



Lance Nelson

disk
ring

$$E = \frac{2k|\lambda|}{r}$$

$$E = \frac{kq}{r^2}$$

$$E_z = \frac{kz|Q|}{(z^2 + R^2)^{3/2}}$$

finite line
infinite line

$$E_z = \frac{k|Q|}{r\sqrt{r^2 + (L/2)^2}}$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{2\vec{p}}{r^3}$$

dipole

sphere

Infinite plane

$$E_z = \frac{\eta}{2\epsilon} \left[1 - \frac{z}{\sqrt{z^2 + R^2}} \right]$$

$$\vec{E} = -\frac{1}{4\pi\epsilon_0} \frac{\vec{p}}{r^3}$$

$$E_x = \frac{\eta}{2\epsilon_0} \quad F = qE$$

$$p = qs$$

disk
ring

$$E = \frac{2k|\lambda|}{r} \quad \boxed{8}$$

$$E = \frac{kq}{r^2} \quad \boxed{7}$$

$$E_z = \frac{kz|Q|}{(z^2 + R^2)^{3/2}} \quad \boxed{6}$$

finite line

infinite line

$$E_z = \frac{k|Q|}{r\sqrt{r^2 + (L/2)^2}} \quad \boxed{9}$$

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dipole

sphere

Infinite plane

$$E_z = \frac{\eta}{2\epsilon} \left[1 - \frac{z}{\sqrt{z^2 + R^2}} \right] \quad \boxed{4}$$

$$p = qs \quad \boxed{1}$$

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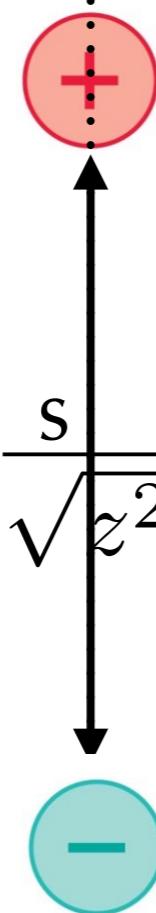
dipole

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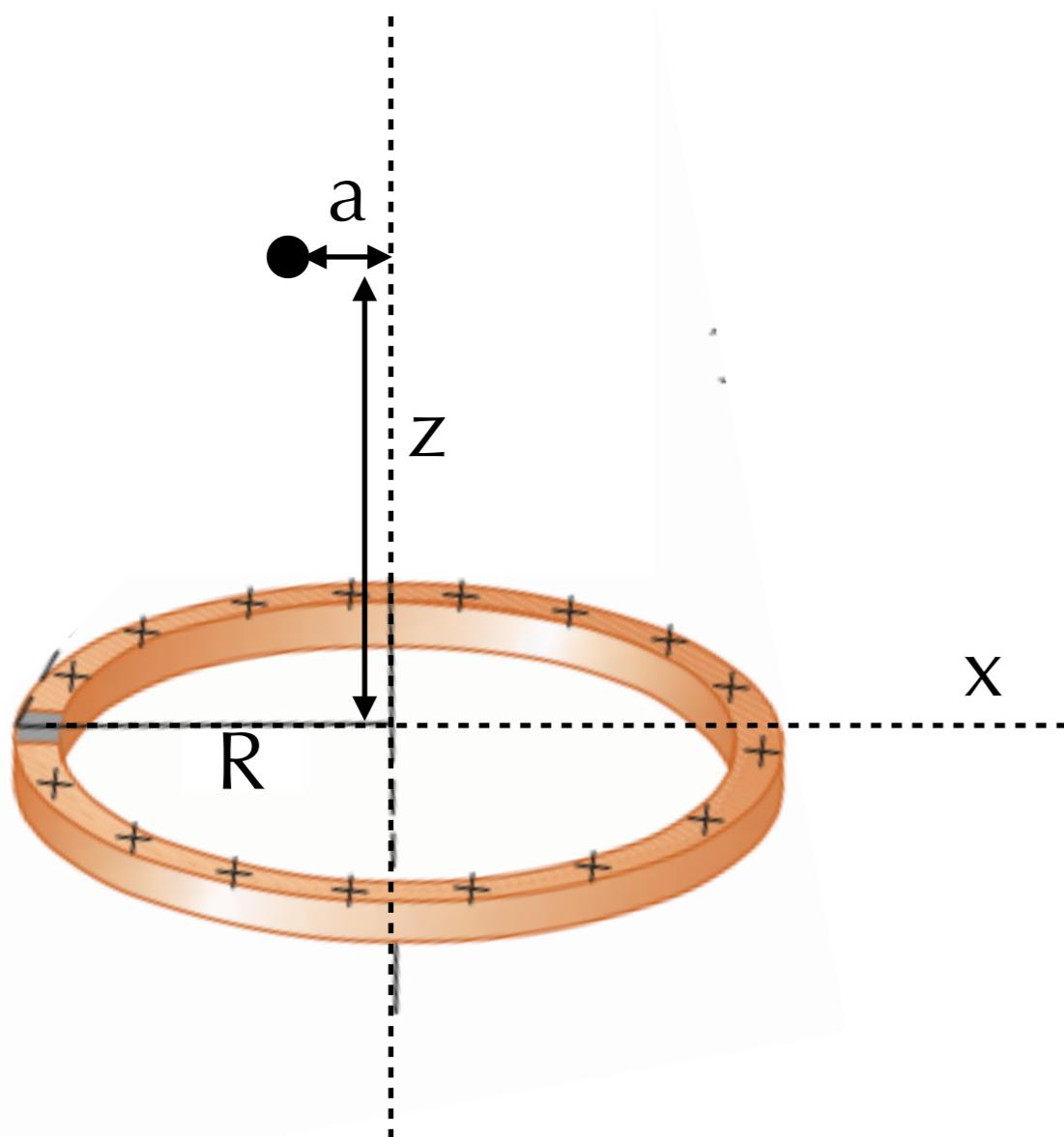
$\boxed{4}$

$$\vec{E} = -\frac{1}{4\pi\epsilon_0} \frac{\vec{p}}{r^3} \quad \boxed{2}$$

$$E_x = \frac{\eta}{2\epsilon_0} \quad F = qE \quad \boxed{10} \quad \boxed{5}$$

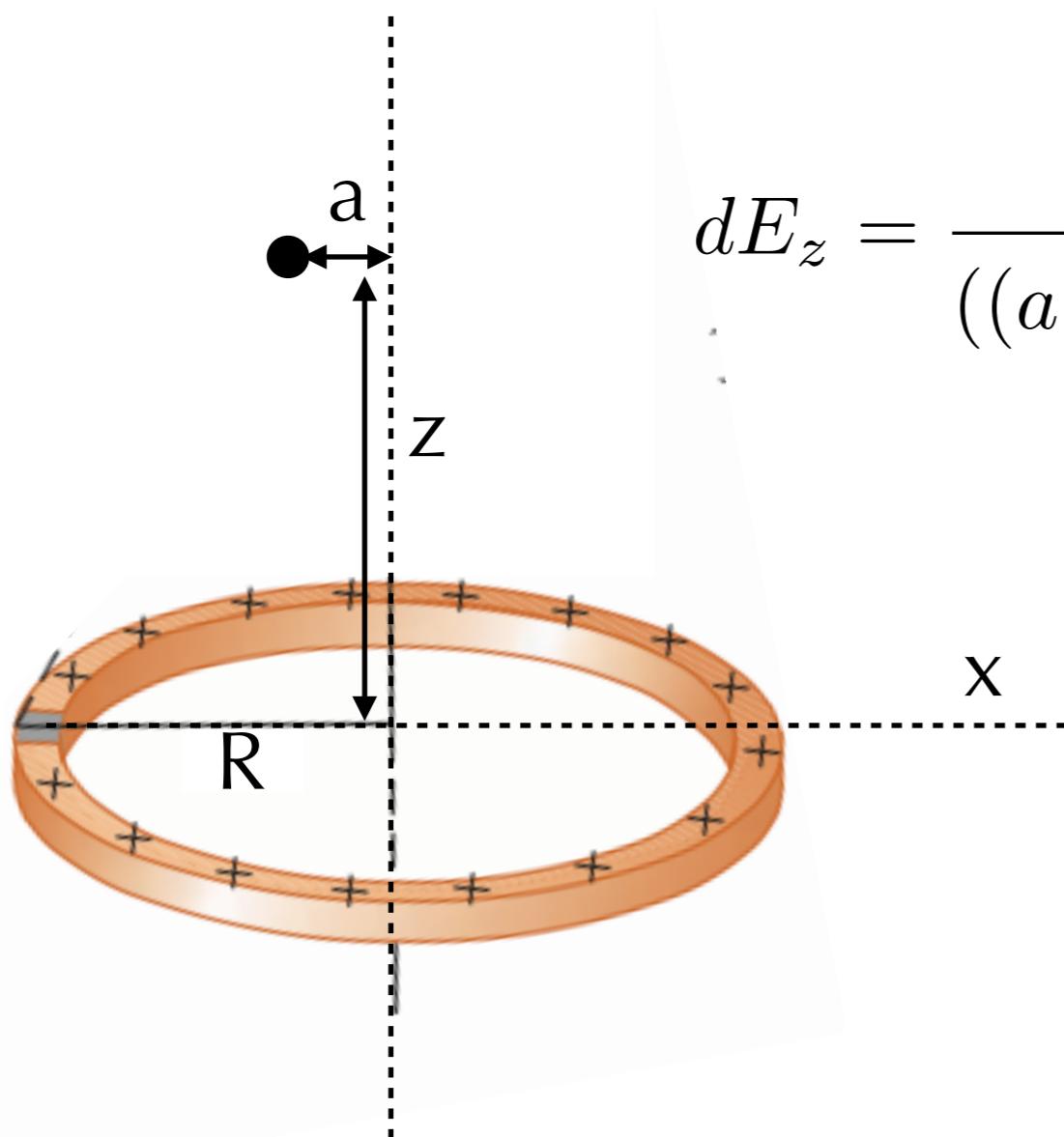
Back to the ring of charge

Let's step off the symmetry axis in one dimension. Which components of the electric field will be nonzero.



Back to the ring of charge

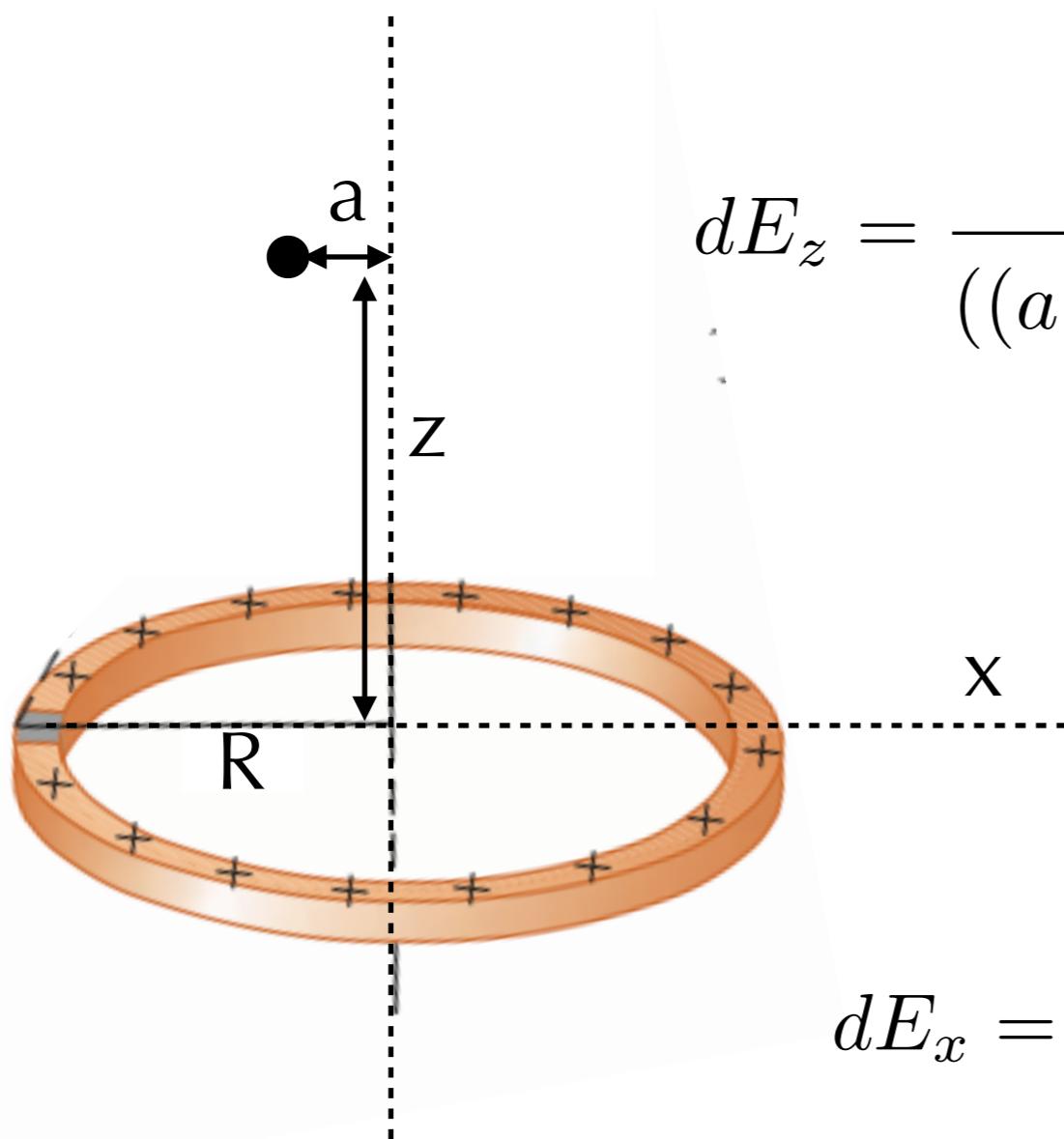
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$$dE_z = \frac{k\lambda R z d\theta}{((a + R \cos \theta)^2 + (R \sin \theta)^2 + z^2)^{3/2}}$$

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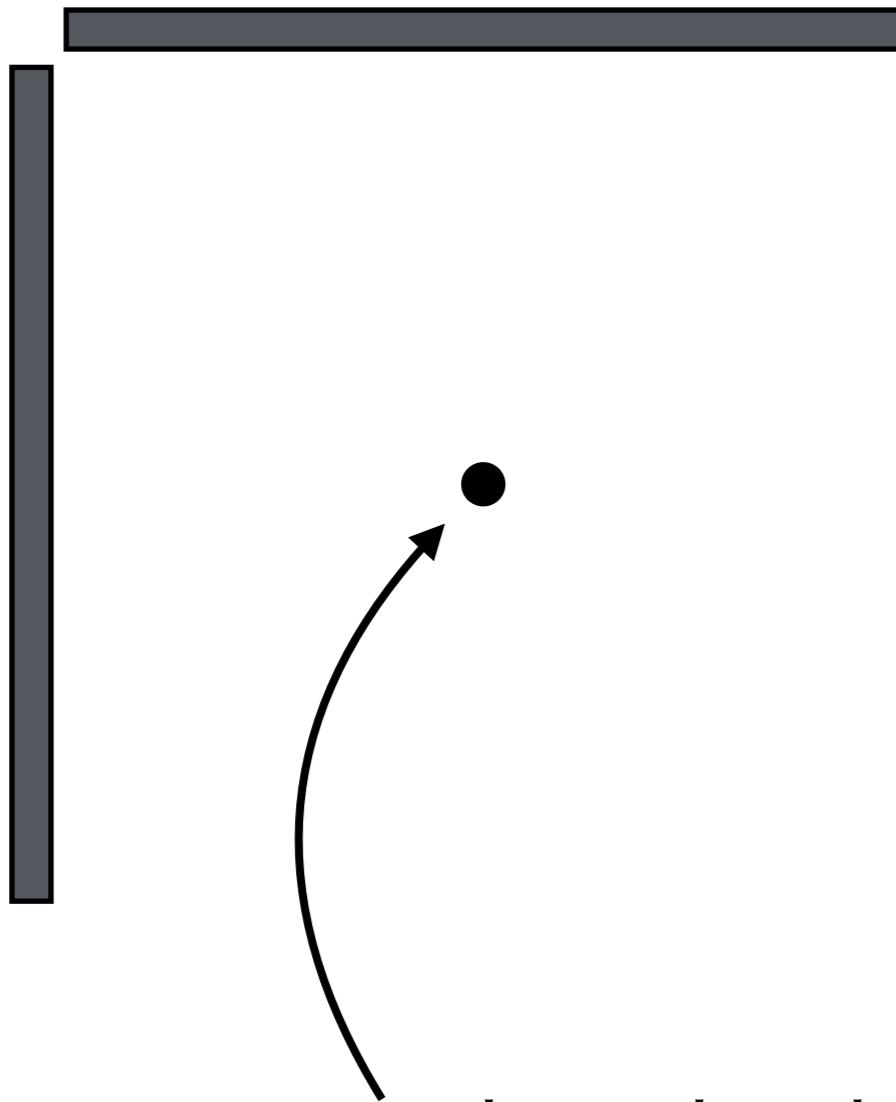


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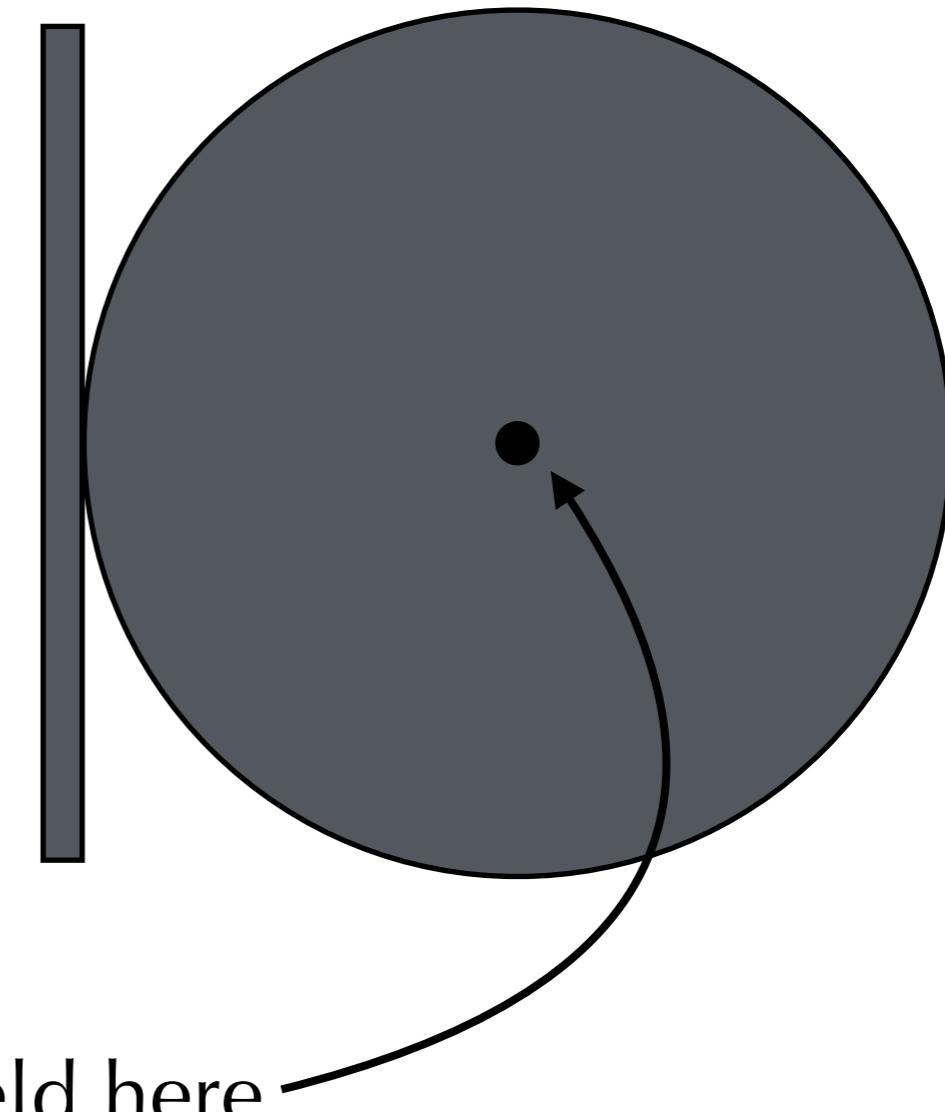
$$dE_x = \frac{k\lambda R (a + R \cos \theta) d\theta}{((a + R \cos \theta)^2 + (R \sin \theta)^2 + z^2)^{3/2}}$$

How would you approach this problem?

