



PH 220

Lance Nelson

$$\boldsymbol{F} = q \vec{v} \times \vec{B}$$

$$\vec{B}=\frac{\mu_0 I}{4\pi}\frac{\Delta \vec{s}\times \hat{r}}{r^2}$$

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I$$

$$\vec{B}=\frac{\mu_0 q}{4\pi}\frac{\vec{v}\times\hat{r}}{r^2}$$

$$F=I\vec{l}\times\vec{B}$$

$$\vec{\tau}=\vec{\mu}\times\vec{B}$$

6

$$\vec{B} = \frac{\mu_0 I}{4\pi} \frac{\Delta \vec{s} \times \hat{r}}{r^2}$$

$$F = q \vec{v} \times \vec{B}$$

4

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I$$

2

$$\vec{B} = \frac{\mu_0 q}{4\pi} \frac{\vec{v} \times \hat{r}}{r^2}$$

1

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

5

$$F = I \vec{l} \times \vec{B}$$

3

moving charges  
**feel** magnetic  
forces.

$$F = q\vec{v} \times \vec{B}$$

4

moving charges  
**create** magnetic  
fields.

$$\vec{B} = \frac{\mu_0 q}{4\pi} \frac{\vec{v} \times \hat{r}}{r^2}$$

1

current loops **feel**  
magnetic torque.

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

5

$$\vec{B} = \frac{\mu_0 I}{4\pi} \frac{\Delta \vec{s} \times \hat{r}}{r^2}$$

currents **create**  
magnetic fields.

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I$$

2

3

$$F = I\vec{l} \times \vec{B}$$

current-carrying wires  
**feel** magnetic forces

# What's ahead

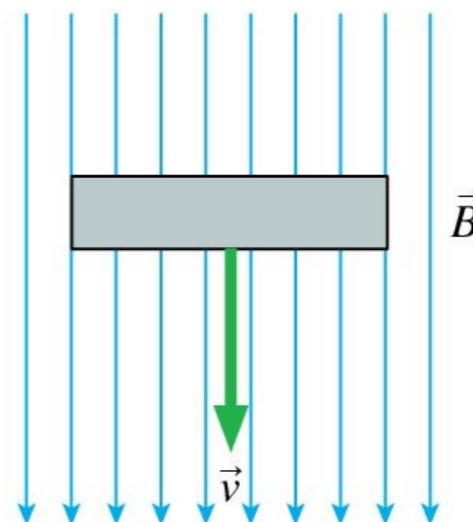
$$\vec{E} = \frac{kq}{r^2} \hat{r}$$

How electric fields are created.... right?

**There is a totally different way to create an electric field!!**

# Quiz Question

A metal bar moves through a magnetic field. The induced charges on the bar are



A



B



C



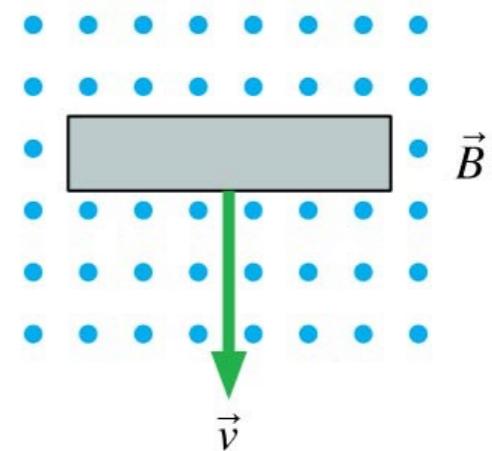
D



E

# Quiz Question

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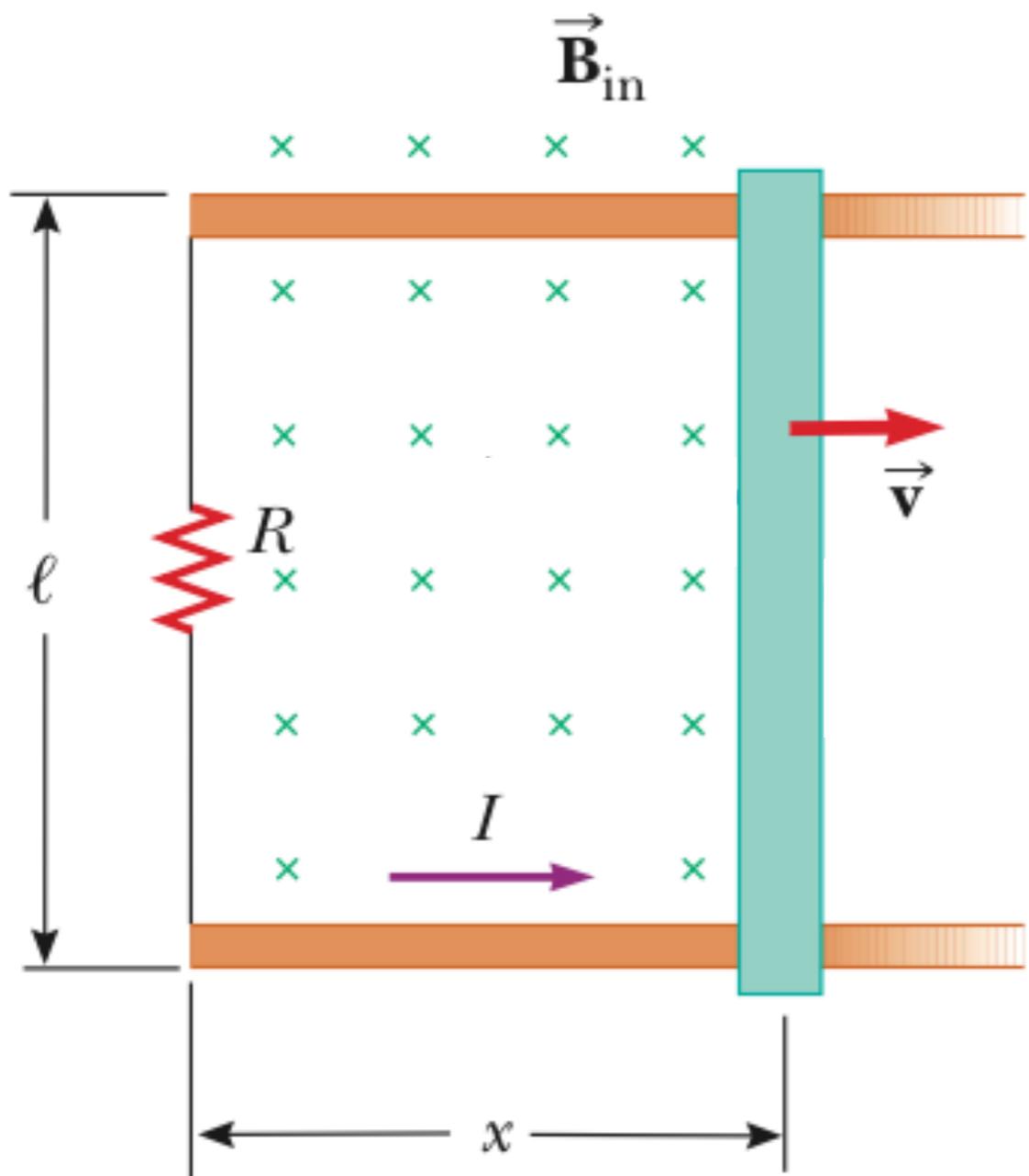
C



D



E



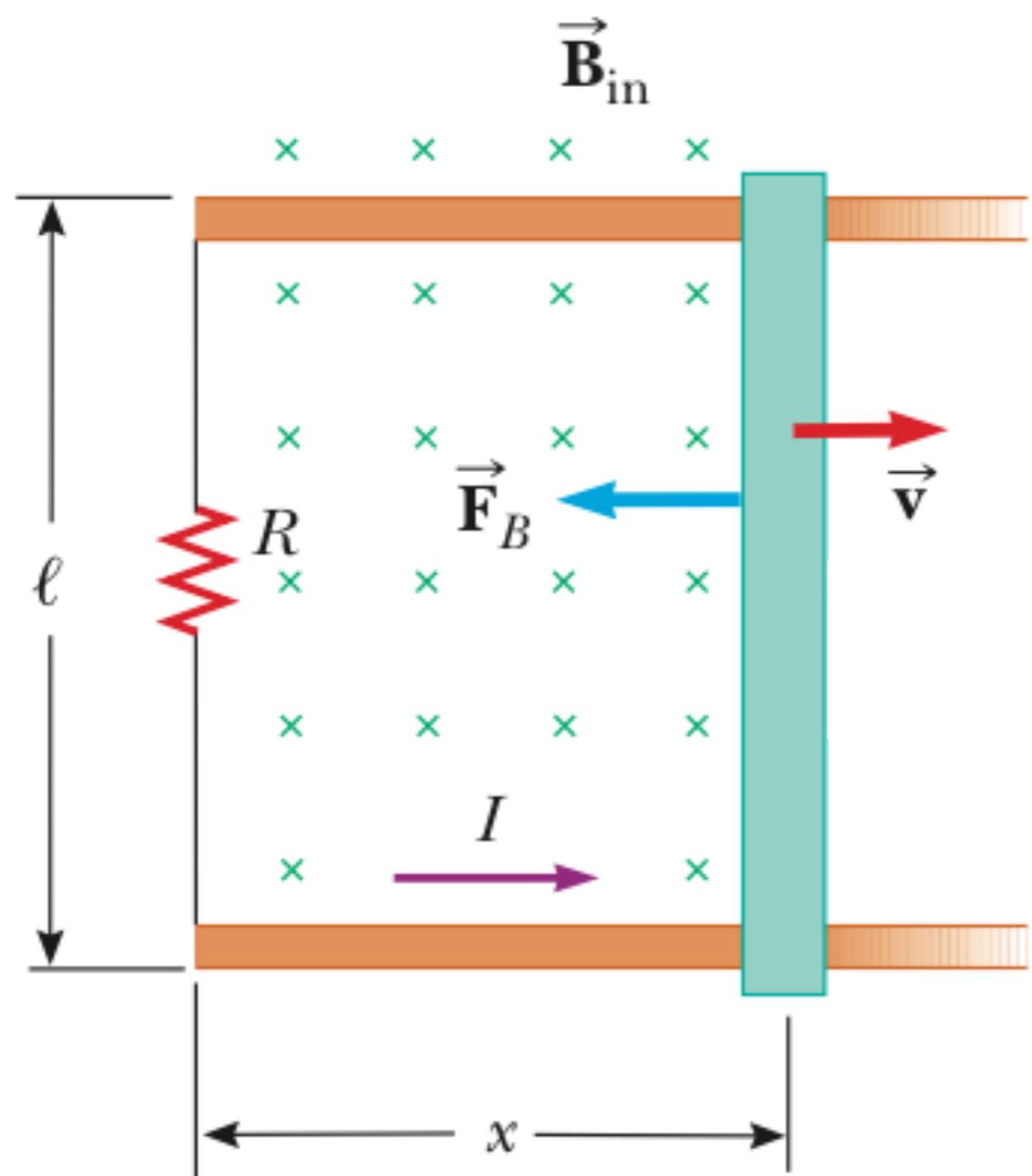
What we know:

$$F = q\vec{v} \times \vec{B}$$

$$F = I\vec{l} \times \vec{B}$$

Explain to your neighbor why a current flows in this situation.

How many forces will the bar experience?



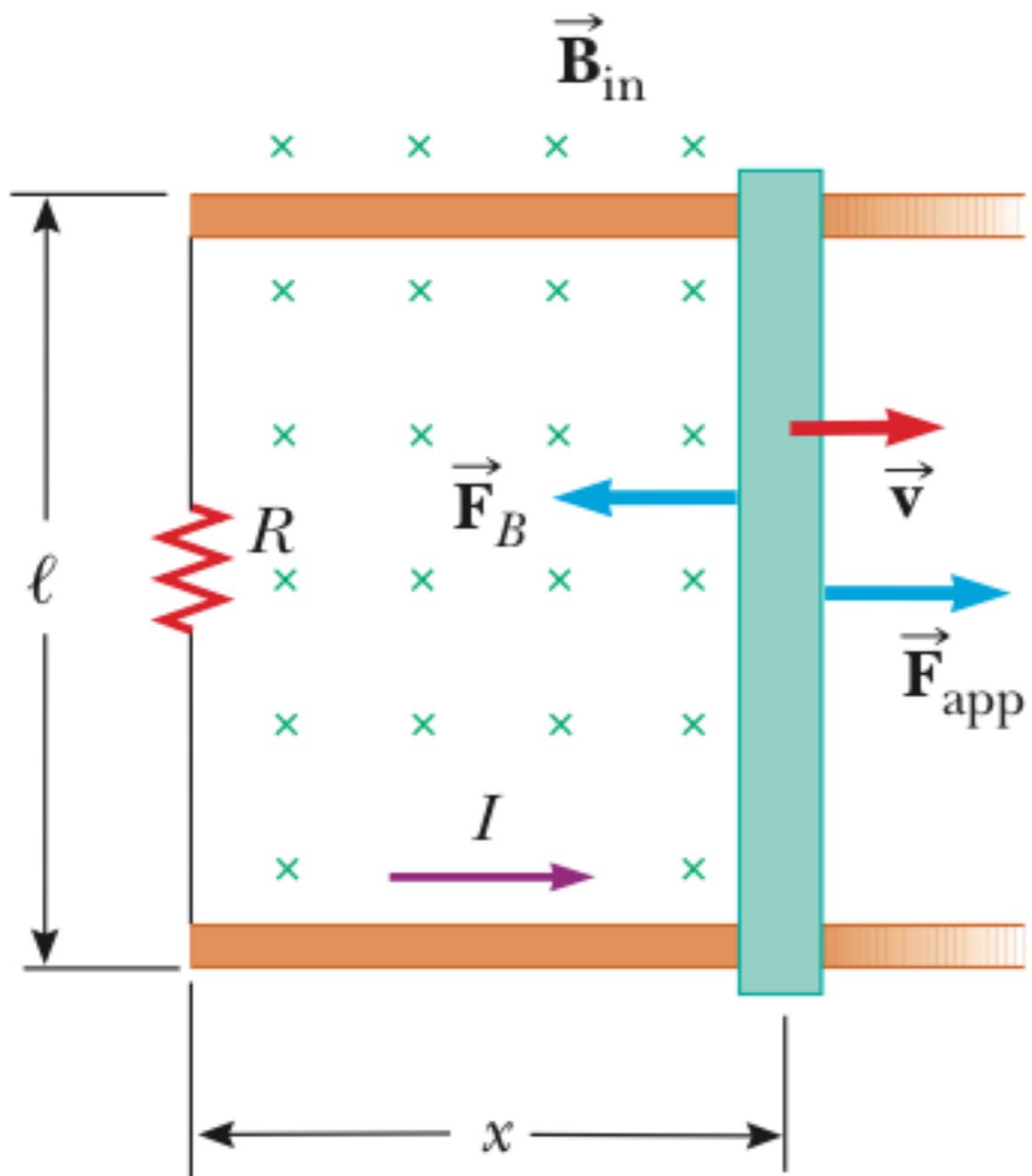
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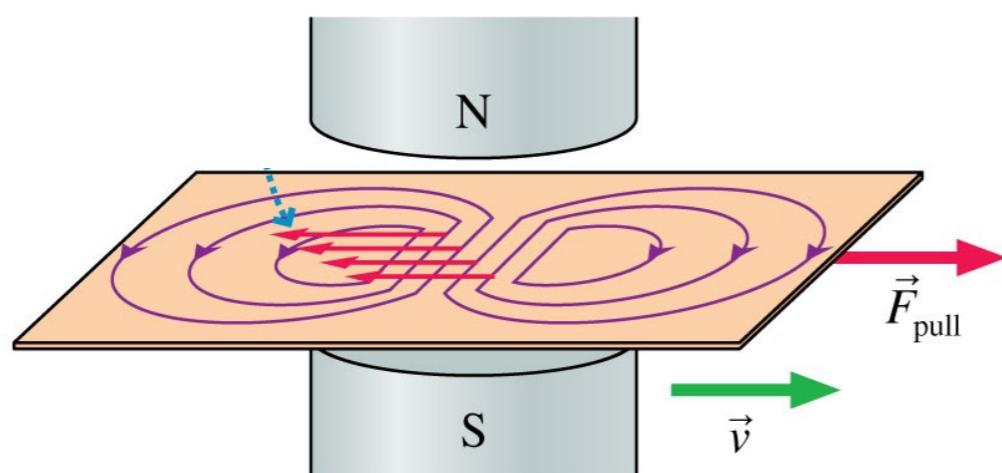
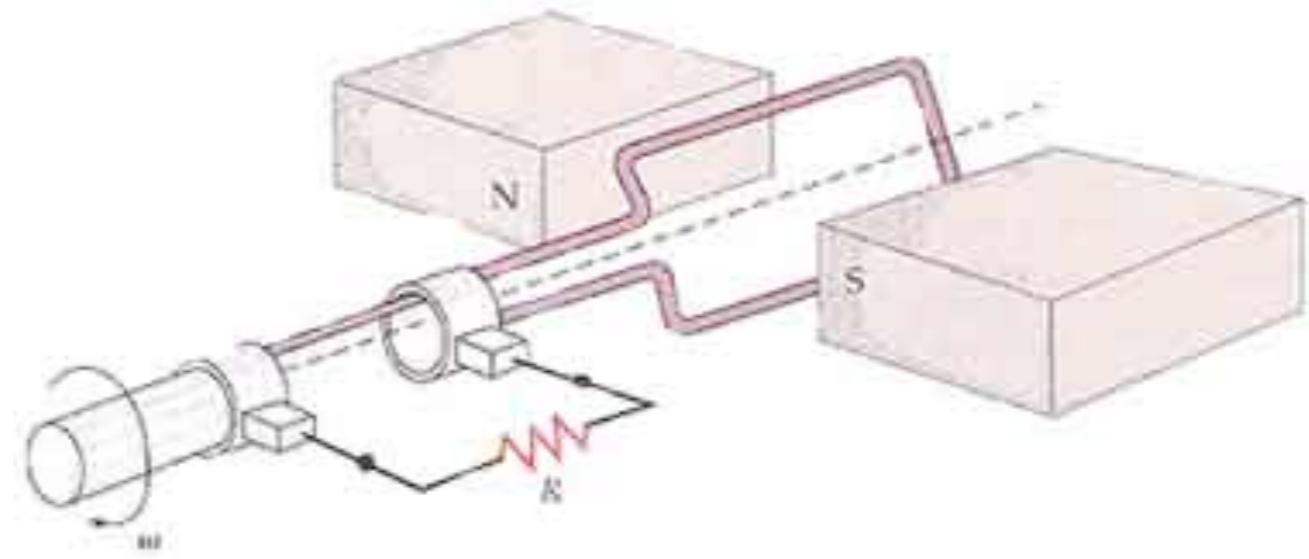
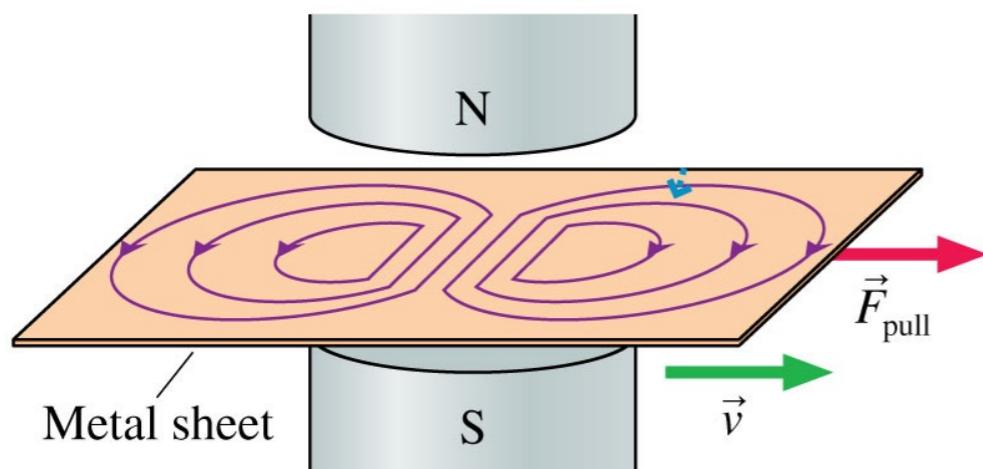
$$F = q\vec{v} \times \vec{B}$$

