



PH 220

Lance Nelson

Important for today

Remember:

- Try to minimize time when I am imparting information and maximize the time when the student is explaining, thinking and doing.
- Ensure that every slide has a clearly-defined purpose.
- Ask concise, well thought-out, and thought-provoking questions that cause the student to ponder and ask why.
- Give the student time to ponder silently, ask their neighbor questions and receive instruction from them.

Outcomes

What is a phasor? Difference between instantaneous value and peak value. Rotating phasor illustrates concept of oscillating currents and voltages.

-AC resistor circuit

Summary

State in words and in math, the meaning of these laws.

Gauss's Law

Gauss's Law for magnetism

Faraday's Law

Ampere-Maxwell

Lorentz force law

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$$(\Phi_e)_{\text{closed surface}} = \oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{in}}}{\epsilon_0}$$

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Gauss's Law

$$(\Phi_m)_{\text{closed surface}} = \oint \vec{B} \cdot d\vec{A} = 0$$

Gauss's Law for magnetism

$$\mathcal{E} = \oint \vec{E} \cdot d\vec{s} = -\frac{d\Phi_m}{dt}$$

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Faraday's Law

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 (I_{\text{through}} + \epsilon_0 \frac{d\Phi_E}{dt})$$

Ampere-Maxwell

Lorentz force law

Summary

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Faraday's Law

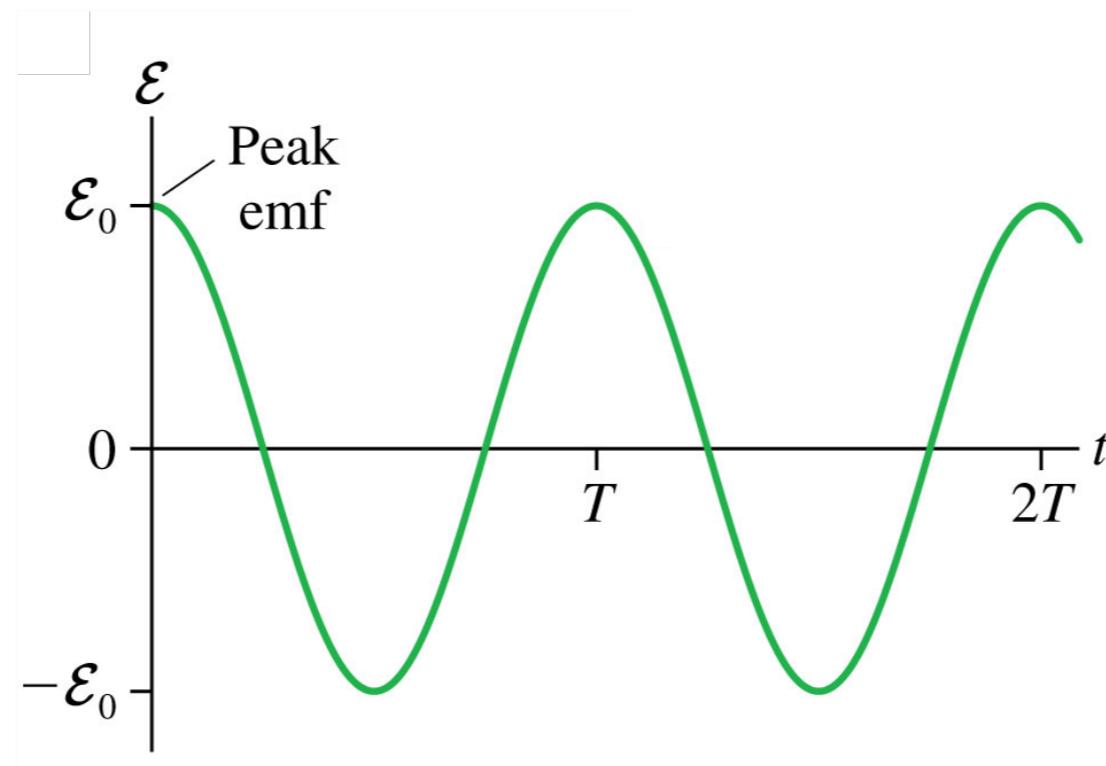
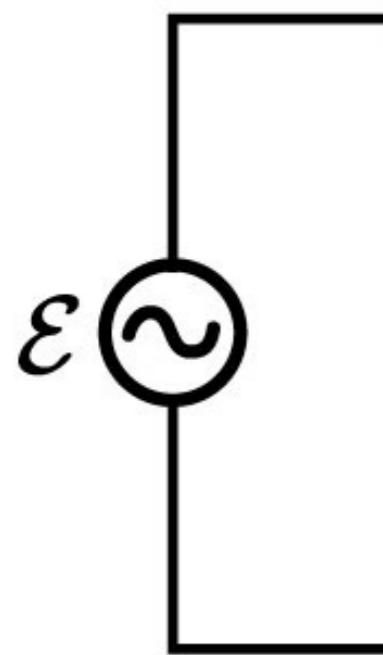
$$\oint \vec{B} \cdot d\vec{s} = \mu_0 (I_{\text{through}} + \epsilon_0 \frac{d\Phi_E}{dt})$$

