



PH 220

Lance Nelson

# Review

1

2

A

Find the magnetic field produced by a current loop. (Or multiple current loops)

B

$$\boxed{4} \quad \vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \hat{r}}{r^2}$$

Asked to calculate the magnetic dipole moment.

3

C

$$\boxed{5} \quad \vec{\mu} = (AI, \text{ from the south pole to the north pole})$$

$$\boxed{6} \quad \vec{B} = \frac{\mu_0}{4\pi} \frac{I\Delta\vec{s} \times \hat{r}}{r^2}$$

Find the magnetic field produced by multiple lines of current.

D

E

Calculate the path integral of the B field

7

F

Leverage the symmetry of the current configuration to determine magnetic field.

# Review

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Find the magnetic field produced by a current loop. (Or multiple current loops)

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$$\vec{B} = \frac{\mu_0 I}{2\pi d}$$

Find the magnetic field produced by a point charge in motion. ( or multiple point charges in motion)

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$$\vec{B} = \frac{\mu_0 I}{2\pi d}$$

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$$B = \frac{\mu_0}{2} \frac{IR^2}{(z^2 + R^2)^{3/2}}$$

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Find the magnetic field produced by multiple lines of current.

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Calculate the path integral of the B field

$$\vec{B}_{\text{dipole}} = \frac{\mu_0}{4\pi} \frac{2\vec{\mu}}{z^3}$$

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(on the axis of a magnetic dipole)

F

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$$E \quad \vec{B}_{\text{dipole}} = \frac{\mu_0}{4\pi} \frac{2\vec{\mu}}{z^3} \quad (on \text{ the axis of a magnetic dipole})$$

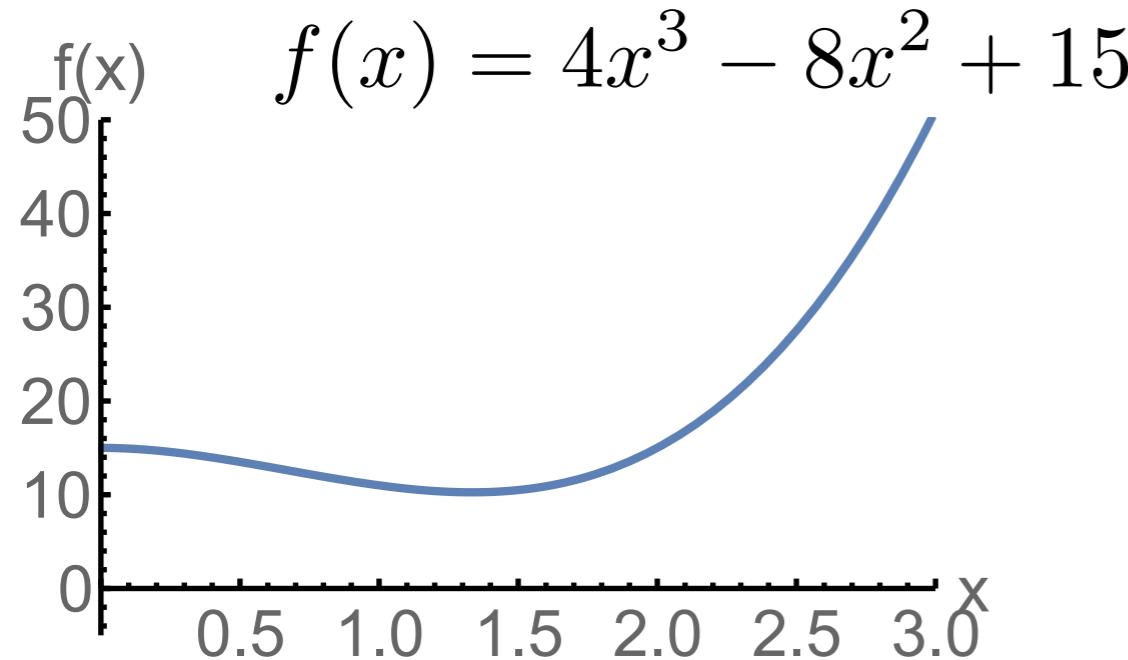
Calculate the path integral of the B field

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F Leverage the symmetry of the current configuration to determine magnetic field.

# Calculus Review

Remind yourself: How would you find the length of this line



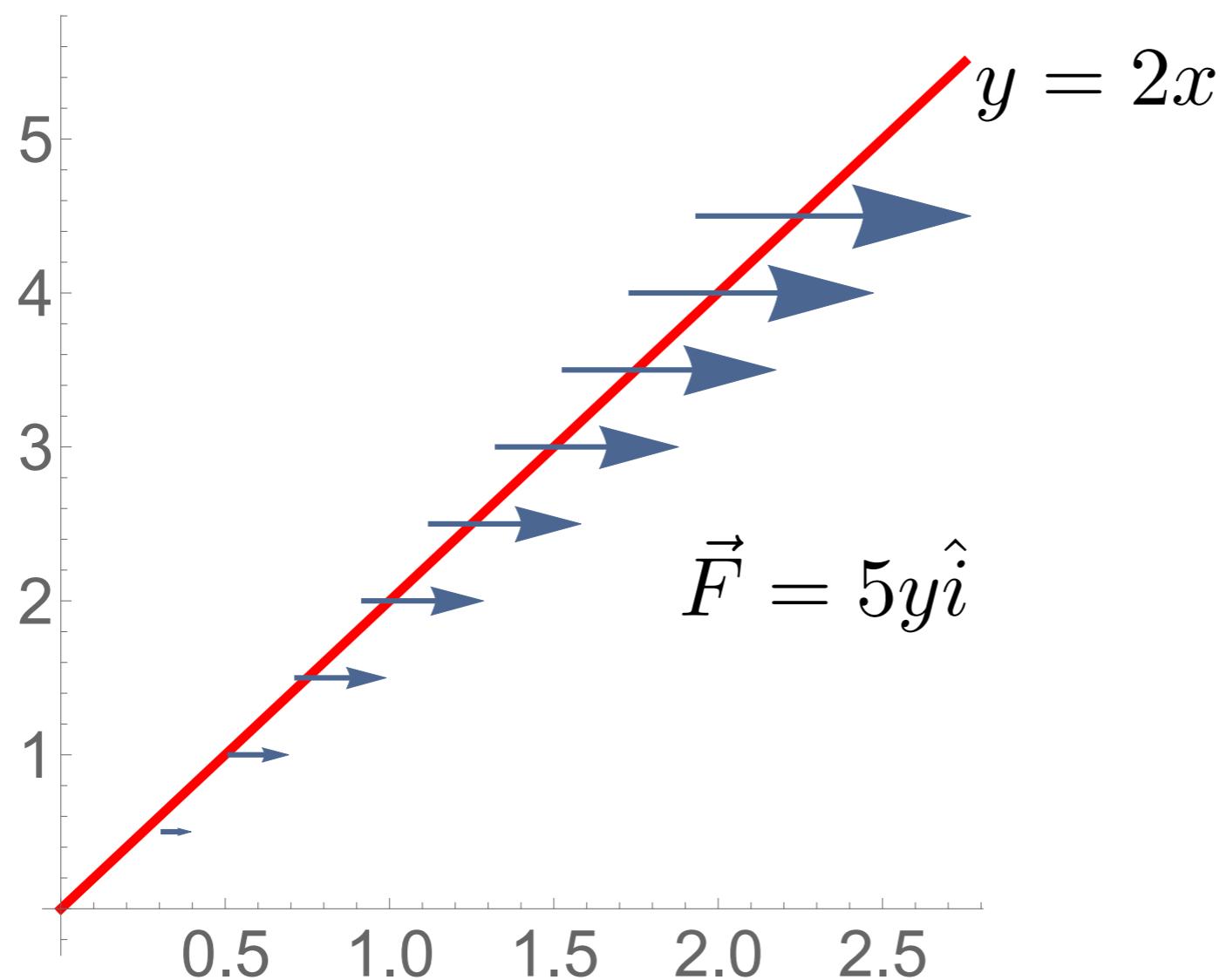
$$f(x) = 4x^3 - 8x^2 + 15$$

$$\int ds$$

$$d\vec{s} = dx\hat{i} + dy\hat{j}$$

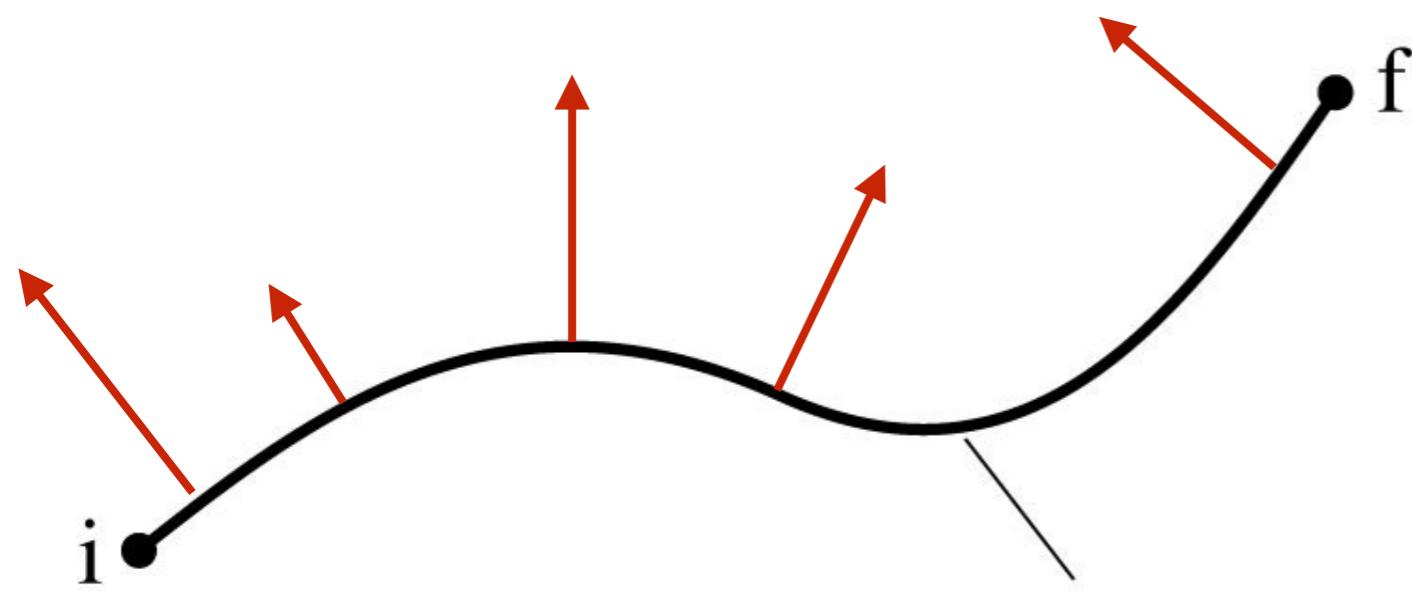
$$ds = \sqrt{dx^2 + dy^2}$$

# Intro to Ampere's law

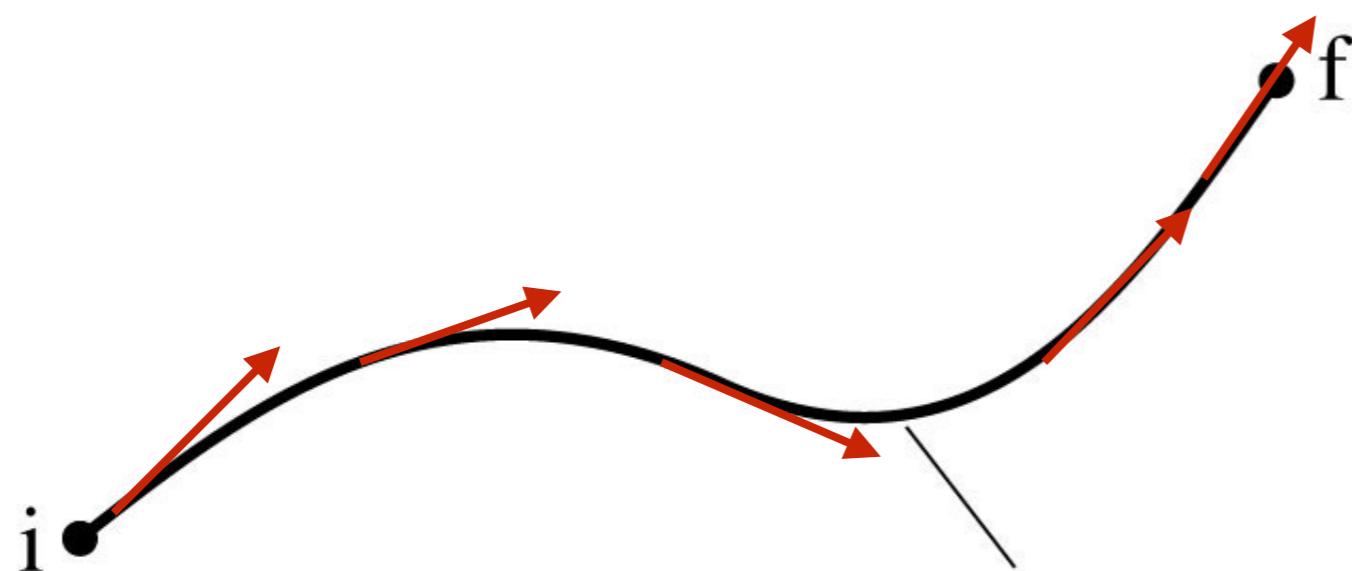


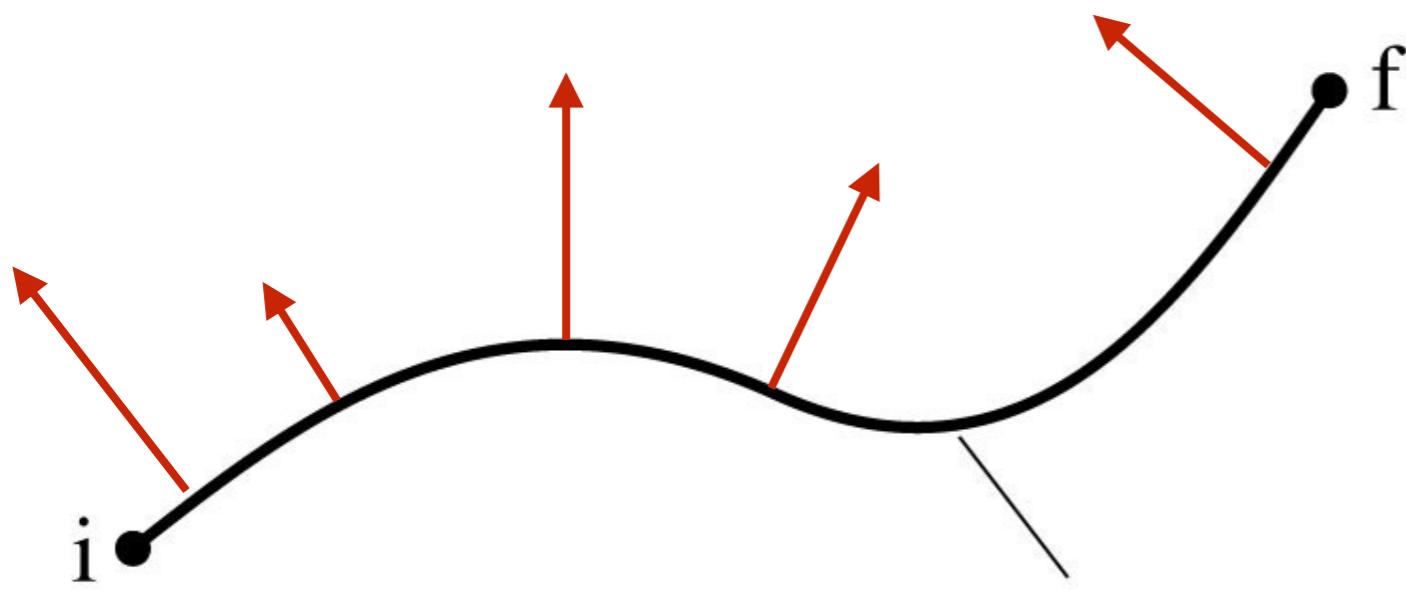
$$\int \vec{F} \cdot d\vec{s}$$

$$d\vec{s} = dx\hat{i} + dy\hat{j}$$



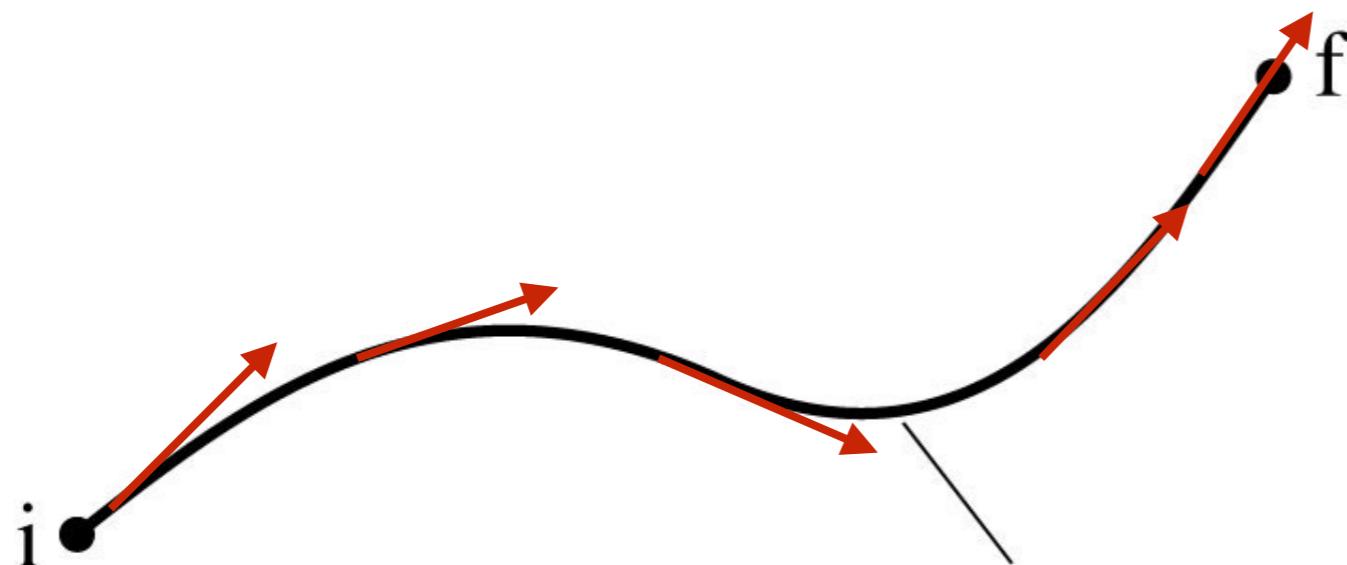
What would these line integrals be?





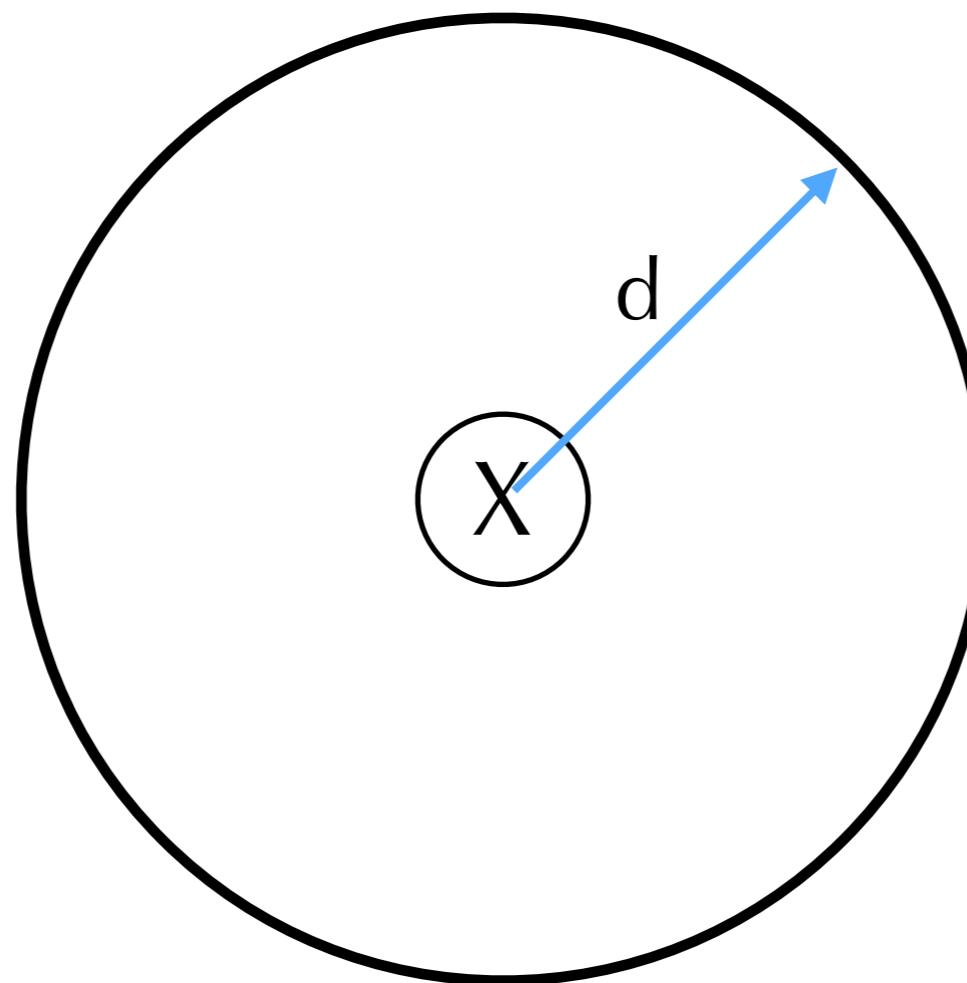
What would these line integrals be?

$$\int_i^f \vec{B} \cdot d\vec{s}$$



# Ampere's Law: Like Gauss's law but for magnetism

What is the value of this integral?