$$F = Il \times \vec{B}$$

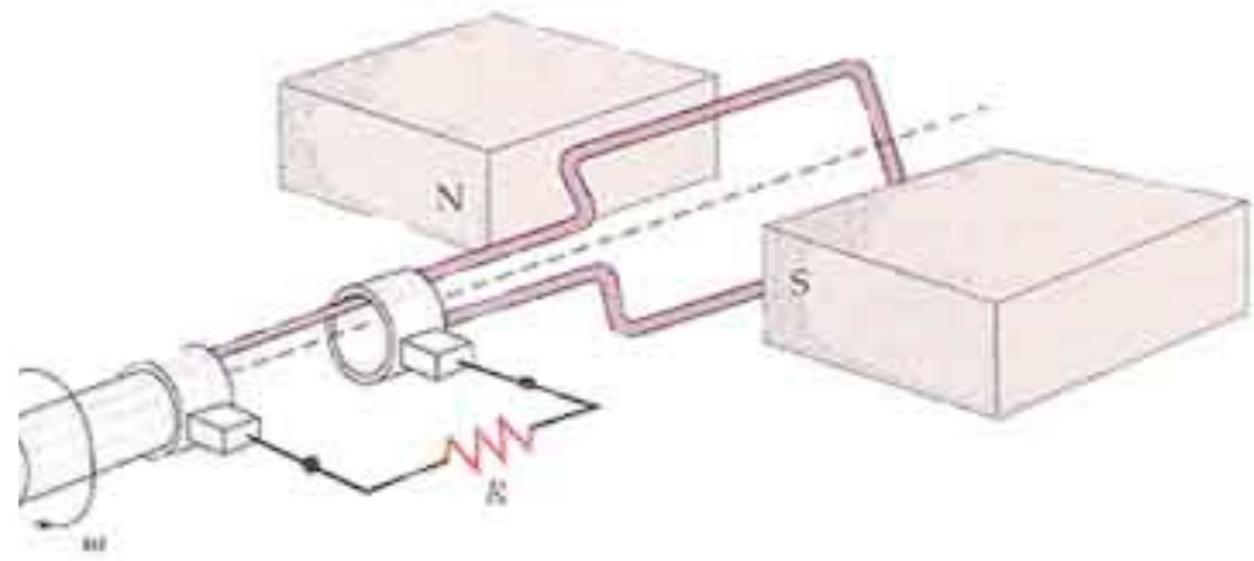
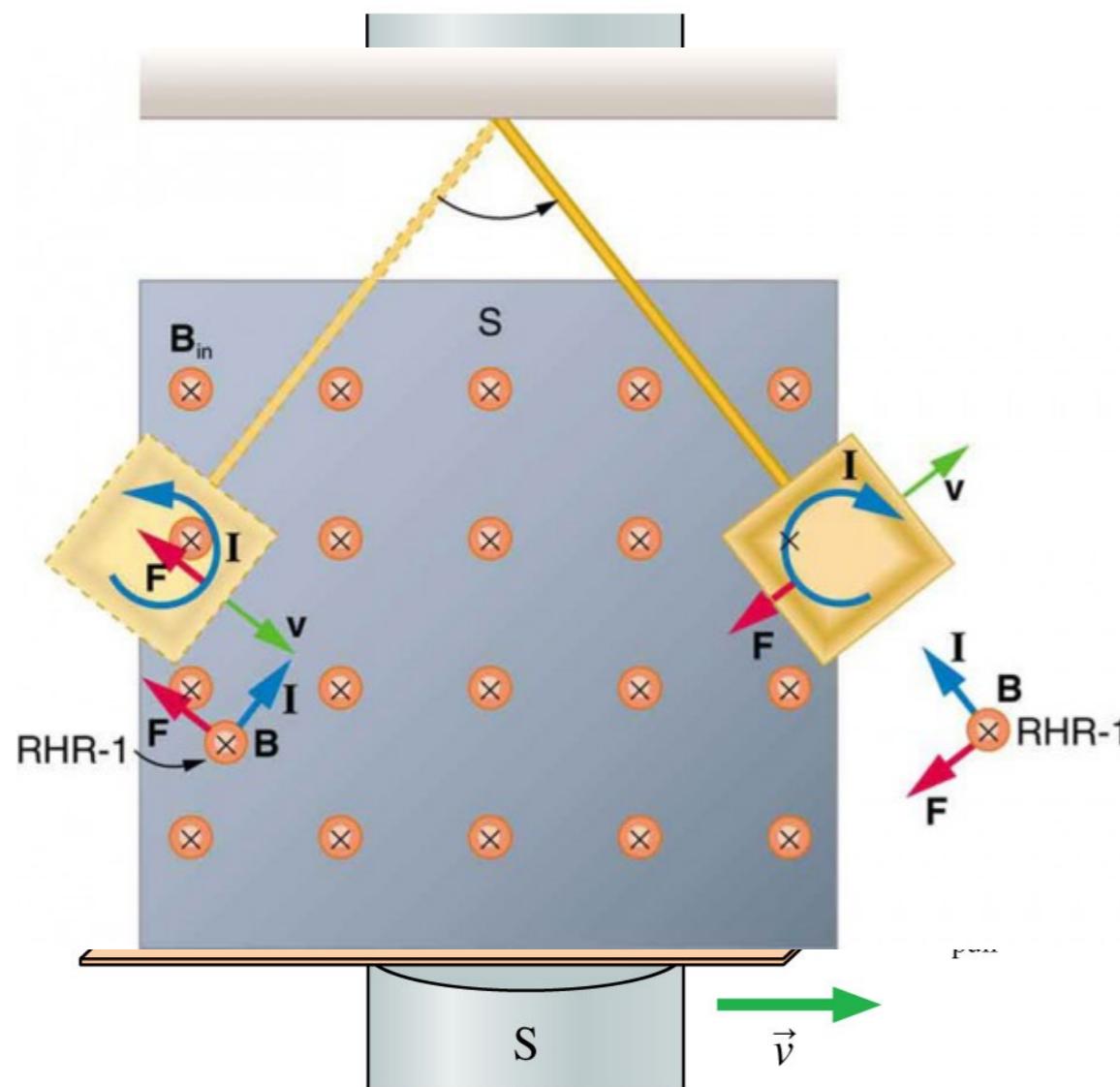
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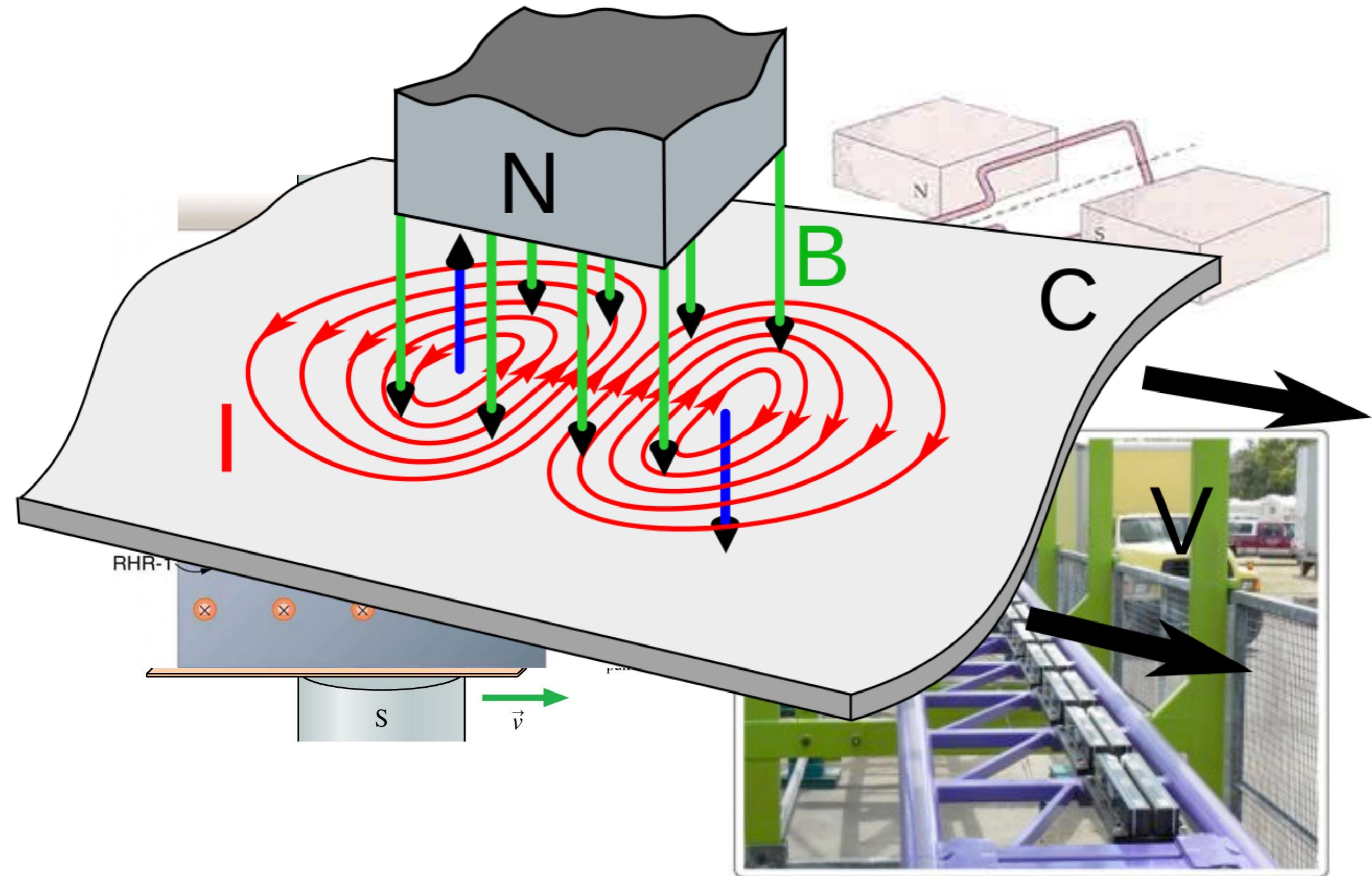
# Eddy currents, magnetic braking, generators



