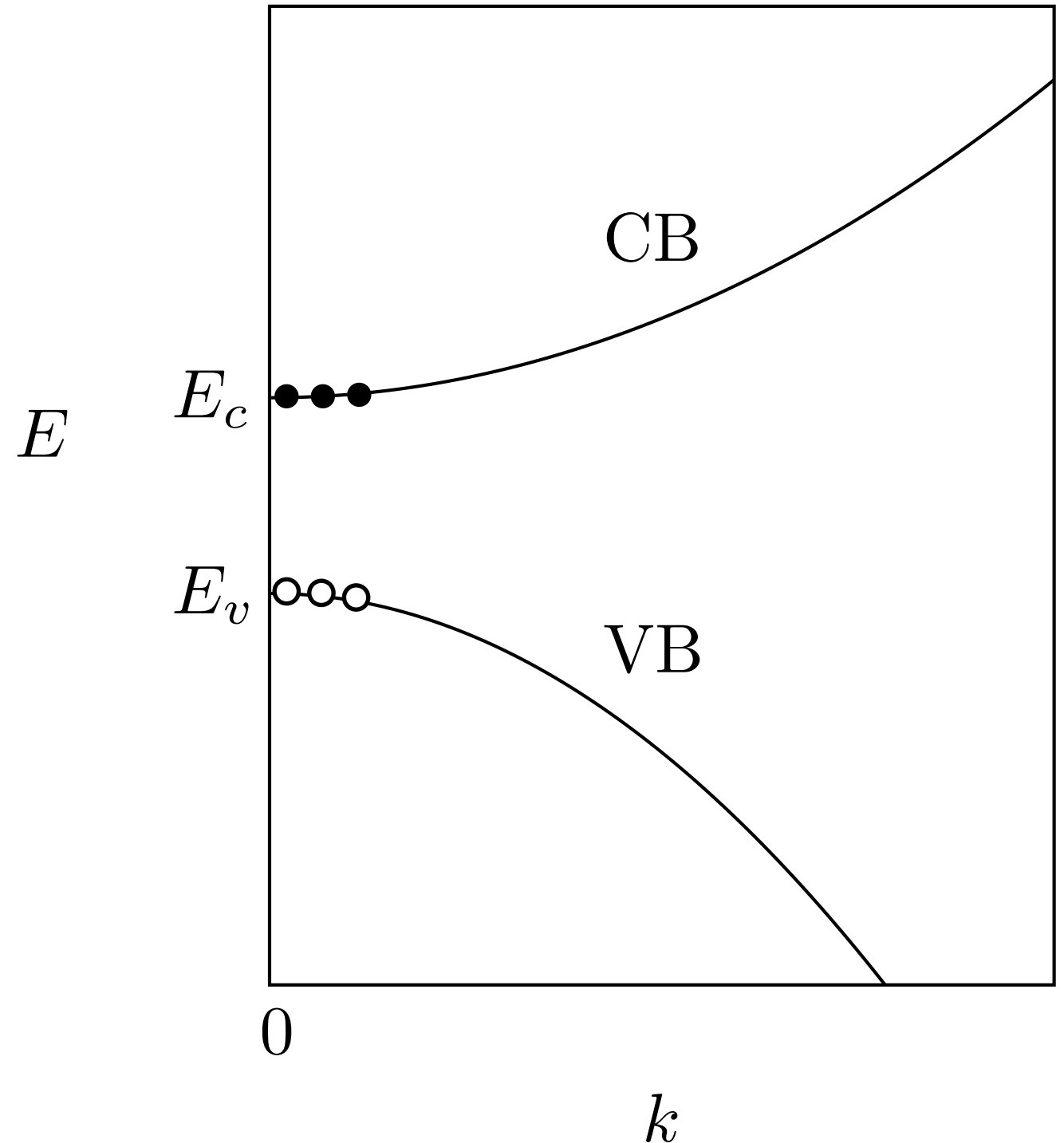


Typical semiconductor bands

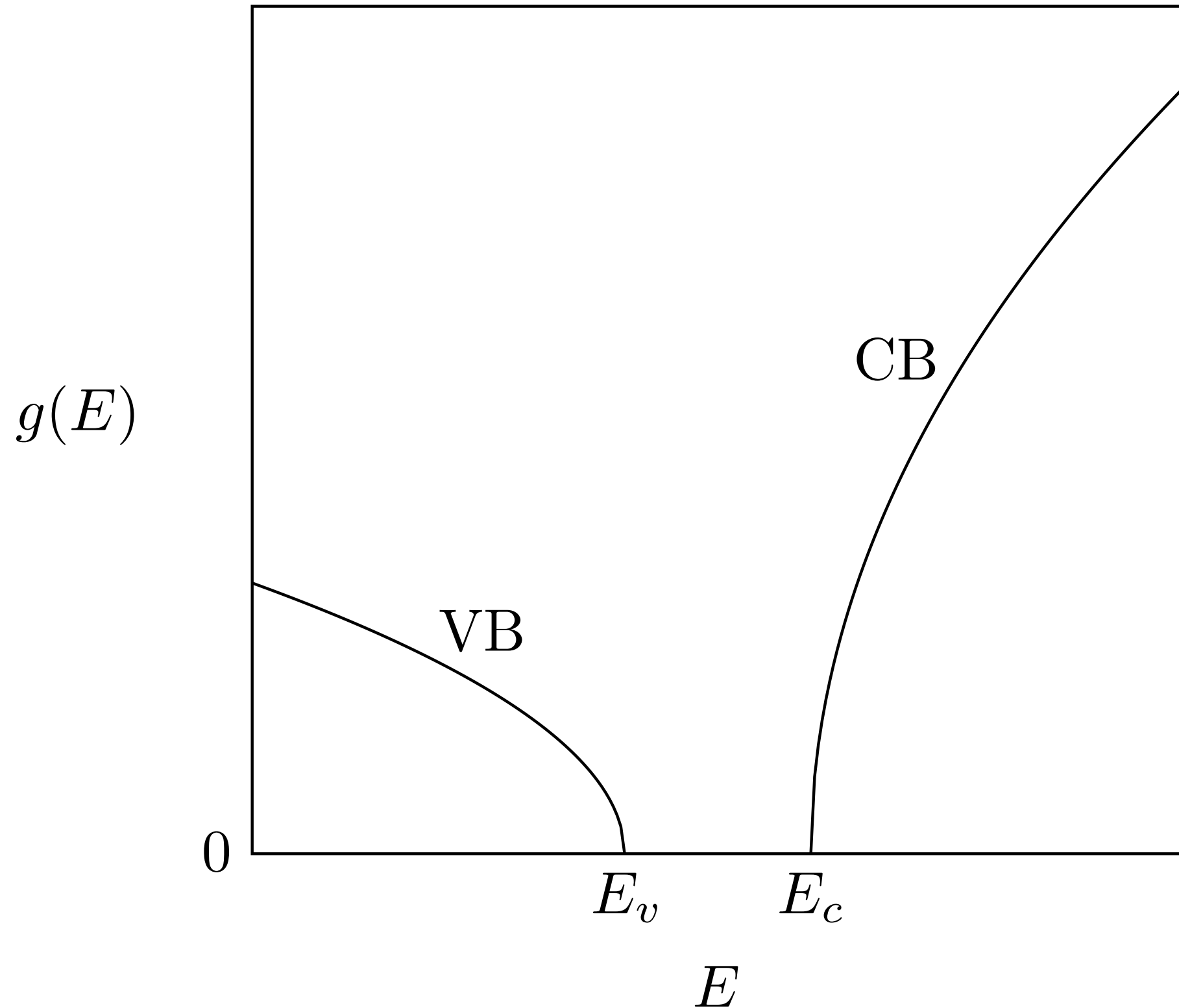
$$E(k) = E(0) + \left. \frac{dE}{dk} \right|_{k=0} k + \frac{1}{2} \left. \frac{d^2 E}{dk^2} \right|_{k=0} k^2 + \dots$$