Ampere-Maxwell

$$F = q(\vec{E} + \vec{v} \times \vec{B})$$

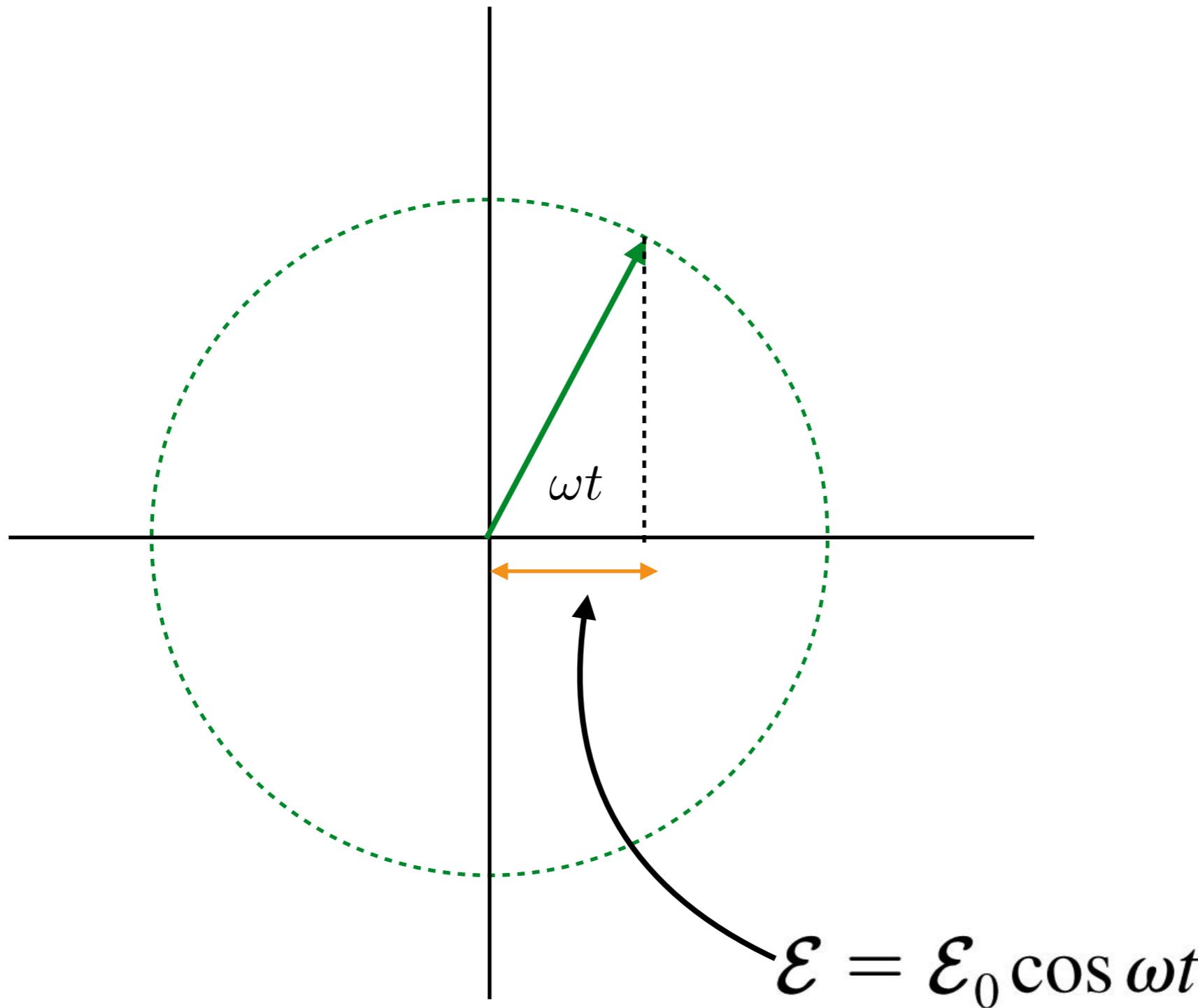
Lorentz force law

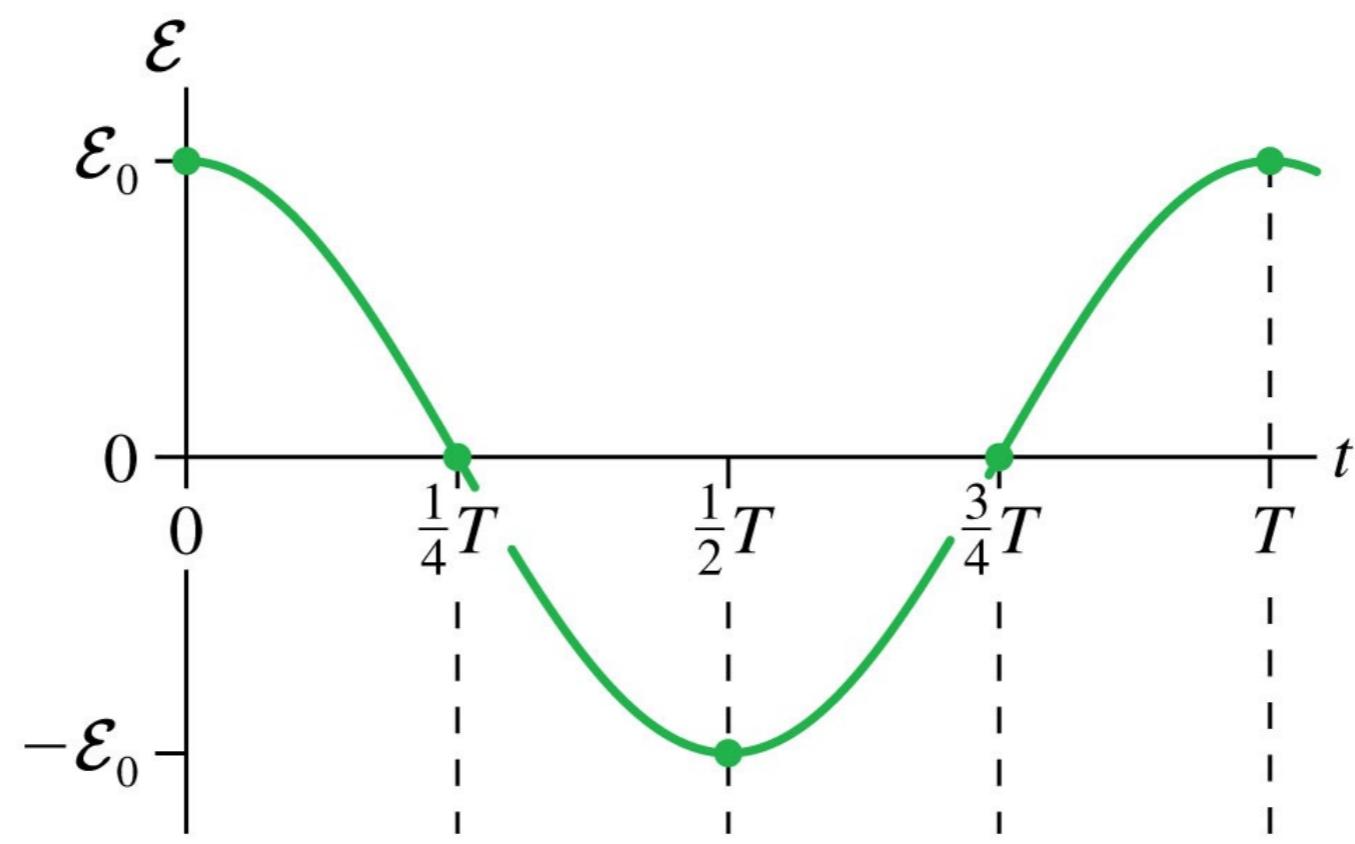
AC sources

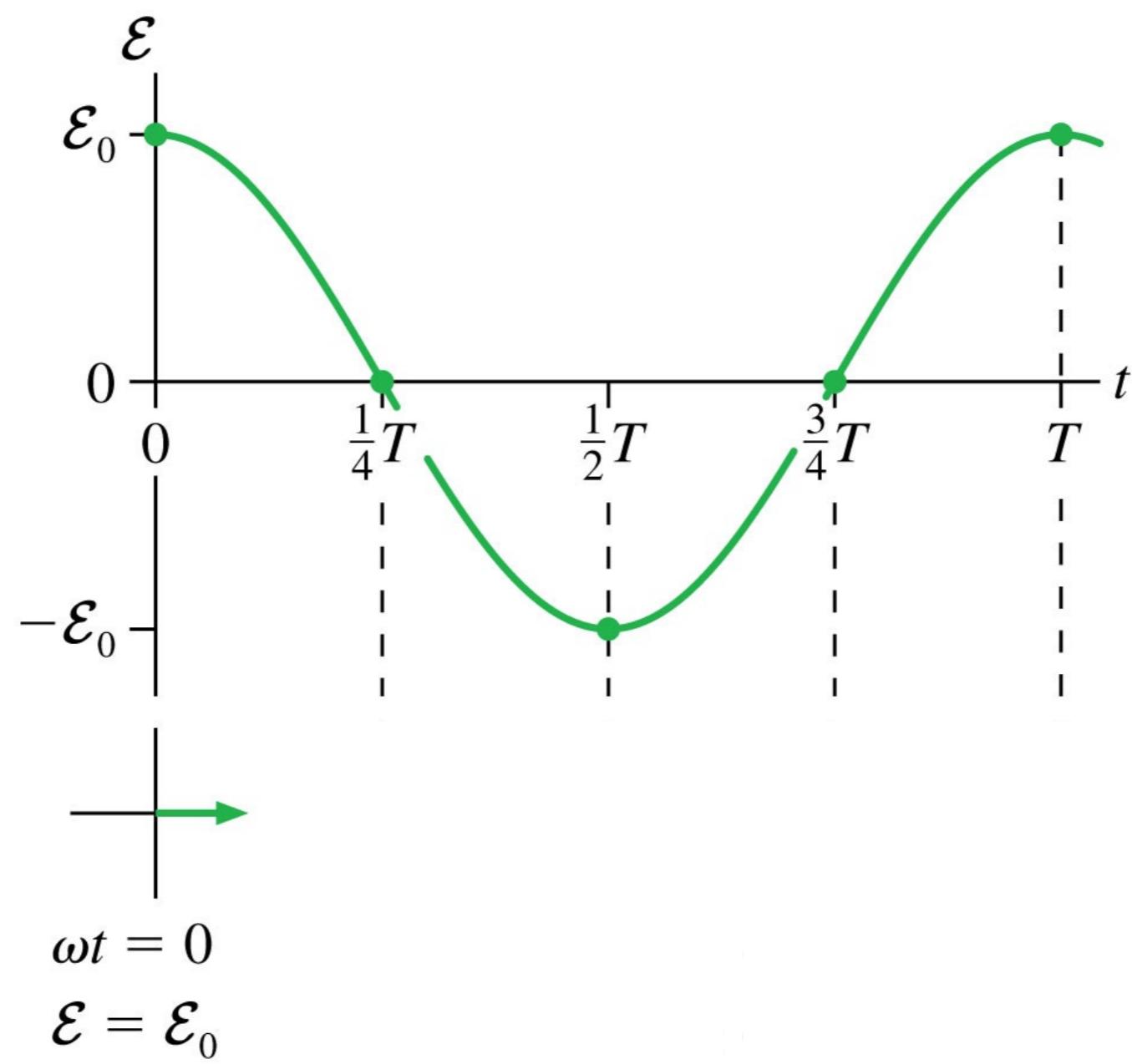


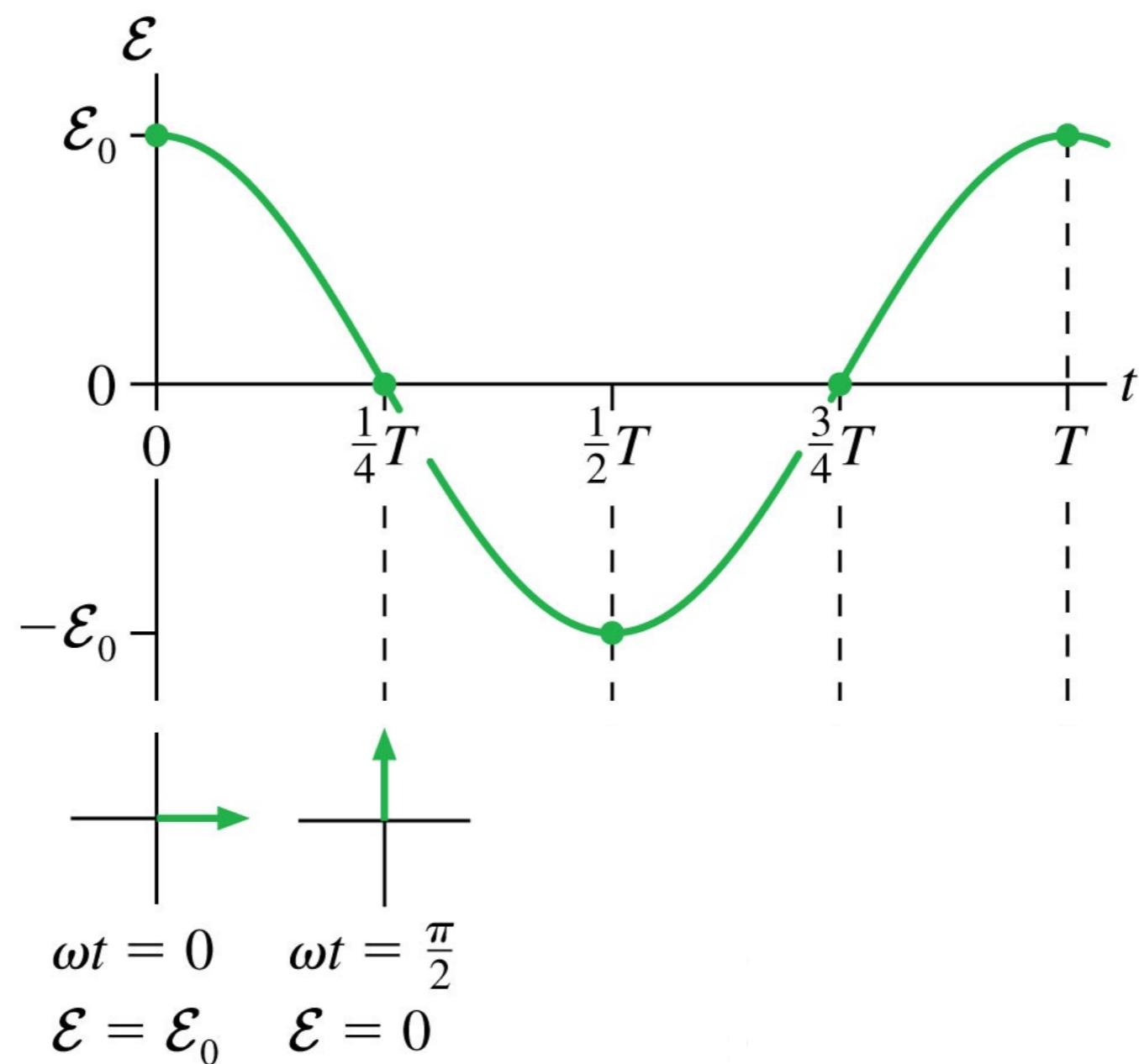
$$\mathcal{E} = \mathcal{E}_0 \cos \omega t$$

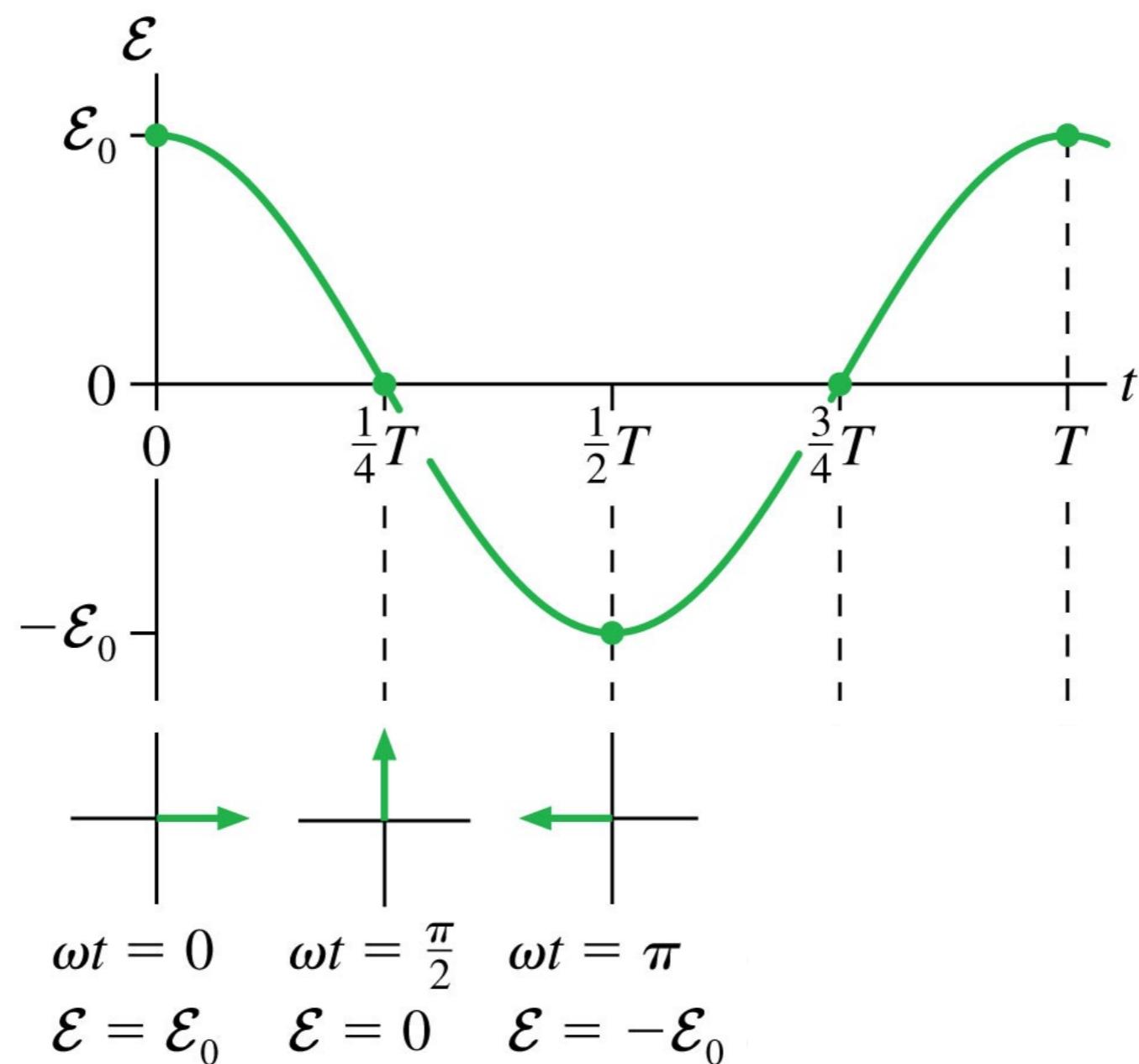
Phasors: Not something from Star Trek

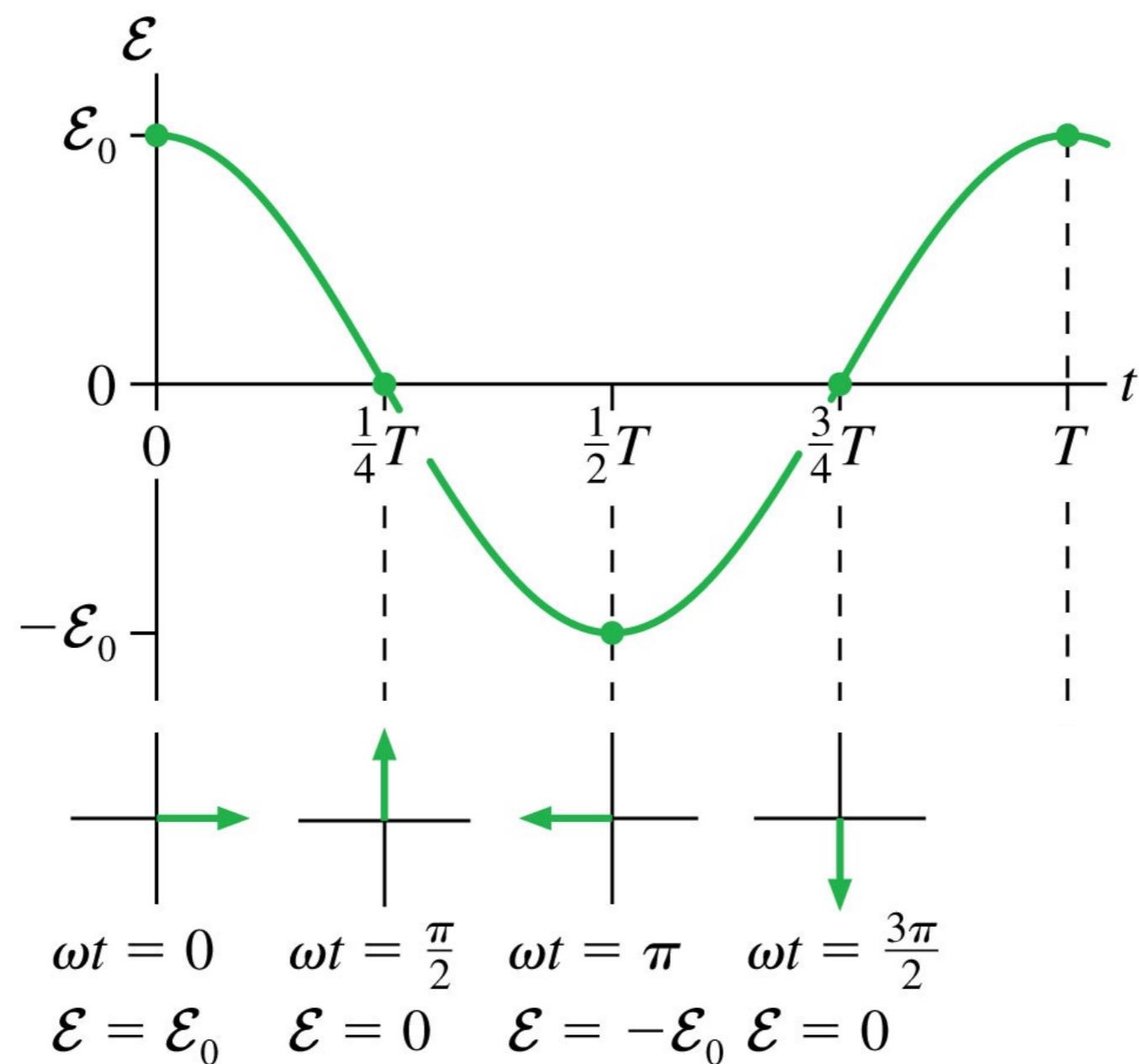


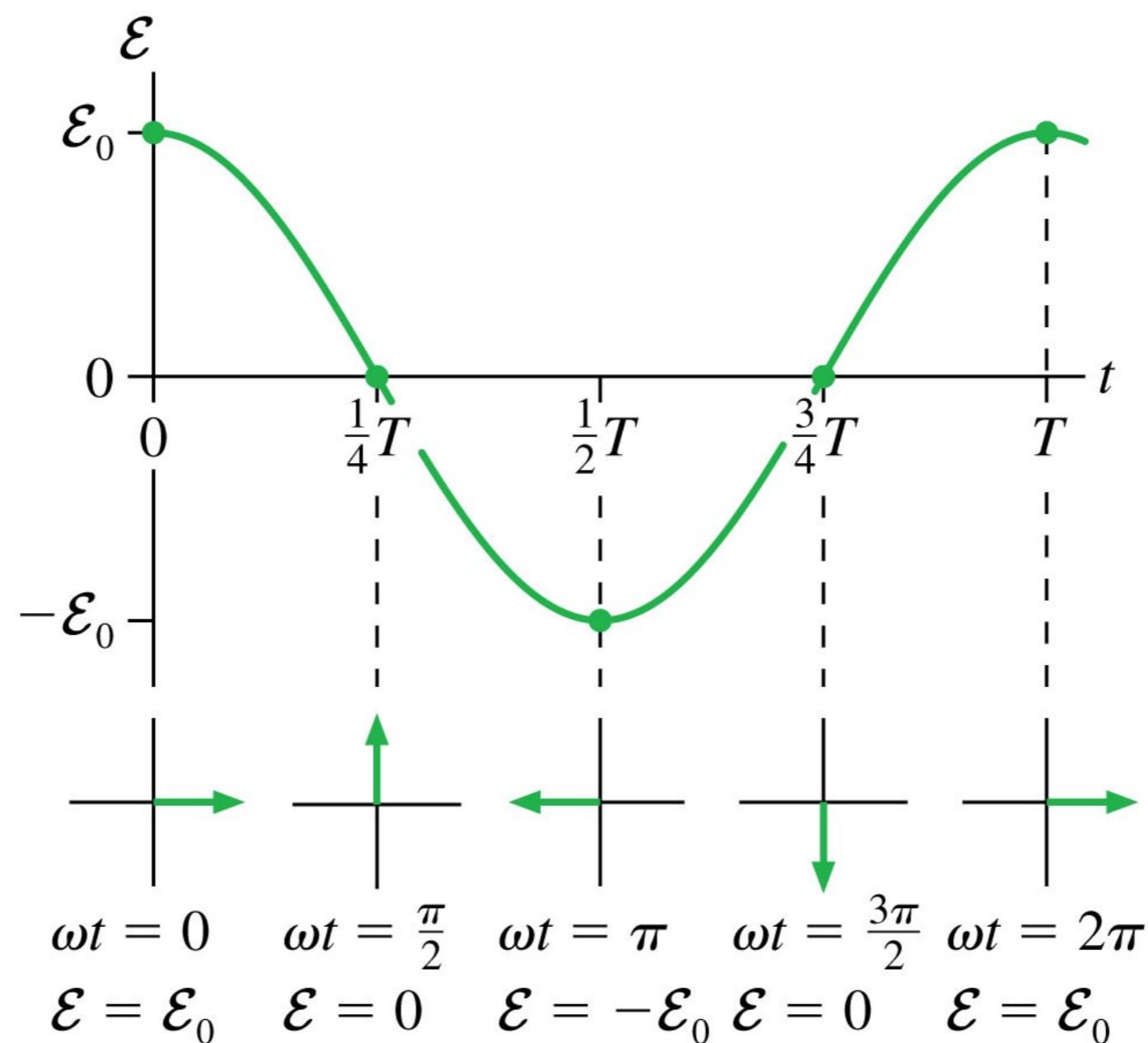








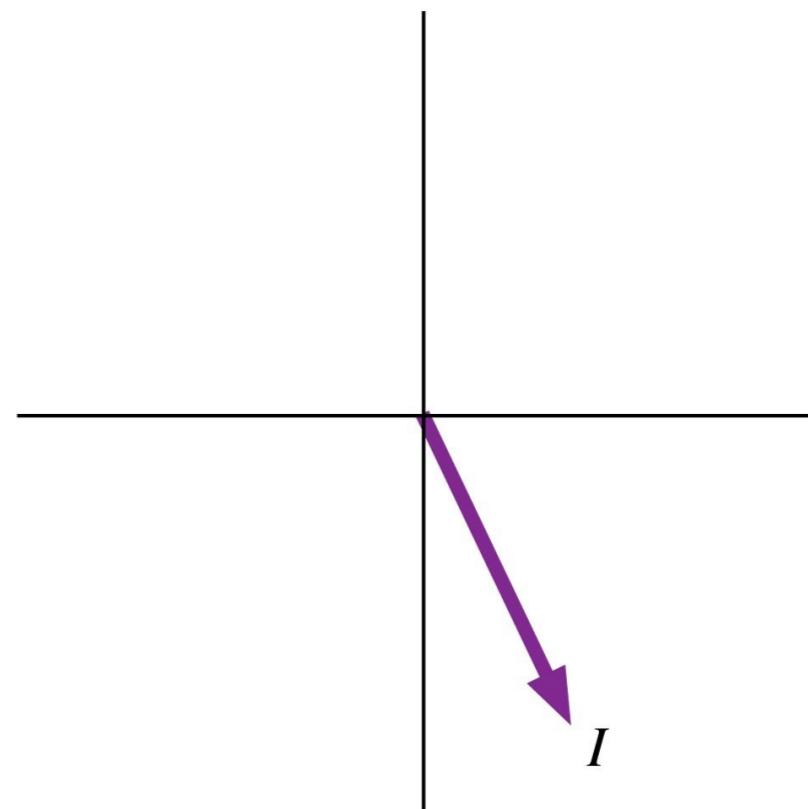




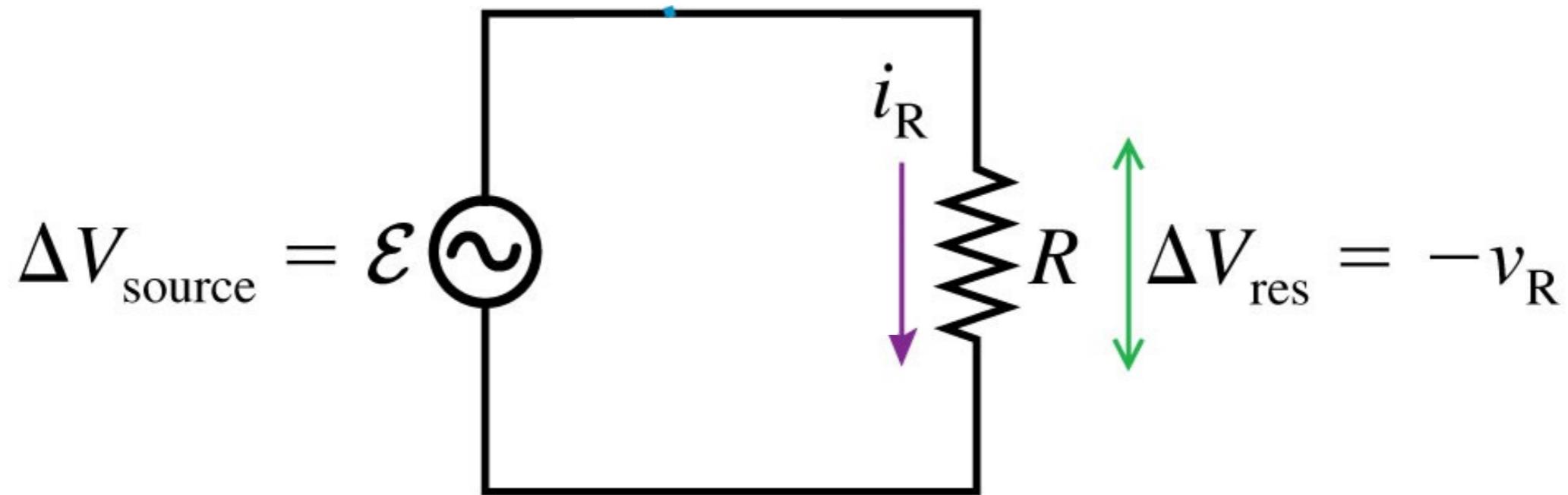
Question #25

This is a current phasor. The magnitude of the instantaneous value of the current is

- A. Increasing.
- B. Decreasing.
- C. Constant.

