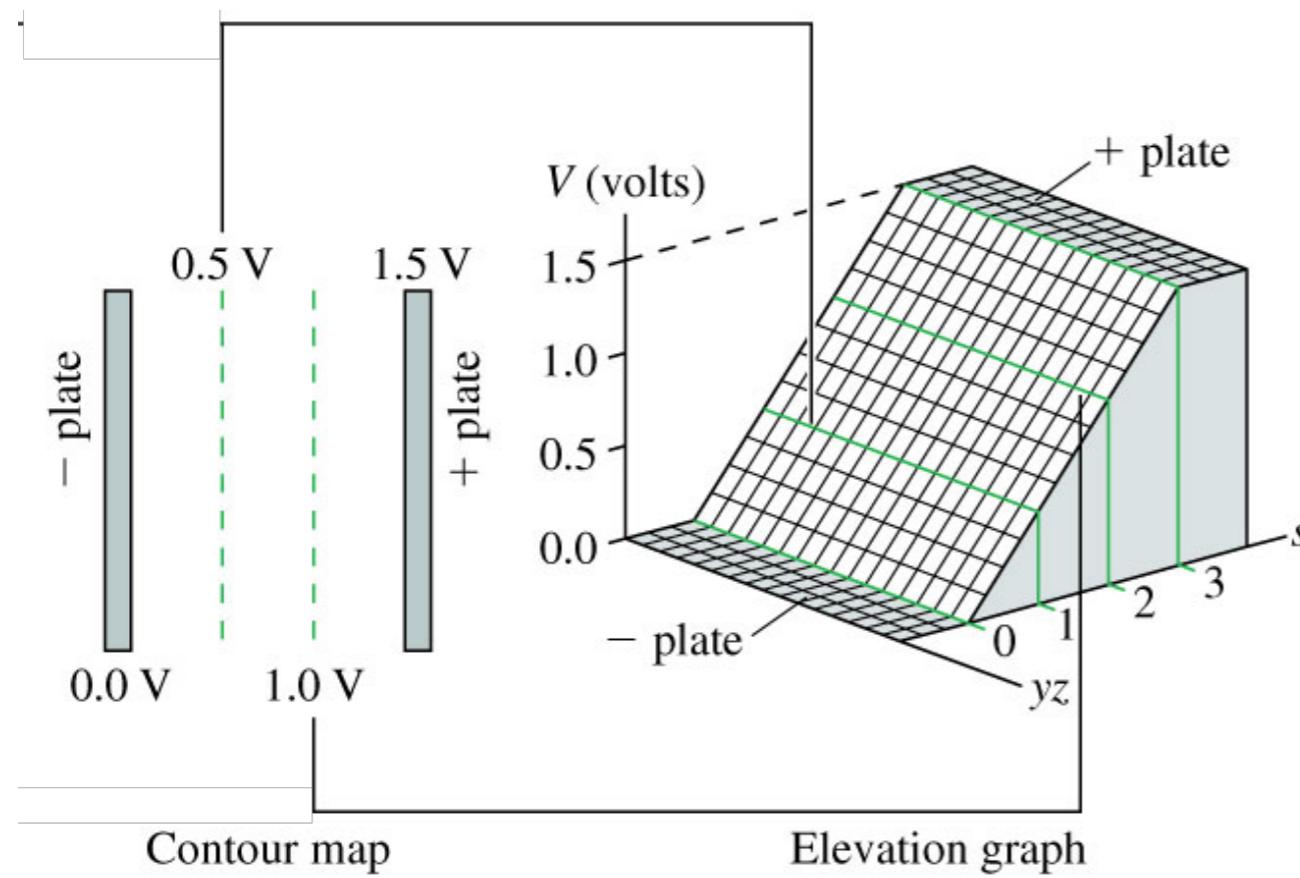
# Parallel-plate capacitor



What would you expect the potential due to the oppositely charged plates to be?

# Parallel-plate capacitor

$$V = Es$$



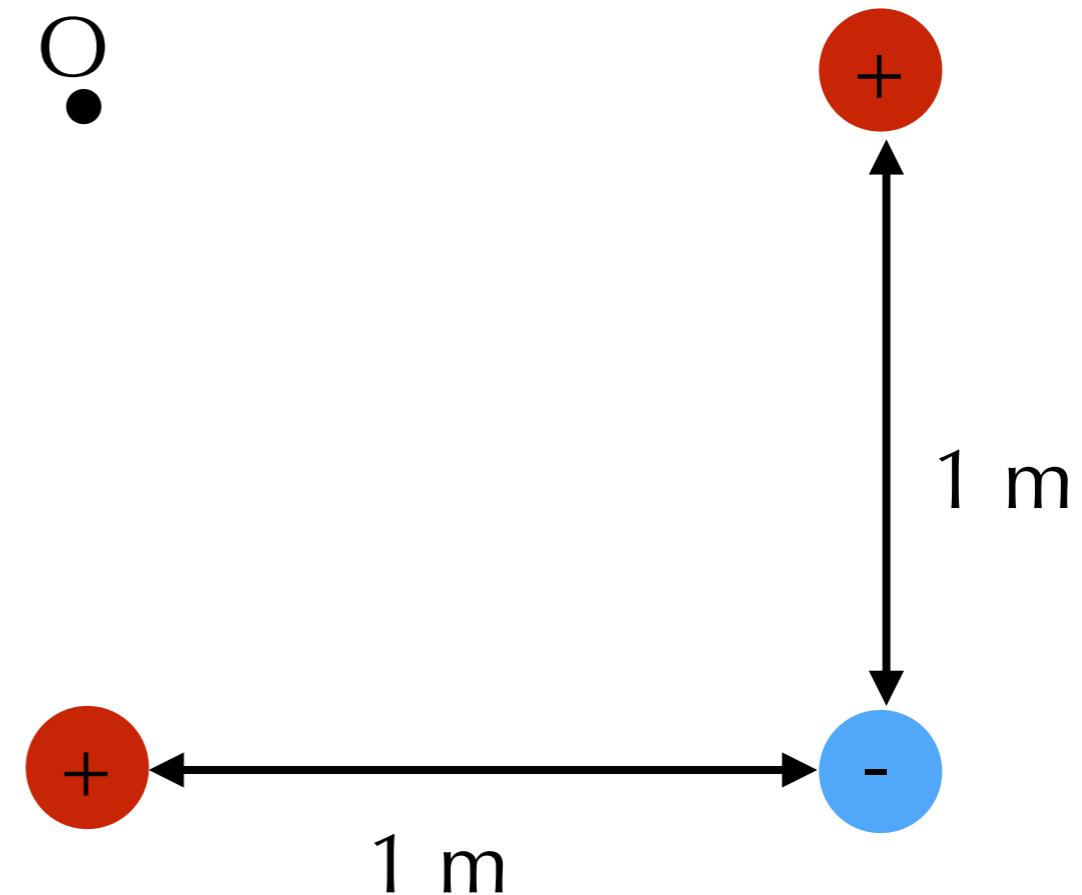
What would you expect the potential due to the oppositely charged plates to be?