$$E = E_c + \frac{\hbar^2}{2m_n^*} k^2$$

$$E = E_v - \frac{\hbar^2}{2m_p^*} k^2$$

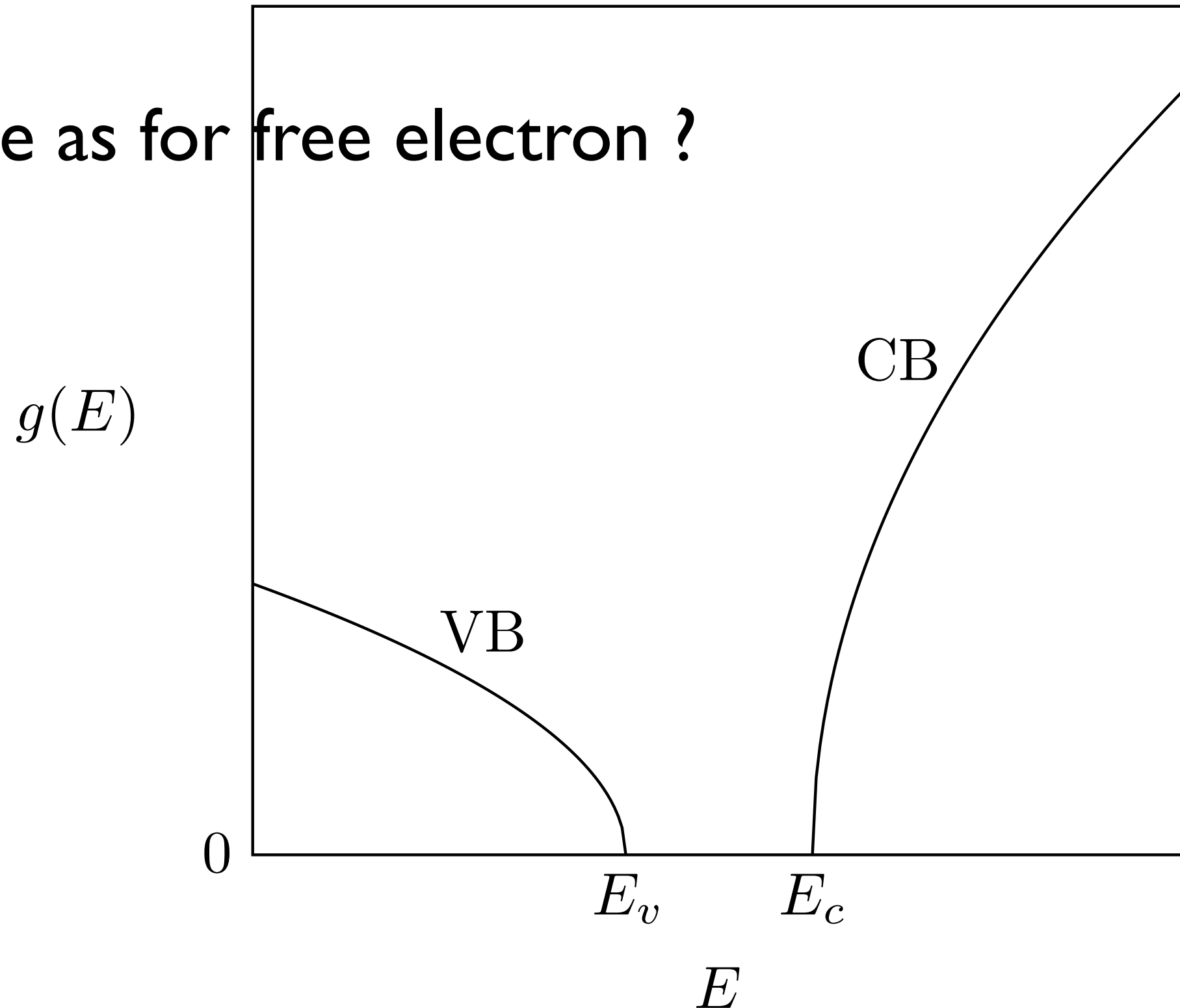


Density of states



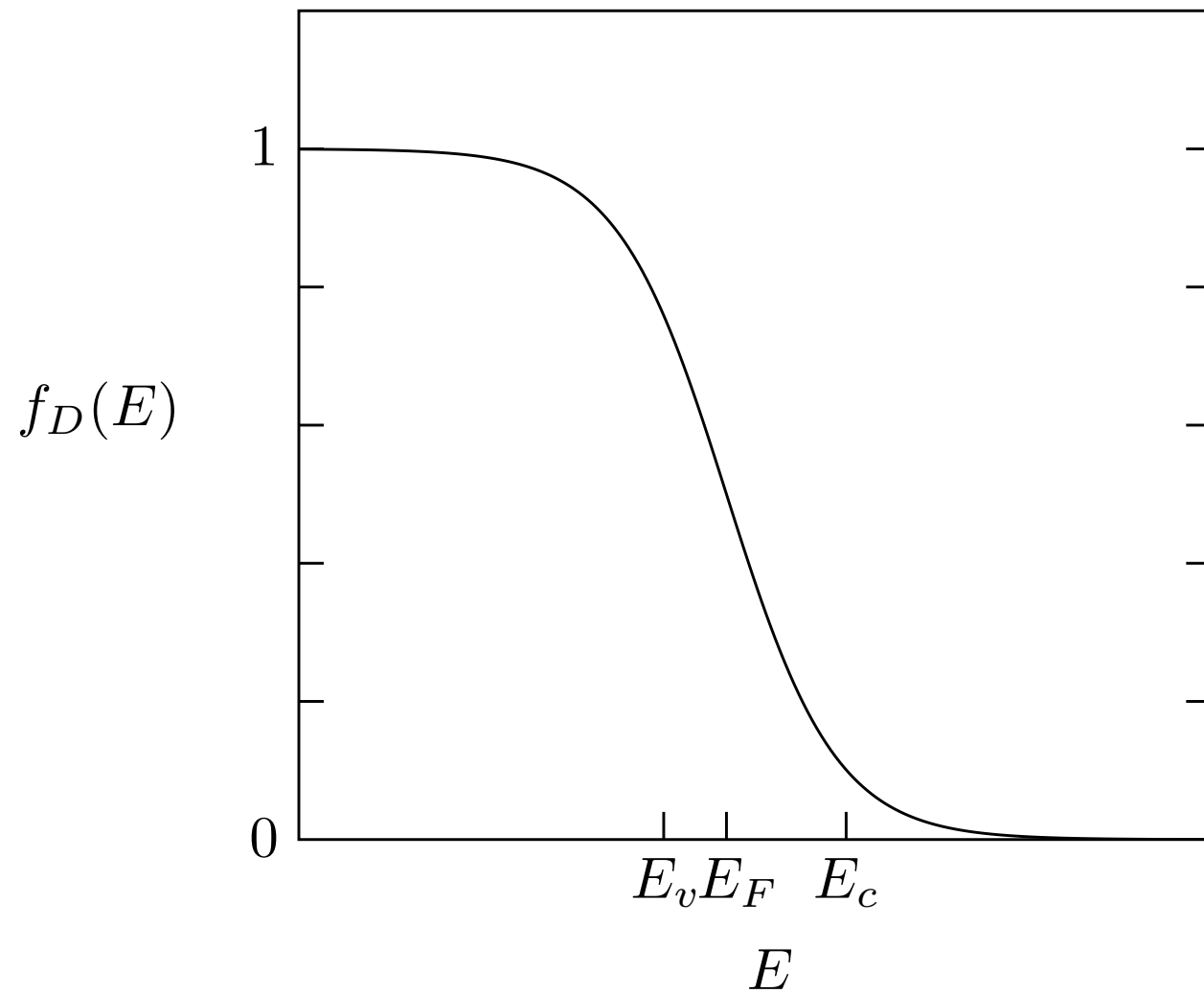
Density of states

Same as for free electron ?



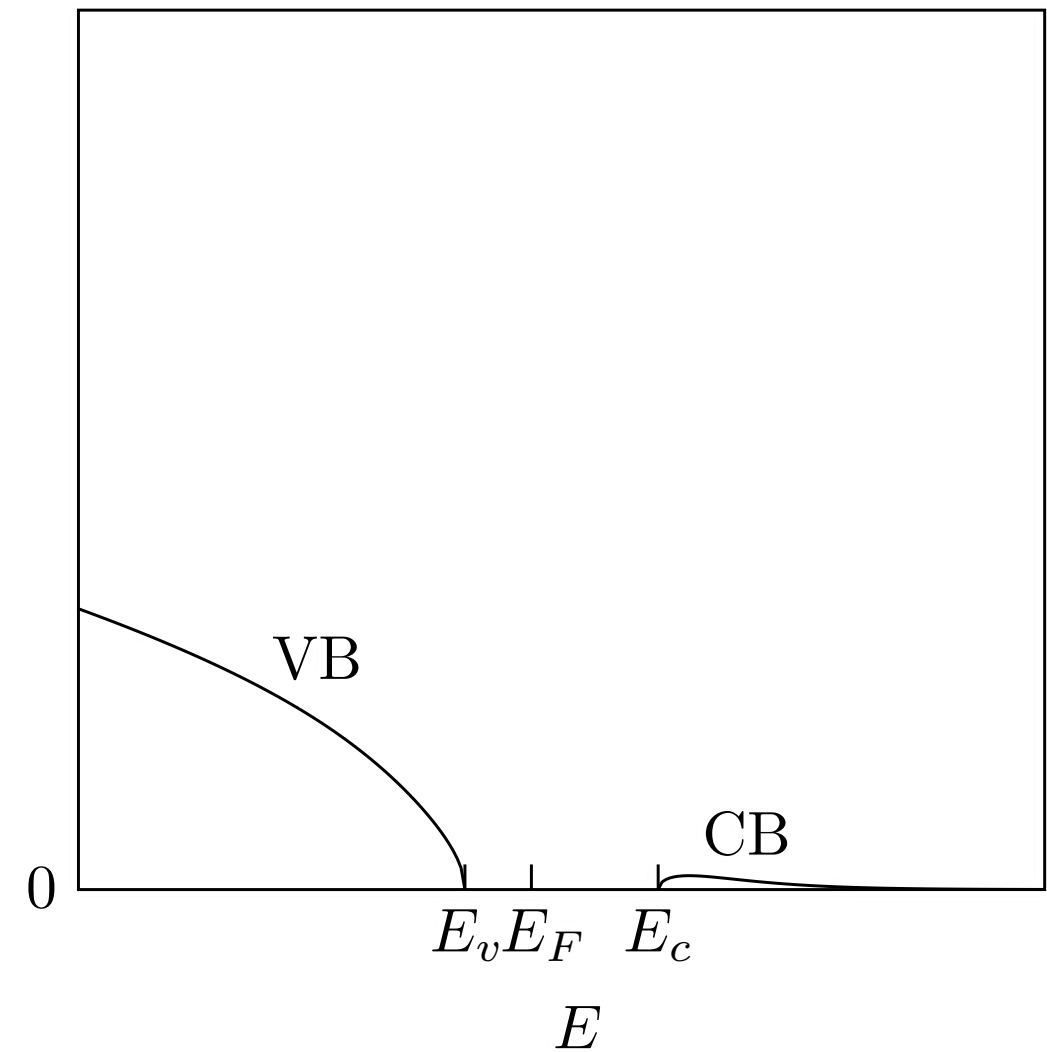
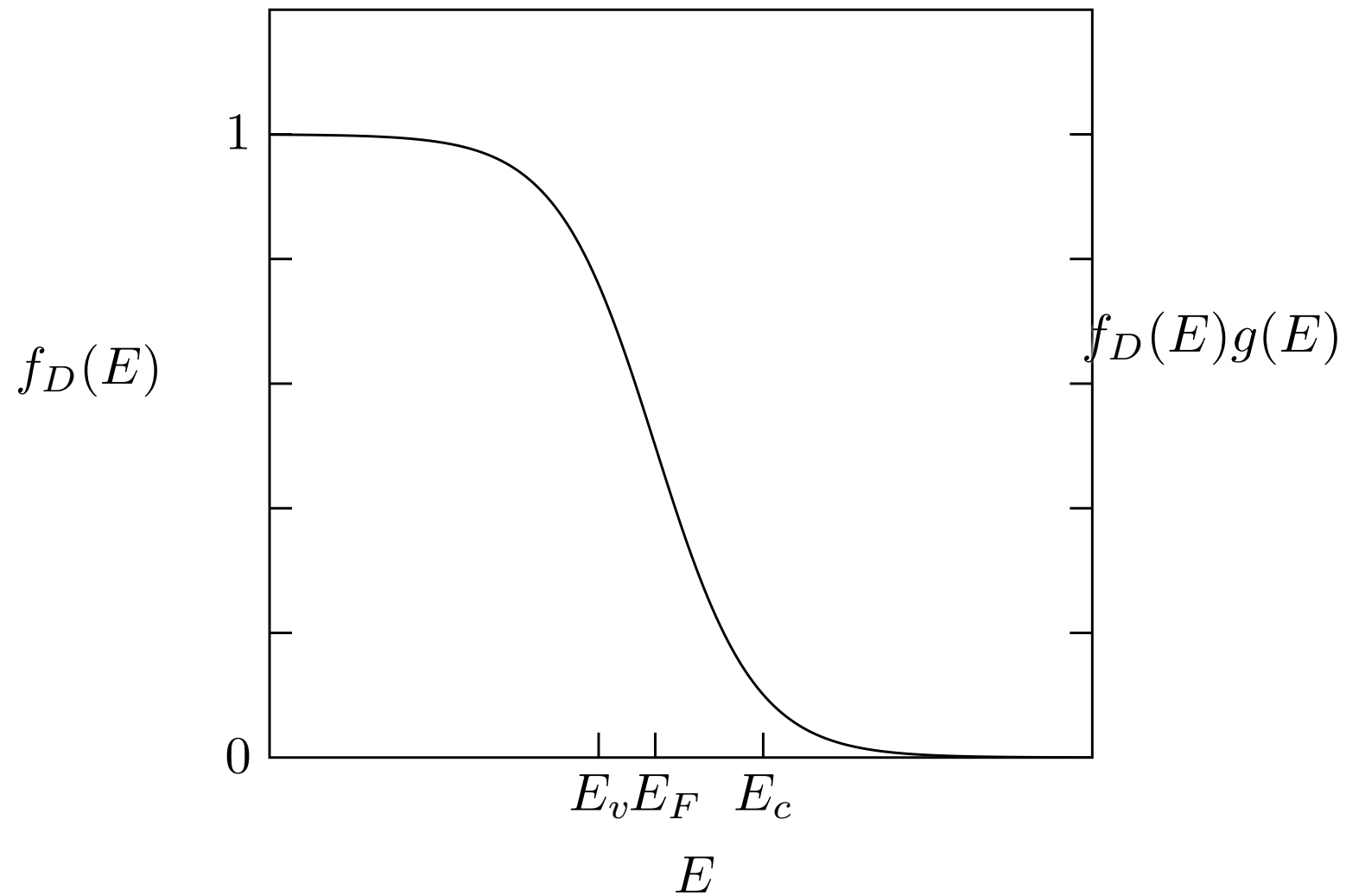
Band occupation at