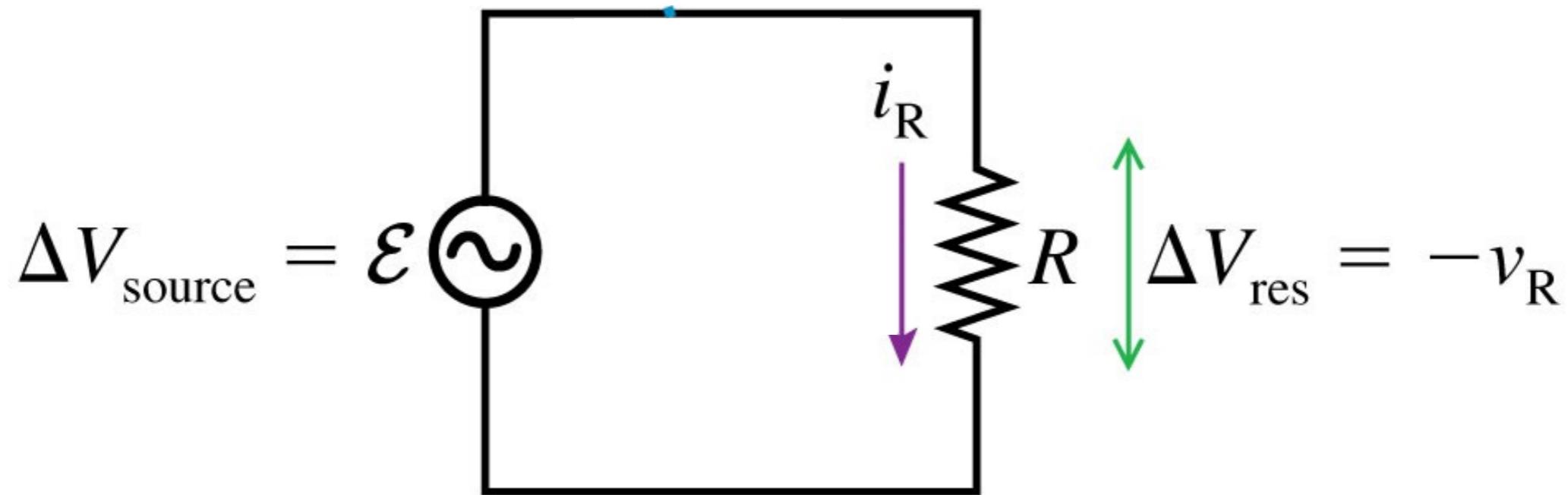


Resistor Circuit



Why little i and little v?

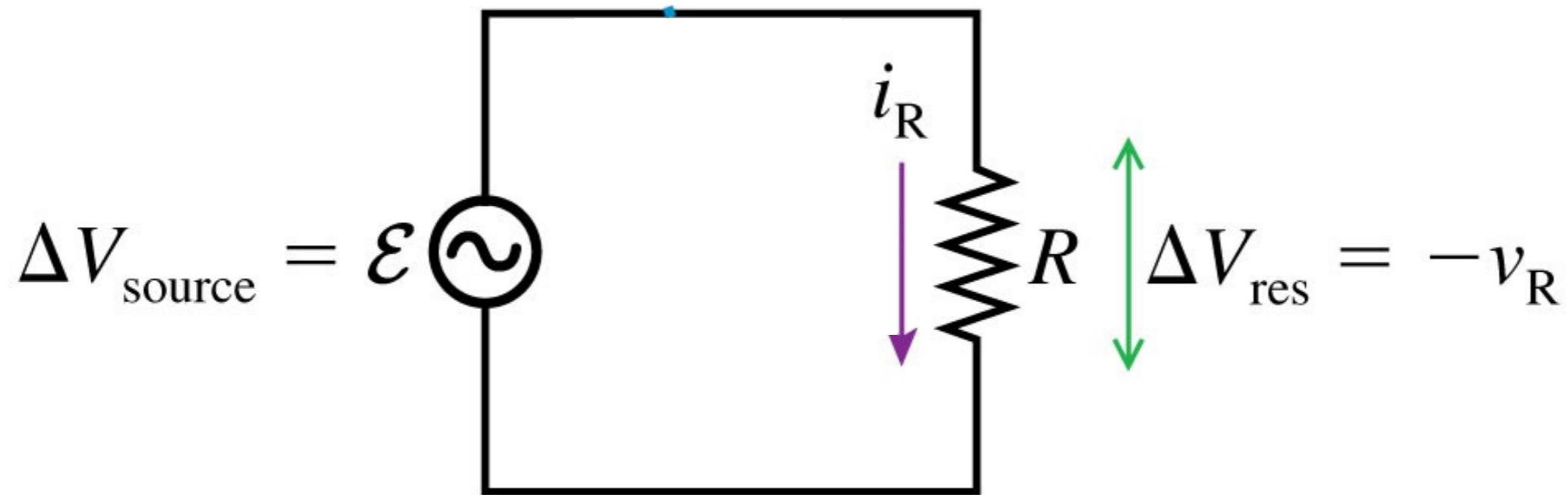
Resistor Circuit



Why little i and little v?

When the current through the resistor is a max/min is the voltage across the resistor a max or a min?

Resistor Circuit

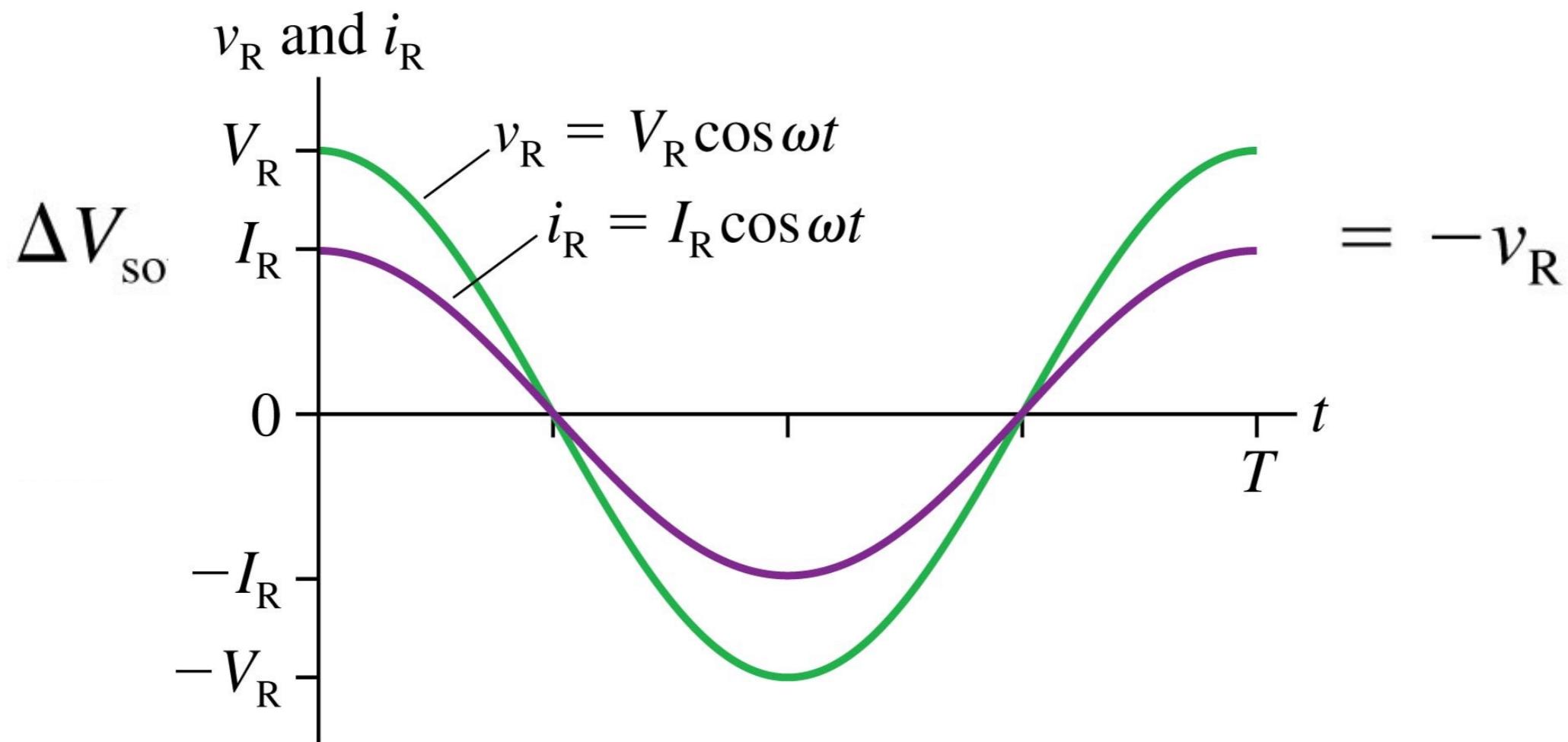


Why little i and little v?

When the current through the resistor is a max/min is the voltage across the resistor a max or a min?

$$i_R = \frac{v_R}{R} = \frac{V_R \cos \omega t}{R} = I_R \cos \omega t$$

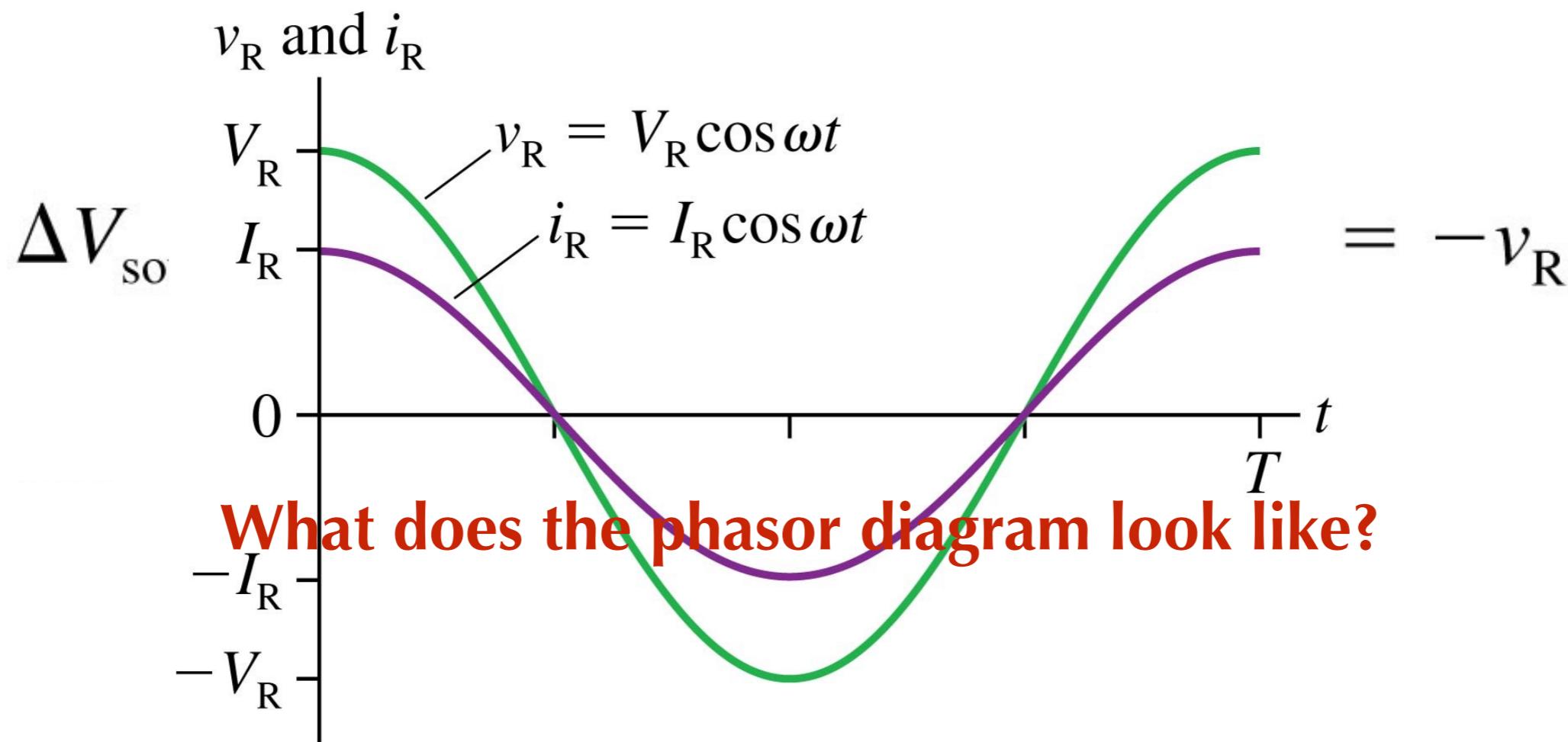
Resistor Circuit



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Resistor Circuit

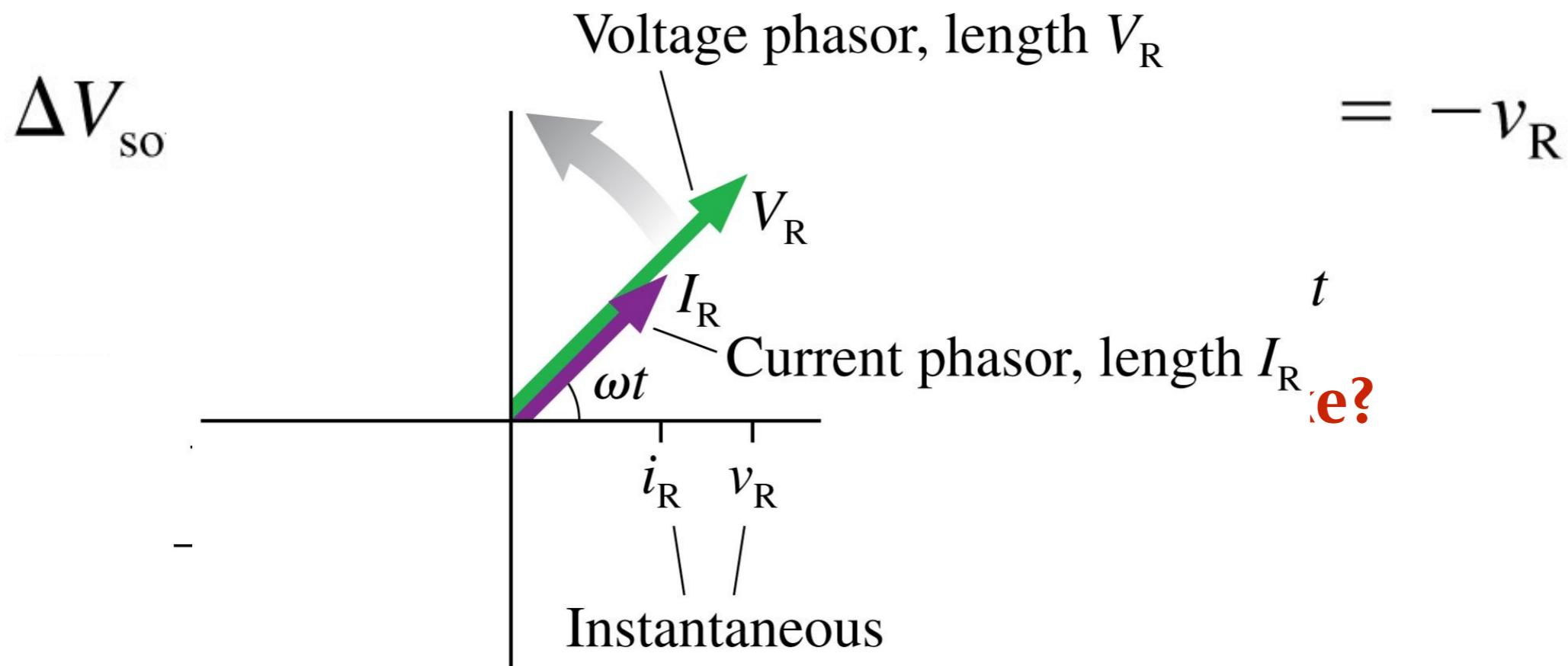


When the current through the resistor is a max/min is the voltage across the resistor a max or a min?