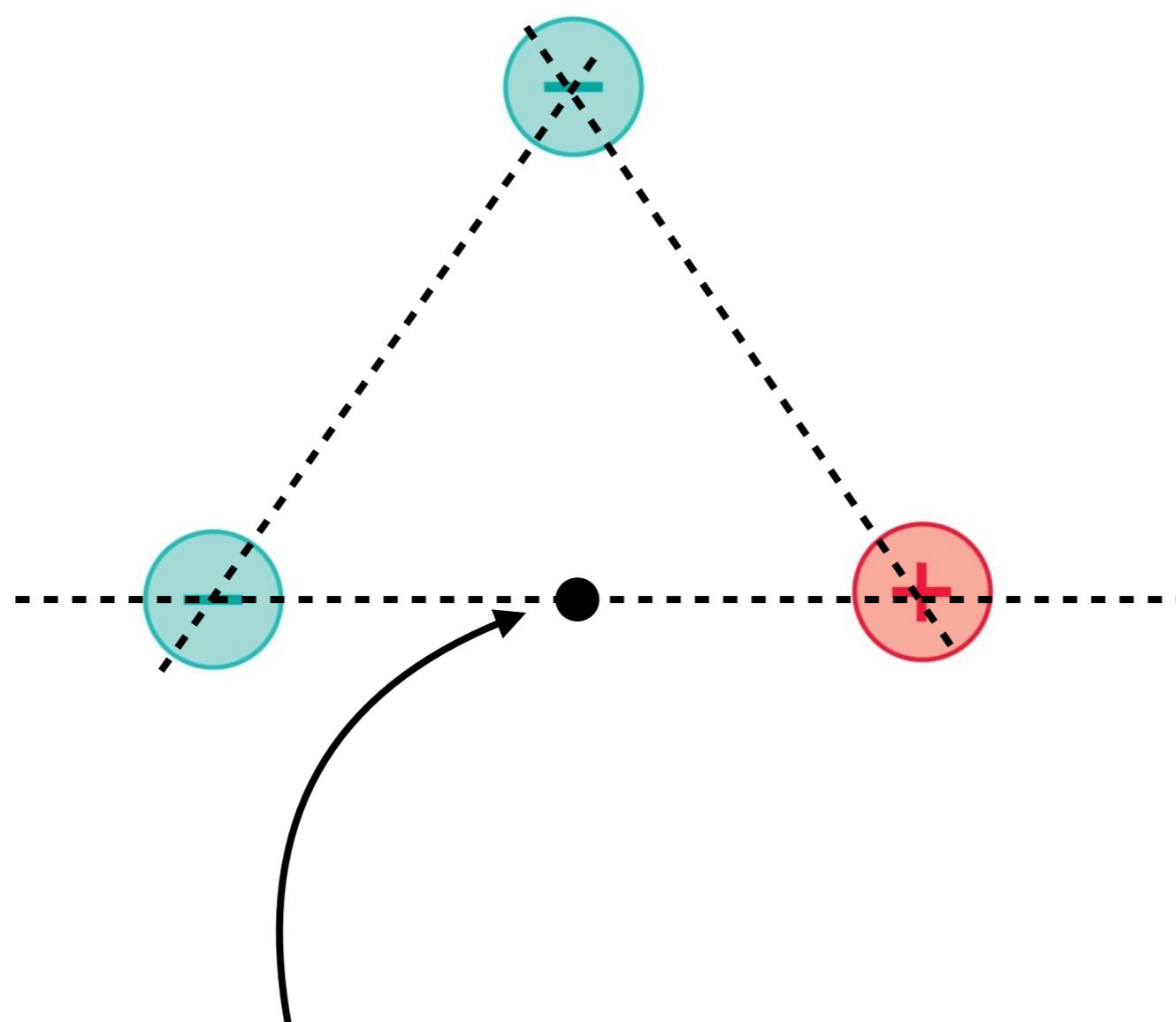
Top View



Side View

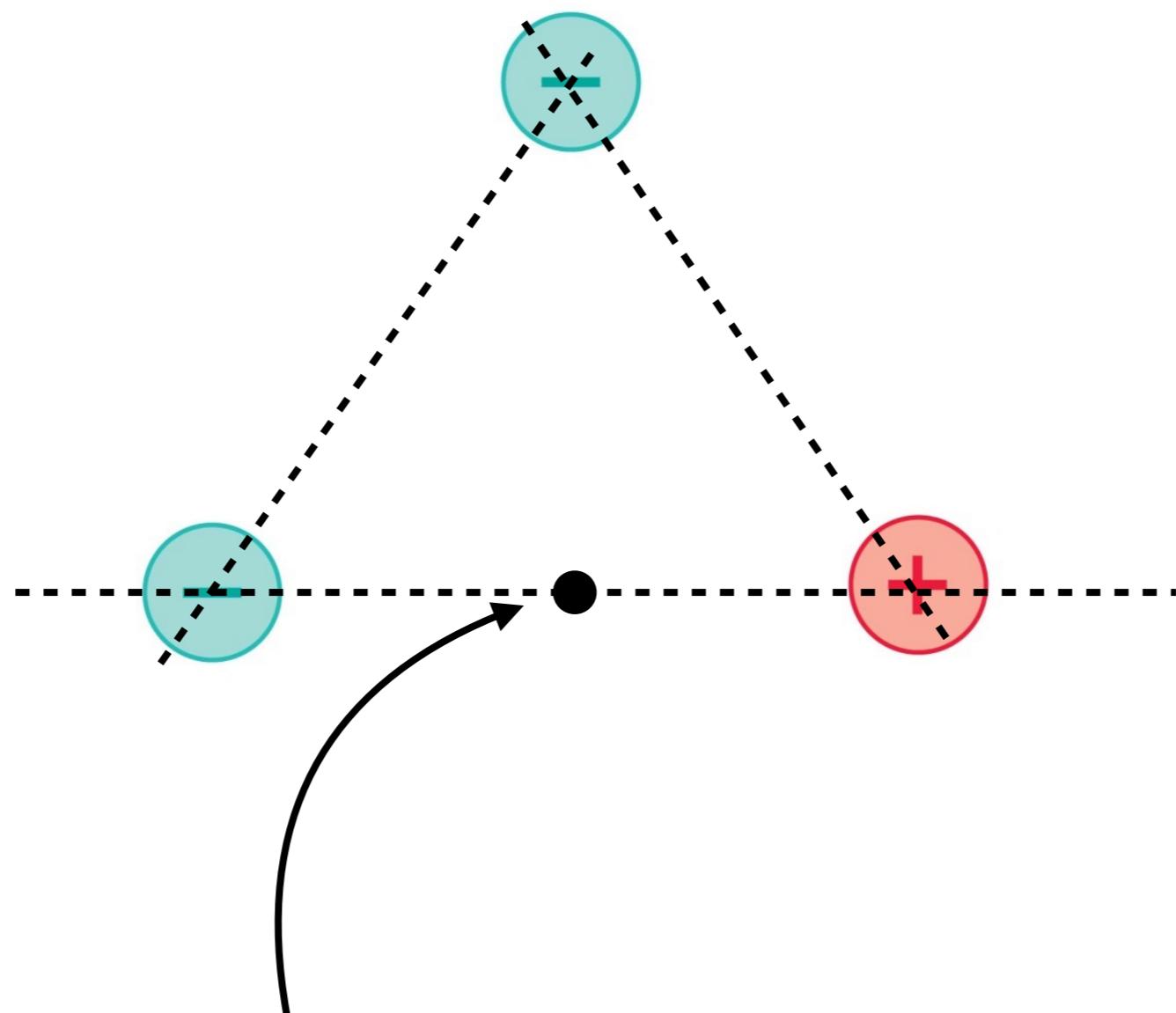


What's the electric field here



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$$E_z = \frac{k|Q|}{r\sqrt{r^2 + (L/2)^2}}$$

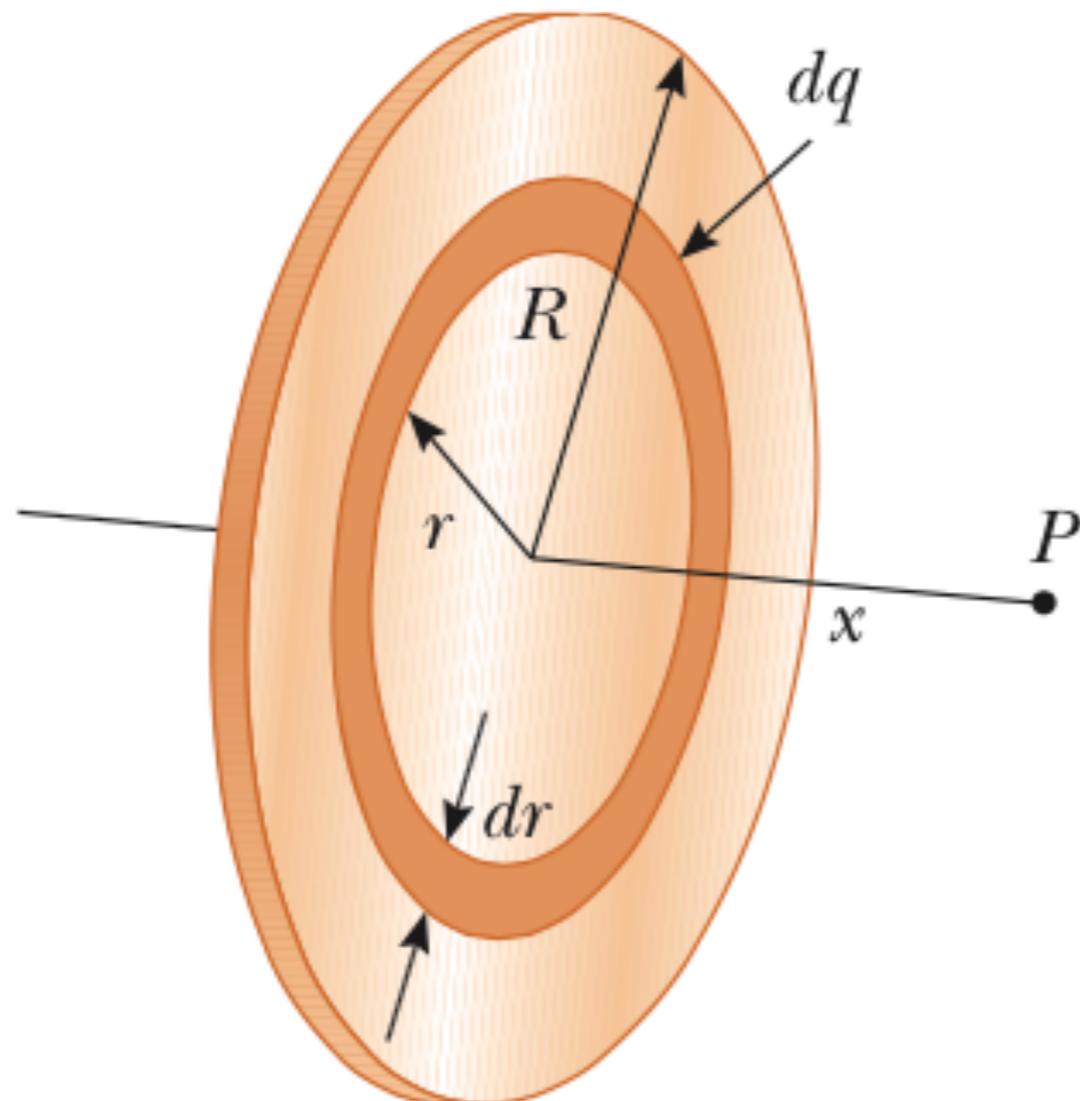


What's the electric field here?

A plane of charge

What does the disk become if we let:

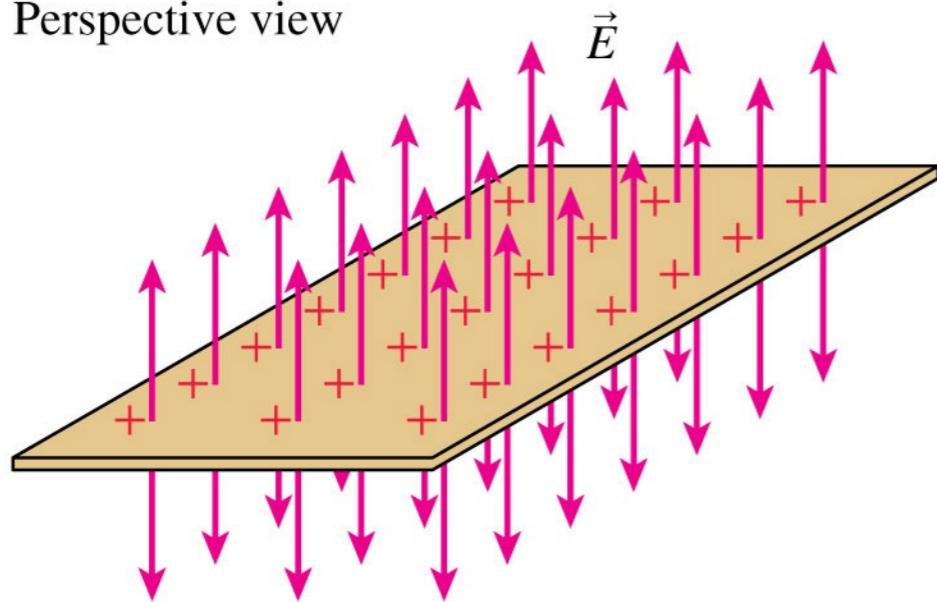
$$R \rightarrow \infty$$



A plane of charge

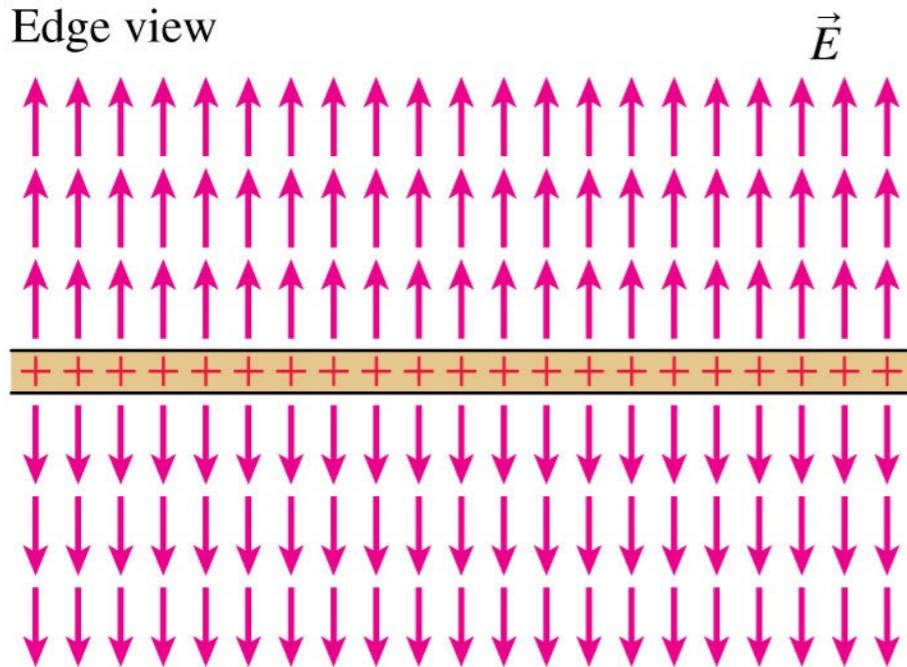
What does the disk become if we let:

Perspective view



$$R \rightarrow \infty$$

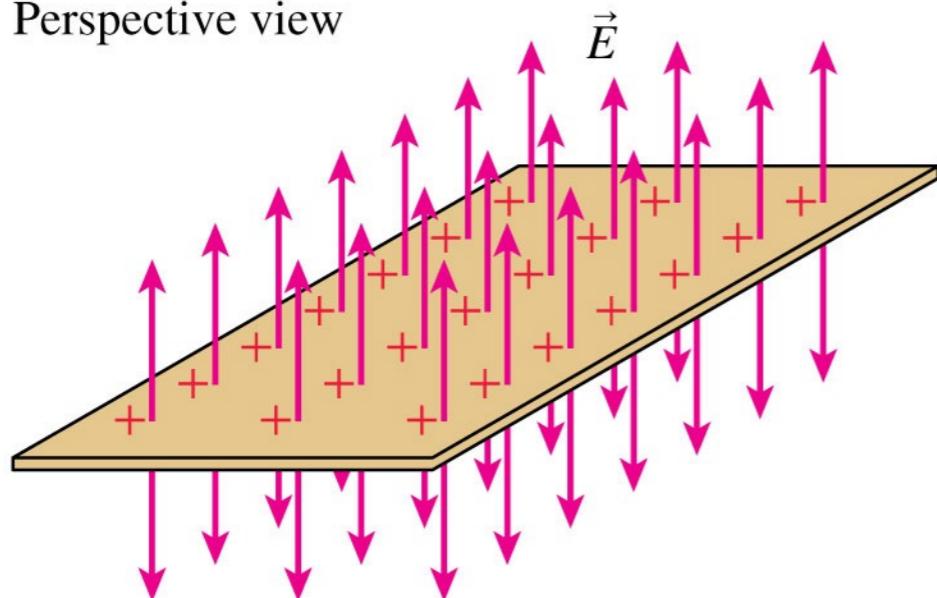
Edge view



A plane of charge

What does the disk become if we let:

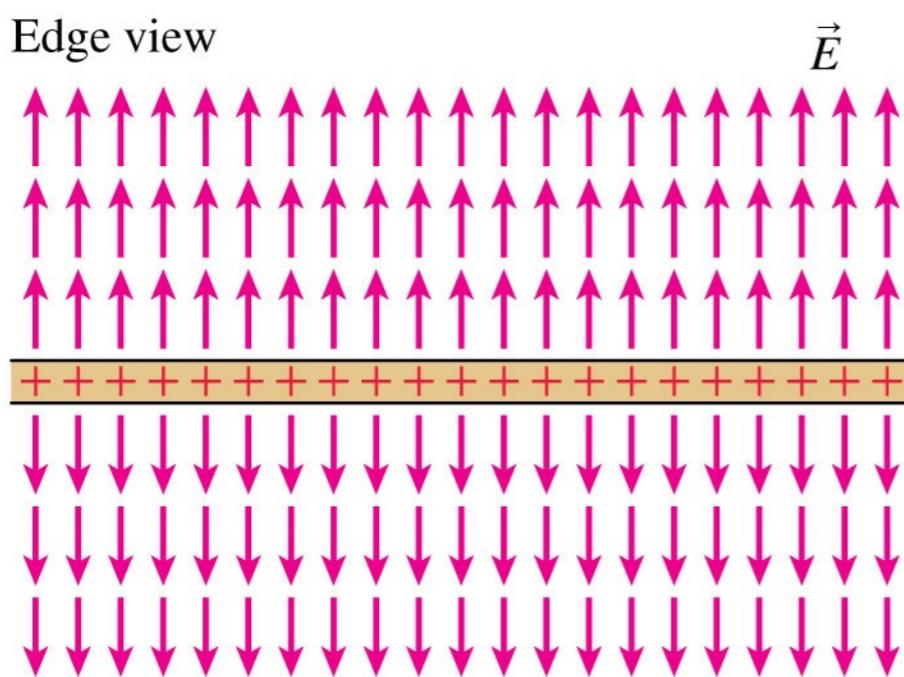
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$$R \rightarrow \infty$$

$$E_x = \frac{\eta}{2\epsilon_0} \left[1 - \frac{x}{\sqrt{x^2 + R^2}} \right]$$

Edge view

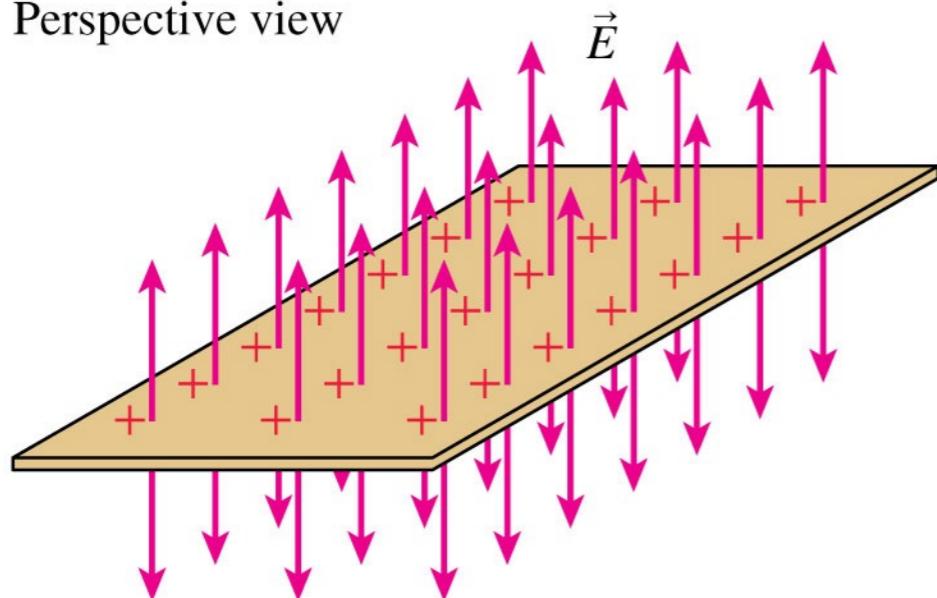


What does this function become?