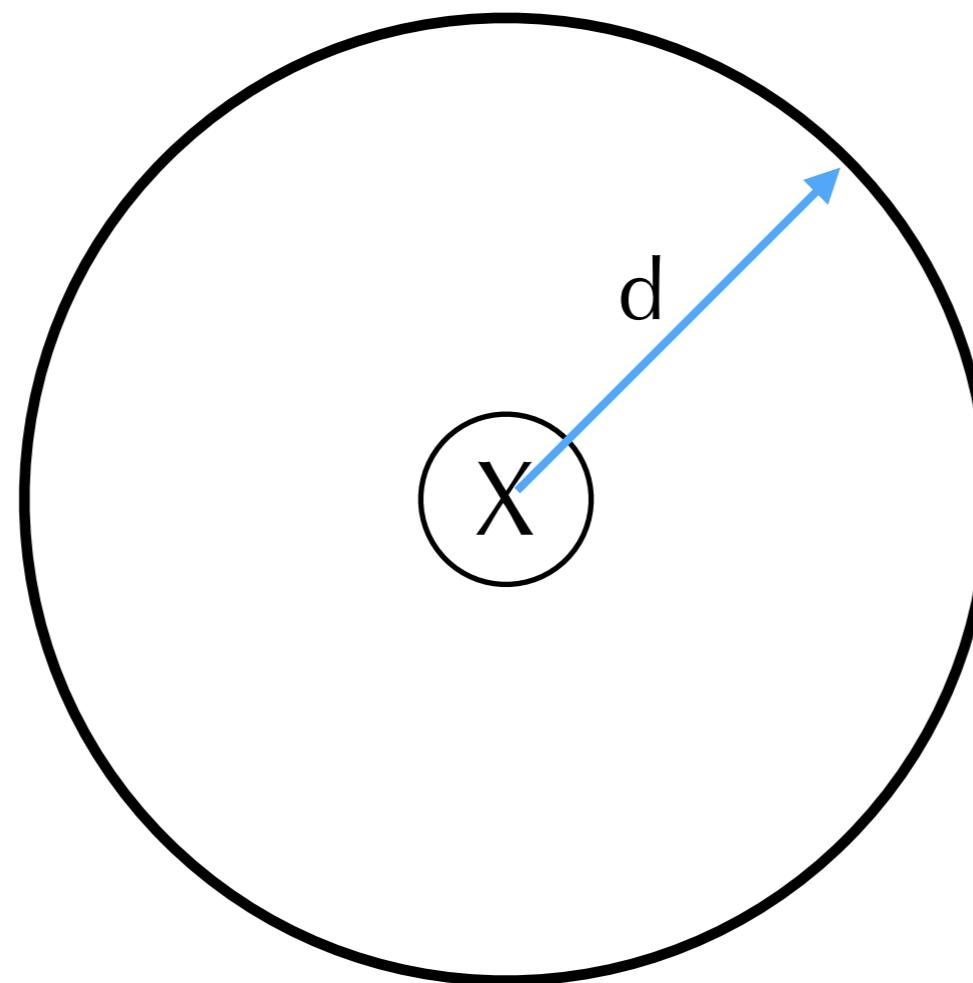


$$\oint \vec{B} \cdot d\vec{s}$$

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$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I$$

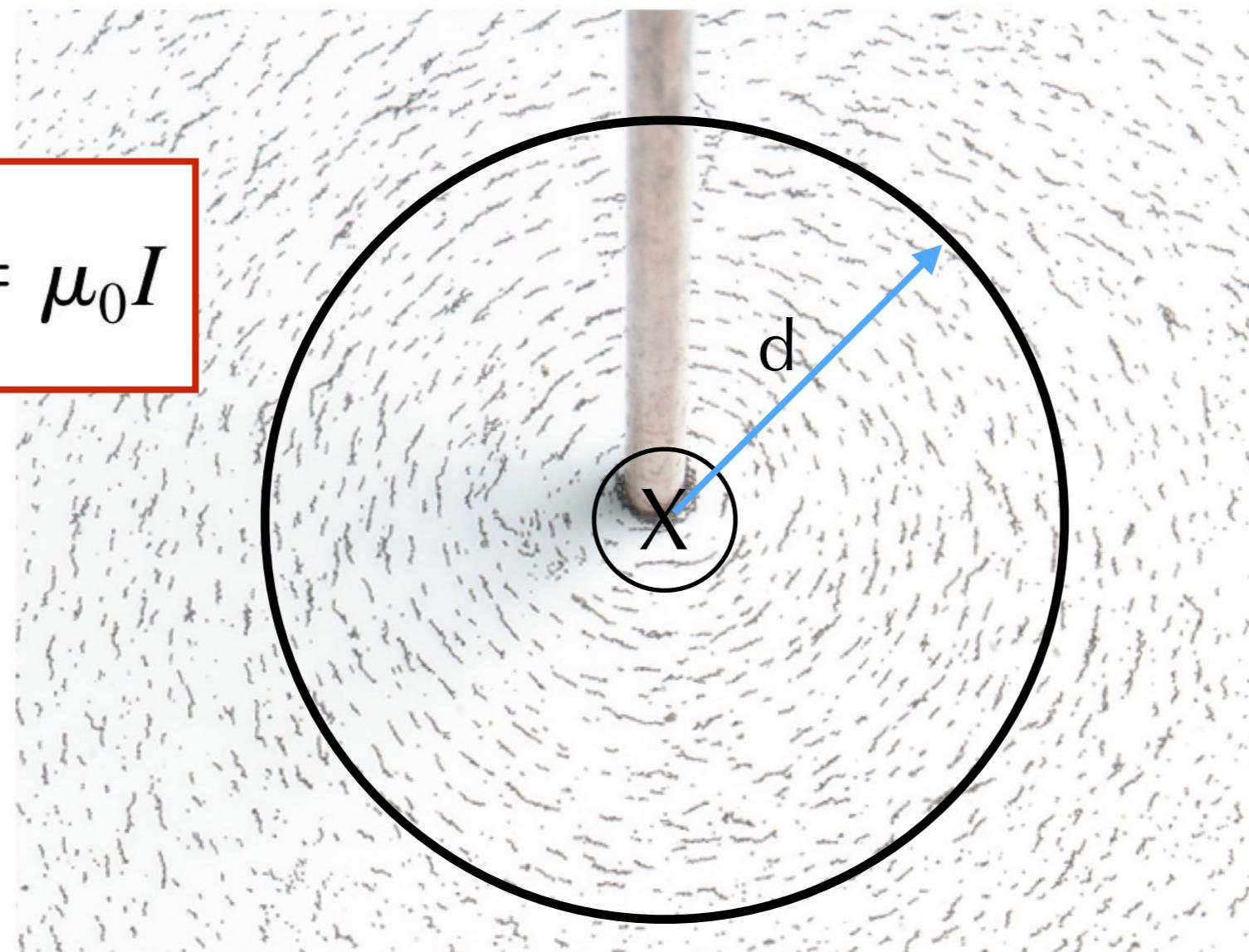


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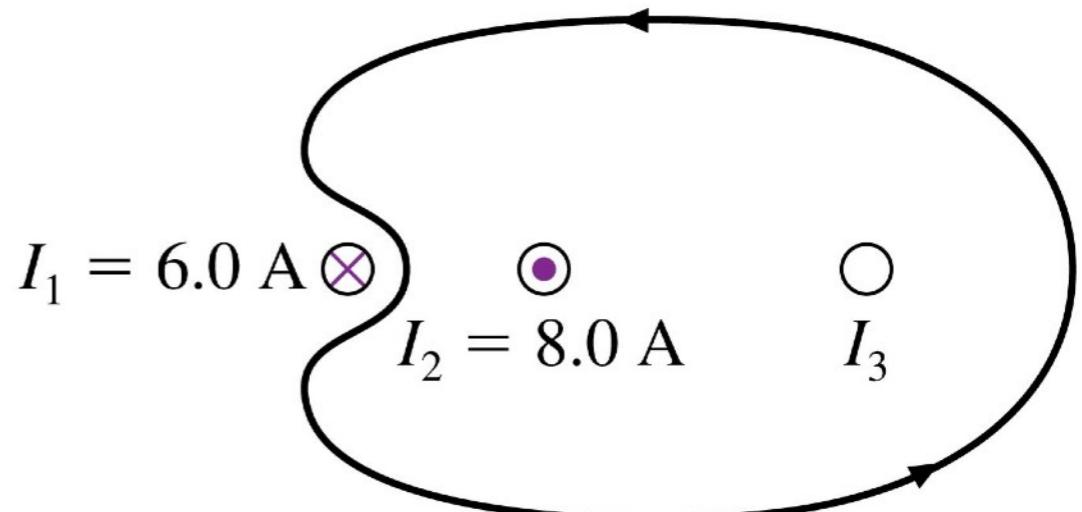


$$\oint \vec{B} \cdot d\vec{s}$$

The line integral of  $B$  around the loop is  $\mu_0 \cdot 7.0 \text{ A}$ .

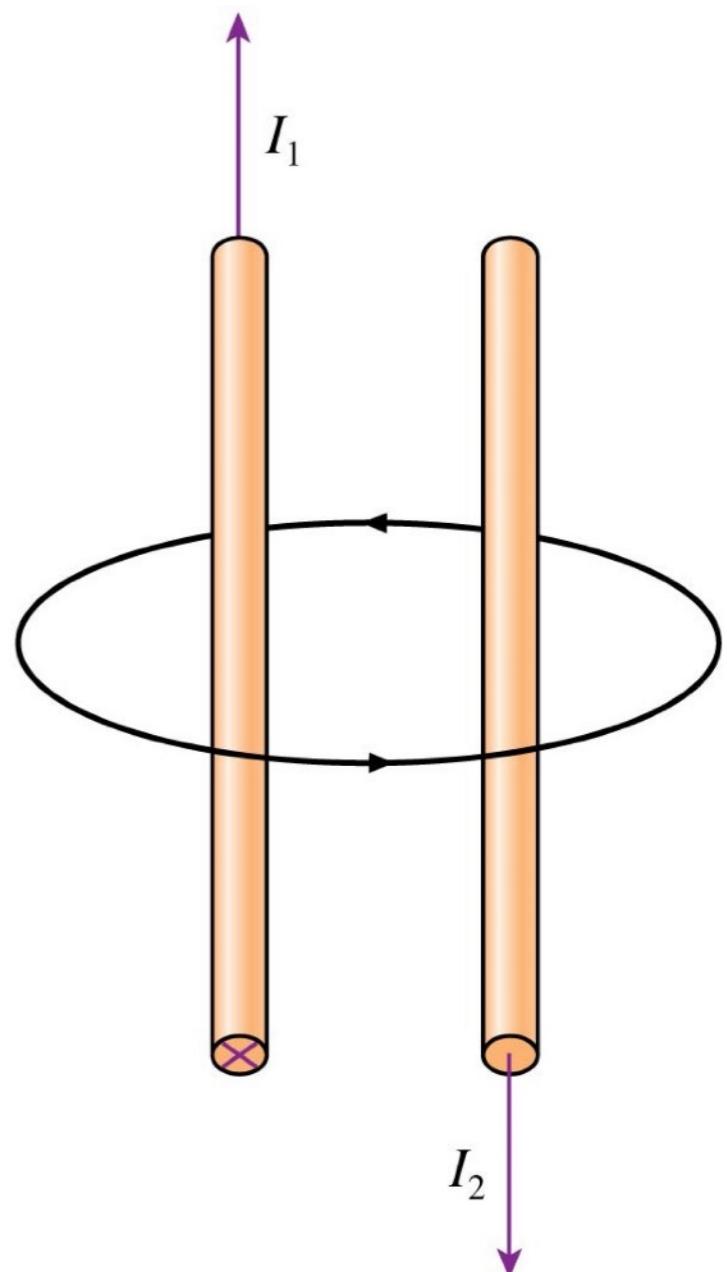
Current  $I_3$  is

- A. 0 A.
- B. 1 A out of the screen.
- C. 1 A into the screen.
- D. 5 A out of the screen.
- E. 5 A into the screen.



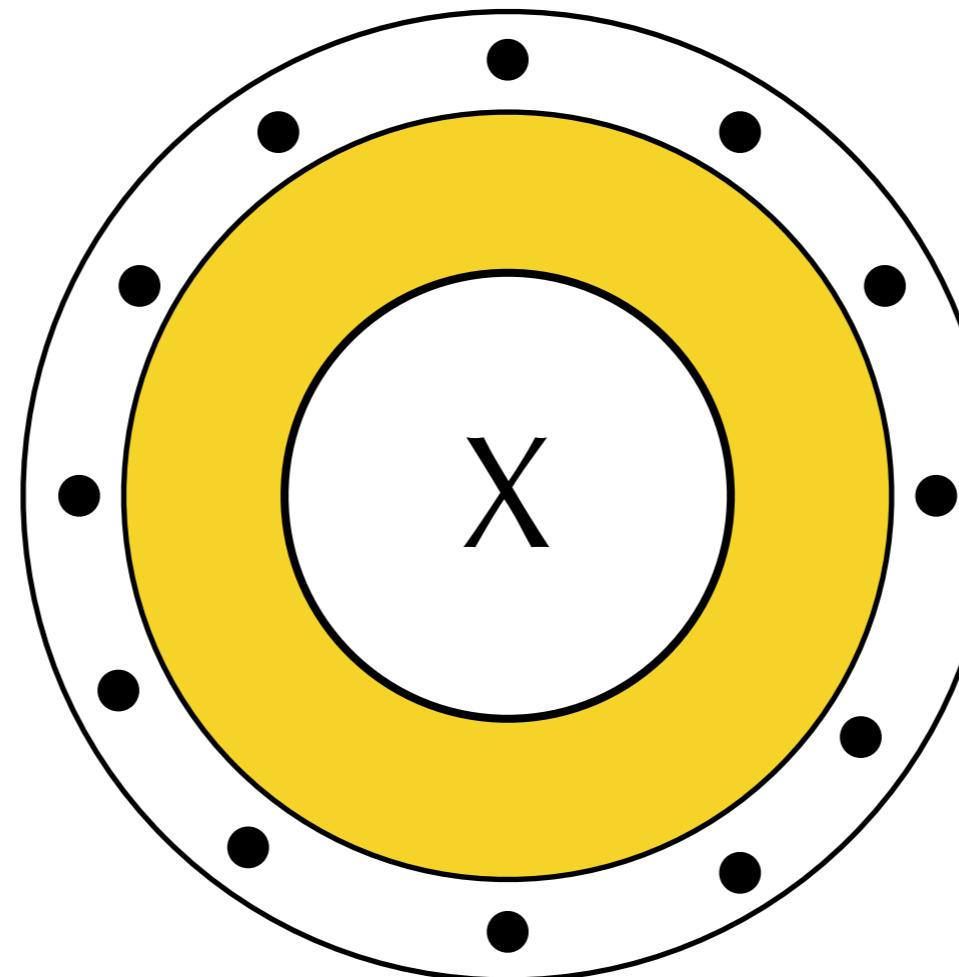
For the path shown,

- A. 0.
- B.  $\mu_0(I_1 - I_2)$ .
- C.  $\mu_0(I_2 - I_1)$ .
- D.  $\mu_0(I_1 + I_2)$ .



# Let's use Ampere's law

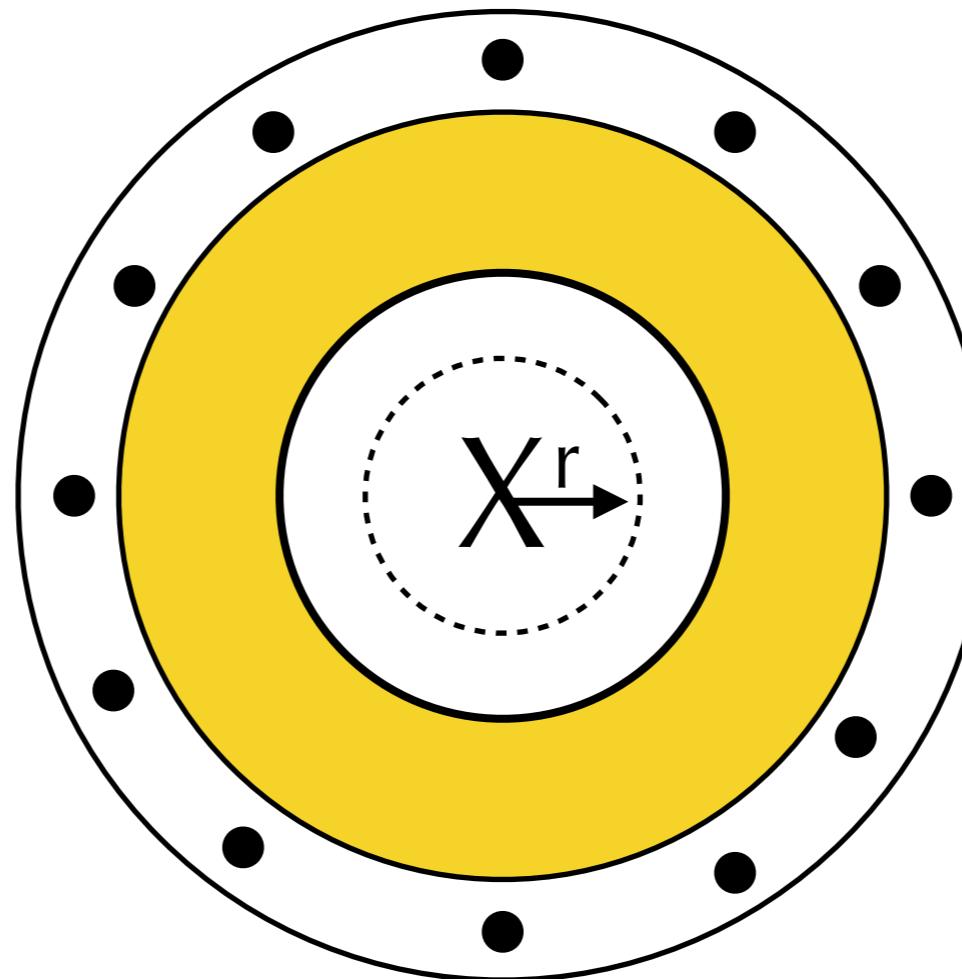
Find the magnetic field for  $r < R_1$



Coaxial cable

# Let's use Ampere's law

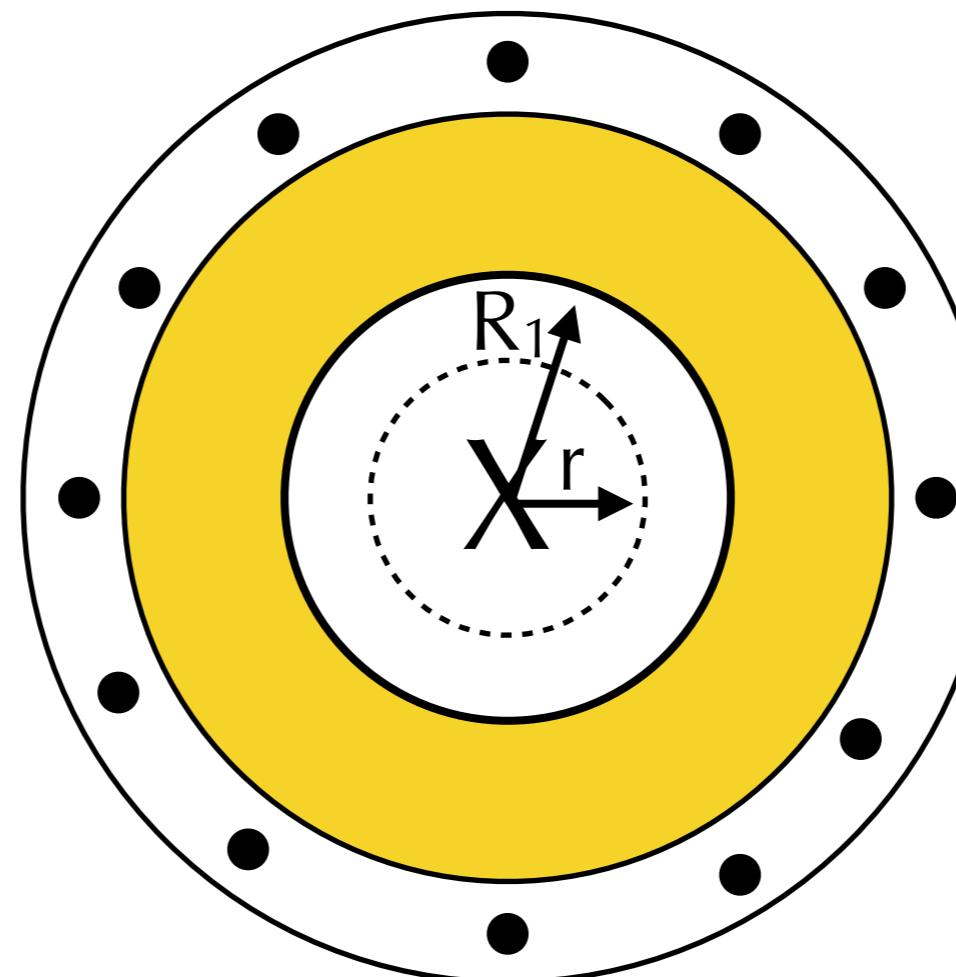
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$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I$$

