

Point Operators

$$C_{4z}^+ \quad C_{4z}^- \quad \sigma_x \quad \sigma_{da}$$

$$C_{2z}^+ \quad \sigma_y \quad \sigma_{db} \quad E$$

Point Group



$Fm\bar{3}m$



Translates

Including a translation

$$\{C_{4z}^+ | 0 \frac{1}{2} \frac{1}{2}\}$$

Identify the Bravais Lattice.

- a) monoclinic I
- b) monoclinic P
- c) Orthorhombic P
- d) Orthorhombic I

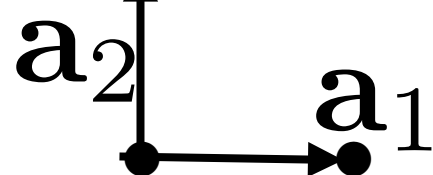


Identify the following planes
in this crystal.

$(2, 1, 0)$

$(2, 3, 0)$

$\frac{A}{h}, \frac{A}{k}, \frac{A}{l}$

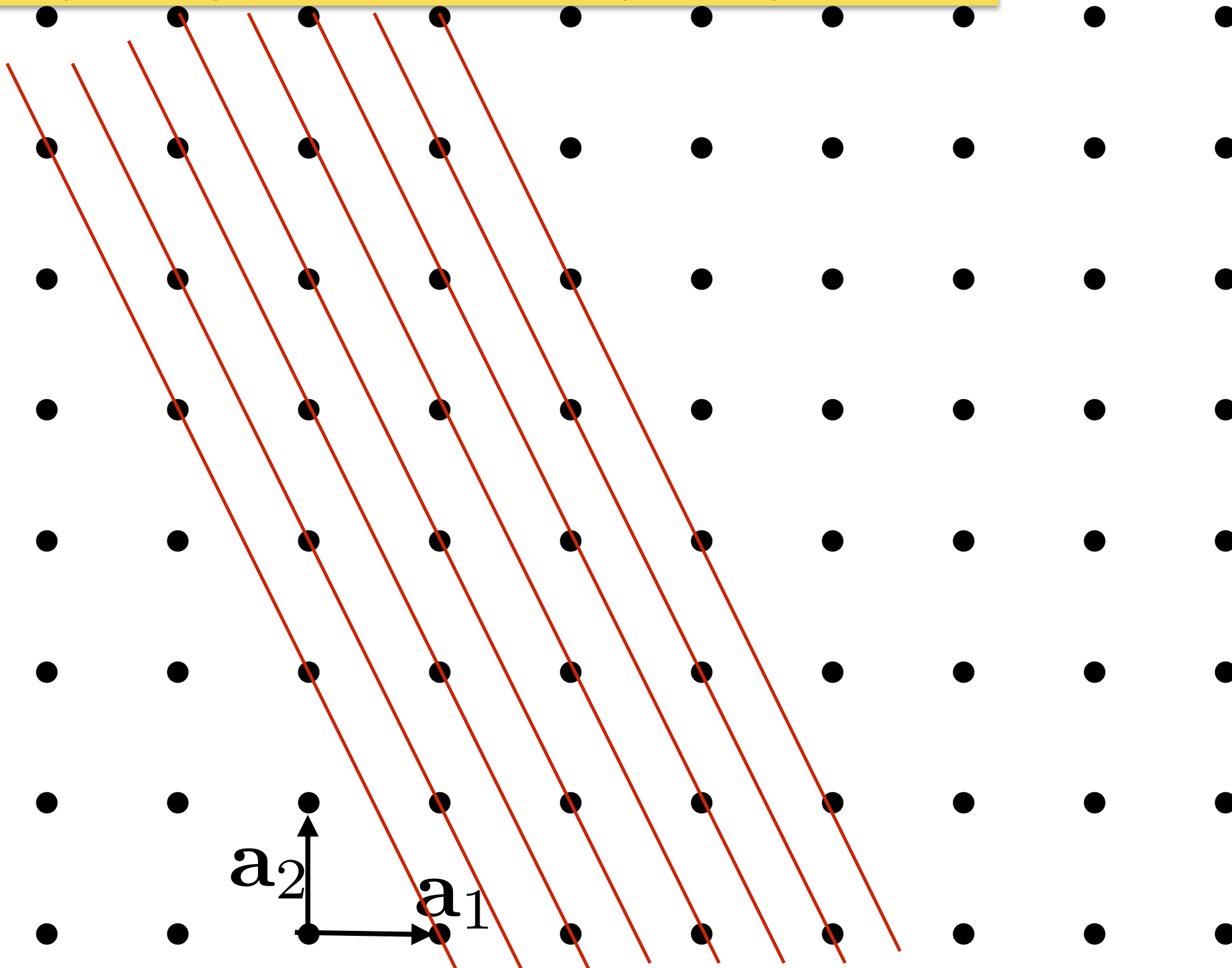


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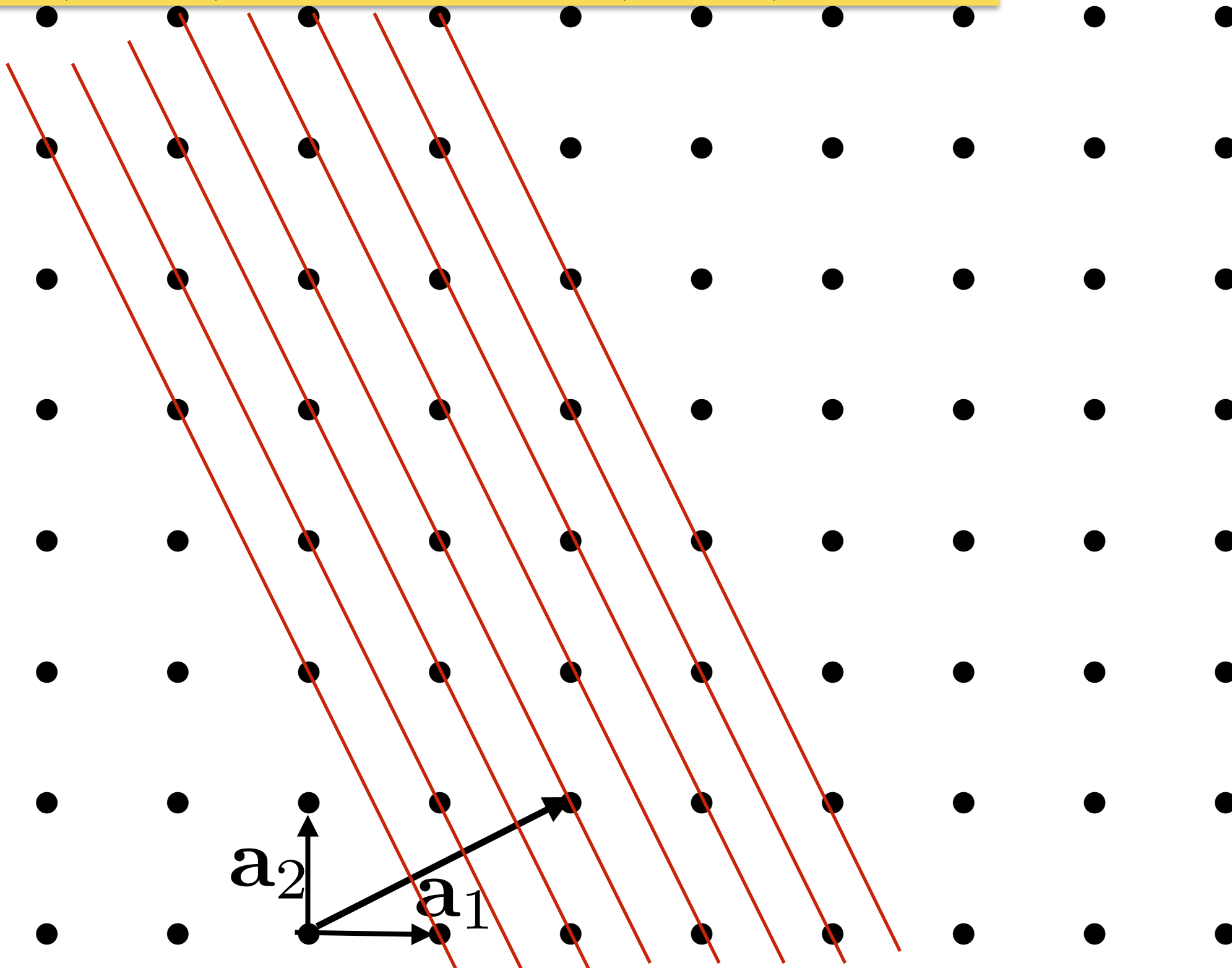


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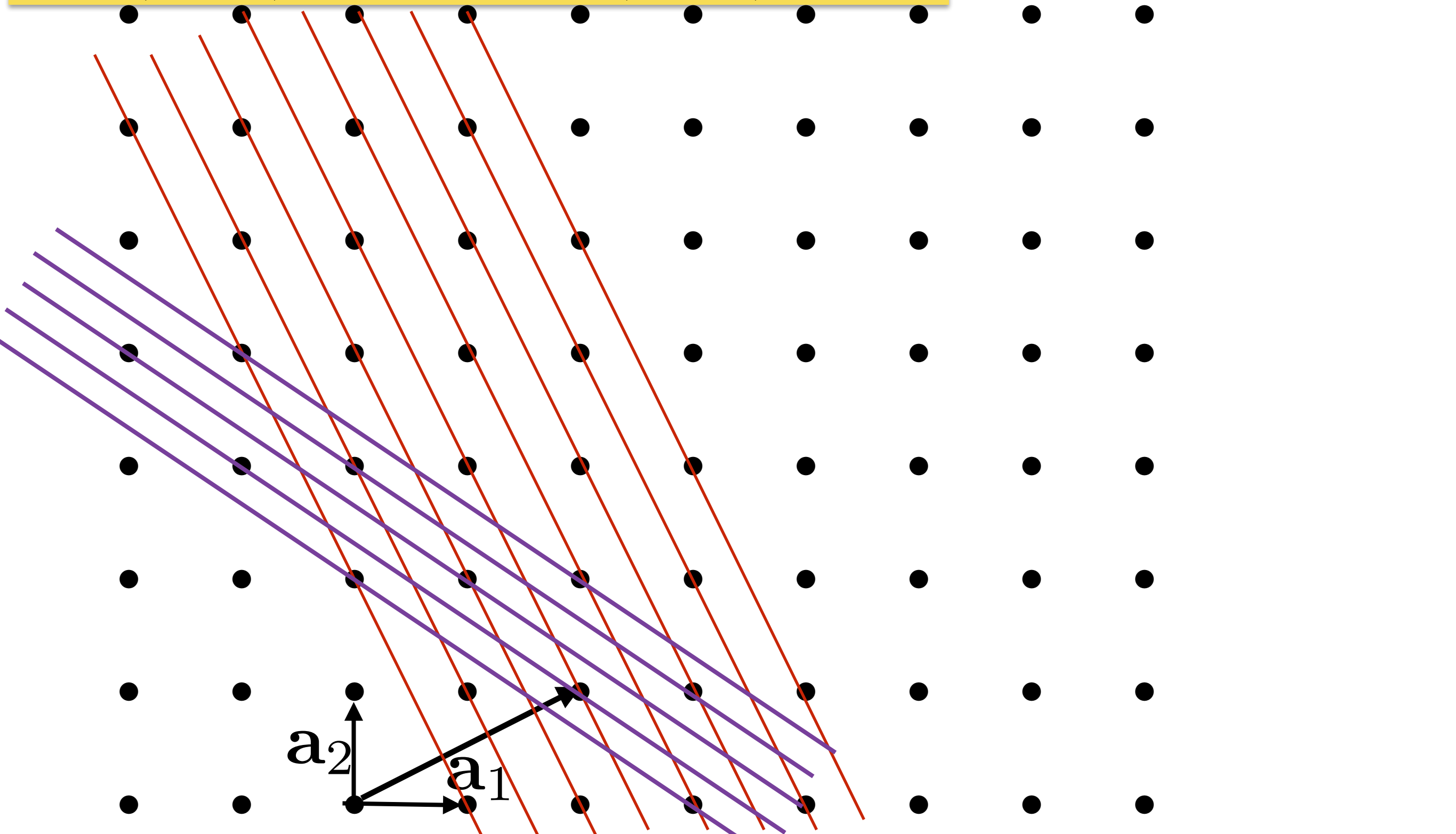


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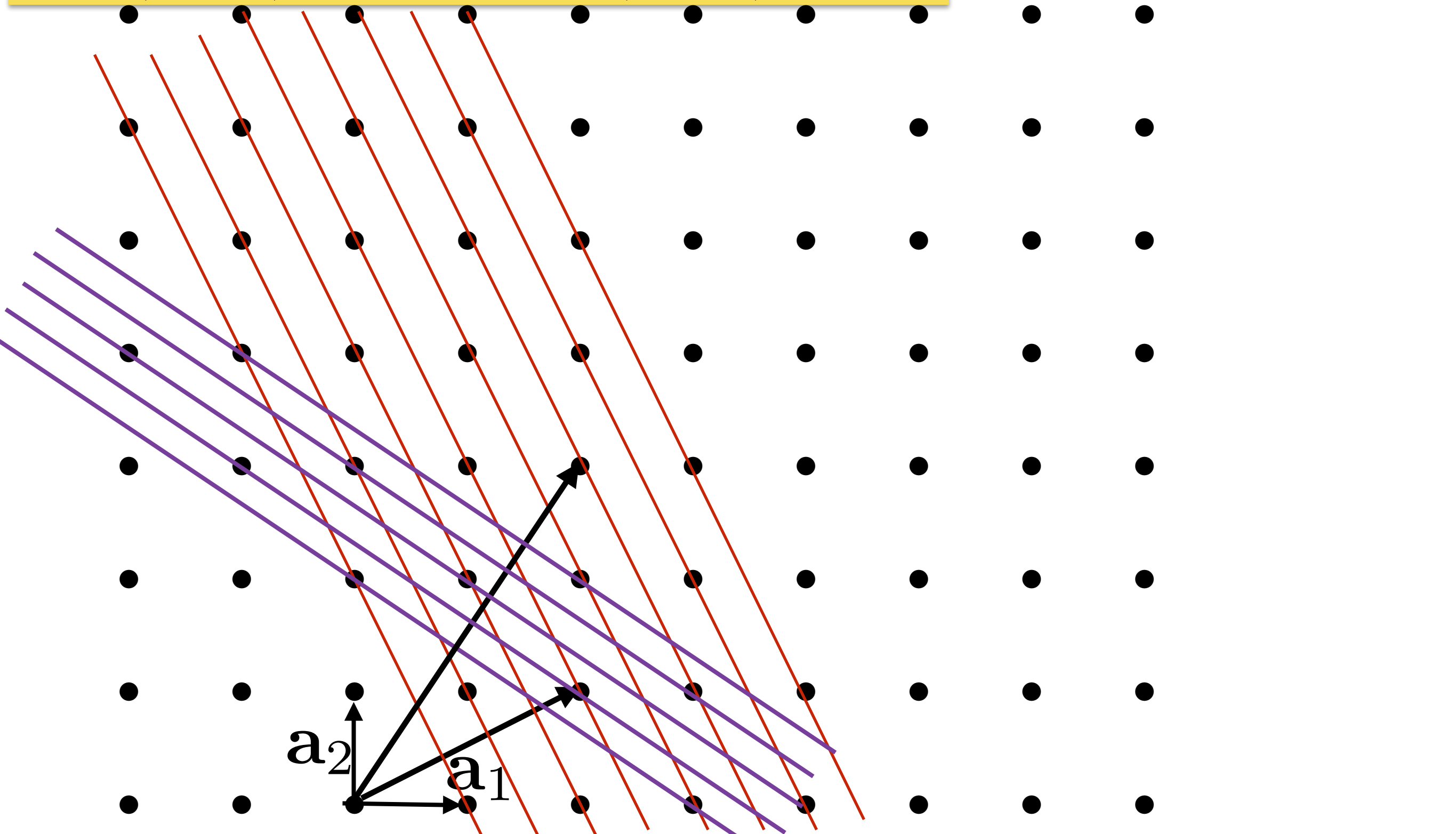