# Electric Potential of Point charge

Make a sketch of the electric potential of these three point charges

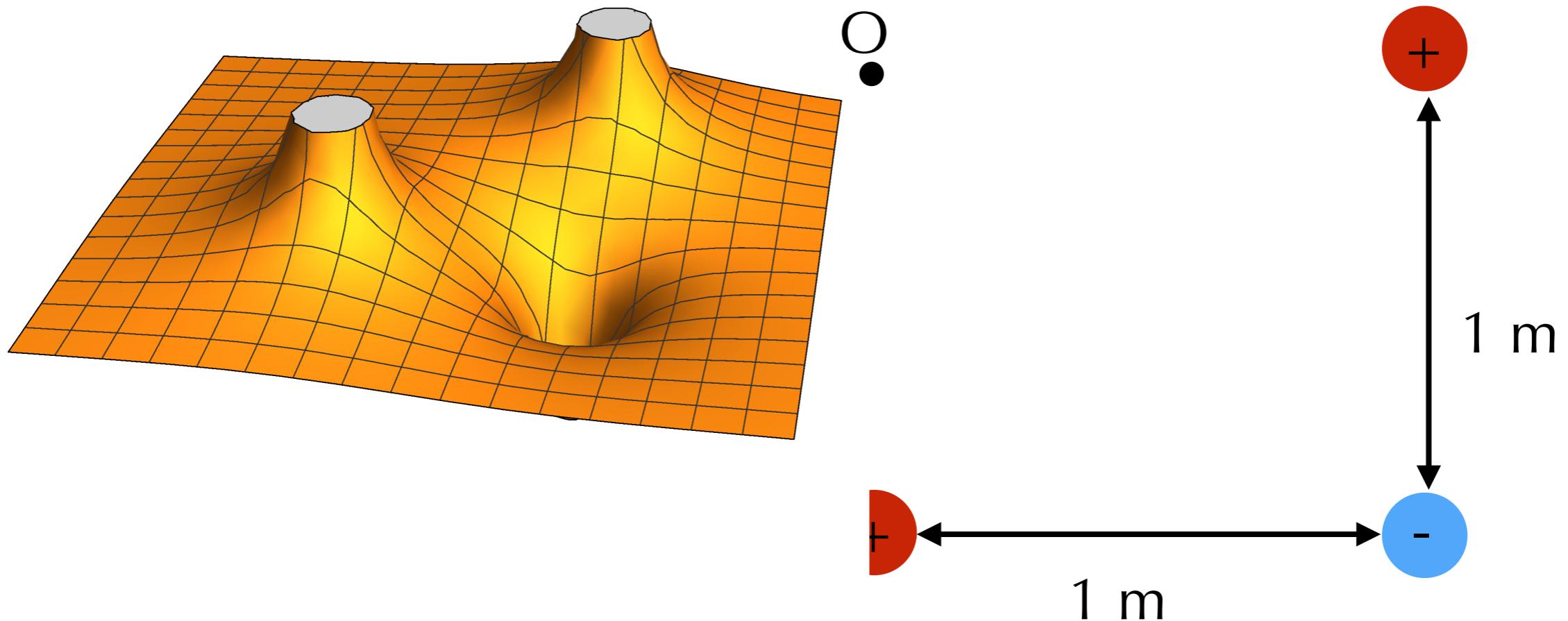
$$U_{\text{elec}} = \frac{Kq_1q_2}{x}$$

$$V = \frac{kq}{r}$$



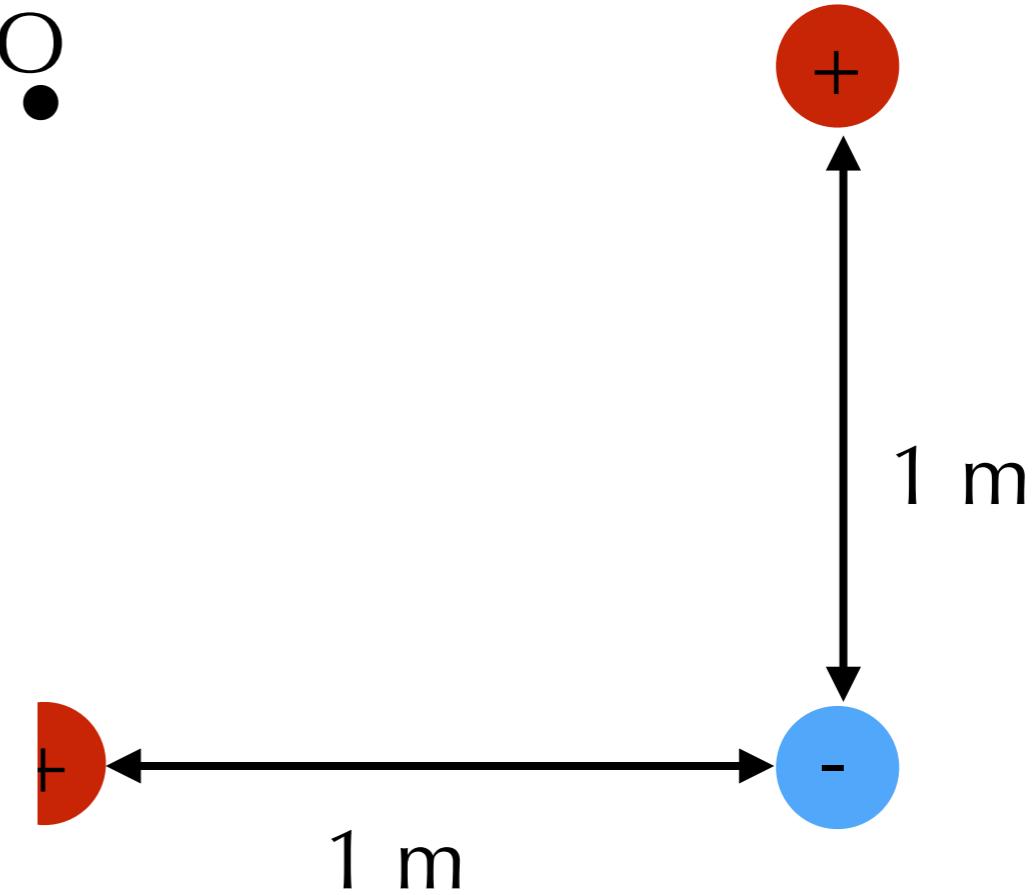
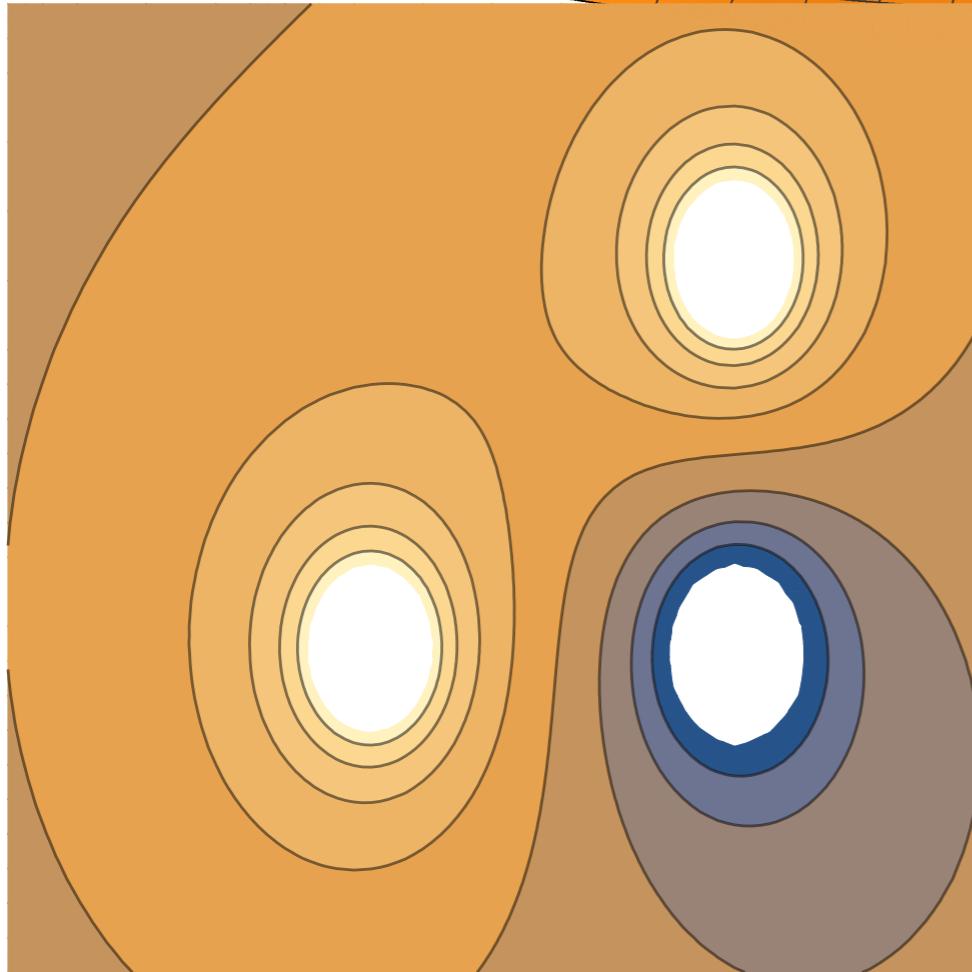
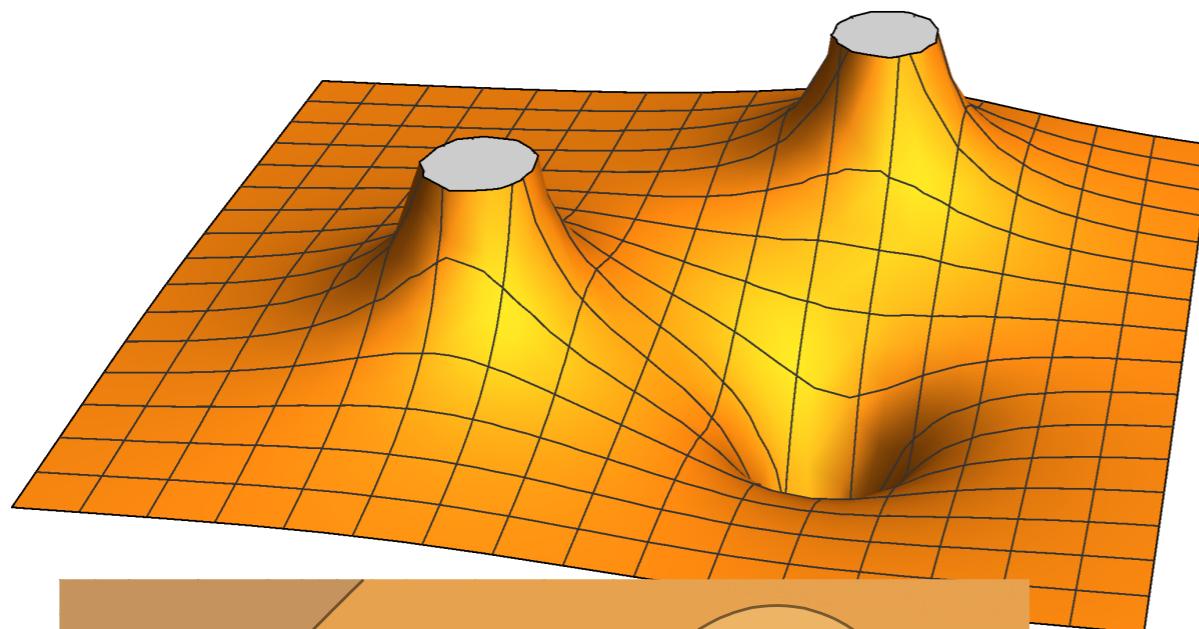
# Electric Potential of Point charge