$$T \neq 0$$



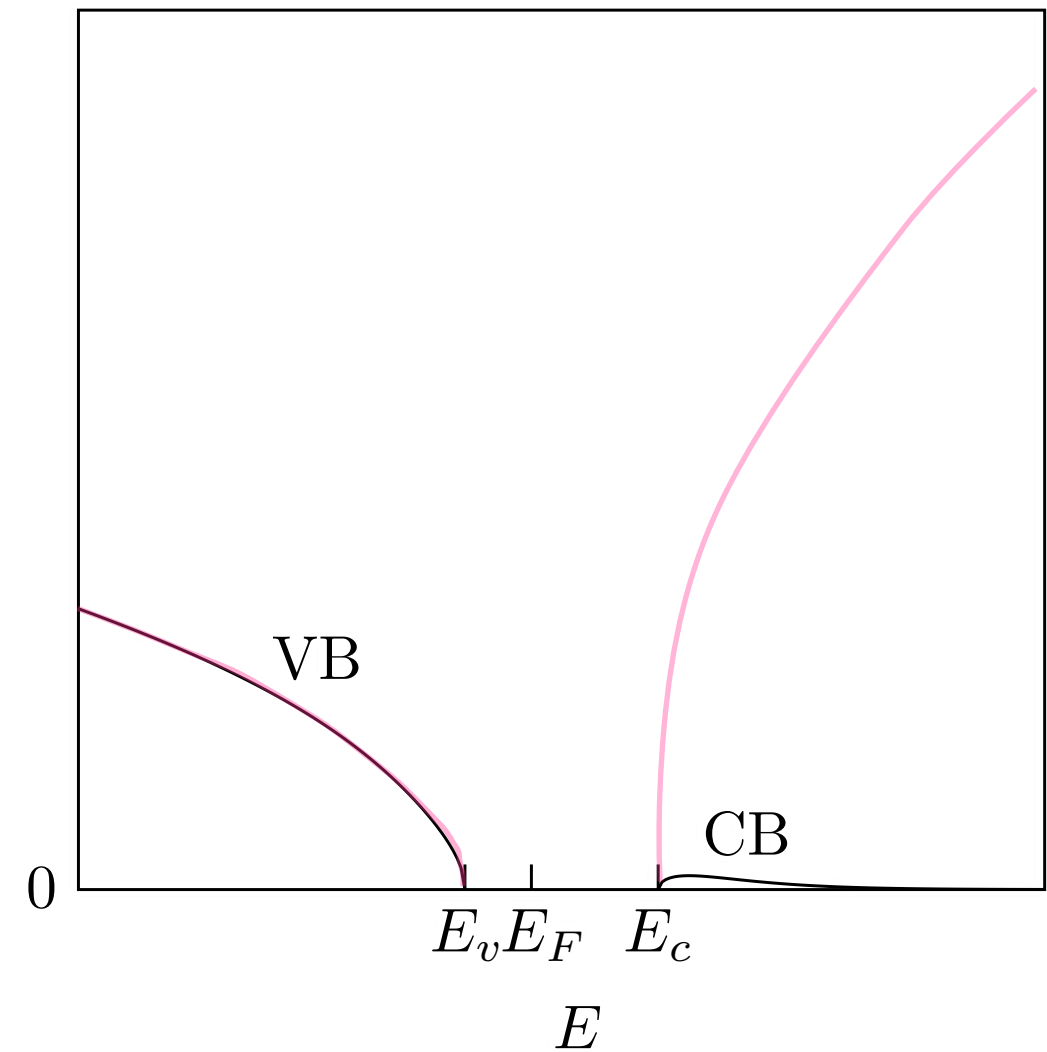
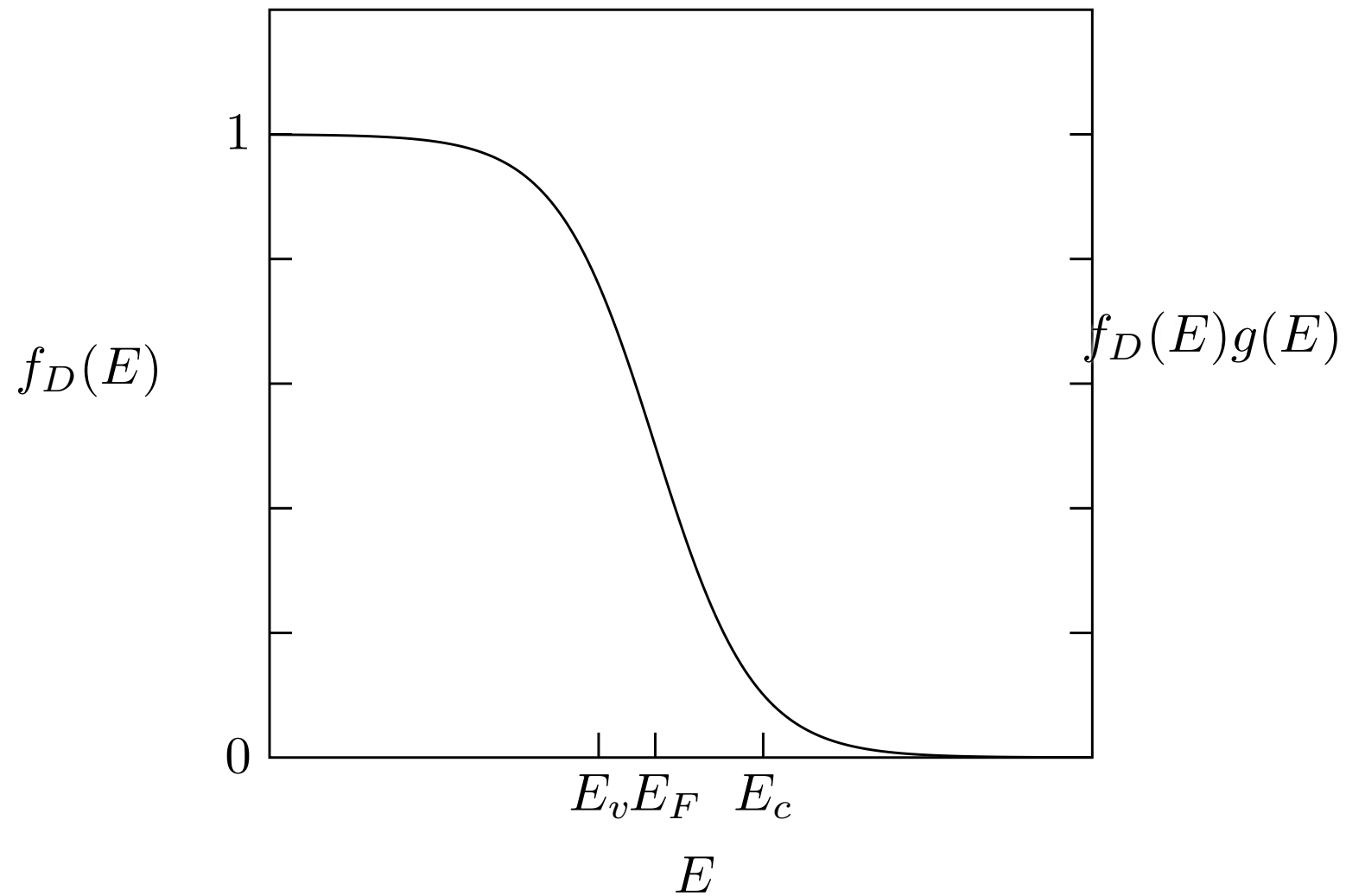
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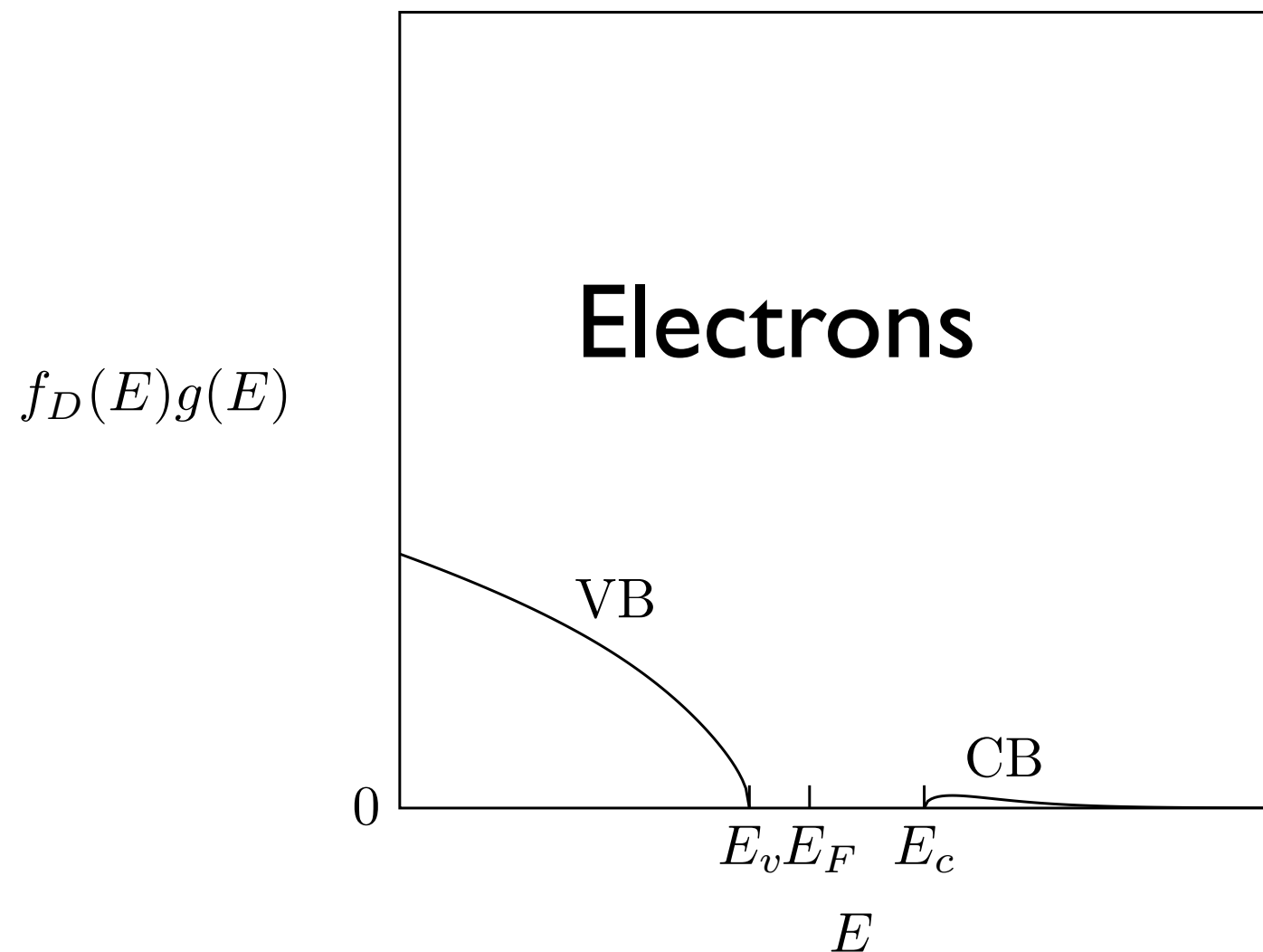
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