$$i_R = \frac{v_R}{R} = \frac{V_R \cos \omega t}{R} = I_R \cos \omega t$$

Resistor Circuit

v_R and i_R



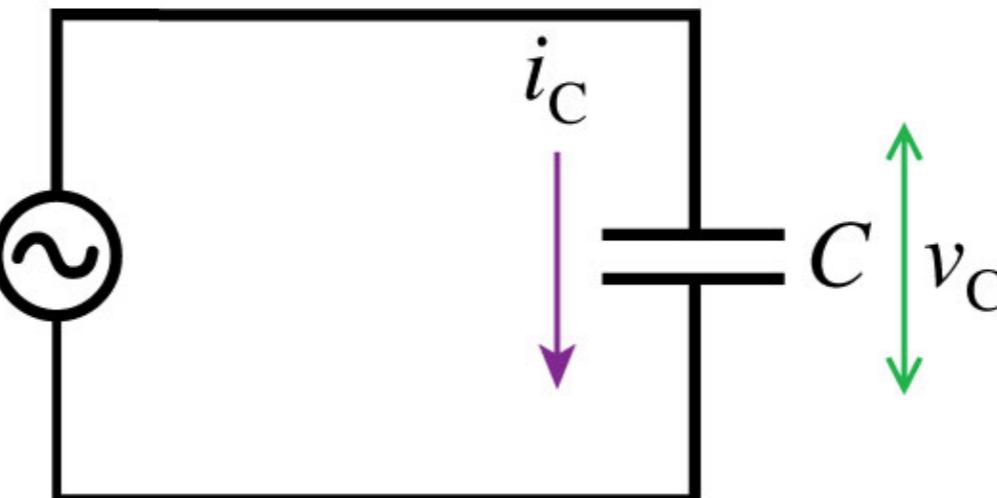
When $\omega t = 90^\circ$, $v_R = 0$ and $i_R = \text{max}$.
When $\omega t = 180^\circ$, $v_R = \text{max}$ and $i_R = 0$.
When $\omega t = 270^\circ$, $v_R = 0$ and $i_R = \text{min}$.
When $\omega t = 360^\circ$, $v_R = \text{max}$ and $i_R = 0$.

Where is the voltage across the resistor a max or a min?

$$i_R = \frac{v_R}{R} = \frac{V_R \cos \omega t}{R} = I_R \cos \omega t$$

Capacitor Circuit

$$\mathcal{E} = \mathcal{E}_0 \cos \omega t$$

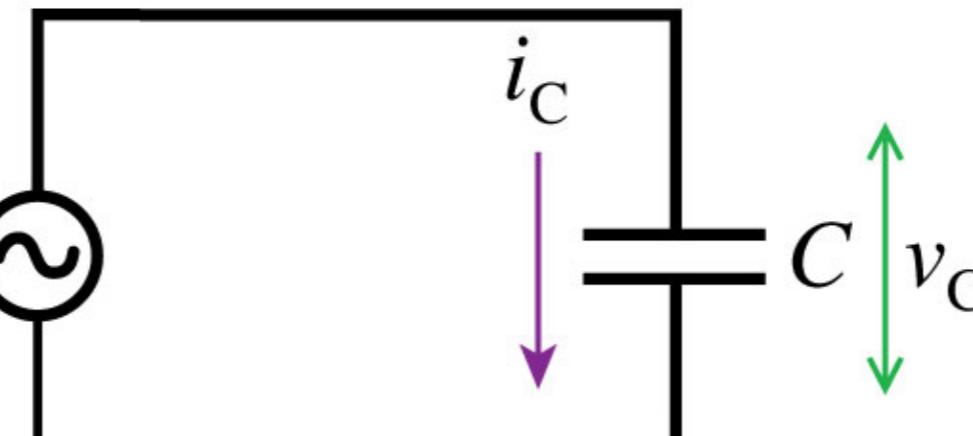


When the current in the circuit is high, the voltage across the capacitor is _____?

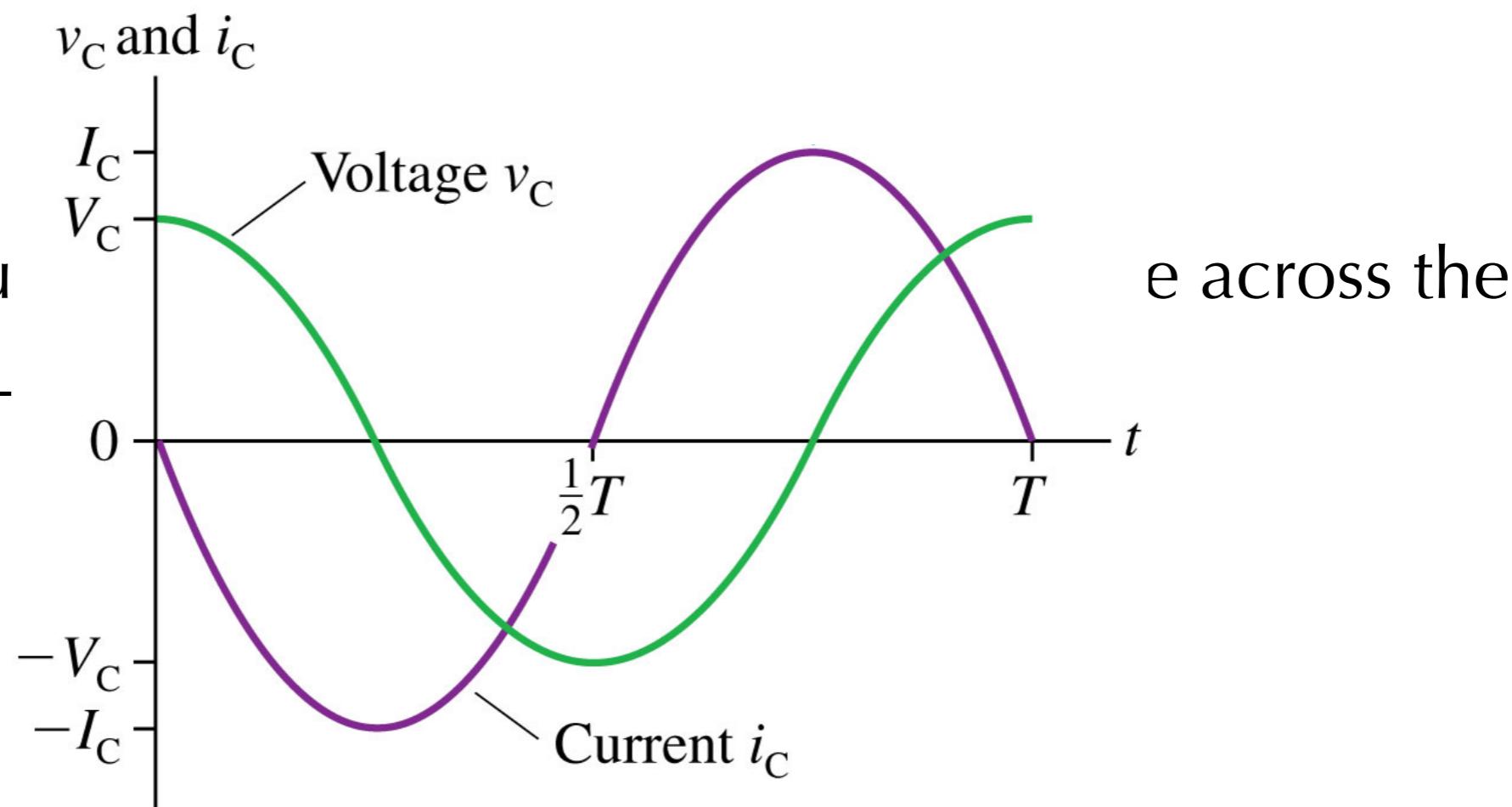
- A- Low
- B- High

Capacitor Circuit

$$\mathcal{E} = \mathcal{E}_0 \cos \omega t$$



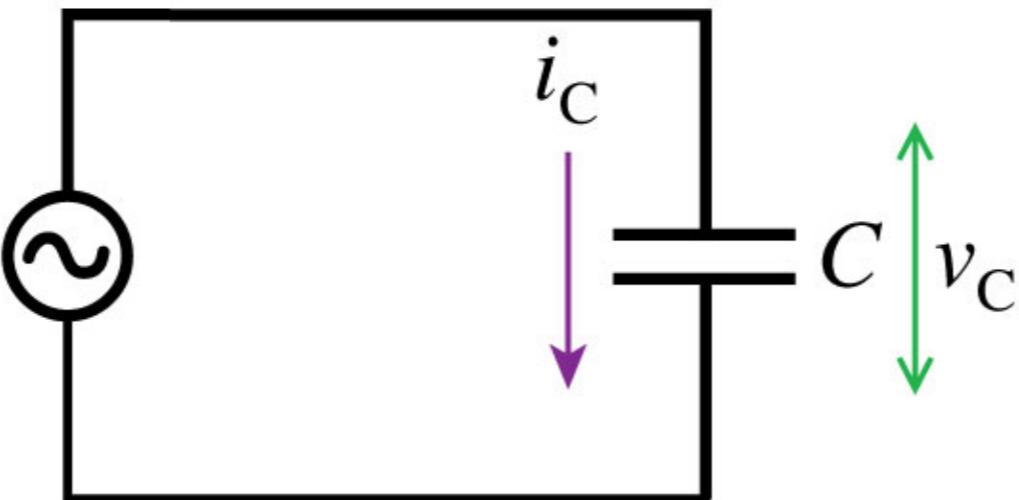
When the current in the capacitor is _



e across the

The Math

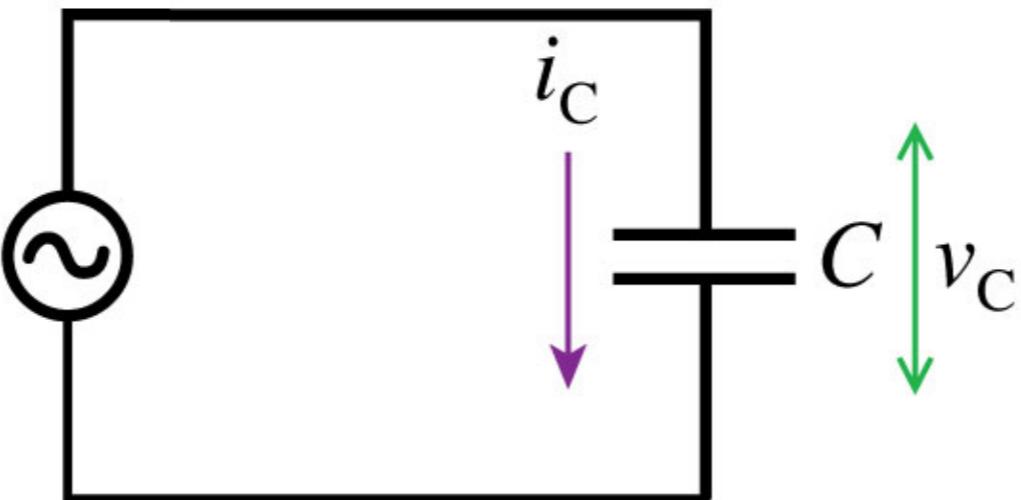
$$\mathcal{E} = \mathcal{E}_0 \cos \omega t$$



$$q = Cv_C = CV_C \cos \omega t$$

The Math

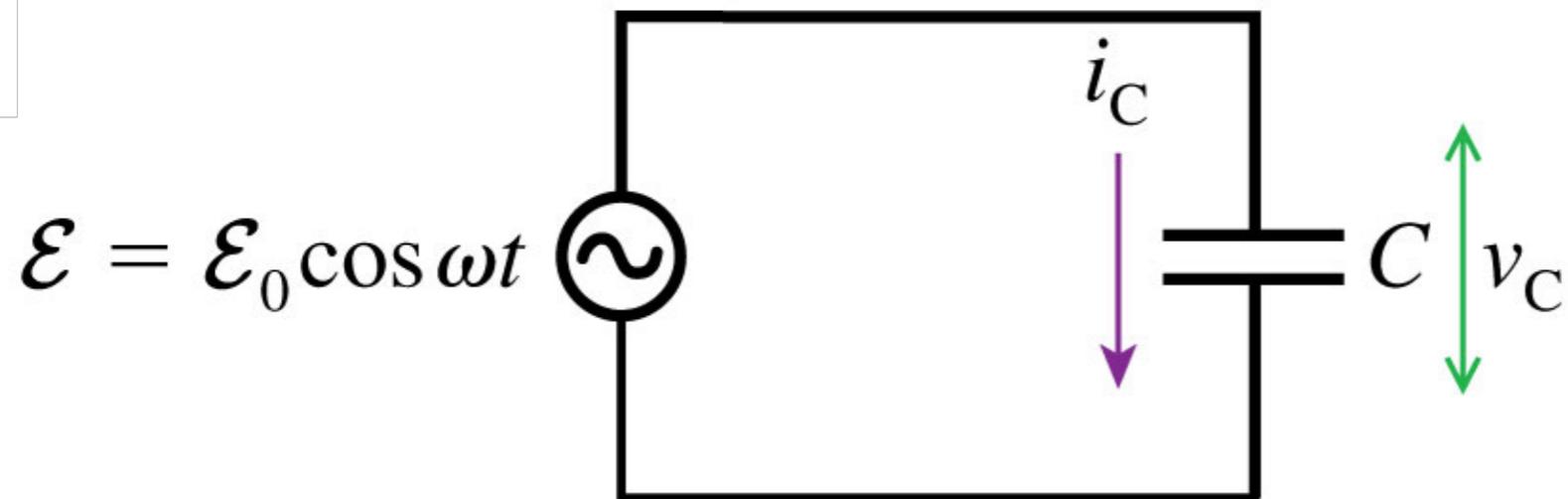
$$\mathcal{E} = \mathcal{E}_0 \cos \omega t$$



$$q = Cv_C = CV_C \cos \omega t$$

$$i_C = \frac{dq}{dt}$$

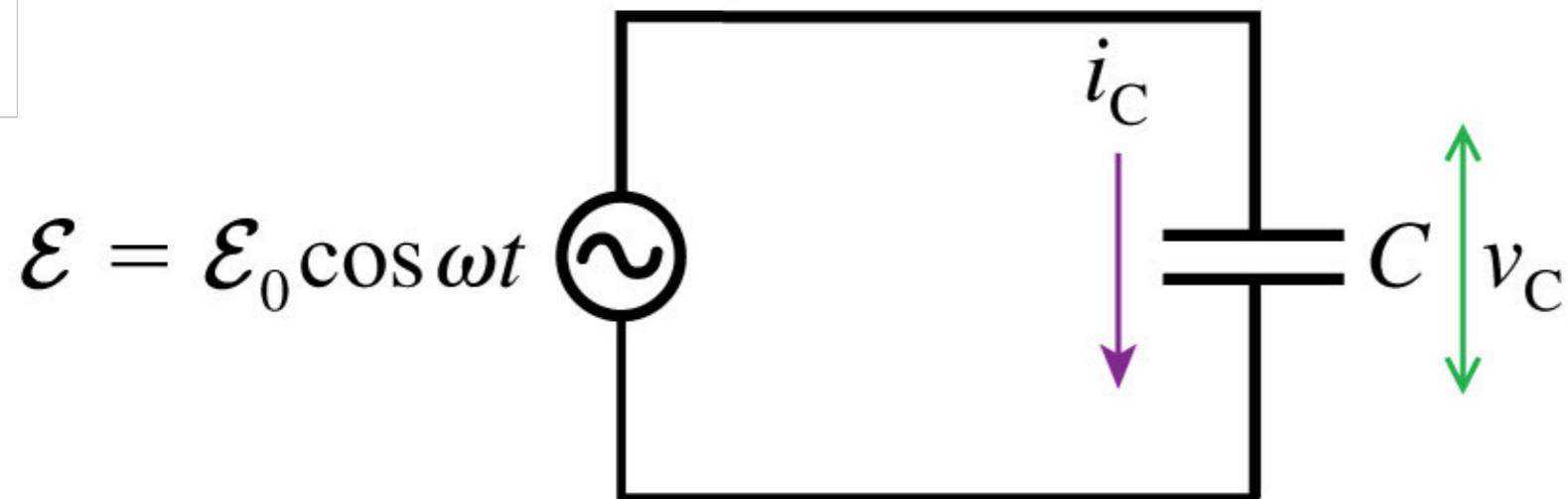
The Math



$$q = Cv_C = CV_C \cos \omega t$$

$$i_C = \frac{dq}{dt} = \frac{d}{dt}(CV_C \cos \omega t) = -\omega CV_C \sin \omega t$$