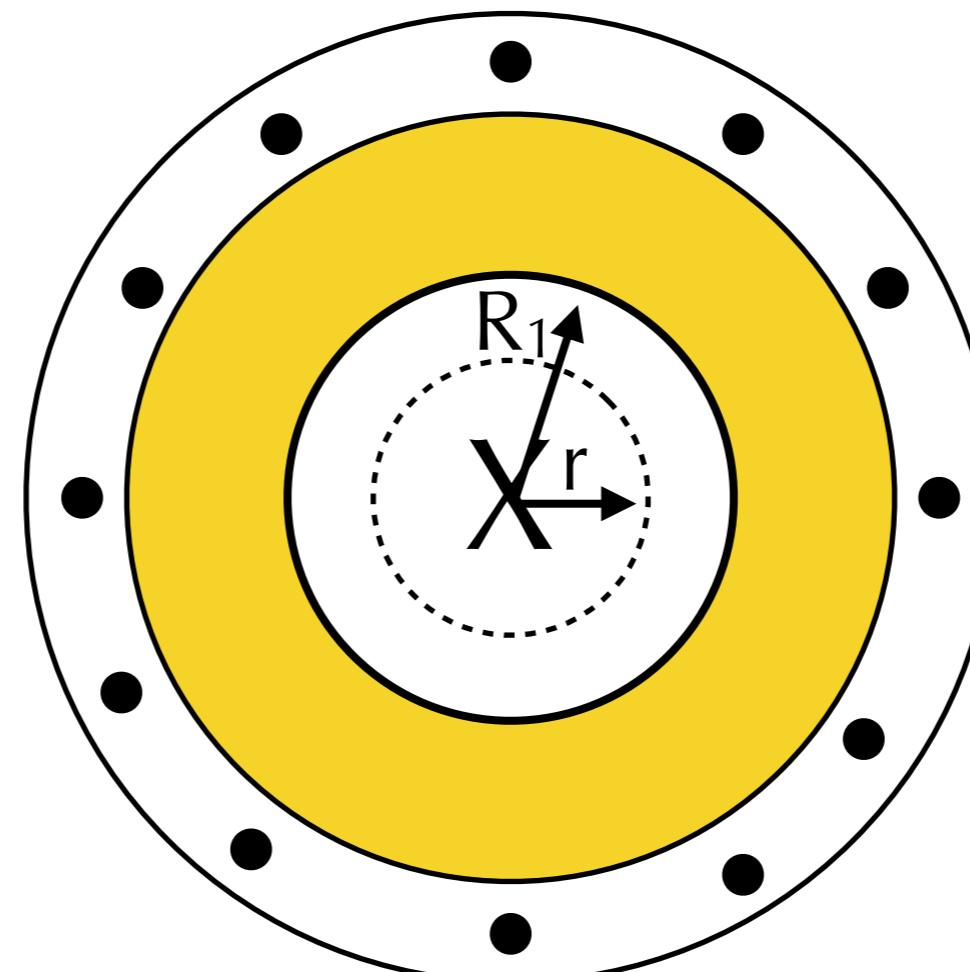
$$B 2\pi r = \mu_0 I_{\text{in}}$$

$$B 2\pi r = \mu_0 \frac{I_{\text{total}}}{\pi R_1^2} \pi r^2$$

$$B 2\pi = \mu_0 \frac{I_{\text{total}}}{R_1^2} r$$

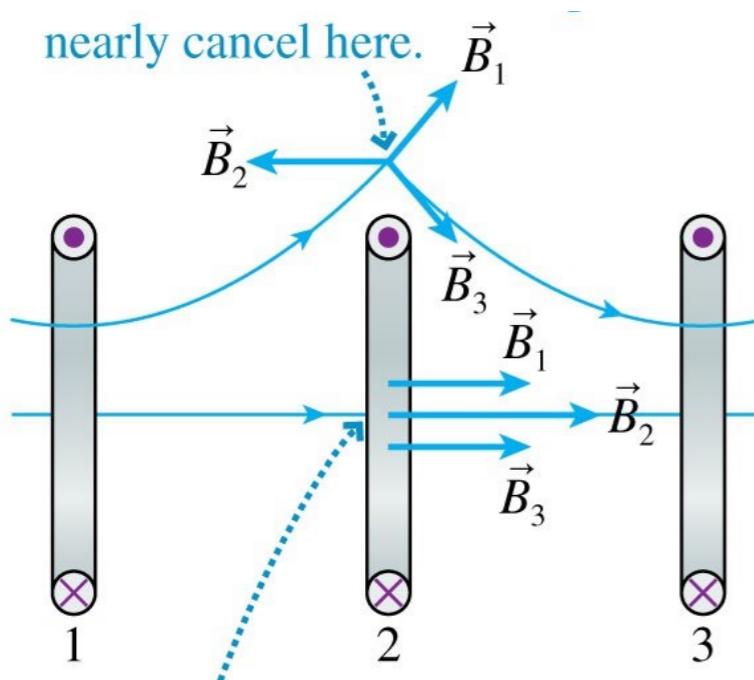
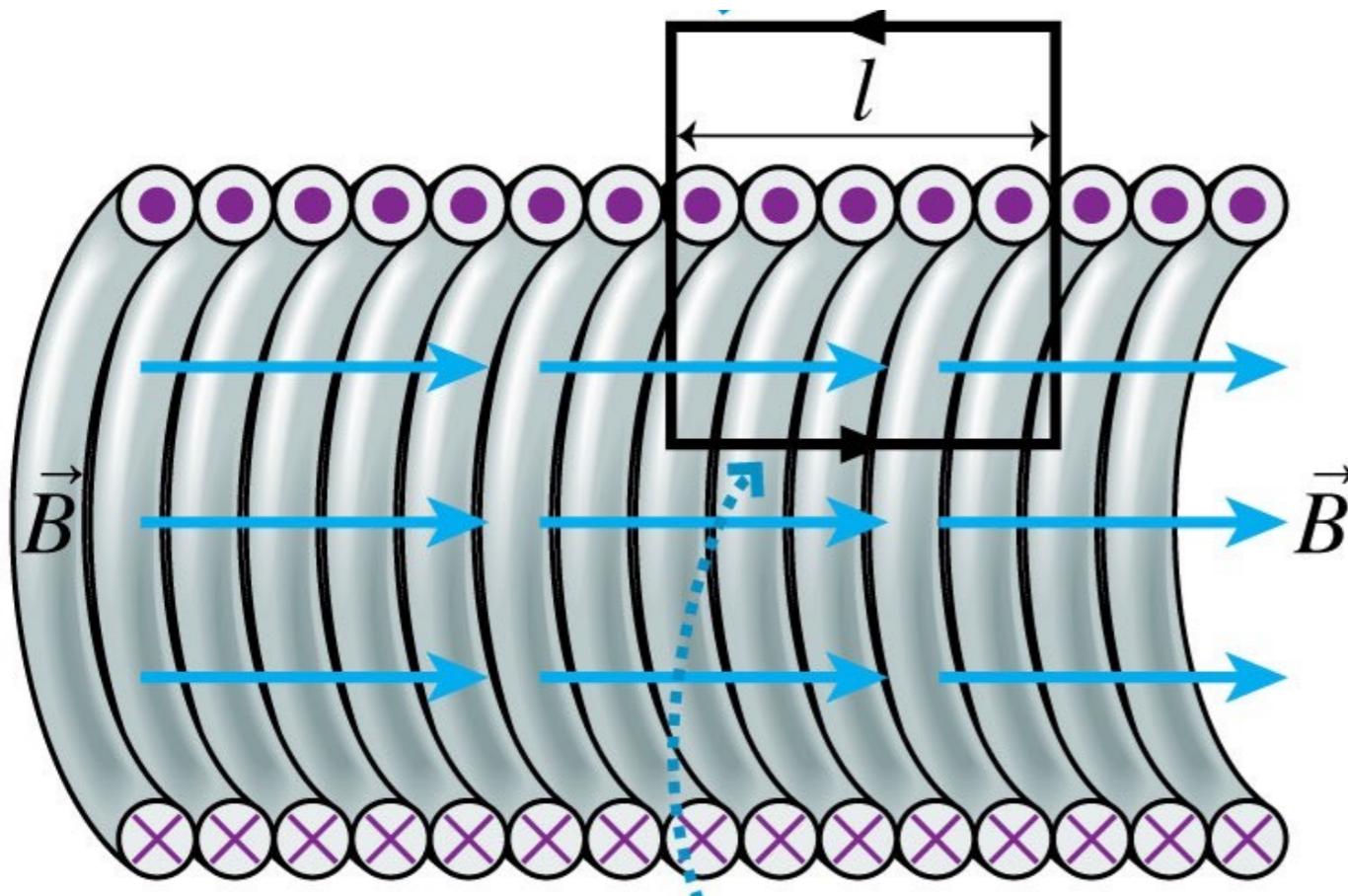
$$B = \mu_0 \frac{I_{\text{total}}}{2\pi R_1^2} r$$

Find the magnetic field for  $r < R_1$



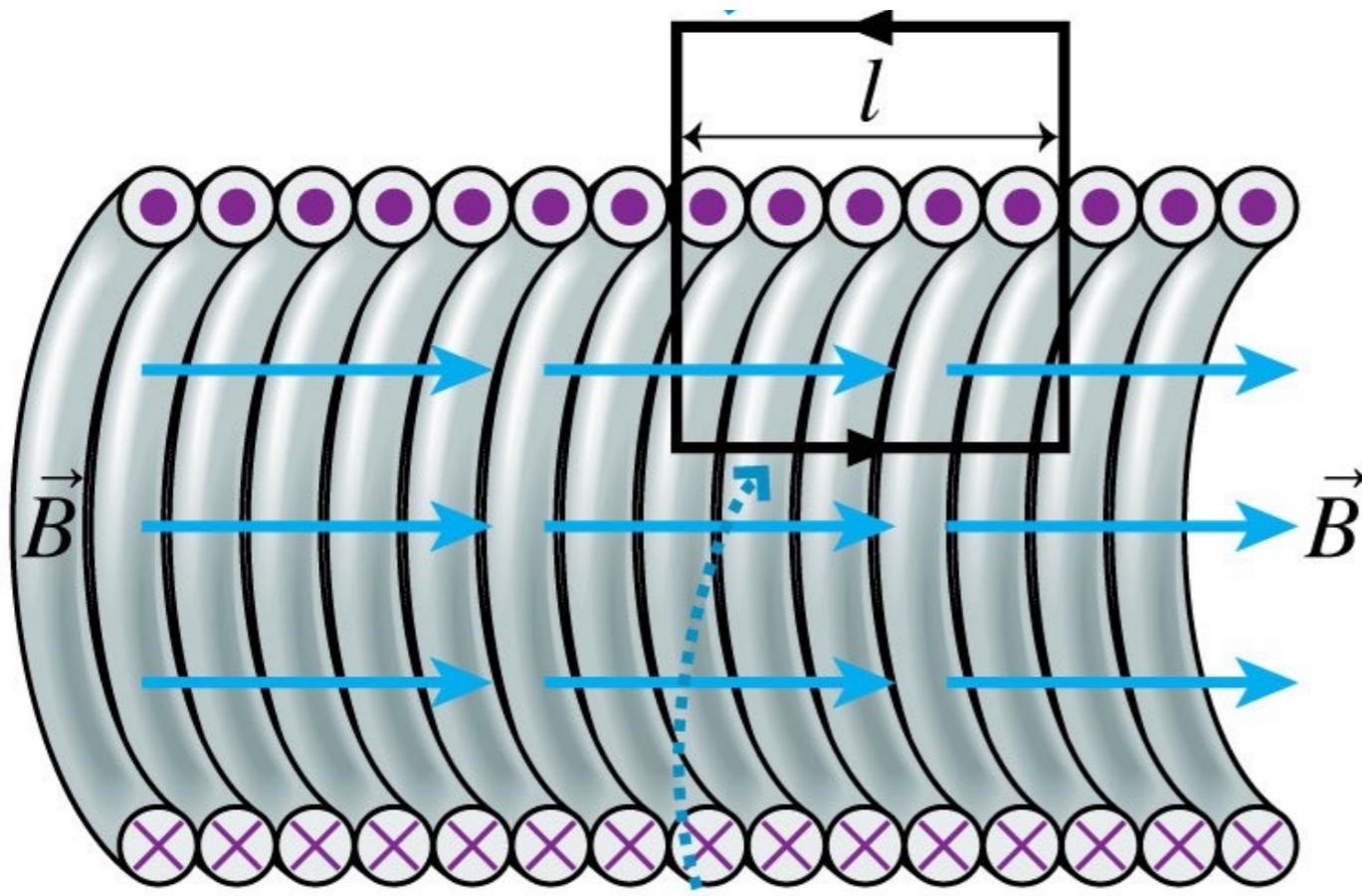
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# Let's use Ampere's law

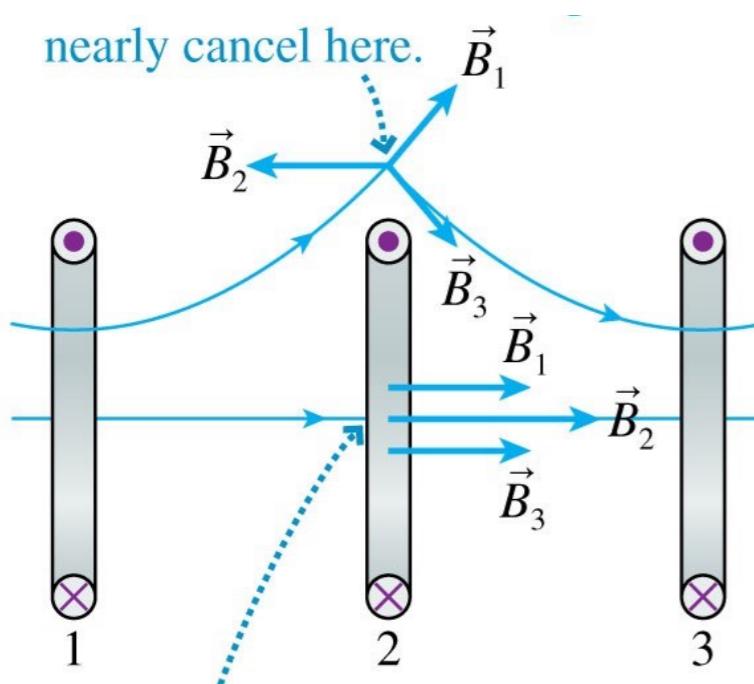


- a) What can you say about the  $B$  field along the path shown?
- b) Can you simplify the integral on the left hand side?
- c) How much current is flowing through this loop?

# Let's use Ampere's law

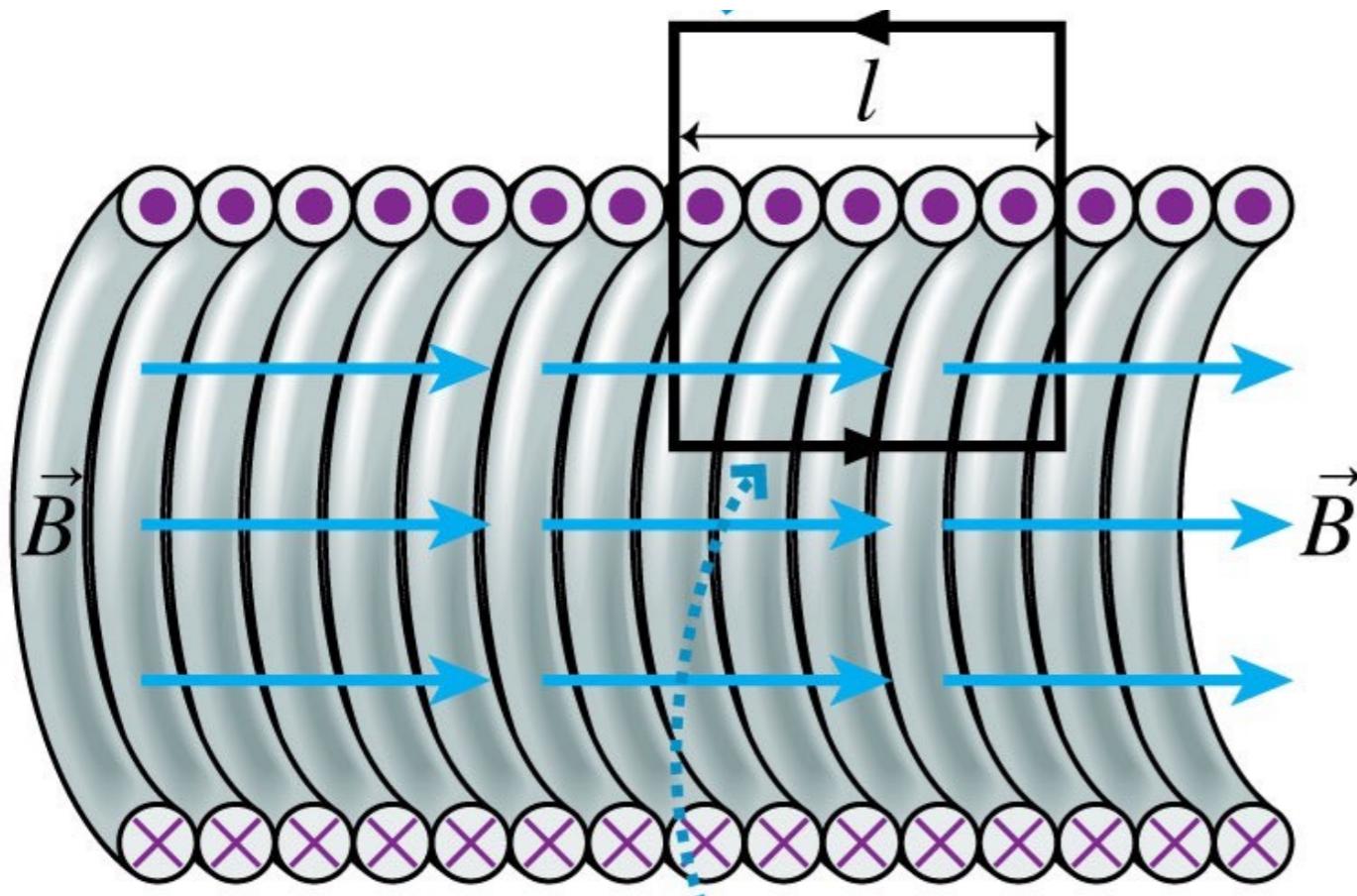


$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I$$

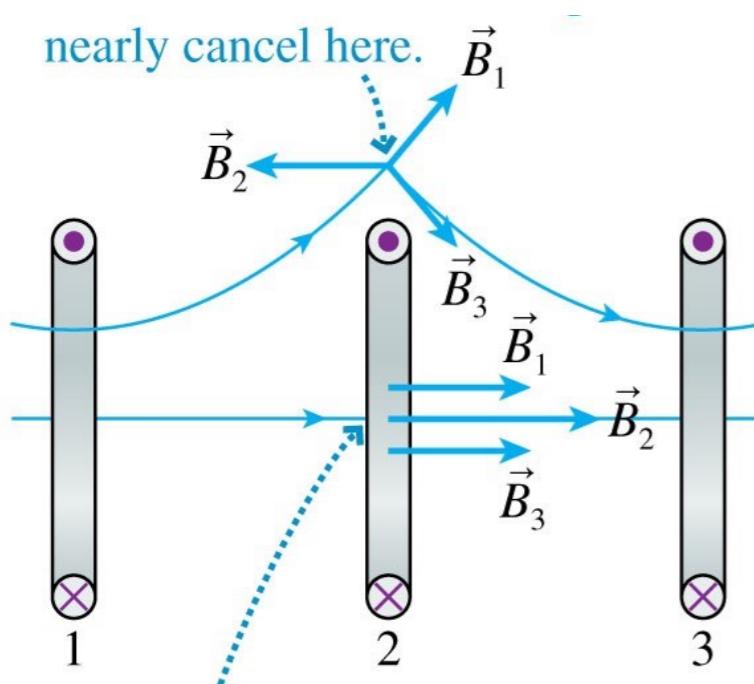


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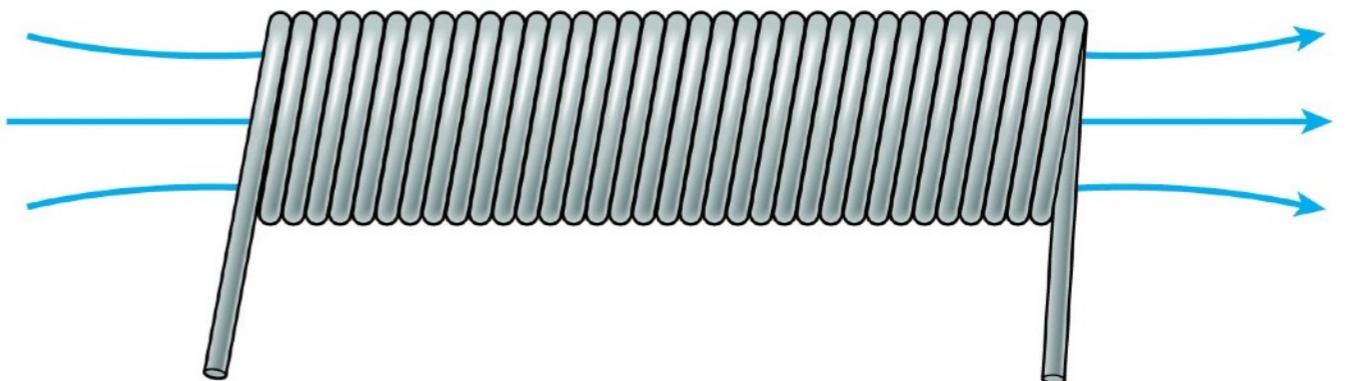
- What can you say about the  $B$  field along the path shown?
- Can you simplify the integral on the left hand side?
- How much current is flowing through this loop?

$$B = \frac{\mu_0 N I}{l} = \mu_0 n I$$

# Question #19

The current in this solenoid

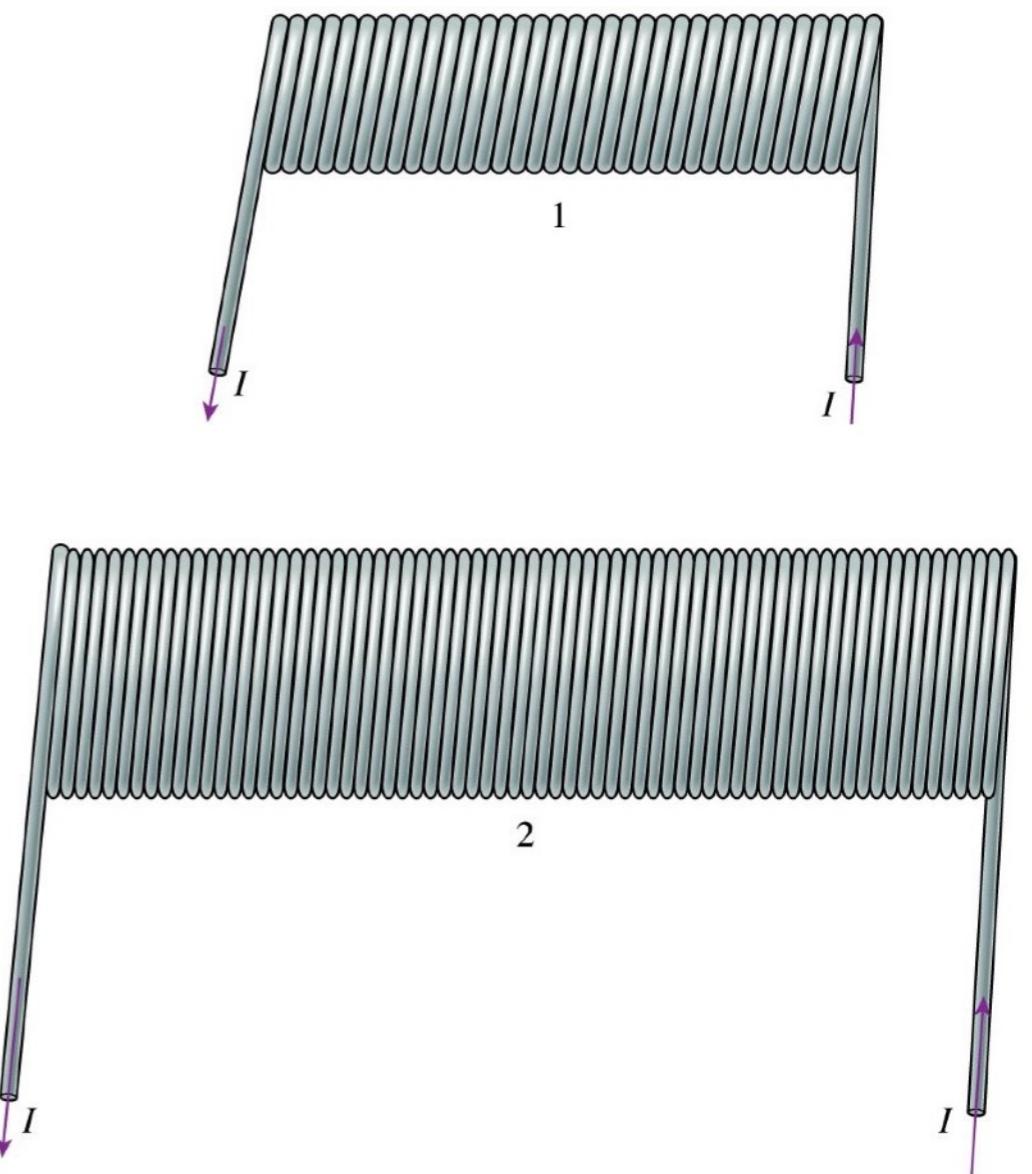
- A. Enters on the left, leaves on the right.
- B. Enters on the right, leaves on the left.
- C. Either A or B would produce this field.