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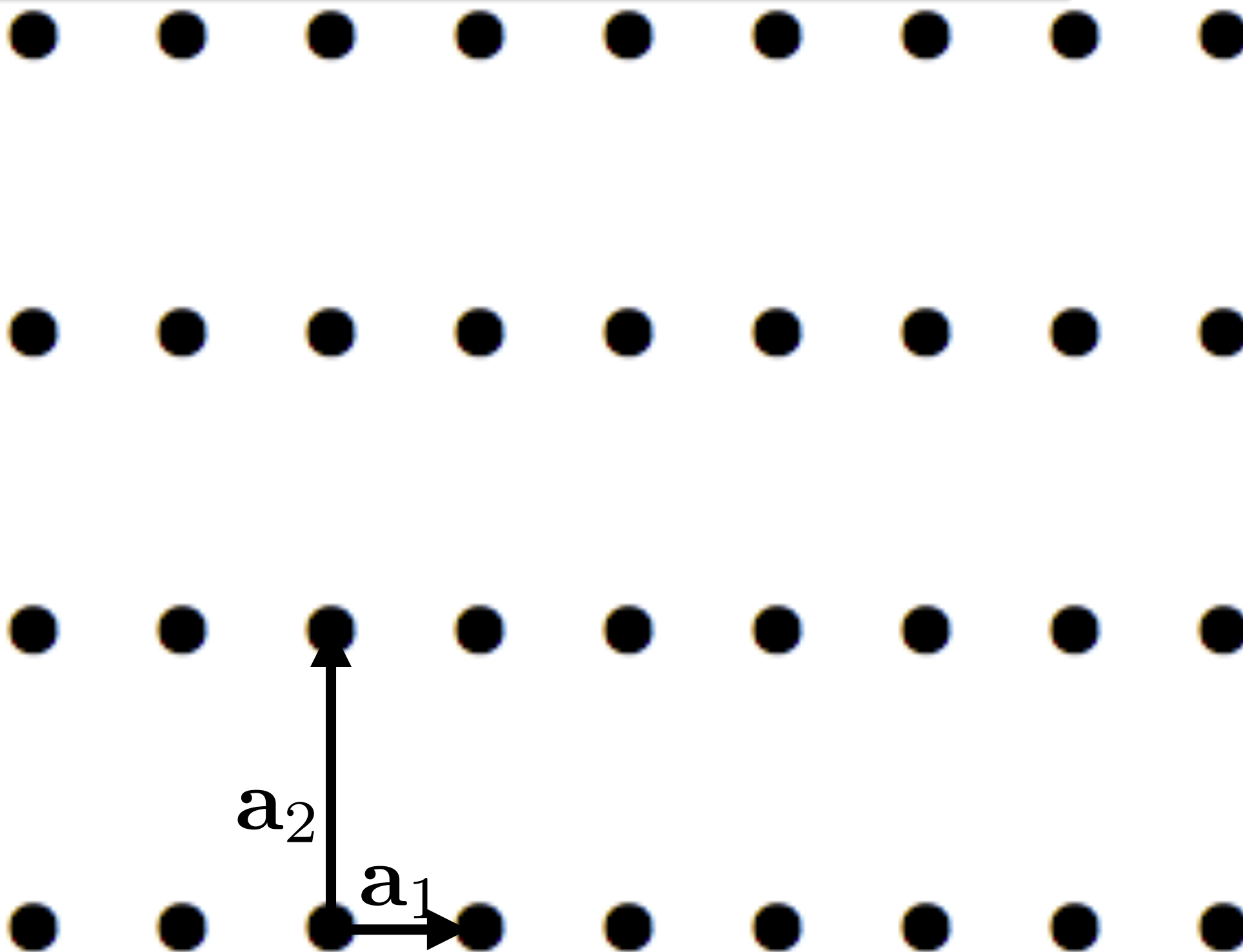
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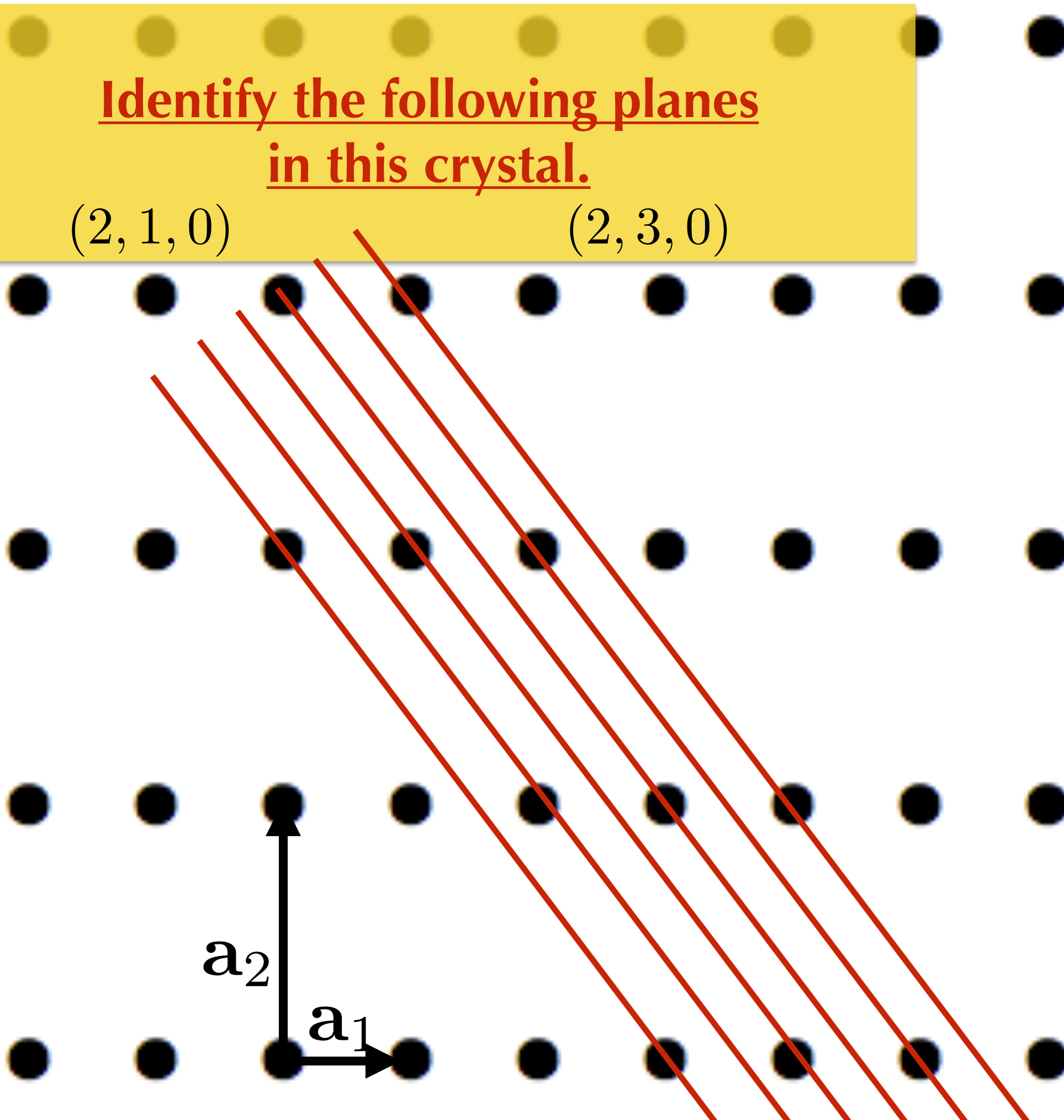
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in this crystal.

$(2, 1, 0)$

$(2, 3, 0)$

a_2

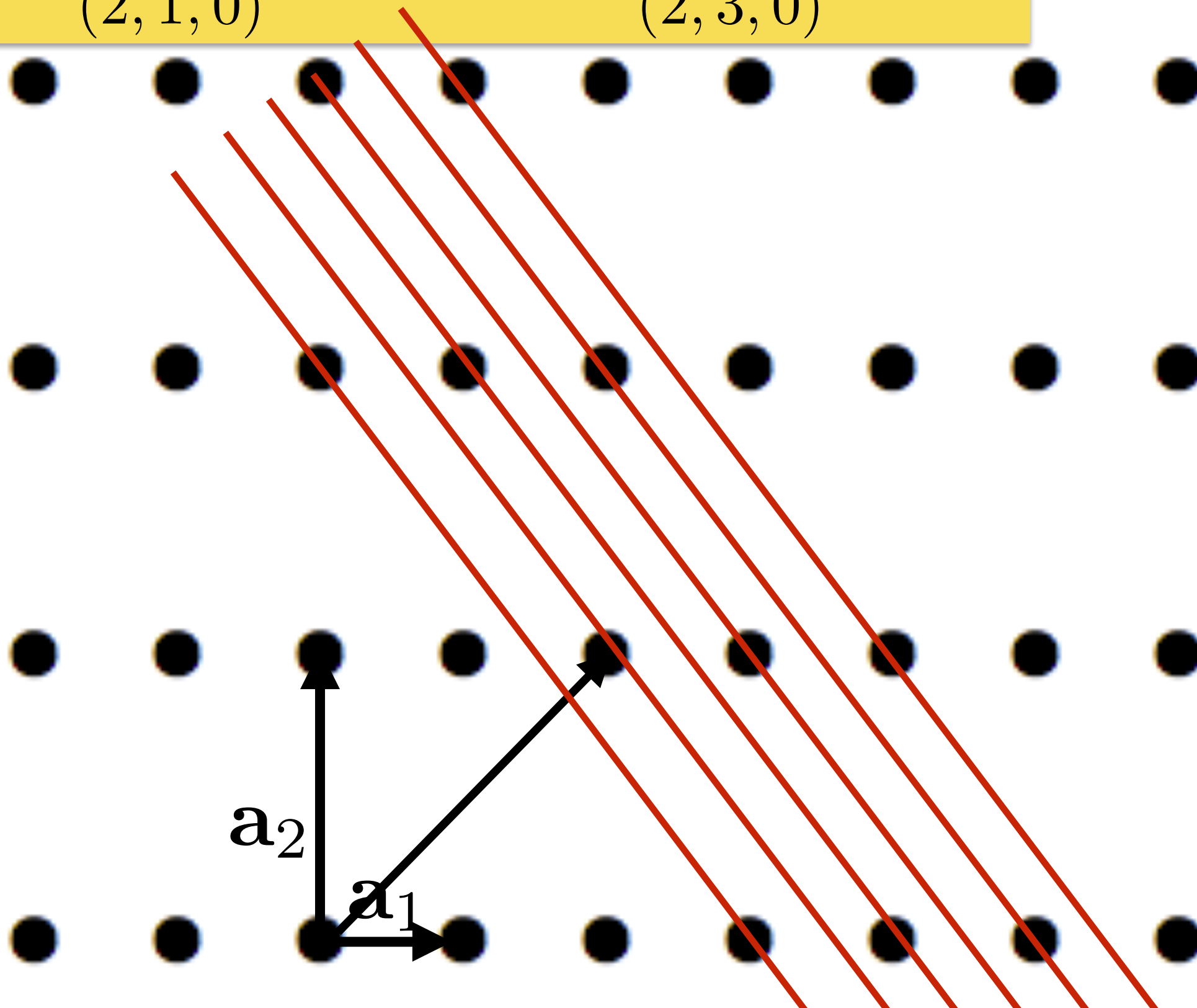
a_1



Identify the following planes
in this crystal.

$(2, 1, 0)$

$(2, 3, 0)$



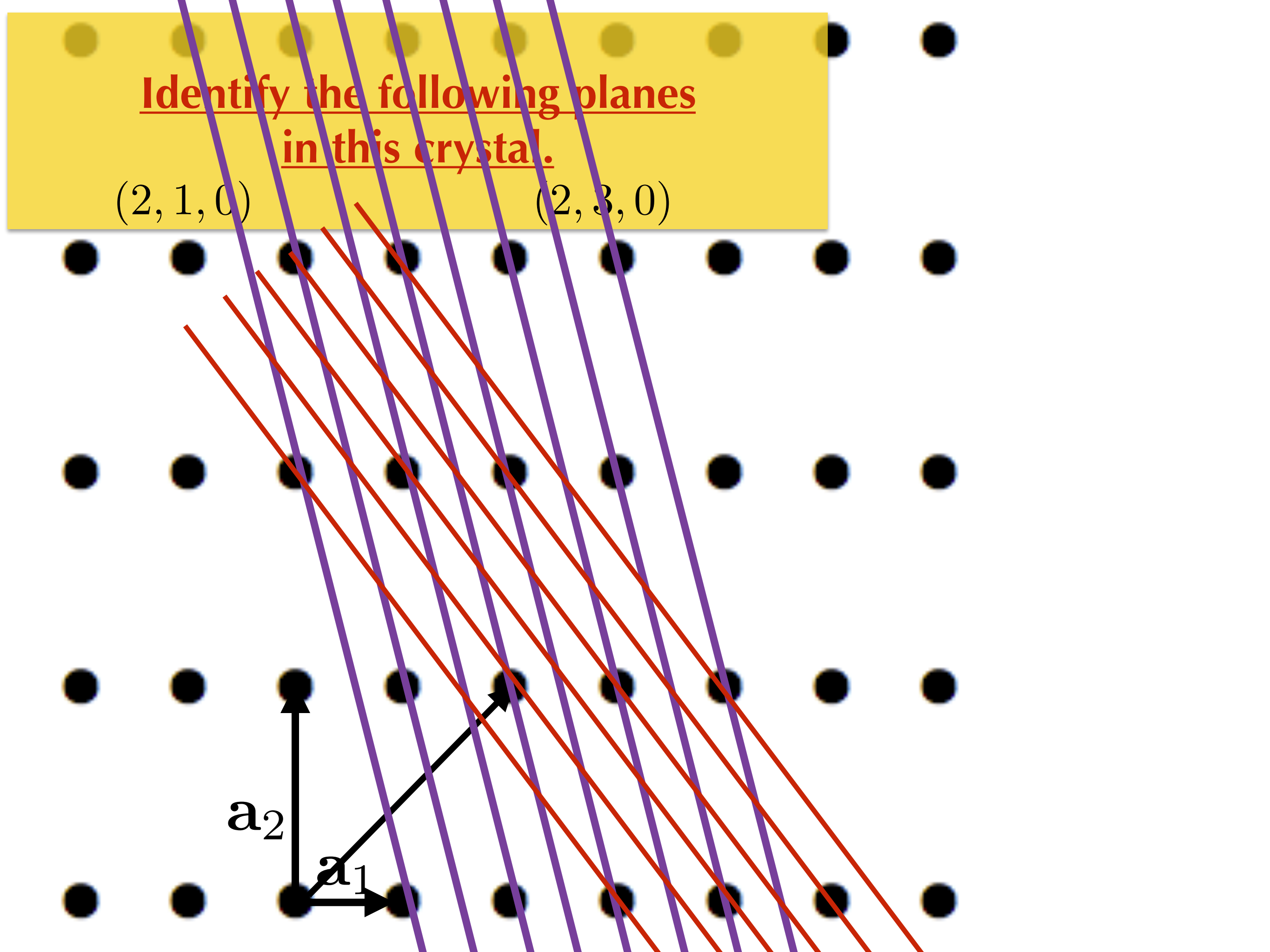
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a_2