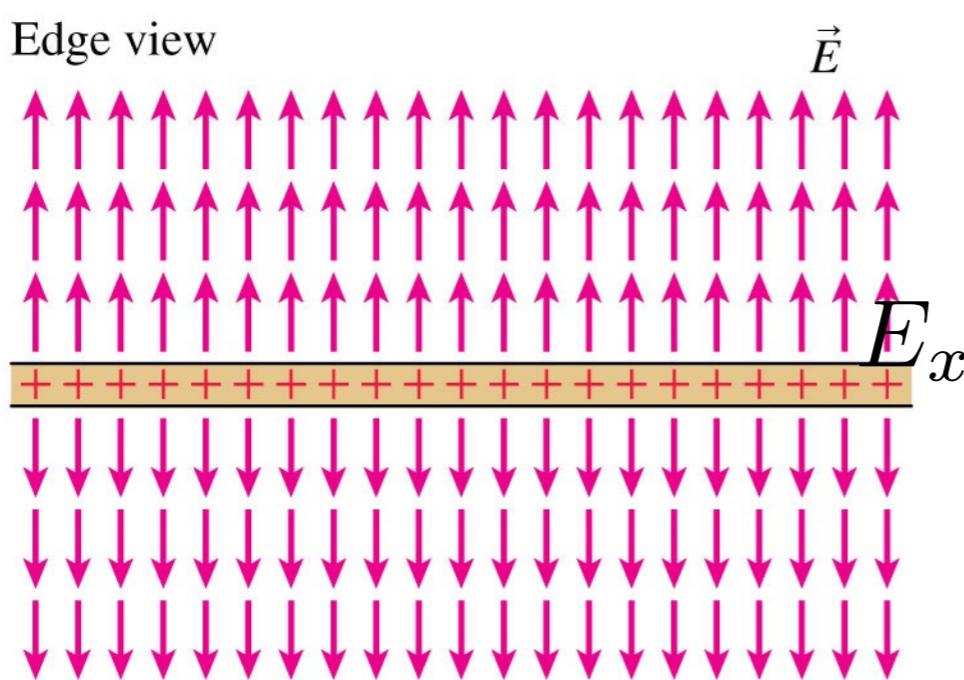
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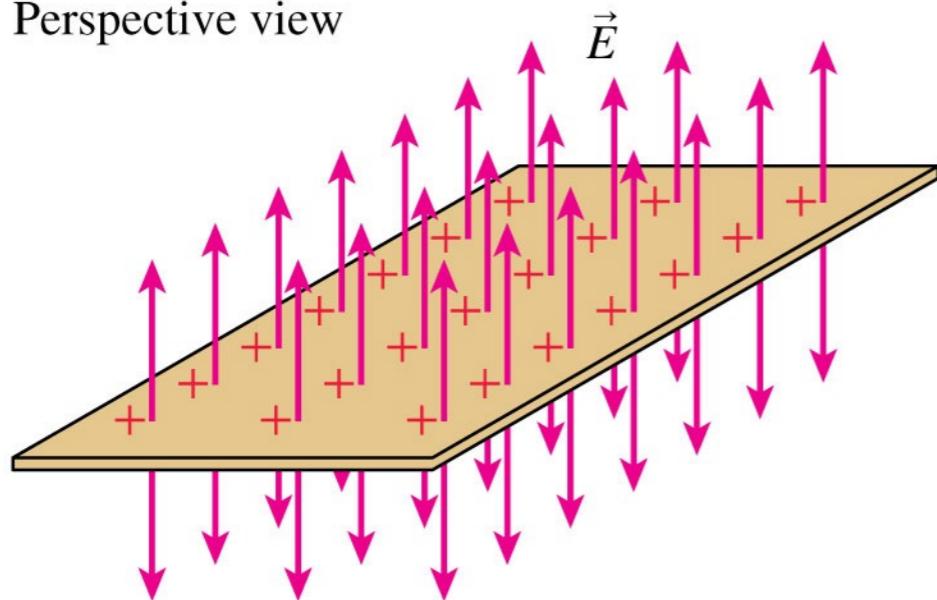
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$$E_x = \frac{\eta}{2\epsilon_0} \left[1 - \frac{x}{\sqrt{R^2 \left(\frac{x^2}{R^2} + 1 \right)}} \right]$$

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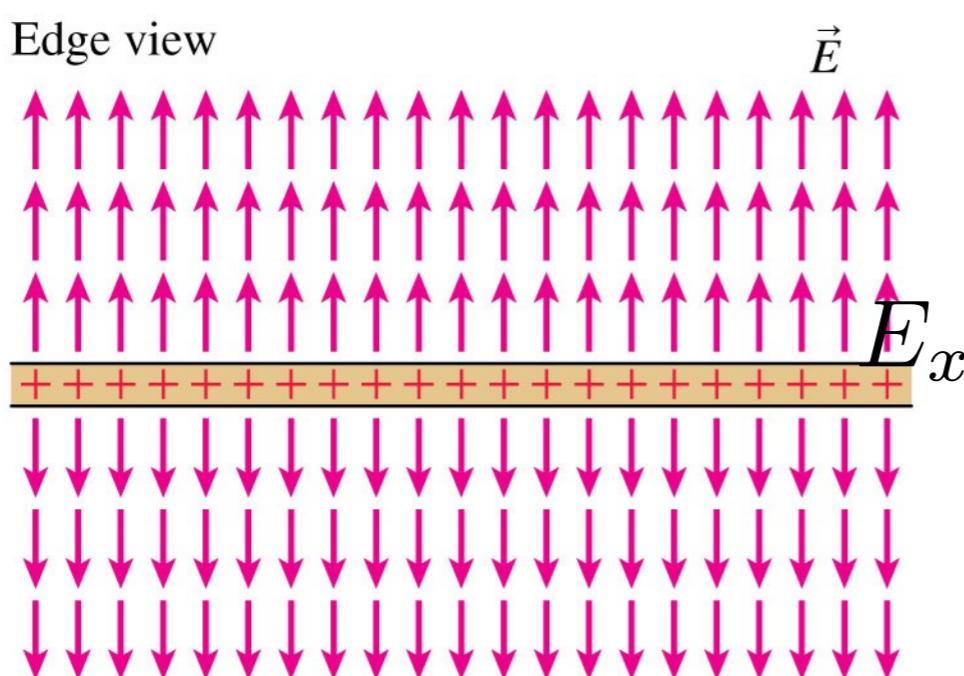
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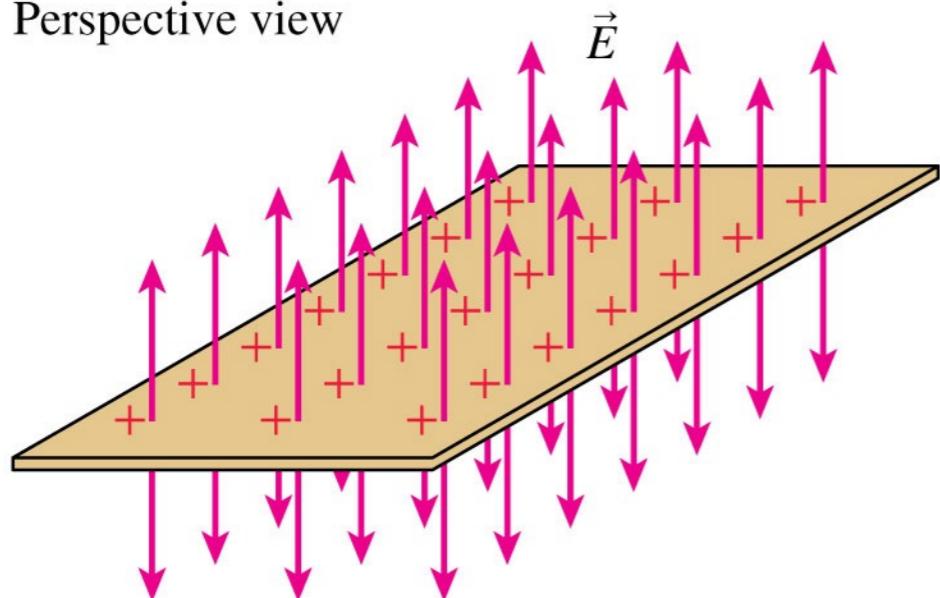
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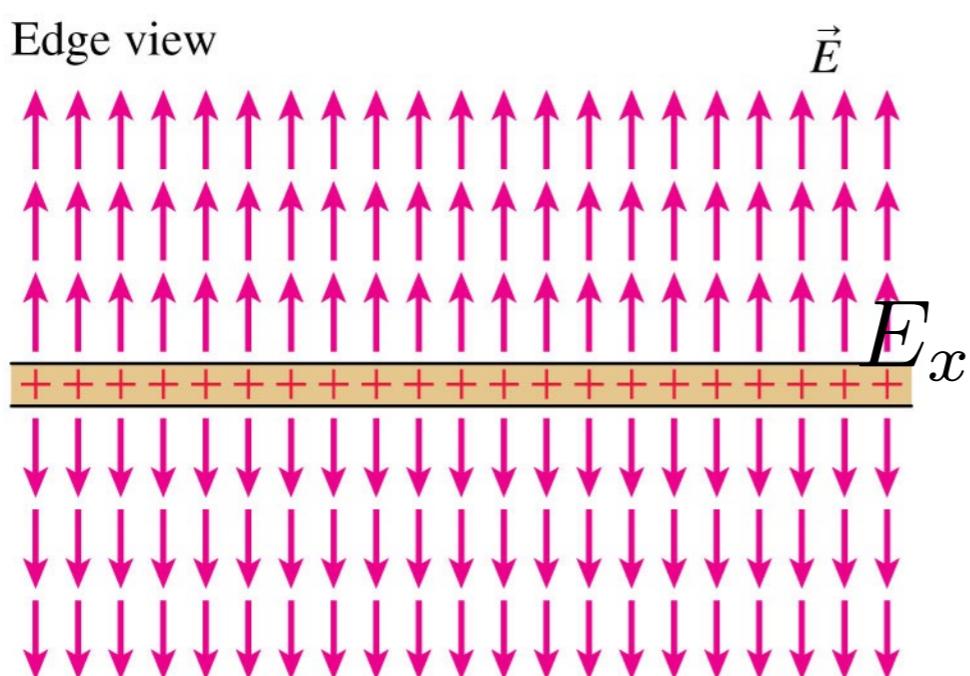
Perspective view



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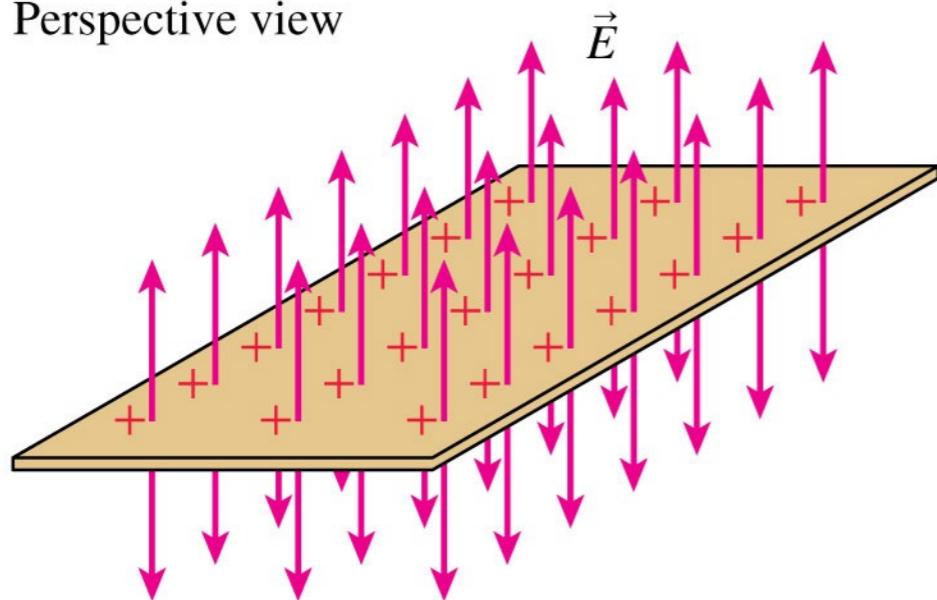
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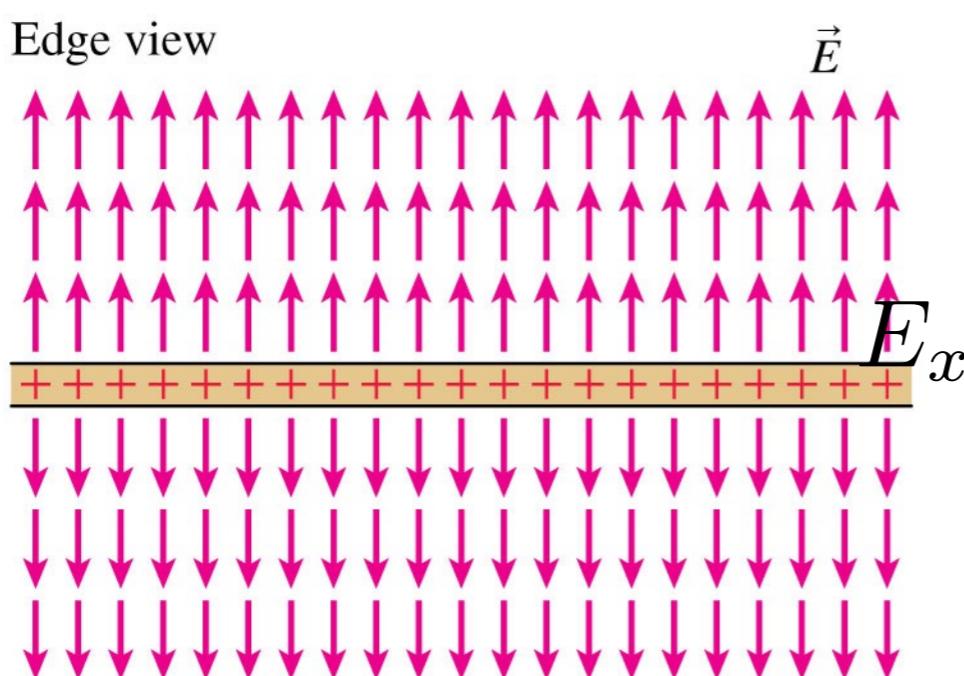
Perspective view



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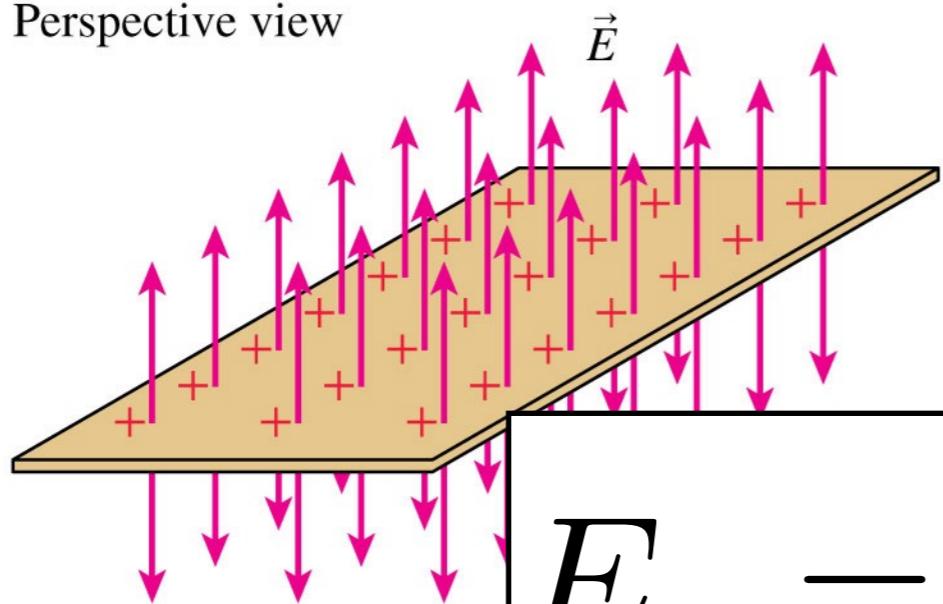
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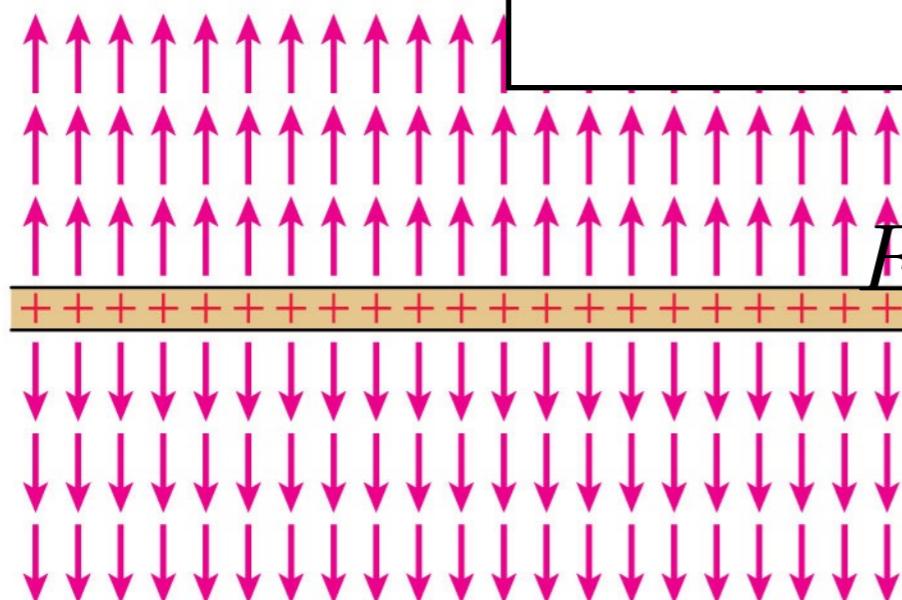
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Perspective view