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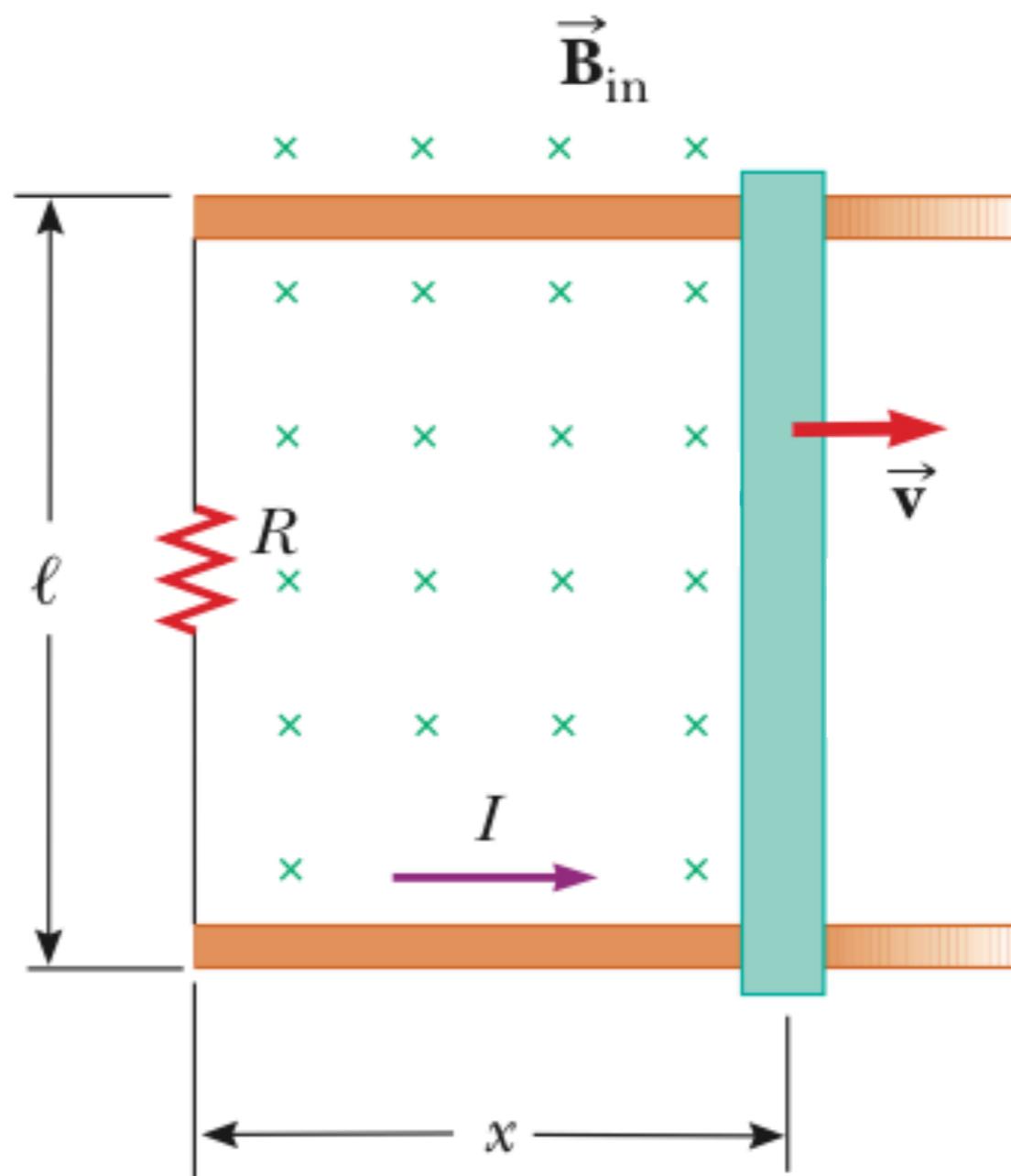
# Eddy currents, magnetic braking, generators



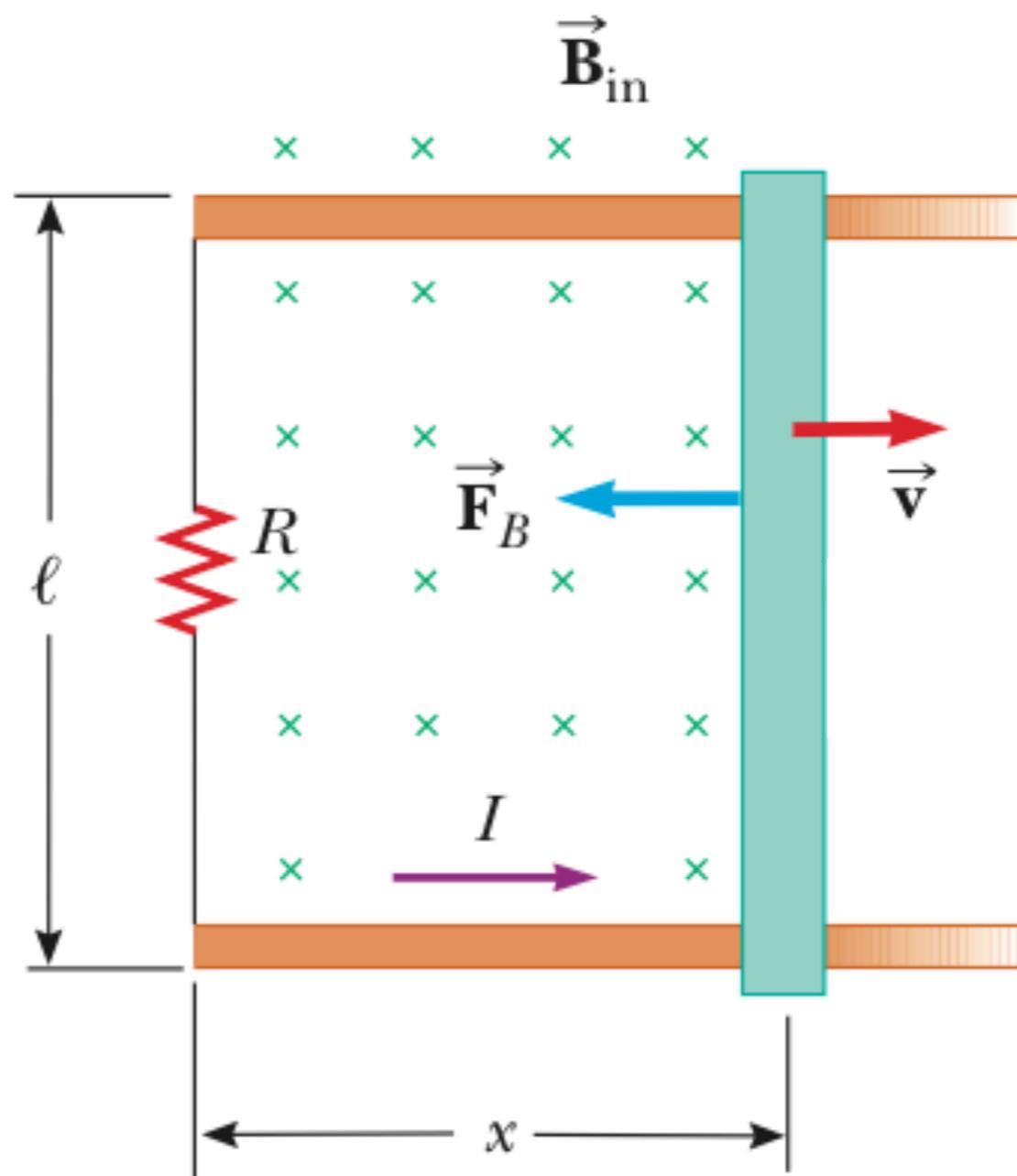
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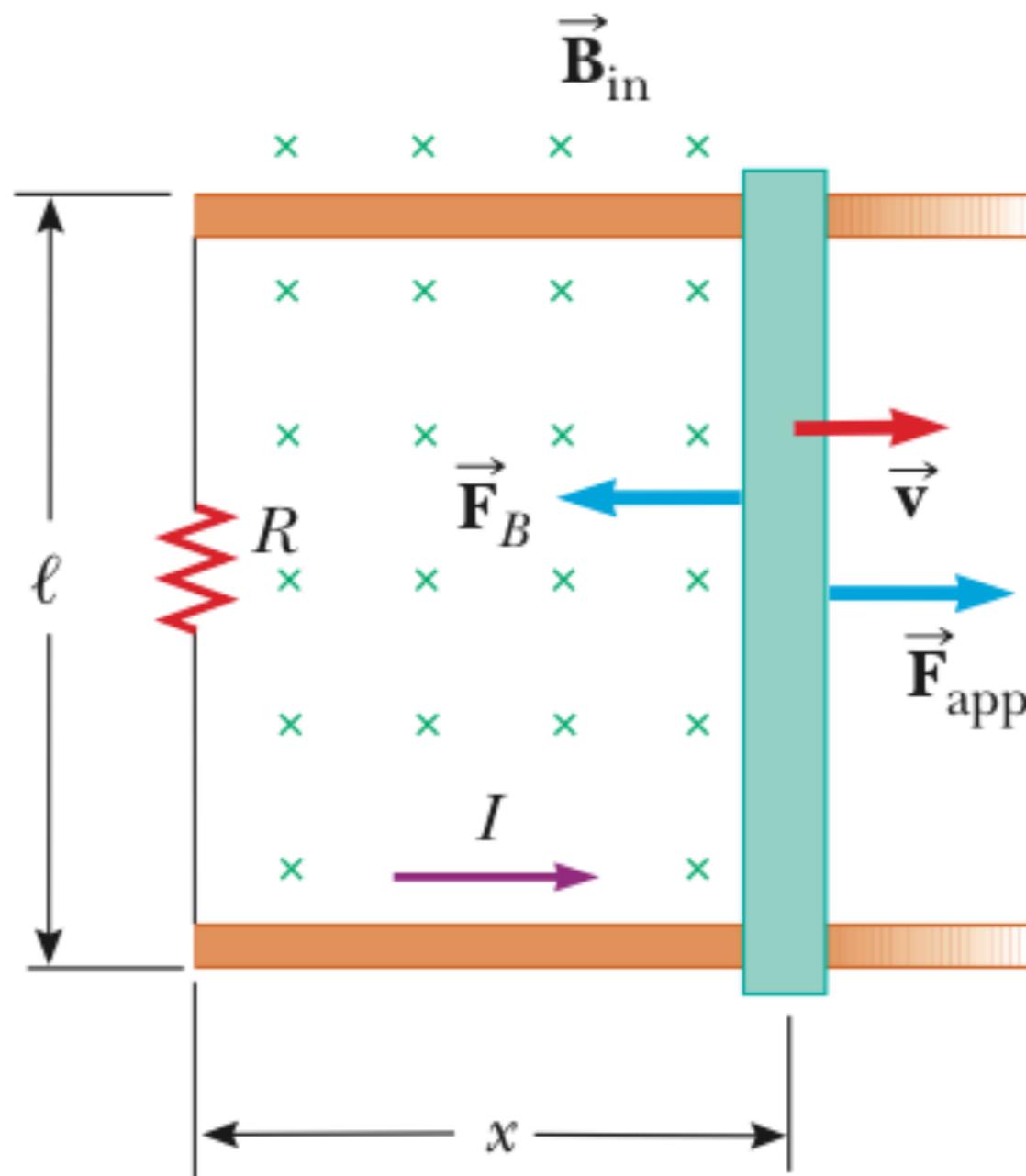
# Lenz's Law



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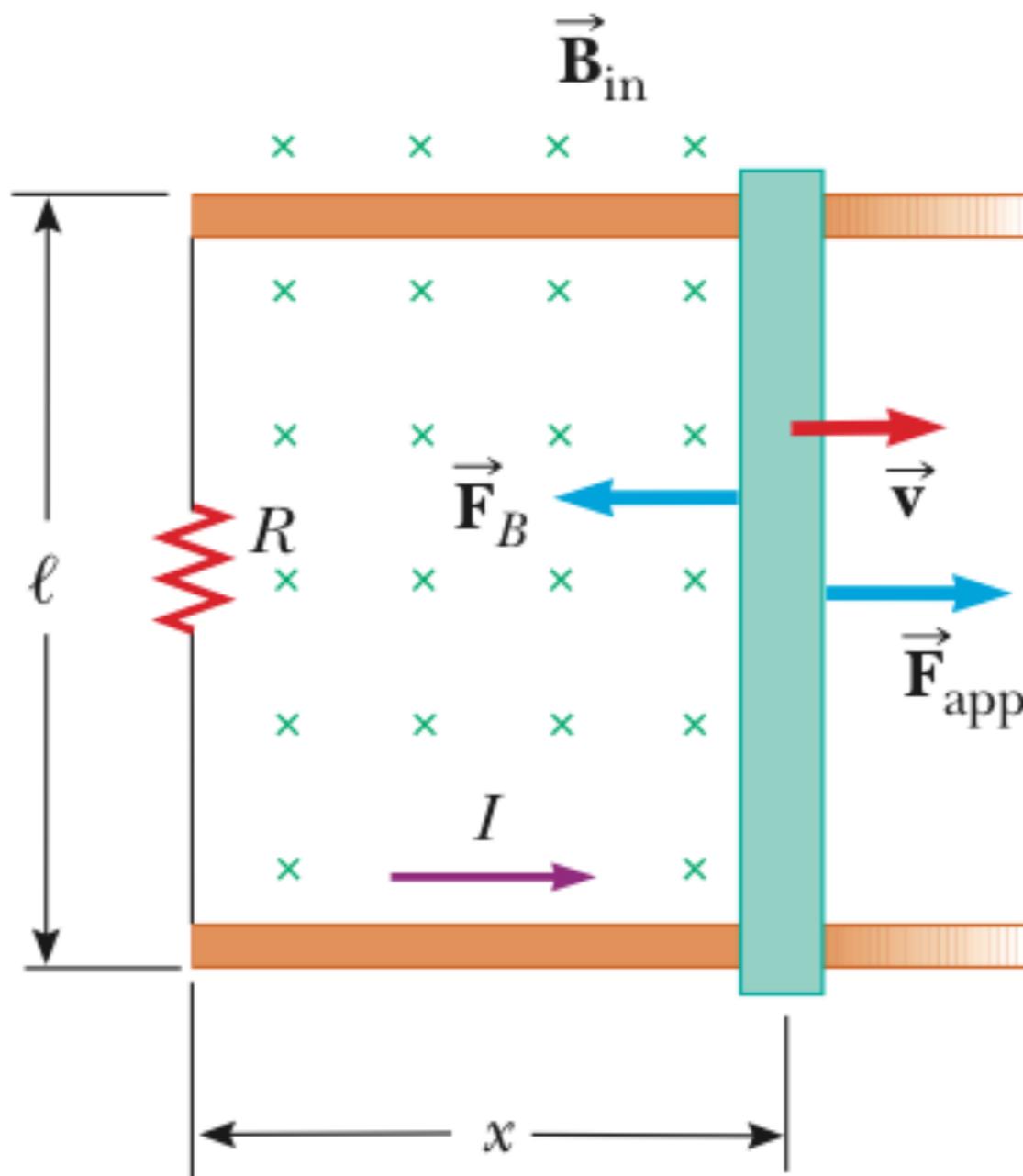