Make a sketch of the electric potential of these three point charges



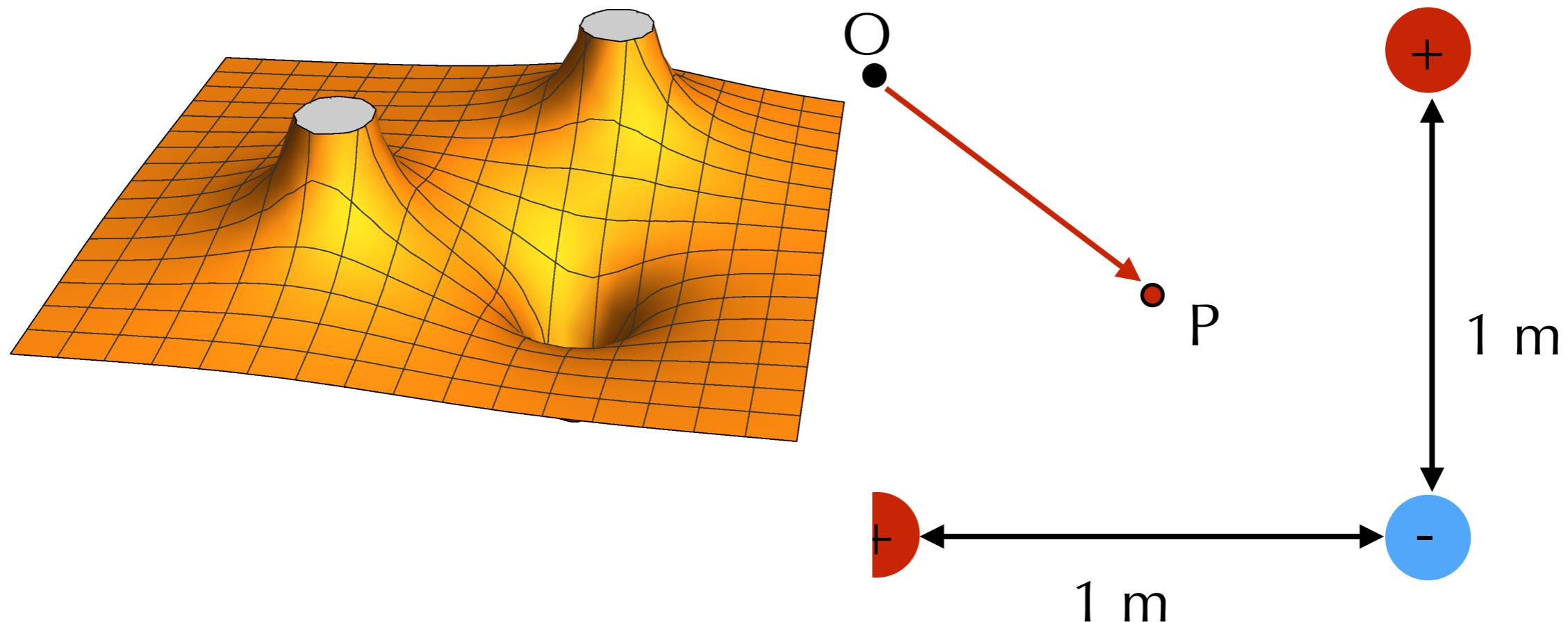
# Electric Potential of Point charge

Make a sketch of the electric potential of these three point charges



# Electric Potential of Point charge

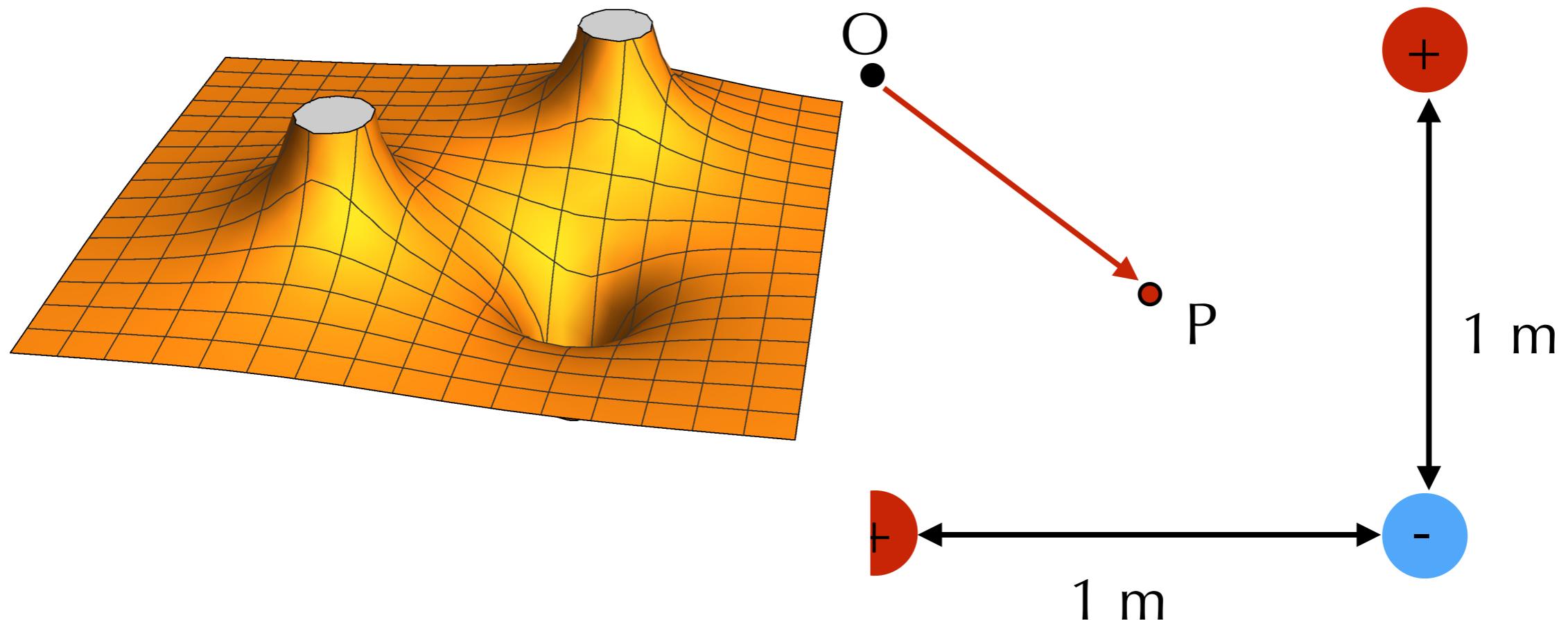
Make a sketch of the electric potential of these three point charges



Find the potential difference between point O and point P.

# Electric Potential of Point charge

Make a sketch of the electric potential of these three point charges



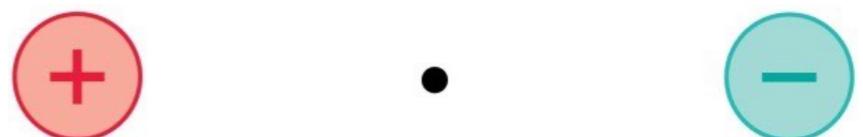
Find the potential difference between point O and point P.

If an electron is placed at O and released, how fast will it be going when it reaches point P?

## Question #17

At the midpoint between these two equal but opposite charges,

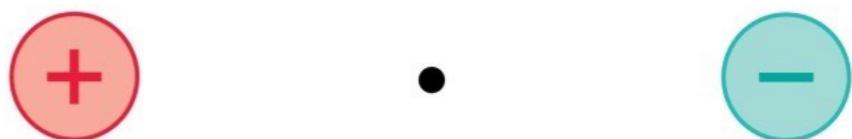
- A.  $E = 0; V = 0.$
- B.  $E = 0; V > 0.$
- C.  $E = 0; V < 0.$
- D.  $E$  points left;  $V = 0.$
- E.  $E$  points right;  $V = 0.$



## Question #17

At the midpoint between these two equal but opposite charges,

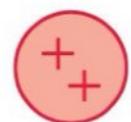
- A.  $E = 0; V = 0.$
- B.  $E = 0; V > 0.$
- C.  $E = 0; V < 0.$
- D.  $E$  points left;  $V = 0.$
- E.  $E$  points right;  $V = 0.$



Does an electric potential of zero mean anything?