The Math

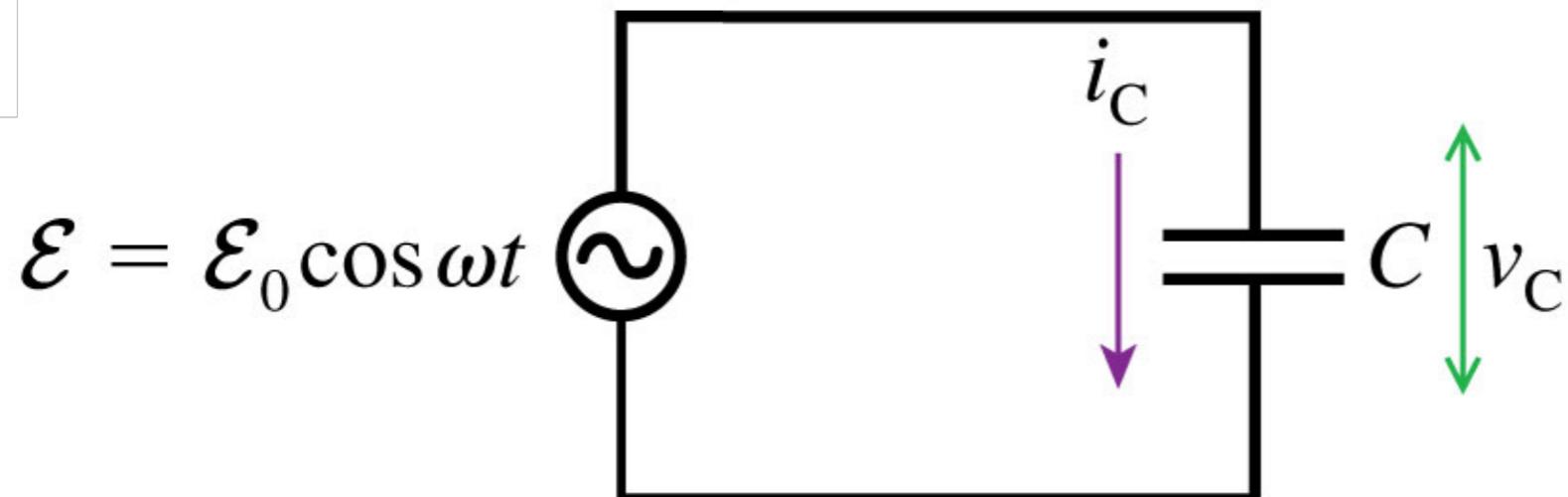


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$$-\sin(x) = \cos(x + \pi/2)$$

The Math



$$q = Cv_C = CV_C \cos \omega t$$

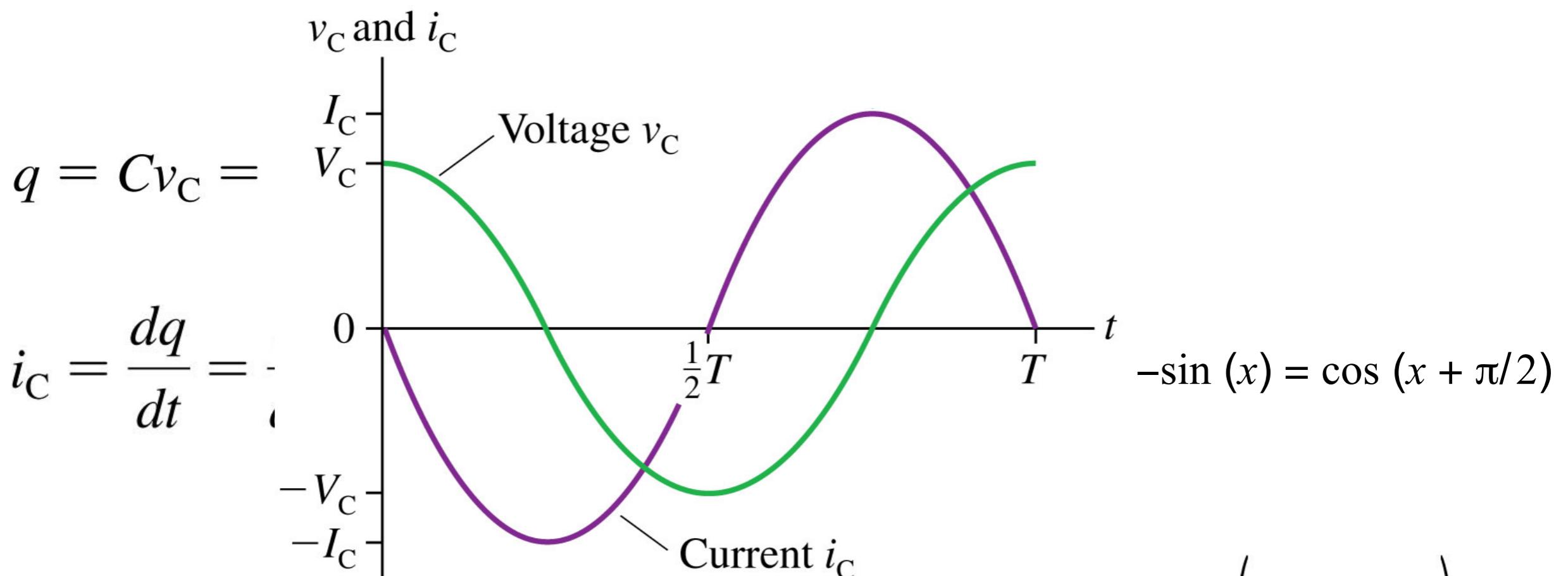
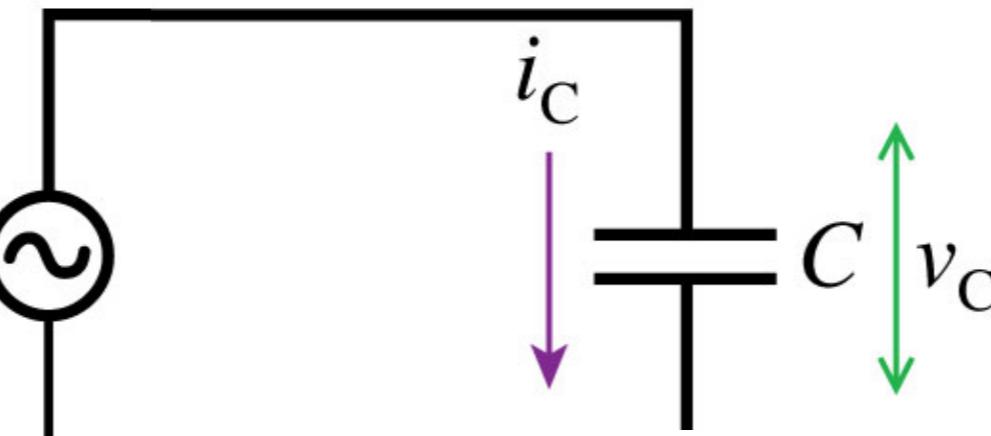
$$i_C = \frac{dq}{dt} = \frac{d}{dt}(CV_C \cos \omega t) = -\omega CV_C \sin \omega t$$