# Lenz's Law

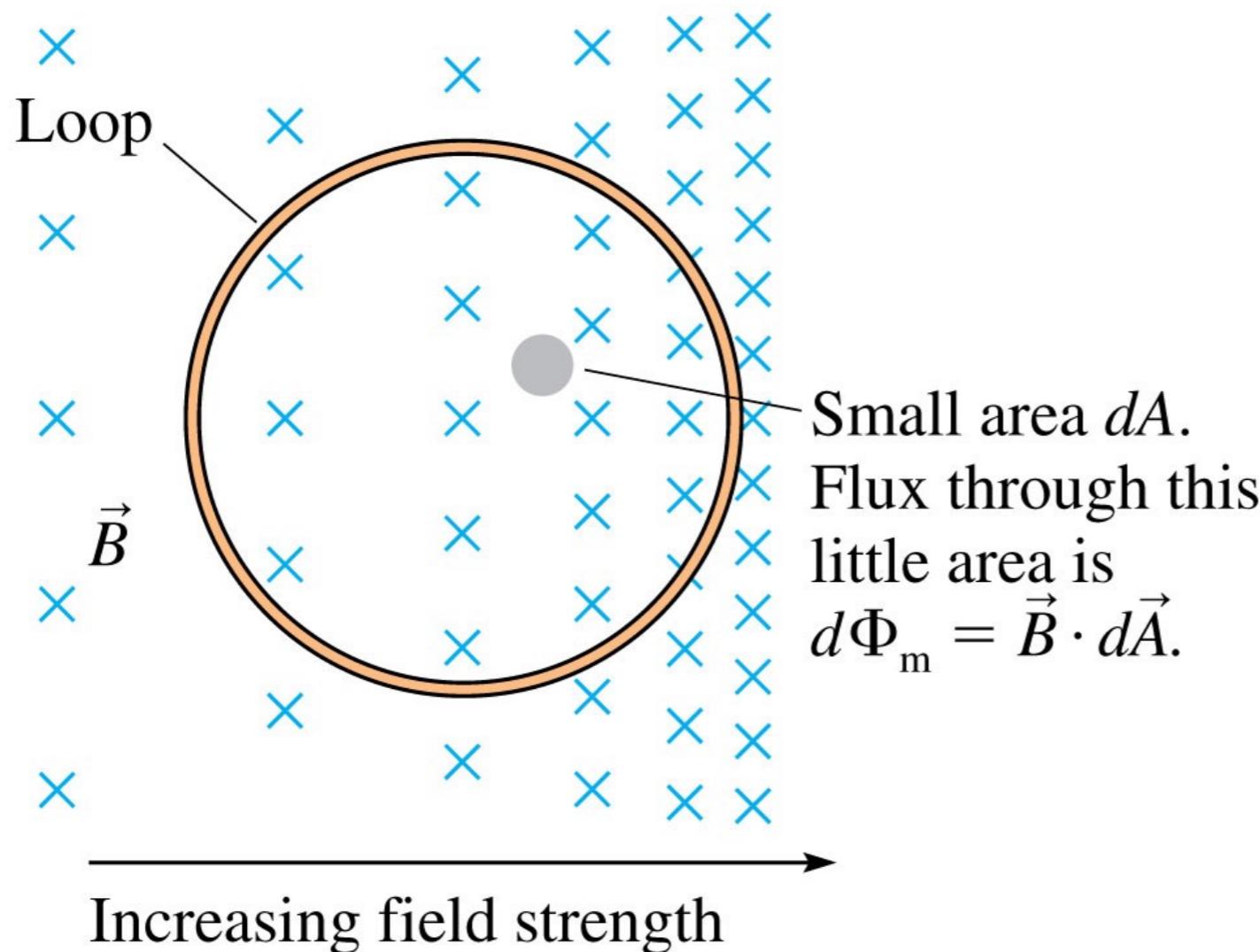


# Lenz's Law

$$\Phi_m = \int_{\text{area of loop}} \vec{B} \cdot d\vec{A}$$



# Magnetic Flux



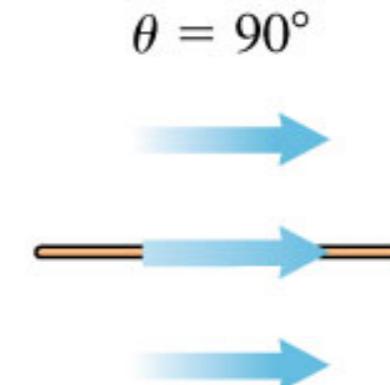
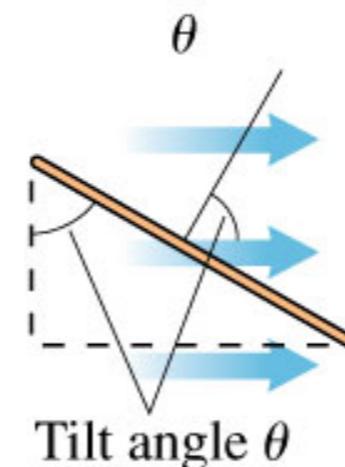
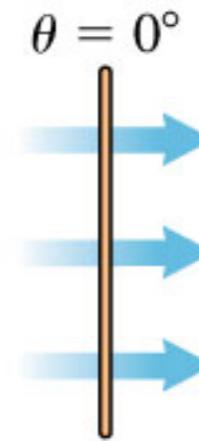
$$\Phi_m = \int_{\text{area of loop}} \vec{B} \cdot d\vec{A}$$

# Flux again

Draw the loop and field from the perspective of a person standing to the right of the loop looking left.



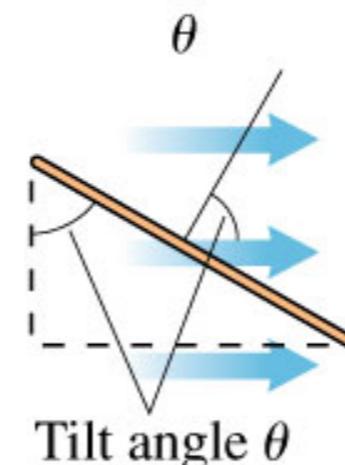
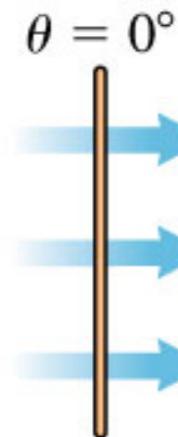
Loop seen from the side



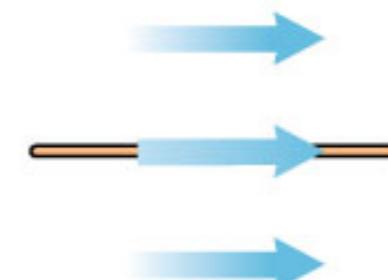
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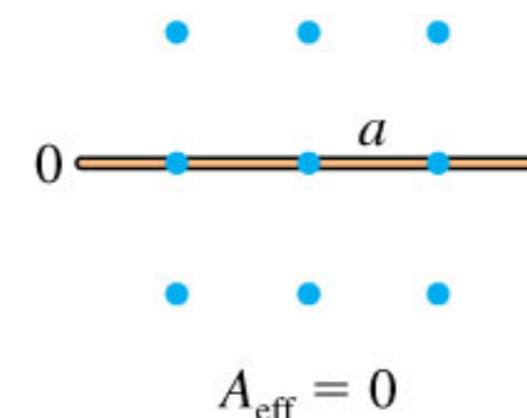
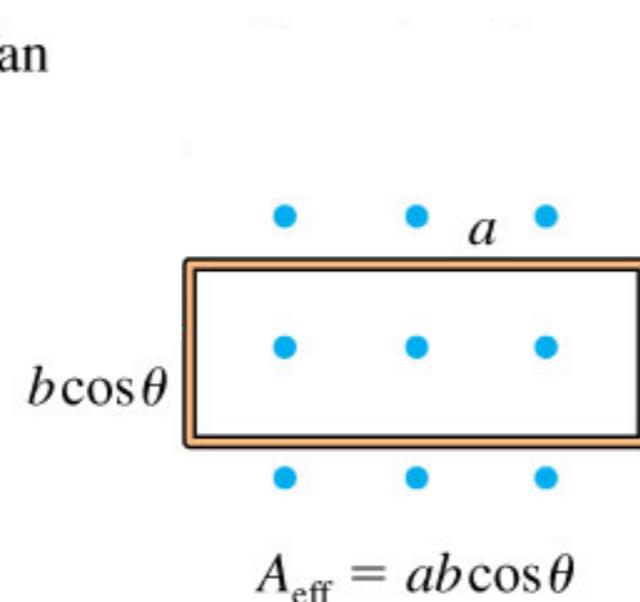
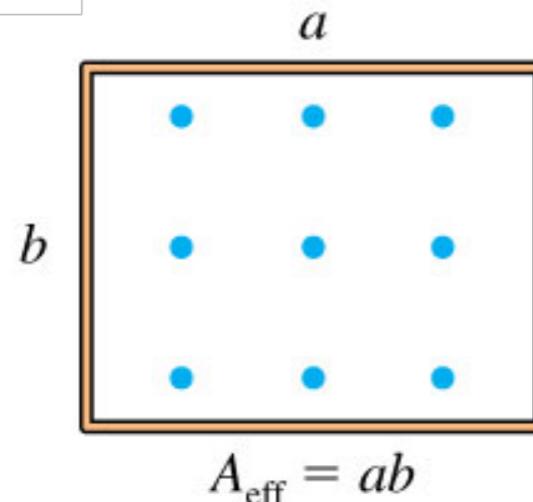
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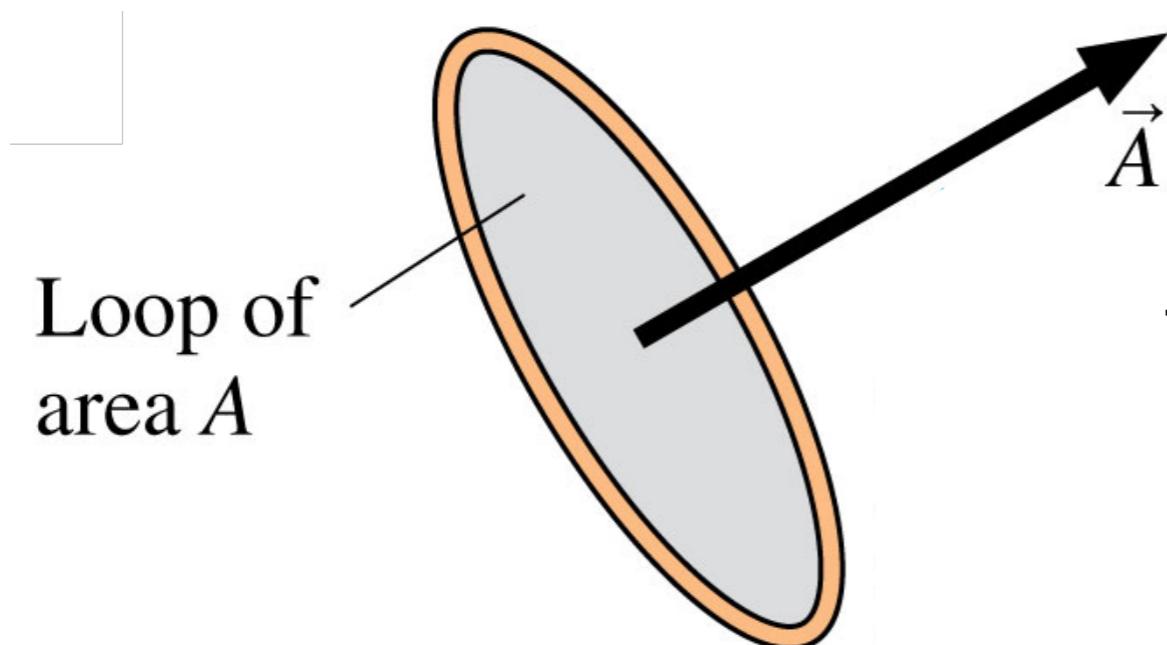
$\theta = 90^\circ$



Loop seen facing the fan



# Area Vector



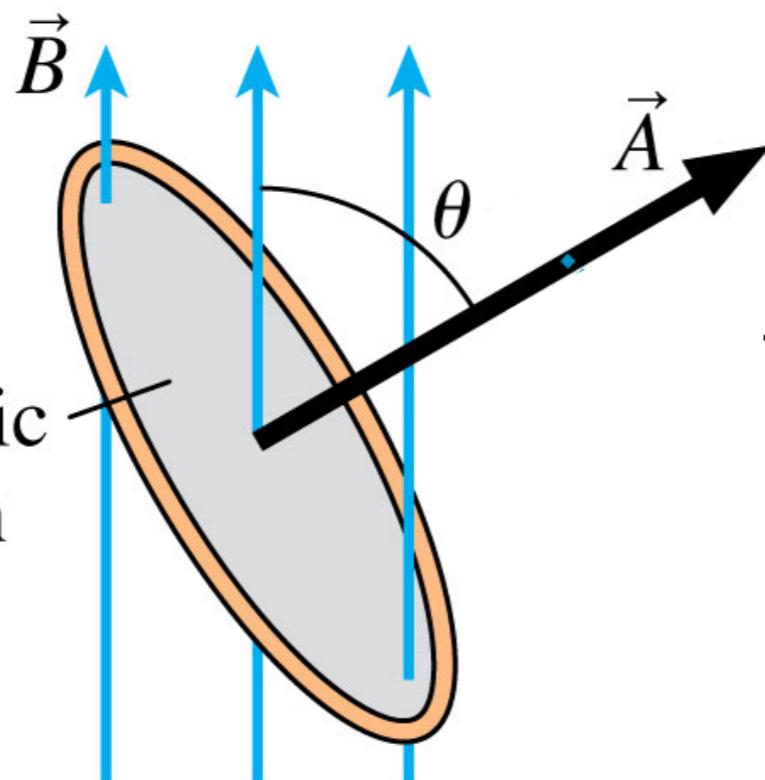
$$\Phi_m = A_{\text{eff}}B = AB \cos \theta$$

Loop of  
area  $A$

The SI unit of magnetic flux is the **weber**:  
1 weber = 1 Wb = 1 T m<sup>2</sup>

# Area Vector

The magnetic flux through the loop is  
 $\Phi_m = \vec{A} \cdot \vec{B}$ .



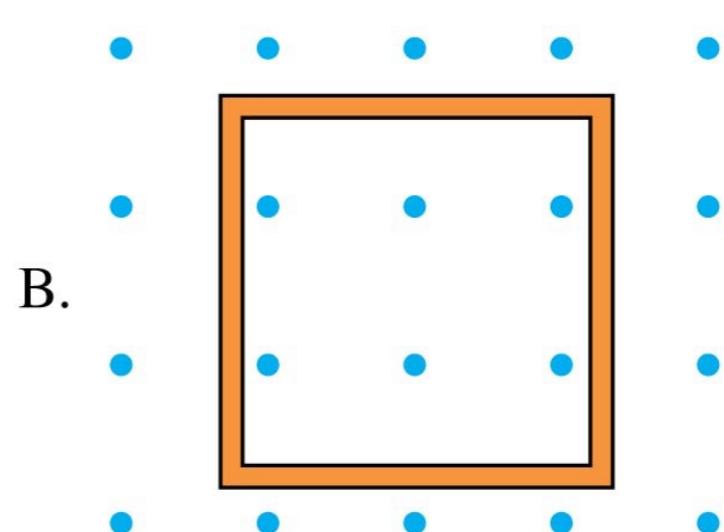
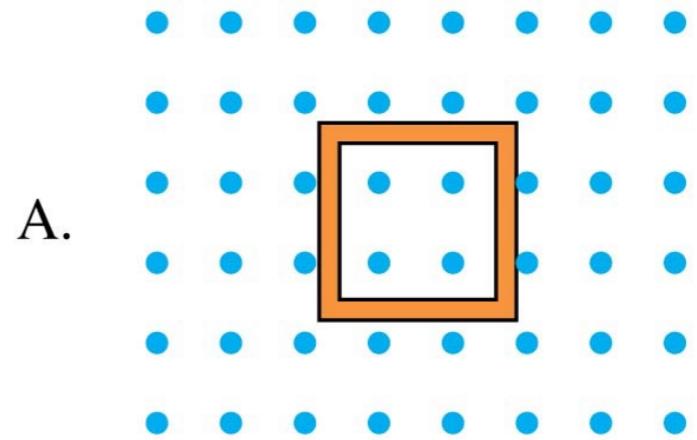
$$\Phi_m = A_{\text{eff}}B = AB \cos \theta$$

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# Quiz Question

Which loop has the larger magnetic flux through it?