Edge view



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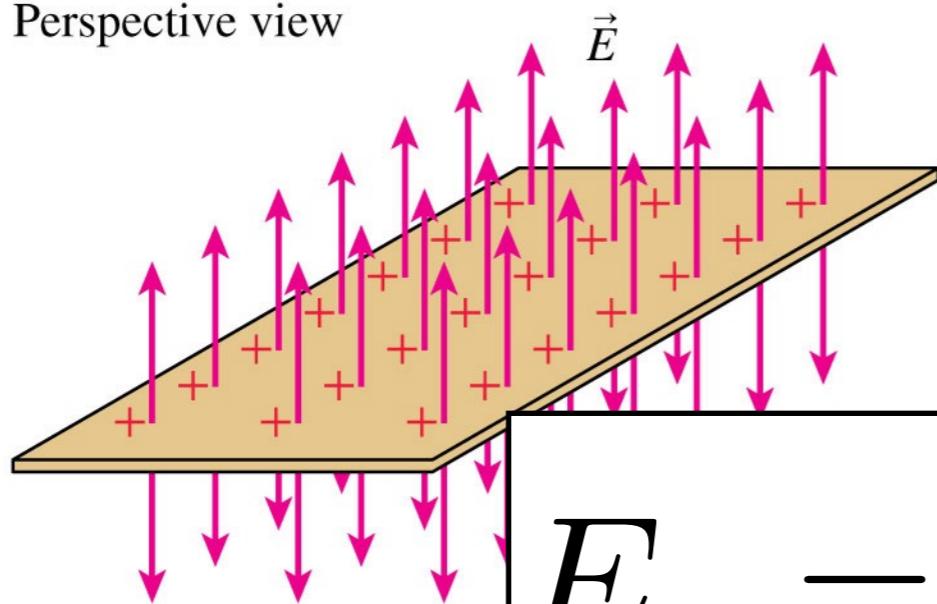
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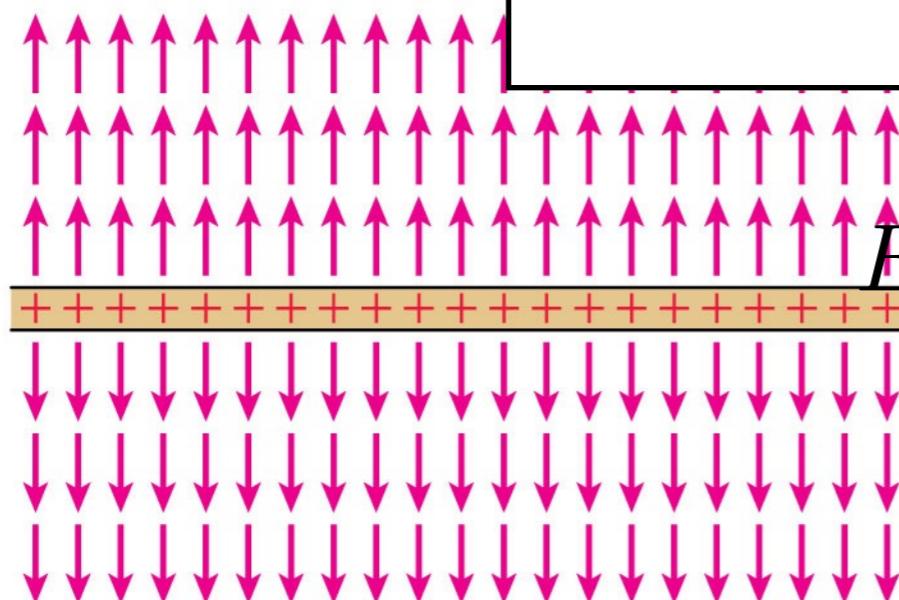
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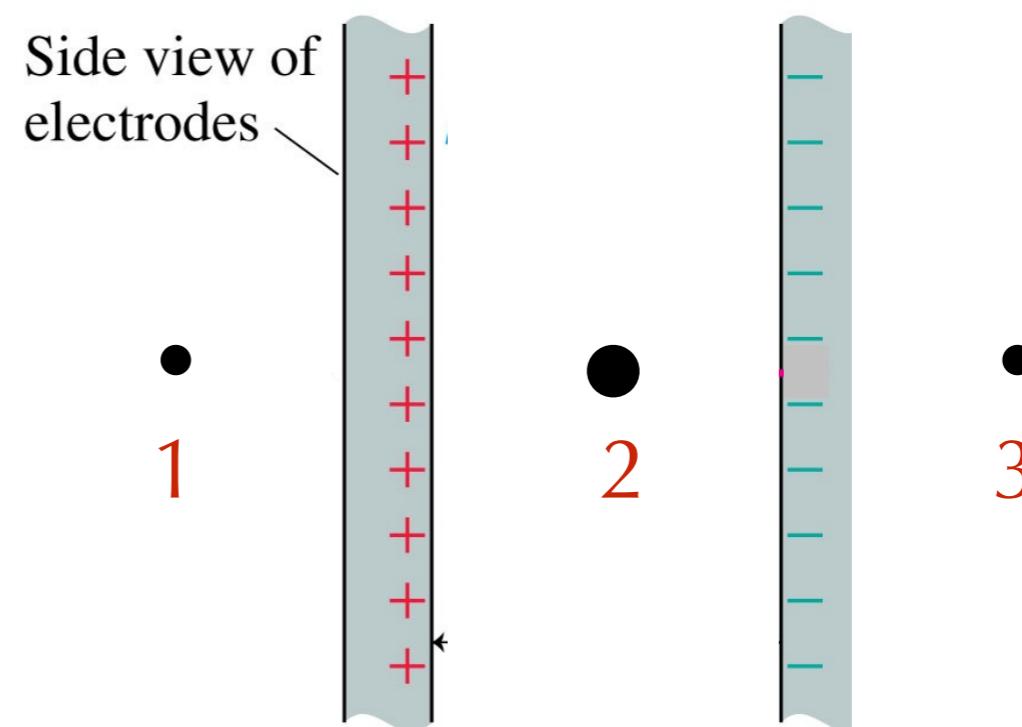
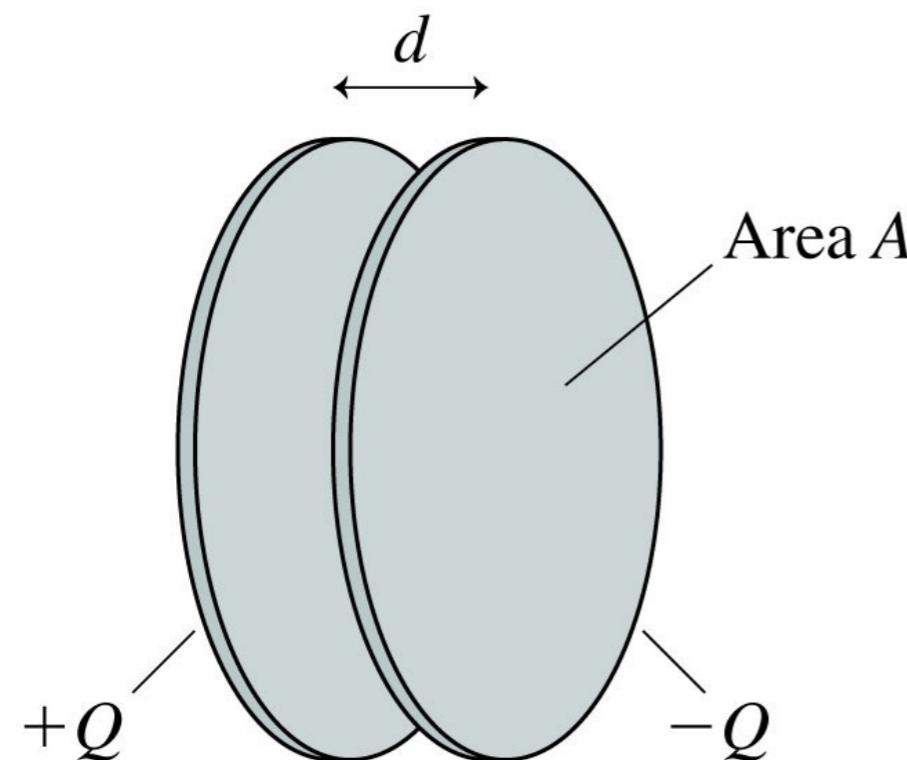
binomial expansion

$$E_x = \frac{\eta}{2\epsilon_0} \left[1 - \frac{x}{R} \right]$$

$$(1 + x)^n \approx 1 + nx \quad (\text{if } x \ll 1)$$

Parallel Plate Capacitor

What is the direction and magnitude of the electric field at these points?



Point 1: A $E = \frac{\eta}{\epsilon_0}$ to the right.

B $E = \frac{\eta}{\epsilon_0}$ to the left.

C $E = \frac{\eta}{2\epsilon_0}$ to the right.

D $E = \frac{\eta}{2\epsilon_0}$ to the left.

E $E = 0$

Point 2: A $E = \frac{\eta}{\epsilon_0}$ to the right.

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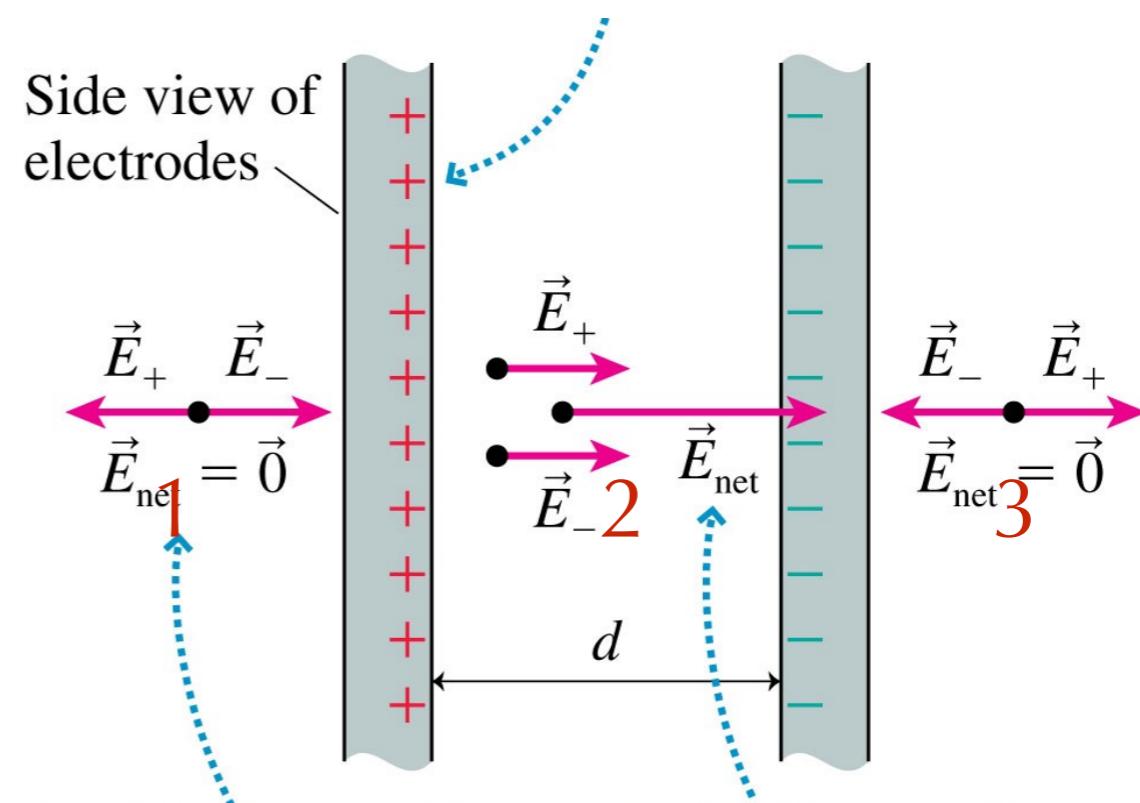
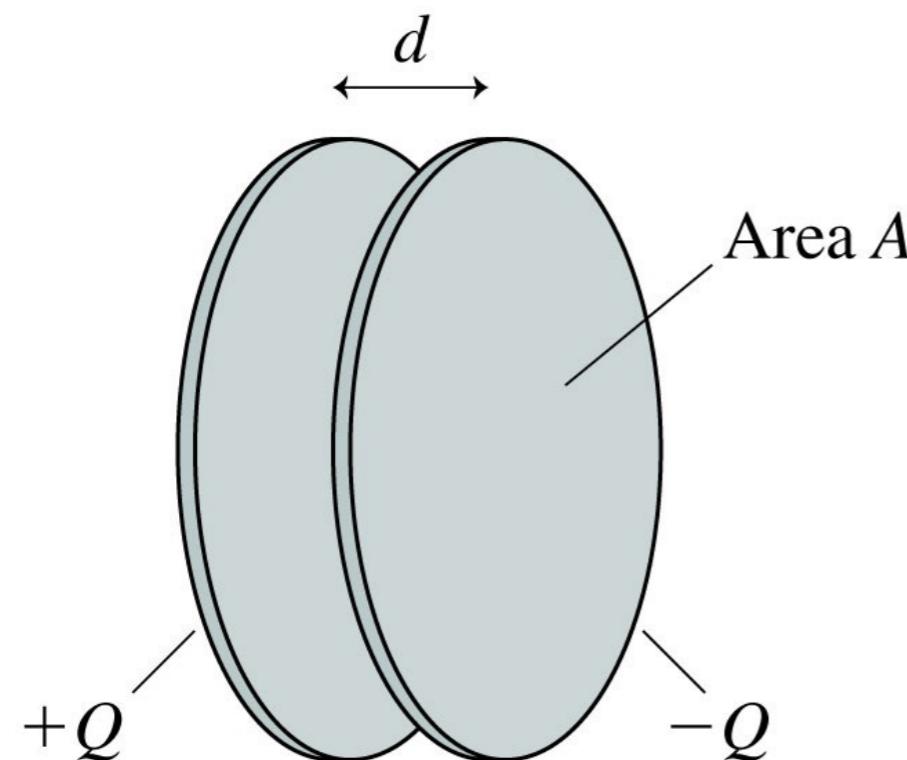
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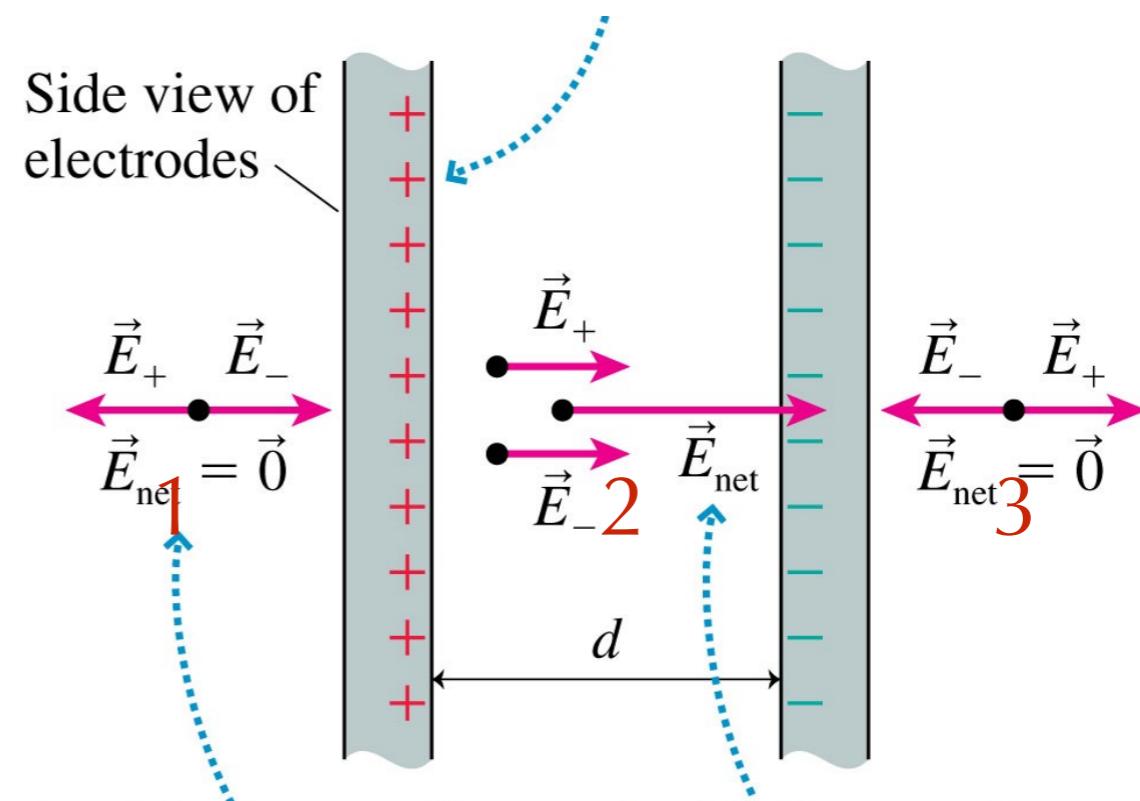
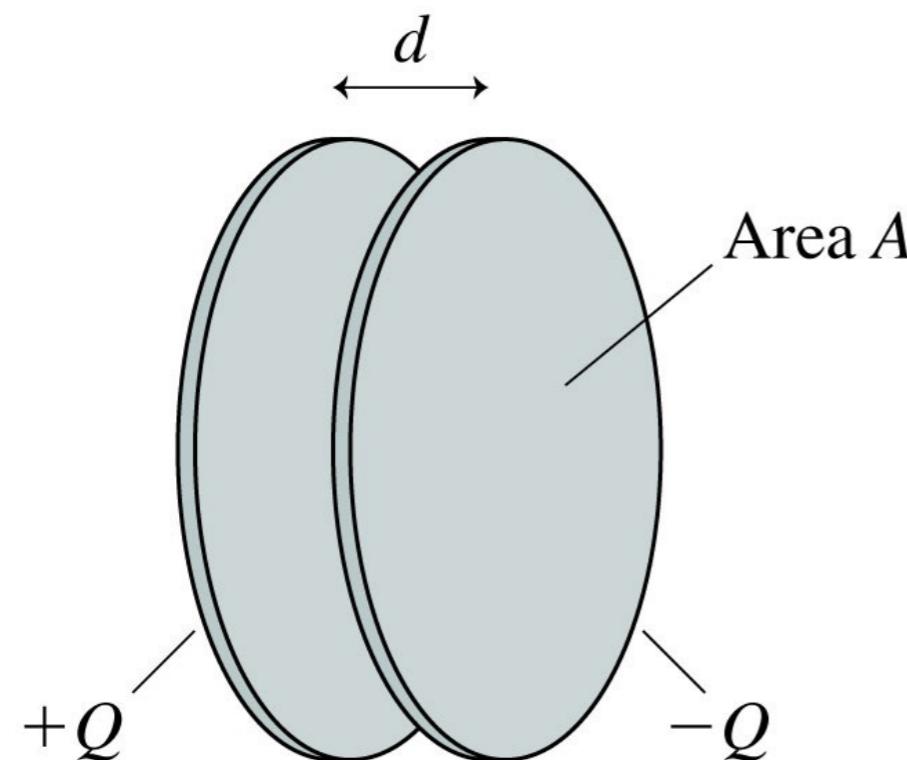
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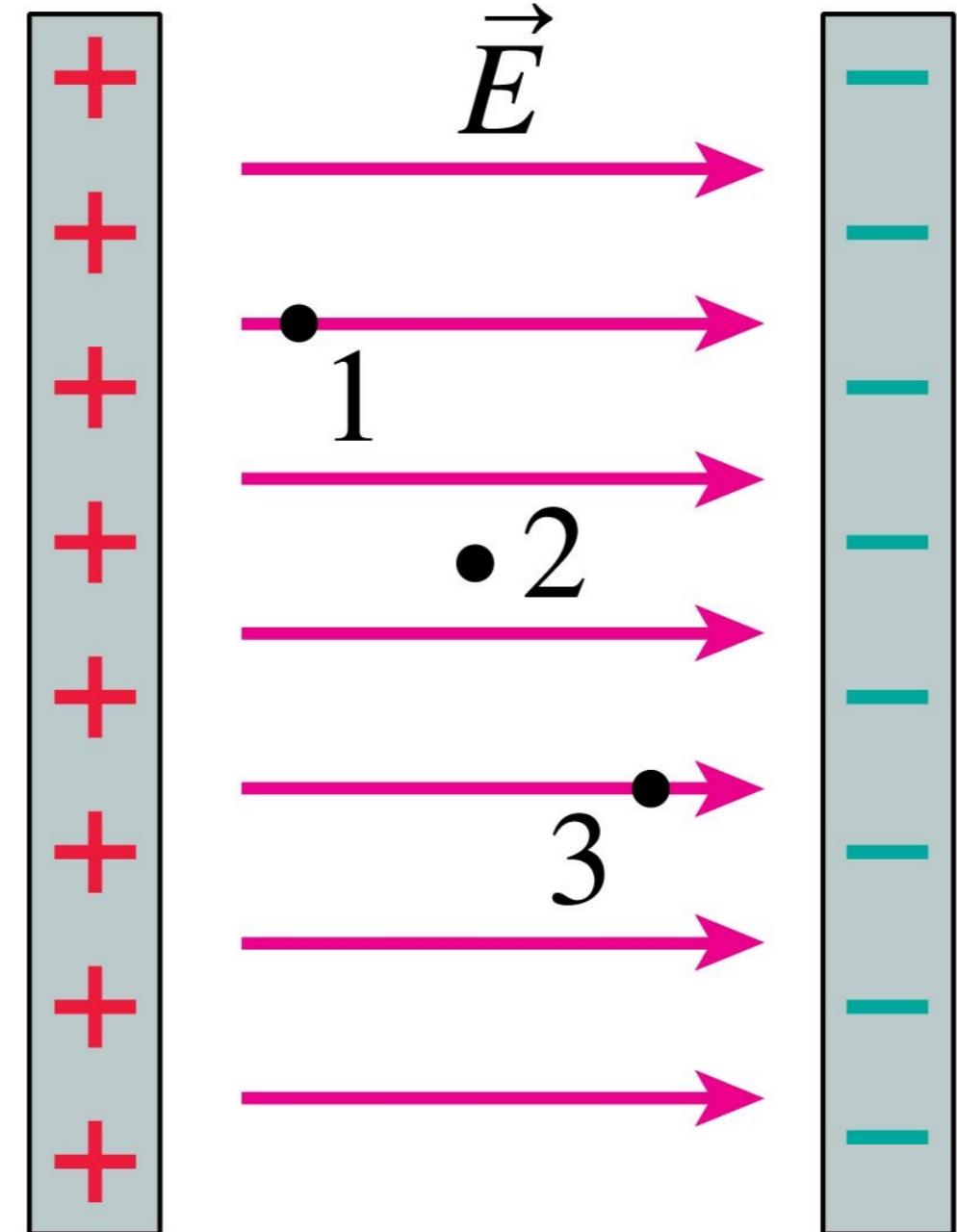
D $E = \frac{\eta}{2\epsilon_0}$ to the left.

