

1 Day 2: Foundational Postulates of Quantum Mechanics

1. The momentum operator is defined as:

$$\hat{p} = -i\hbar \frac{\partial}{\partial x} \quad (1)$$

Find the eigenstates and eigenvalues for this operator.

2. The displacement operator is defined as:

$$\hat{D}\psi(x) = \psi(x + \xi) \quad (2)$$

Confirm that

$$\psi(x) = e^{\beta x} g(x) \quad (3)$$

where

$$g(x) = g(x + \xi) \quad (4)$$

$\psi(x)$ is an eigenfunction of the displacement operator. What is the eigenvalue associated with this eigenfunction?