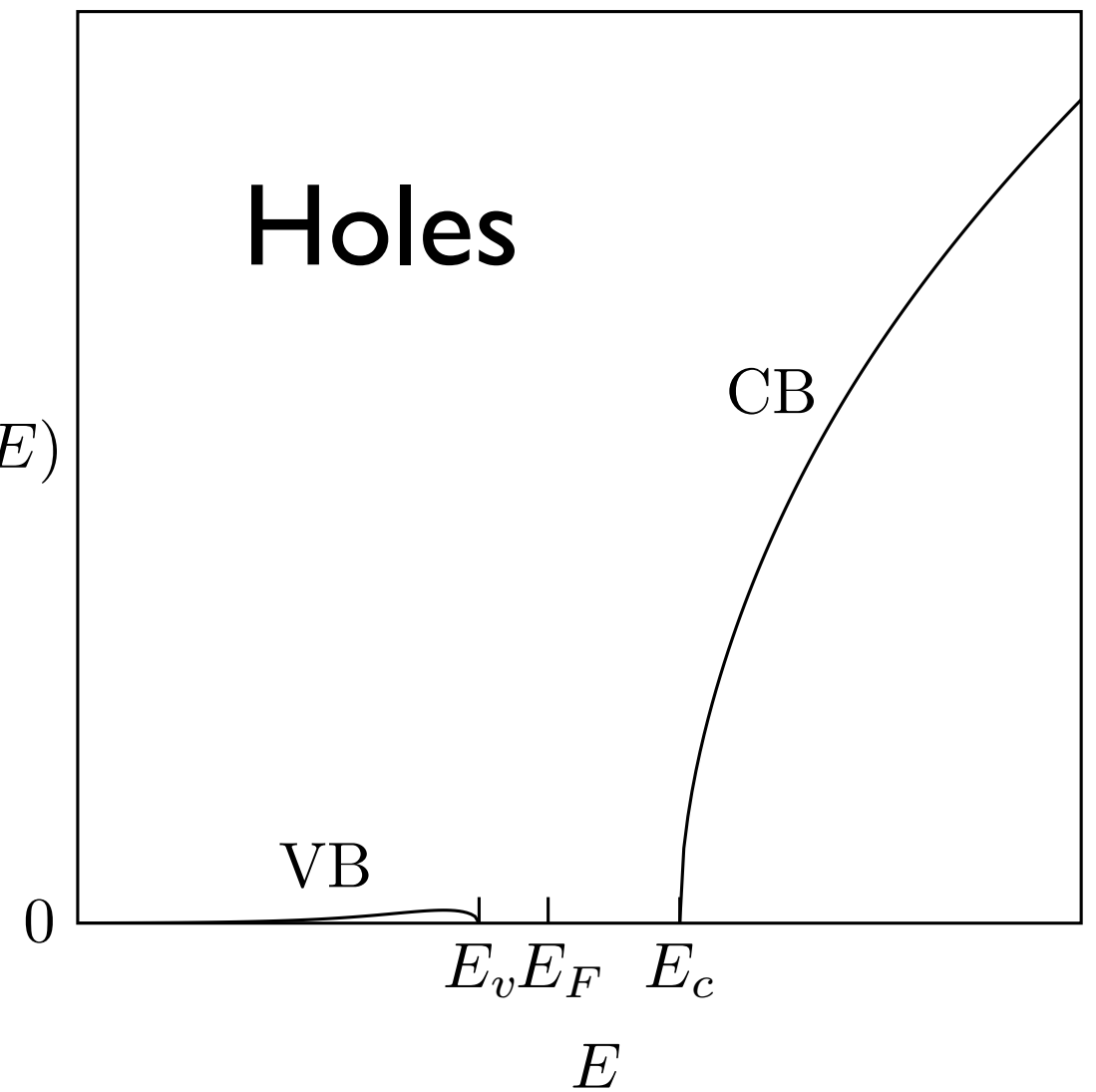
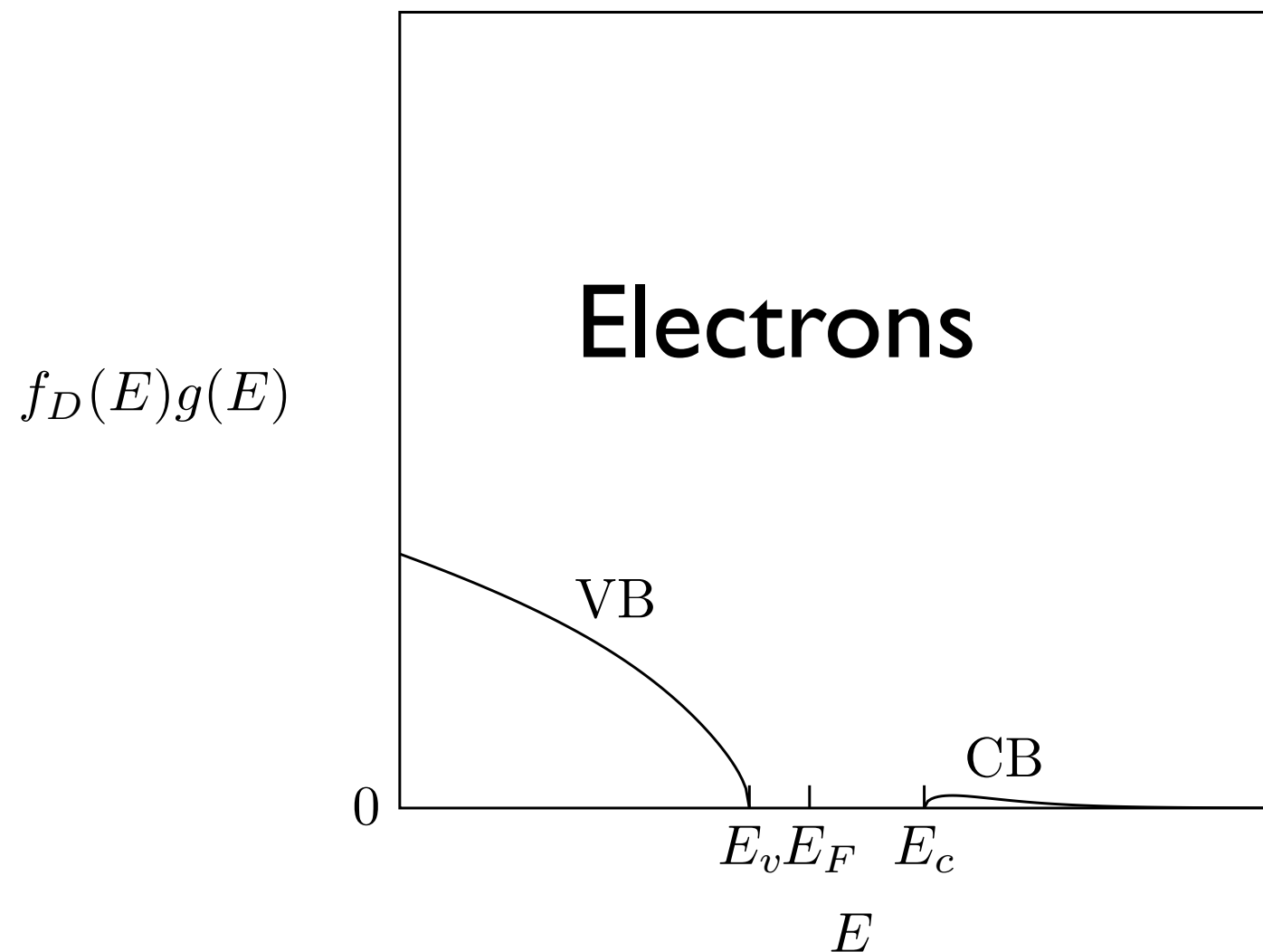
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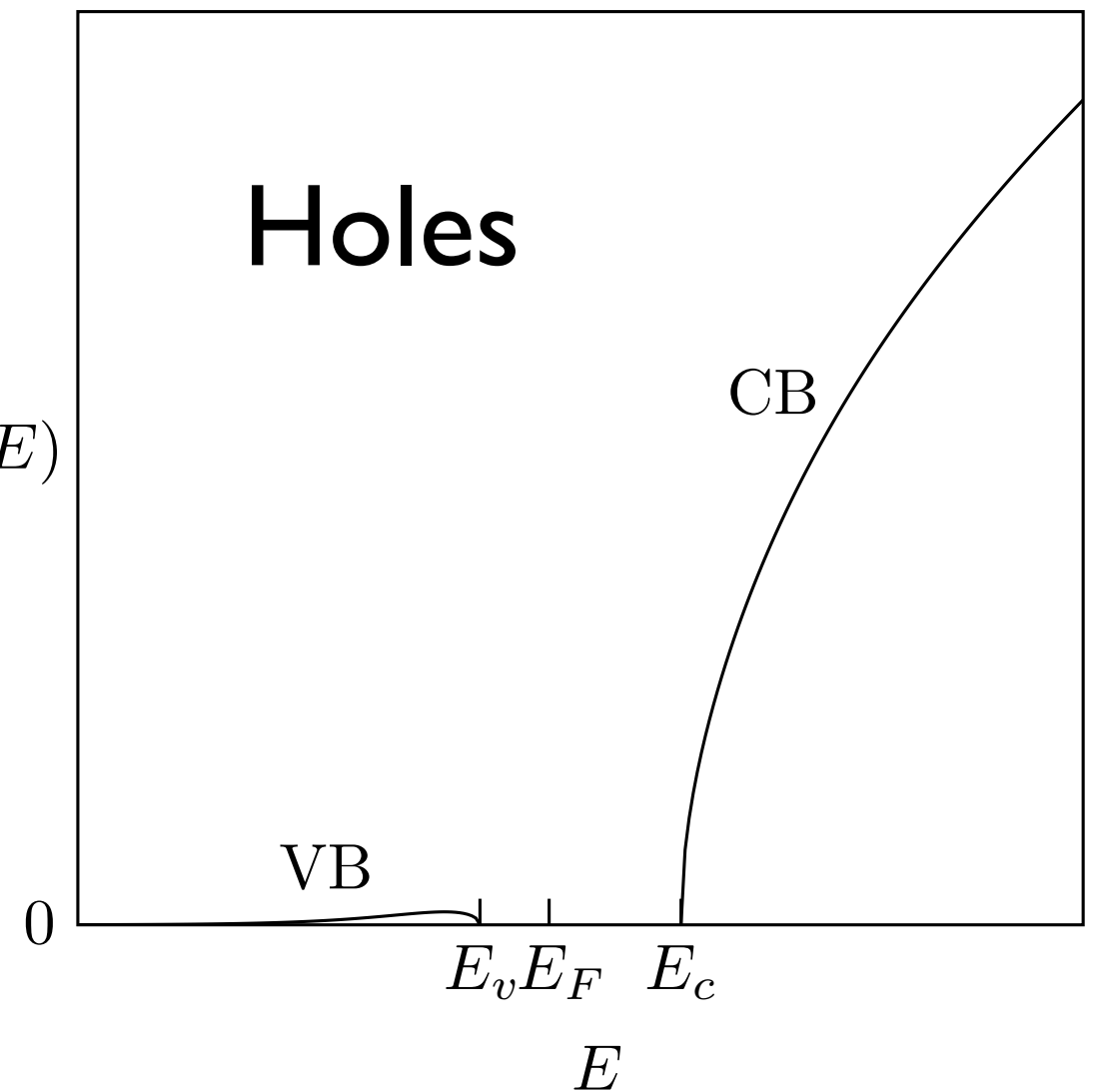
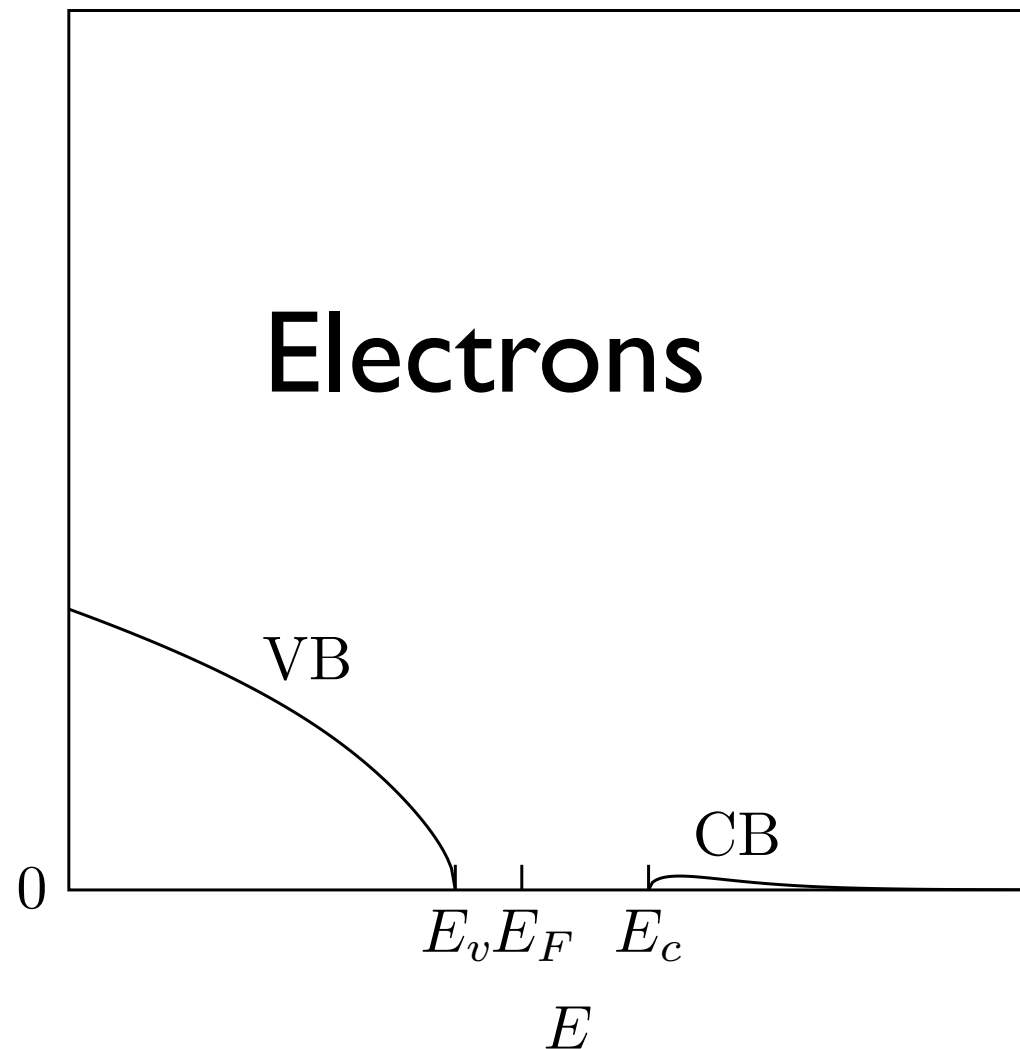
Band occupation at