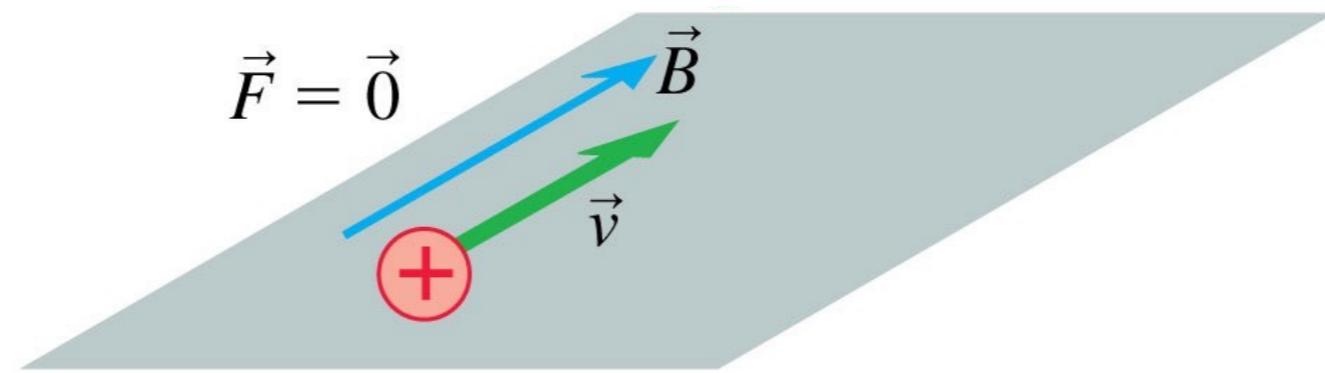
# Question #20

Solenoid 2 has twice the diameter, twice the length, and twice as many turns as solenoid 1. How does the field  $B_2$  at the center of solenoid 2 compare to  $B_1$  at the center of solenoid 1?

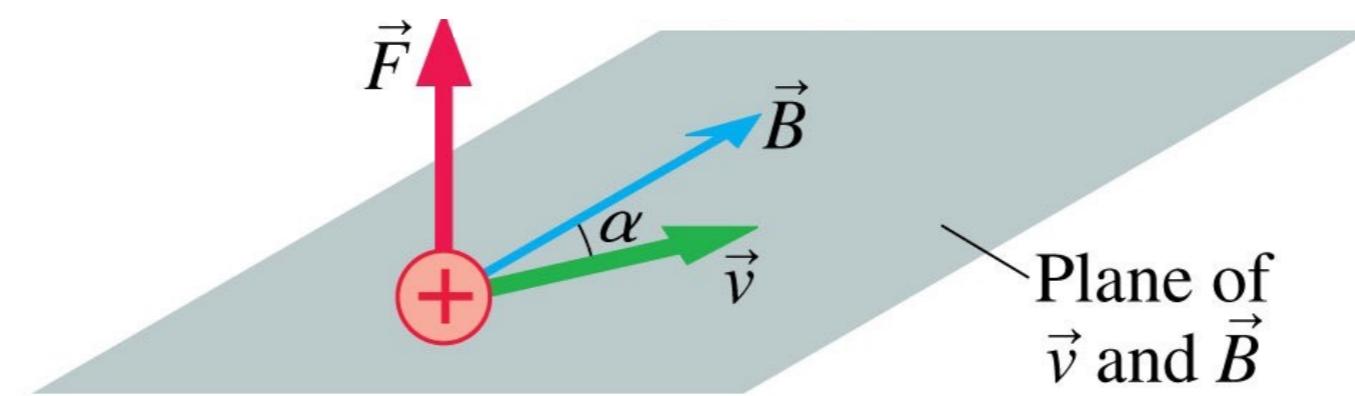
- A.  $B_2 = B_1/4.$
- B.  $B_2 = B_1/2.$
- C.  $B_2 = 2B_1.$
- D.  $B_2 = B_1.$
- E.  $B_2 = 4B_1.$



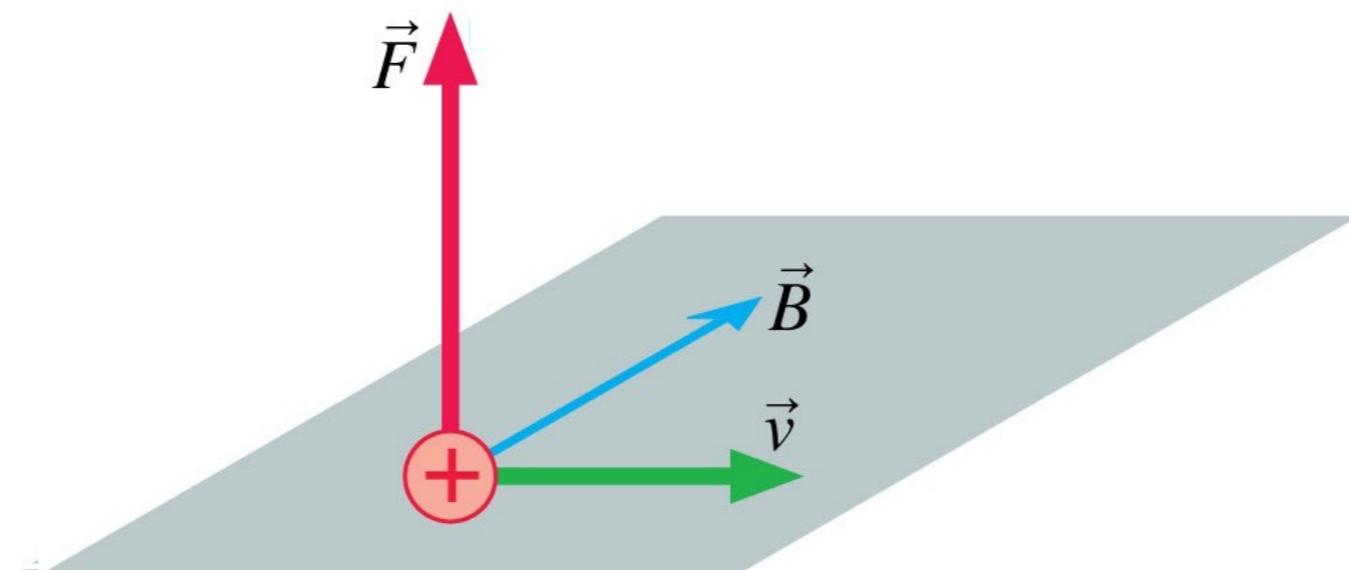
# Magnetic force on moving charge



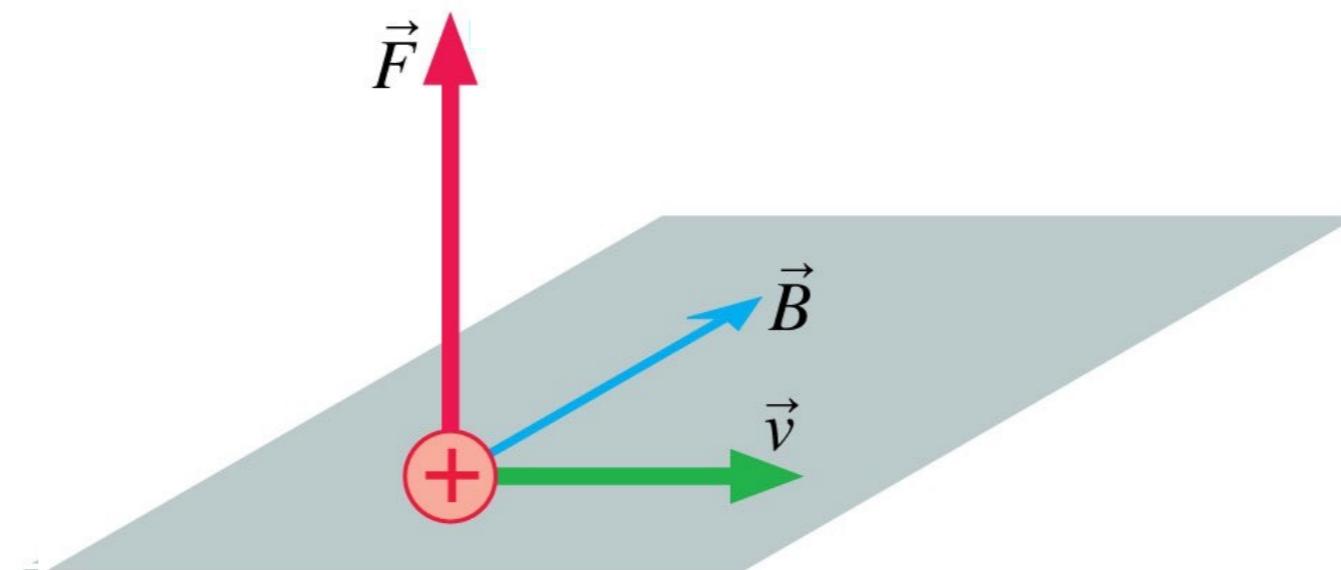
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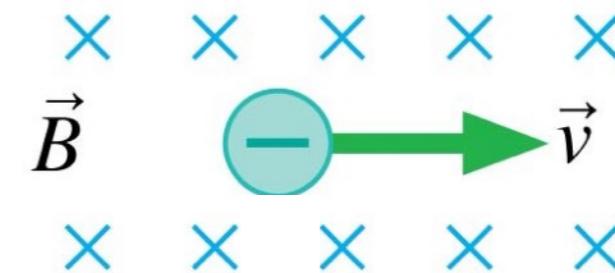
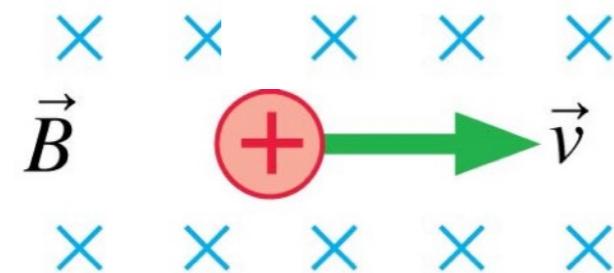
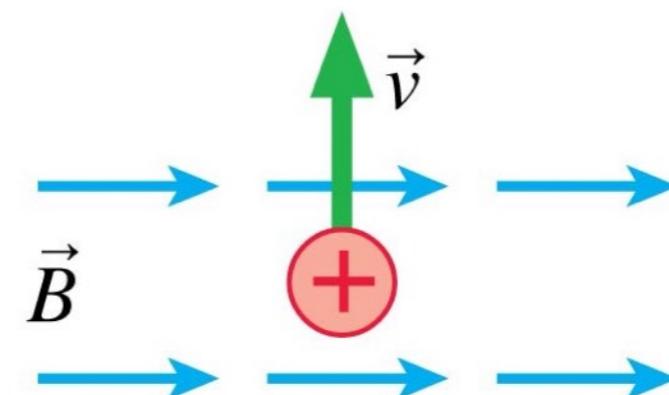
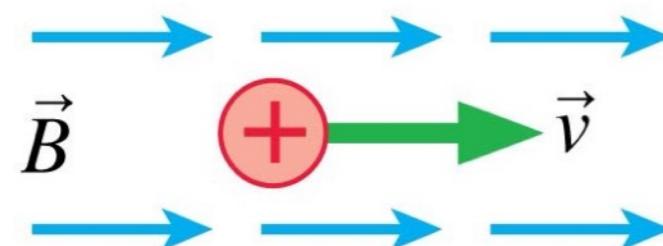


# Magnetic force on moving charge

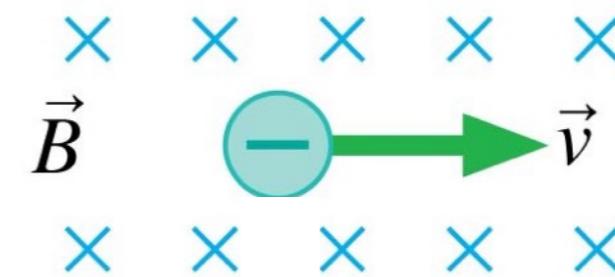
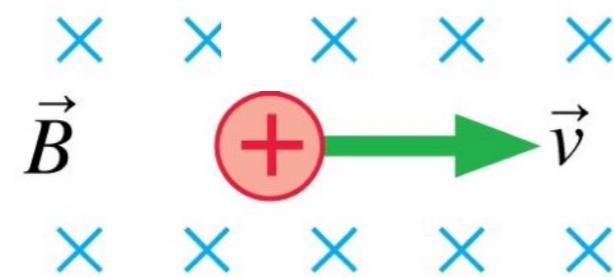
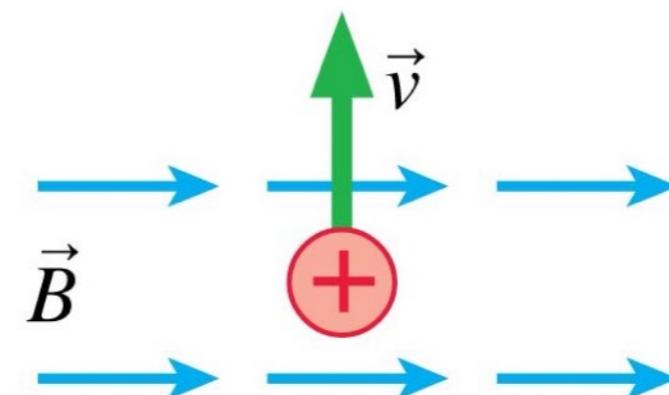
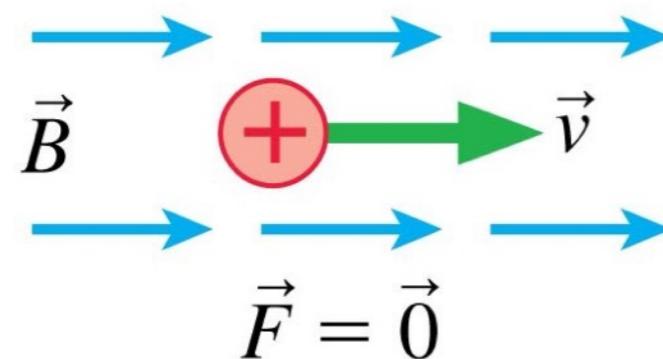


$$\vec{F} = q\vec{v} \times \vec{B}$$

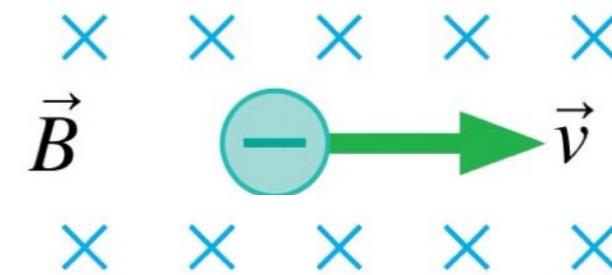
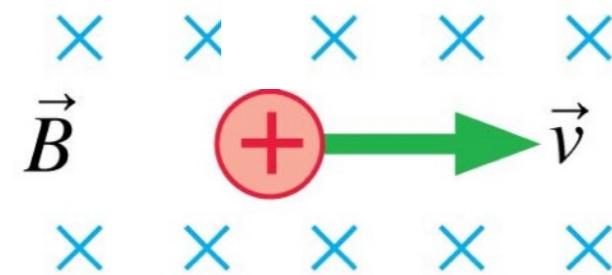
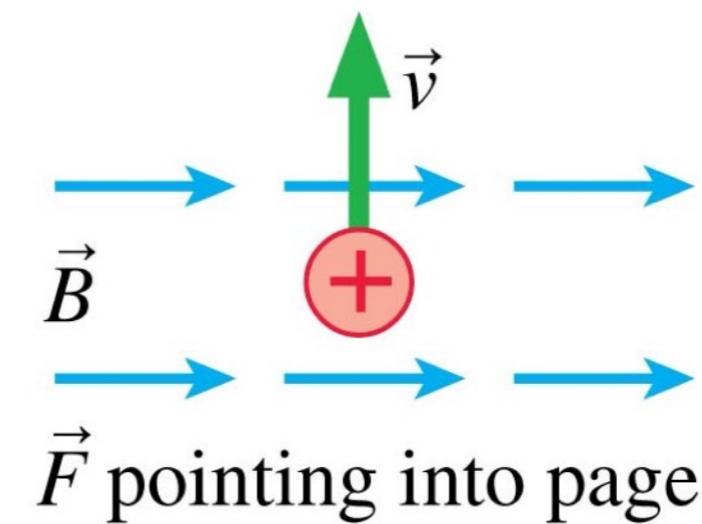
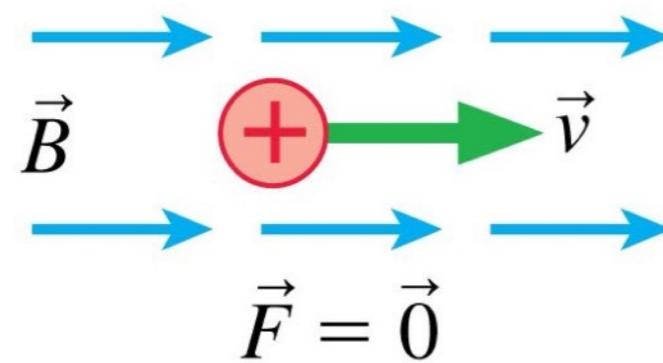
Tell your neighbor what the direction of the magnetic force is