E $E = 0$

Quiz

Three points inside a parallel-plate capacitor are marked. Which is true?

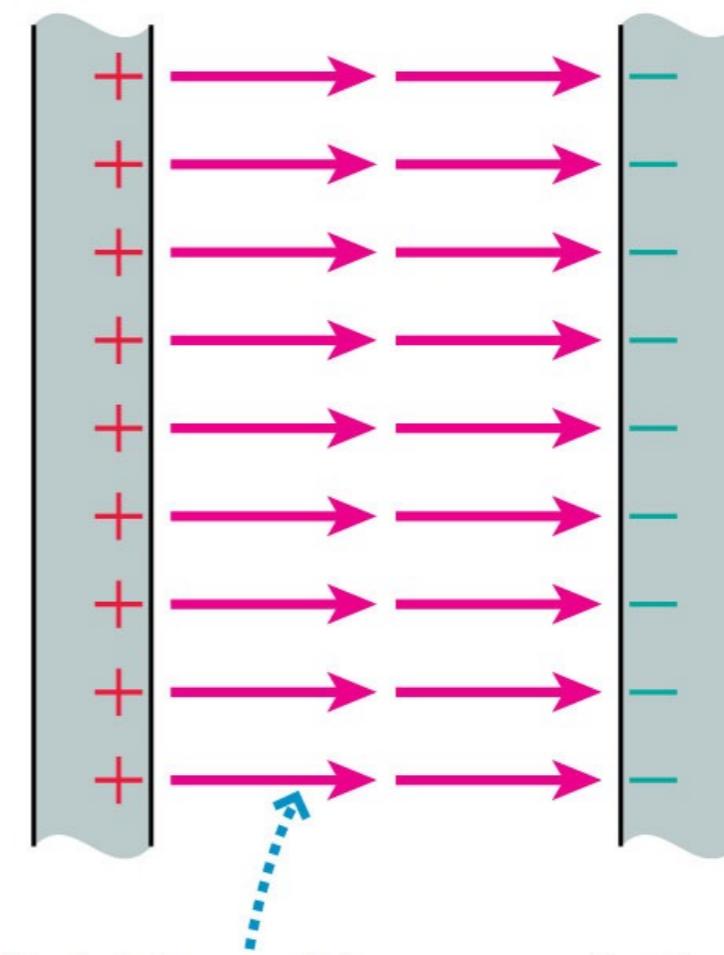
- A. $E_1 > E_2 > E_3$
- B. $E_1 < E_2 < E_3$
- C. $E_1 = E_3 > E_2$
- D. $E_1 = E_2 = E_3$



uniform field

Ideal capacitor

If d is much smaller than electrode size.

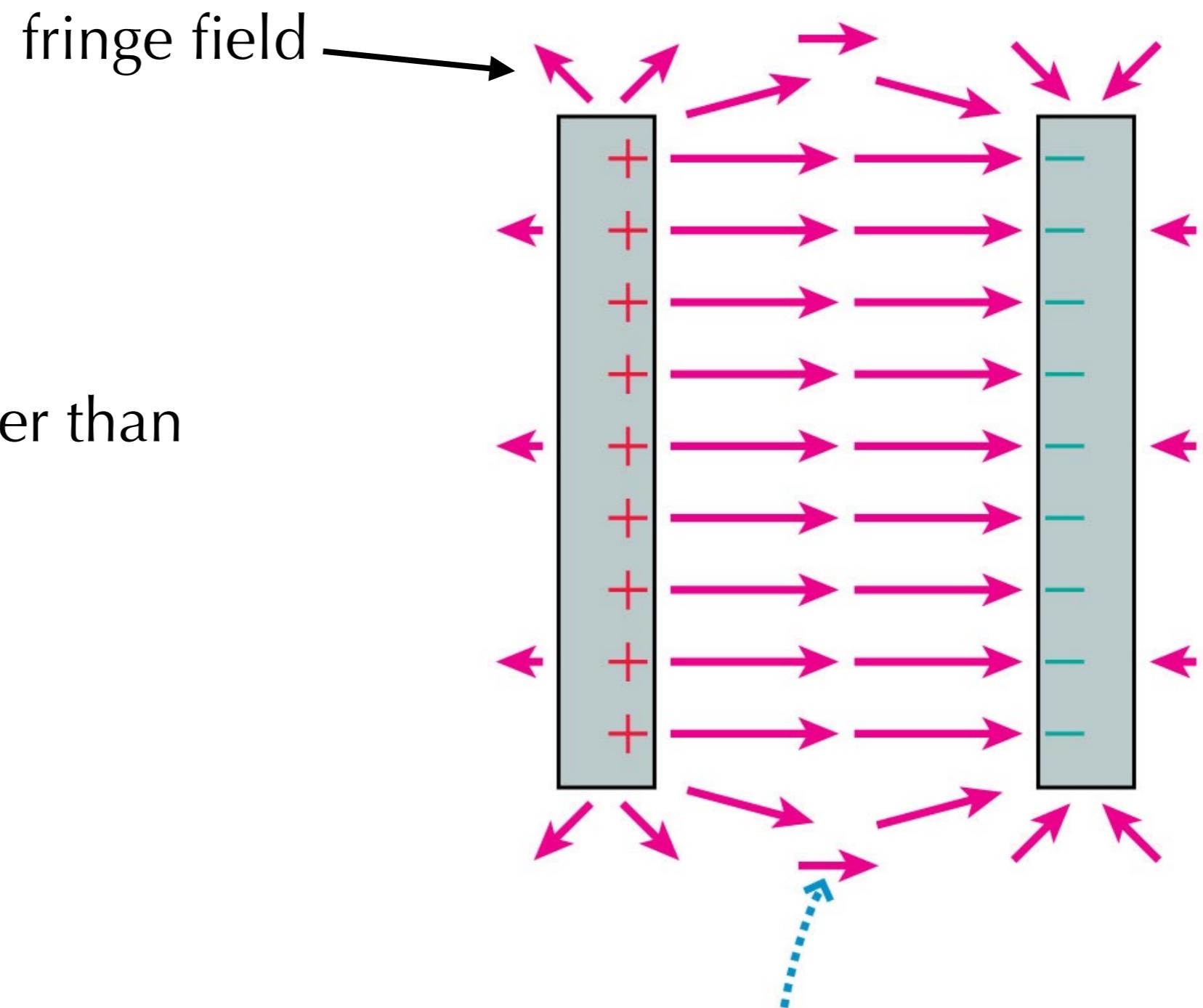


This is
an edge
view of the
electrodes.

The field is uniform, pointing from the positive to the negative electrode.

Ideal capacitor

If d is much smaller than electrode size.

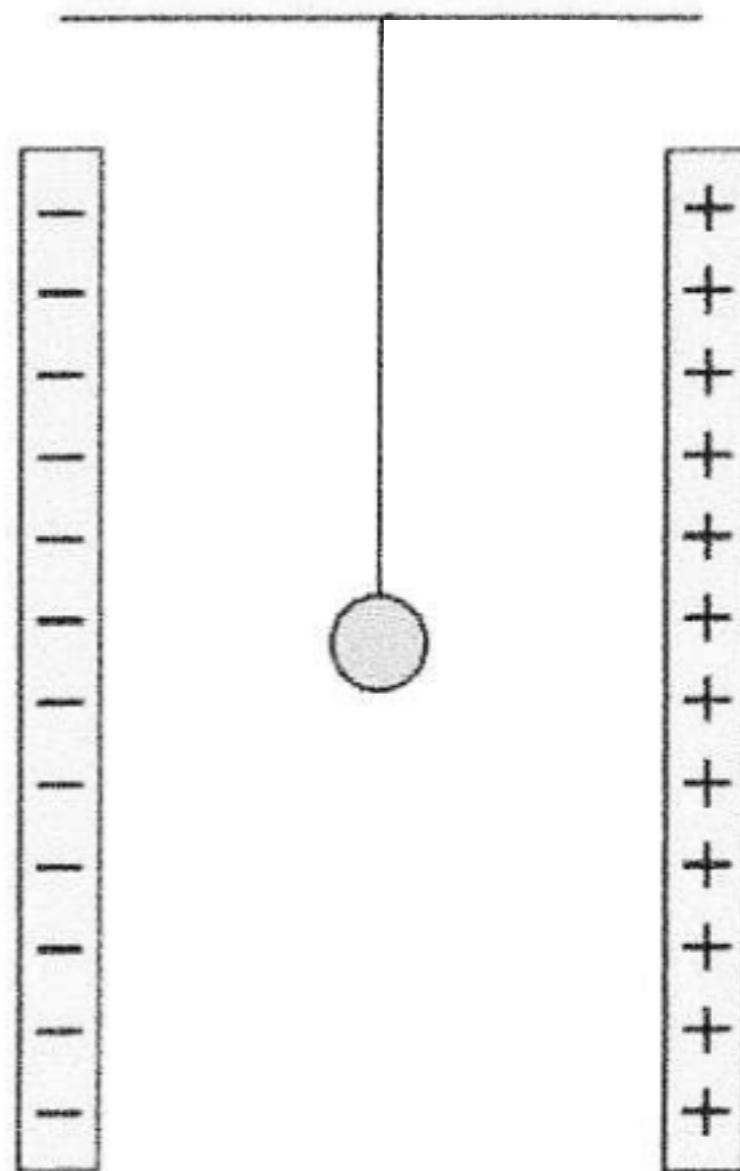


A weak fringe field extends outside the electrodes.

Quiz

If I place a negative charge on this ball, what will happen?

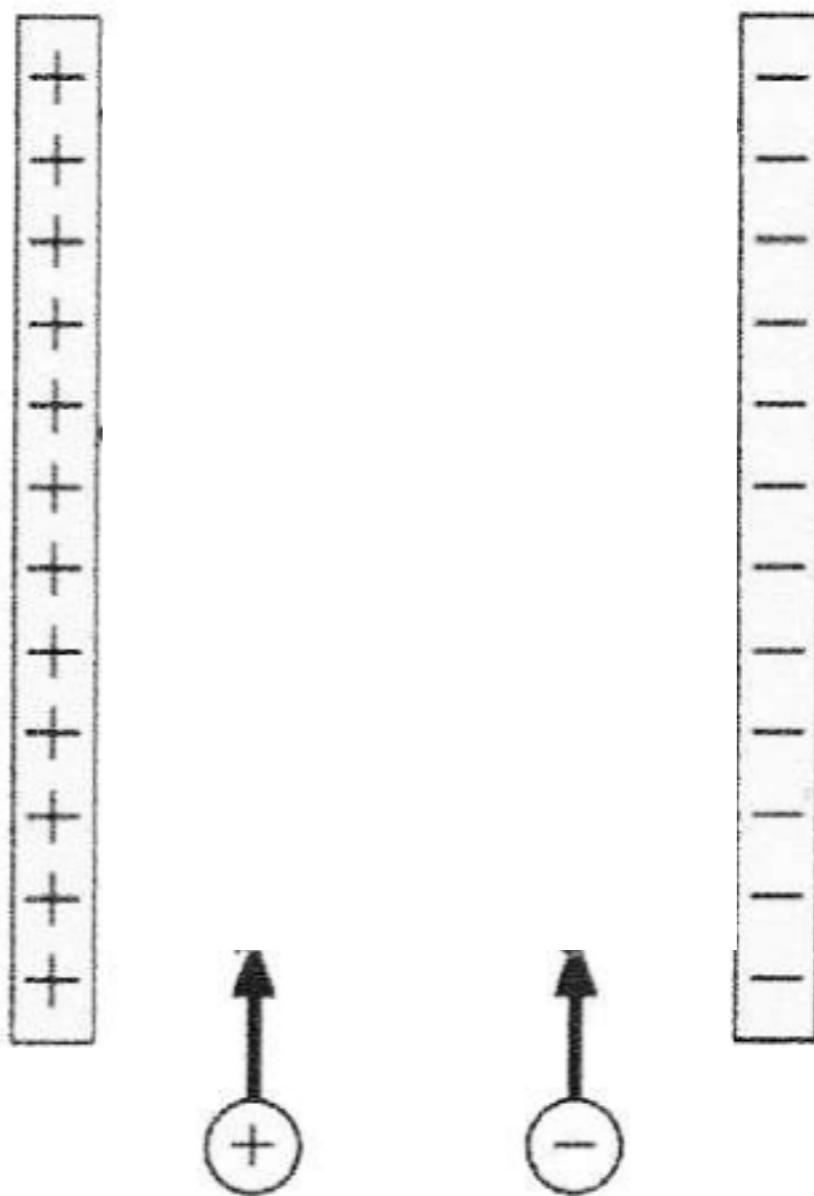
- a) stays where its at.
- b) swings to the left
- c) swings to the right.



Quiz

What will the trajectories of the particles look like?

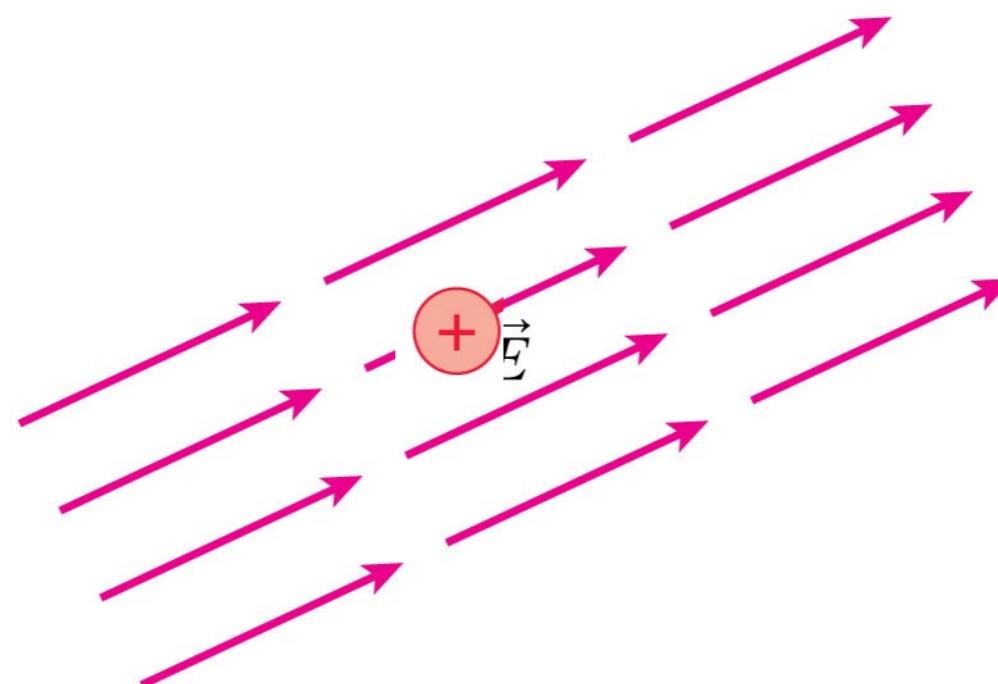
- a) proton curves left, electron curves right.
- b) proton moves straight, electron curves left
- c) proton curves right, electron curves left.
- d) electron moves straight, proton curves right.



Motion of a charged particle in uniform field

Draw the force vector on the proton.