$$T \neq 0$$

Why $1 - f_D$?

$$[1 - f_D(E)]g(E)$$

$$f_D(E)g(E)$$



$$n = \frac{1}{V} \int f_D(E) g(E) dE$$

$$= 2 \left(\frac{m_n^* k_B T}{2\pi \hbar^2} \right)^{3/2} \exp \left(-\frac{E_c - E_F}{k_B T} \right)$$

$$p = 2 \left(\frac{m_p^* k_B T}{2\pi \hbar^2} \right)^{3/2} \exp \left(-\frac{E_F - E_v}{k_B T} \right)$$

Set $n = p$

$$E_f \approx \frac{1}{2} (E_c + E_v)$$

At 300 K

$$n_i = 9.8 \times 10^{15}$$

$$n_i = \sqrt{N_c N_v} \exp \left(-\frac{E_g}{2k_B T} \right)$$

At 373 K

$$n_i = 9.5 \times 10^{17}$$

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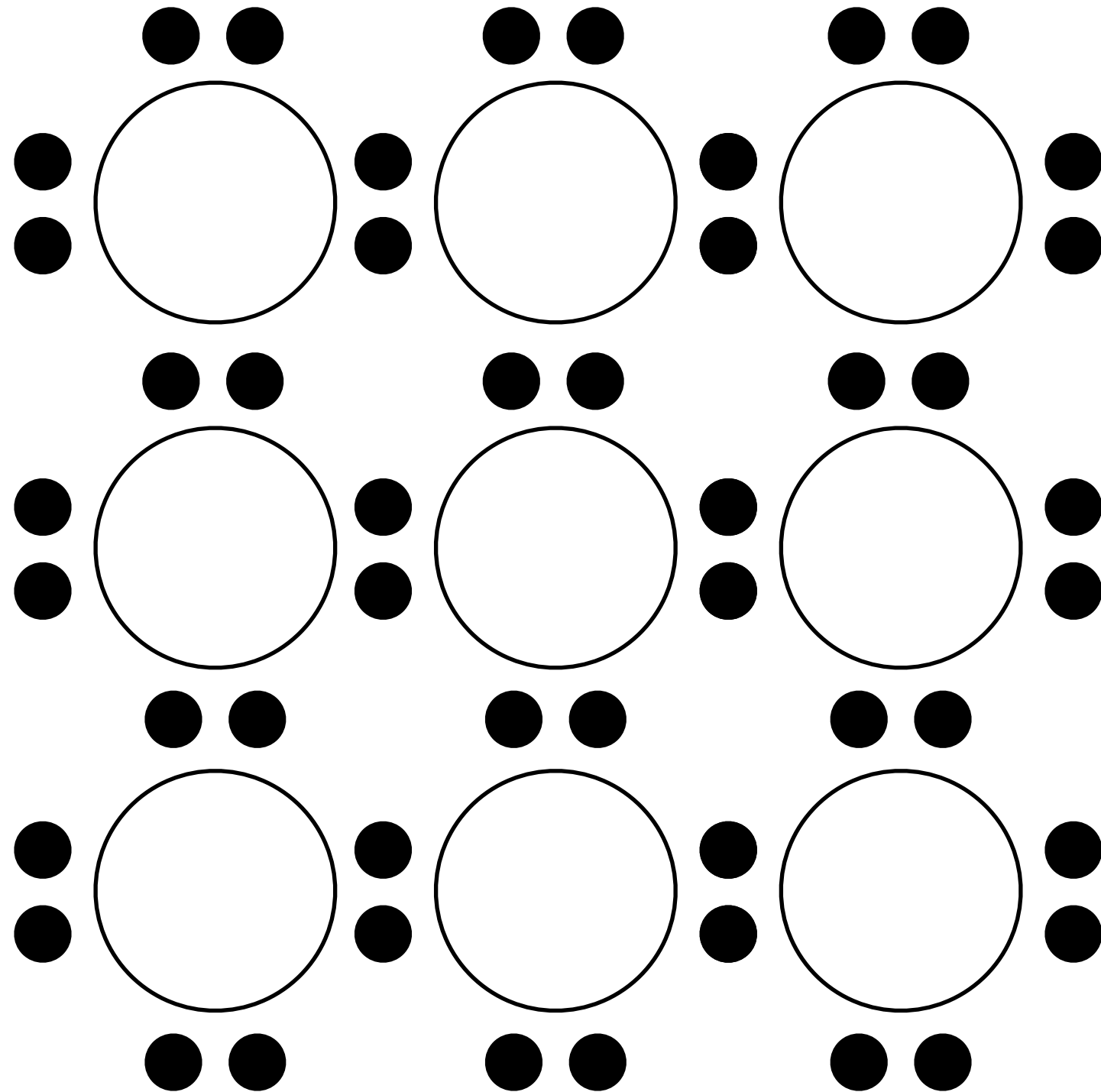
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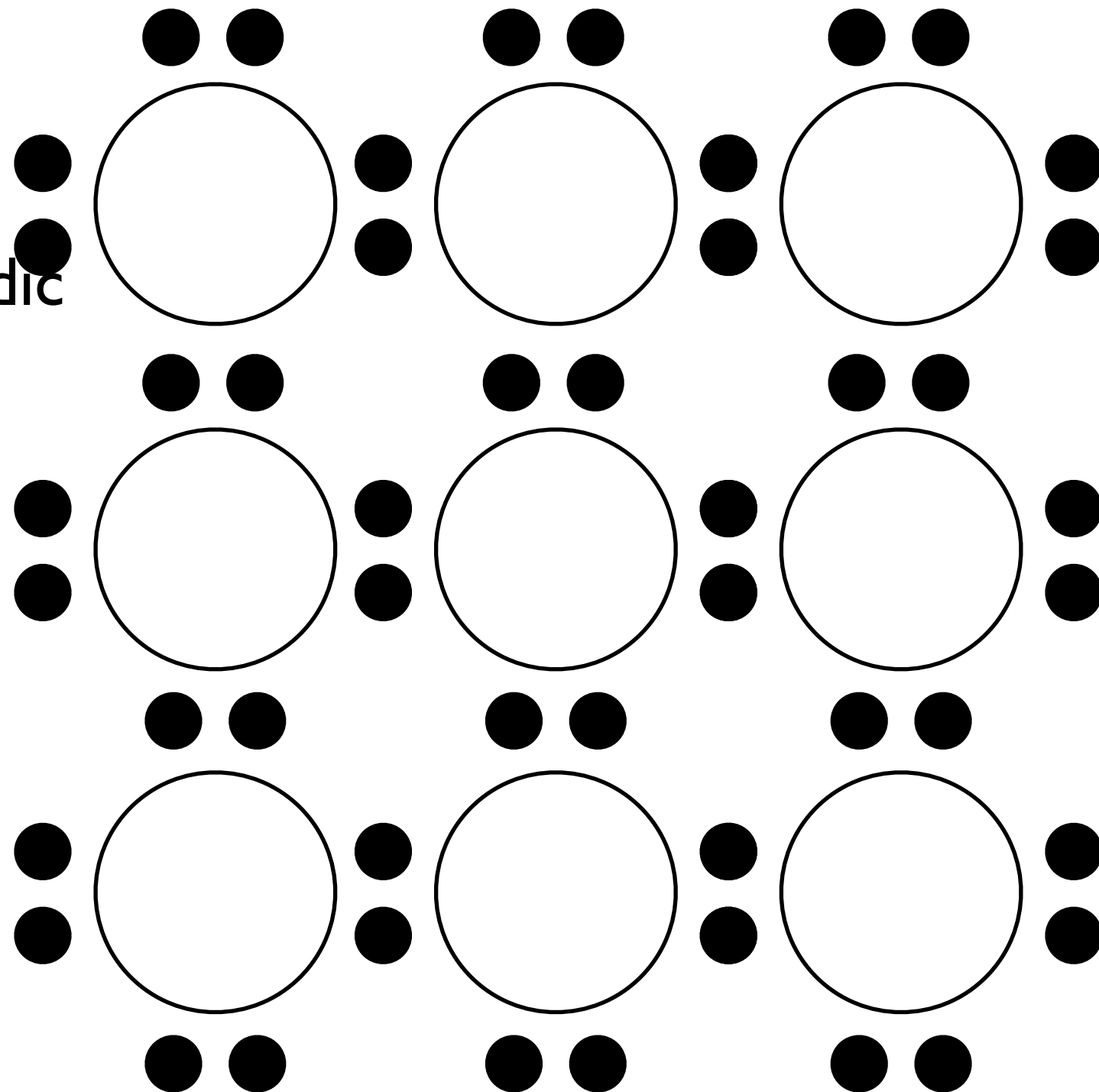
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2D Model of a Semiconductor