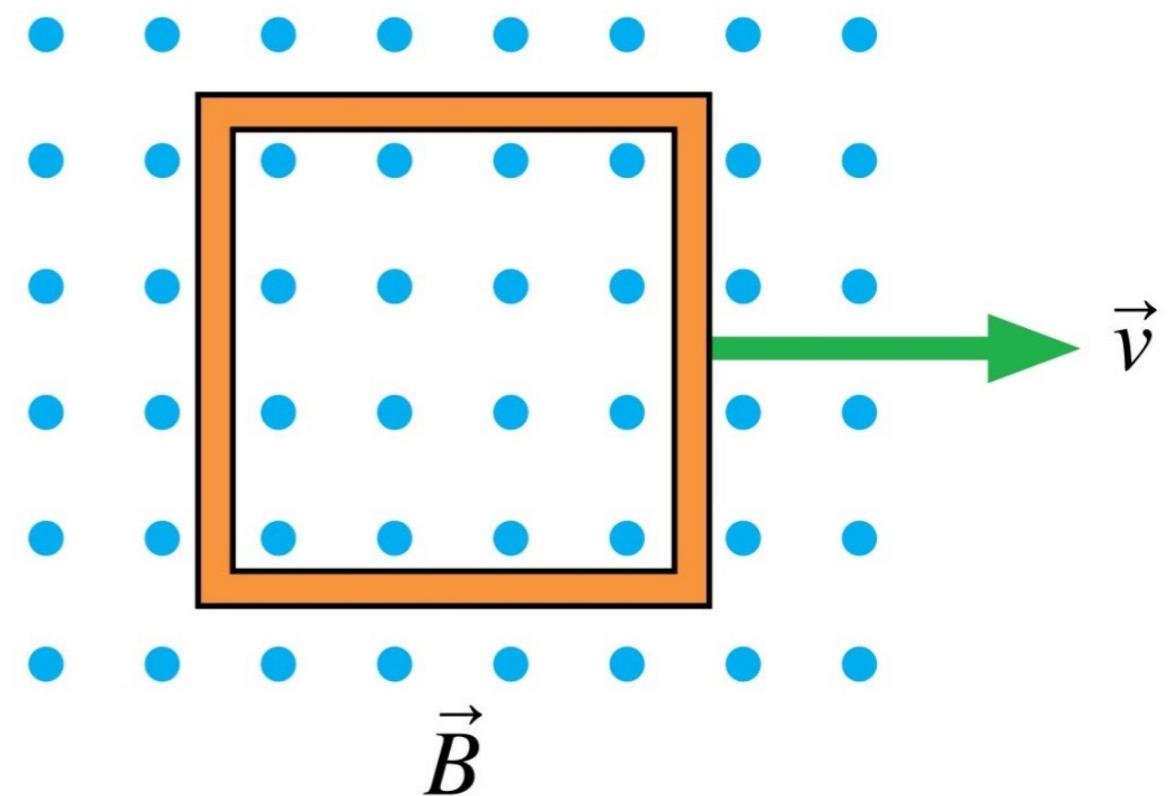
- A. Loop A.
- B. Loop B.
- C. The fluxes are the same.
- D. Not enough information to tell.



# Quiz Question

The metal loop is being pulled through a uniform magnetic field. Is the magnetic flux through the loop changing?

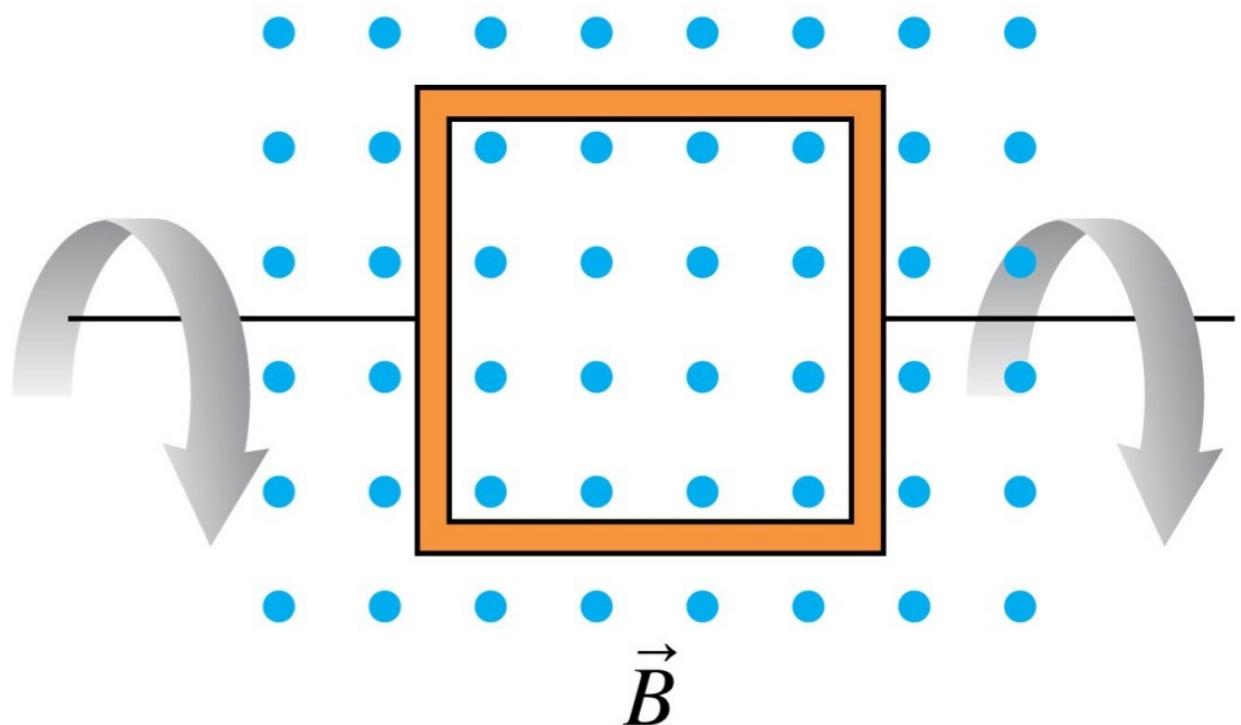
- A. No.
- B. Yes.



# Quiz Question

The metal loop is rotating in a uniform magnetic field. Is the magnetic flux through the loop changing?

- A. Yes.
- B. No.



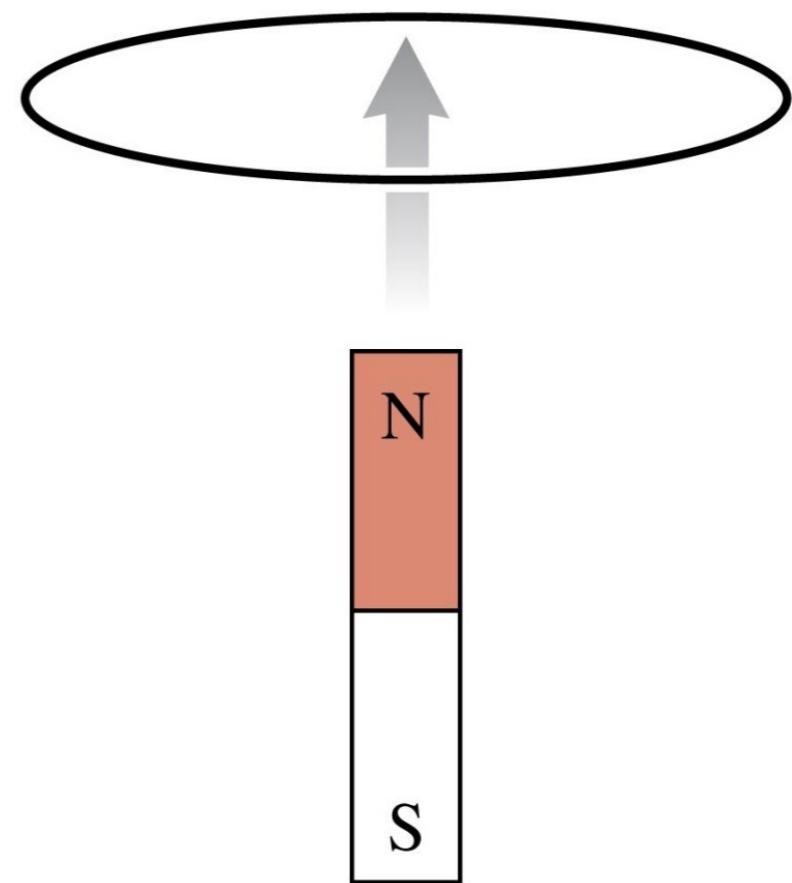
# Lenz's Law

There is an induced current in a closed, conducting loop if and only if the magnetic flux through the loop is changing. The direction of the induced current is such that the induced magnetic field opposes the change in flux.

# Quiz Question

The bar magnet is pushed toward the center of a wire loop. Which is true?

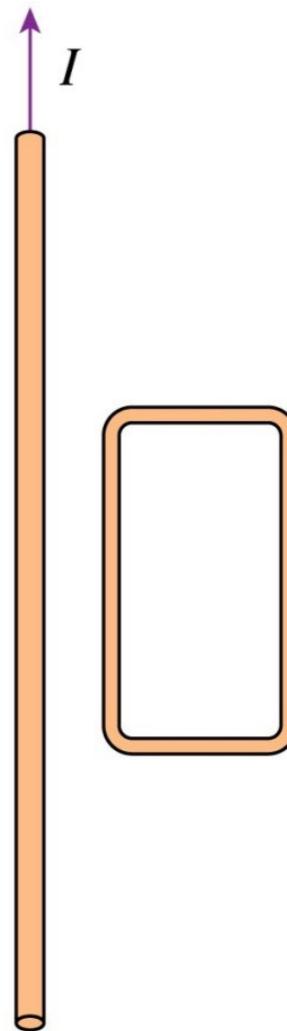
- A. There is no induced current in the loop.
- B. There is a counterclockwise induced current in the loop.
- C. There is a clockwise induced current in the loop.



# Quiz Question

The current in the straight wire is decreasing. Which is true?

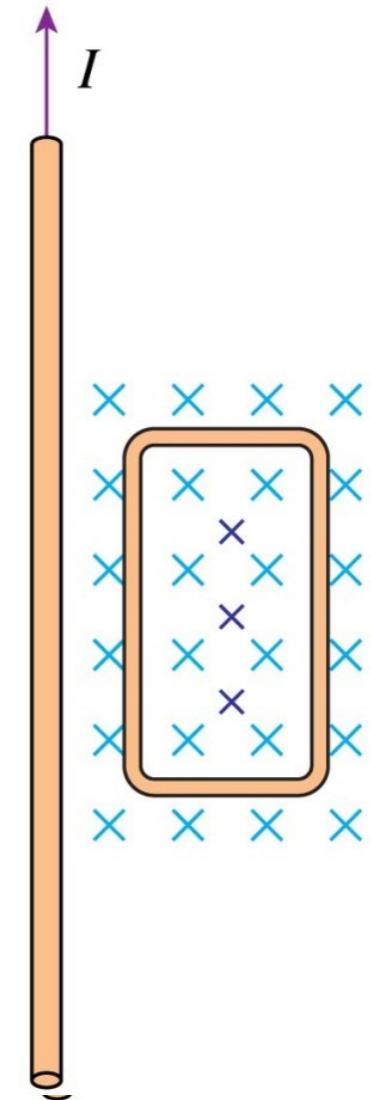
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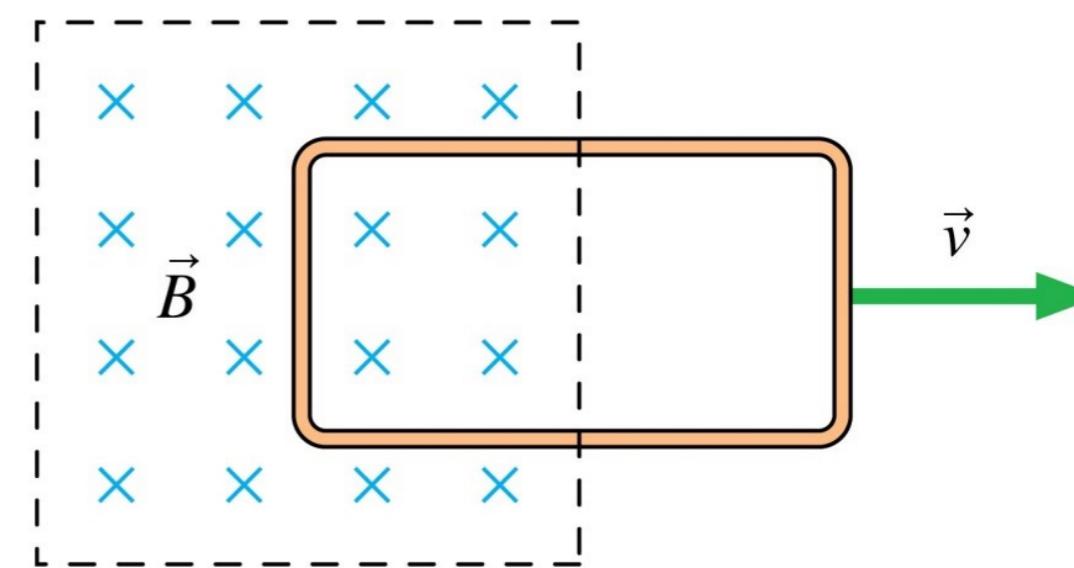
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# Quiz Question

The magnetic field is confined to the region inside the dashed lines; it is zero outside. The metal loop is being pulled out of the magnetic field. Which is true?

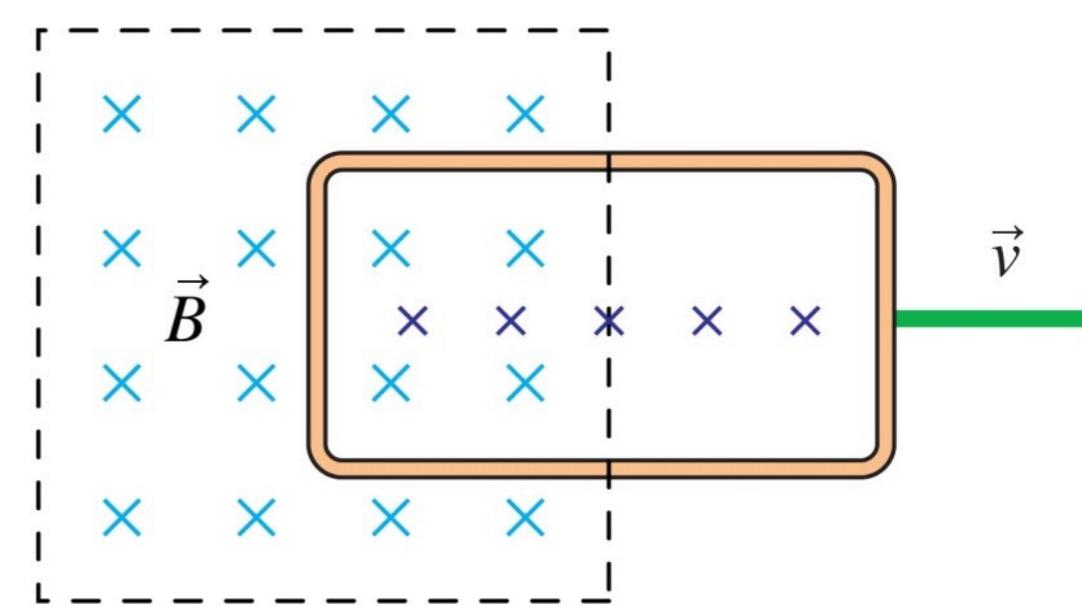
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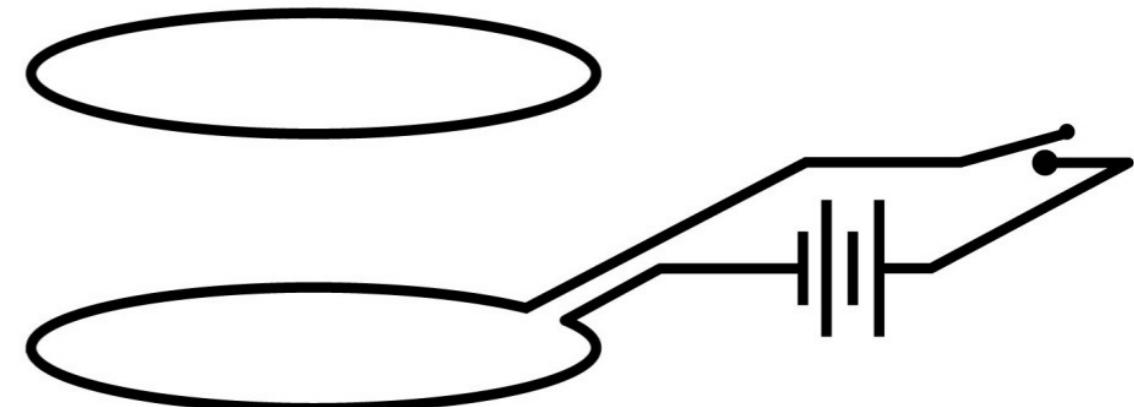
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# Quiz Question

Immediately after the switch is closed, the lower loop exerts \_\_\_\_ on the upper loop.

- A. a torque
- B. an upward force
- C. a downward force
- D. no force or torque



# Faraday's Law

The magnitude of the potential difference is given by Faraday's law.....