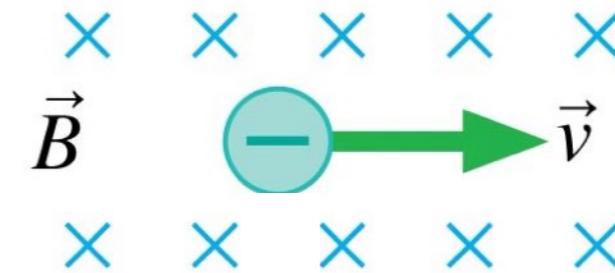
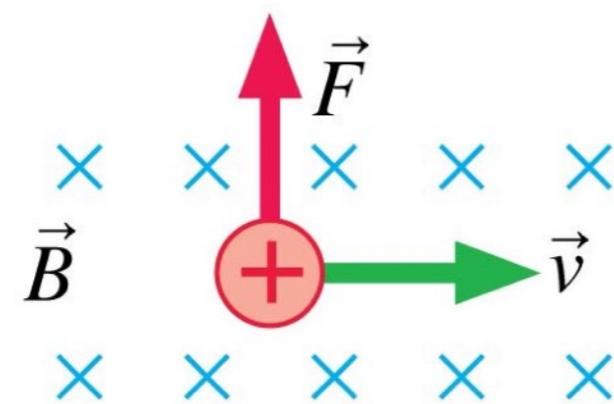
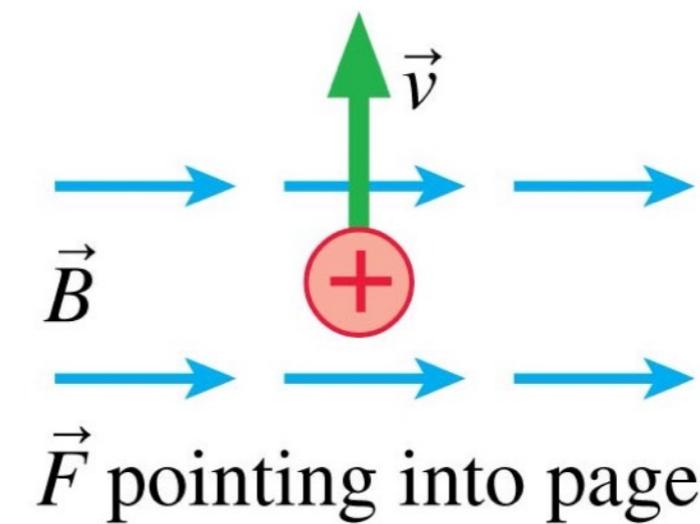
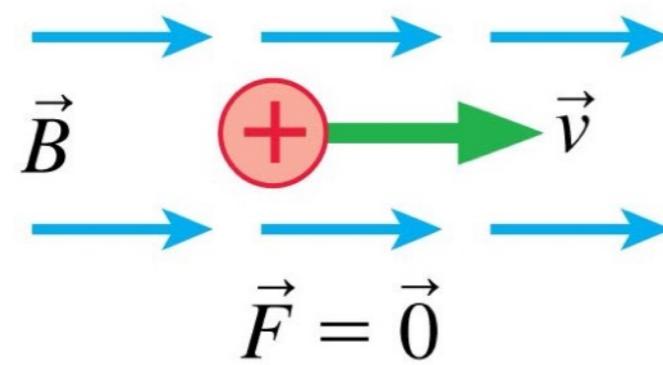
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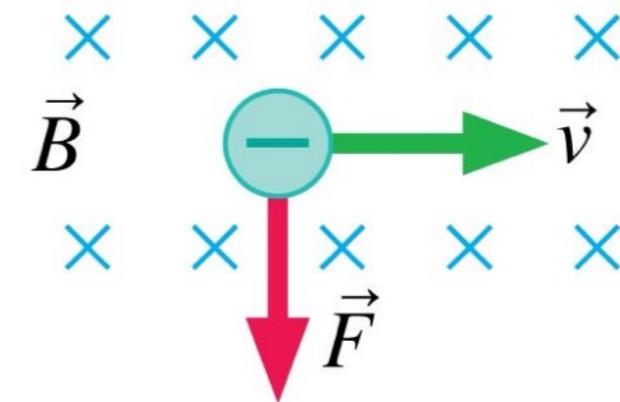
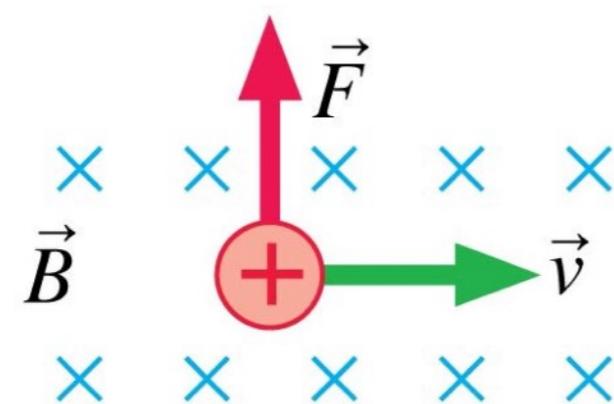
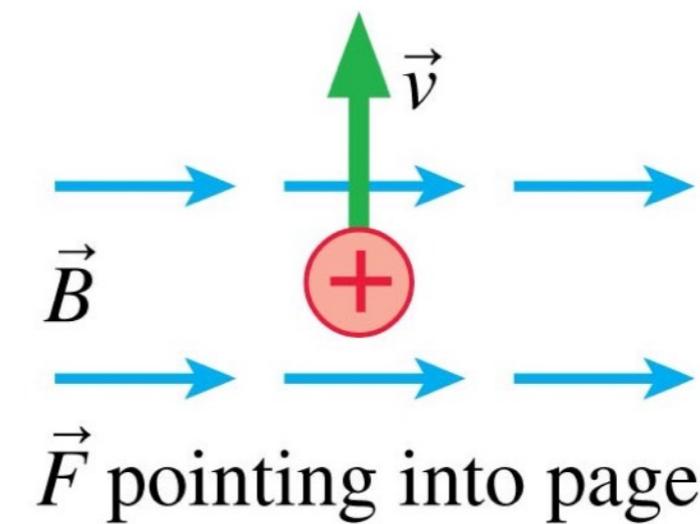
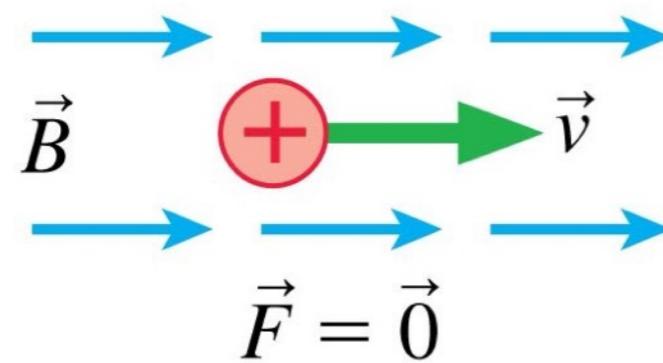
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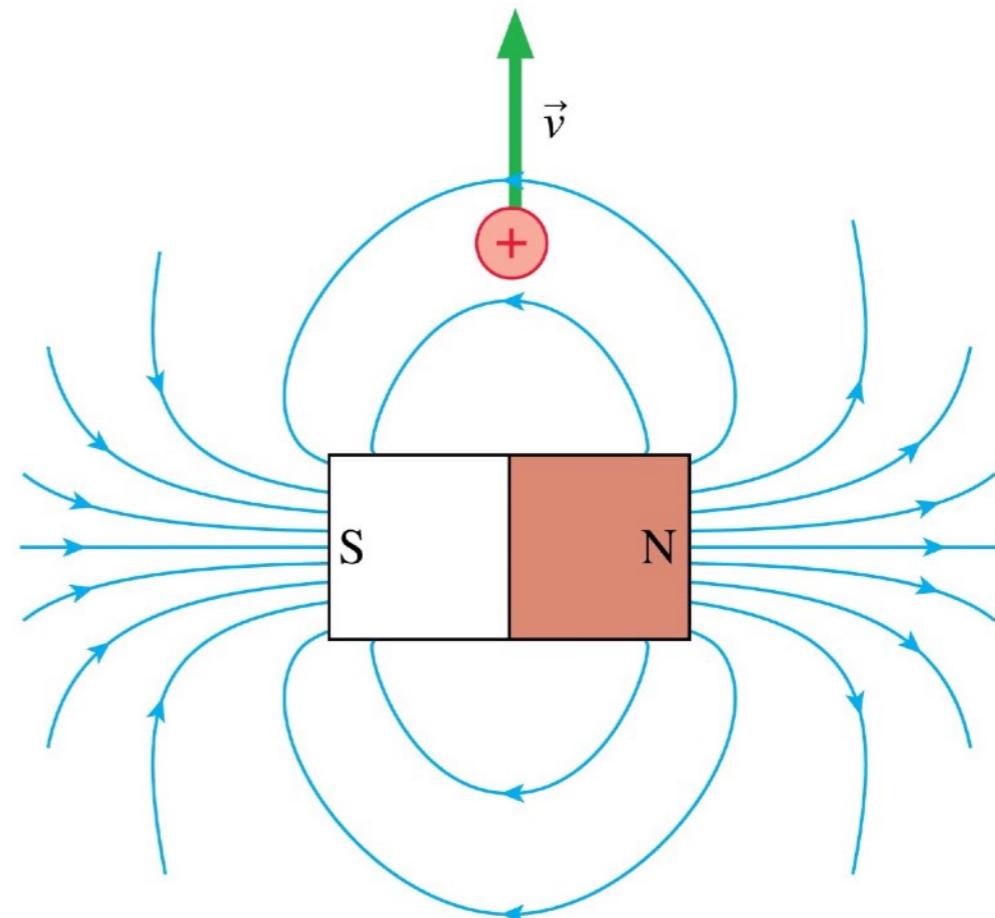
Tell your neighbor what the direction of the magnetic force is



# Question #21

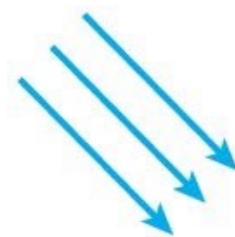
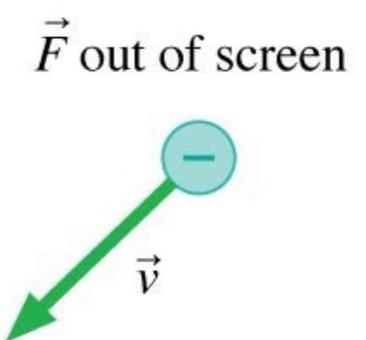
The direction of the magnetic force on the proton is

- A. Out of the screen.
- B. To the left.
- C. Into the screen.
- D. To the right.
- E. The magnetic force is zero.

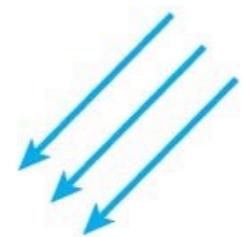


# Question #22

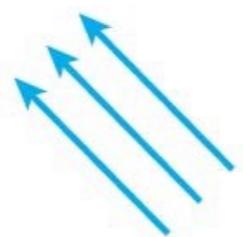
Which magnetic field causes the observed force?



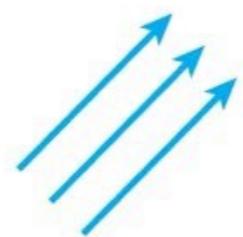
E



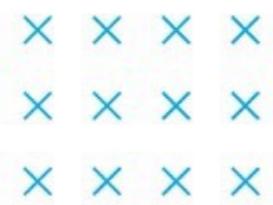
B



A



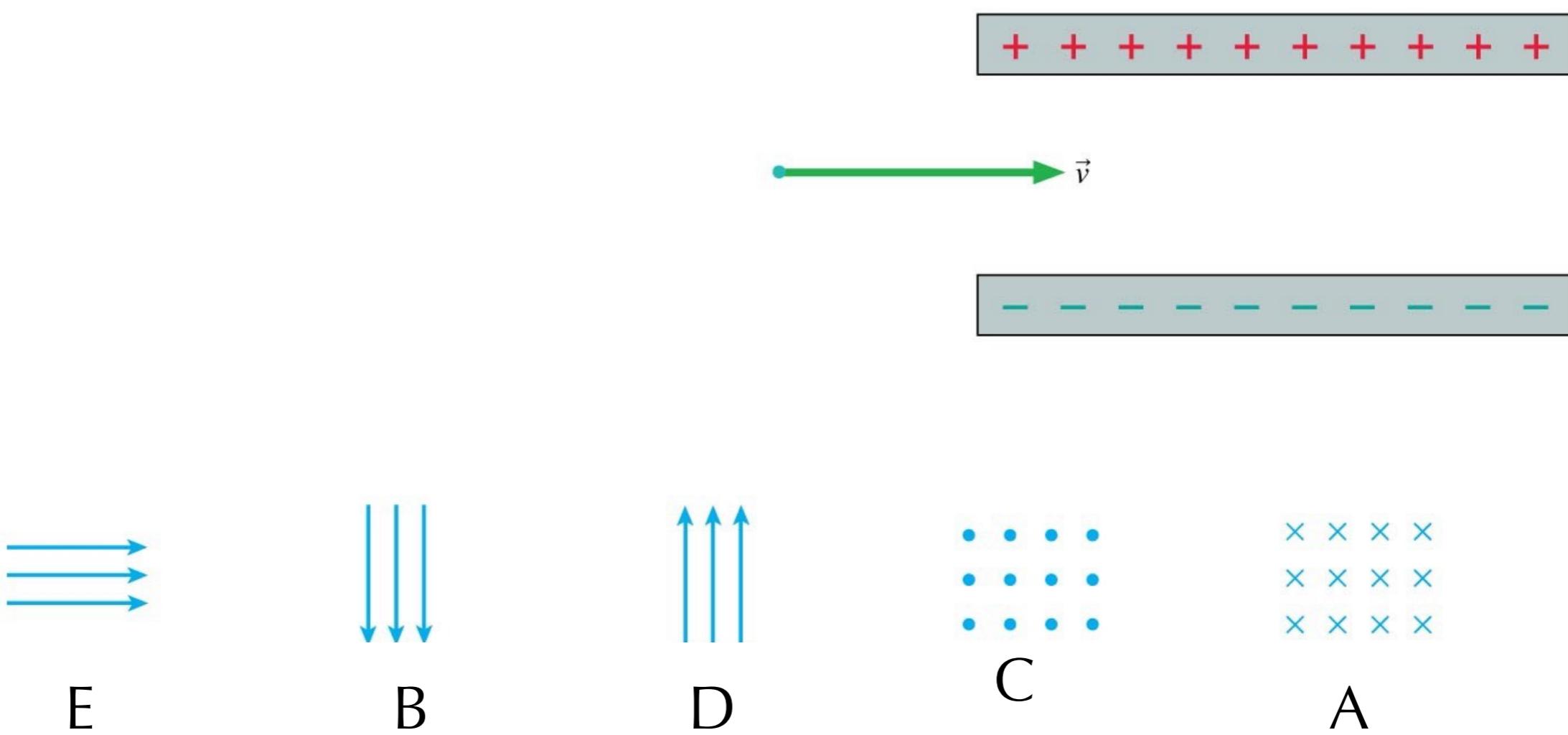
C



D

# Question #23

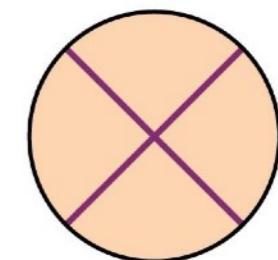
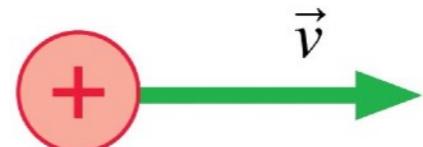
Which magnetic field (if it's the correct strength) allows the electron to pass through the charged electrodes without being deflected?



# Question #24

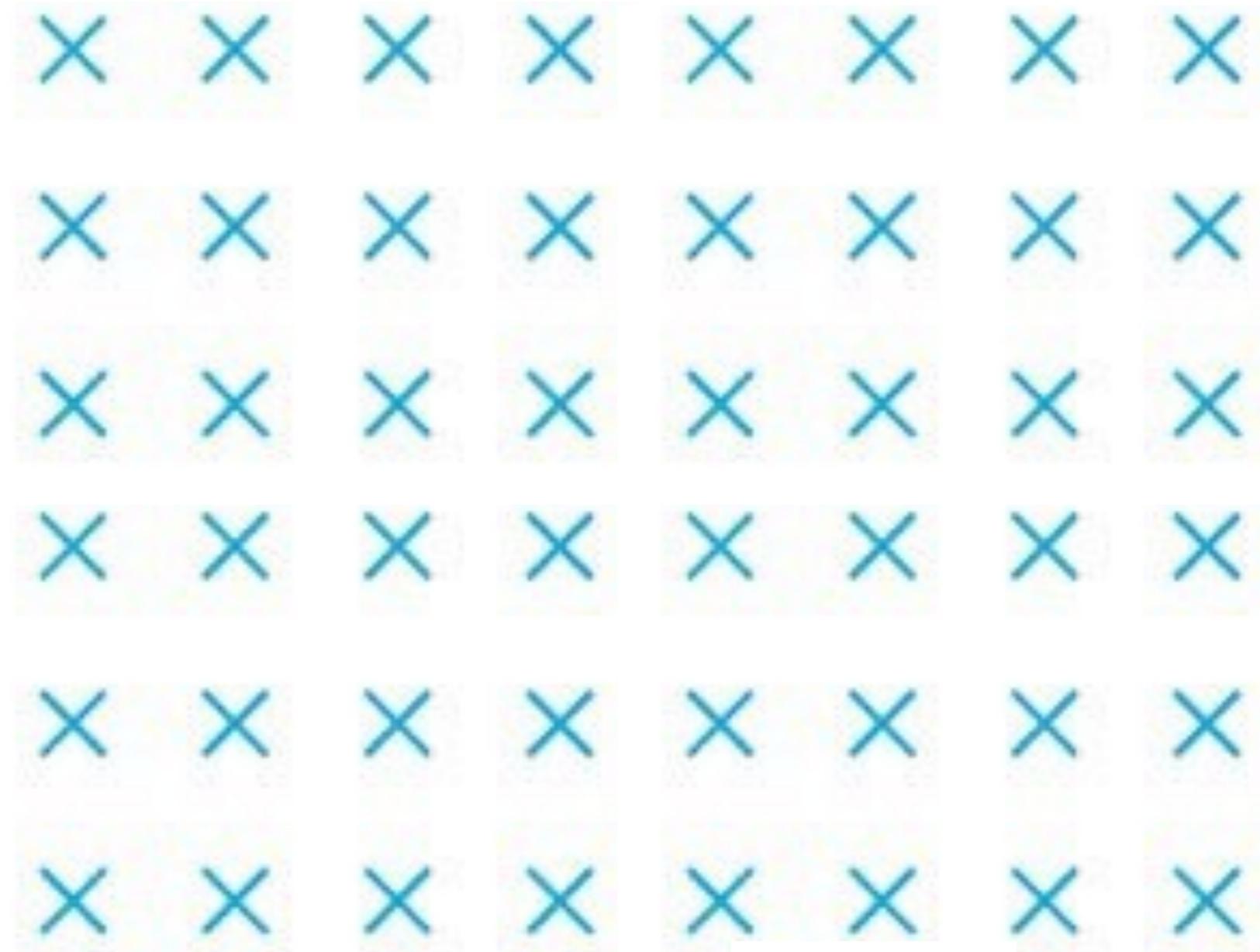
A proton is shot straight at the center of a long, straight wire carrying current into the screen. The proton will

- A. Go straight into the wire.
- B. Hit the wire in front of the screen.
- C. Hit the wire behind the screen.
- D. Be deflected over the wire.
- E. Be deflected under the wire.

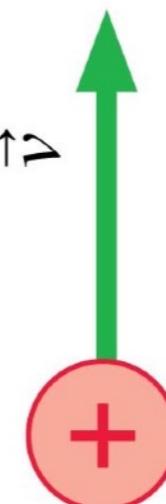


Long wire into screen

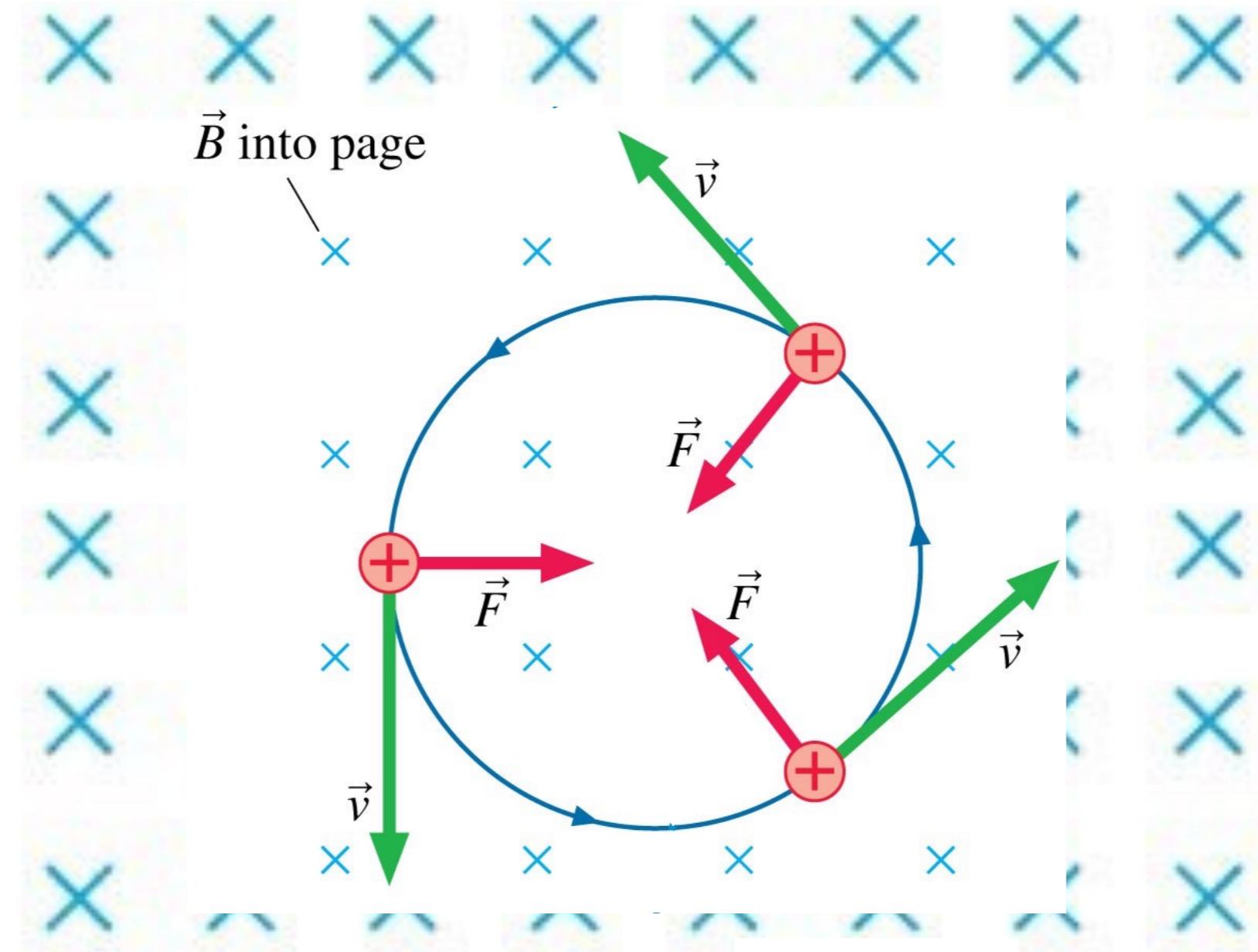
# Cyclotron



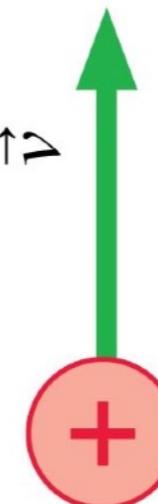
What will the motion of  
the particle be after  
entering the field?