## Question #18

At which point or points is the electric potential zero?



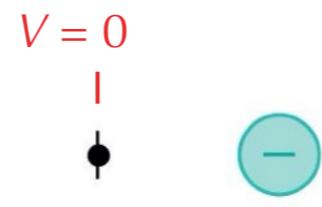
- A.
- B.
- C.
- D.
- E. More than one of these.

## Question #18

At which point or points is the electric potential zero?



A.



B. C.

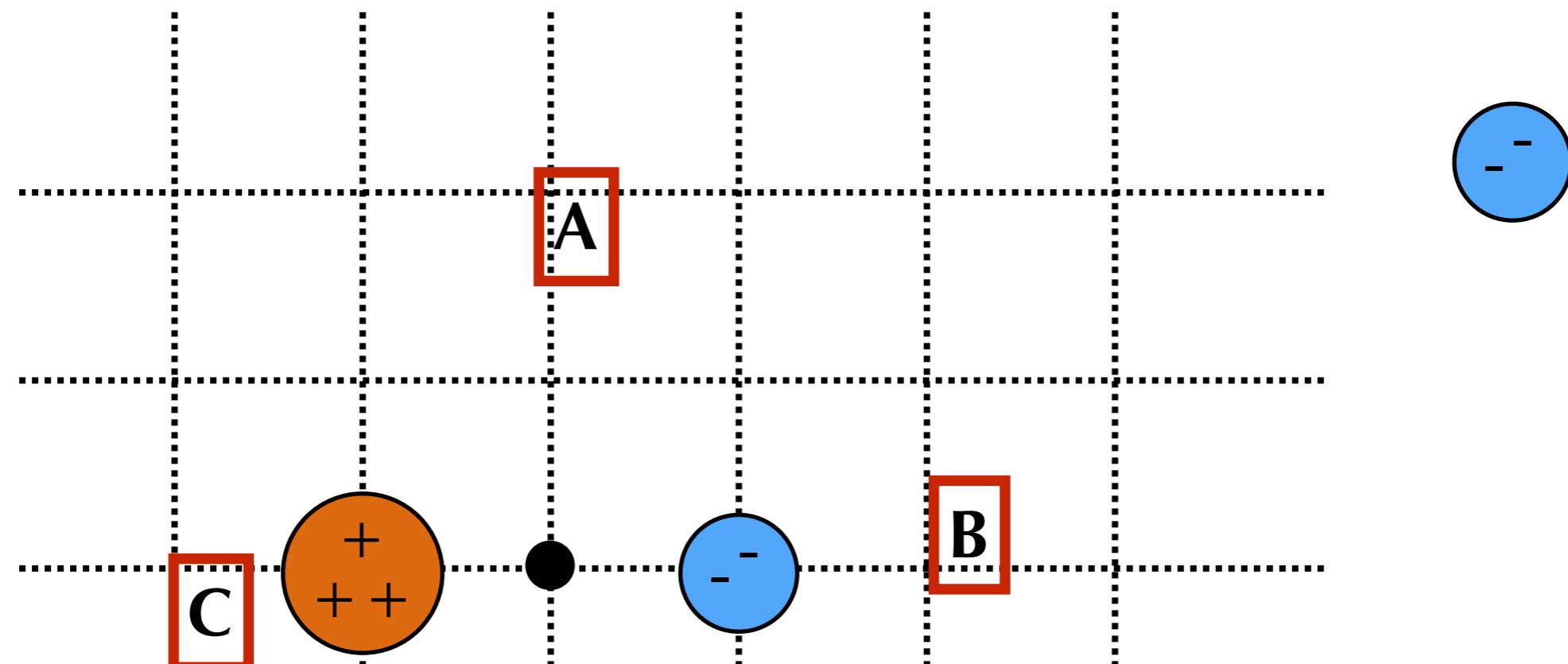


D.

E. More than one of these.

## Question #19

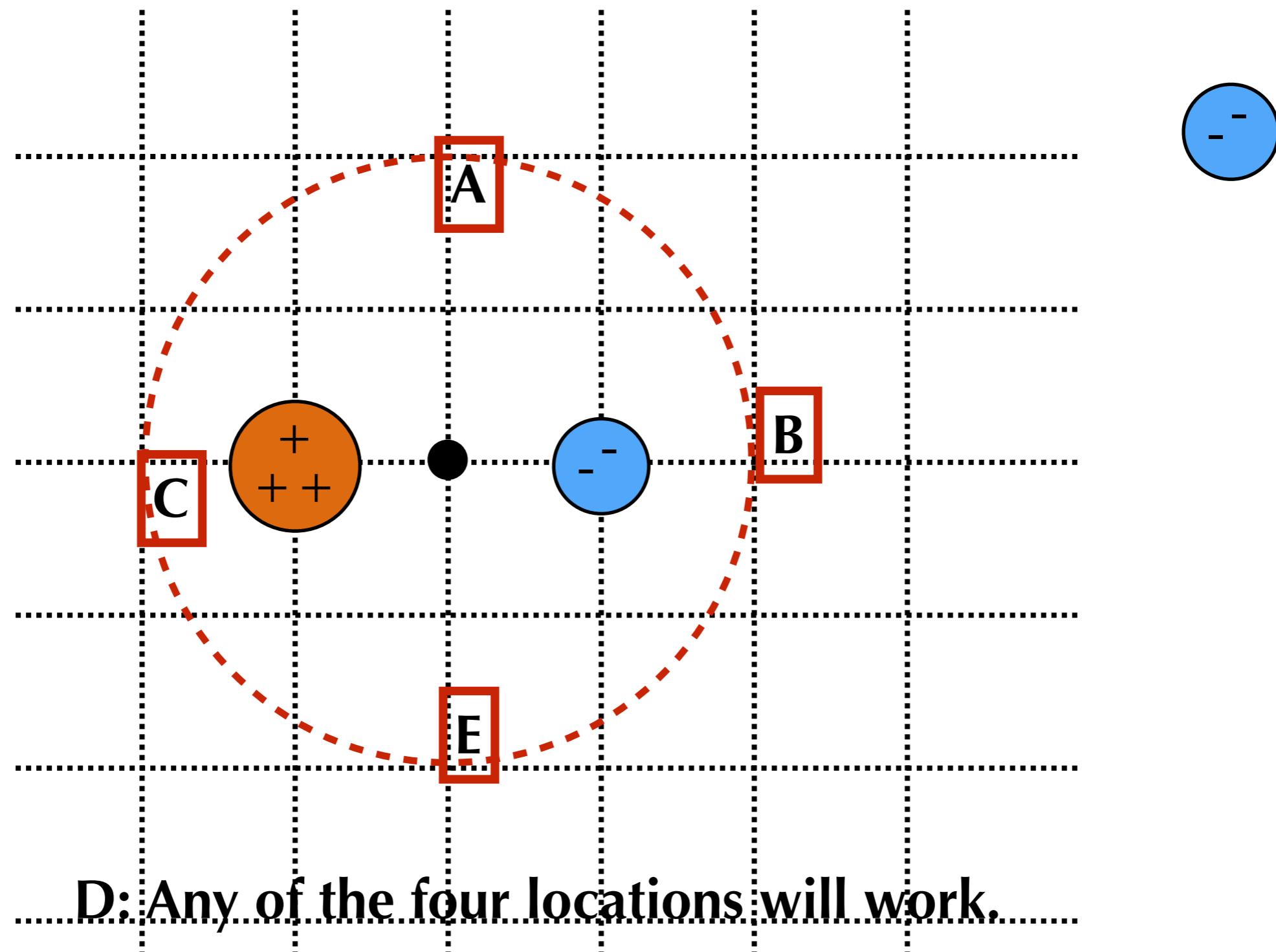
Where should I place this charge so that the electric potential at the dot is zero?



D: Any of the four locations will work.