a_1



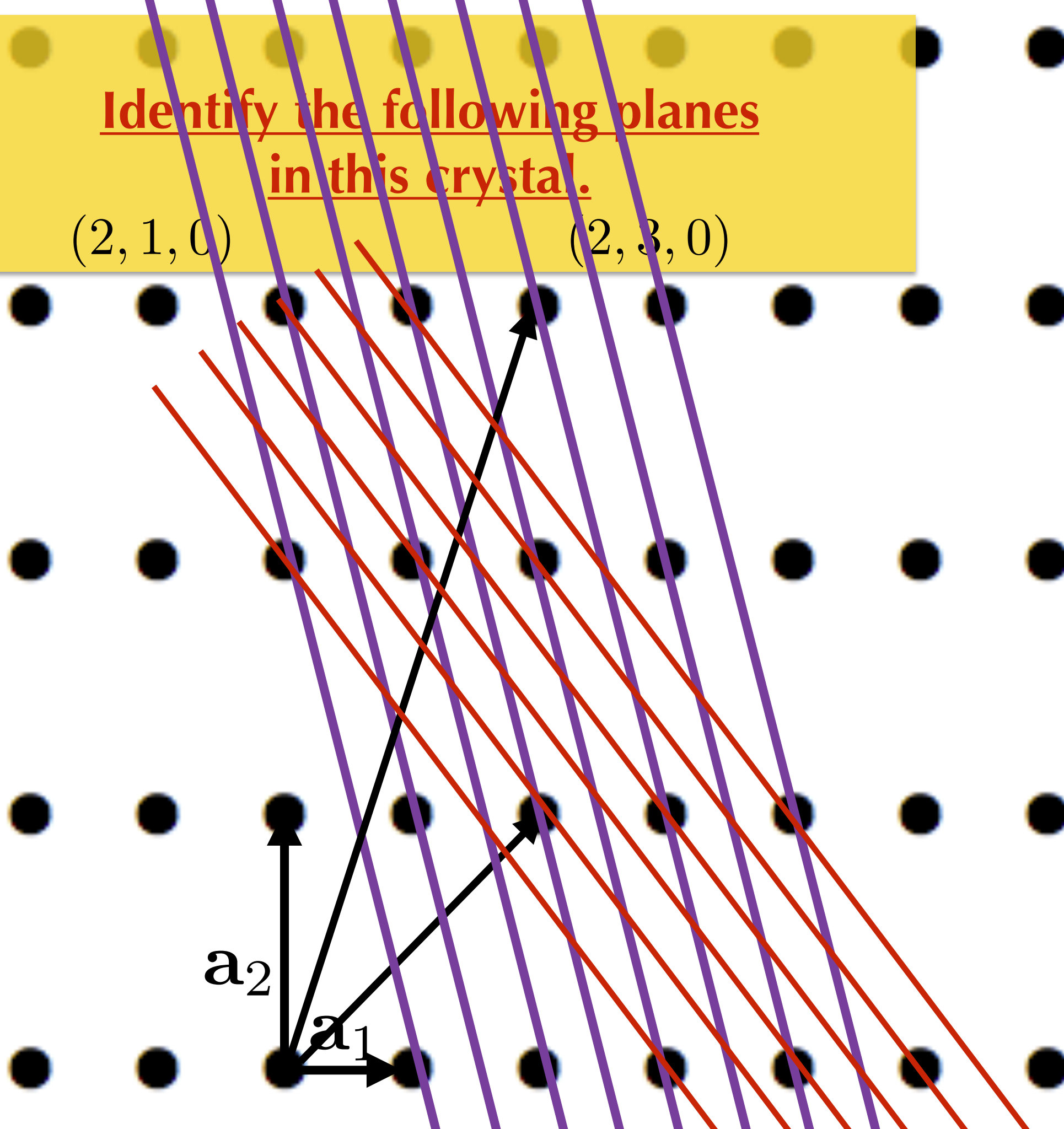
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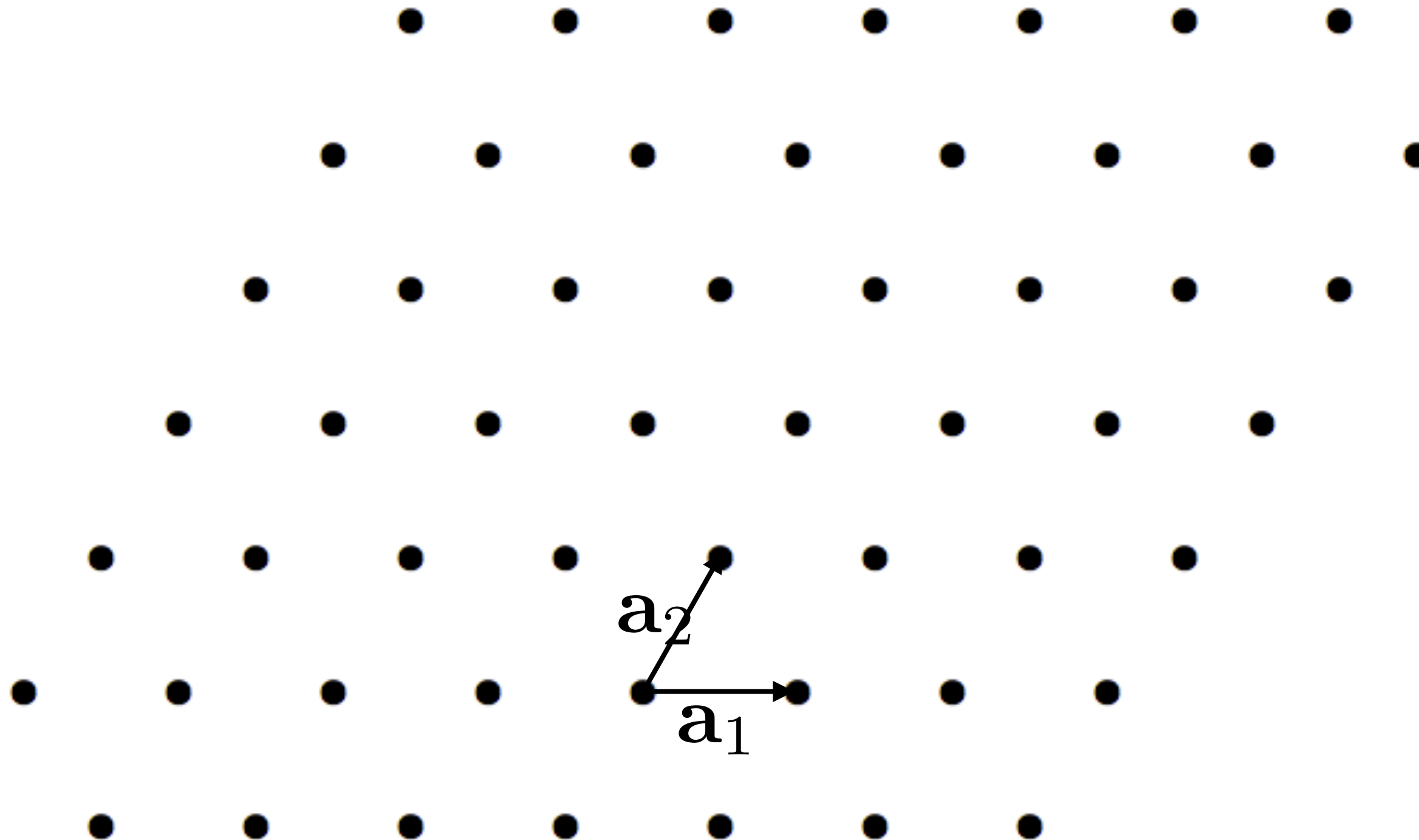


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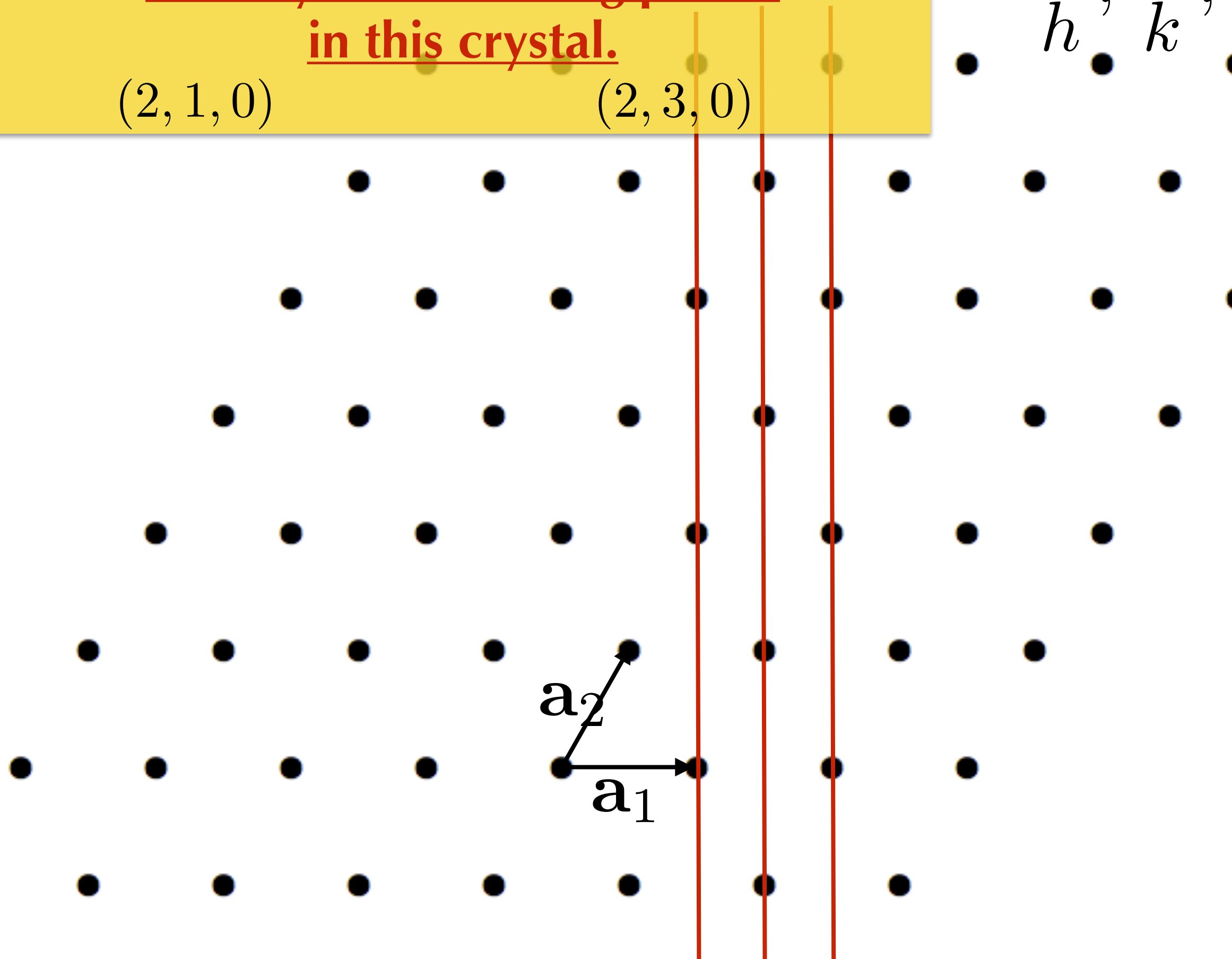


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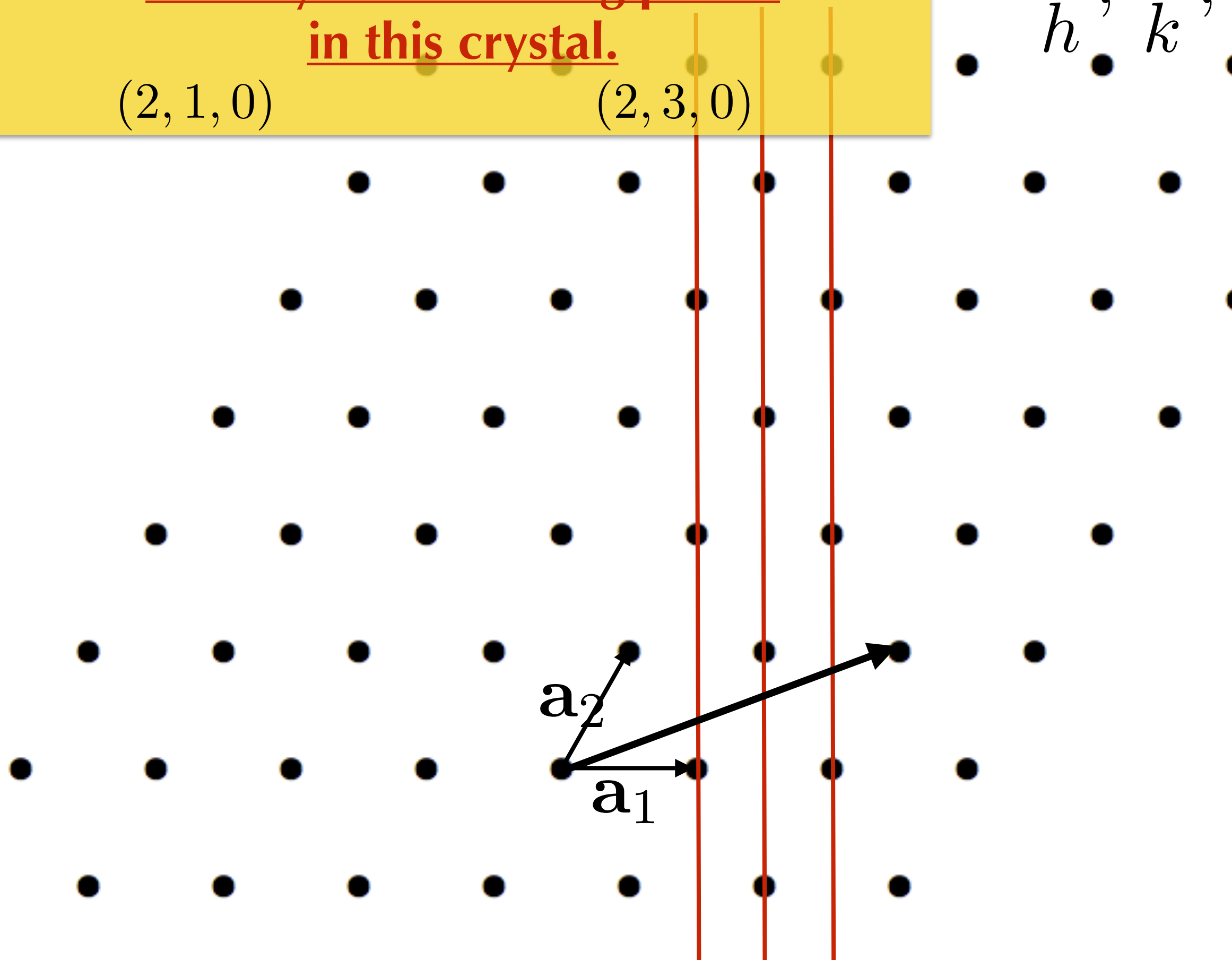