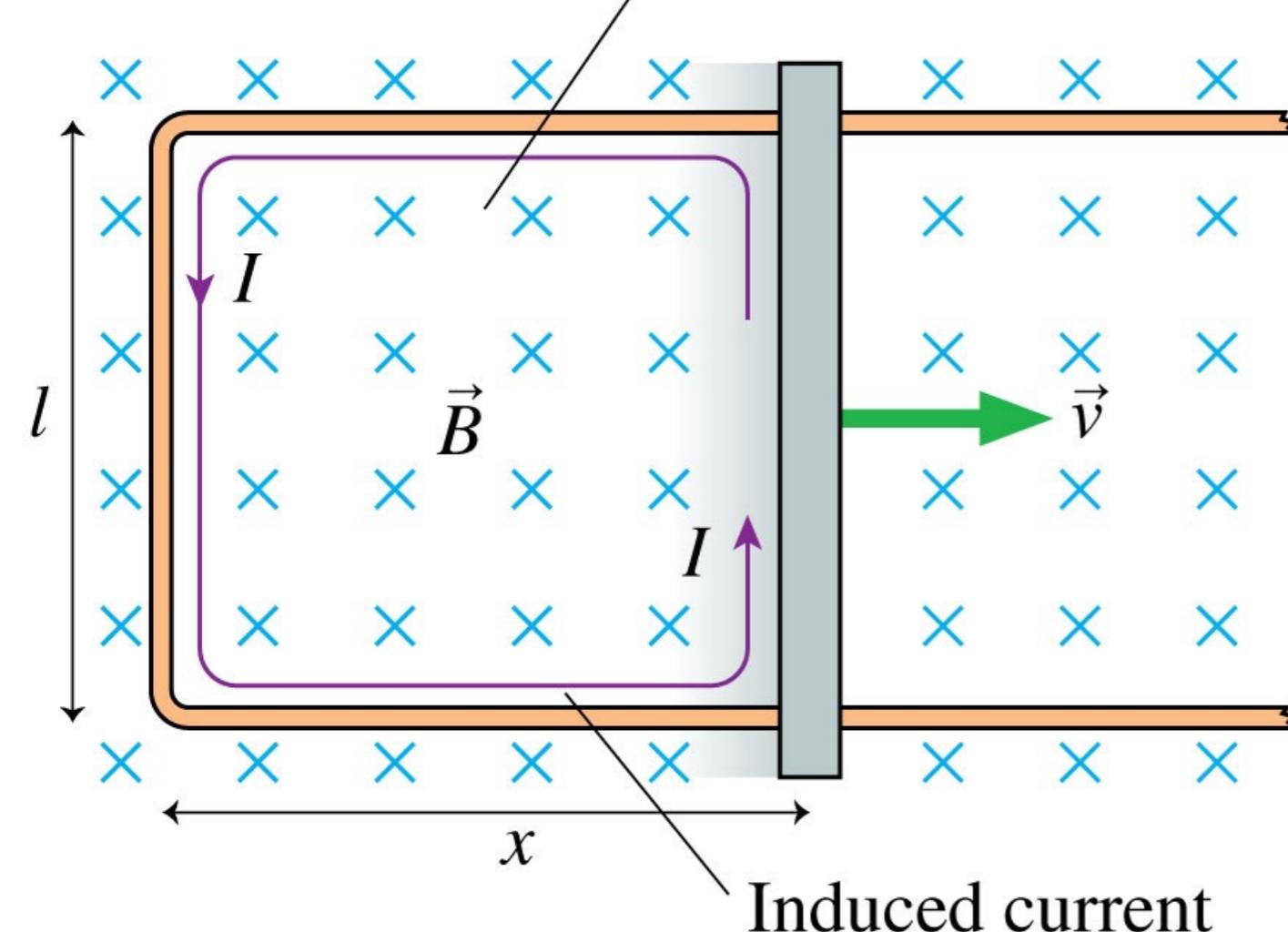
$$\mathcal{E} = \left| \frac{d\Phi}{dt} \right|$$

The direction is given by Lenz's law...

# Let's try it out

$$\text{Magnetic flux } \Phi_m = AB = xlB$$

$$\mathcal{E} = \left| \frac{d\Phi}{dt} \right|$$



You and your neighbor use different methods for finding the induced emf.

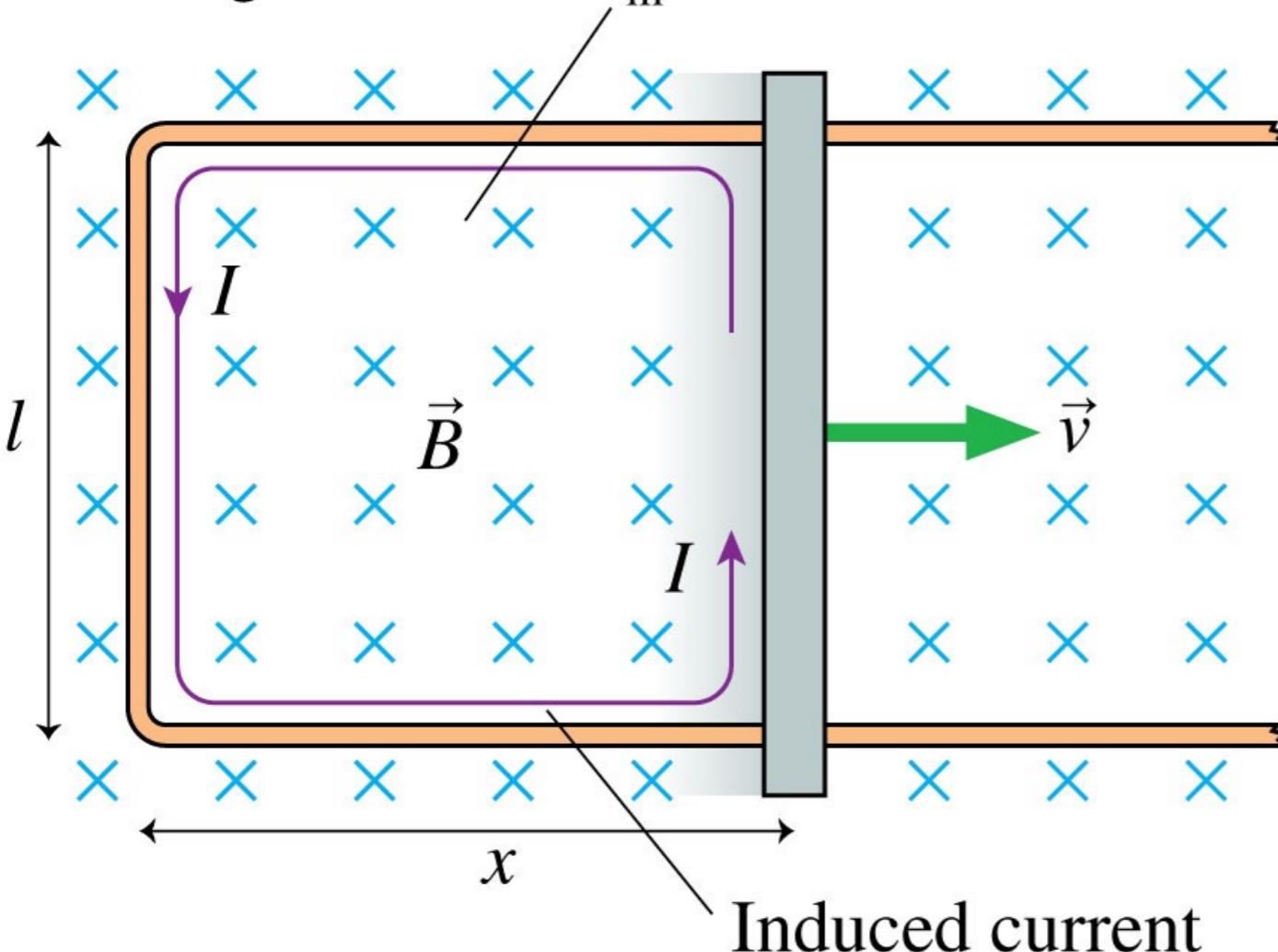
- 1) Use the idea of magnetic forces.
- 2) Use Faraday's law.

Compare your answers.

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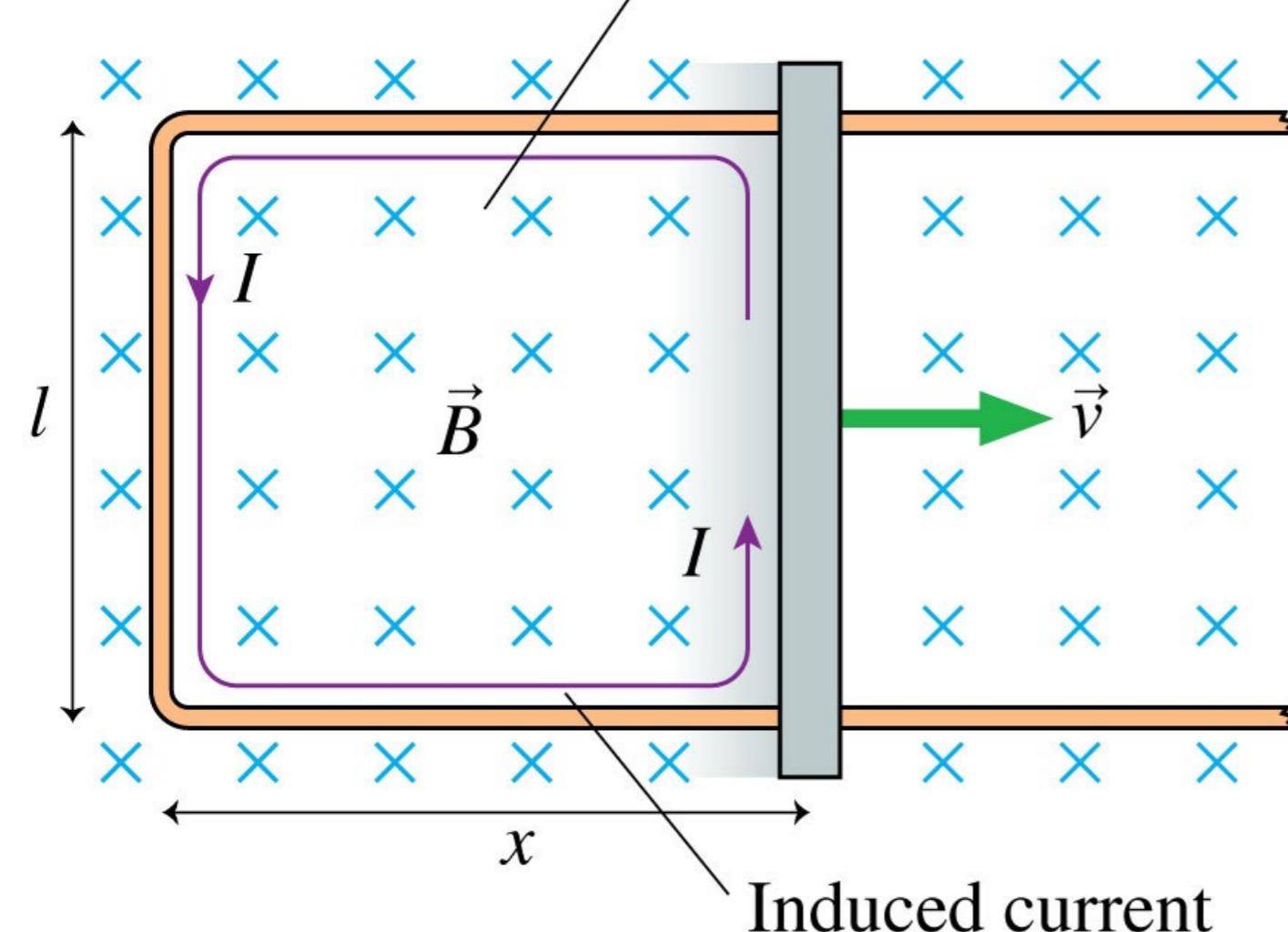
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$$\mathcal{E} = \left| \frac{d\Phi_m}{dt} \right| = \frac{d}{dt}(xlB) = \frac{dx}{dt}lB = vLB$$

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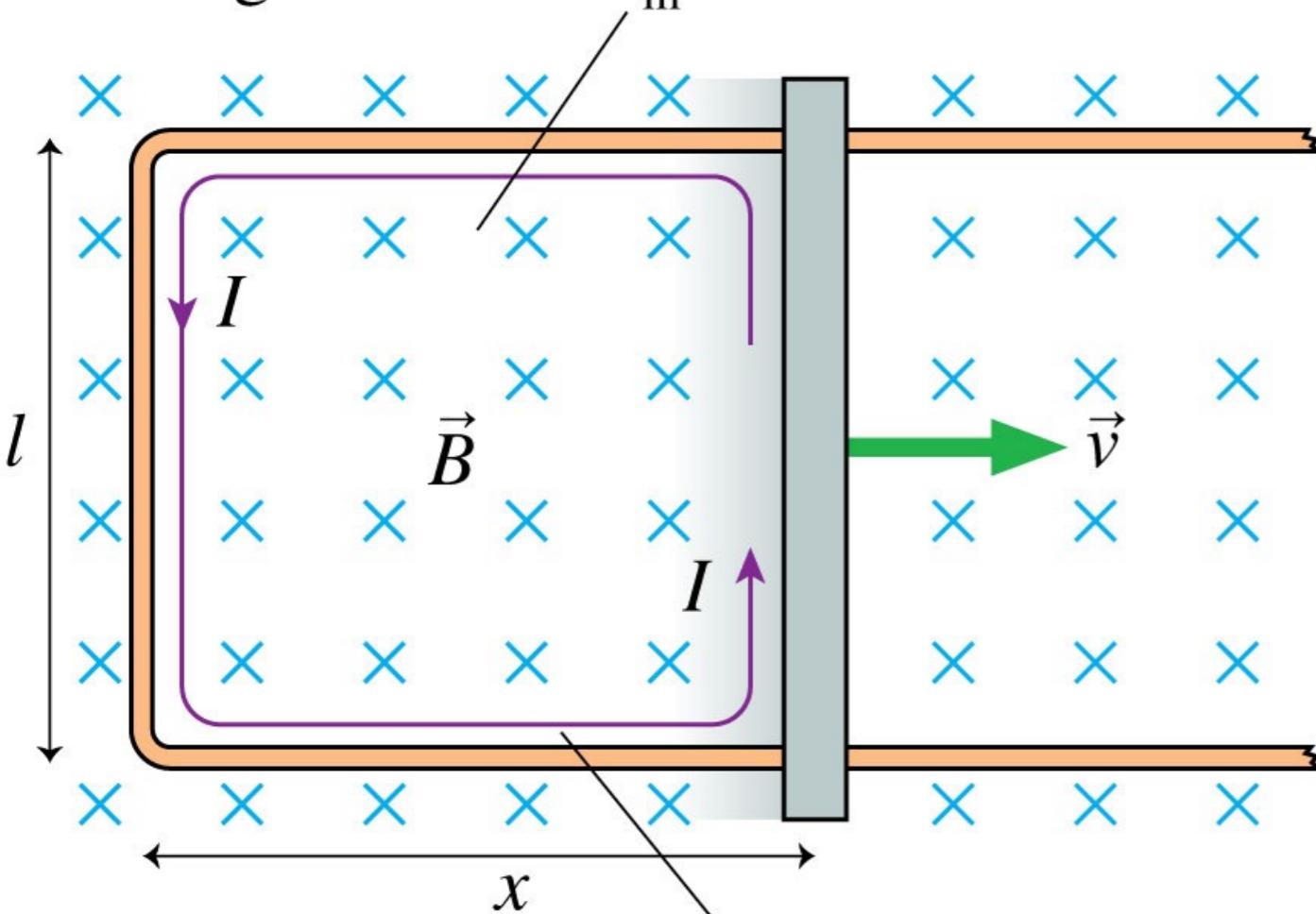
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Magnetic flux  $\Phi_m = AB = xlB$