## Question #19

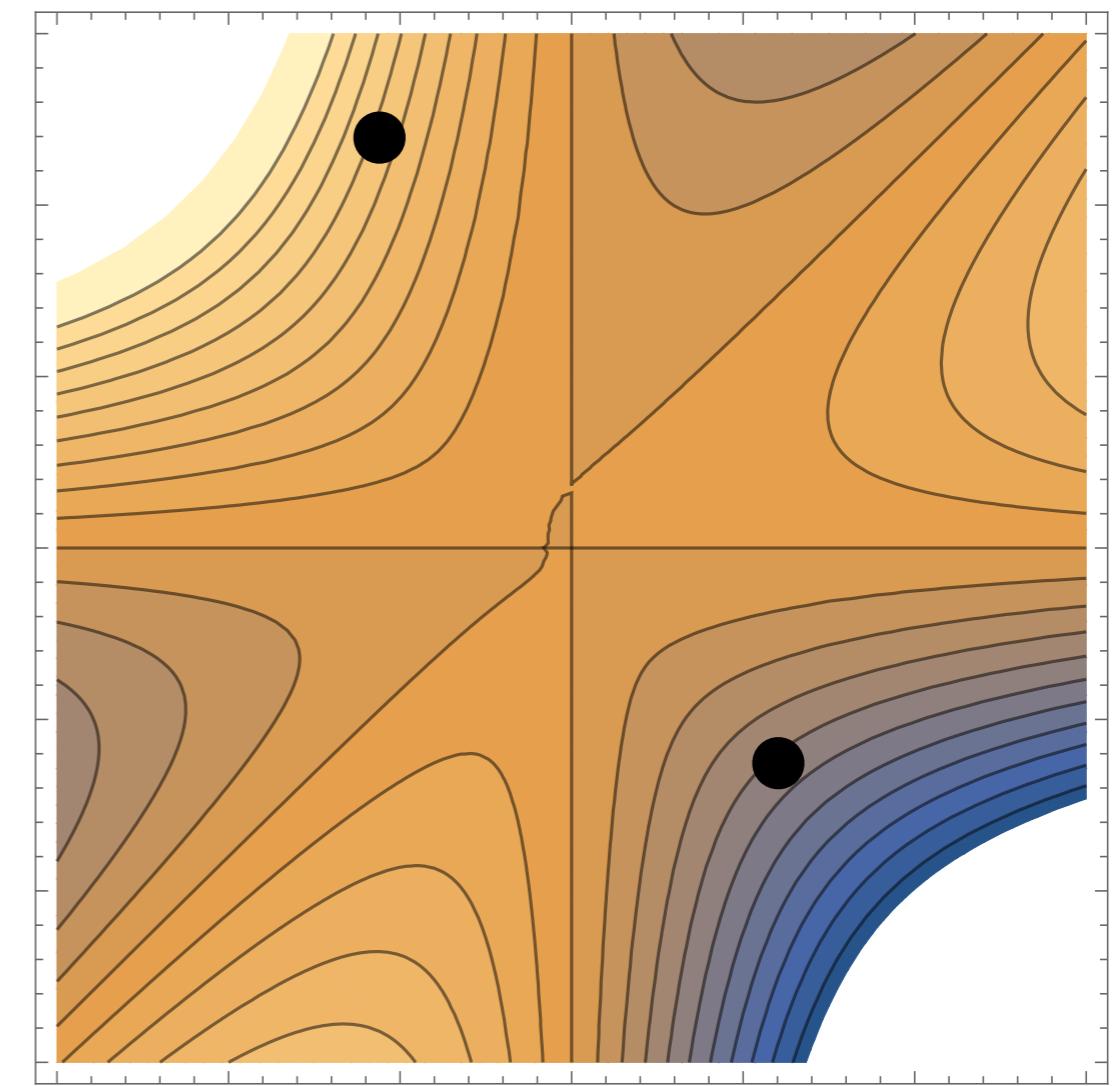
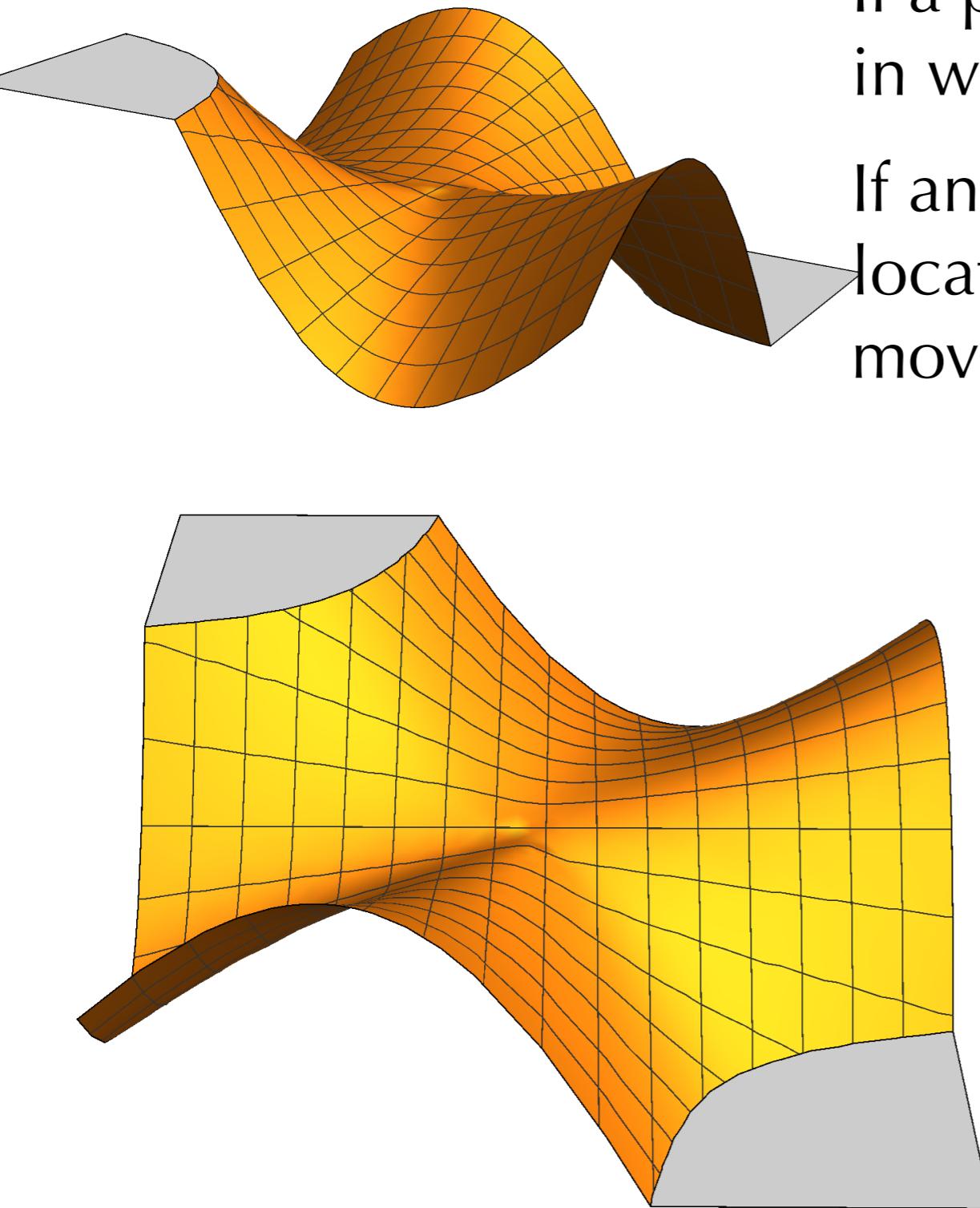
Where should I place this charge so that the electric potential at the dot is zero?



# Electric Potential

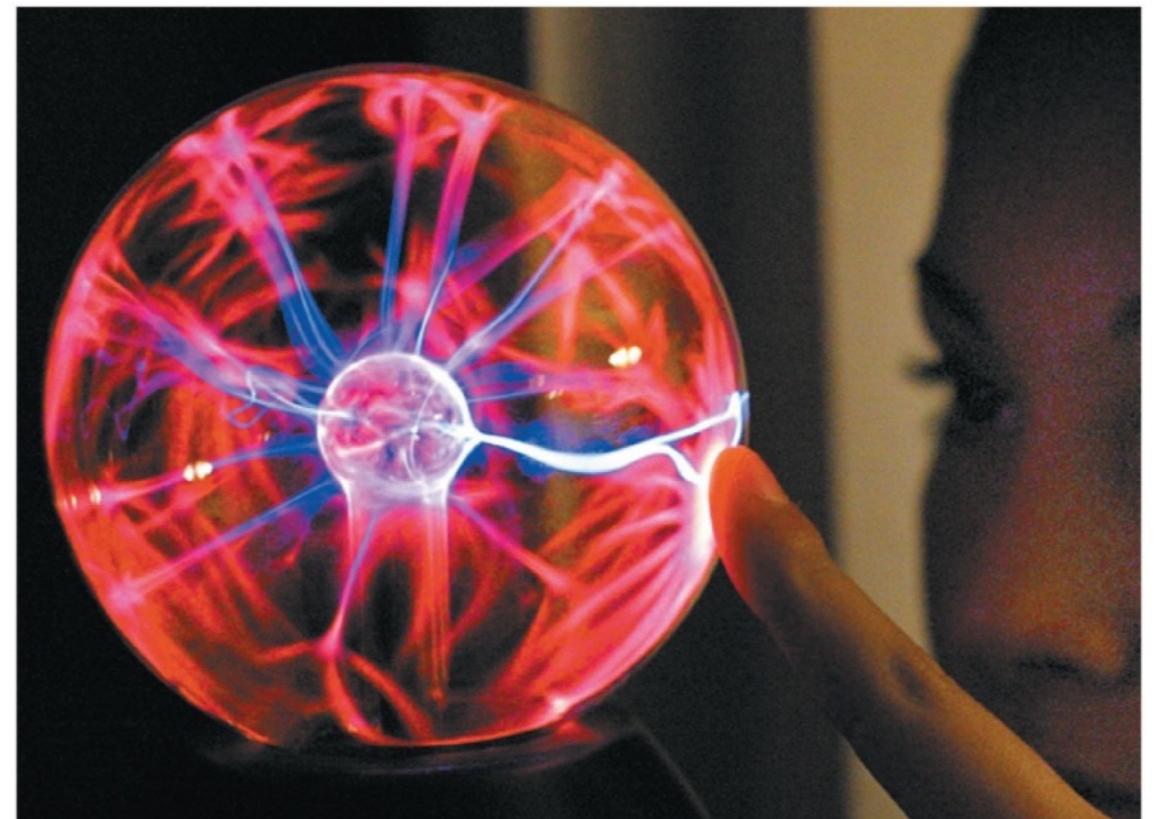
If a proton were placed at these locations, in which direction would it move?