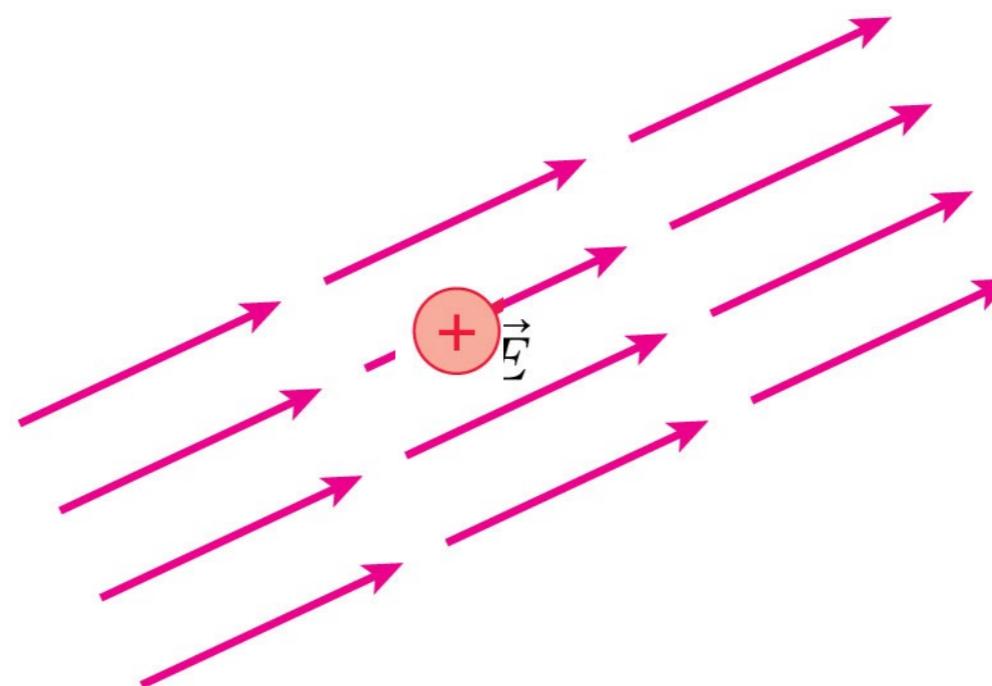
Write an expression for the acceleration of this proton



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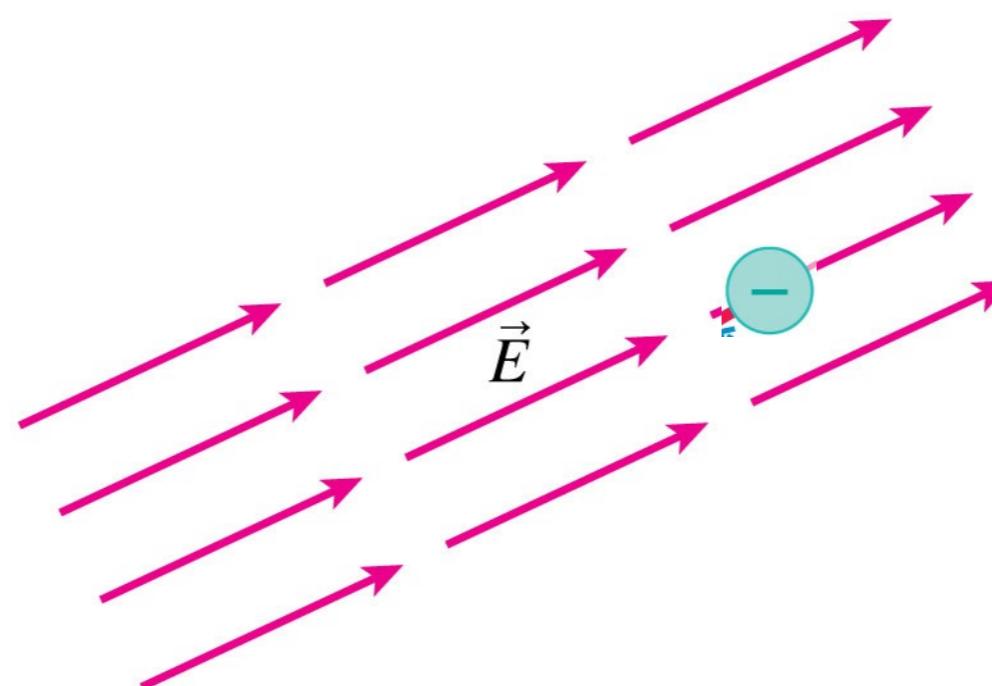


$$a = \frac{F}{m} = \frac{eE}{m}$$

Motion of a charged particle in uniform field

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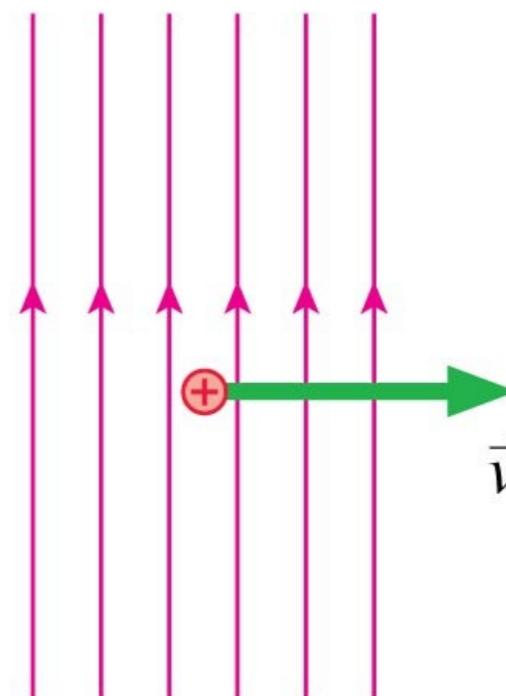


$$a = \frac{F}{m} = \frac{eE}{m}$$

Quiz

A proton is moving to the right in a vertical electric field. A very short time later, the proton's velocity is

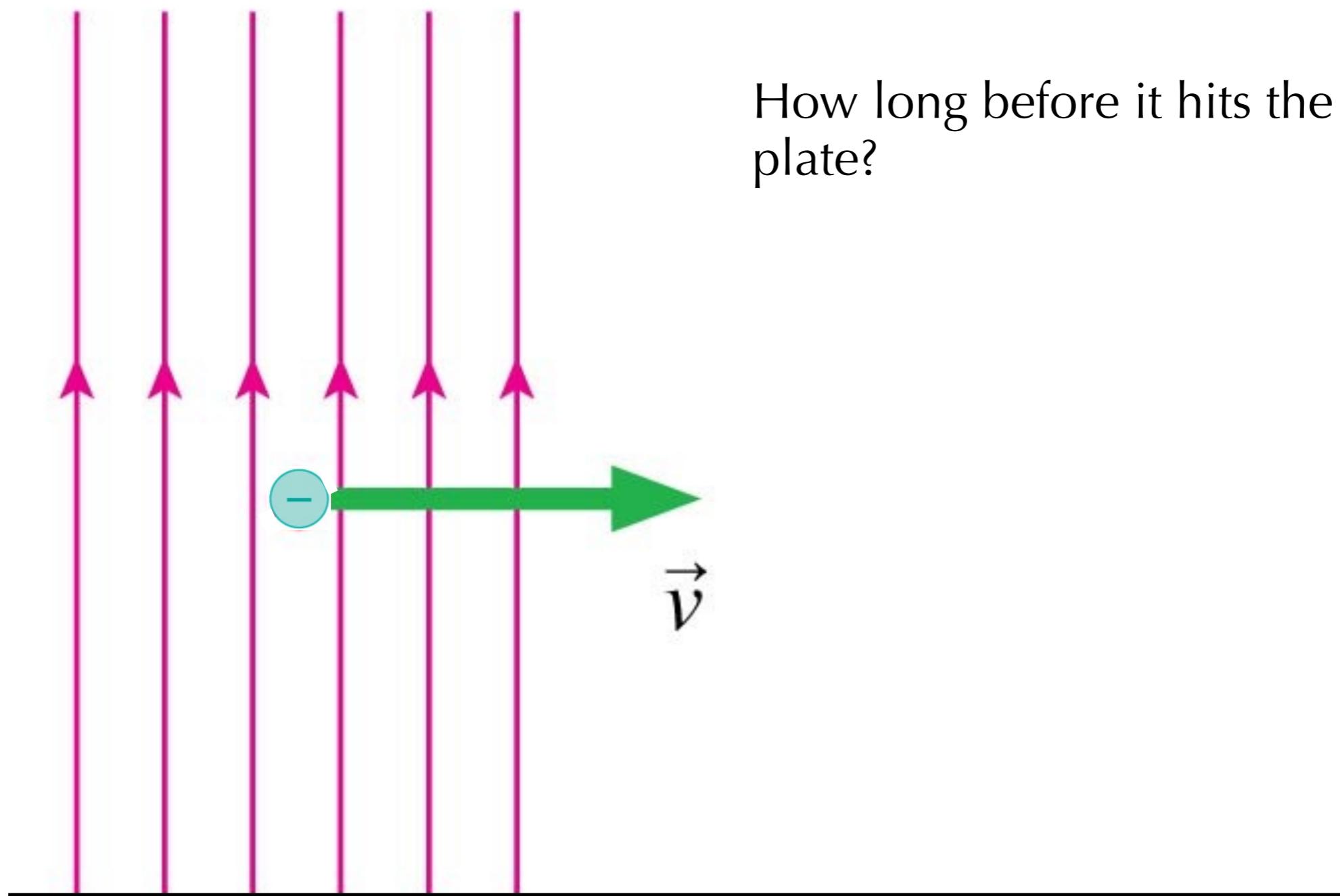
- A
- B
- C
- D
- E



Homework-Style Problem

If the electron is fired horizontally,
how far will it travel before hitting the
bottom plate.

How long before it hits the bottom
plate?