2D Model of a Semiconductor

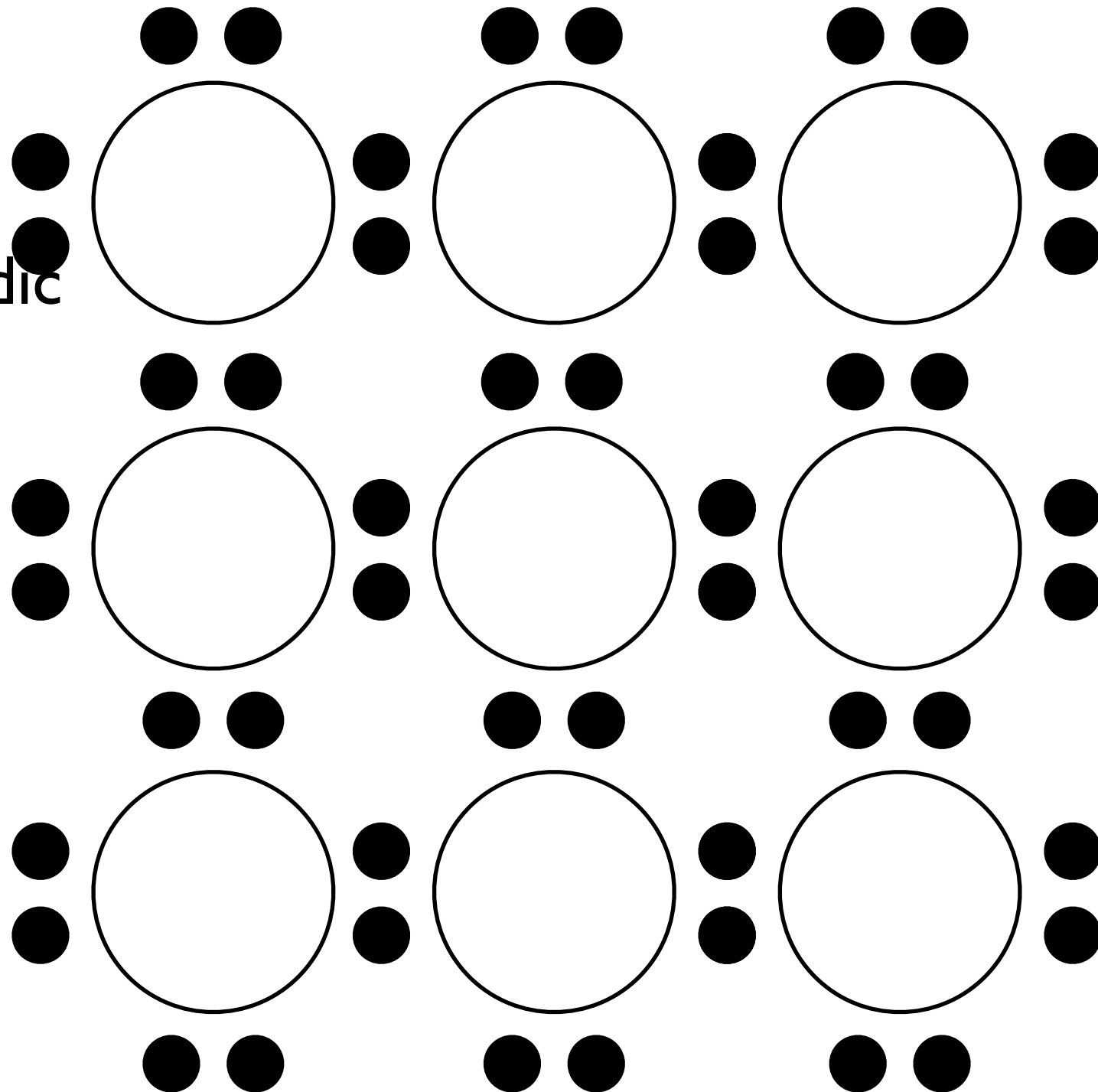
Where is
silicon
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table?



2D Model of a Semiconductor

Where is
silicon
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Why is that
significant?

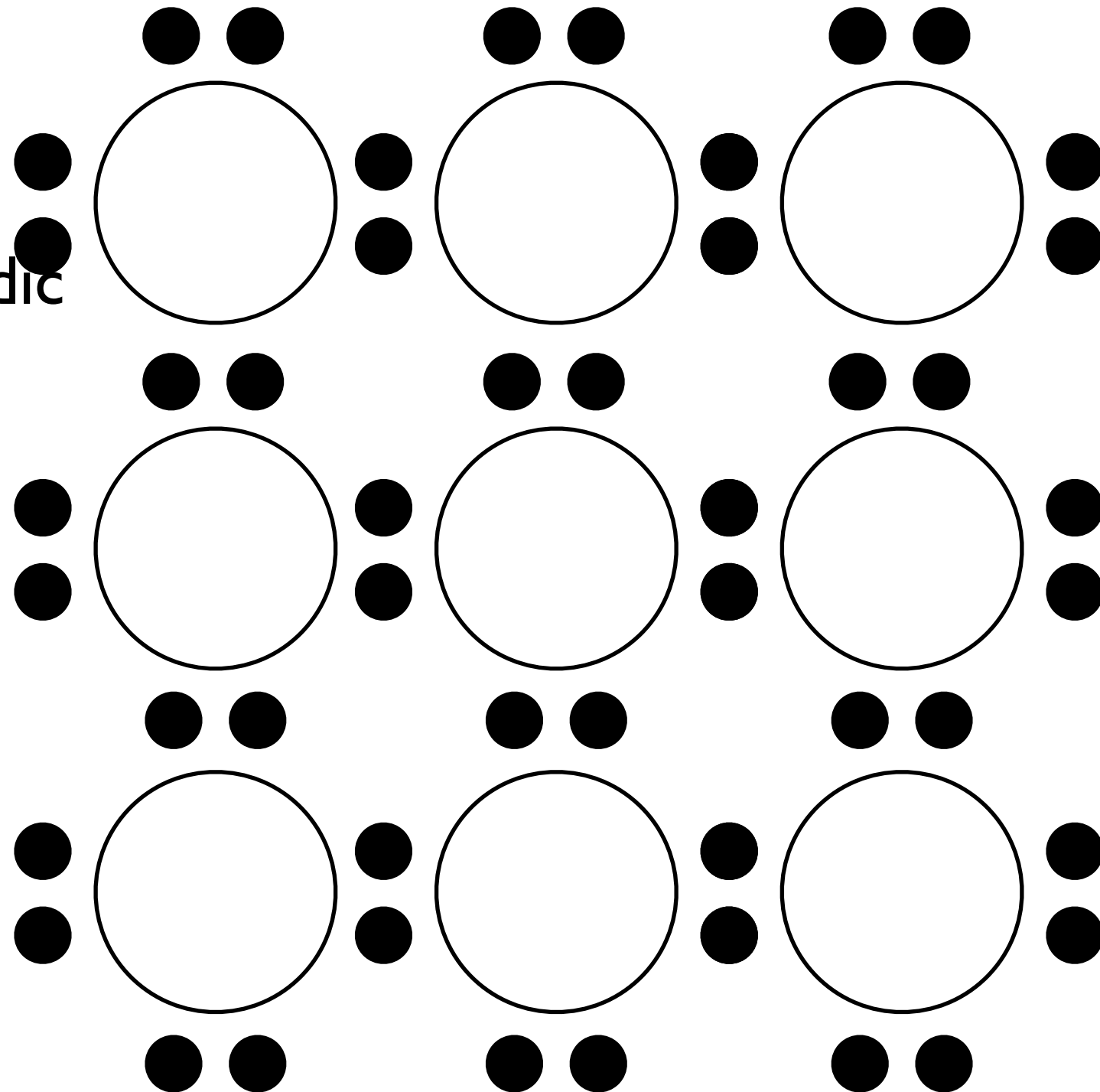


2D Model of a Semiconductor

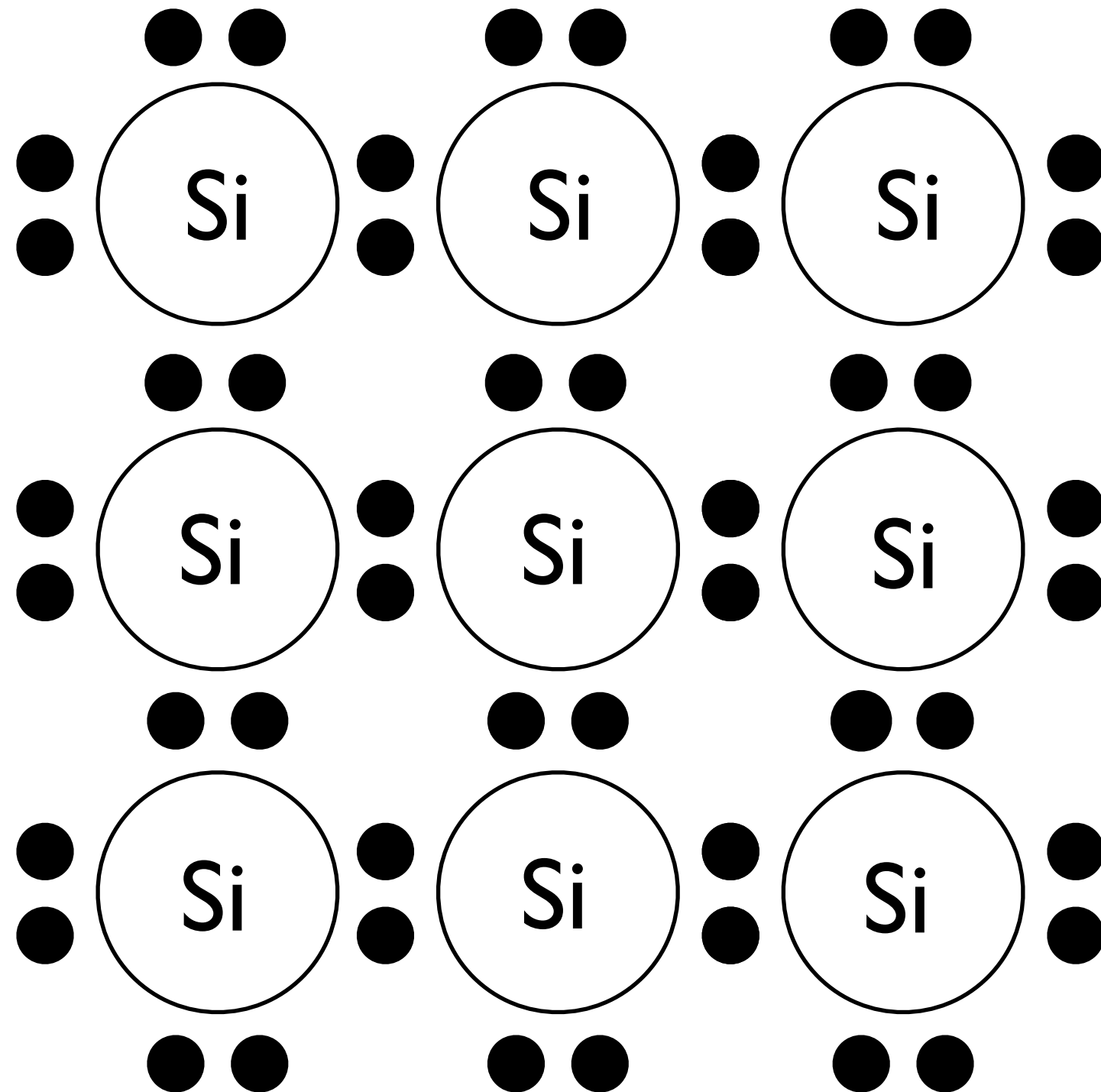
Where is
silicon
on the periodic
table?

What role
does temper-
ature play?