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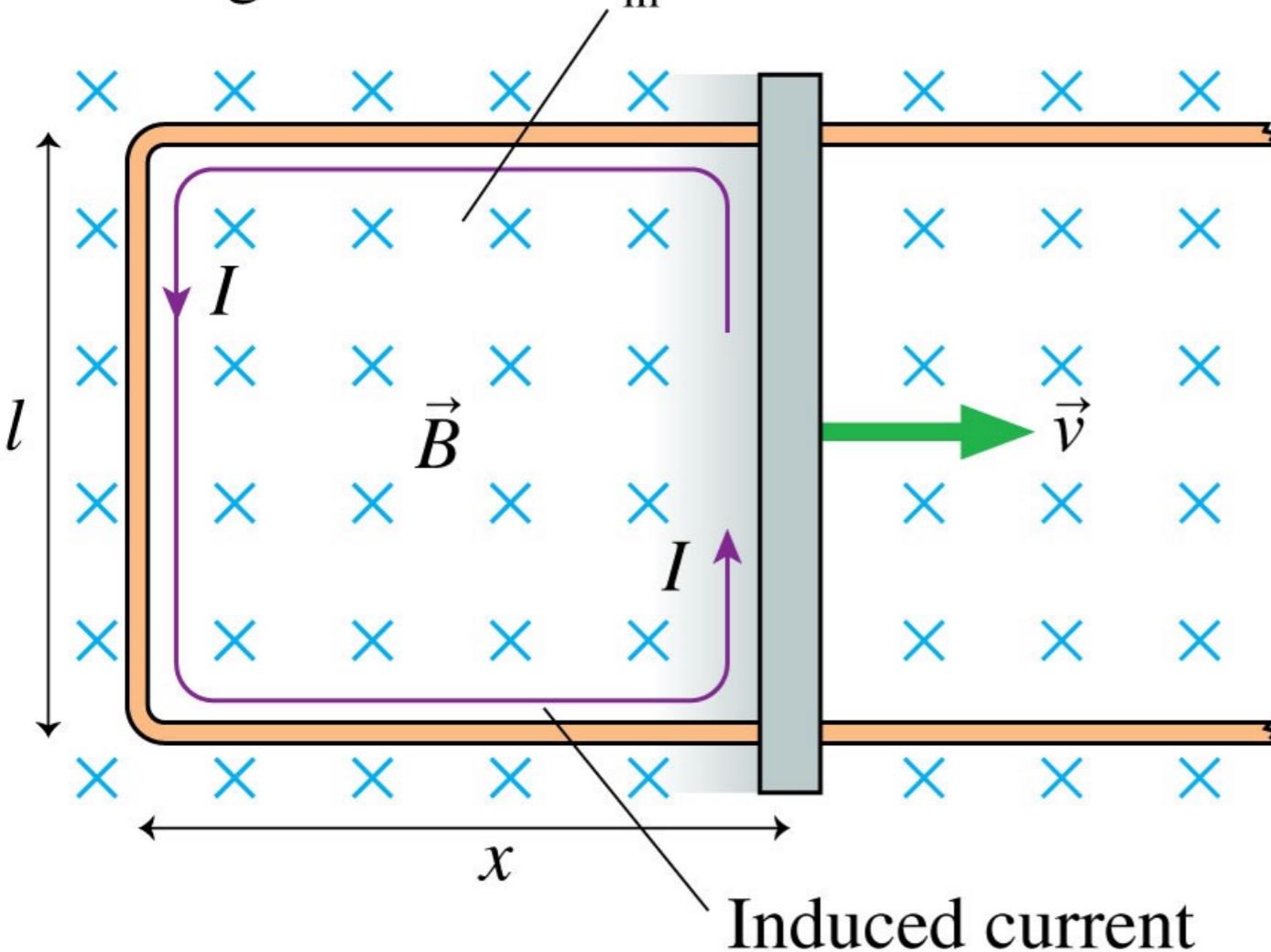
Compare your answers.

$$qE = qvB$$
$$E = vB$$

# Let's try it out

$$\text{Magnetic flux } \Phi_m = AB = xlB$$

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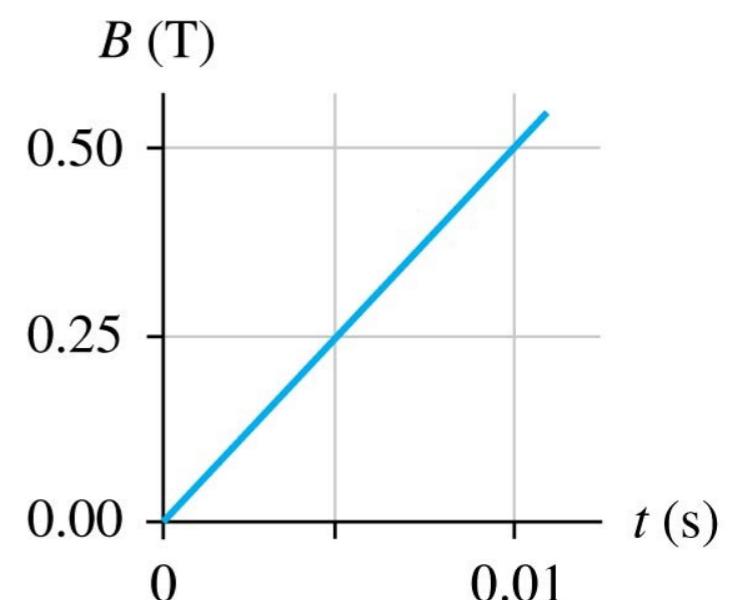
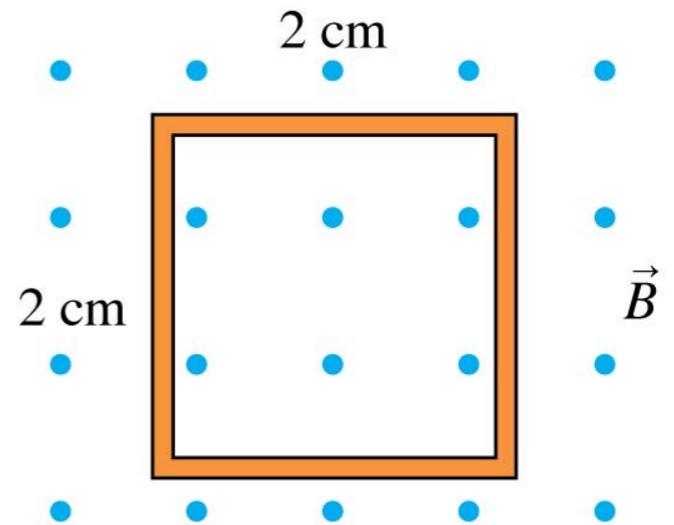
Compare your answers.

$$\begin{aligned} qE &= qvB \\ E &= vB \end{aligned}$$

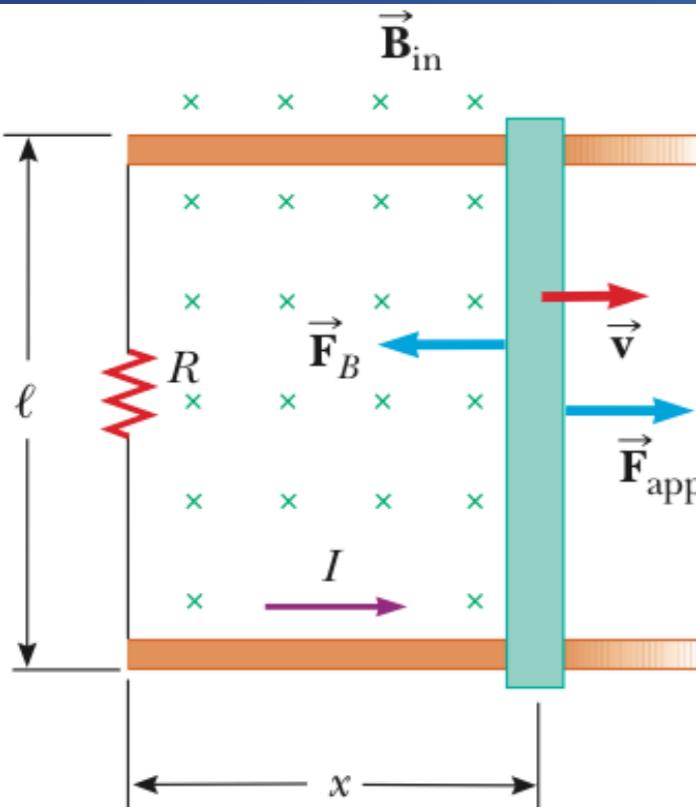
$$V = vBl$$

The induced emf around this loop is

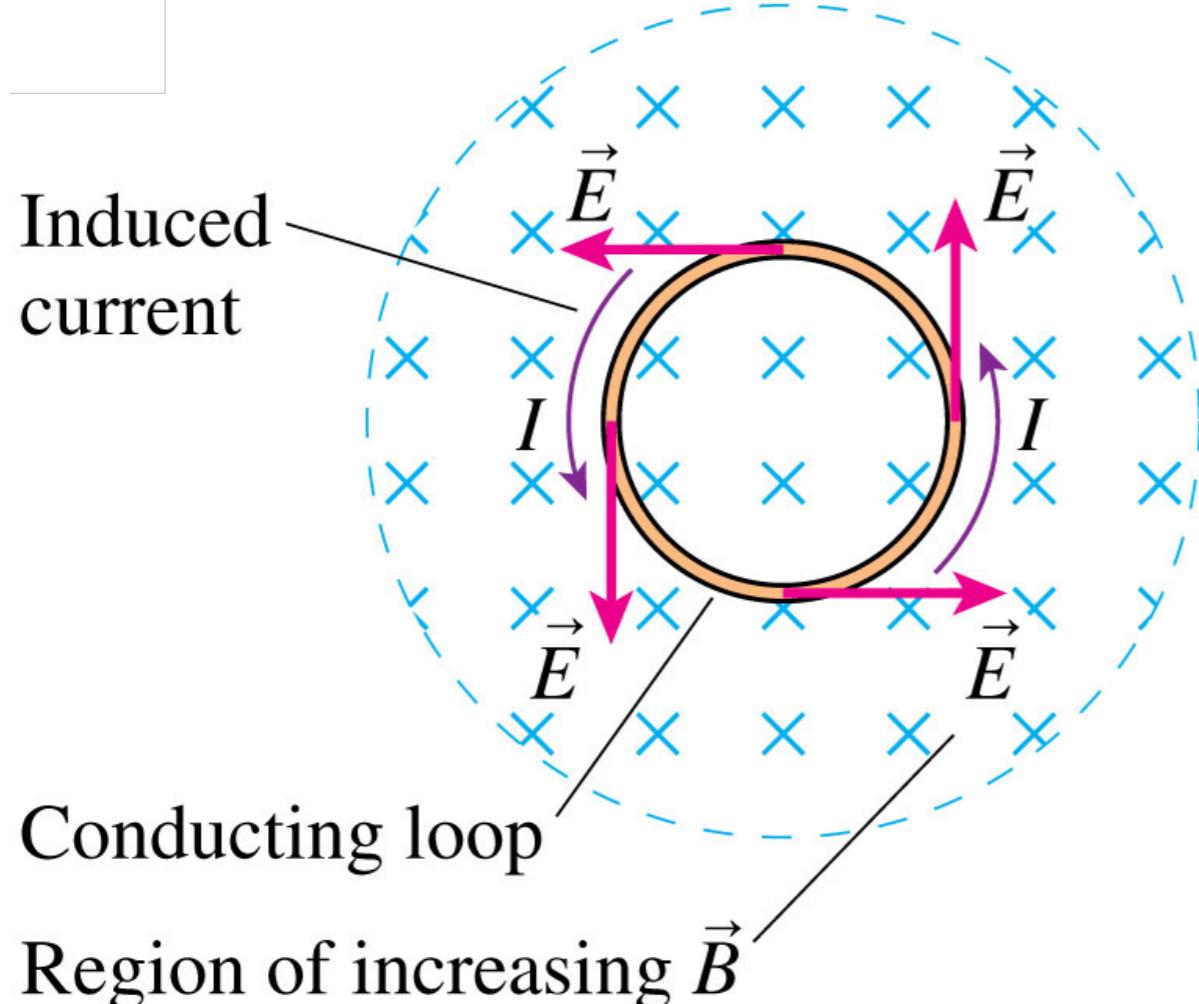
- A. 200 V.
- B. 50 V.
- C. 2 V.
- D. 0.5 V.
- E. 0.02 V.



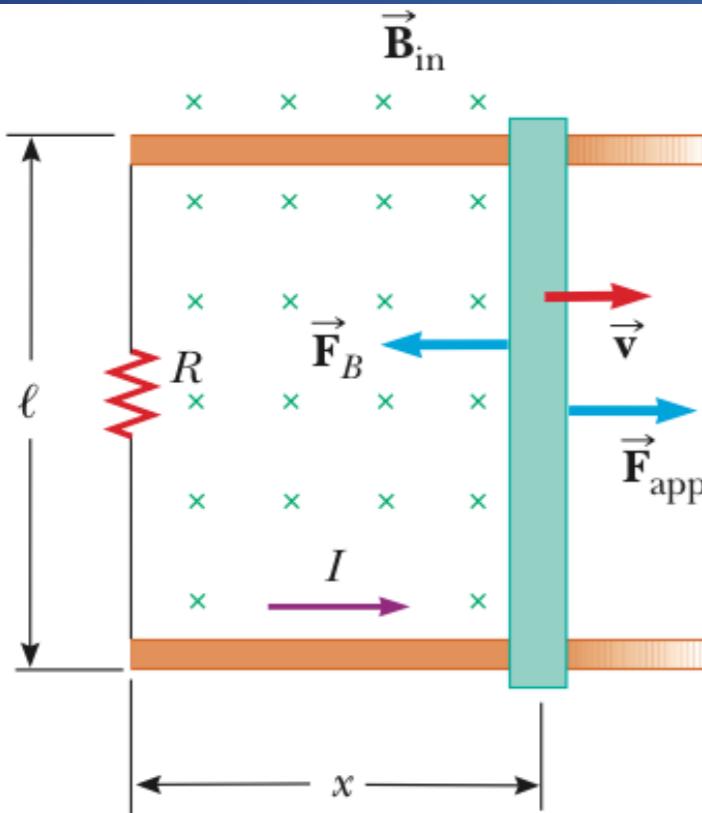
# Induced Field



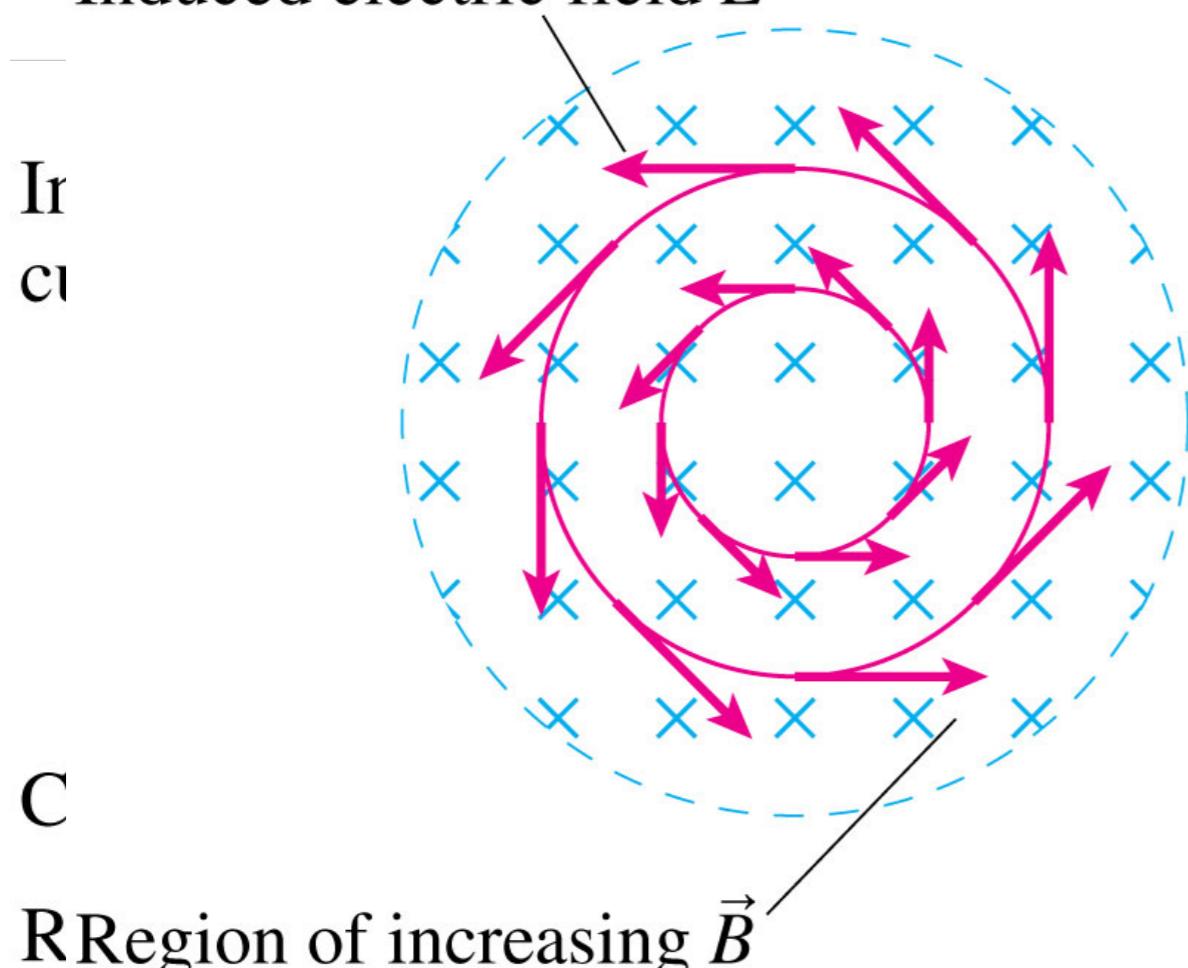
This is not the electric field that we are used to. It's a new kind of field called an "induced" electric field