$$-\sin(x) = \cos(x + \pi/2)$$

$$i_C = \omega CV_C \cos \left(\omega t + \frac{\pi}{2} \right)$$

The Math

$$\mathcal{E} = \mathcal{E}_0 \cos \omega t$$



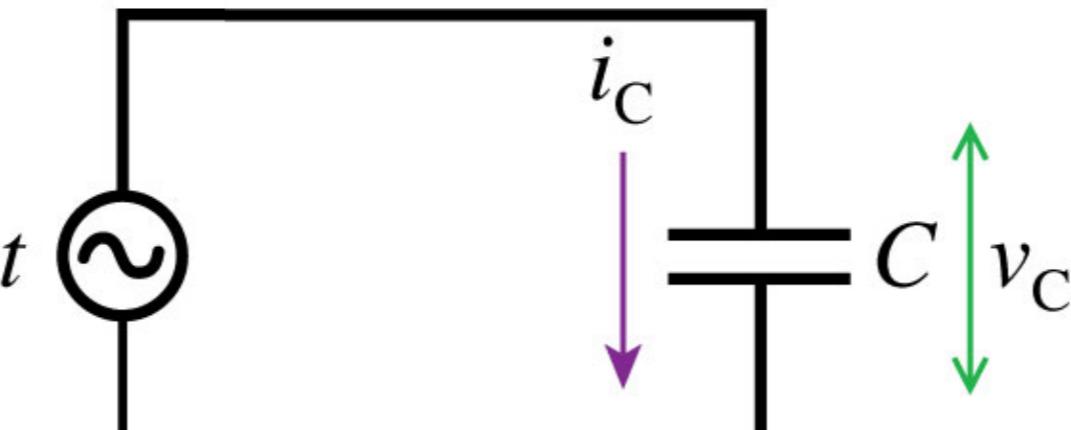
$$i_C = \frac{dq}{dt} = -$$

$$-\sin(x) = \cos(x + \pi/2)$$

$$i_C = \omega C V_C \cos\left(\omega t + \frac{\pi}{2}\right)$$

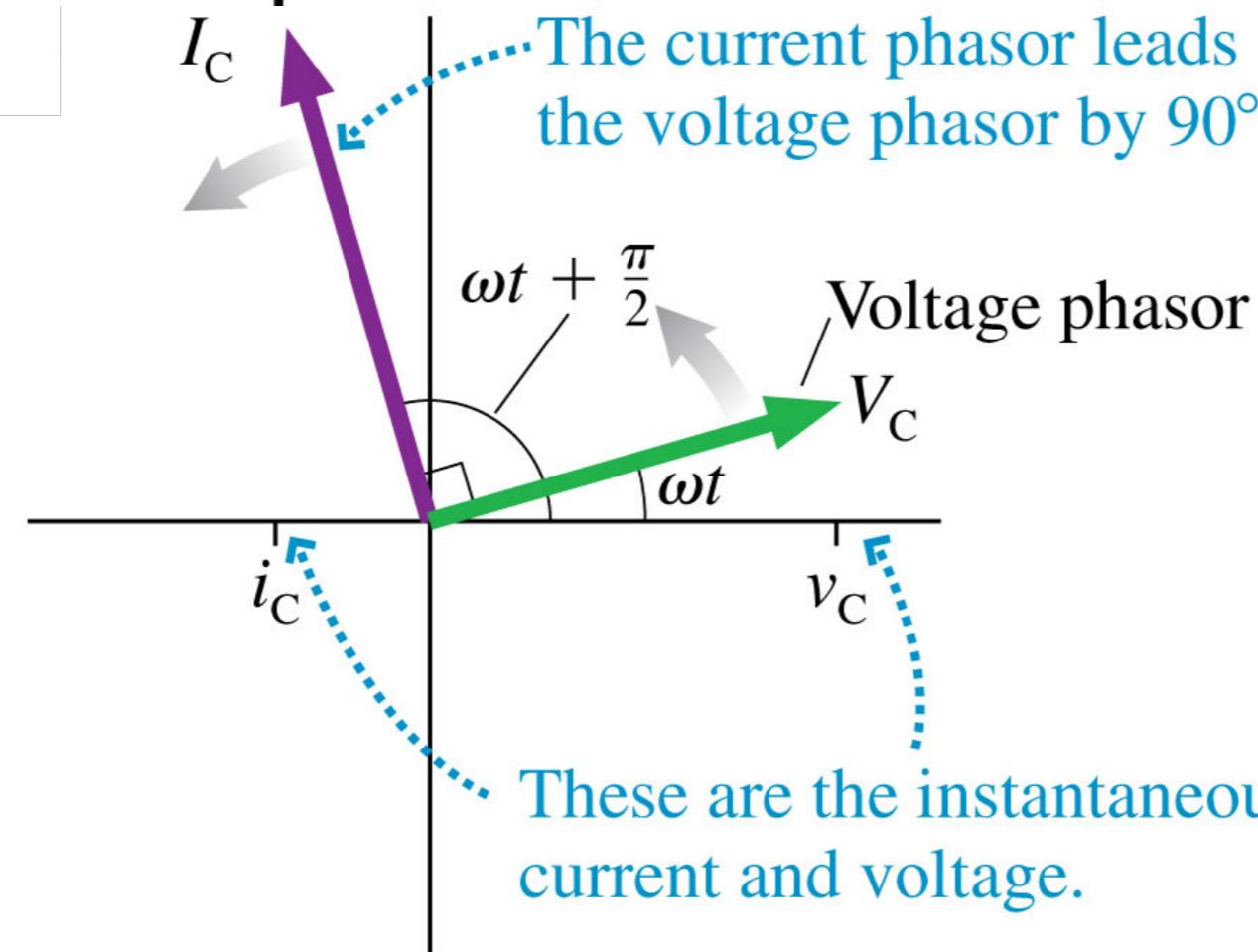
The Math

$$\mathcal{E} = \mathcal{E}_0 \cos \omega t$$



$$q = Cv_C =$$

$$i_C = \frac{dq}{dt} =$$



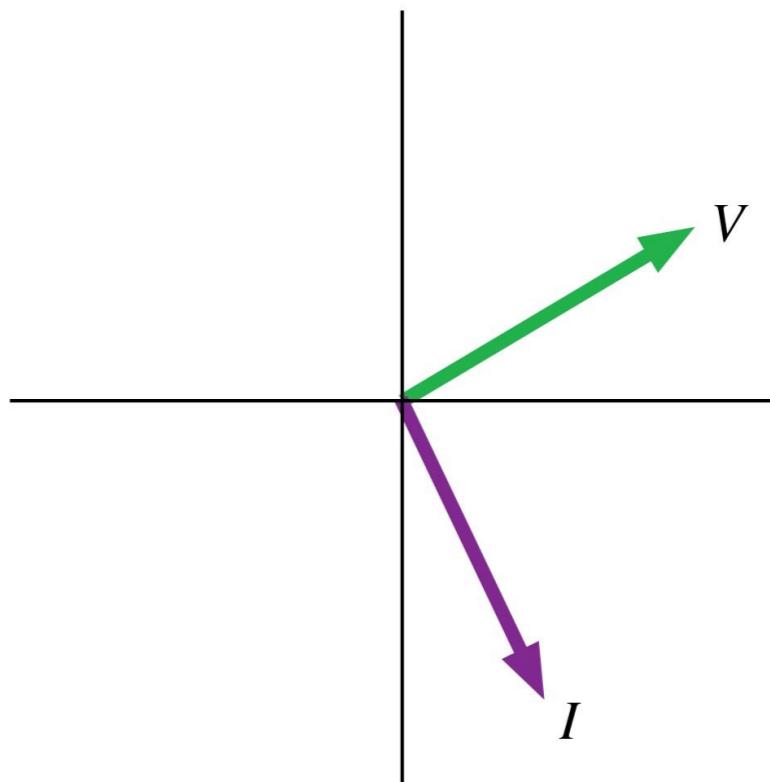
$$t \quad -\sin(x) = \cos(x + \pi/2)$$

$$i_C = \omega CV_C \cos \left(\omega t + \frac{\pi}{2} \right)$$

Quiz Question

In the circuit represented by these phasors, the current ____ the voltage

- A. leads
- B. is perpendicular to
- C. lags
- D. is out of phase with

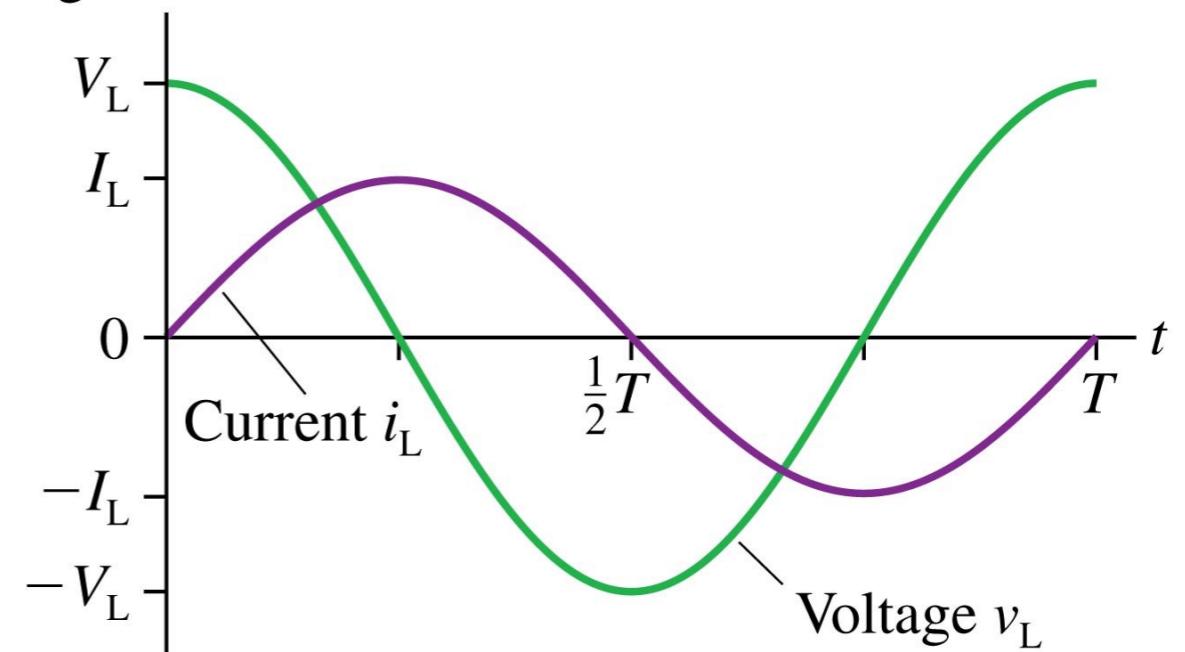


Quiz Question

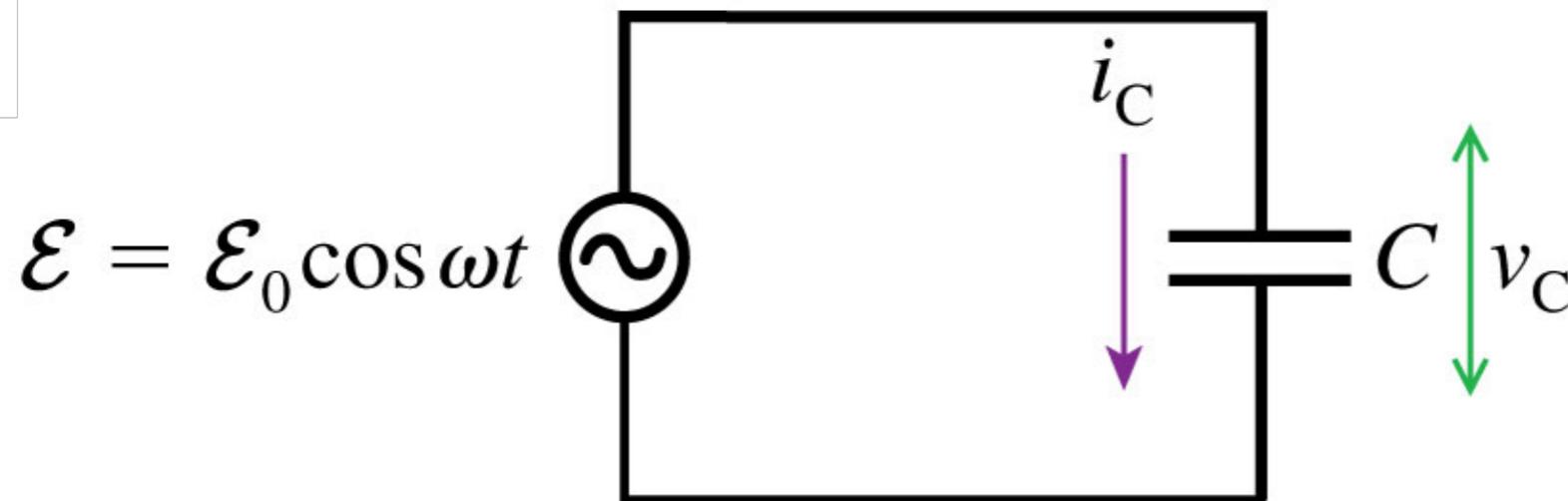
In the circuit represented by these graphs, the current ____ the voltage

- A. leads
- B. is less than
- C. is out of phase with
- D. lags

Voltage and current



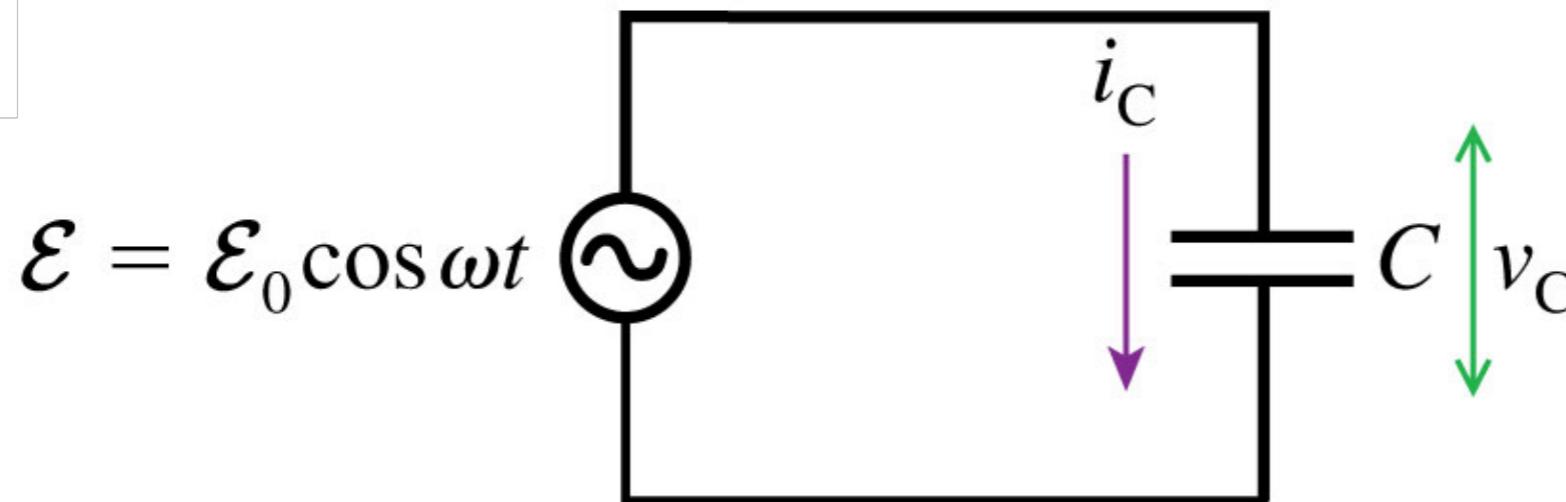
What about the frequency of the source



If the frequency of the source is high will the max current in the circuit be high or low?

- A- Low
- B- High

What about the frequency of the source

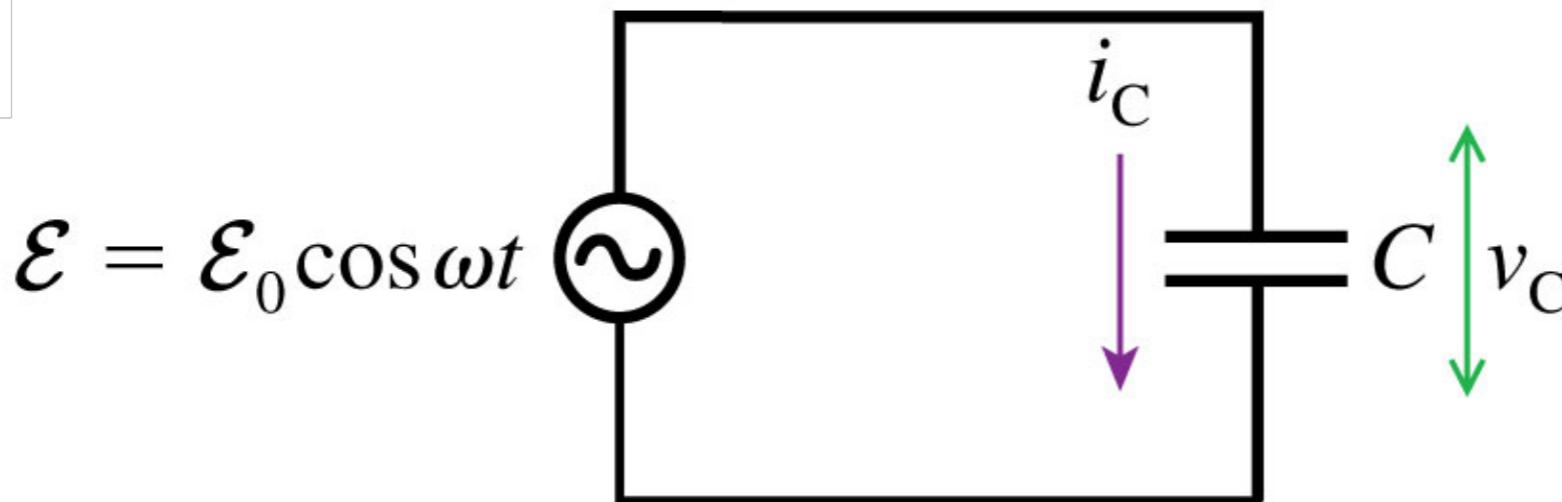


$$\mathcal{E} = \mathcal{E}_0 \cos \omega t$$

If the frequency of the source is high will the max current in the circuit be high or low?

$$i_C = \omega C V_C \cos \left(\omega t + \frac{\pi}{2} \right)$$

What about the frequency of the source



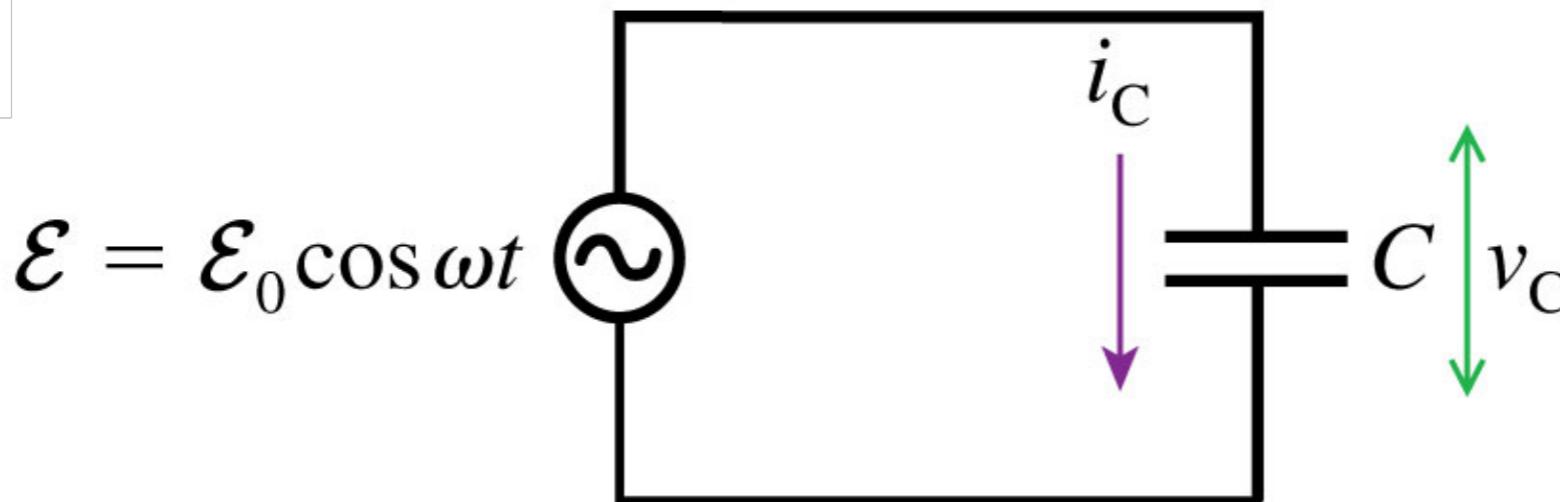
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$$i_C = \omega C V_C \cos\left(\omega t + \frac{\pi}{2}\right)$$

$$I_C = \omega C V_C \quad (\text{Max current in the circuit})$$

What about the frequency of the source



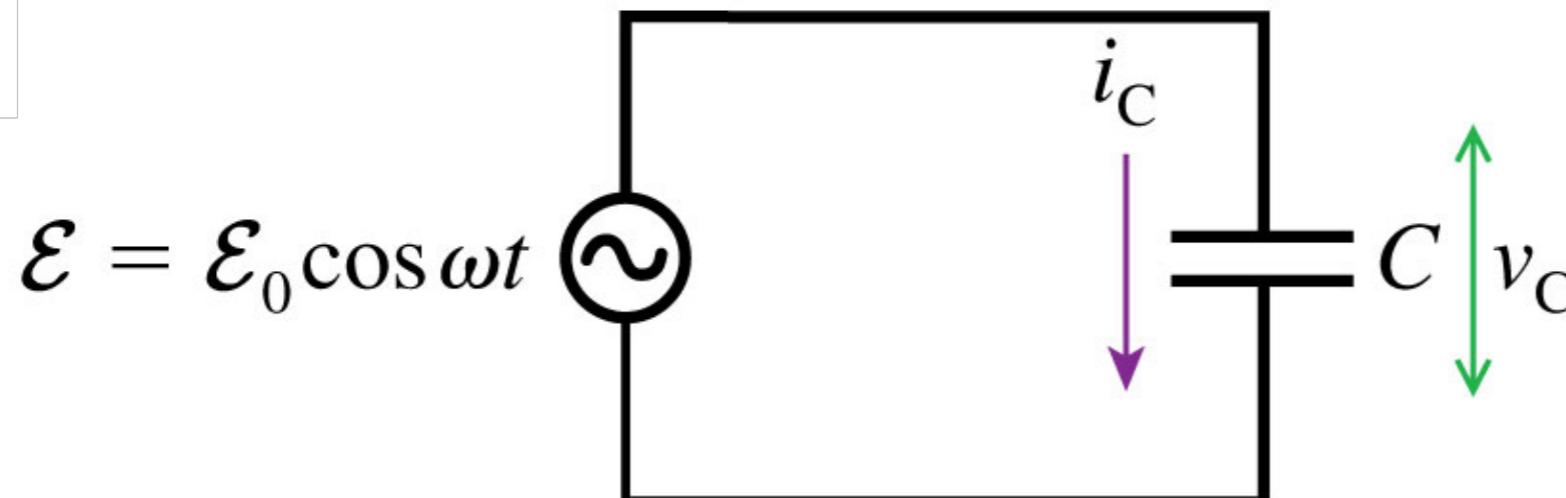
If the frequency of the source is high will the max current in the circuit be high or low?

$$i_C = \omega C V_C \cos\left(\omega t + \frac{\pi}{2}\right)$$

$$I_C = \omega C V_C \quad (\text{Max current in the circuit})$$

$$X_C = \frac{1}{\omega C} \quad (\text{Capacitive Reactance})$$

What about the frequency of the source



$$\mathcal{E} = \mathcal{E}_0 \cos \omega t$$

If the frequency of the source is high will the max current in the circuit be high or low?

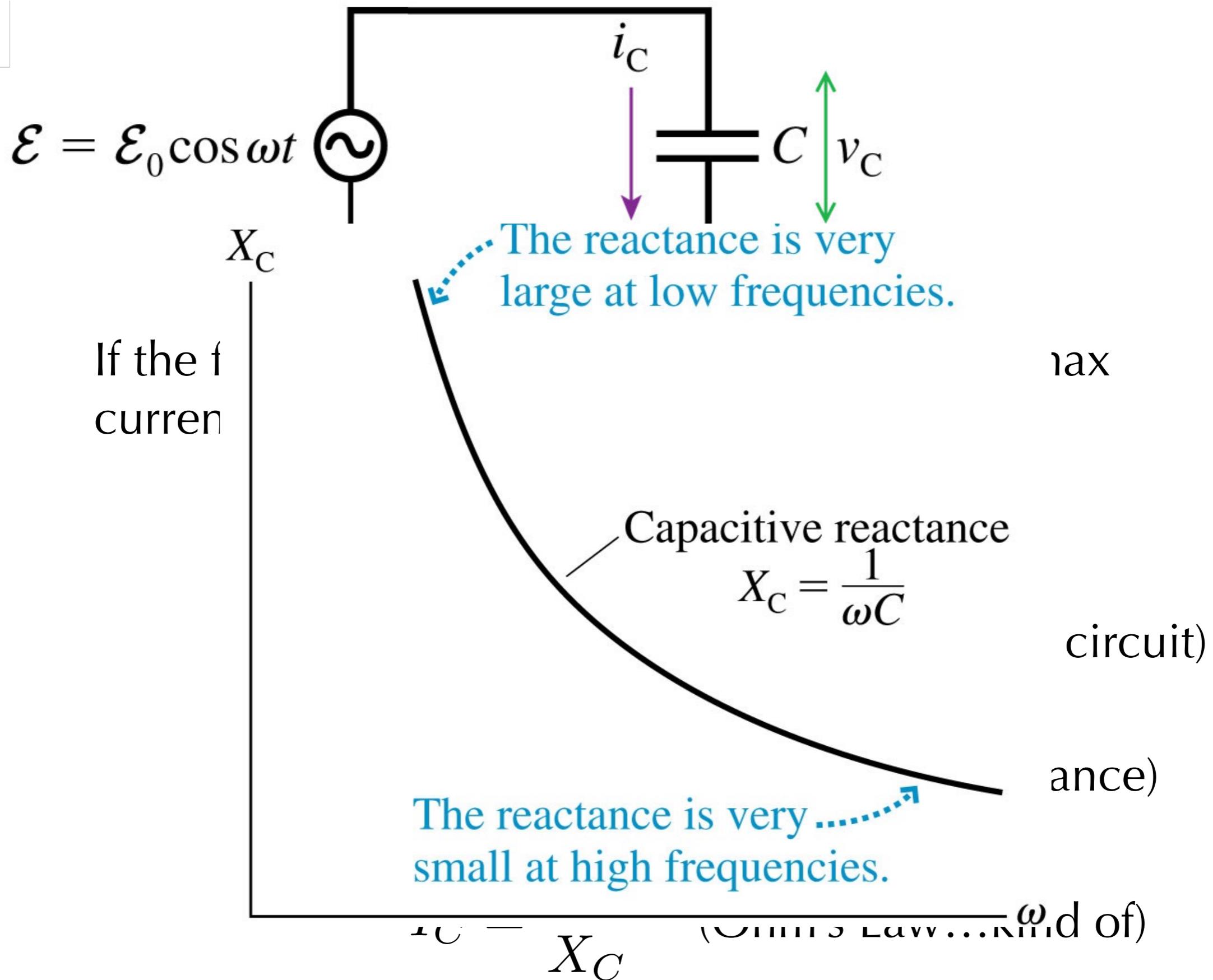
$$i_C = \omega C V_C \cos \left(\omega t + \frac{\pi}{2} \right)$$

$$I_C = \omega C V_C \quad (\text{Max current in the circuit})$$

$$X_C = \frac{1}{\omega C} \quad (\text{Capacitive Reactance})$$

$$I_C = \frac{V_C}{X_C} \quad (\text{Ohm's Law...kind of})$$

What about the frequency of the source

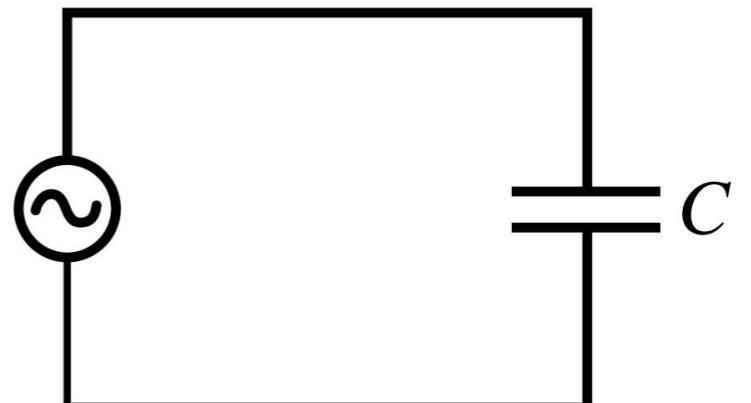


Quiz Question

If the value of the capacitance is doubled,
the capacitive reactance

- A. Is quartered.
- B. Is halved.
- C. Is doubled.
- D. Is quadrupled.
- E. Can't tell without knowing ω .