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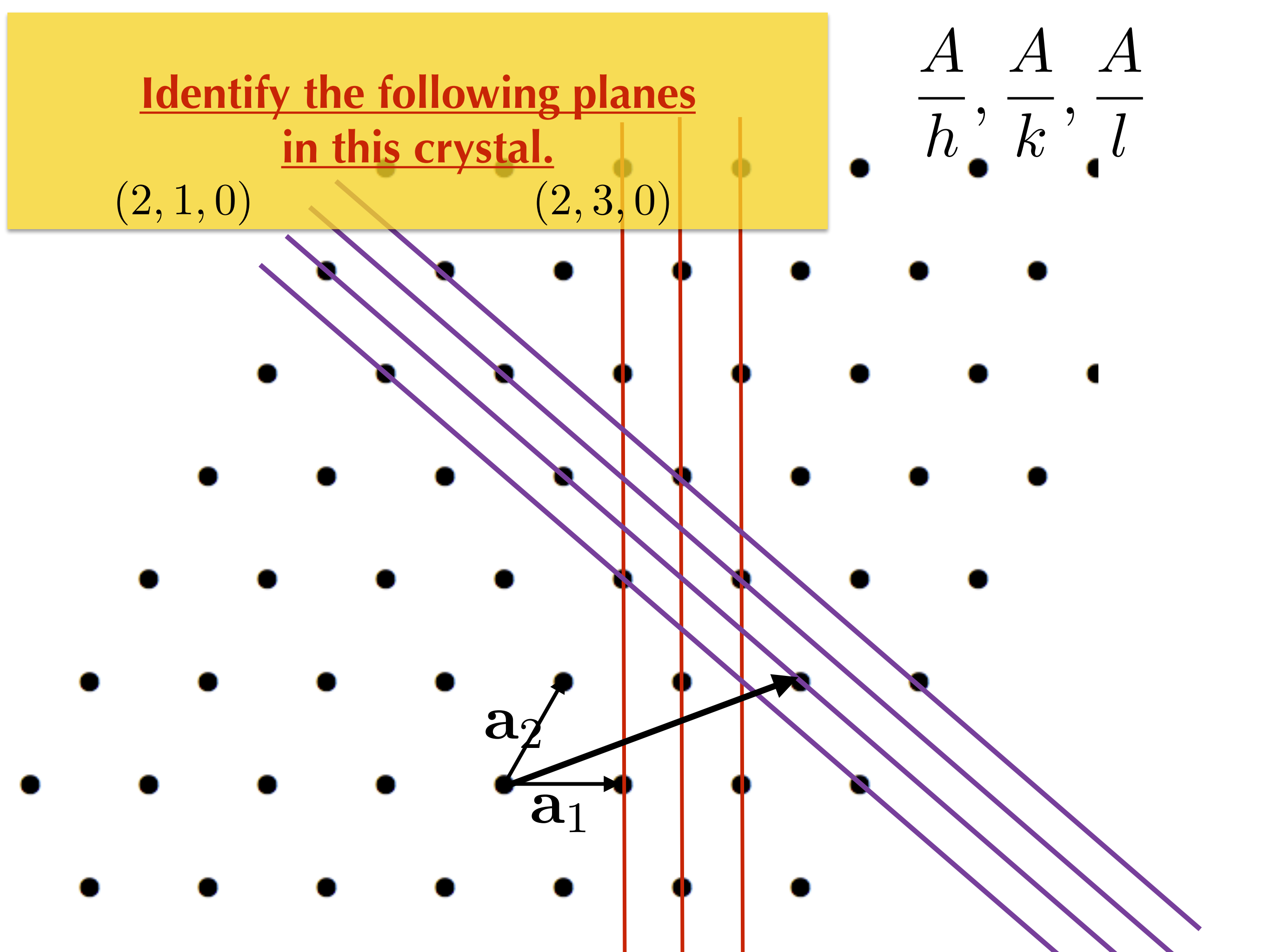
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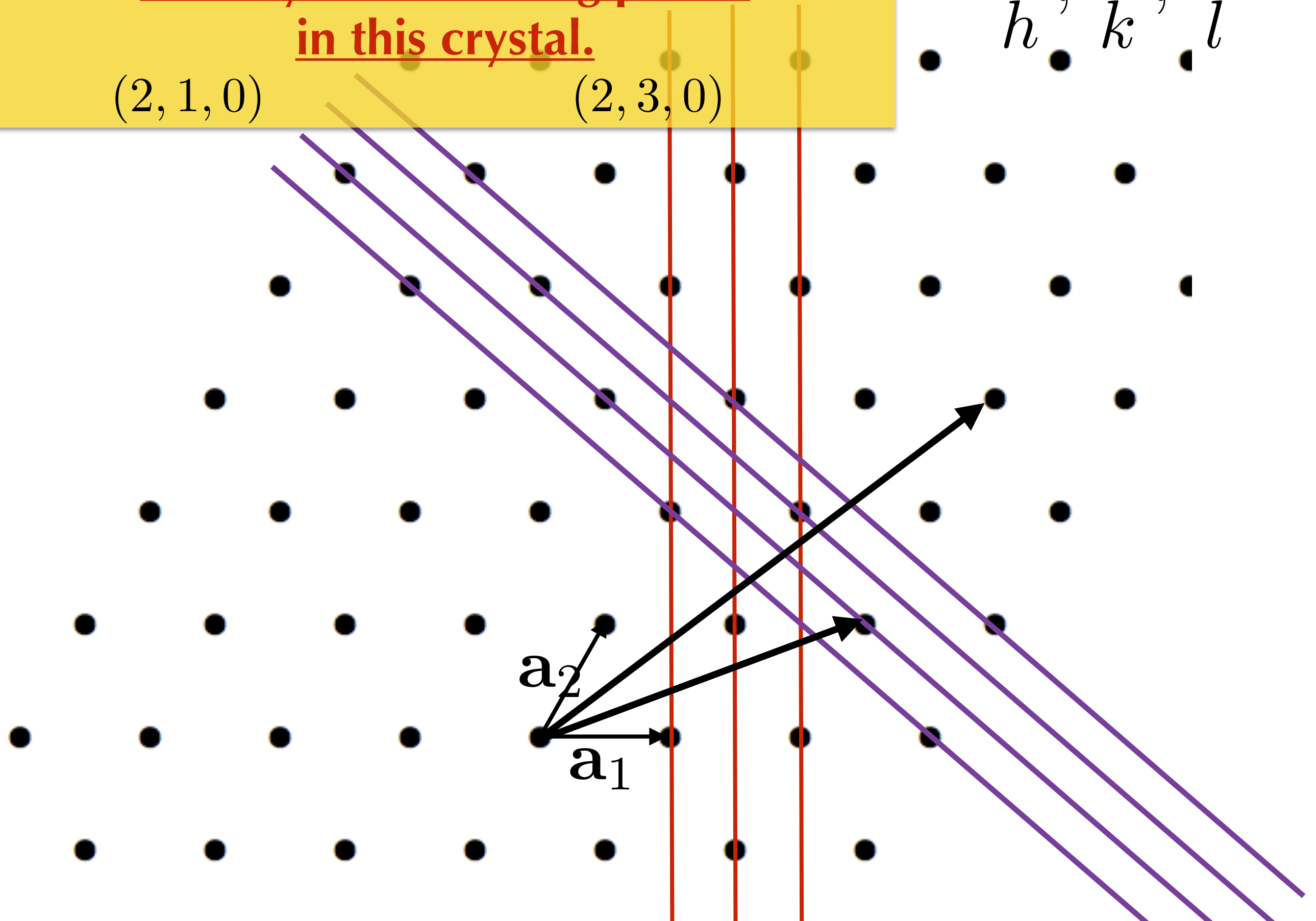


Identify the following planes
in this crystal.

$$\frac{A}{h}, \frac{A}{k}, \frac{A}{l}$$

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Which are not symmetry operators
for NaCl?

$$\{C_{4z}^+ | 0 \frac{1}{2} \frac{1}{2}\}$$

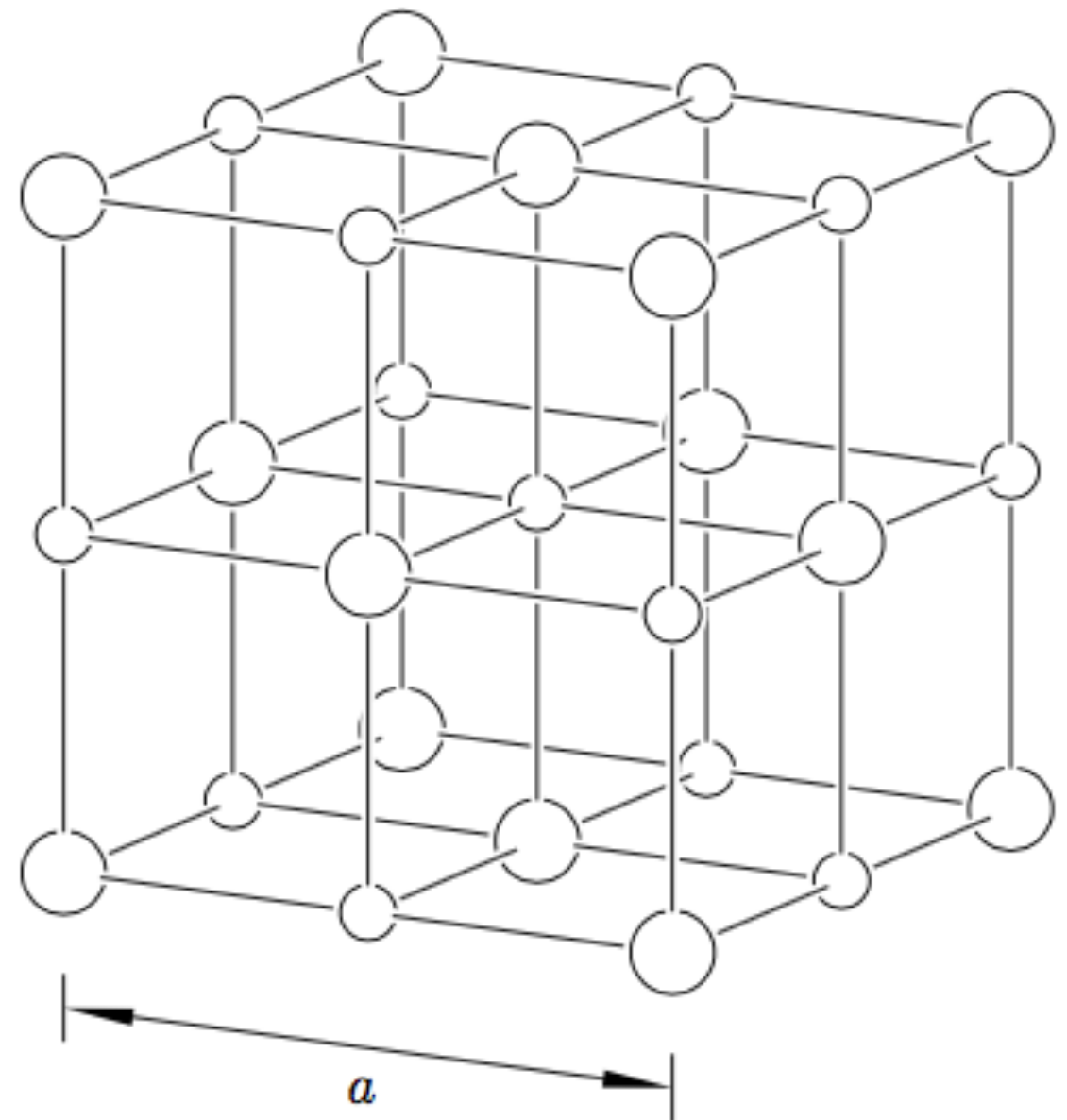
$$\{C_{2x}^+ | \frac{1}{2} \frac{1}{2} \frac{1}{2}\}$$