If an electron were placed at these locations, in which direction would it move?



# Electric Potential of sphere of charge

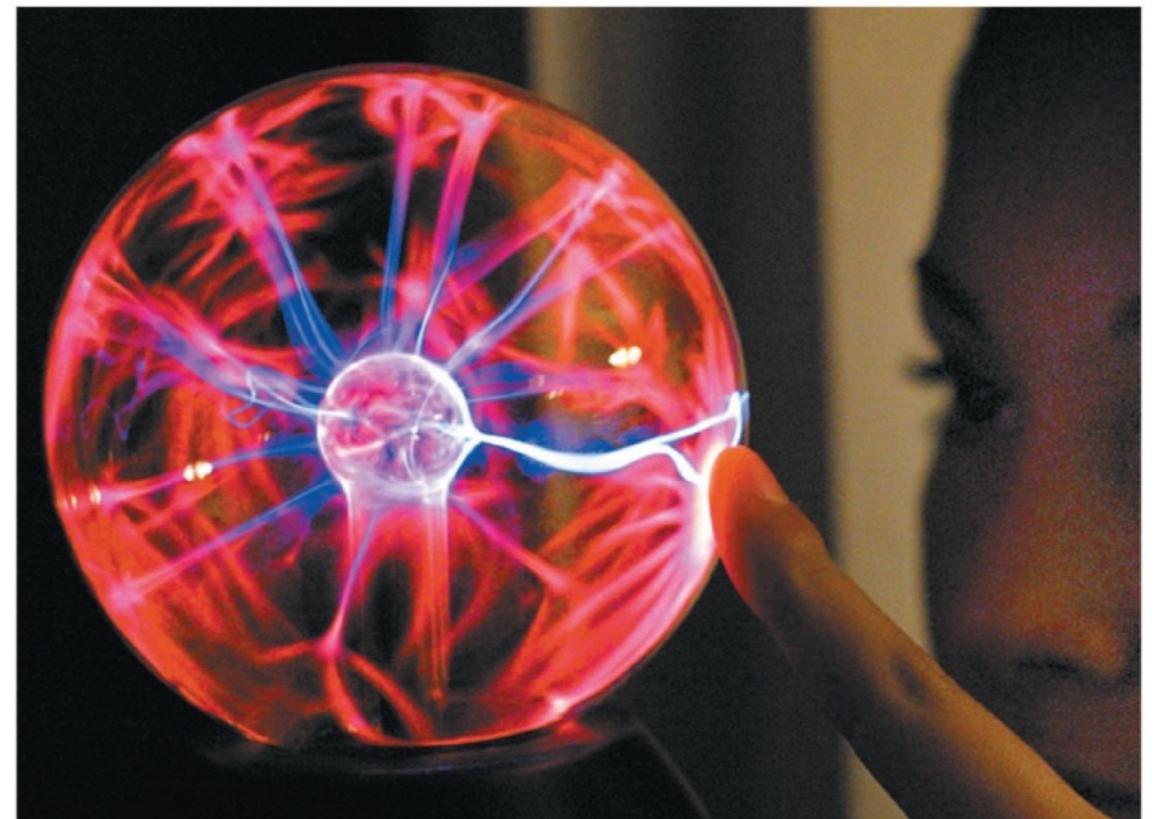
$$V = \frac{1}{4\pi\epsilon_0} \frac{Q}{r} \quad \text{outside}$$