$$\mathcal{E} = \mathcal{E}_0 \cos \omega t$$

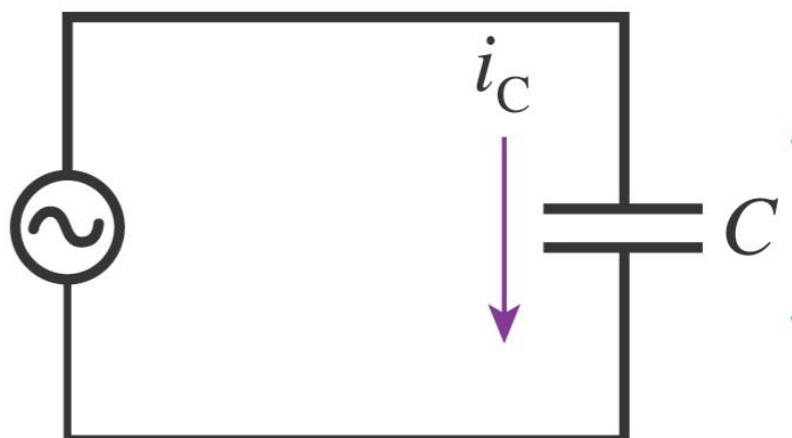


Quiz Question

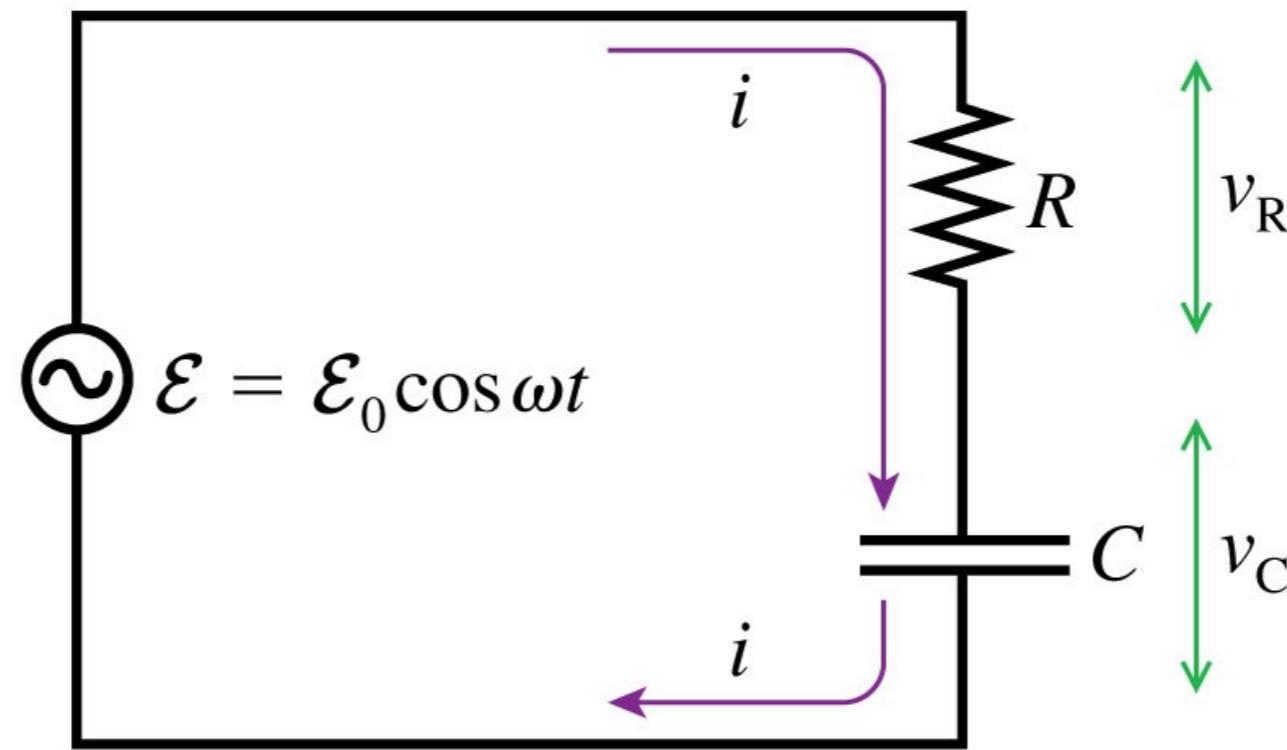
If the value of the capacitance is doubled, the peak current

- A. Is quartered.
- B. Is doubled.
- C. Is halved.
- D. Is quadrupled.
- E. Can't tell without knowing C .

$$\mathcal{E} = \mathcal{E}_0 \cos \omega t$$

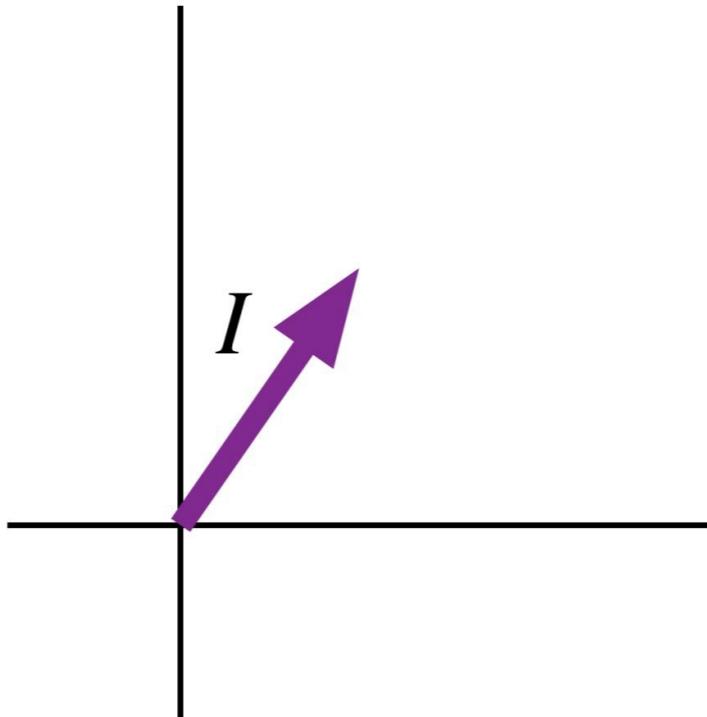


AC RC circuit



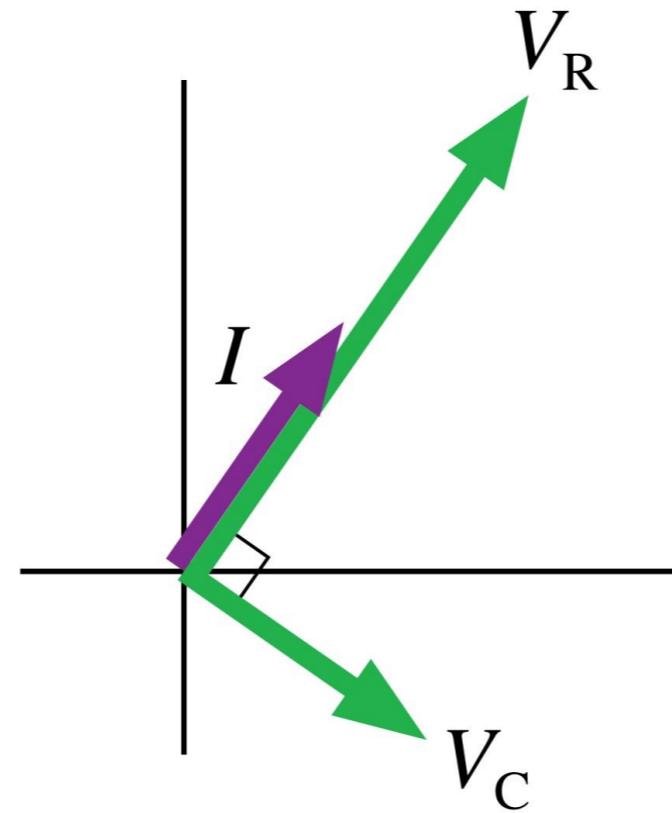
If the source frequency is high(low), will the peak voltage across the resistor (capacitor) be high or low?

Phasor Diagram



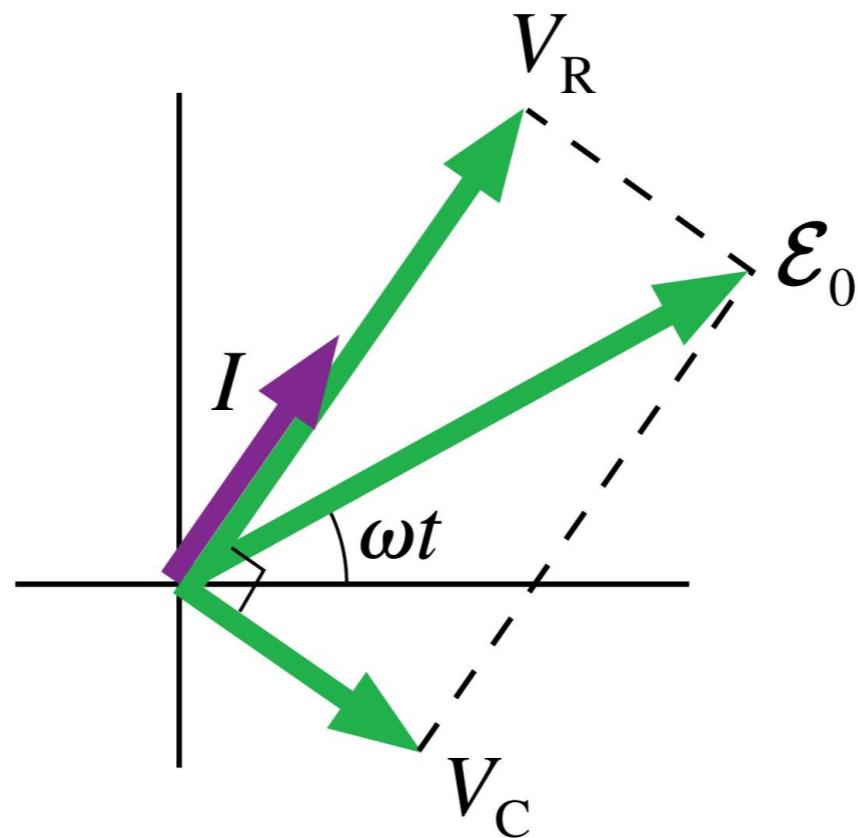
Draw the resistor voltage phasor and the capacitor voltage phasor

Phasor Diagram



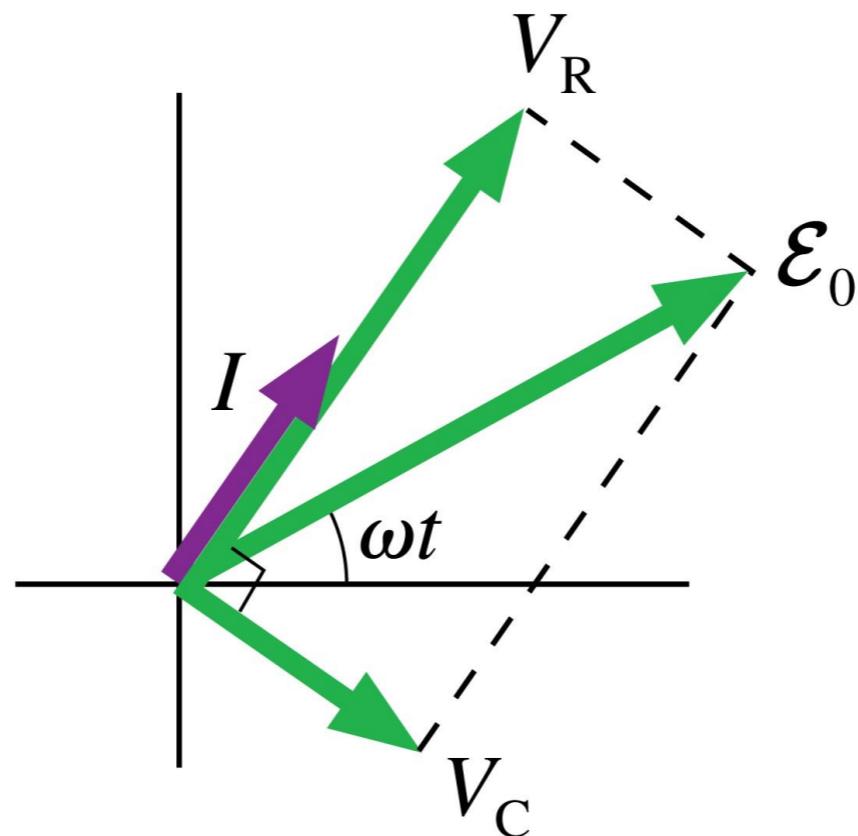
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Phasor Diagram



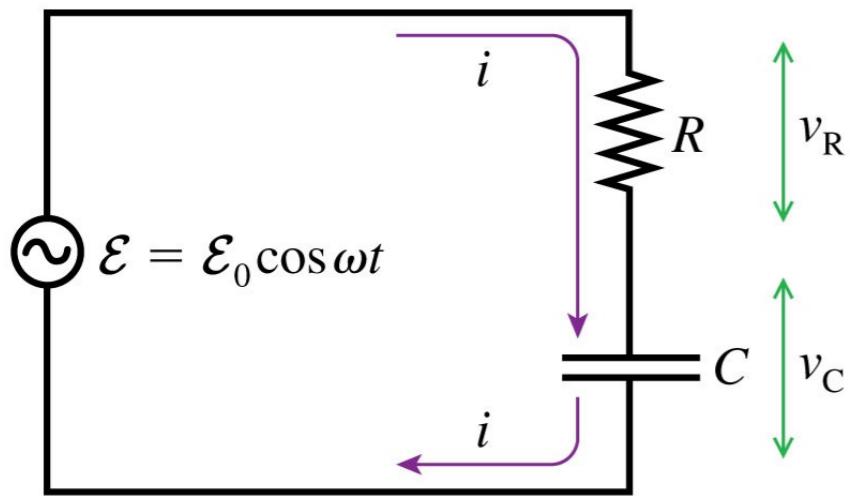
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Phasor Diagram



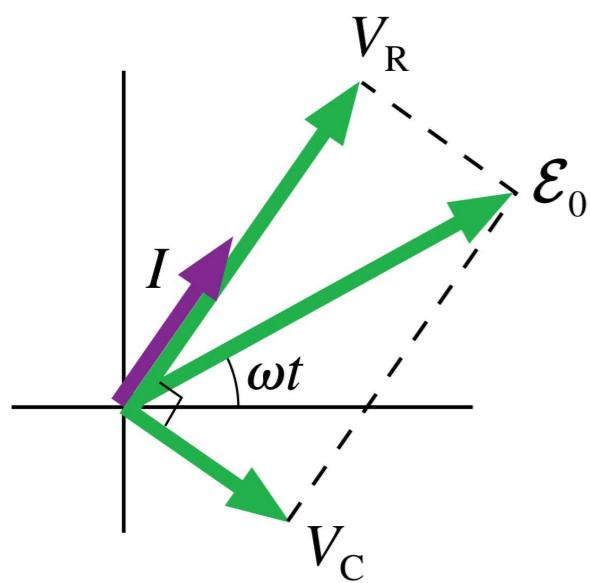
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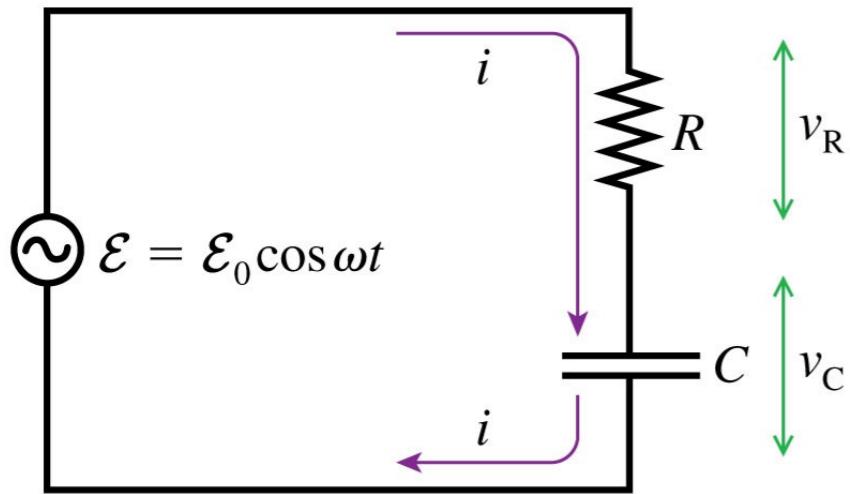
$$\mathcal{E}_0^2 = V_R^2 + V_C^2$$