# Induced Field



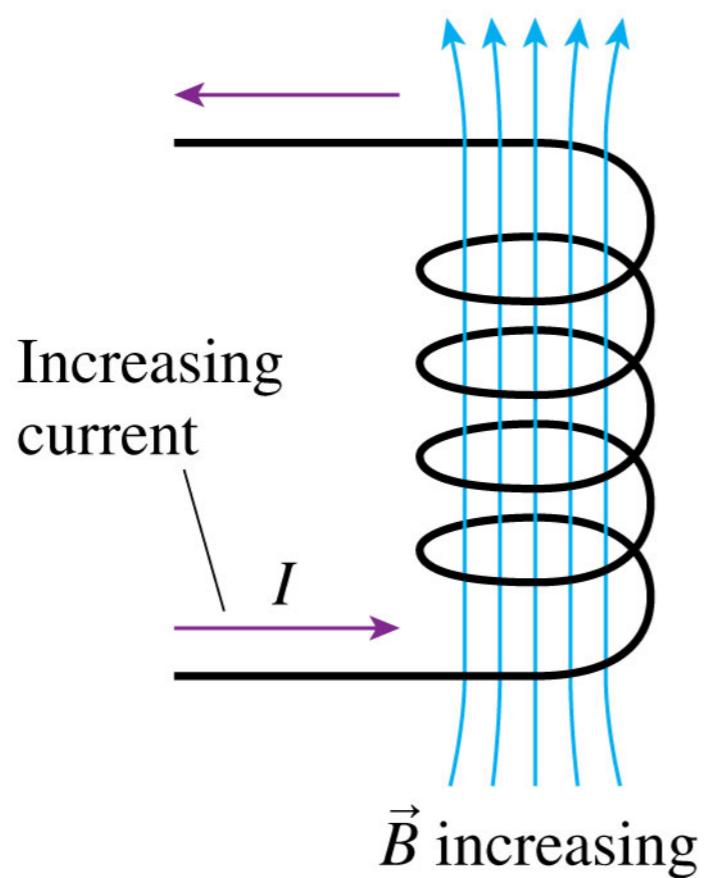
Induced electric field  $\vec{E}$



This is not the electric field that we are used to. It's a new kind of field called an "induced" electric field

The field is there whether there is a conductive loop present or not.

The current through the solenoid is increasing.



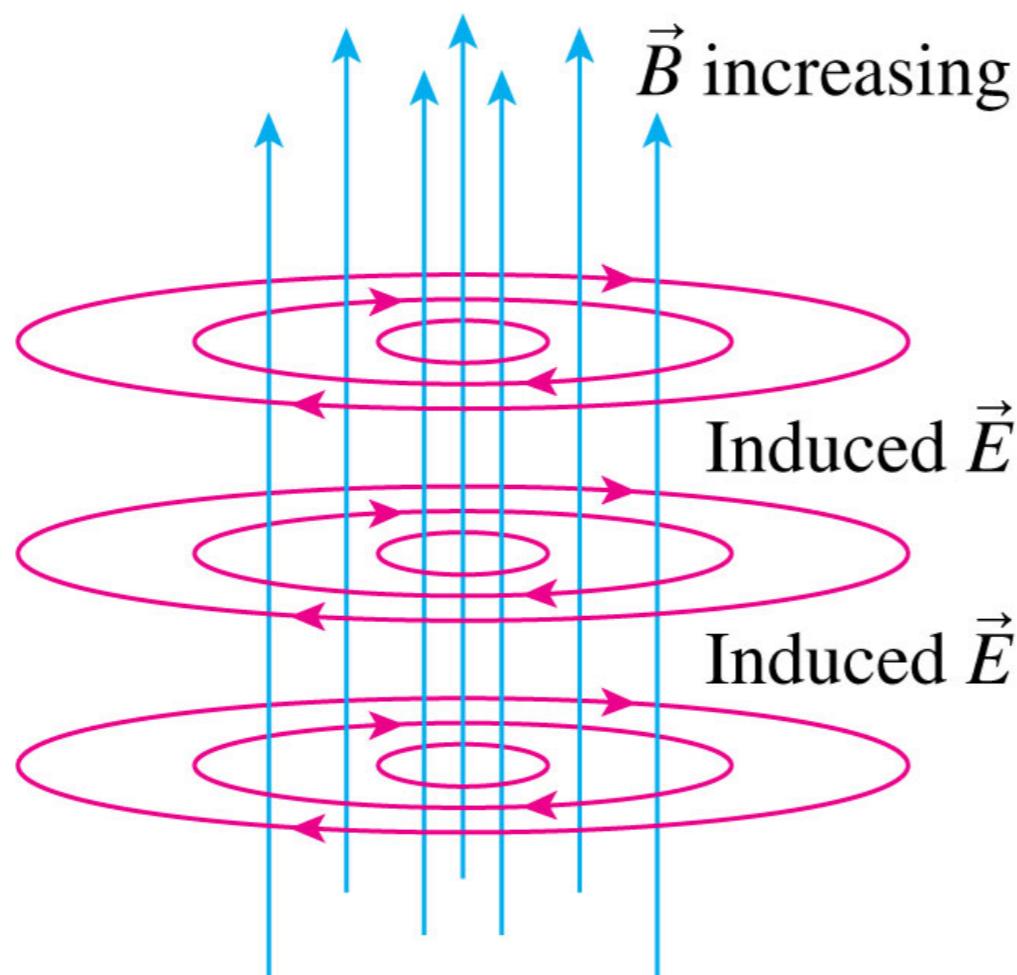
$$\mathcal{E} = \left| \frac{d\Phi}{dt} \right|$$

Convince yourself that the expression below is the same as the expression above for this situation. Then convince your neighbor.

$$\oint \vec{E} \cdot d\vec{s} = A \left| \frac{dB}{dt} \right|$$

Once again: The induced field is there whether the solenoid is present or not.

- The induced electric field circulates around the magnetic field lines.



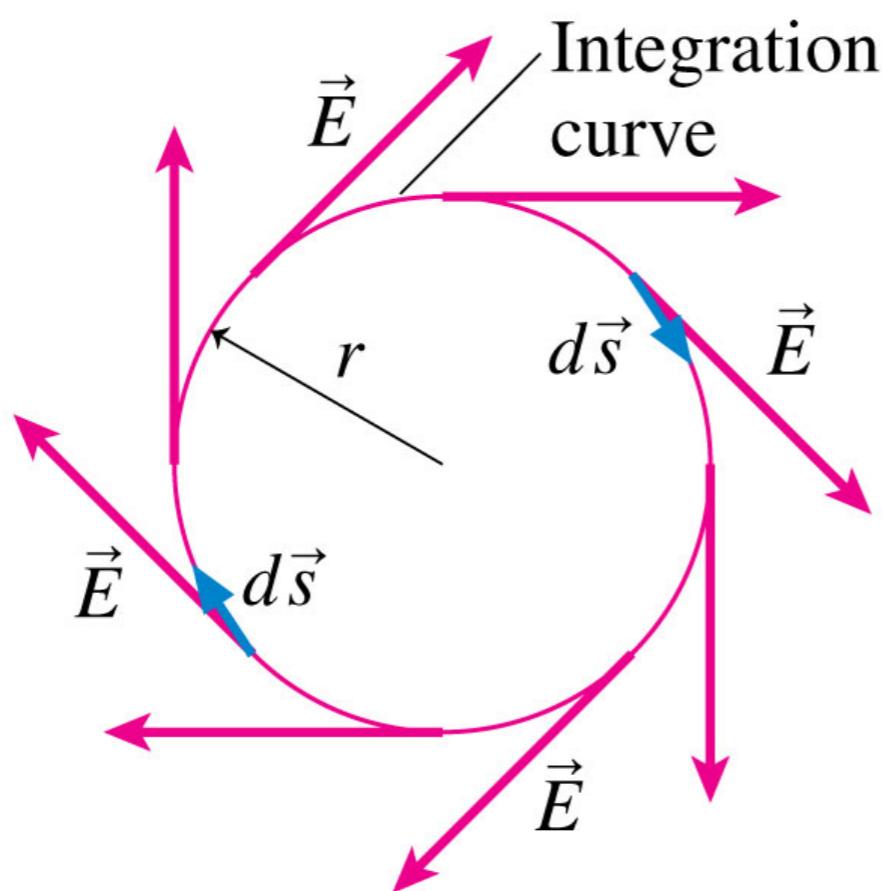
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- Top view into the solenoid.  
 $\vec{B}$  is coming out of the page.

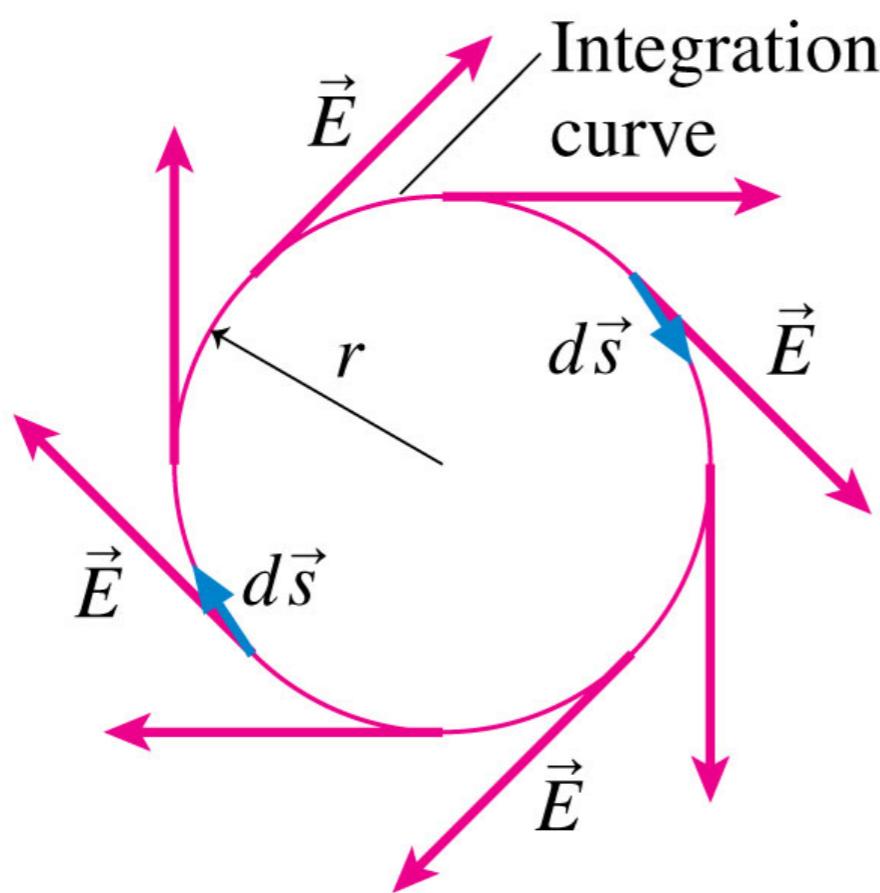
$$\oint \vec{E} \cdot d\vec{s} = A \left| \frac{dB}{dt} \right|$$



Assemble this equation for this situation and solve for the induced electric field

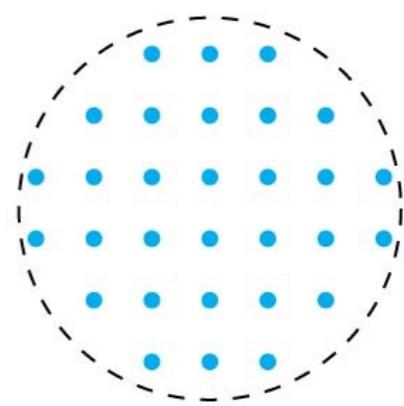
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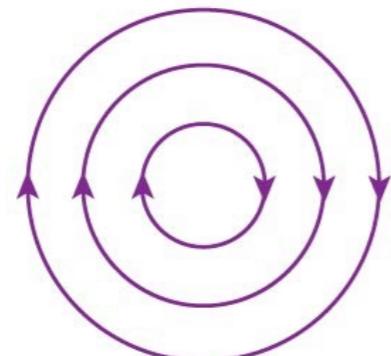


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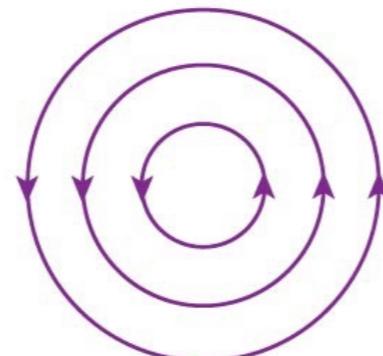
$$E_{\text{inside}} = \frac{r}{2} \left| \frac{dB}{dt} \right|$$



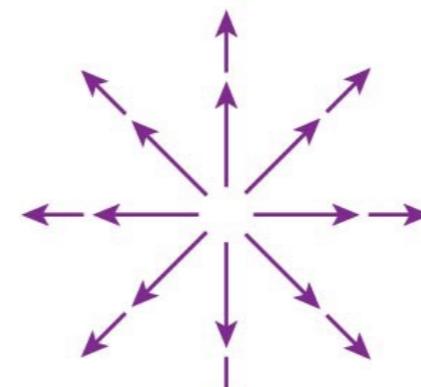
The magnetic field is decreasing.  
Which is the induced electric field?



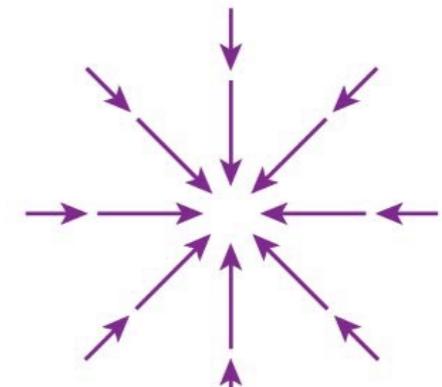
A.



B.



C.



D.

E. There's no induced field in this case.