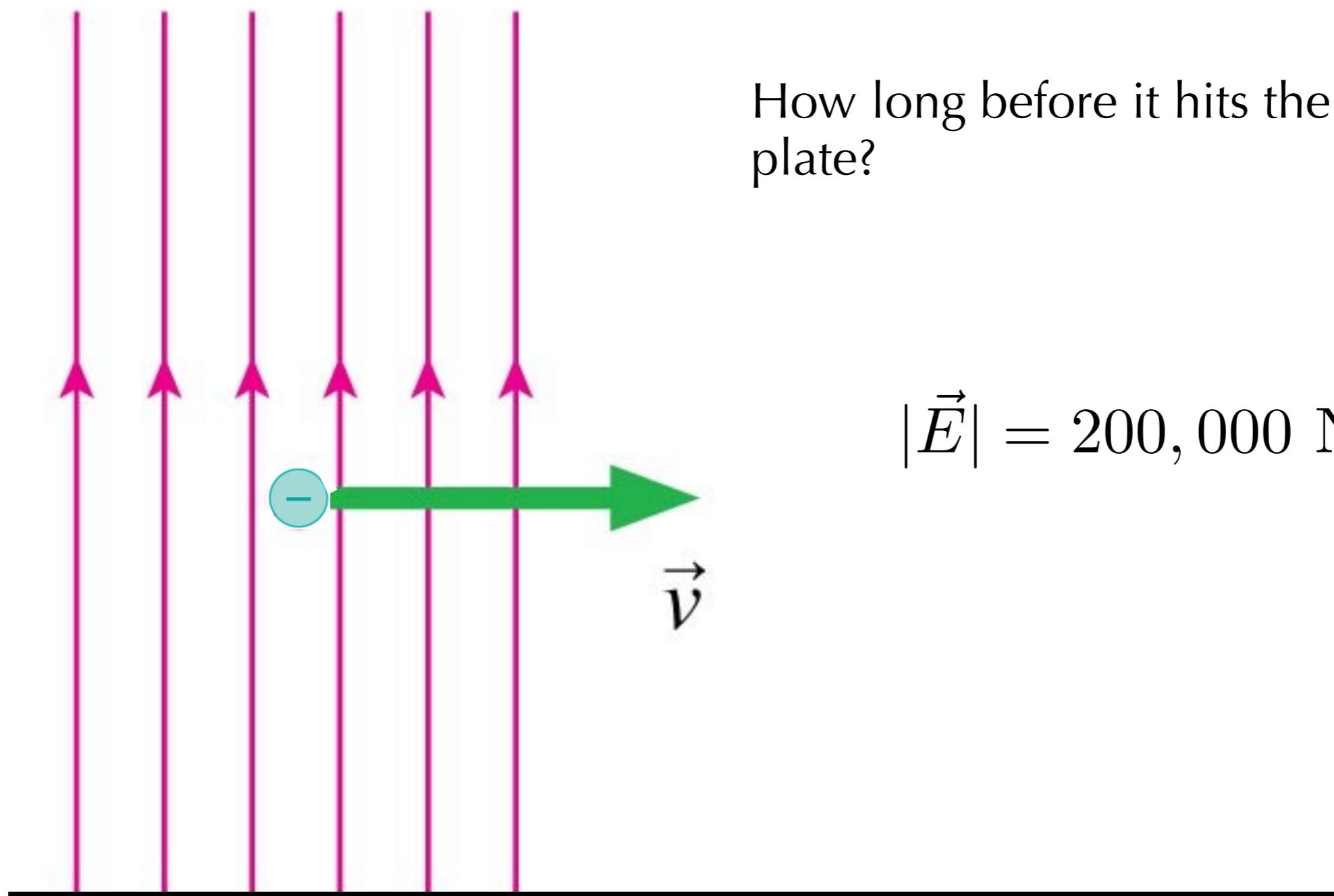


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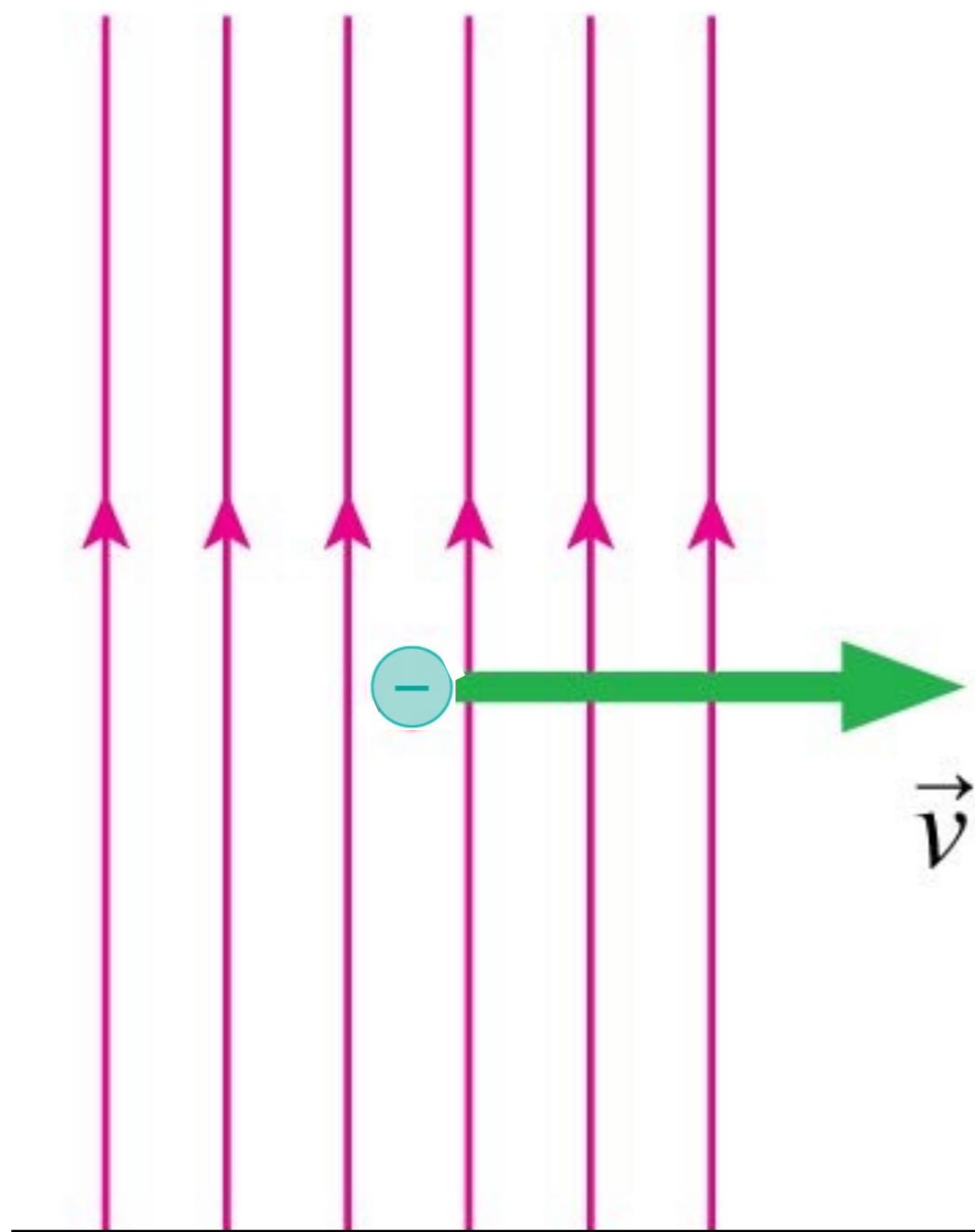
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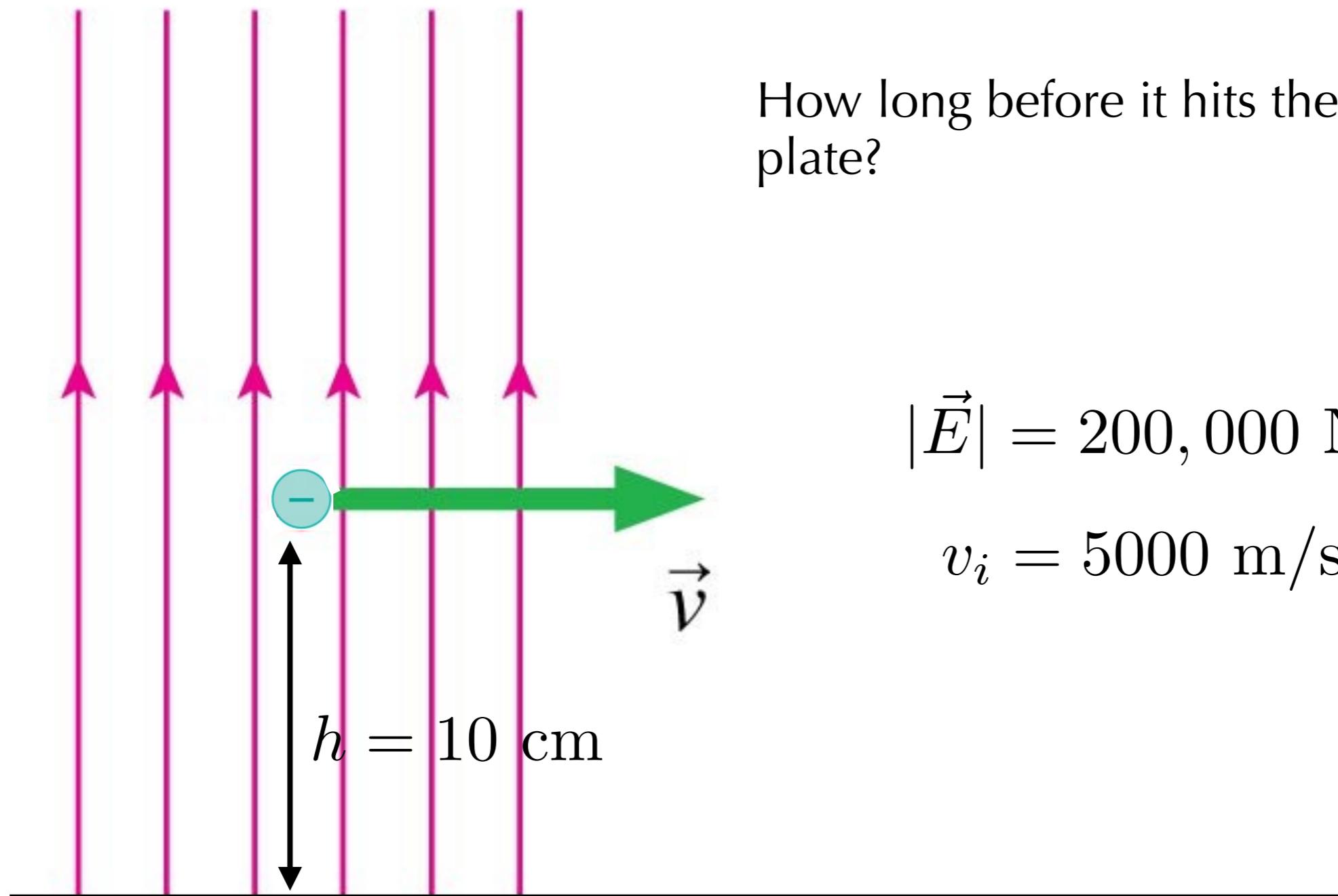
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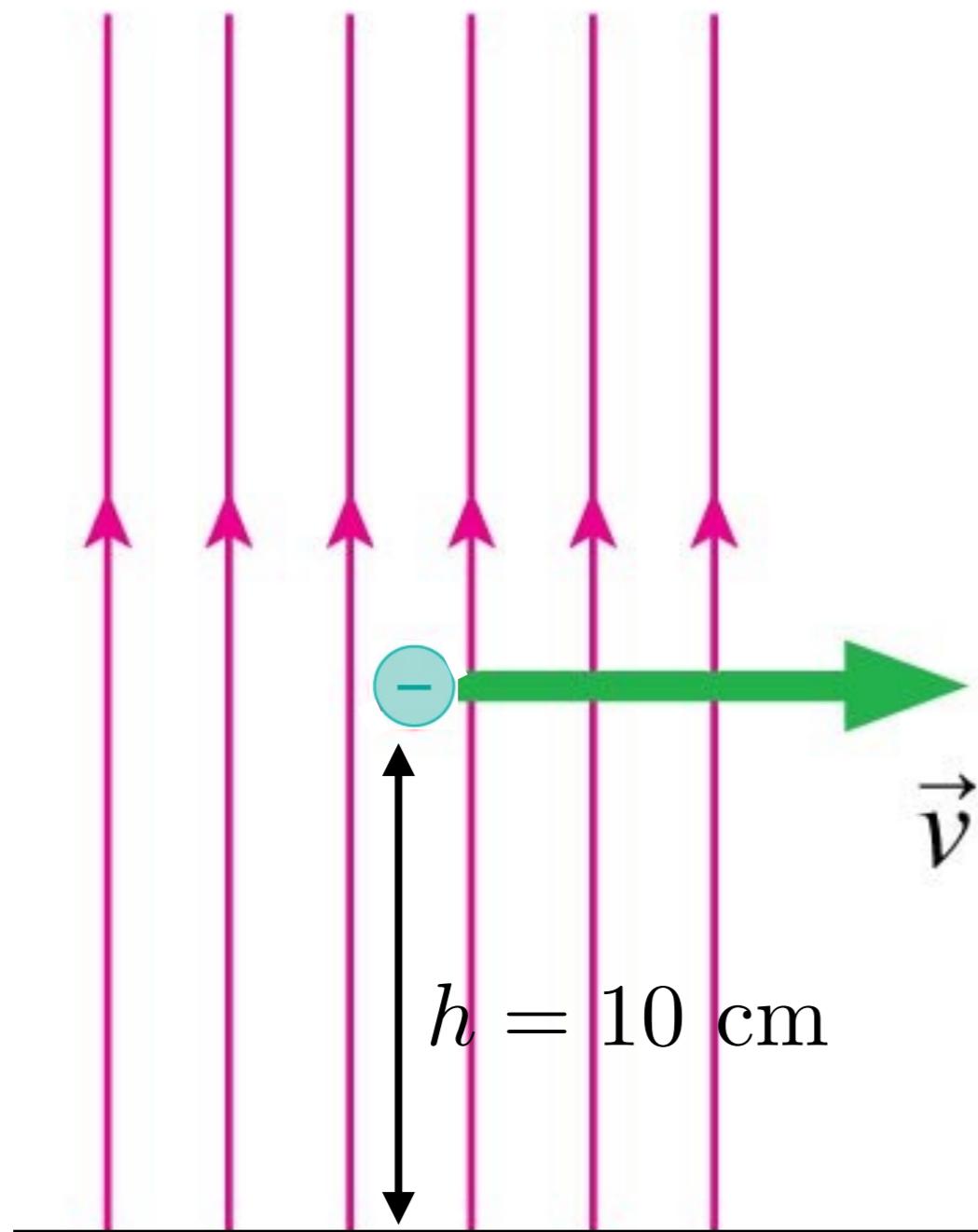
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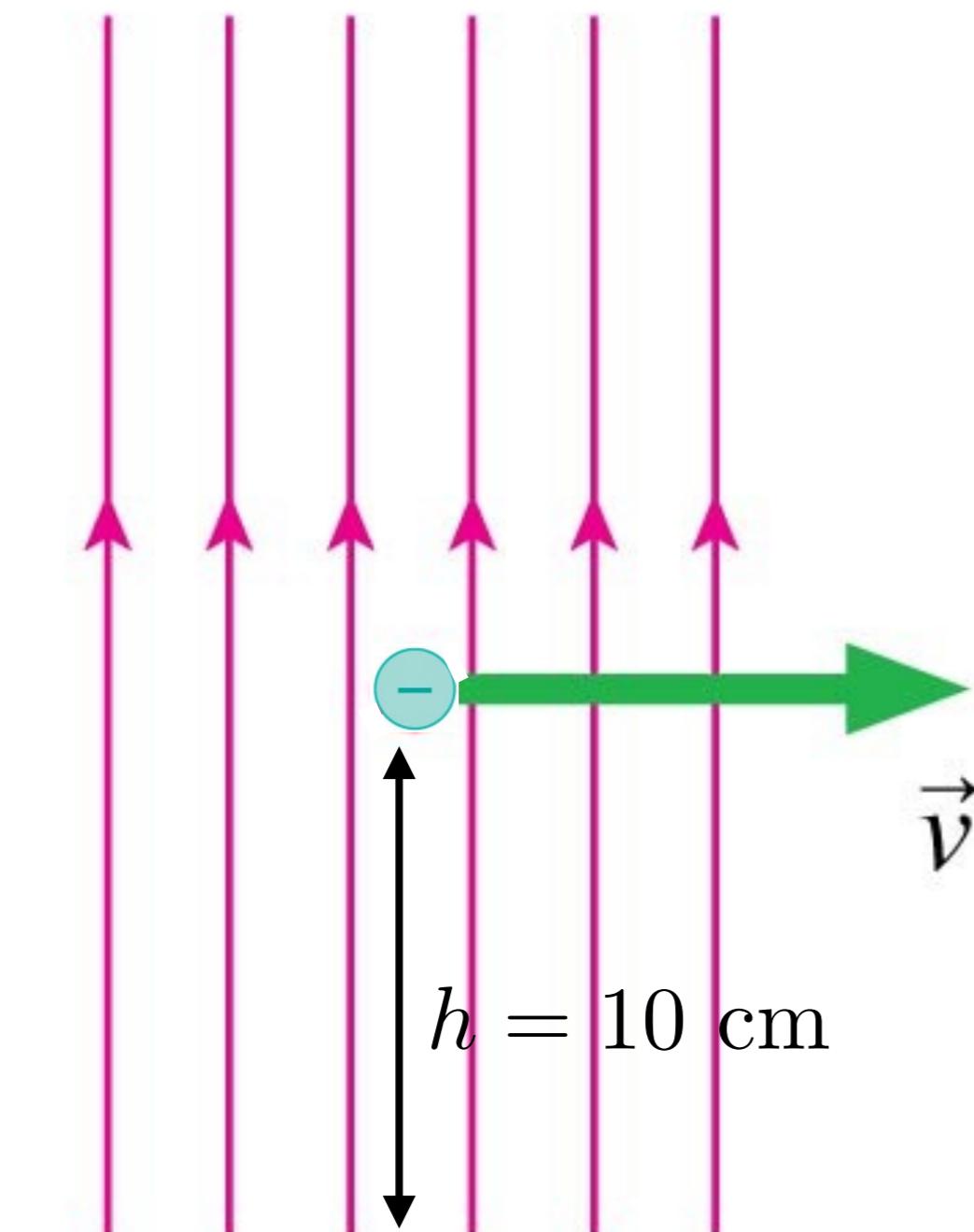
$$v_i = 5000 \text{ m/s}$$

$$\Delta t = 7.5 \times 10^{-8} \text{ s}$$

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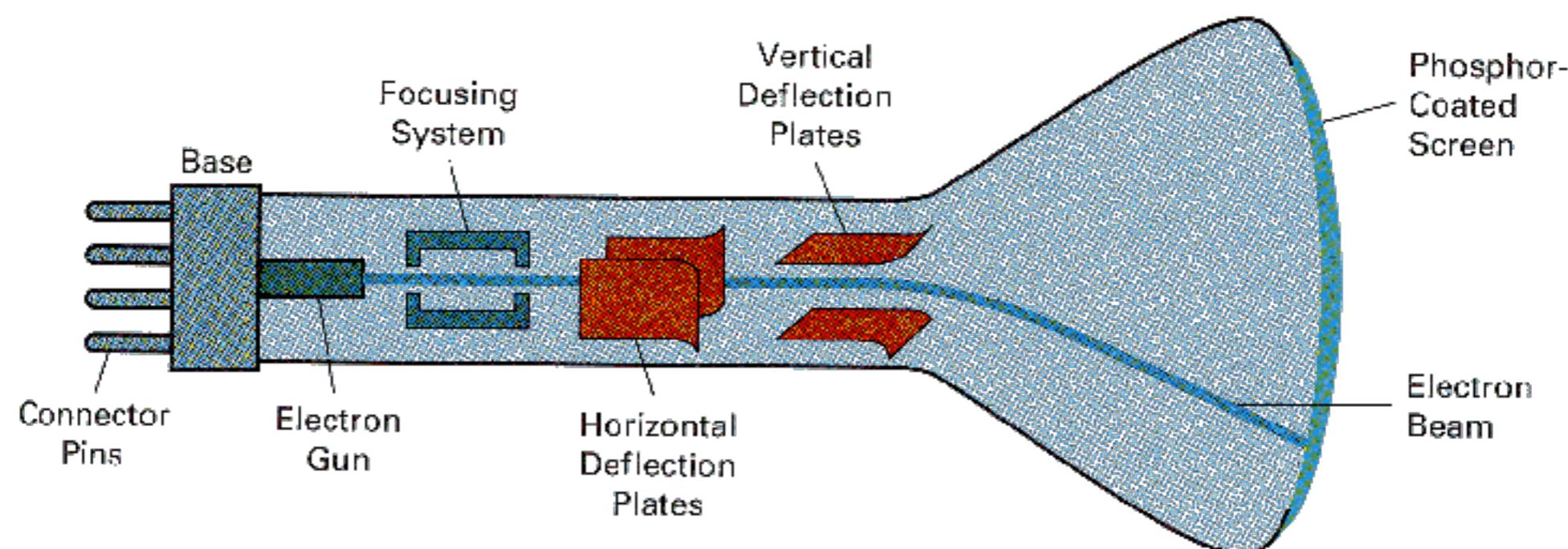
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$$\Delta x = 3.8 \text{ mm}$$

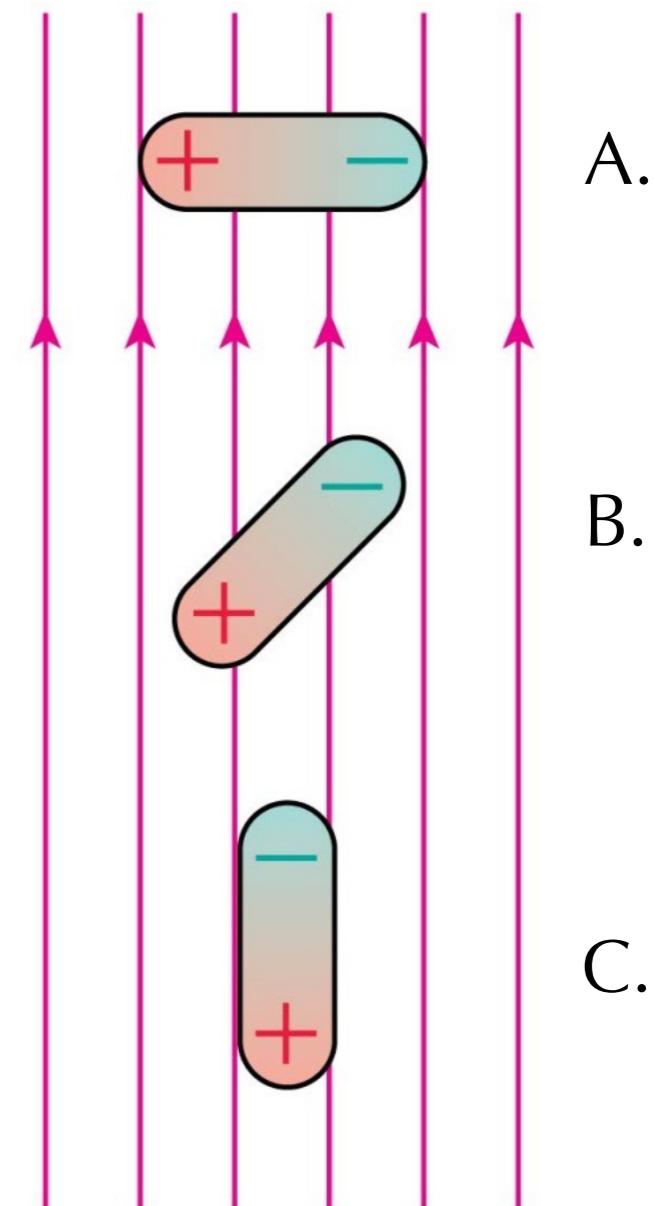
Cathode Ray Tube



Quiz

Which dipole experiences no net force in the electric field?

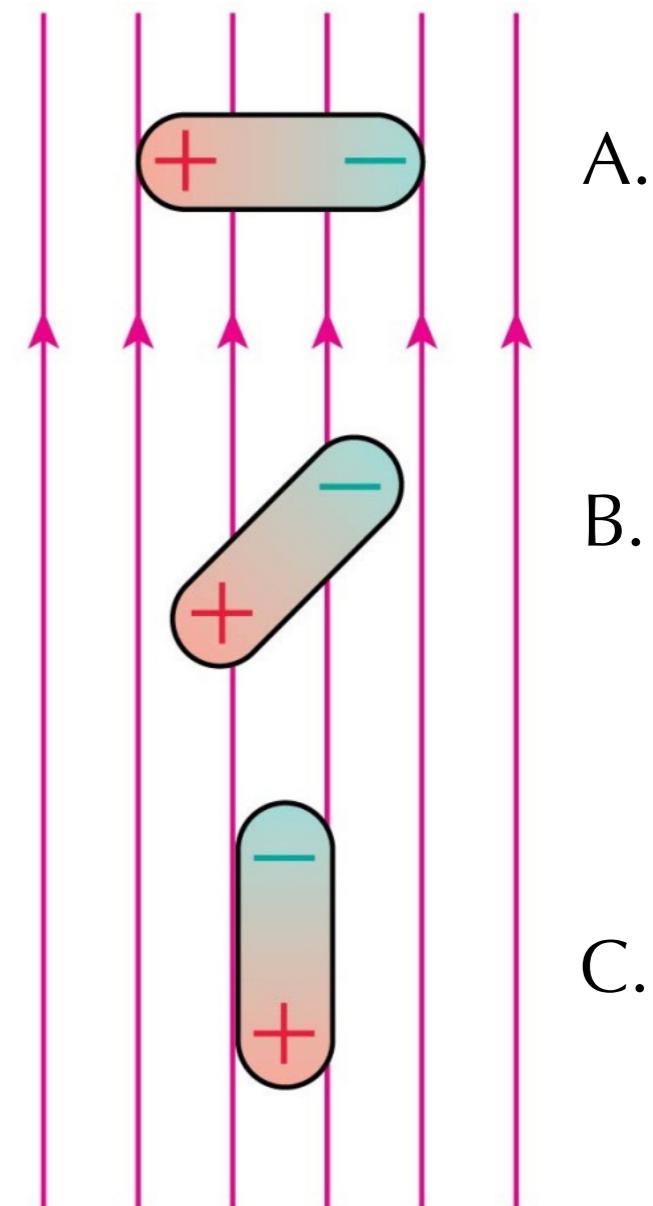
- A. Dipole A.
- B. Dipole B.
- C. Dipole C.
- D. Both dipoles A and C.
- E. All three dipoles.



Quiz

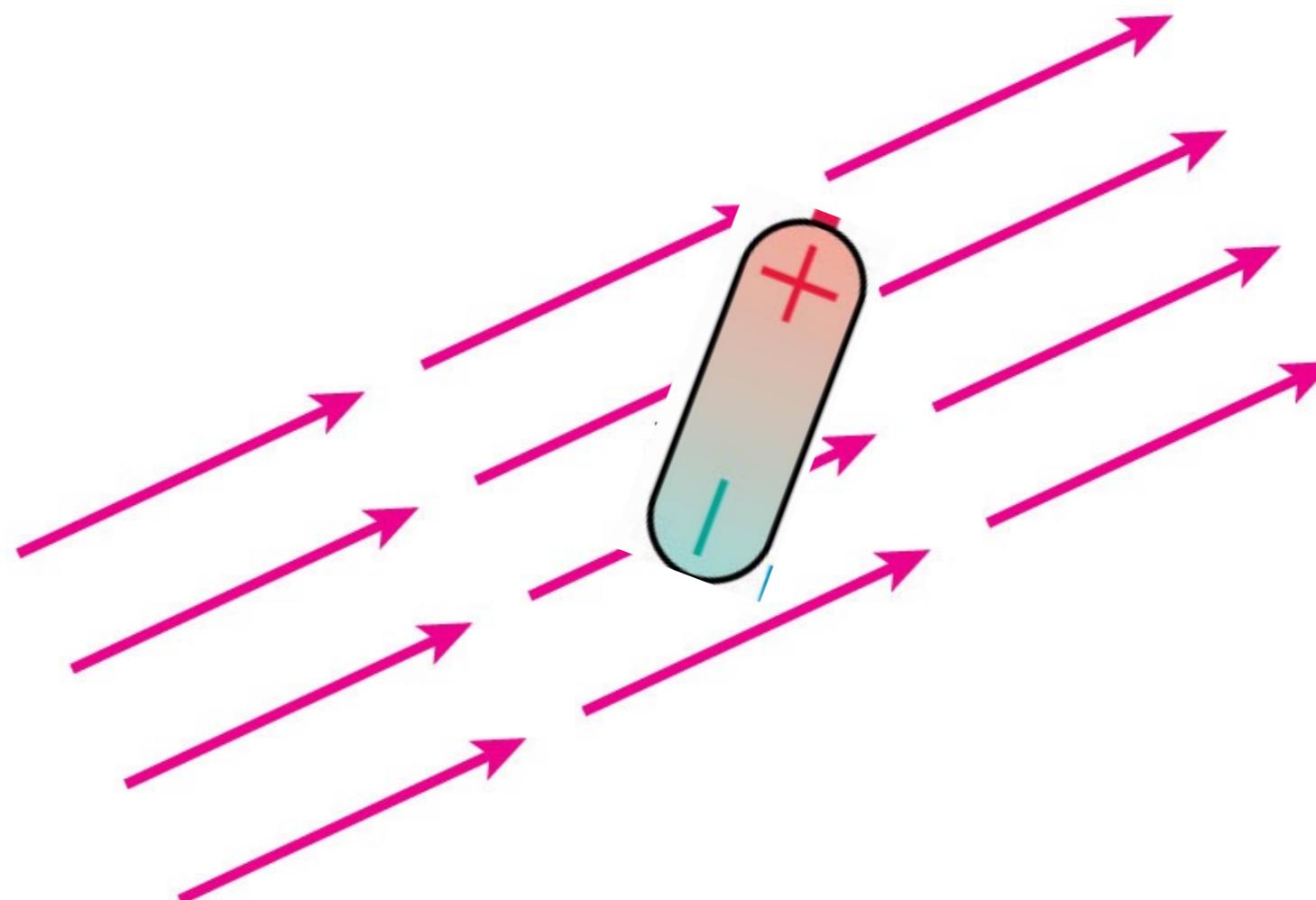
Which dipole experiences no net torque in the electric field?