$$\{E | \frac{1}{2} 0 \frac{1}{2}\}$$

$$\{C_{4z}^- | \frac{3}{2} \frac{1}{2} 0\}$$

$$\{C_{4x}^- | 000\}$$

$$\{E | \frac{1}{2} \frac{1}{2} \frac{1}{2}\}$$



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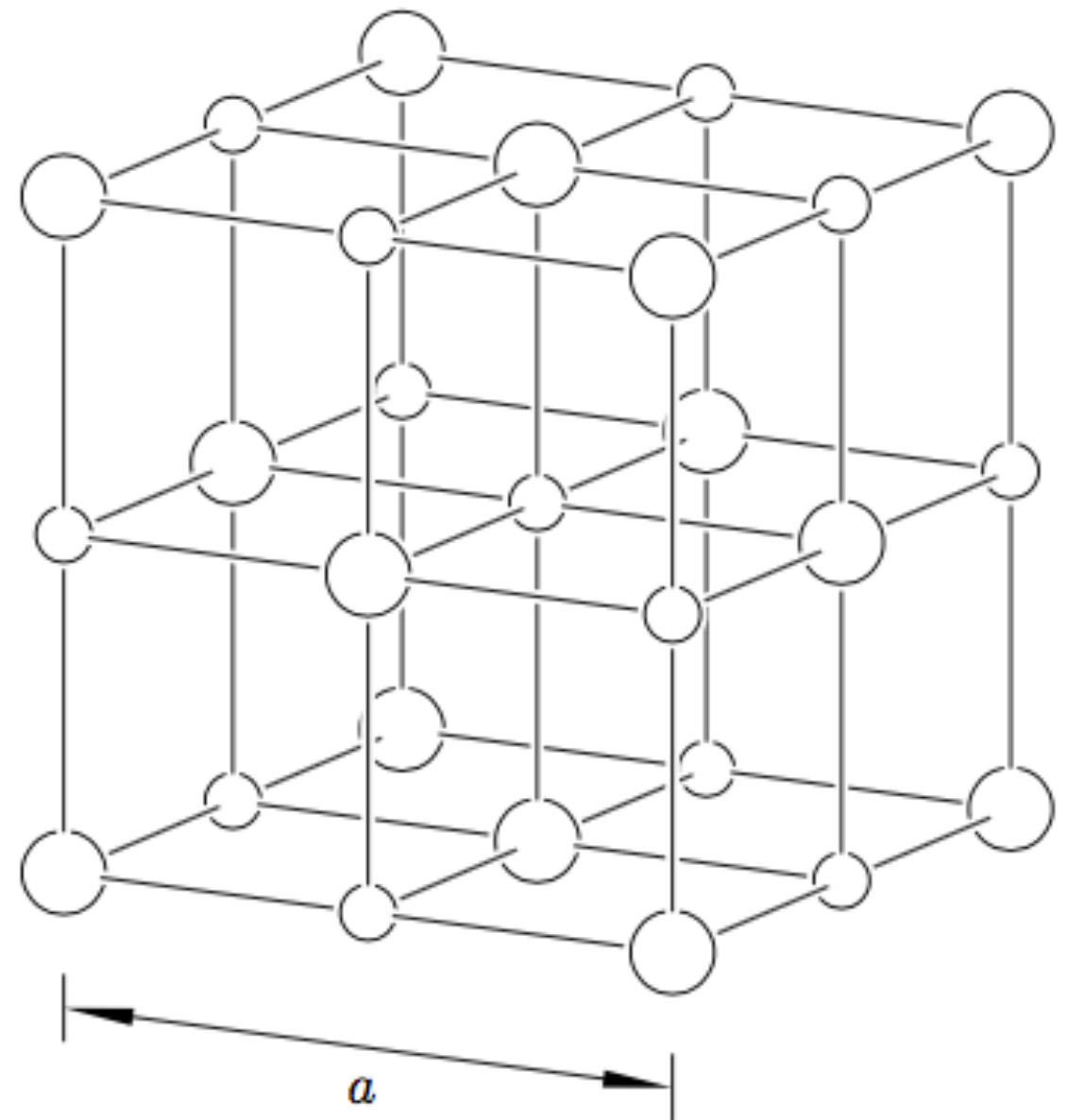
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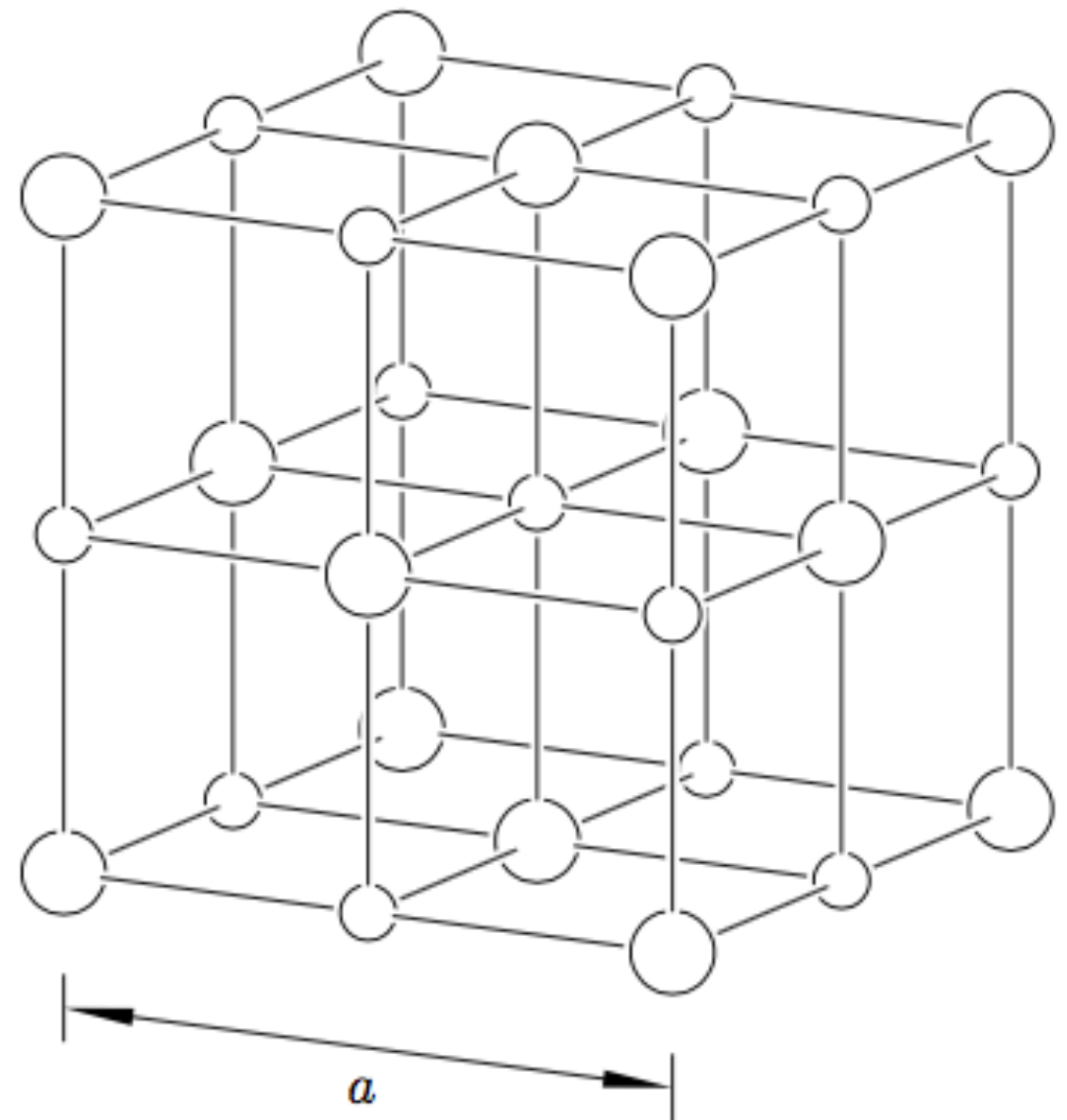
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$Fm\bar{3}m$

Which are not symmetry operators
for zincblende?

$$\{C_{4z}^+ | 0 \frac{1}{2} \frac{1}{2}\}$$

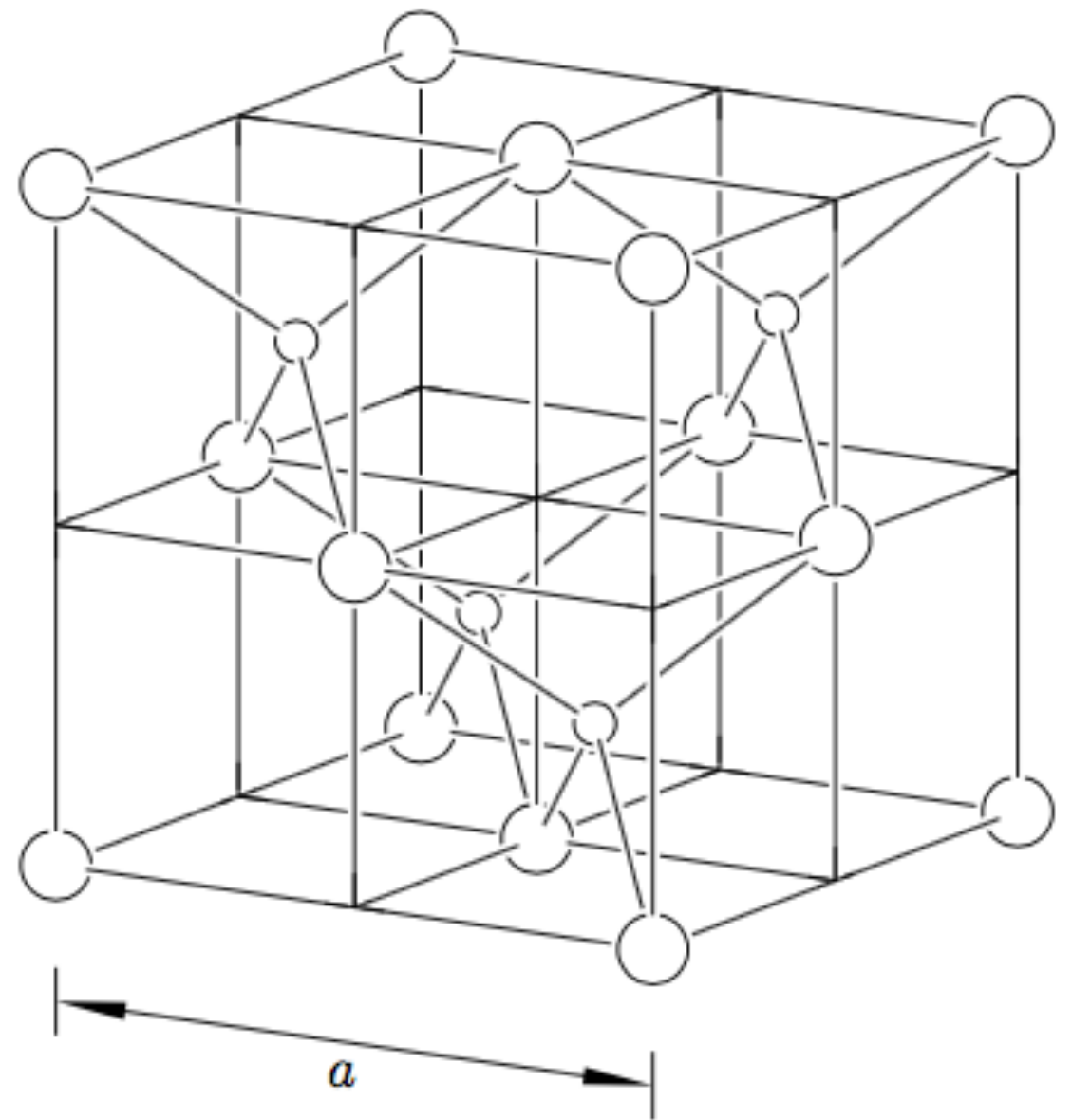
$$\{C_{2x}^+ | \frac{1}{2} \frac{1}{2} \frac{1}{2}\} \quad \{C_{2x}^+ | \frac{1}{2} 0 \frac{1}{2}\}$$

$$\{E | \frac{1}{2} 0 \frac{1}{2}\}$$

$$\{C_{4x}^- | 000\}$$

$$\{C_{4z}^- | \frac{3}{2} \frac{1}{2} 0\}$$

$$\{E | \frac{1}{2} \frac{1}{2} \frac{1}{2}\}$$



Which are not symmetry operators
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$$\{C_{4z}^+ | \overset{\text{X}}{\frac{1}{2}} \frac{1}{2} \frac{1}{2}\}$$

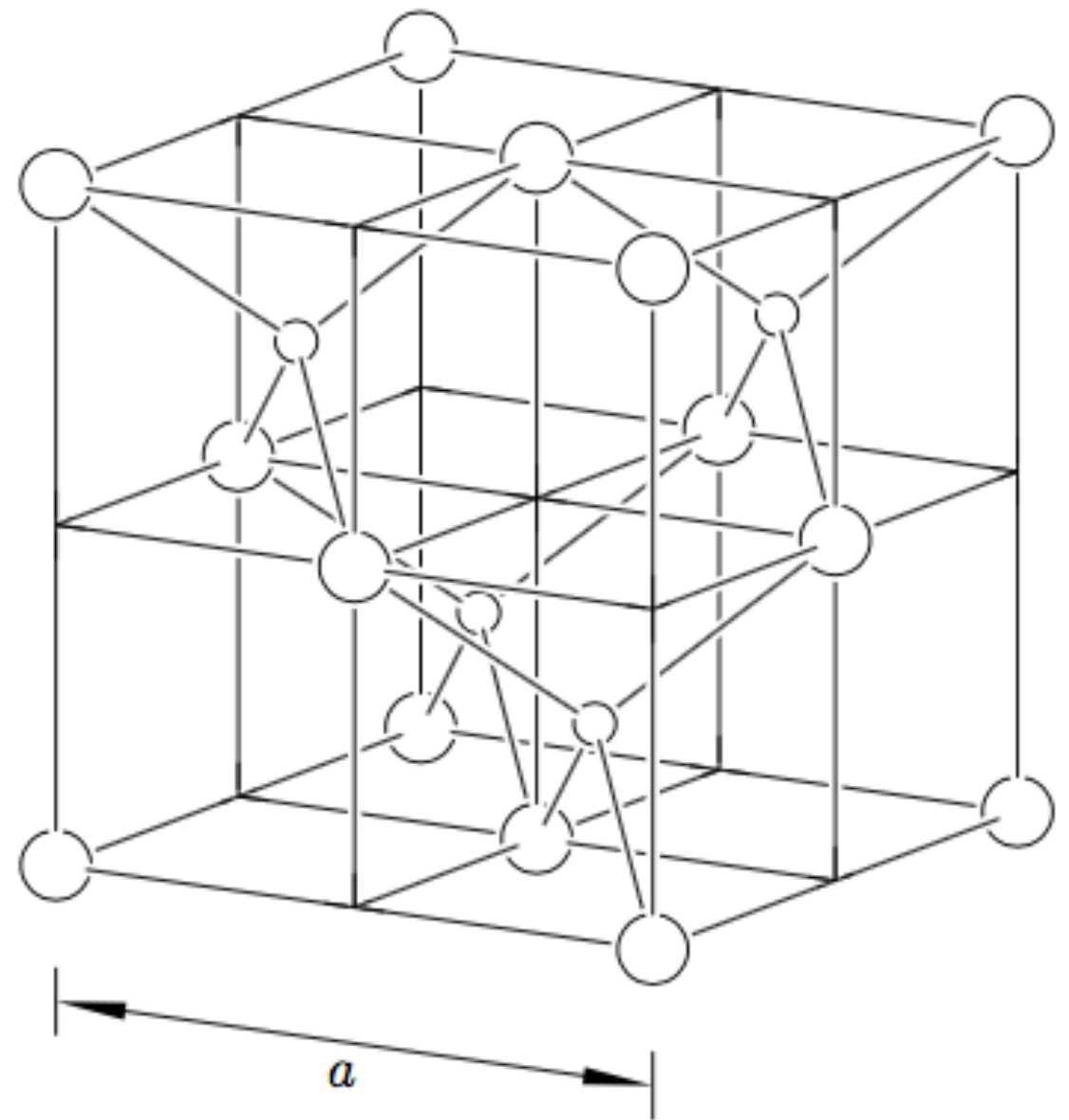
$$\{C_{2x}^+ | \overset{\text{X}}{\frac{1}{2}} \frac{1}{2} \frac{1}{2}\} \quad \{C_{2x}^+ | \frac{1}{2} 0 \frac{1}{2}\}$$

$$\{E | \frac{1}{2} 0 \frac{1}{2}\}$$

$$\{C_{4x}^- | \overset{\text{X}}{0} 0 0\}$$

$$\{C_{4z}^- | \overset{\text{X}}{\frac{3}{2}} \frac{1}{2} 0\}$$

$$\{E | \overset{\text{X}}{\frac{1}{2}} \frac{1}{2} \frac{1}{2}\}$$



Which are not symmetry operators
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$$\{C_{4z}^+ | \overset{\text{X}}{\frac{1}{2}} \frac{1}{2} \frac{1}{2}\}$$

$$\{C_{2x}^+ | \overset{\text{X}}{\frac{1}{2}} \frac{1}{2} \frac{1}{2}\} \quad \{C_{2x}^+ | \frac{1}{2} 0 \frac{1}{2}\}$$