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-
- Fill in the details and solve for I
-

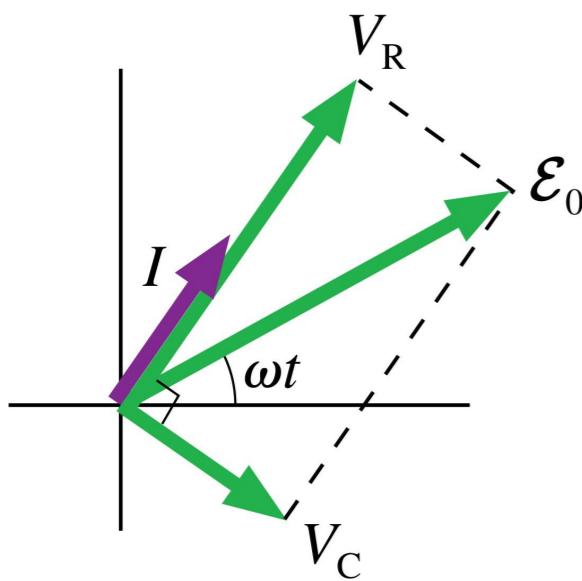


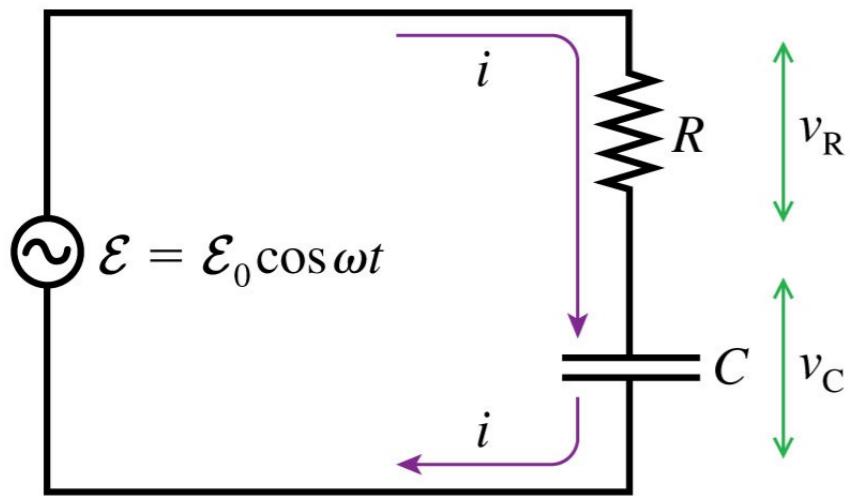


$$\mathcal{E}_0^2 = V_R^2 + V_C^2$$

-
- Fill in the details and solve for I
-

$$\begin{aligned}\mathcal{E}_0^2 &= V_R^2 + V_C^2 = (IR)^2 + (IX_C)^2 = (R^2 + X_C^2)I^2 \\ &= (R^2 + 1/\omega^2 C^2)I^2\end{aligned}$$



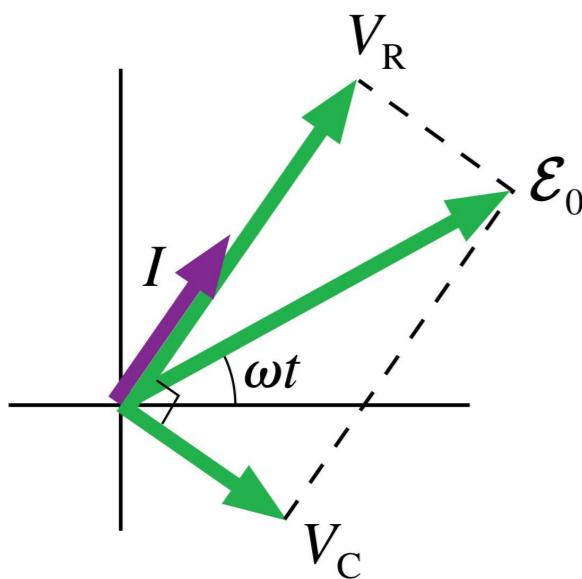


$$\mathcal{E}_0^2 = V_R^2 + V_C^2$$

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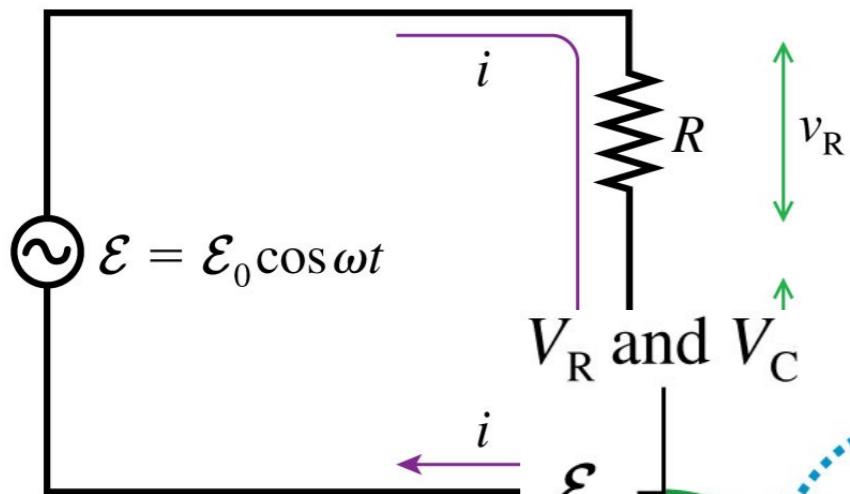
Fill in the details and solve for I

$$\begin{aligned}\mathcal{E}_0^2 &= V_R^2 + V_C^2 = (IR)^2 + (IX_C)^2 = (R^2 + X_C^2)I^2 \\ &= (R^2 + 1/\omega^2 C^2)I^2\end{aligned}$$

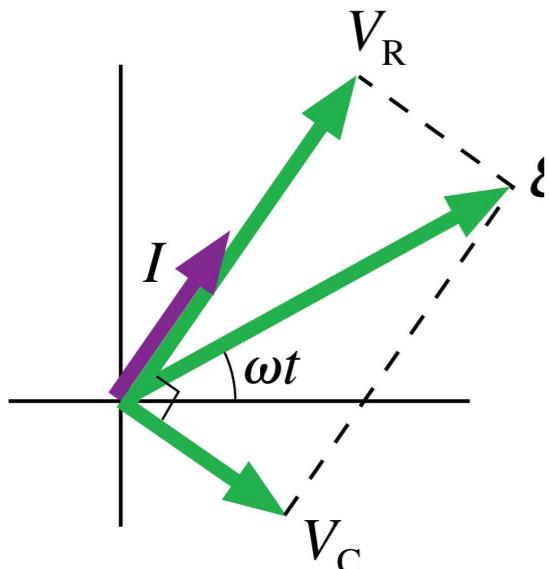


$$V_R = IR = \frac{\mathcal{E}_0 R}{\sqrt{R^2 + X_C^2}} = \frac{\mathcal{E}_0 R}{\sqrt{R^2 + 1/\omega^2 C^2}}$$

$$V_C = IX_C = \frac{\mathcal{E}_0 X_C}{\sqrt{R^2 + X_C^2}} = \frac{\mathcal{E}_0 / \omega C}{\sqrt{R^2 + 1/\omega^2 C^2}}$$



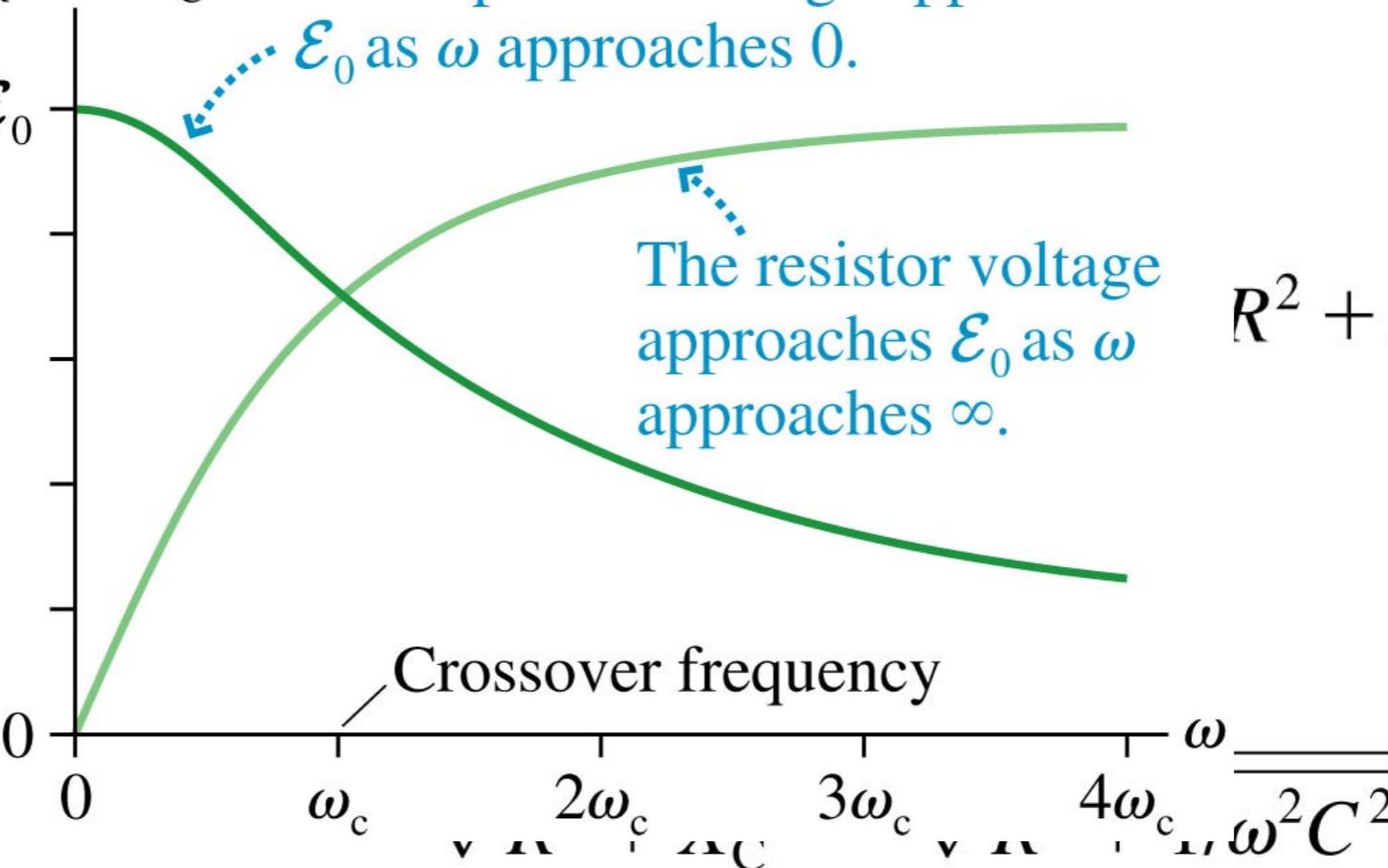
$$\omega_c = \frac{1}{RC}$$



$$E_0^2 = V_R^2 + V_C^2$$

- Fill in the details and solve for I

The capacitor voltage approaches E_0 as ω approaches 0.

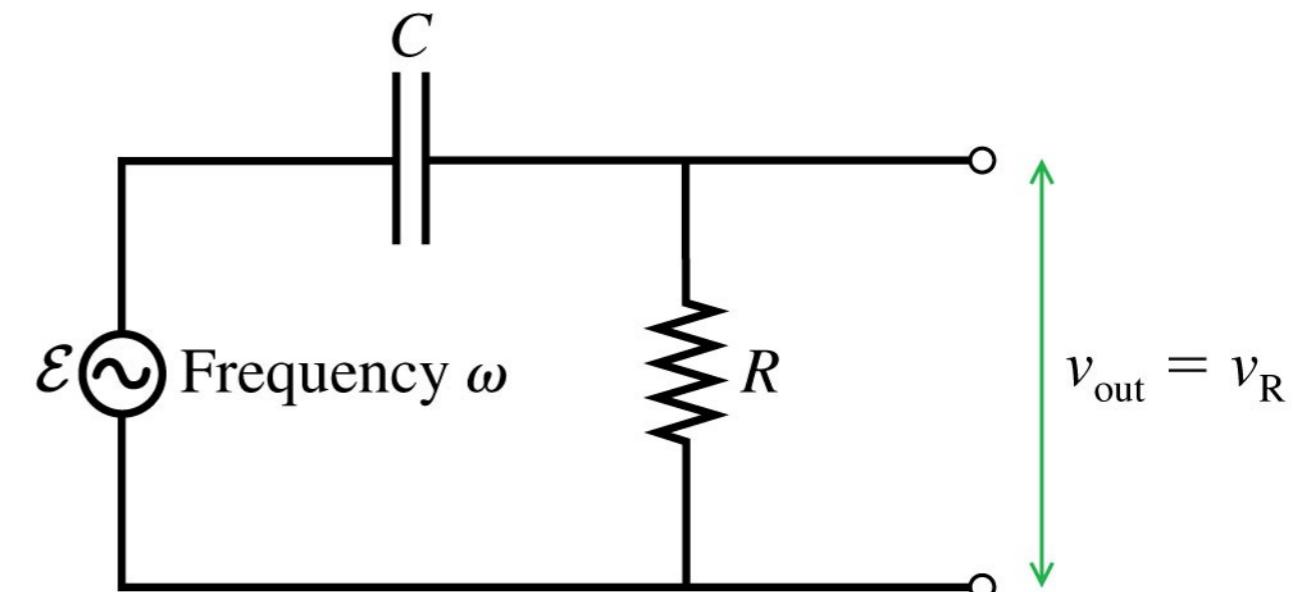
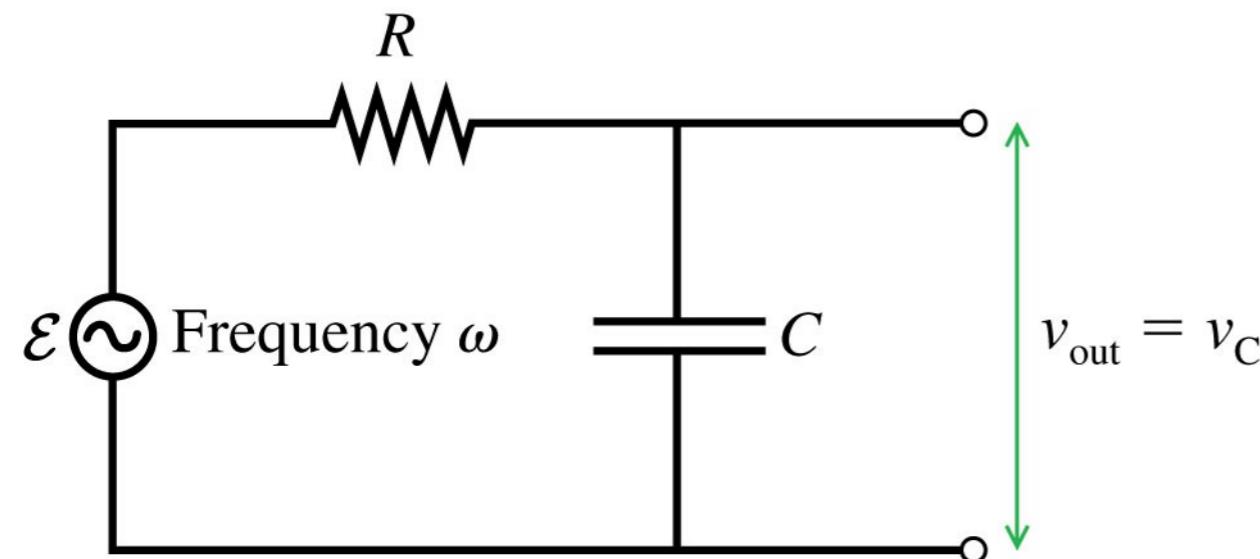


$$(R^2 + X_C^2)I^2$$

The resistor voltage approaches E_0 as ω approaches ∞ .

$$I_C = IX_C = \frac{E_0 X_C}{\sqrt{R^2 + X_C^2}} = \frac{E_0 / \omega C}{\sqrt{R^2 + 1/\omega^2 C^2}}$$

Filters



Which circuit will transmit high frequency signals through?