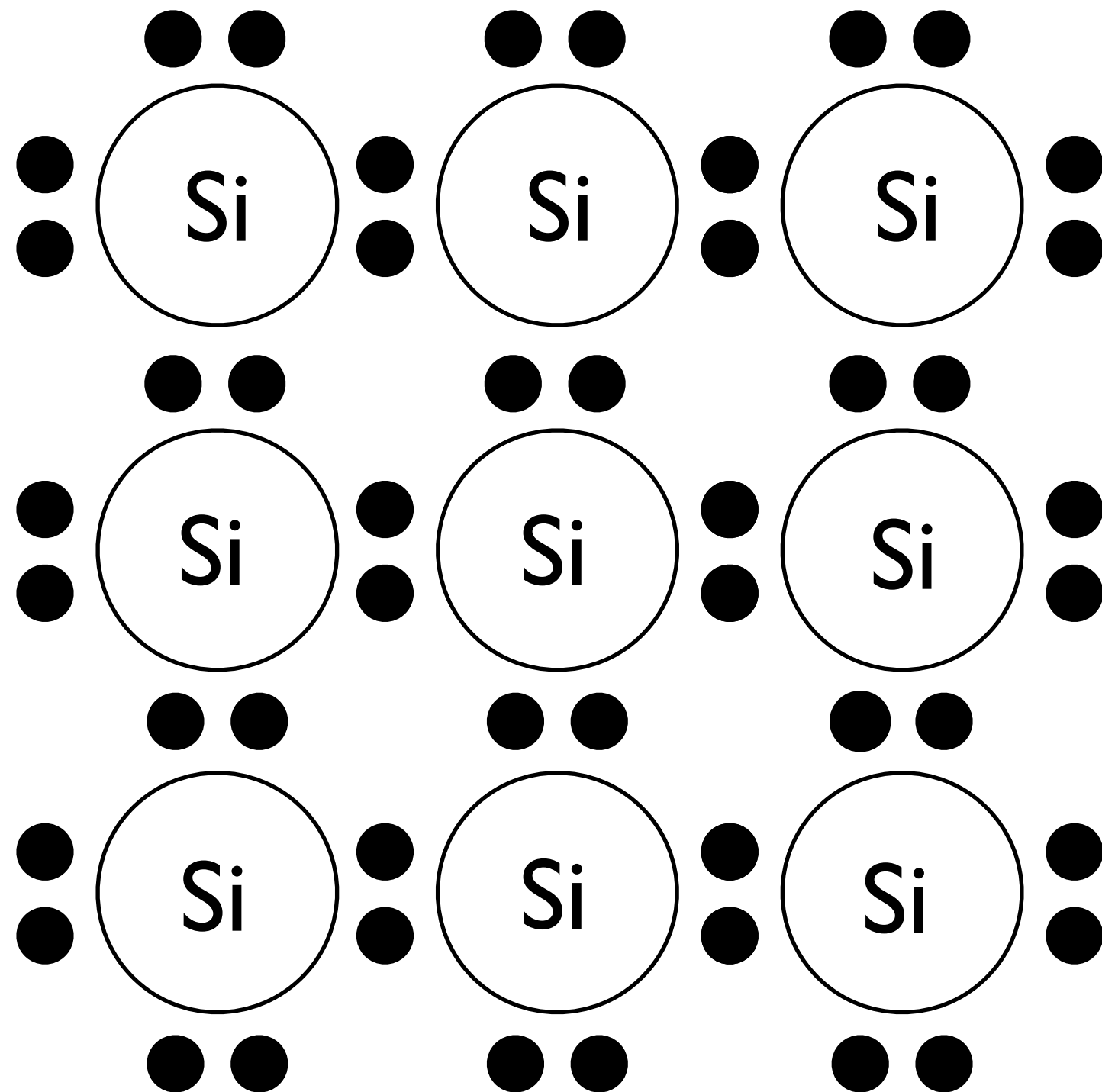
Why is that
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Intrinsic semiconductor