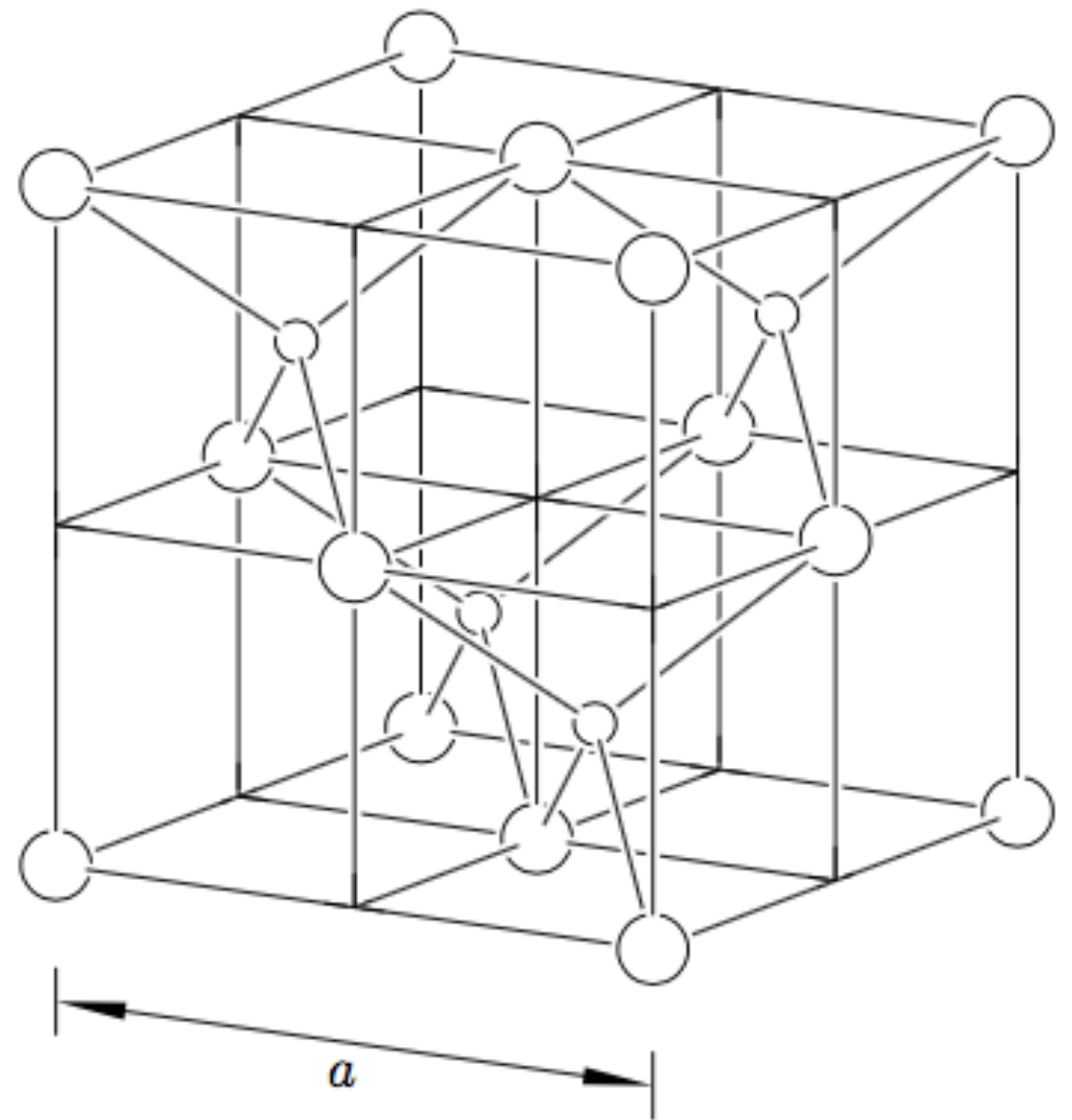
$$\{E | \frac{1}{2} 0 \frac{1}{2}\}$$

$$\{C_{4x}^- | \overset{\text{X}}{0} 0 0\}$$

$F\bar{4}3m$

$$\{C_{4z}^- | \overset{\text{X}}{\frac{3}{2}} \frac{1}{2} 0\}$$

$$\{E | \overset{\text{X}}{\frac{1}{2}} \frac{1}{2} \frac{1}{2}\}$$



Which are not symmetry operators for diamond?

$$\{C_{4z}^+ | 0 \frac{1}{2} \frac{1}{2}\}$$

$$\{C_{4z}^+ | 00 \frac{1}{4}\}$$

$$\{C_{2x}^+ | 0 \frac{1}{2} \frac{1}{2}\}$$

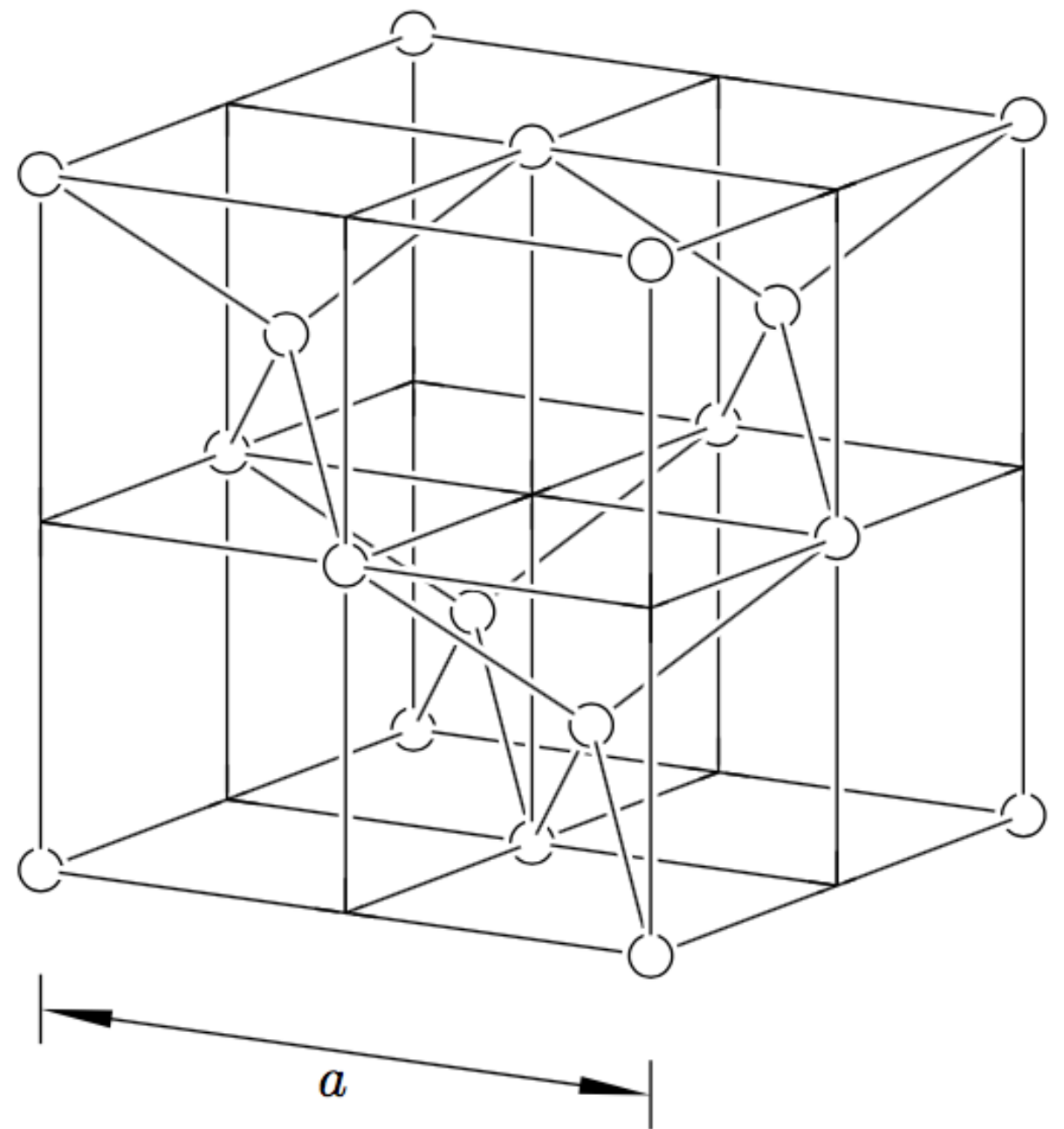
$$\{C_{2x}^+ | \frac{1}{2} 0 \frac{1}{2}\}$$

$$\{E | \frac{1}{2} 0 \frac{1}{2}\}$$

$$\{\sigma_z | \frac{1}{4} \frac{1}{4} \frac{1}{4}\}$$

$$\{C_{4z}^- | \frac{3}{2} \frac{1}{2} 0\}$$

$$\{E | \frac{1}{2} \frac{1}{2} \frac{1}{2}\}$$



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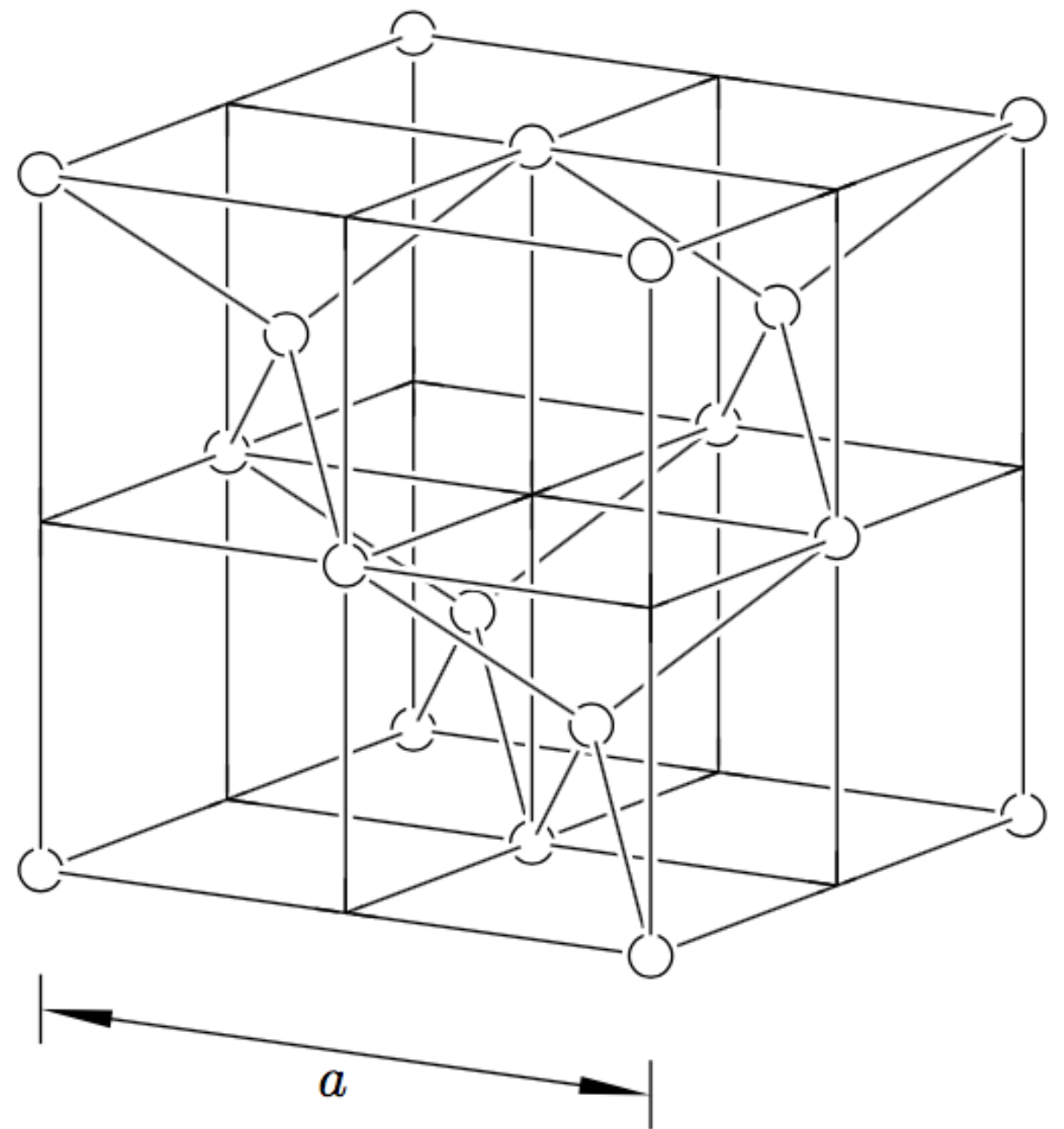
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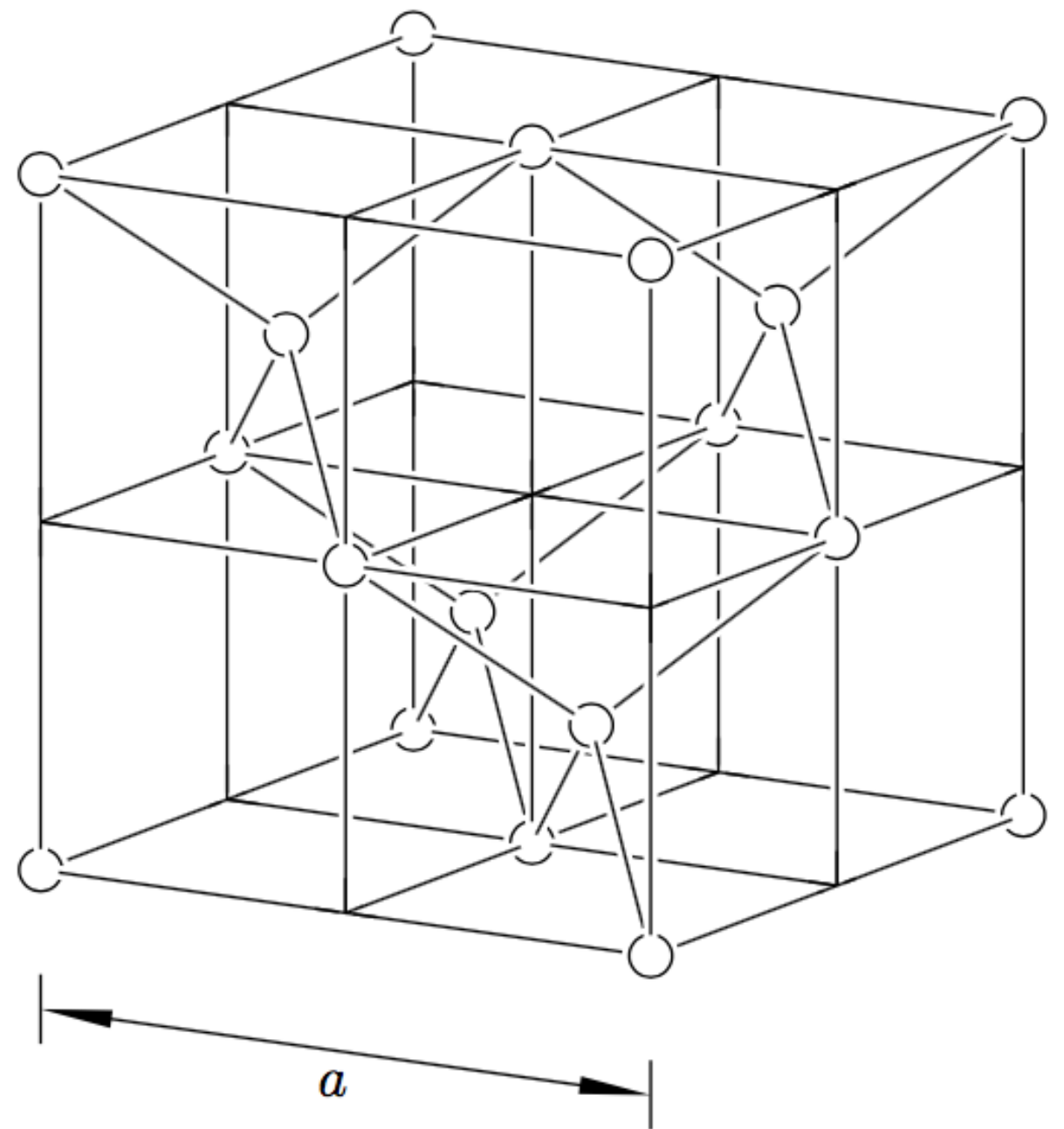
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$Fm\bar{3}m$

Which are not symmetry operators for diamond?