# Electric Potential of sphere of charge

$$V = \frac{1}{4\pi\epsilon_0} \frac{Q}{r} \quad \text{outside}$$

$$V_0 = \frac{1}{4\pi\epsilon_0} \frac{Q}{R}$$

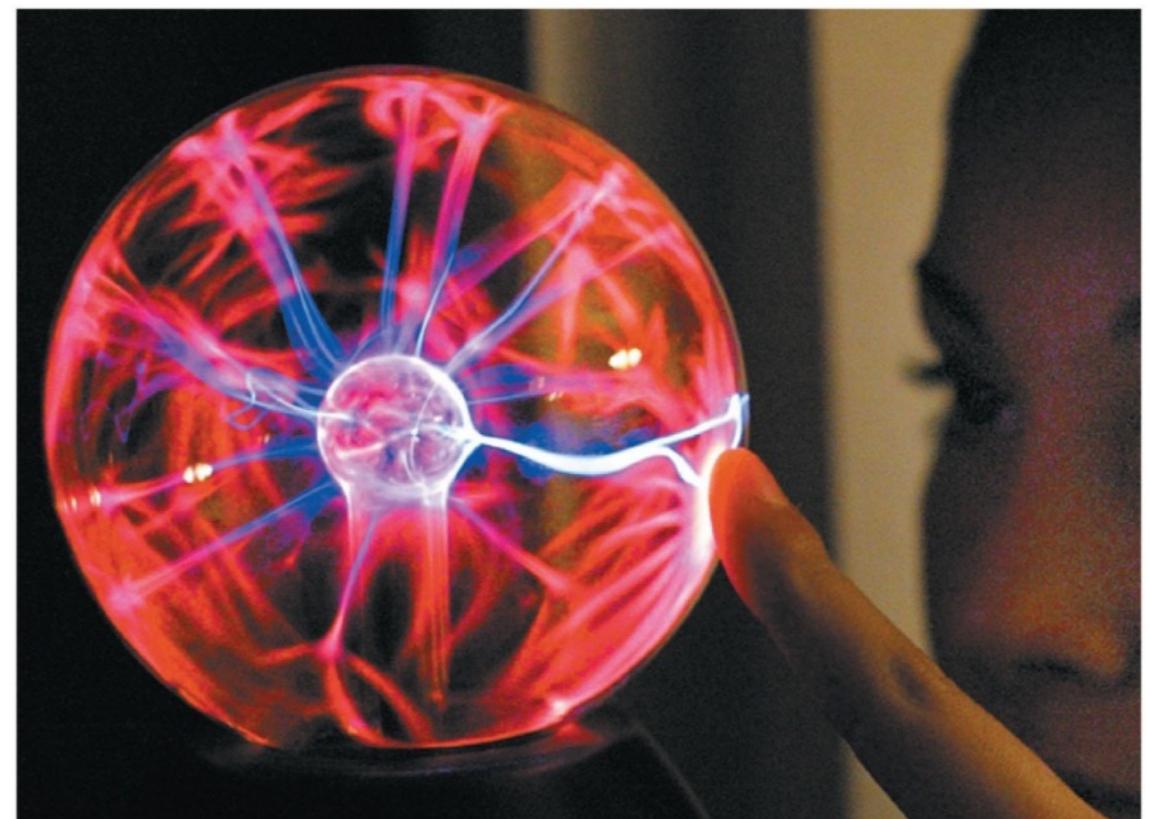


# Electric Potential of sphere of charge

$$V = \frac{1}{4\pi\epsilon_0} \frac{Q}{r} \quad \text{outside}$$

$$V_0 = \frac{1}{4\pi\epsilon_0} \frac{Q}{R}$$

$$Q = V_0 4\pi\epsilon_0 R$$

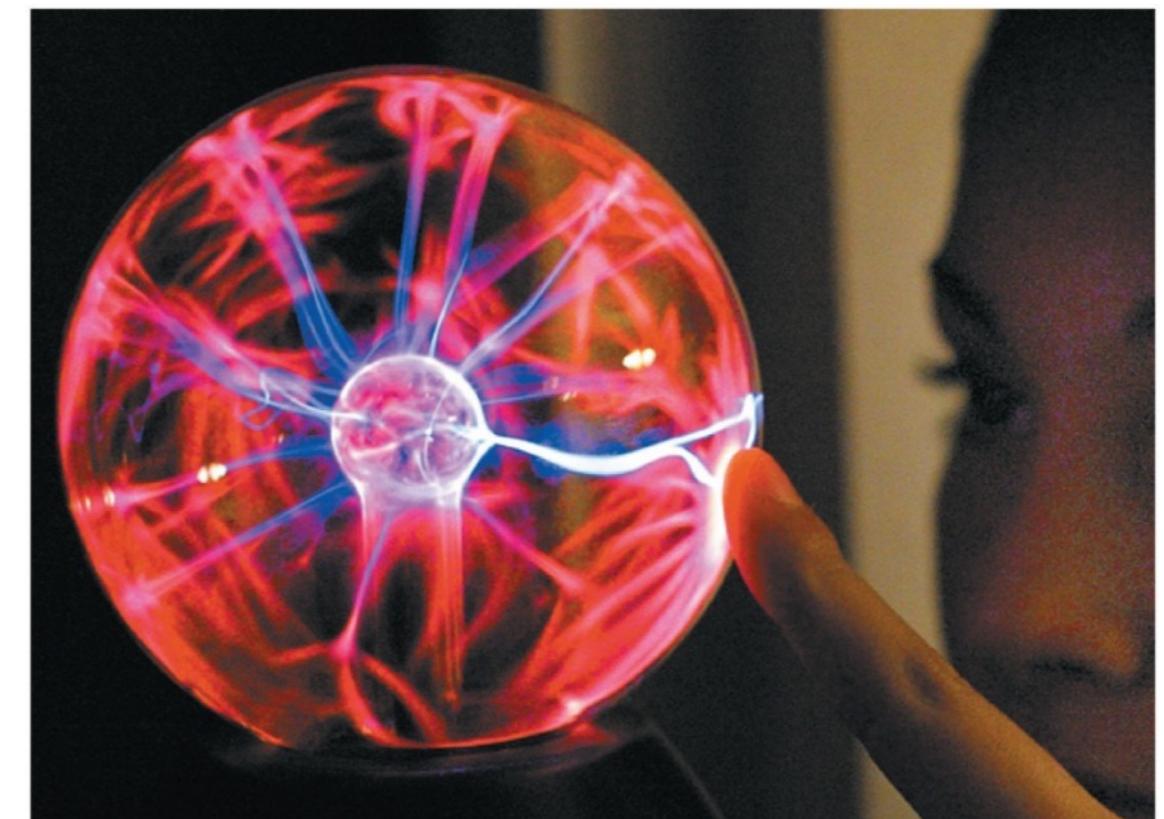


# Electric Potential of sphere of charge

$$V = \frac{1}{4\pi\epsilon_0} \frac{Q}{r} \quad \text{outside}$$

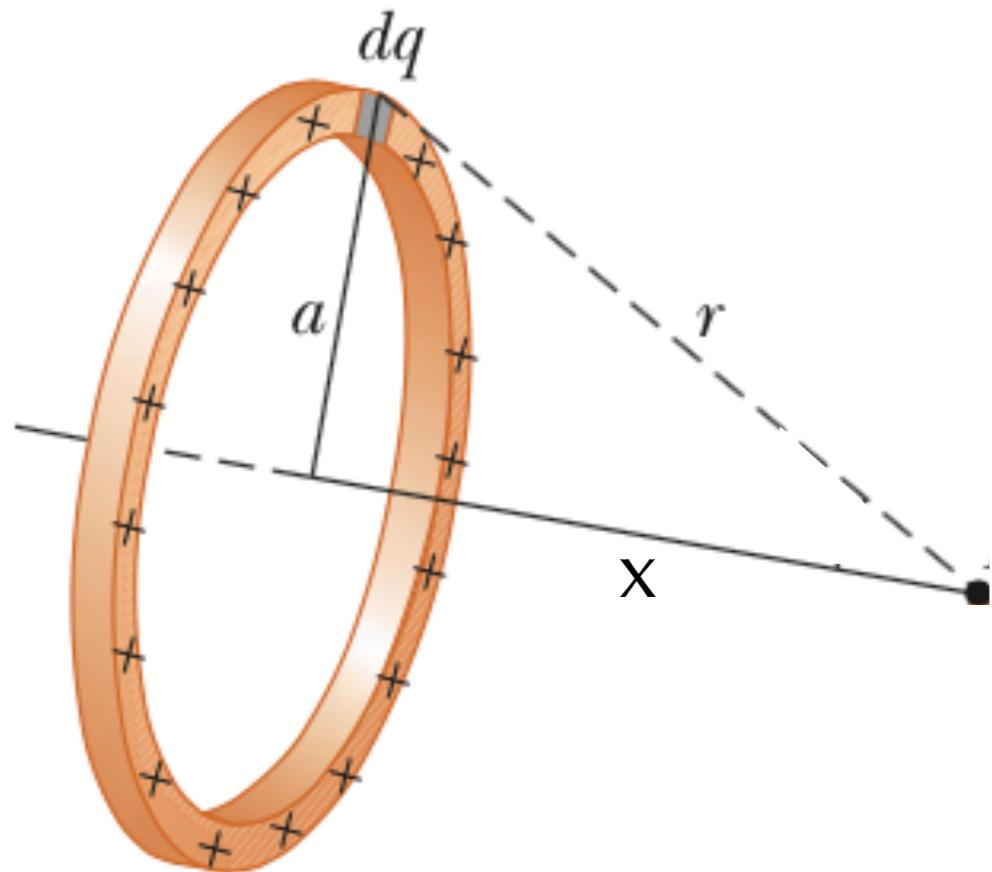
$$V_0 = \frac{1}{4\pi\epsilon_0} \frac{Q}{R}$$

$$Q = V_0 4\pi\epsilon_0 R$$

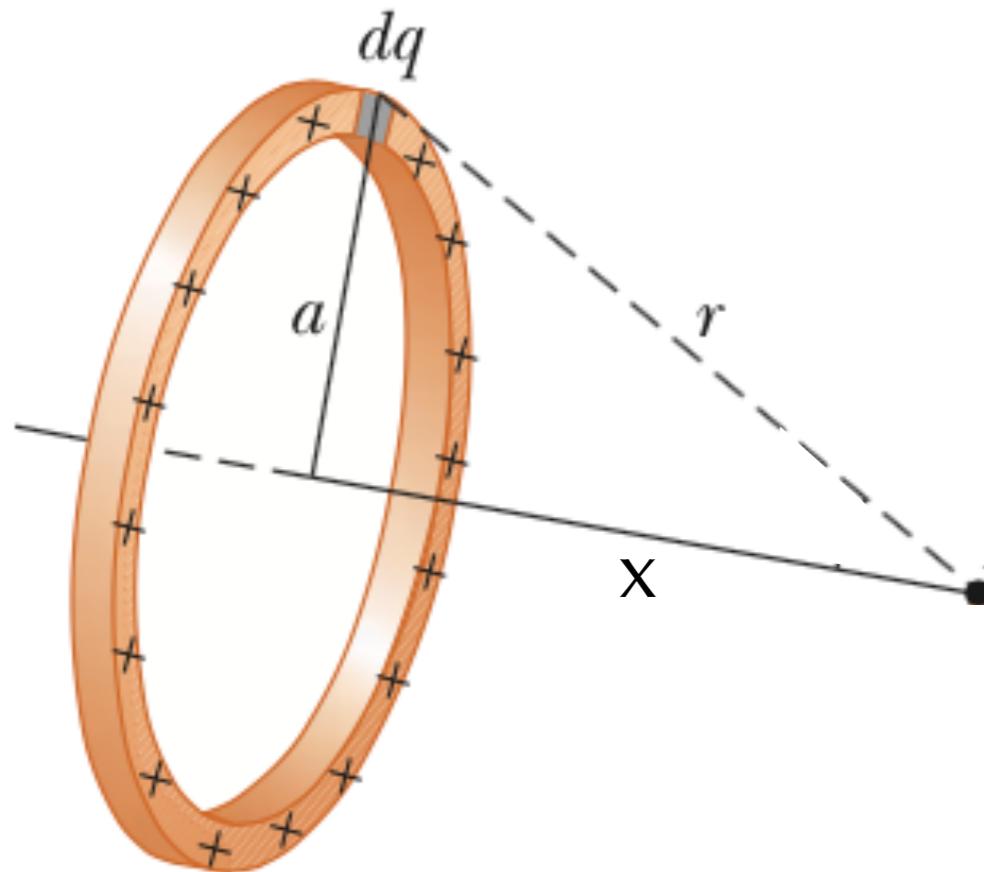


$$V = \frac{R}{r} V_0 \quad \text{potential of a charged sphere}$$

Can you calculate the electric potential due to this ring of charge?



Can you calculate the electric potential due to this ring of charge?