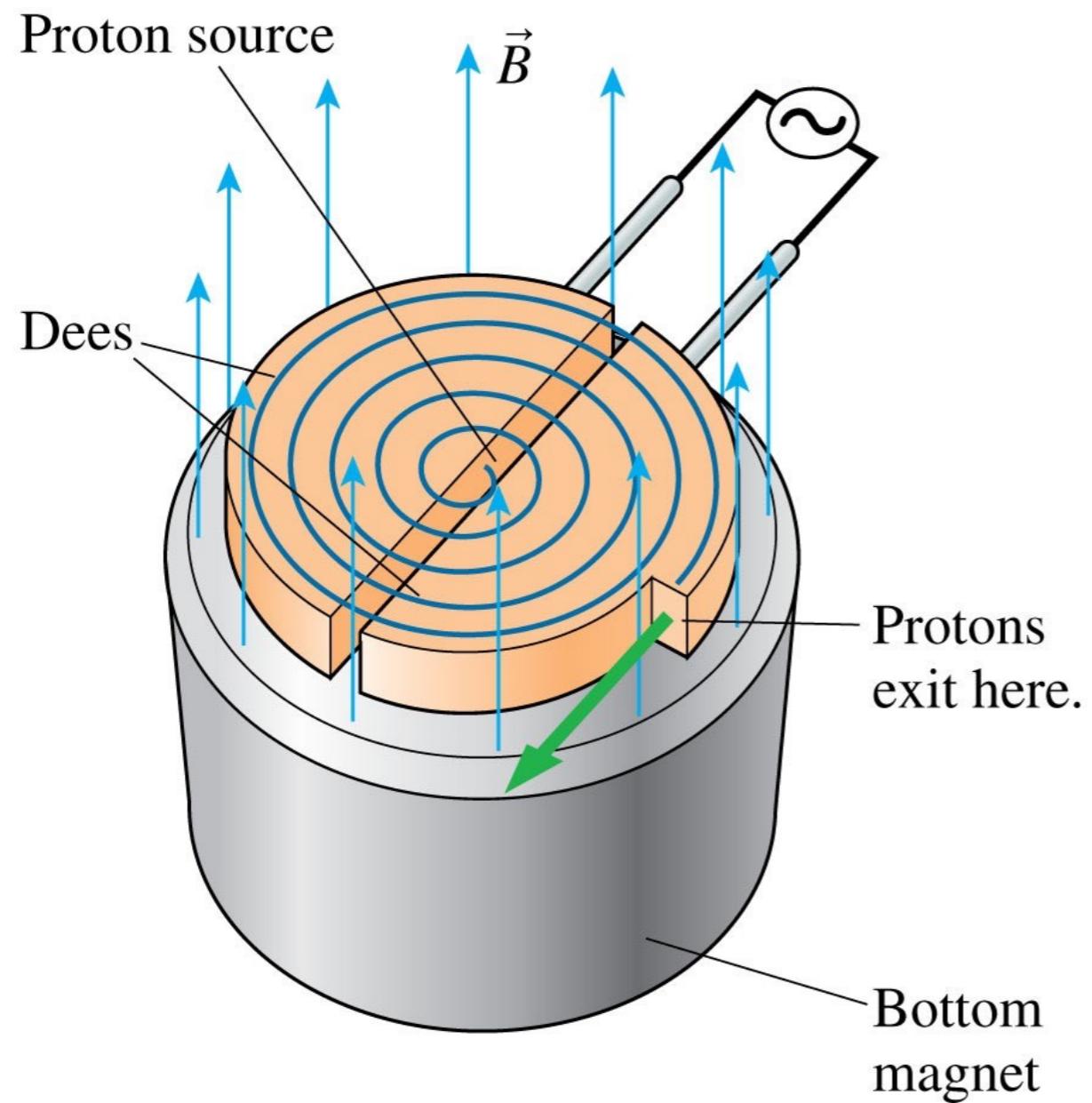
# Cyclotron

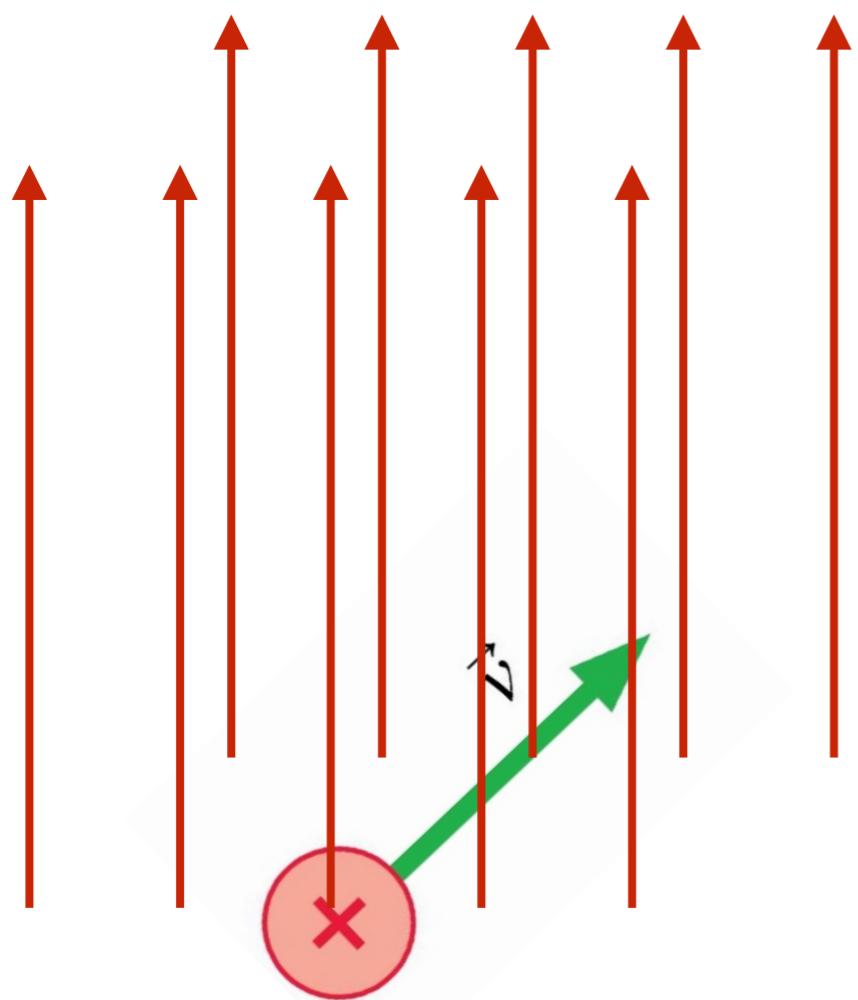


What will the motion of  
the particle be after  
entering the field?



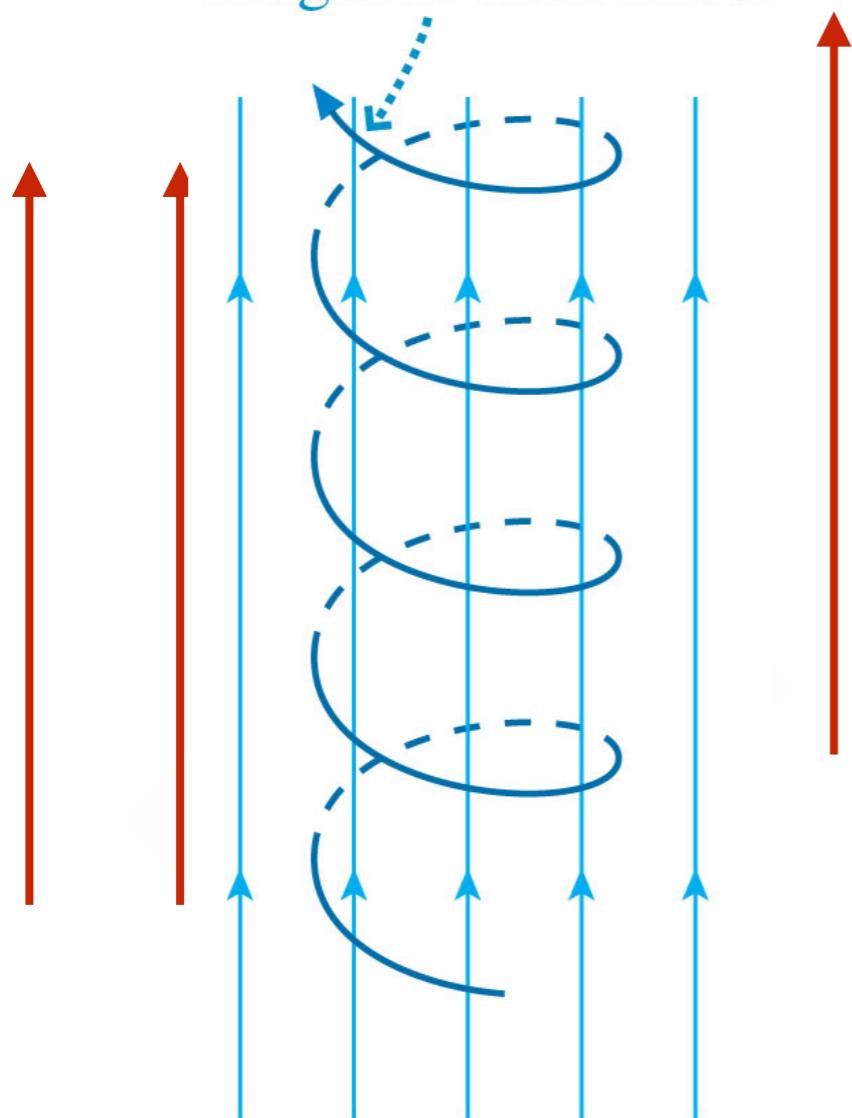
# Cyclotron





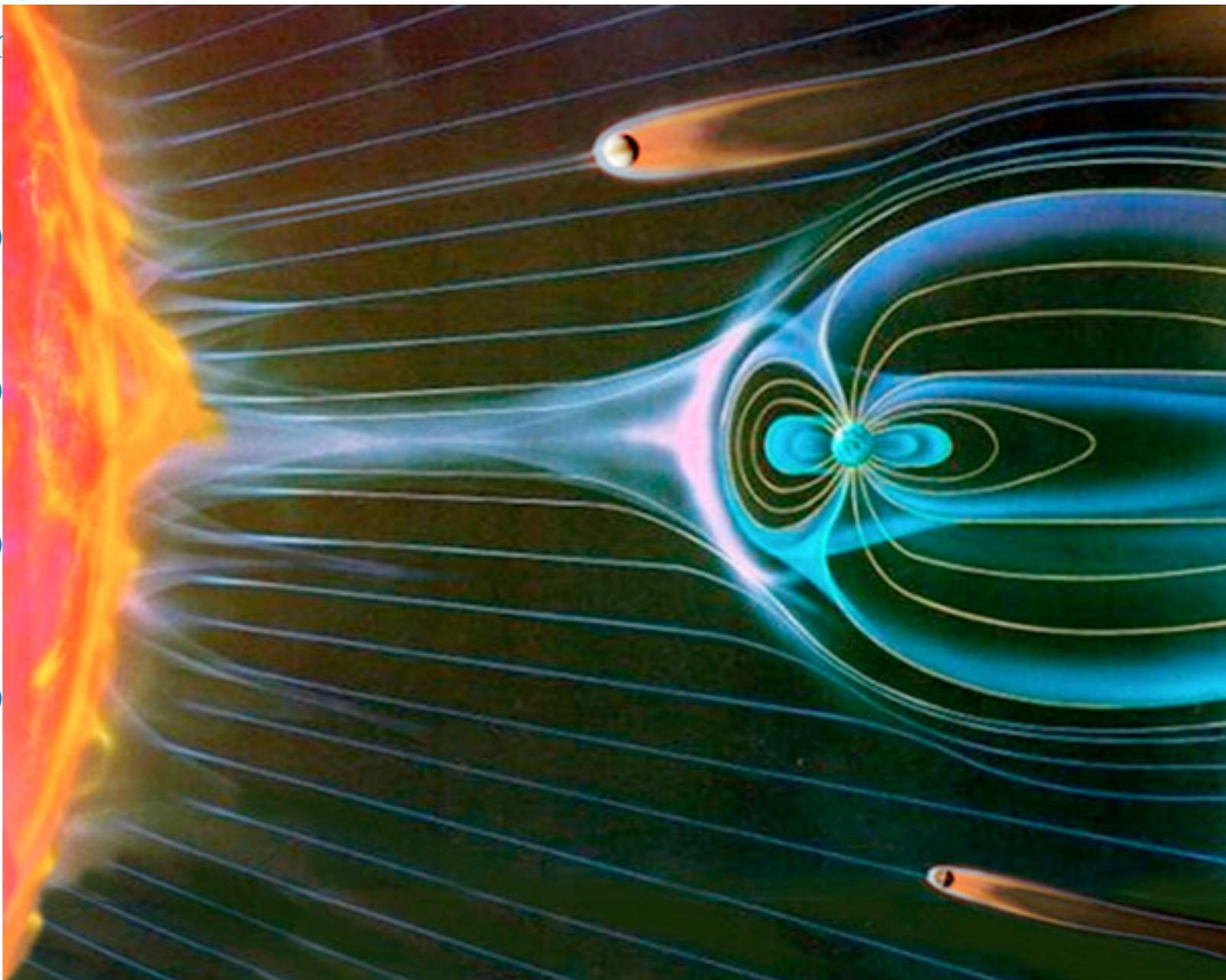
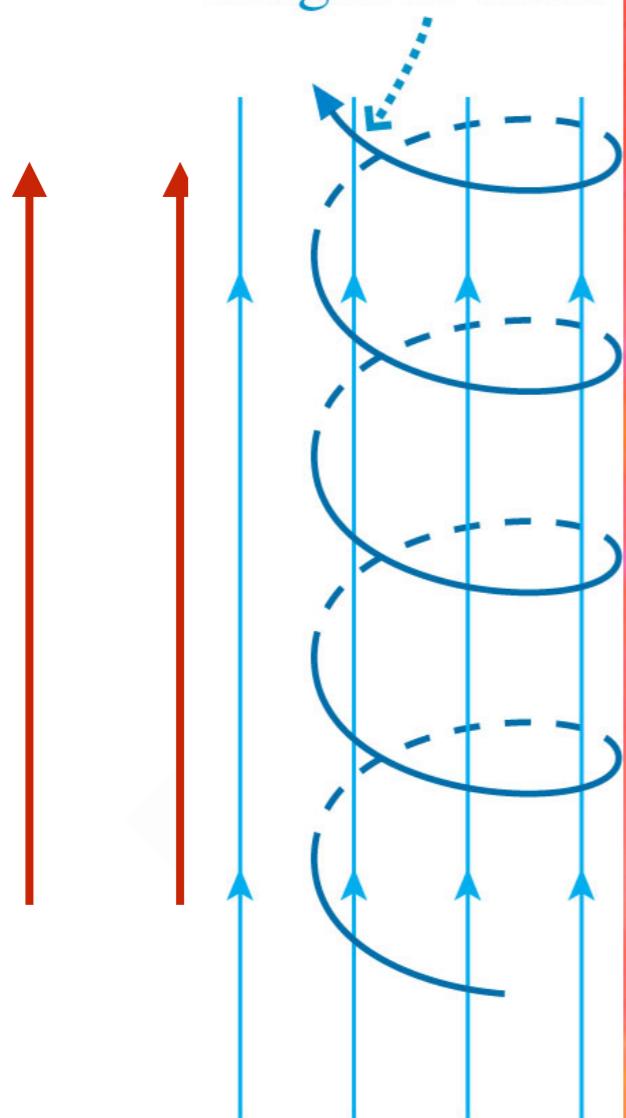
If I now give the proton a component of velocity in the z direction, what will the motion look like?

Charged particles spiral around the magnetic field lines.

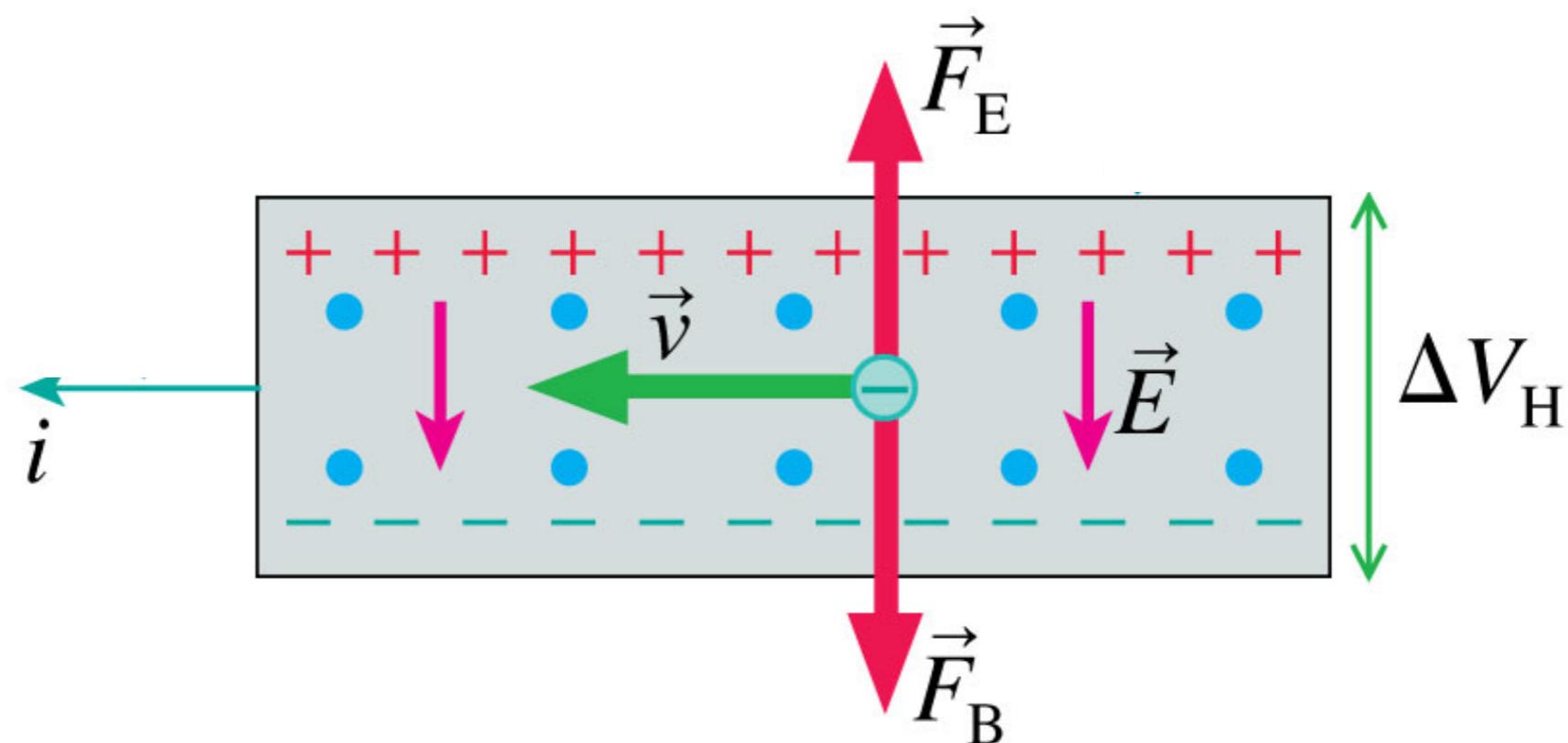


If I now give the proton a component of velocity in the z direction, what will the motion look like?