Screw axis

$$\{C_{4z}^+ | 0 \frac{1}{2} \frac{1}{2}\}$$

$$\{C_{4z}^+ | 00 \frac{1}{4}\}$$

$$\{C_{2x}^+ | 0 \frac{1}{2} \frac{1}{2}\}$$

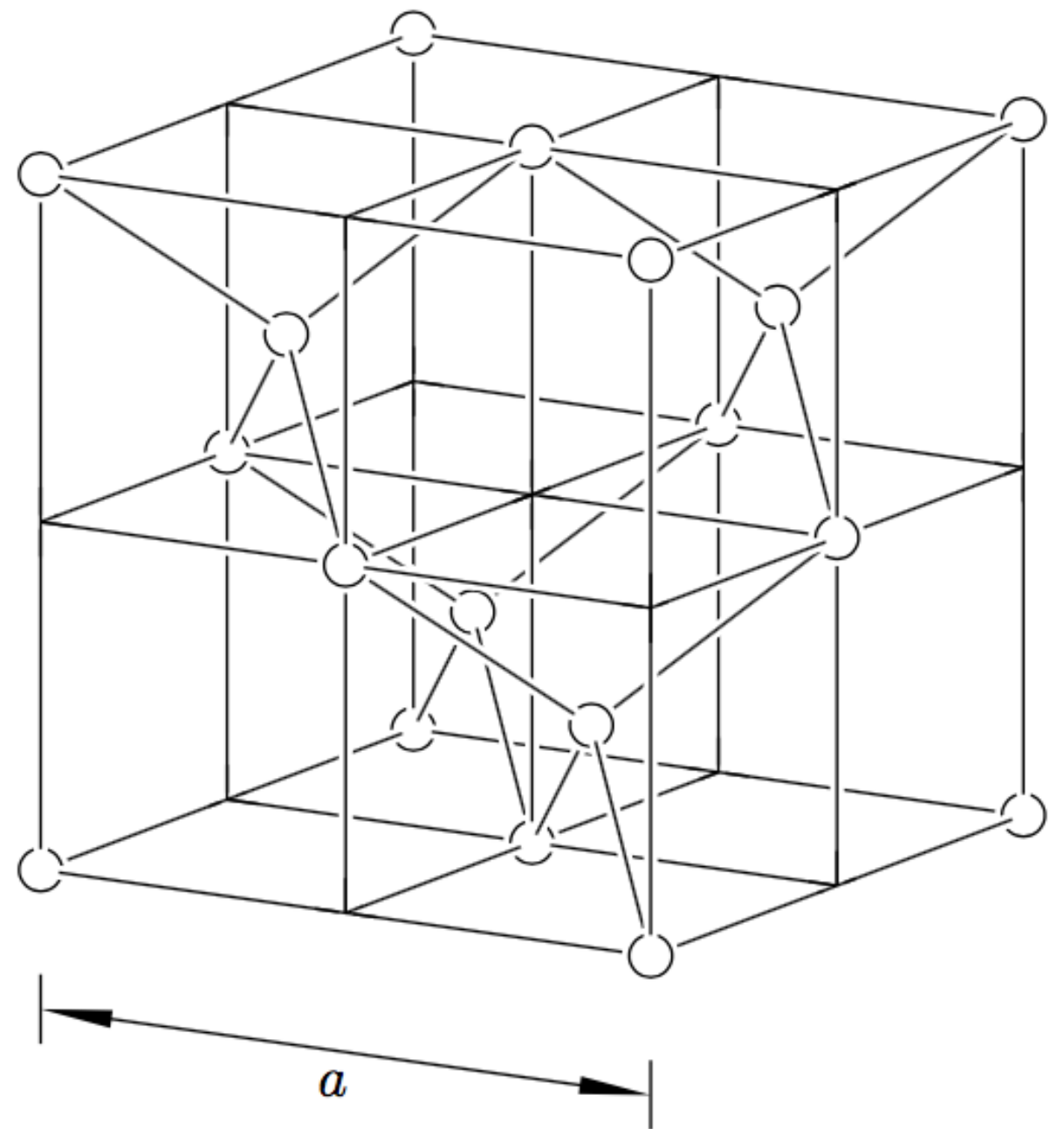
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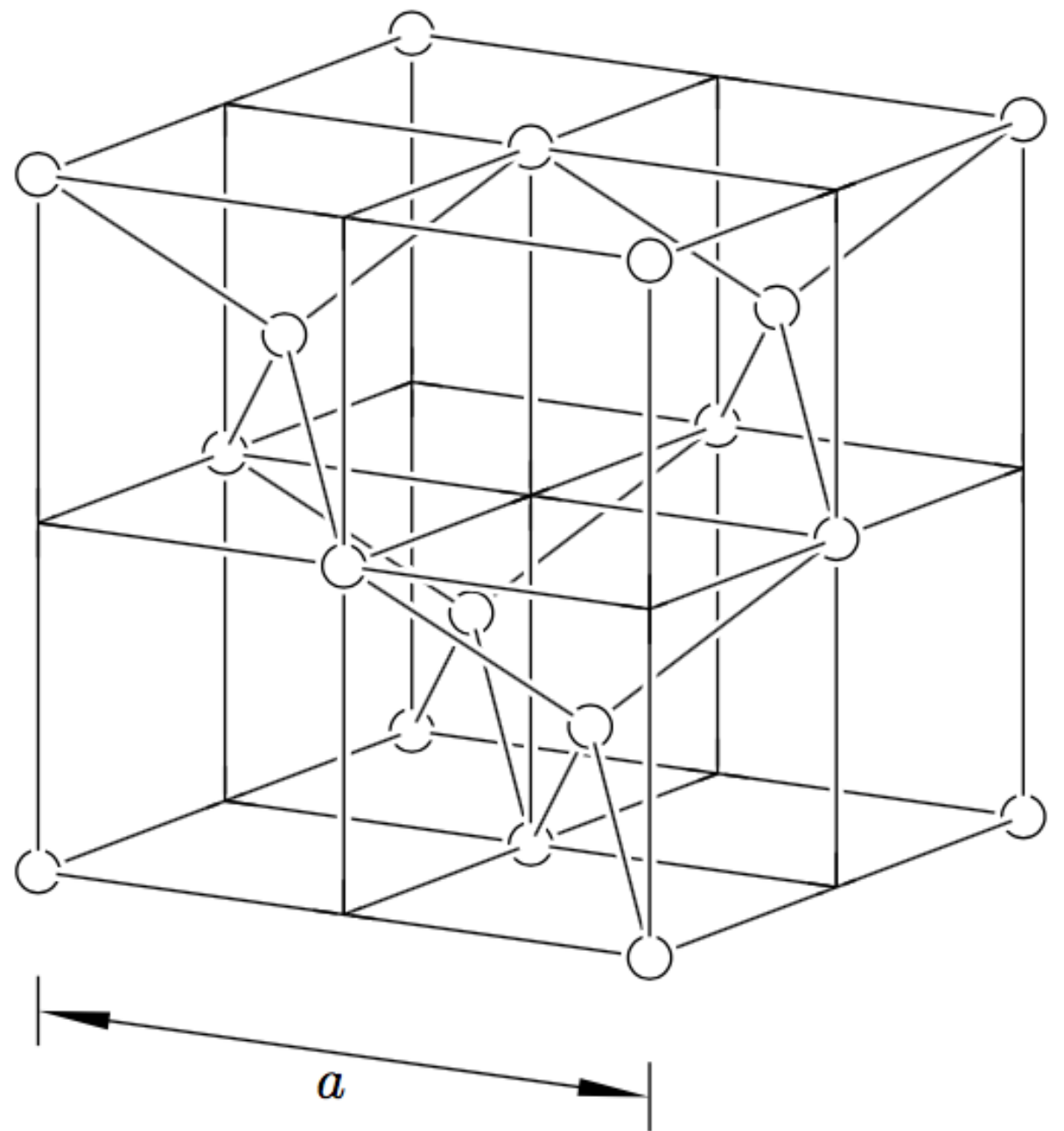
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Glide plane

$$\{C_{4z}^- | \frac{3}{2} \frac{1}{2} 0\}$$

$$\{E | \frac{1}{2} \frac{1}{2} \frac{1}{2}\}$$

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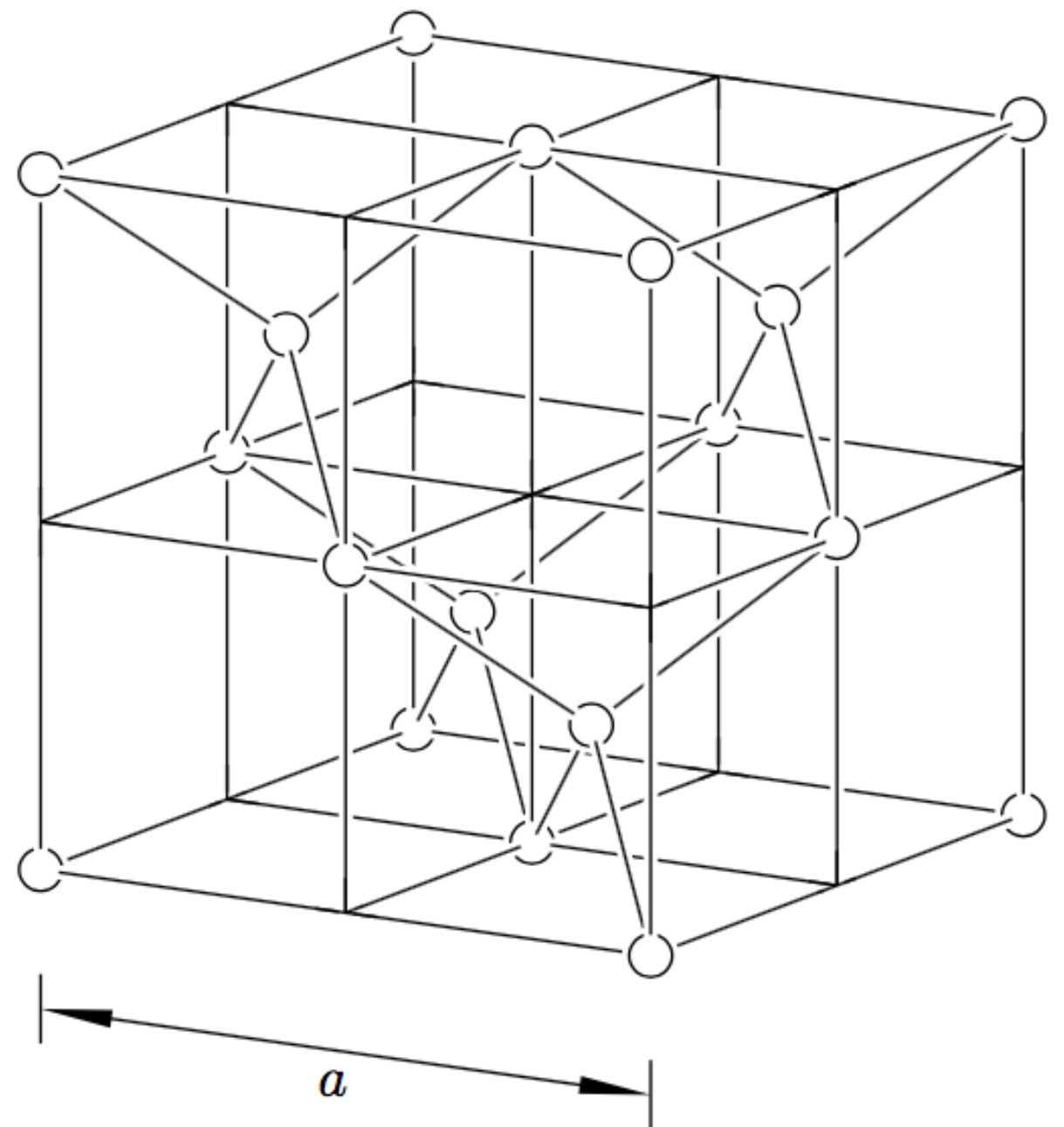
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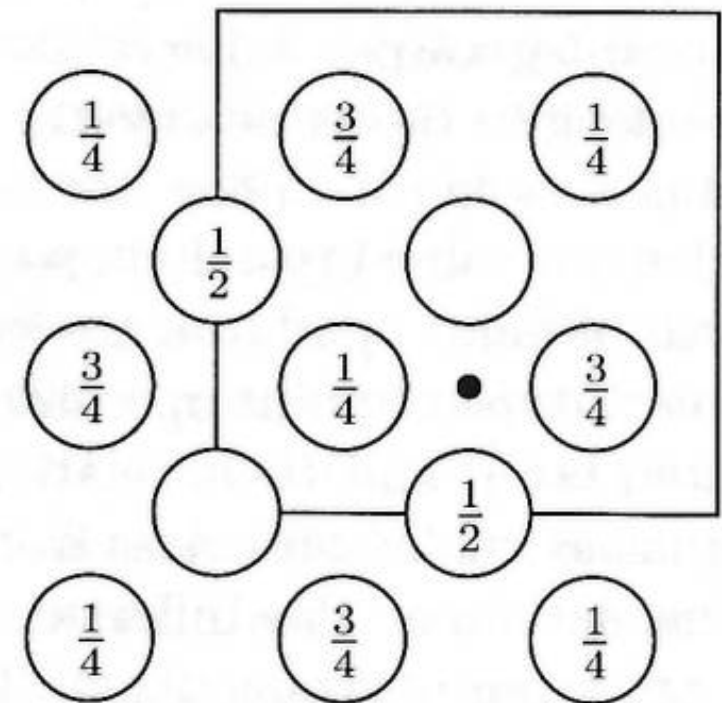
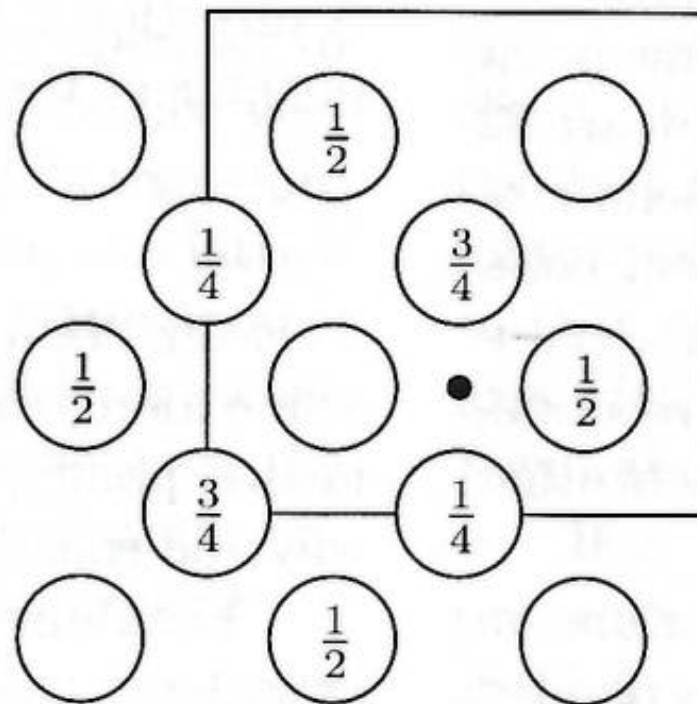
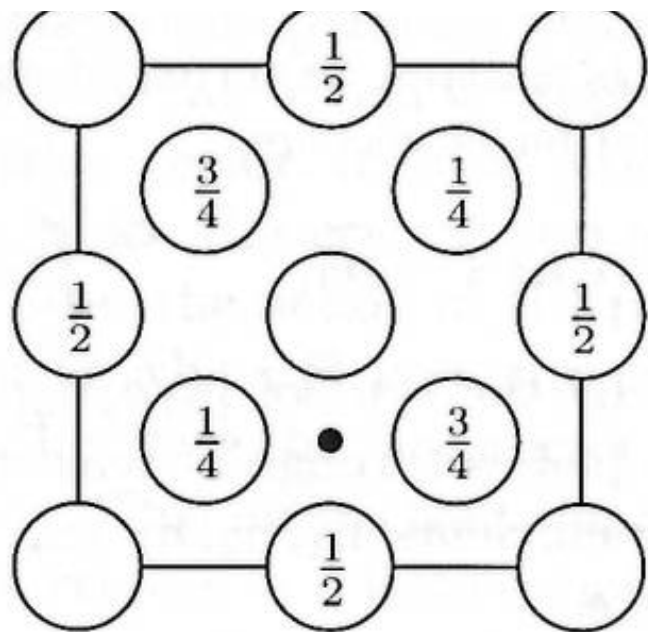
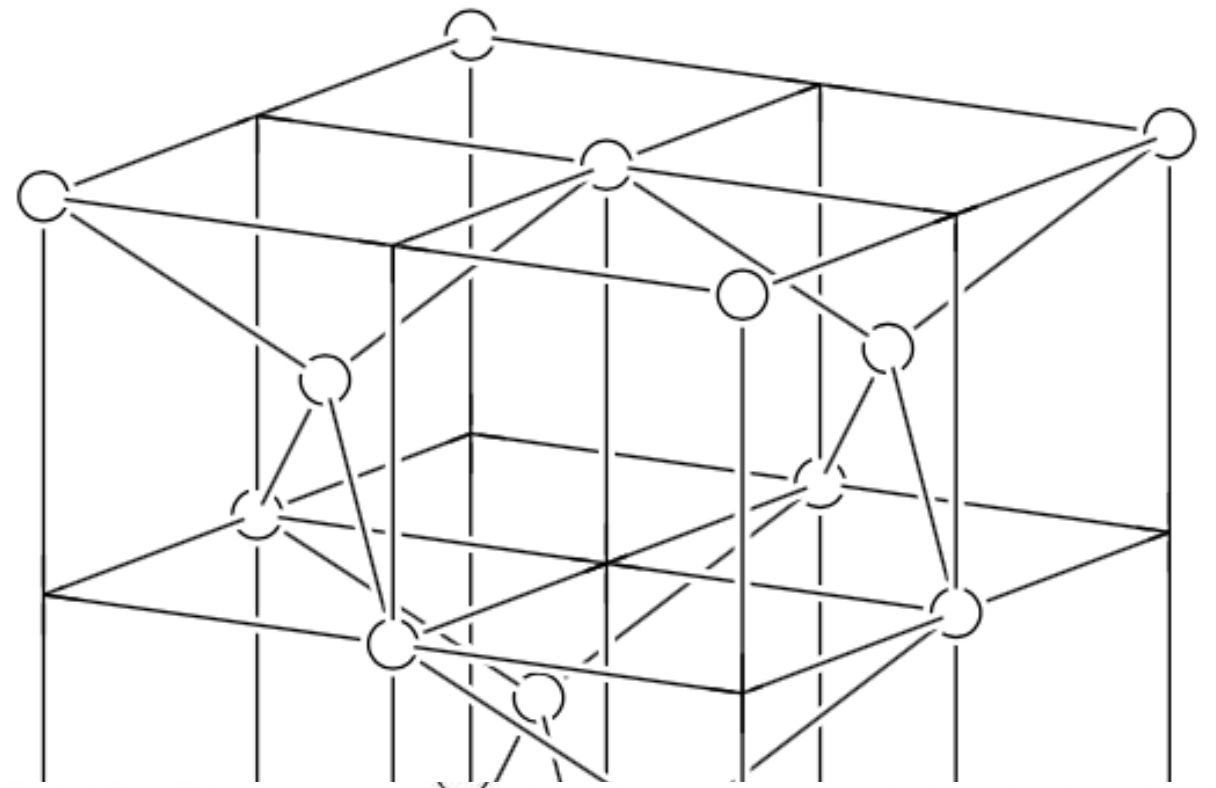
Non-symmorphic