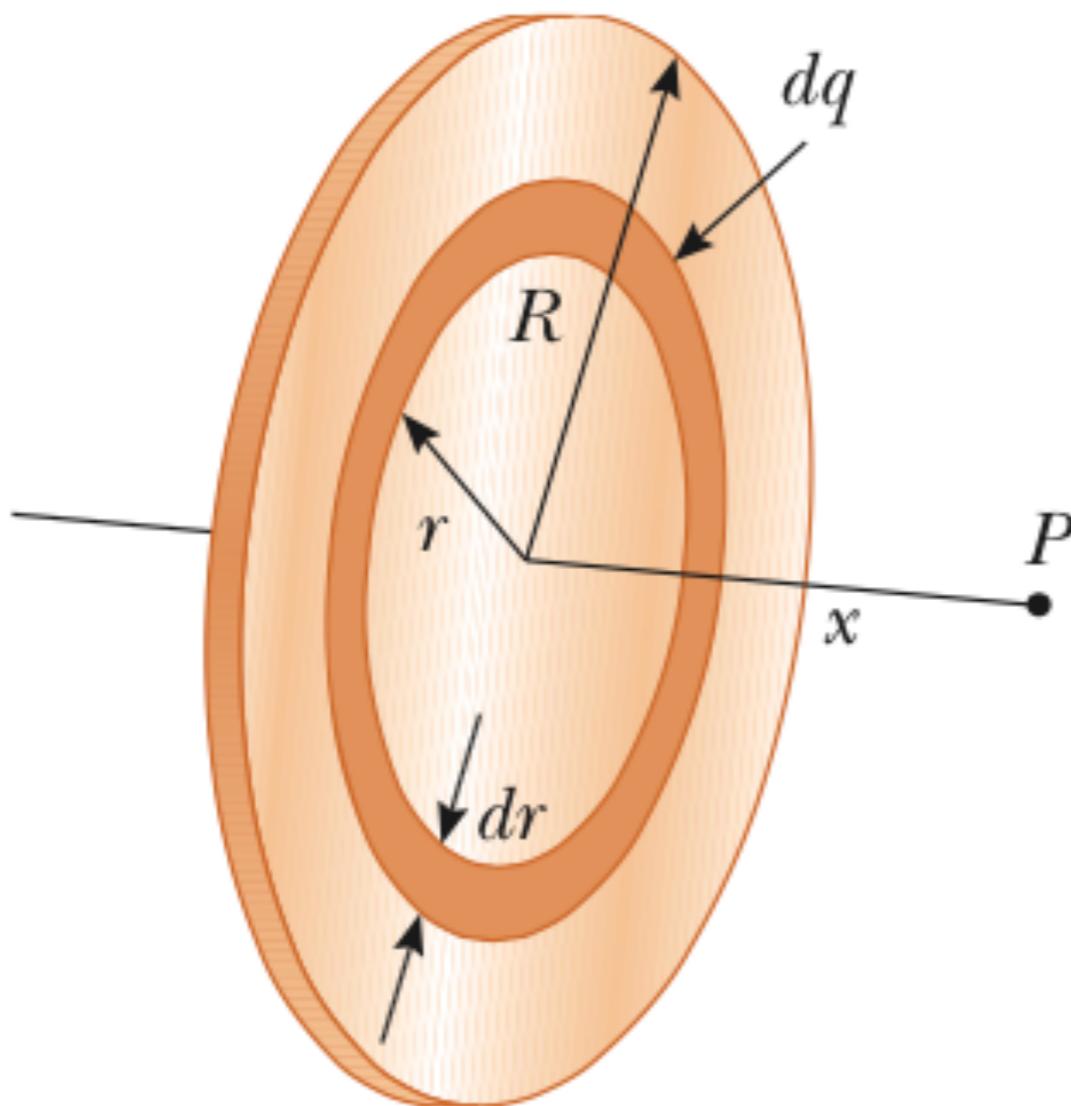
$$V = \frac{kq}{\sqrt{x^2 + a^2}}$$

$R = 17.5 \text{ mm}$

$Q = + 5.00 \text{ nC}$

Find the potential of this disk at  $x$  ?

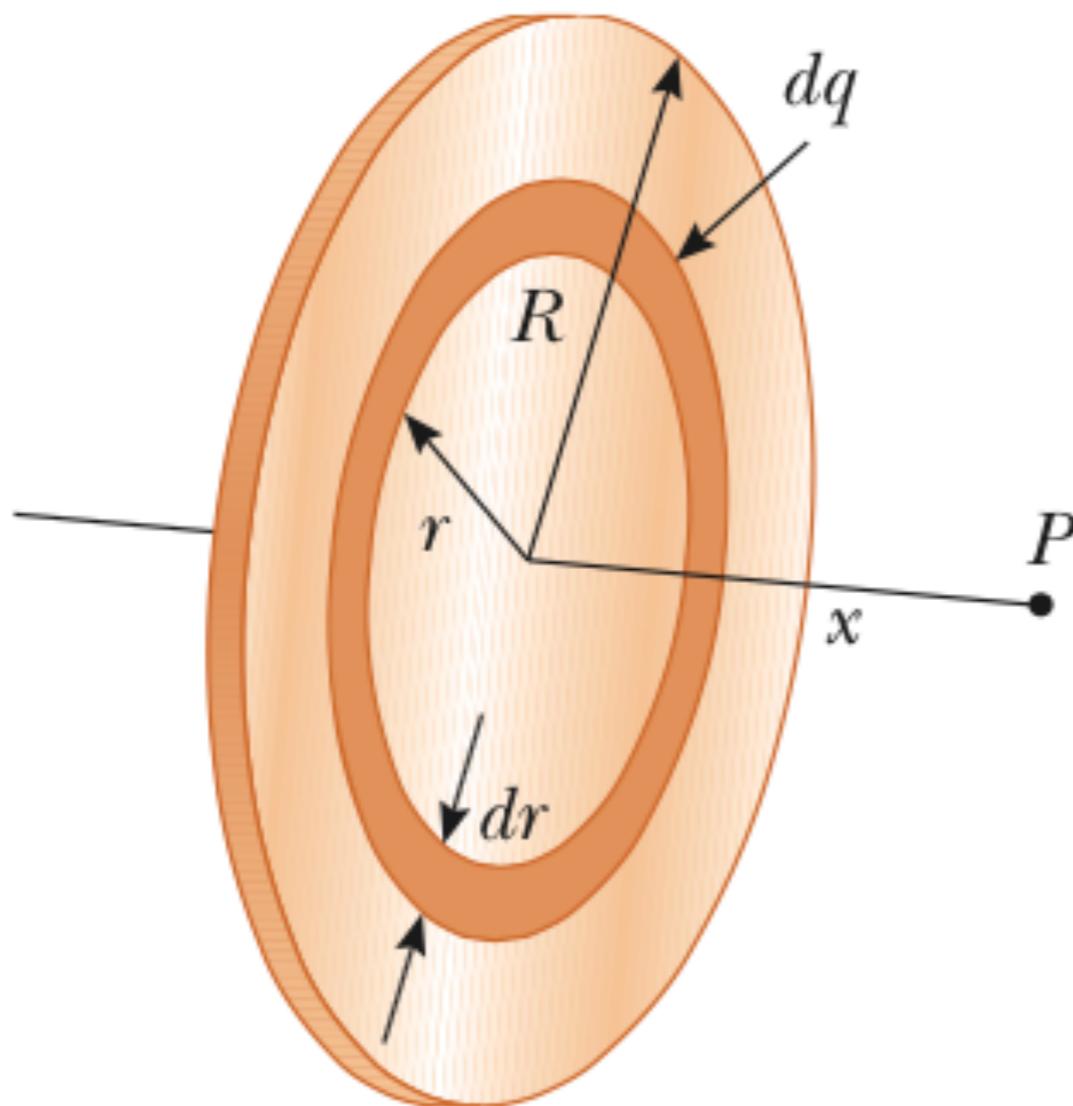
Evaluate at  $x=0$  and  $x = 1.00 \text{ cm}$ .



$R = 17.5 \text{ mm}$

$Q = + 5.00 \text{ nC}$

Find the potential of this disk at  $x$  ?



Evaluate at  $x=0$  and  $x = 1.00 \text{ cm}$ .

$$V = \frac{Q}{2\pi\epsilon_0 R^2} (\sqrt{R^2 + x^2} - x)$$

$$\int \vec{E} \cdot d\vec{A} = \frac{q_{\text{in}}}{\epsilon_0}$$

$$\rho=\frac{Q}{V}\qquad\qquad\lambda=\frac{Q}{L}\\[1mm]\vec{E}=\frac{kq}{r^2}\hat{r}$$

$$\Phi_e=\int \vec{E} \cdot d\vec{A}$$

$$U=\frac{kq_1q_2}{r}\qquad\qquad U=Vq\\[1mm] V=\frac{kq}{r}\qquad\qquad dV=\frac{kdq}{r}$$

$$dE=\frac{k dq}{r^2}\qquad\qquad \eta=\frac{Q}{A}\qquad\qquad U=-\vec{p}\!\cdot\!\vec{E}$$

$$\vec{F}=\vec{E}q$$

9

$$\int \vec{E} \cdot d\vec{A} = \frac{q_{\text{in}}}{\epsilon_0}$$

2

$$\rho = \frac{Q}{V}$$

$$\lambda = \frac{Q}{L} \boxed{5}$$

$$\vec{E} = \frac{kq}{r^2} \hat{r} \boxed{14}$$

11

$$\Phi_e = \int \vec{E} \cdot d\vec{A}$$

1

$$U = \frac{kq_1 q_2}{r}$$

$$U = Vq \boxed{13}$$

$$\boxed{6} \vec{\tau} = \vec{p} \times \vec{E}$$

$$V = \frac{kq}{r} \boxed{10}$$

$$dV = \frac{kdq}{r} \boxed{8}$$

$$\boxed{3} dq = \frac{kdq}{r^2}$$

$$\eta = \frac{Q}{A} \boxed{7}$$

$$U = -\vec{p} \cdot \vec{E} \boxed{4}$$

$$\vec{F} = \vec{E}q \boxed{12}$$