- A. Dipole A.
- B. Dipole B.
- C. Dipole C.
- D. Both dipoles A and C.
- E. All three dipoles.



Dipoles in Uniform fields

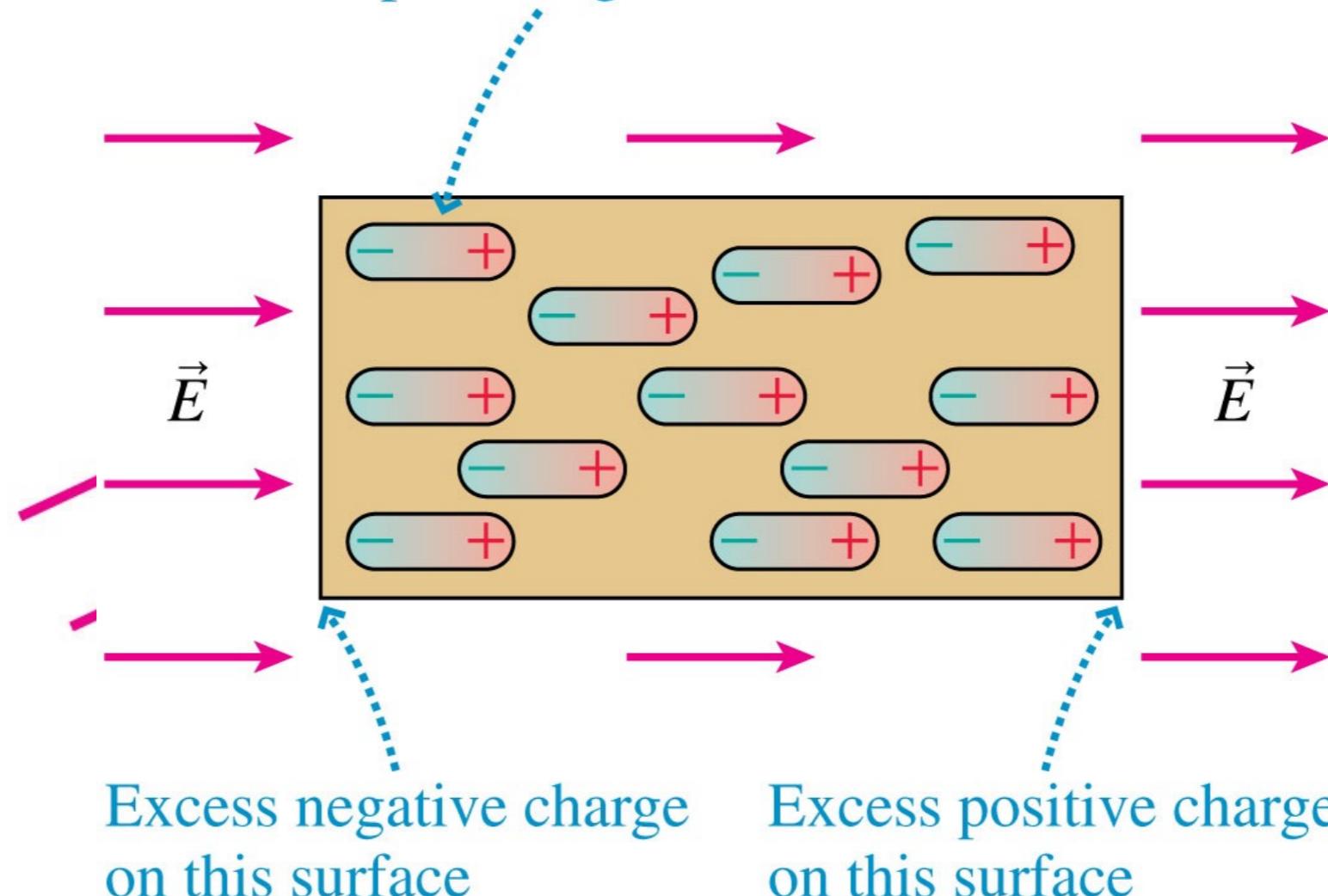
What will happen to the dipole?



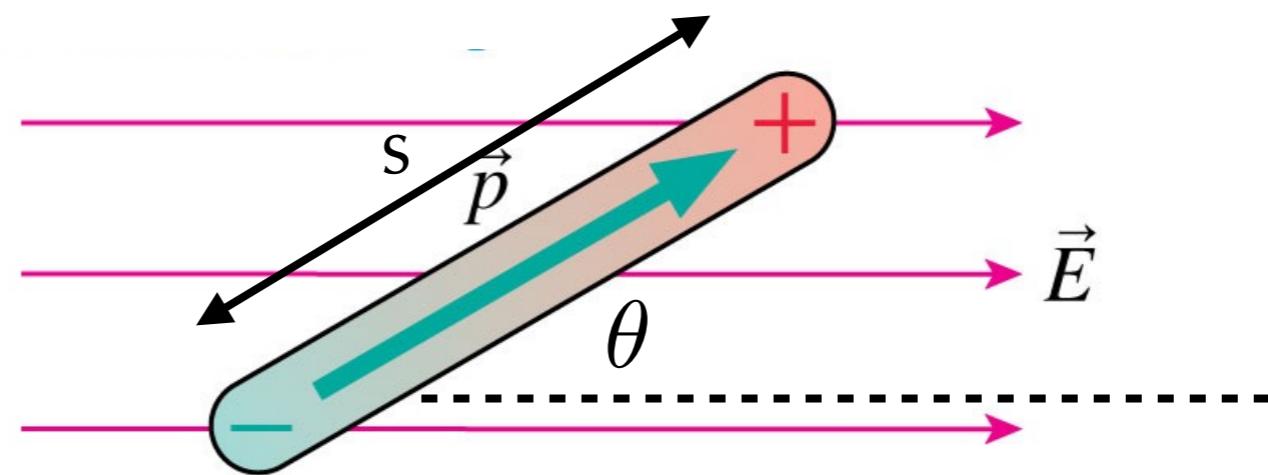
Dipoles in Uniform fields

What will happen to the dipole?

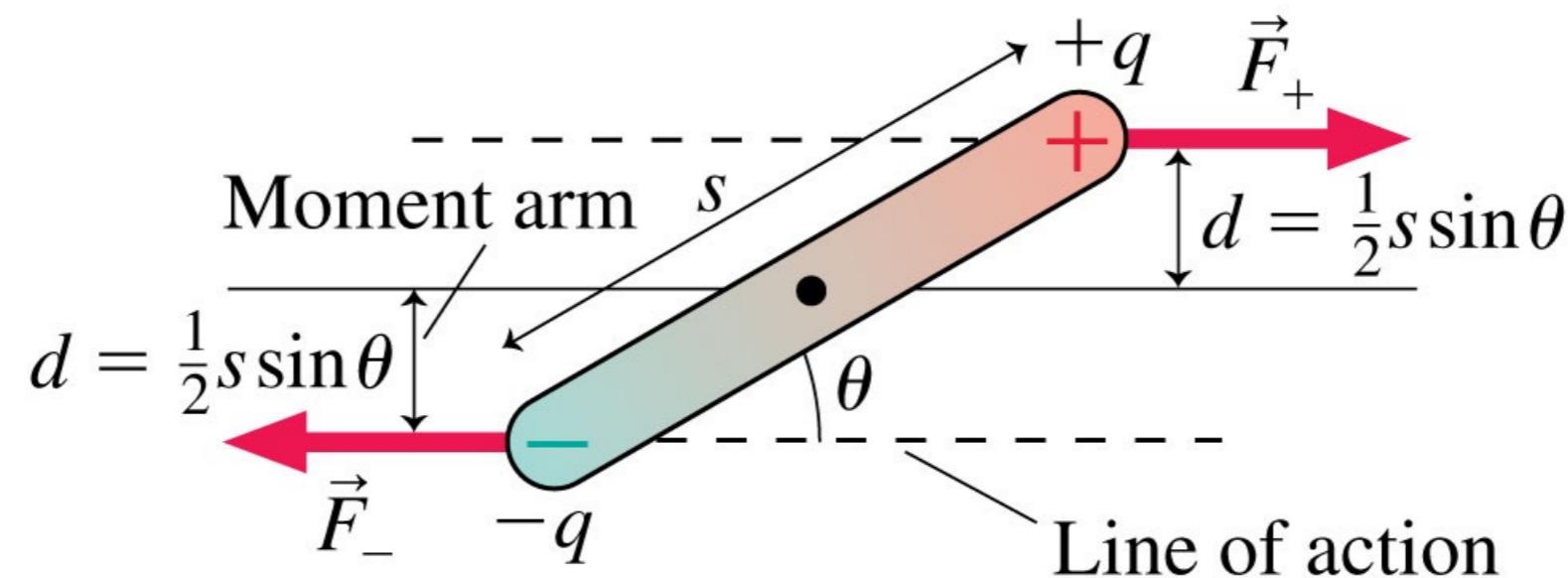
The dipoles align with the electric field.



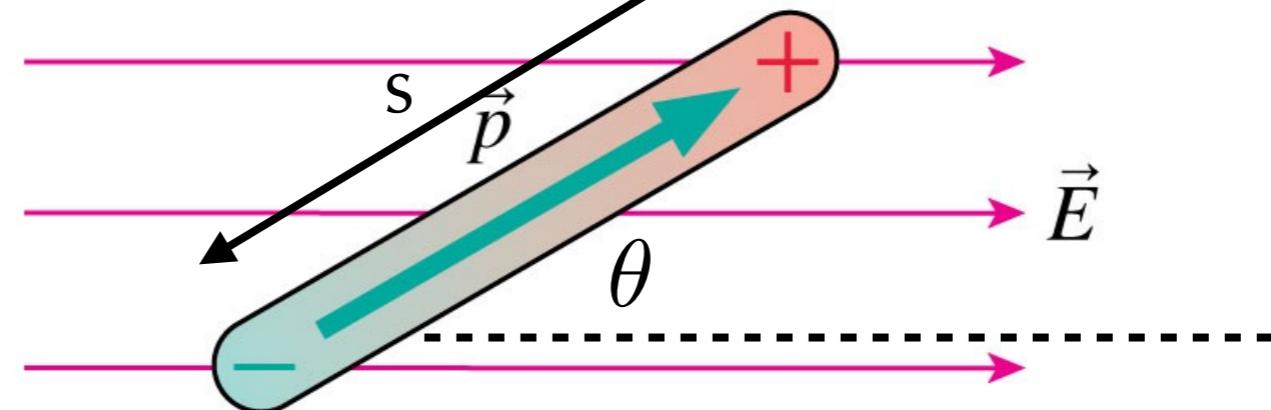
Write down an expression for the torque that this dipole experiences



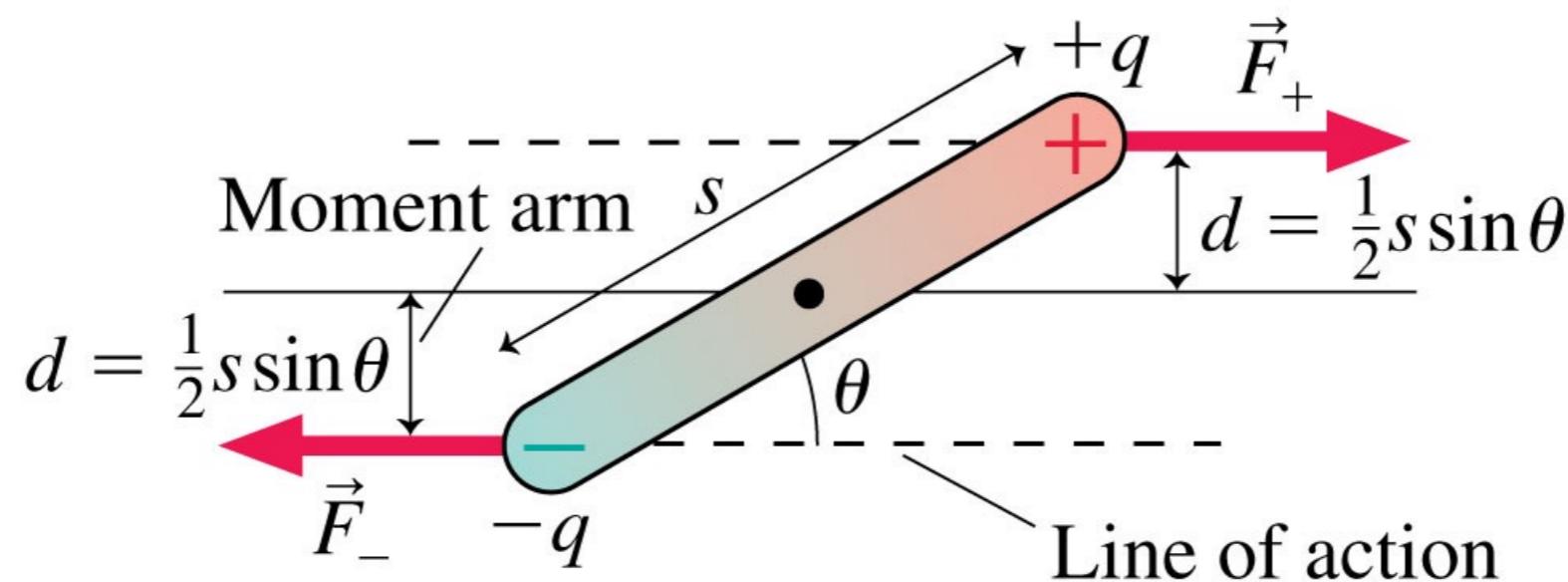
Write down an expression for the torque that this dipole experiences



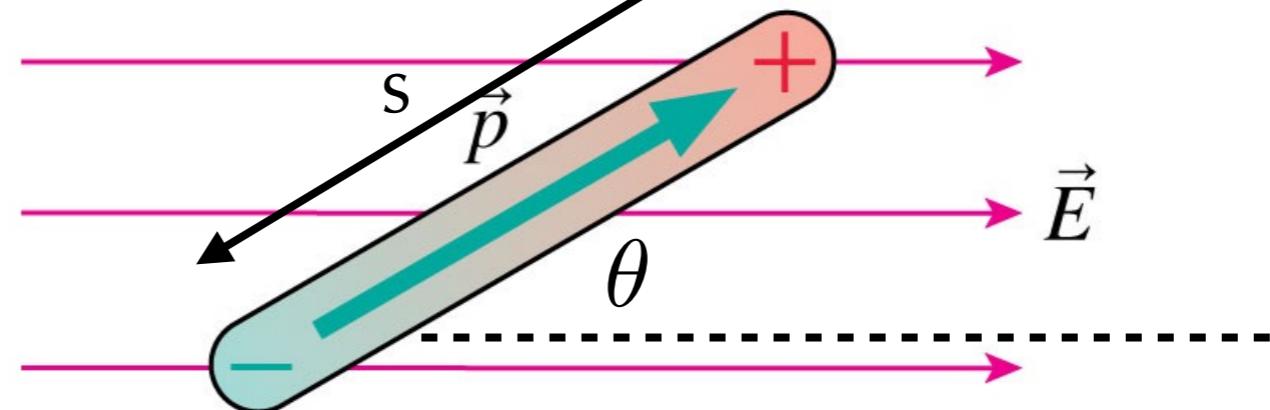
In terms of vectors, $\vec{\tau} = \vec{p} \times \vec{E}$



Write down an expression for the torque that this dipole experiences



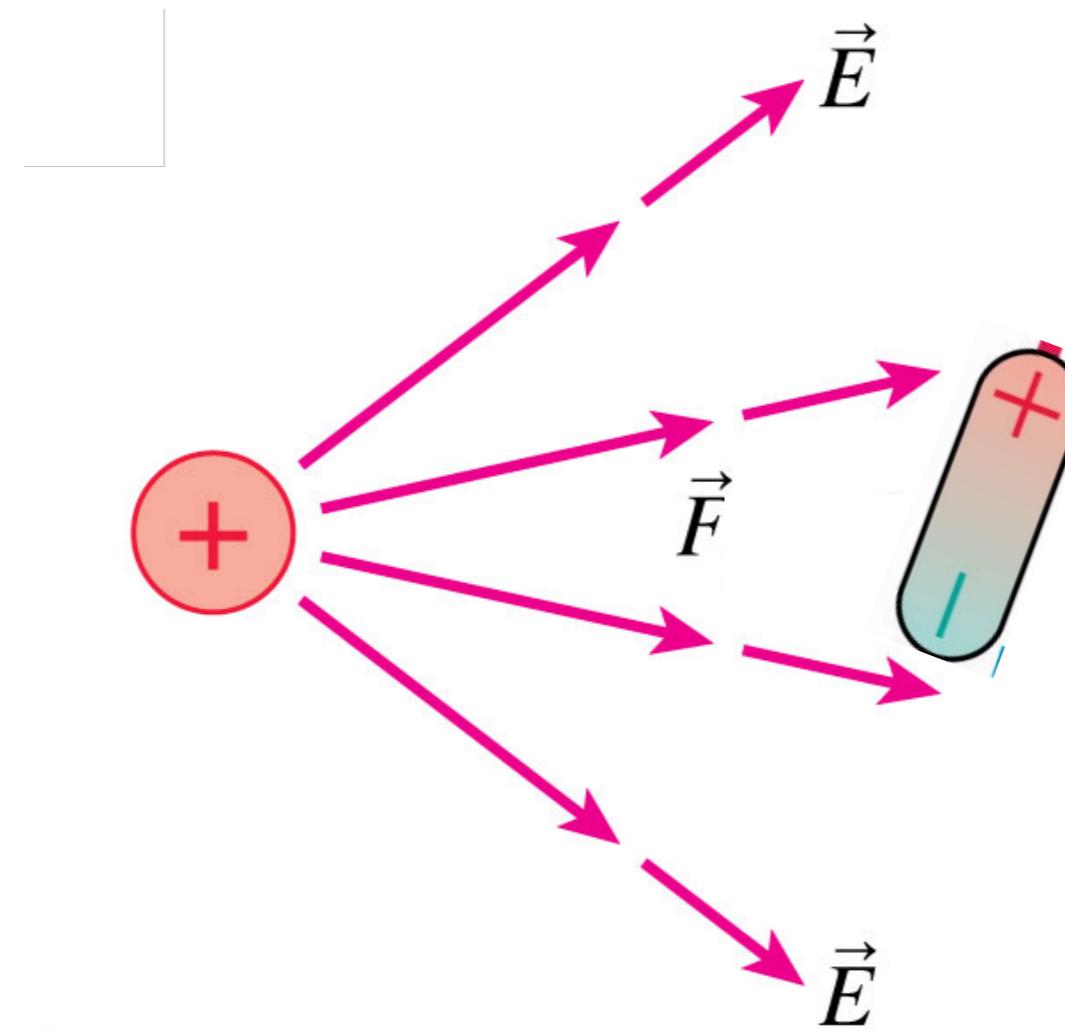
In terms of vectors, $\vec{\tau} = \vec{p} \times \vec{E}$



$$\tau = 2 \times dF_+ = 2(\frac{1}{2}s \sin \theta)(qE) = pE \sin \theta$$

Dipole in nonuniform field

A dipole is placed near a positive point charge.
Describe the motion of the dipole.



Dipole in nonuniform field

A dipole is placed near a positive point charge.
Describe the motion of the dipole.