Which are not symmetry operators for diamond?

Screw axis

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$$\{C_{4z}^+ | 00 \frac{1}{4}\}$$



$$\{C_{4z}^- | 0 \frac{1}{2} \frac{1}{2} 0\}$$

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$Fm\bar{3}m$

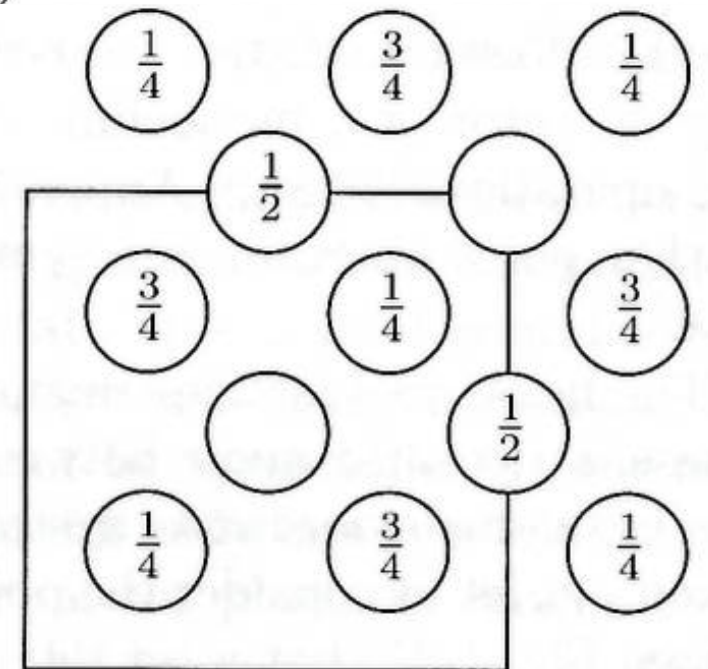
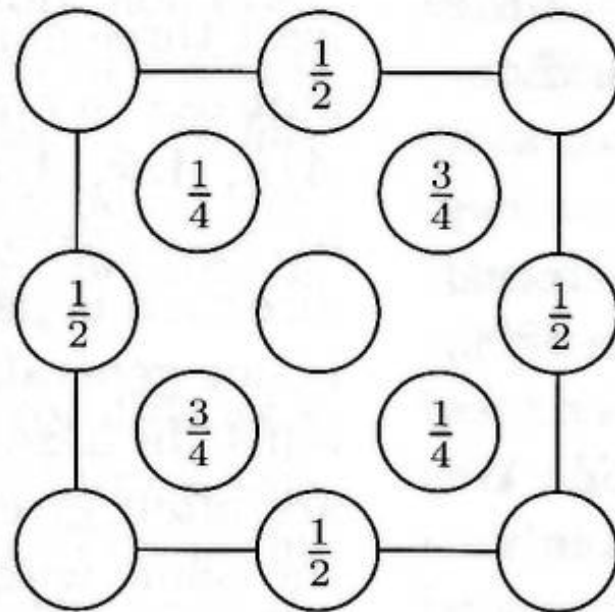
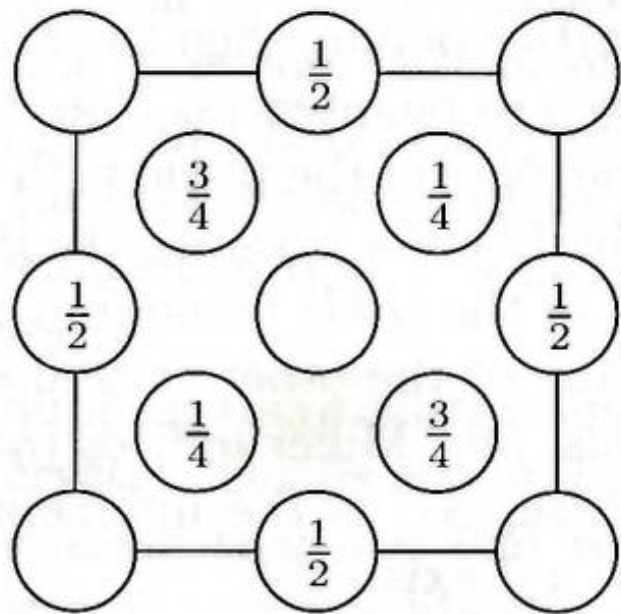
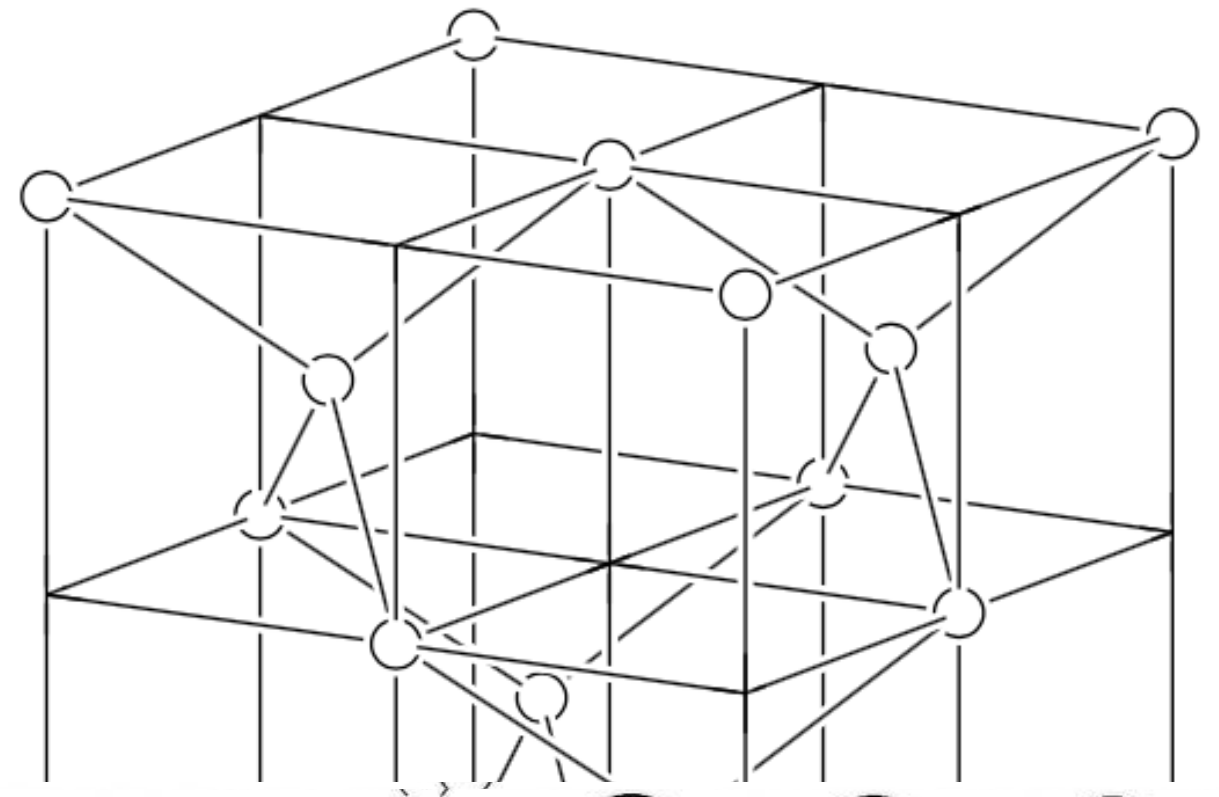
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$$\{E | \frac{1}{2} \frac{1}{2} \frac{1}{2}\}$$

$Fm\bar{3}m$

Non-symmorphic

Wyckoff Positions

You are told that a crystal has the space group shown and that there is one A atom at location $(0,0,0)$ and one B atom at location $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$

$Fm\bar{3}m$

What is the crystal?

- a) NaCl
- b) Zincblend
- c) Diamond
- d) CsCl
- e) fcc

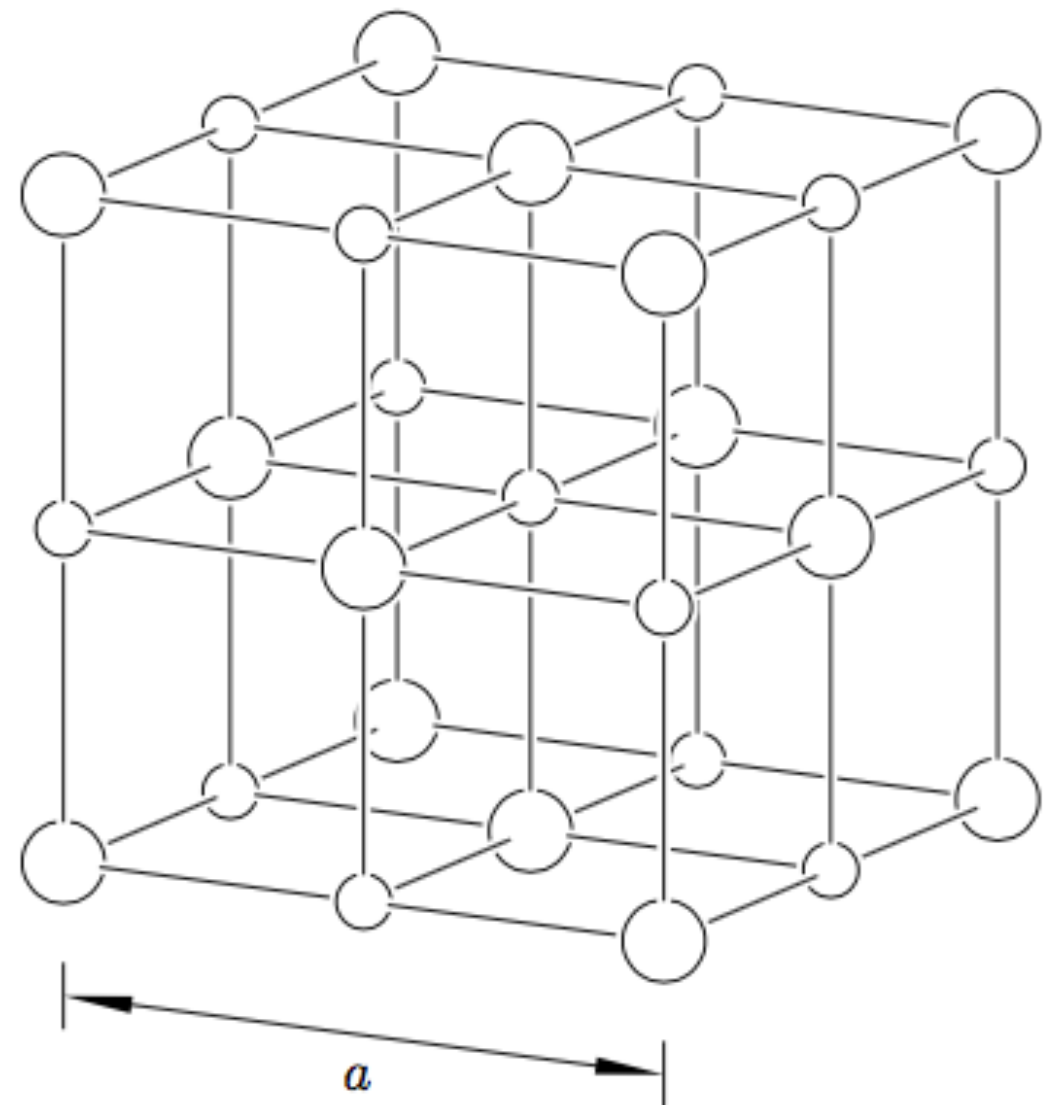
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	Bravais Lattice (only consider the lattice)	Crystal Structure (consider the lattice + the atoms)
Number of Point groups. (Just point operators)	7 (The 7 crystal systems)	32 (The 32 crystallographic point groups)
Number of Space Groups. (now add translations)	14 (The 14 Bravais Lattices)	230 (The 230 space groups)