Charged particles  
spiral around the  
magnetic field



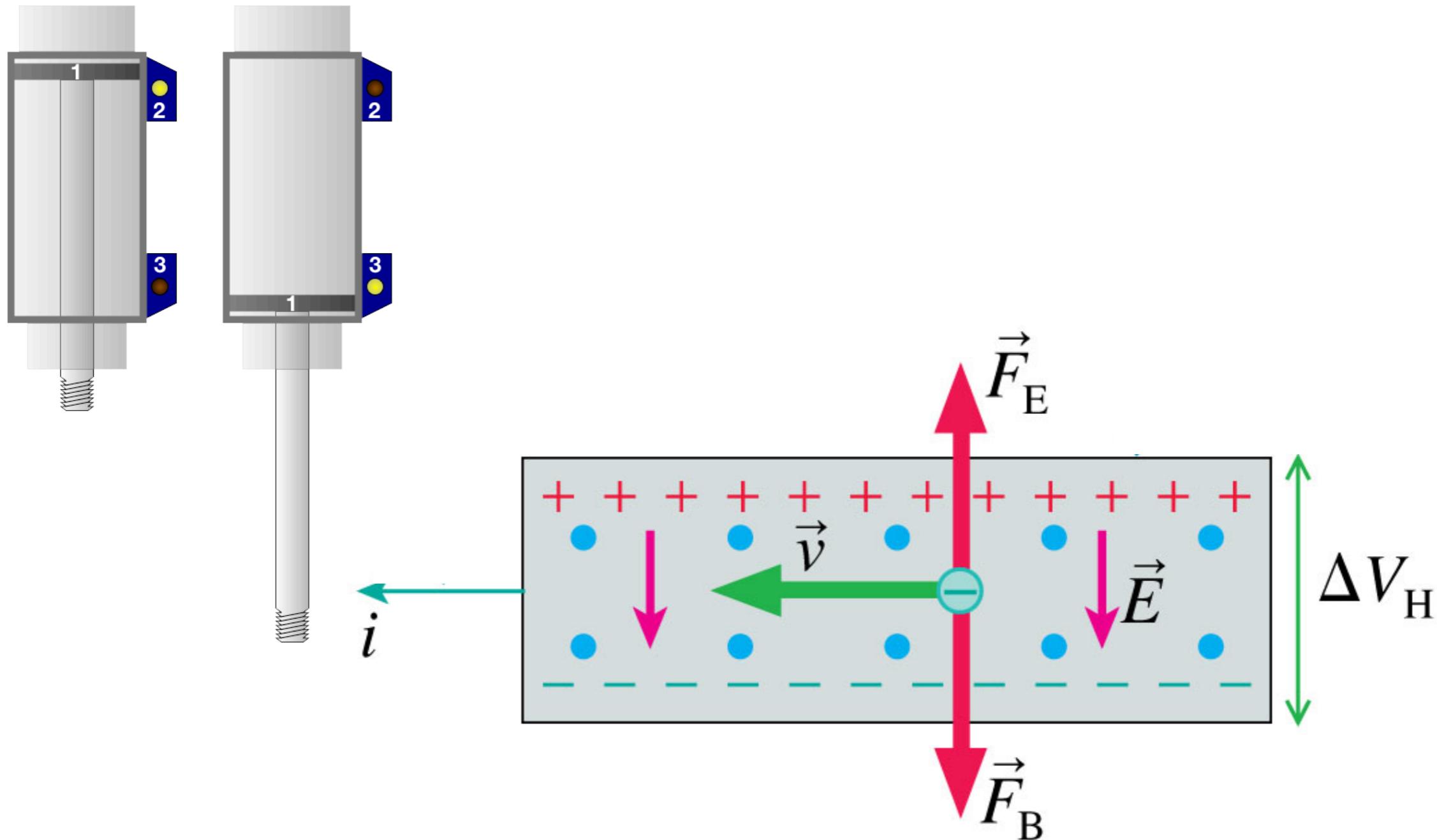
# The Hall Effect



video demo

$$\Delta V_H = \frac{IB}{tne}$$

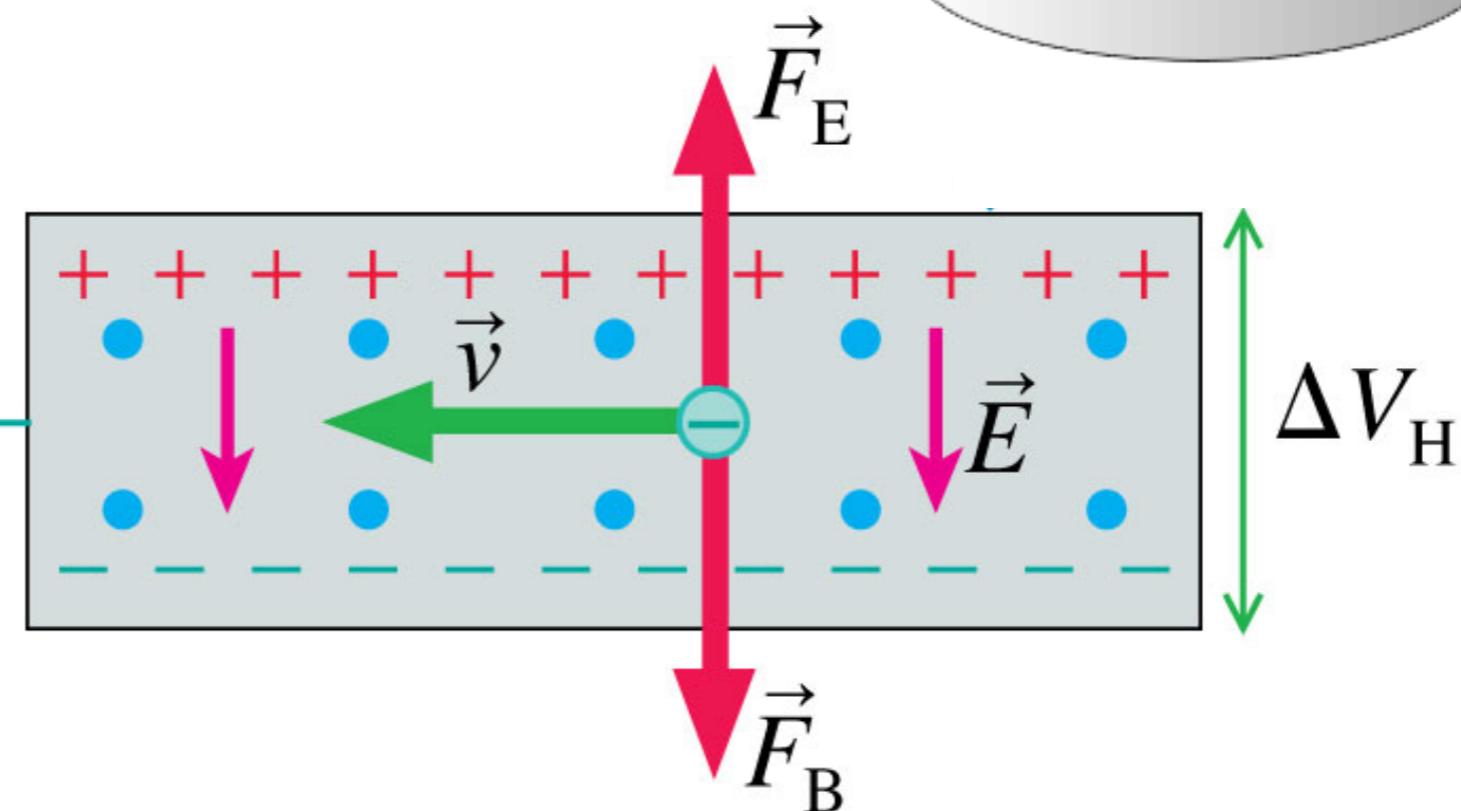
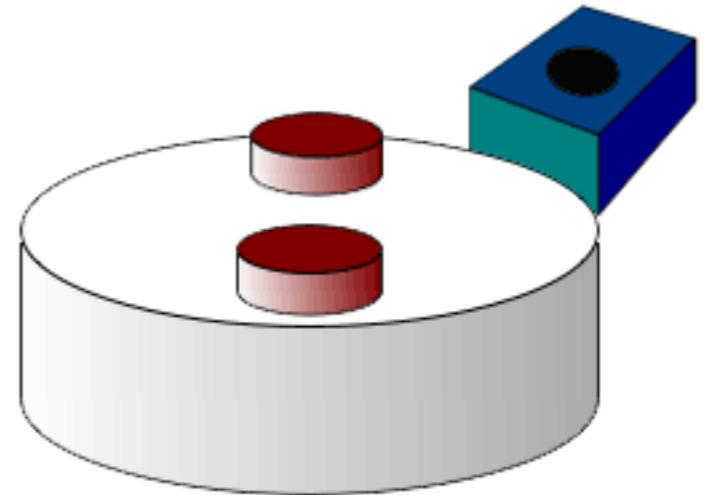
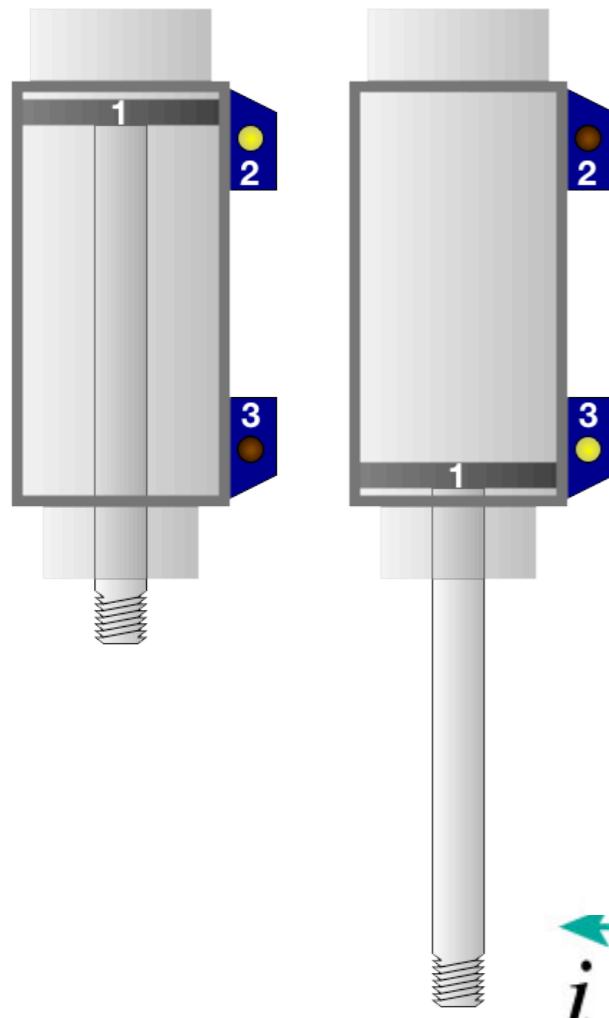
# The Hall Effect



video demo

$$\Delta V_H = \frac{IB}{tne}$$

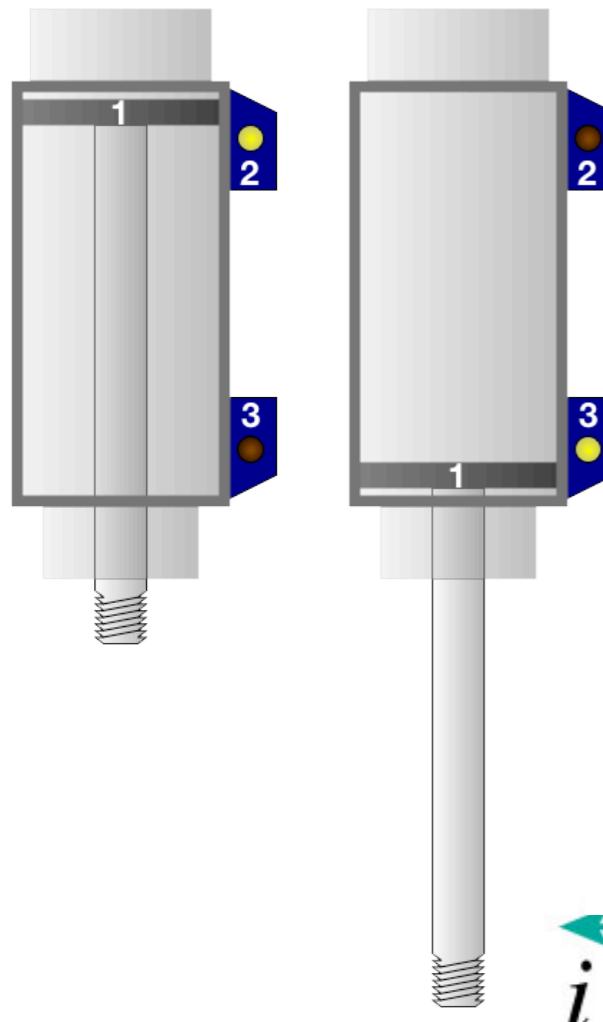
# The Hall Effect



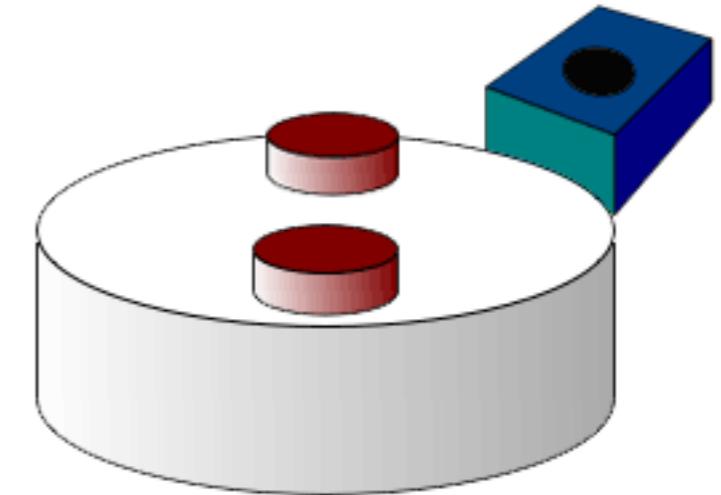
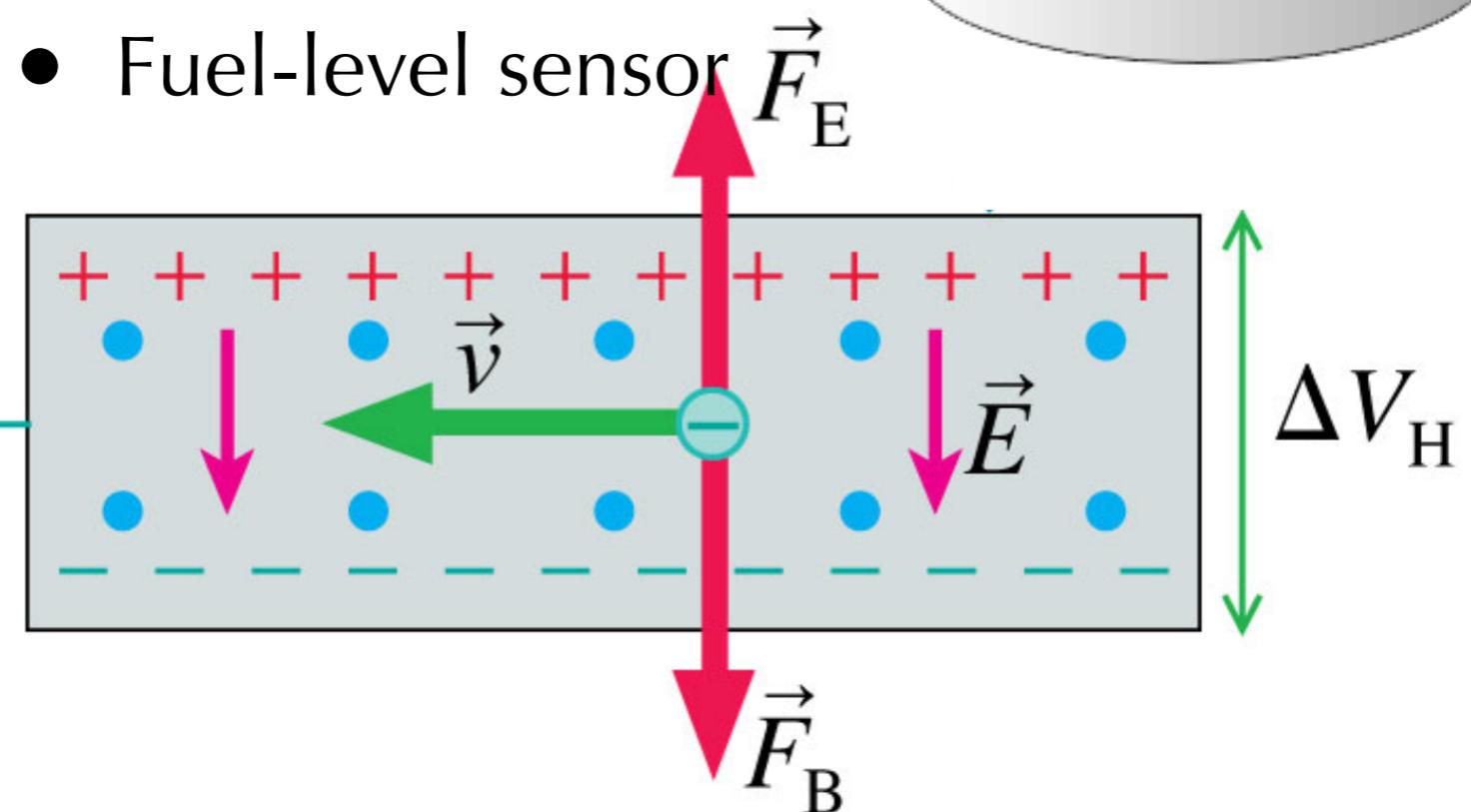
video demo

$$\Delta V_H = \frac{IB}{tne}$$

# The Hall Effect



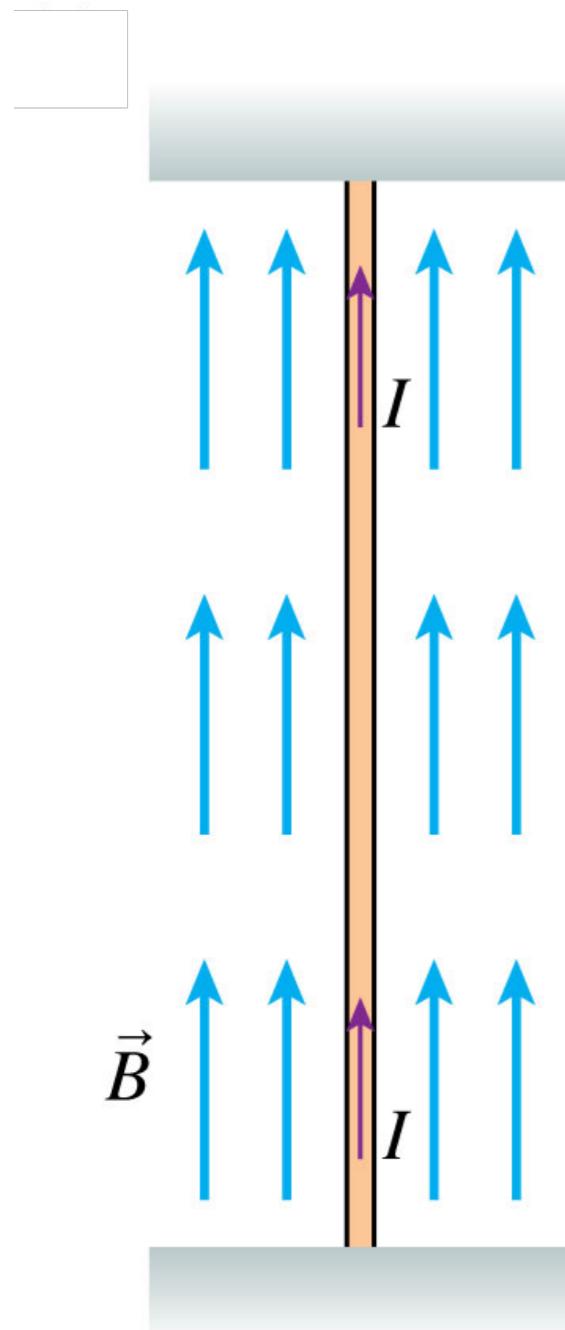
- Proximity Sensing
- Positioning
- Speed Detection
- Current Sensing
- Fuel-level sensor



video demo

$$\Delta V_H = \frac{IB}{tne}$$

# Magnetic force on current



Demo!

$$\vec{F} = I\vec{l} \times \vec{B}$$

# Force on two current-carrying wires

1



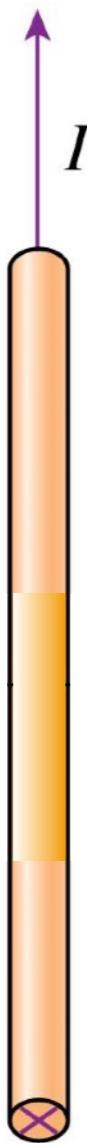
2



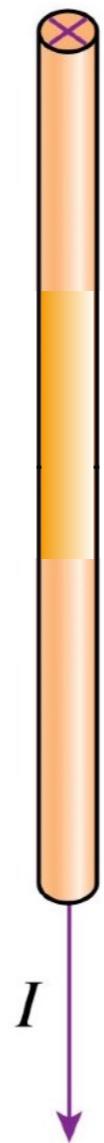
What is the direction of the force exerted by wire 1 onto wire 2?

# Force on two current-carrying wires

1



2



What is the direction of the force exerted by wire 1 onto wire 2?

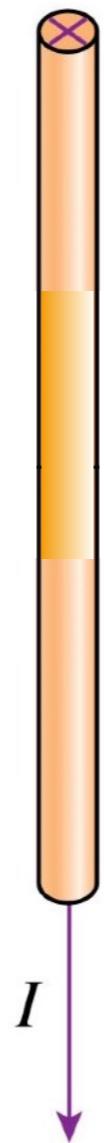
What about now?

# Force on two current-carrying wires

1



2



What is the direction of the force exerted by wire 1 onto wire 2?

What about now?

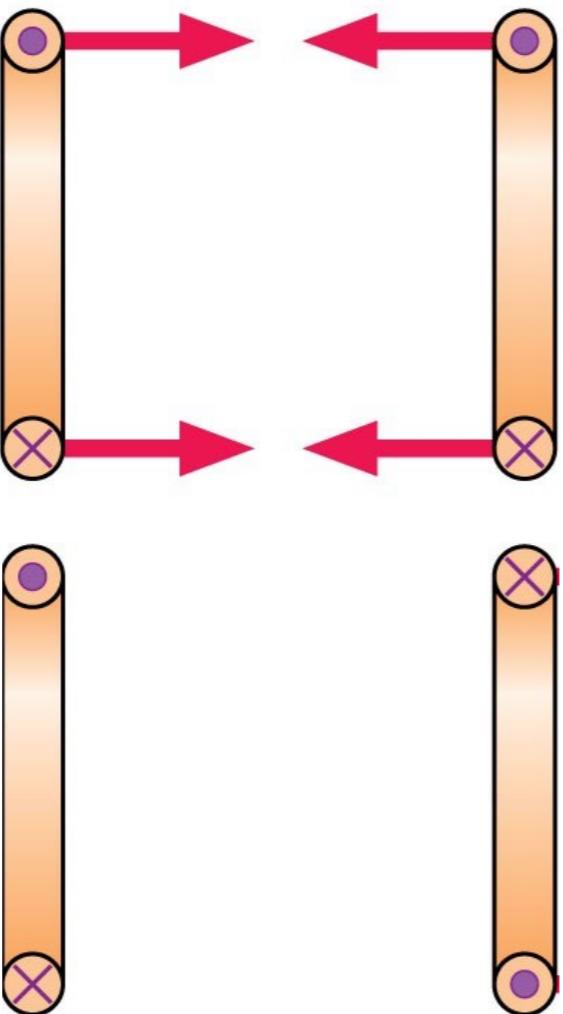
$$F = I_1 l B_2 = I_1 l \frac{\mu_0 I_2}{2\pi d}$$

# Force on current loops



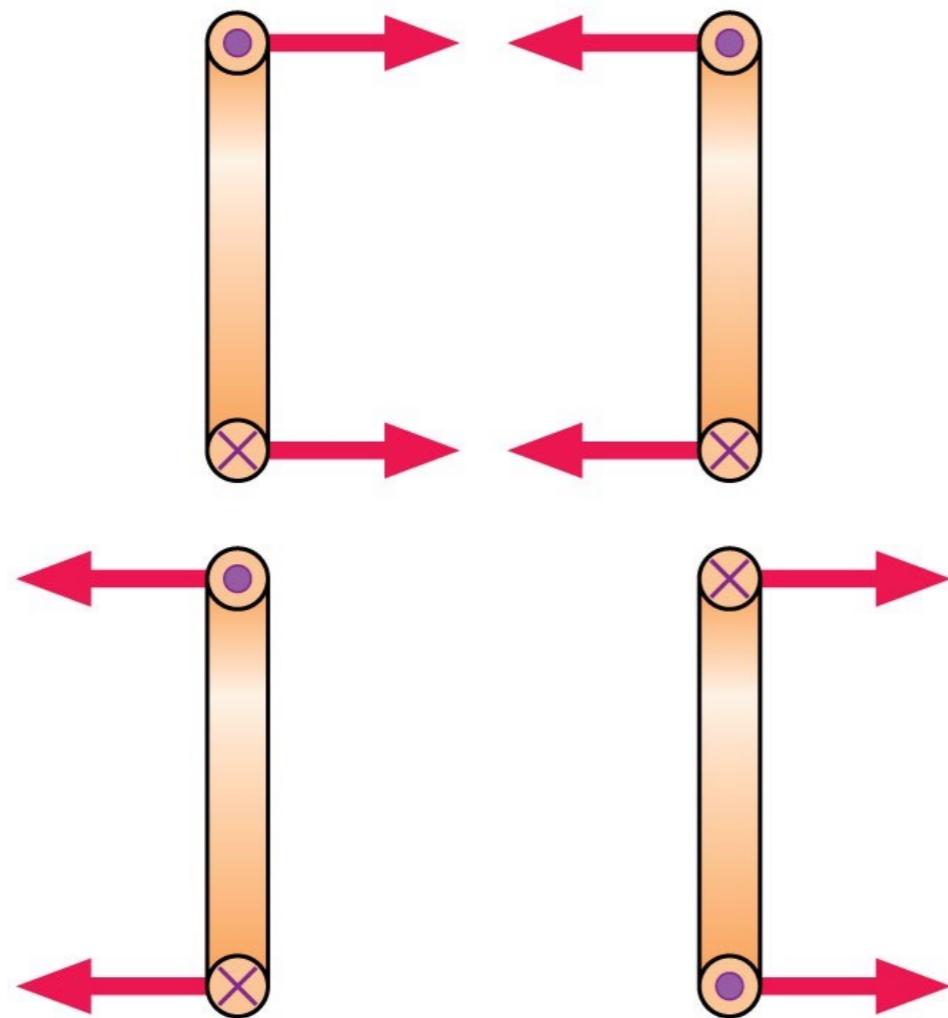
What are the forces on  
these current loops?

# Force on current loops



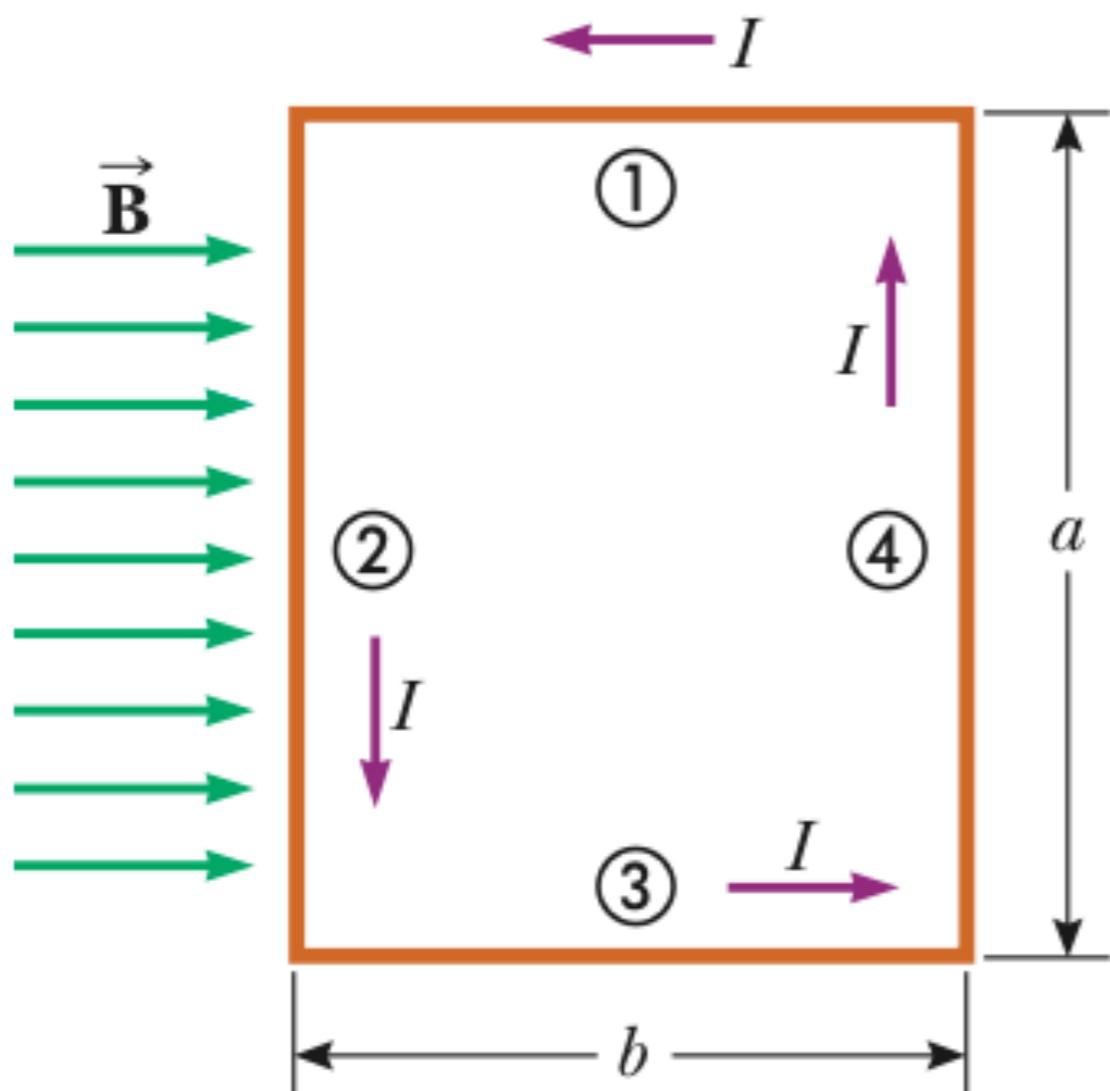
What are the forces on  
these current loops?

# Force on current loops



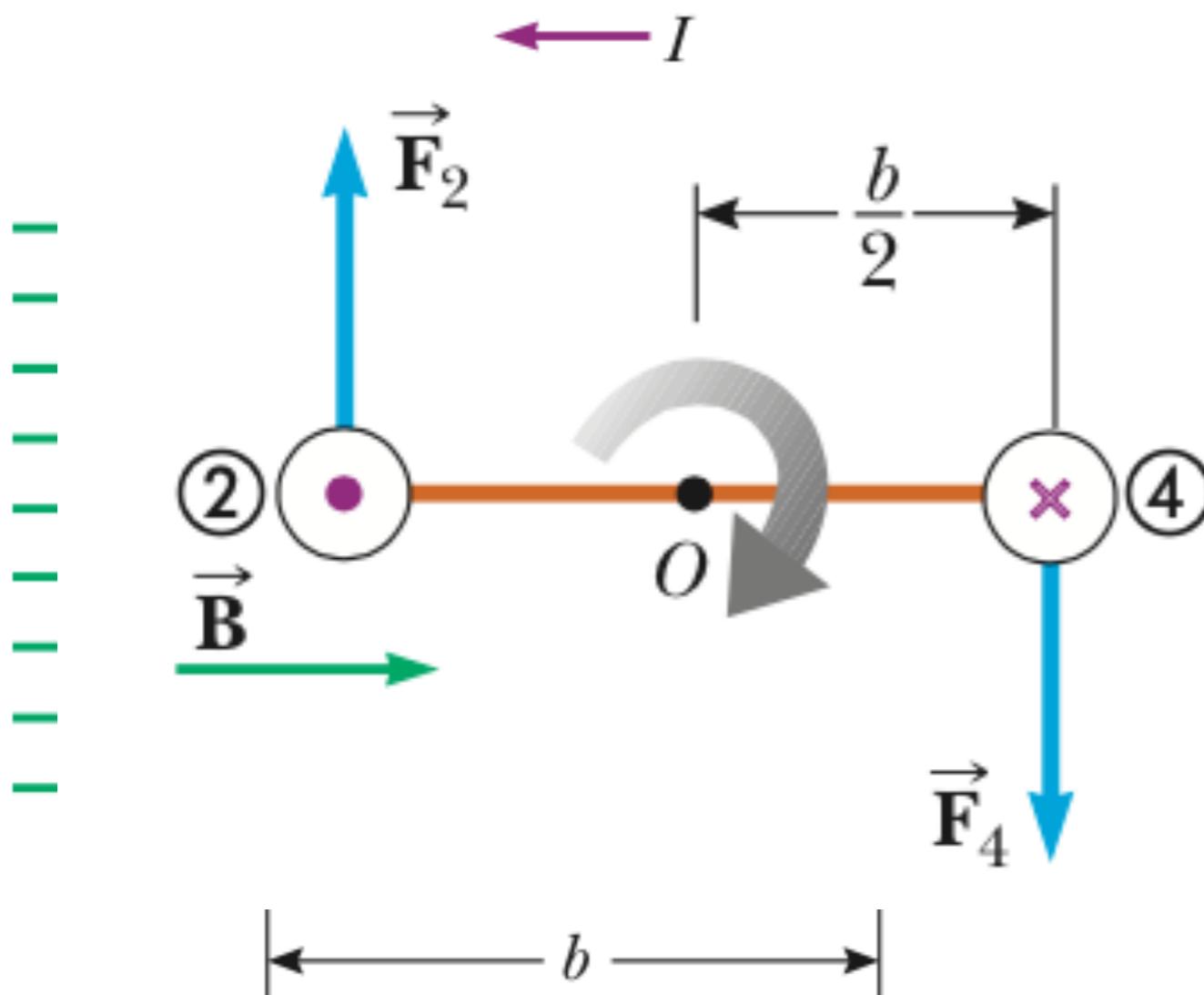
What are the forces on  
these current loops?

# Torque on current loop



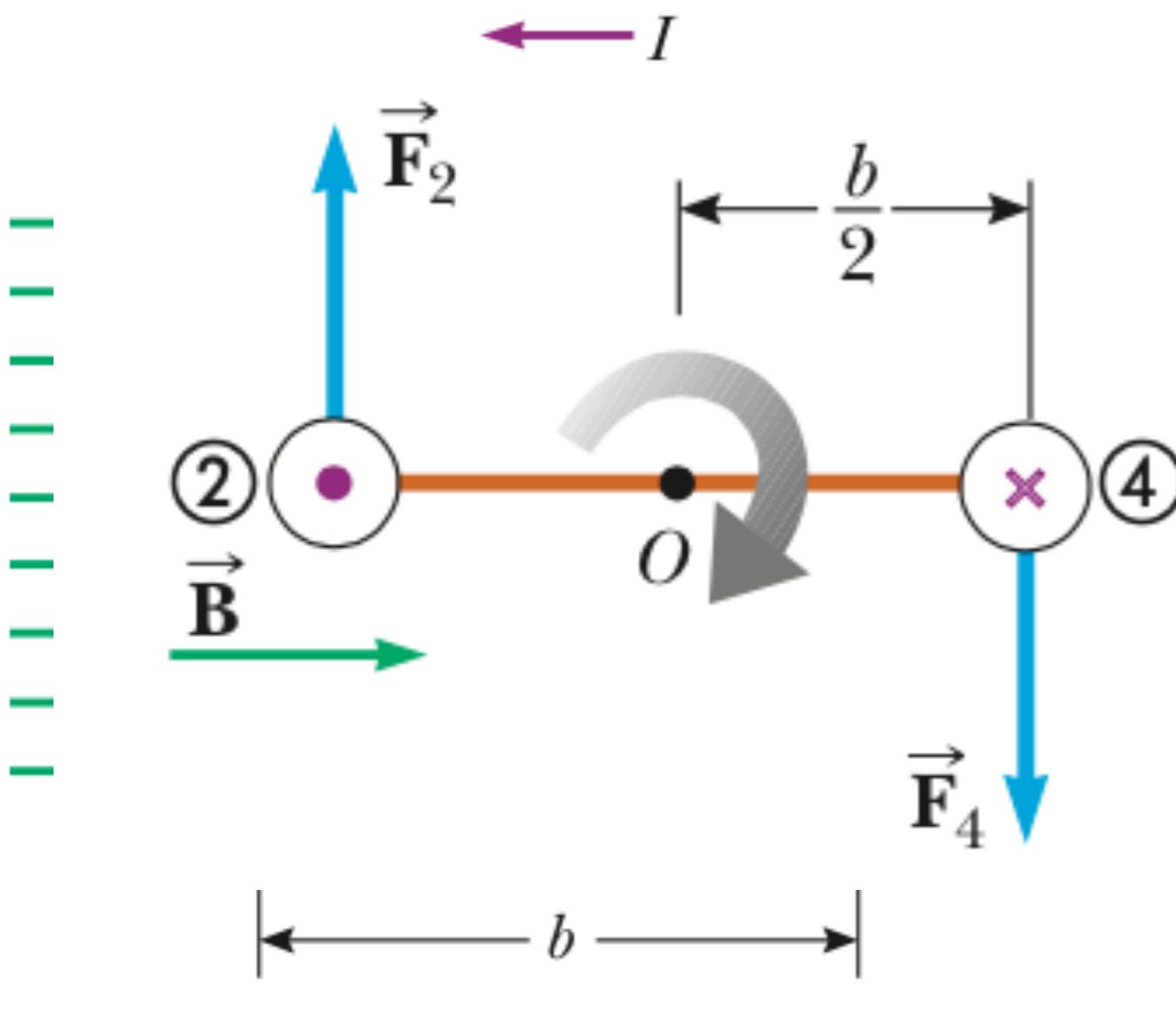
What are the forces on each wire segment?

# Torque on current loop



What are the forces on  
each wire segment?

# Torque on current loop



What are the forces on each wire segment?

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

# Question #25

If released from rest, the current loop will

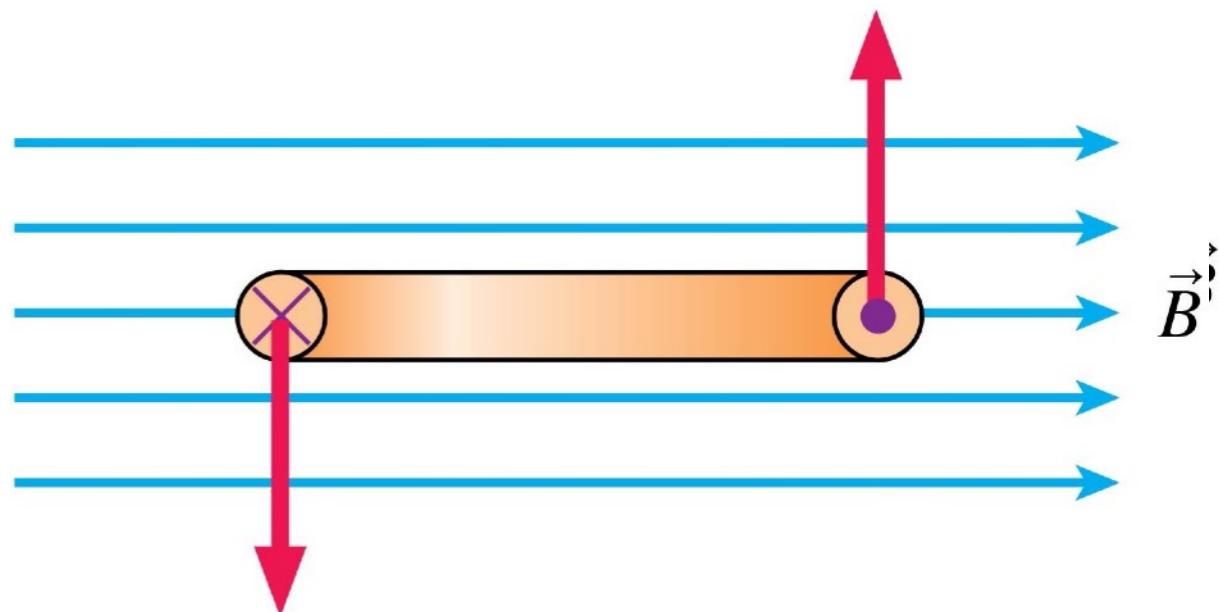
- A. Move upward.
- B. Move downward.
- C. Rotate counterclockwise.
- D. Rotate clockwise.
- E. Do something not listed here.



# Question #25

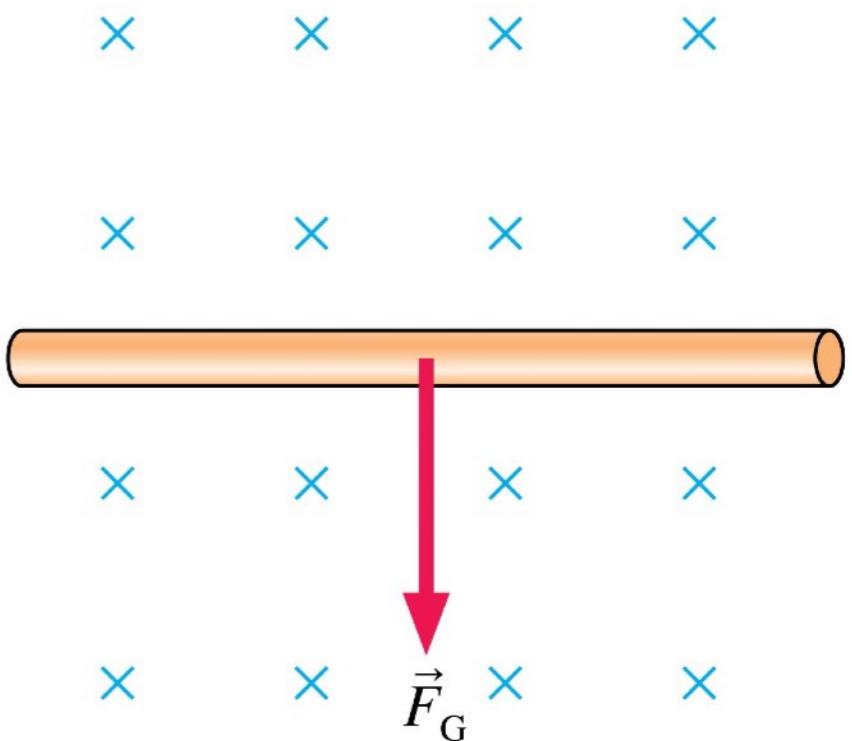
If released from rest, the current loop will

- A. Move upward.
- B. Move downward.
- C. Rotate counterclockwise.
- D. Rotate clockwise.
- E. Do something not listed here.

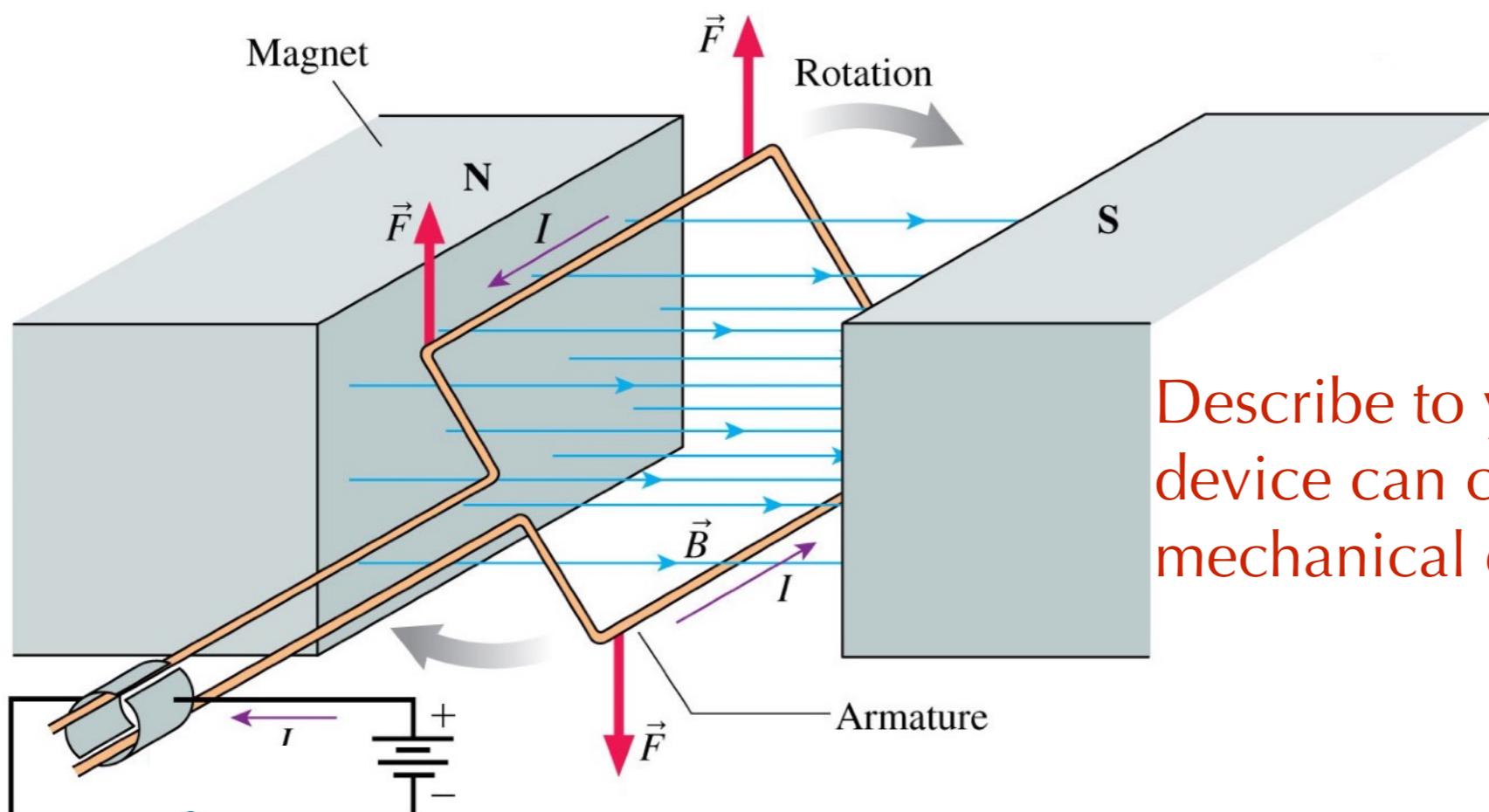


The horizontal wire can be levitated – held up against the force of gravity – if the current in the wire is

- A. Right to left.
- B. Left to right.
- C. It can't be done with this magnetic field.



# A simple electric motor



Describe to your neighbor how this device can convert electrical energy into mechanical energy.