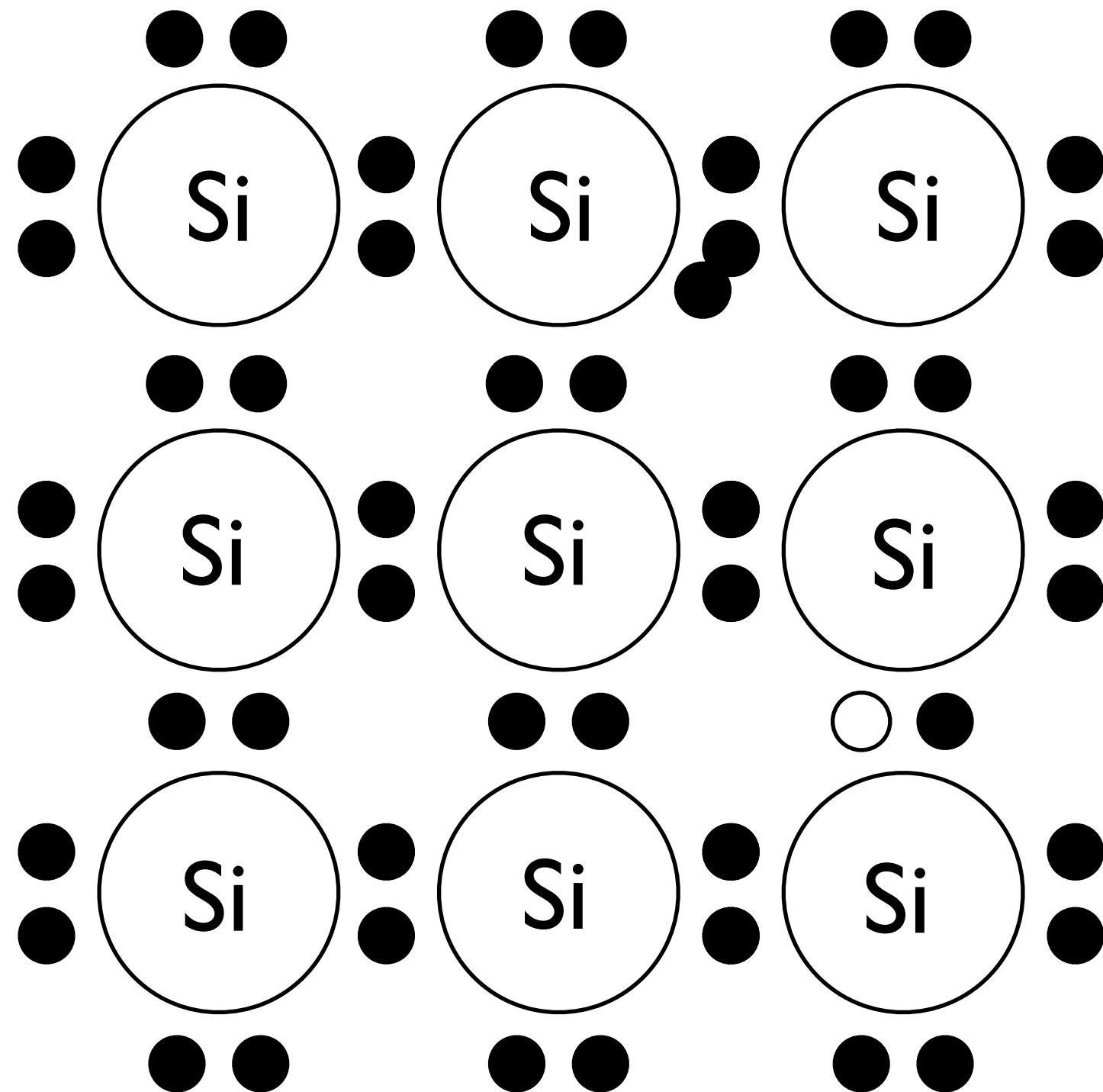


Intrinsic semiconductor



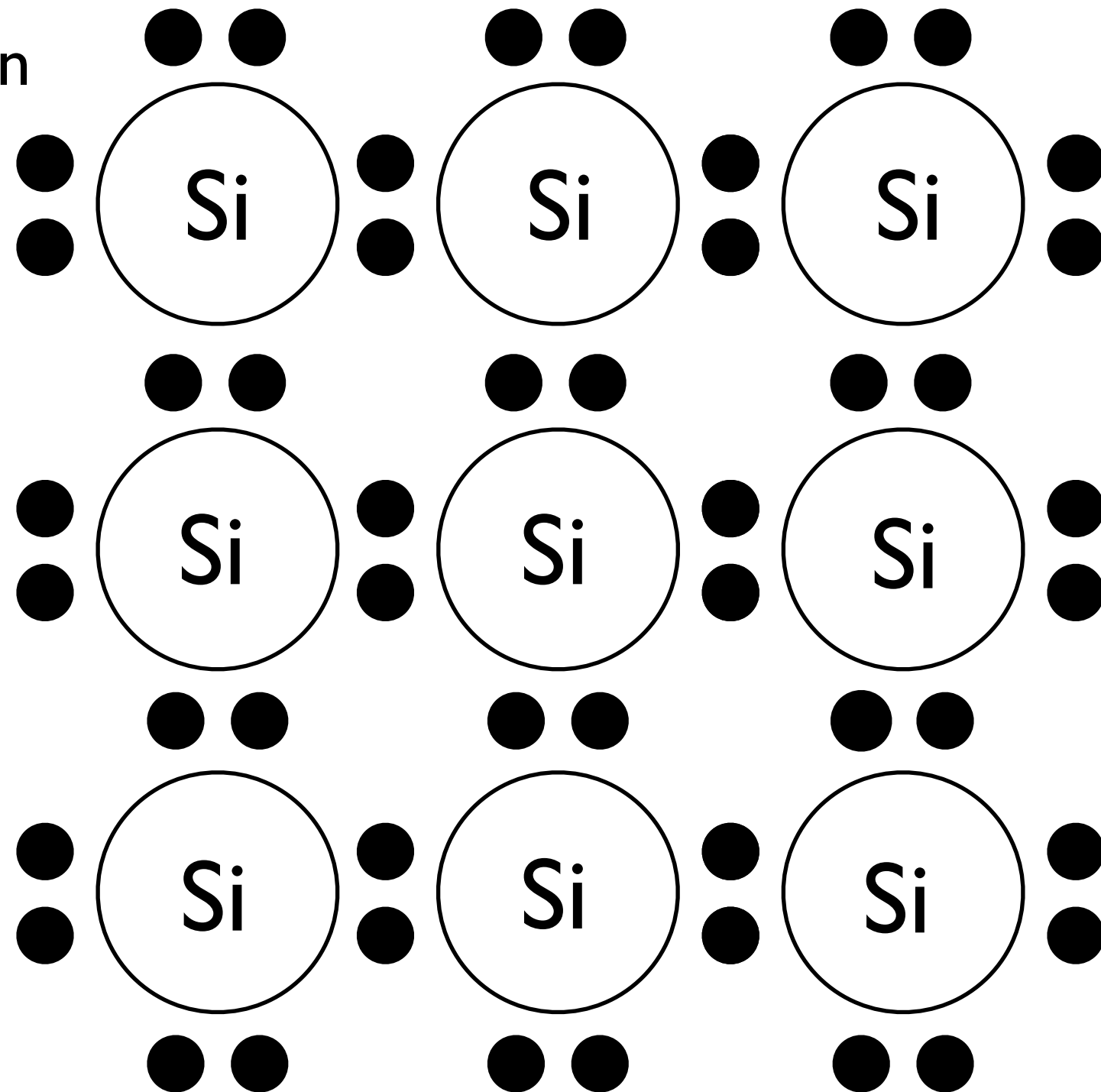
e-h pair creation

Intrinsic semiconductor



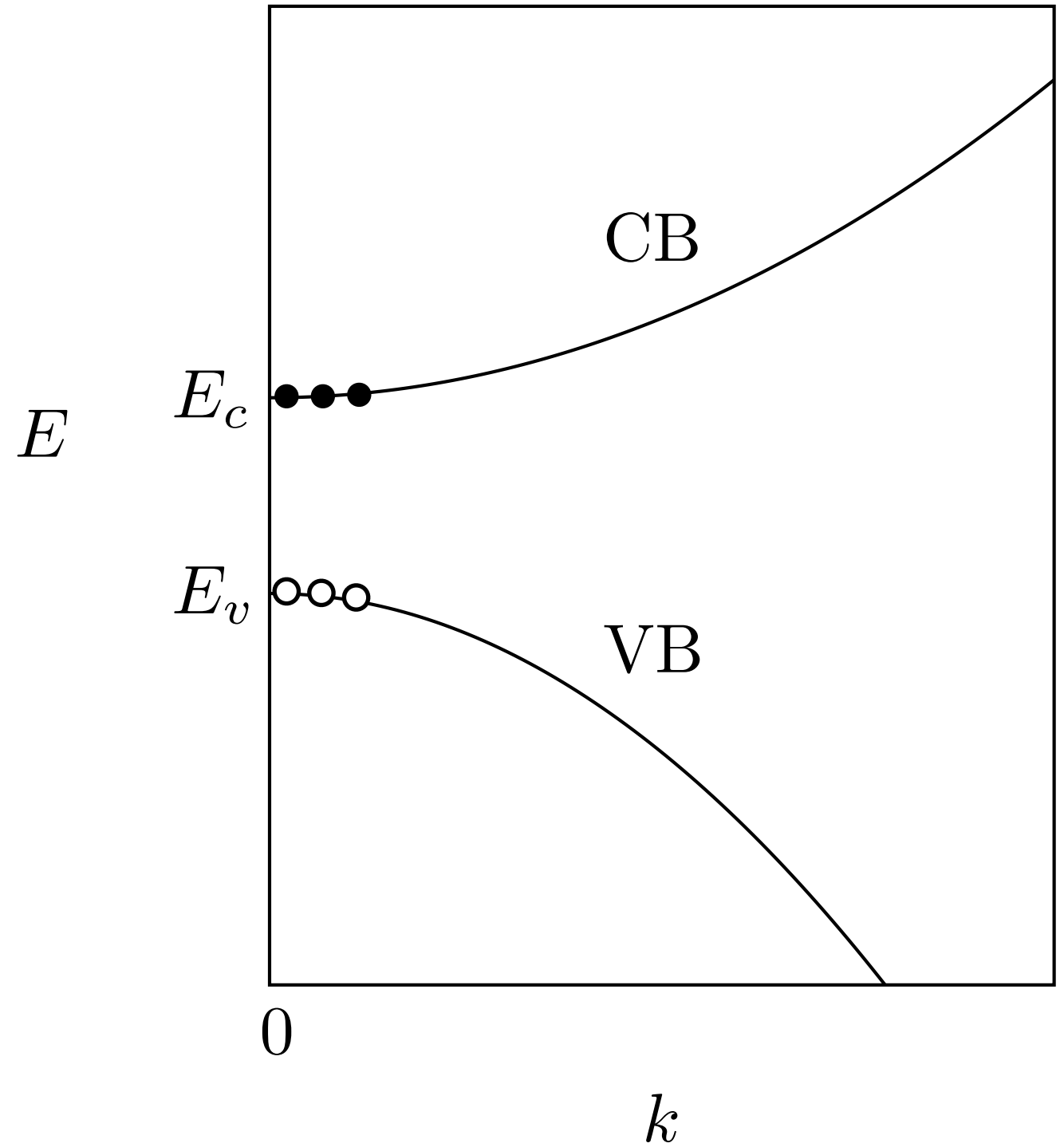
Intrinsic semiconductor

Recombination



Dynamic Equilibrium

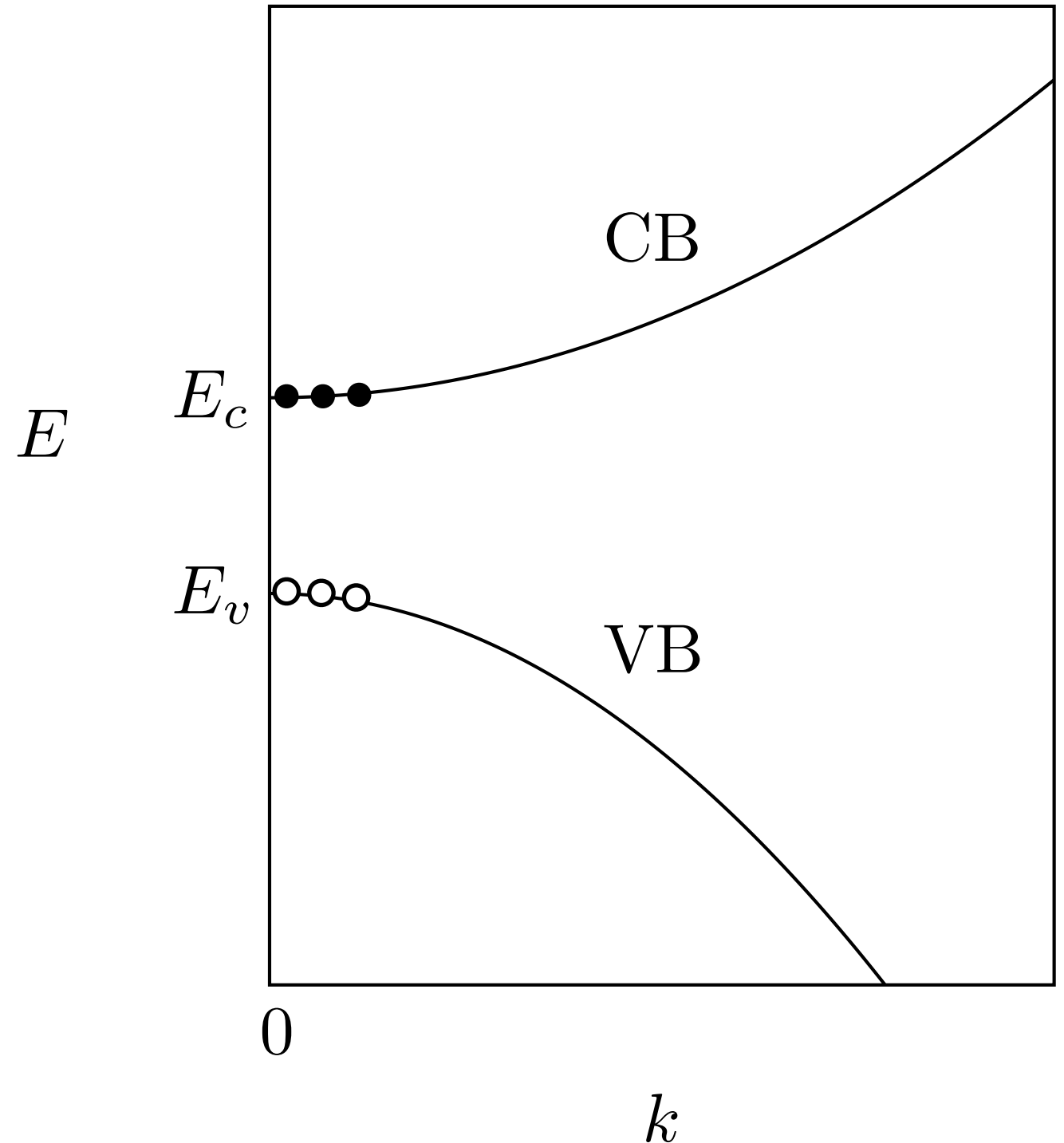
$$\text{rate}_{\text{recomb}} = \text{rate}_{\text{e-h creation}}$$



Dynamic Equilibrium

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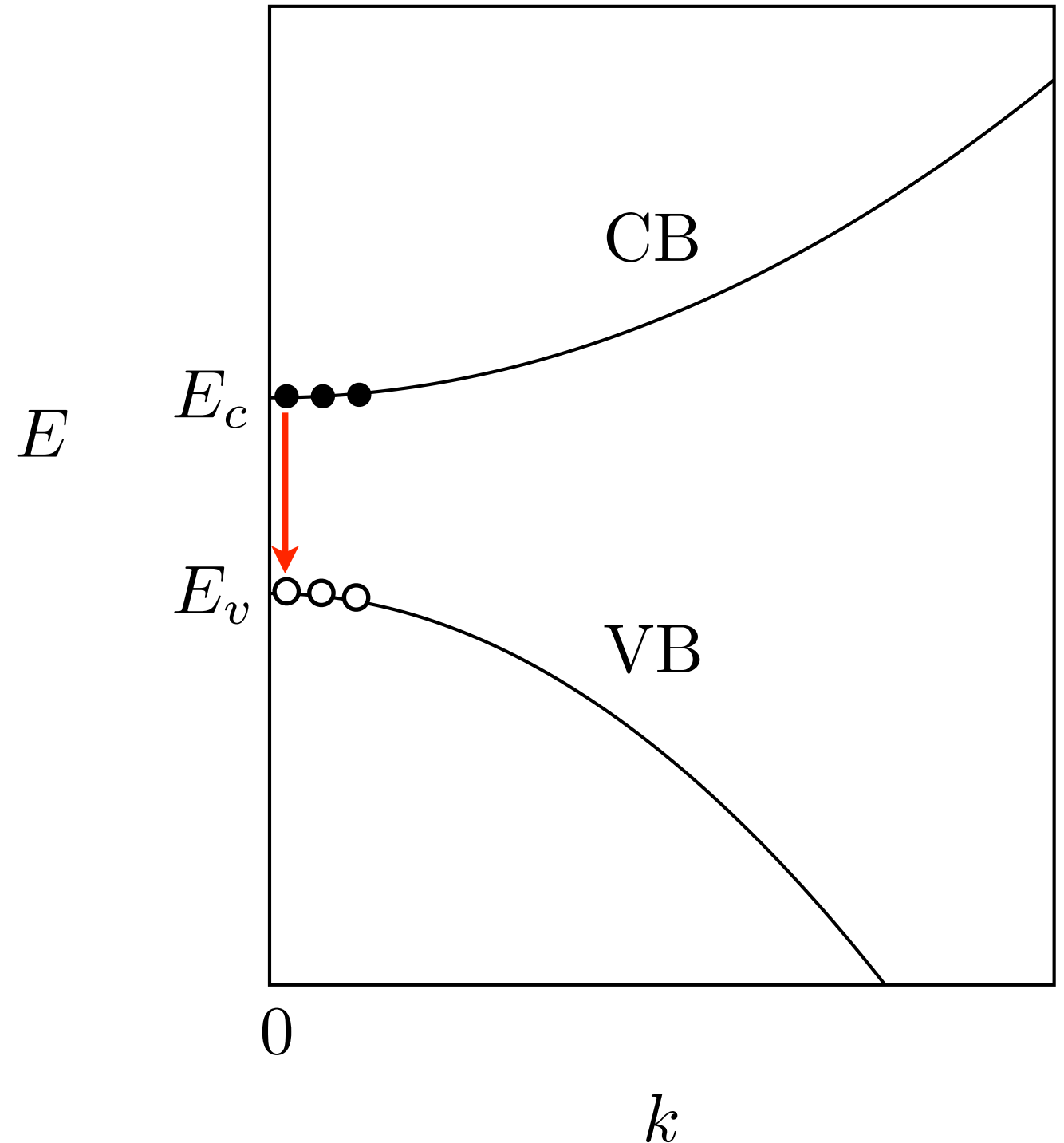
Electrons
tunnel into the
neighboring
hole



Dynamic Equilibrium

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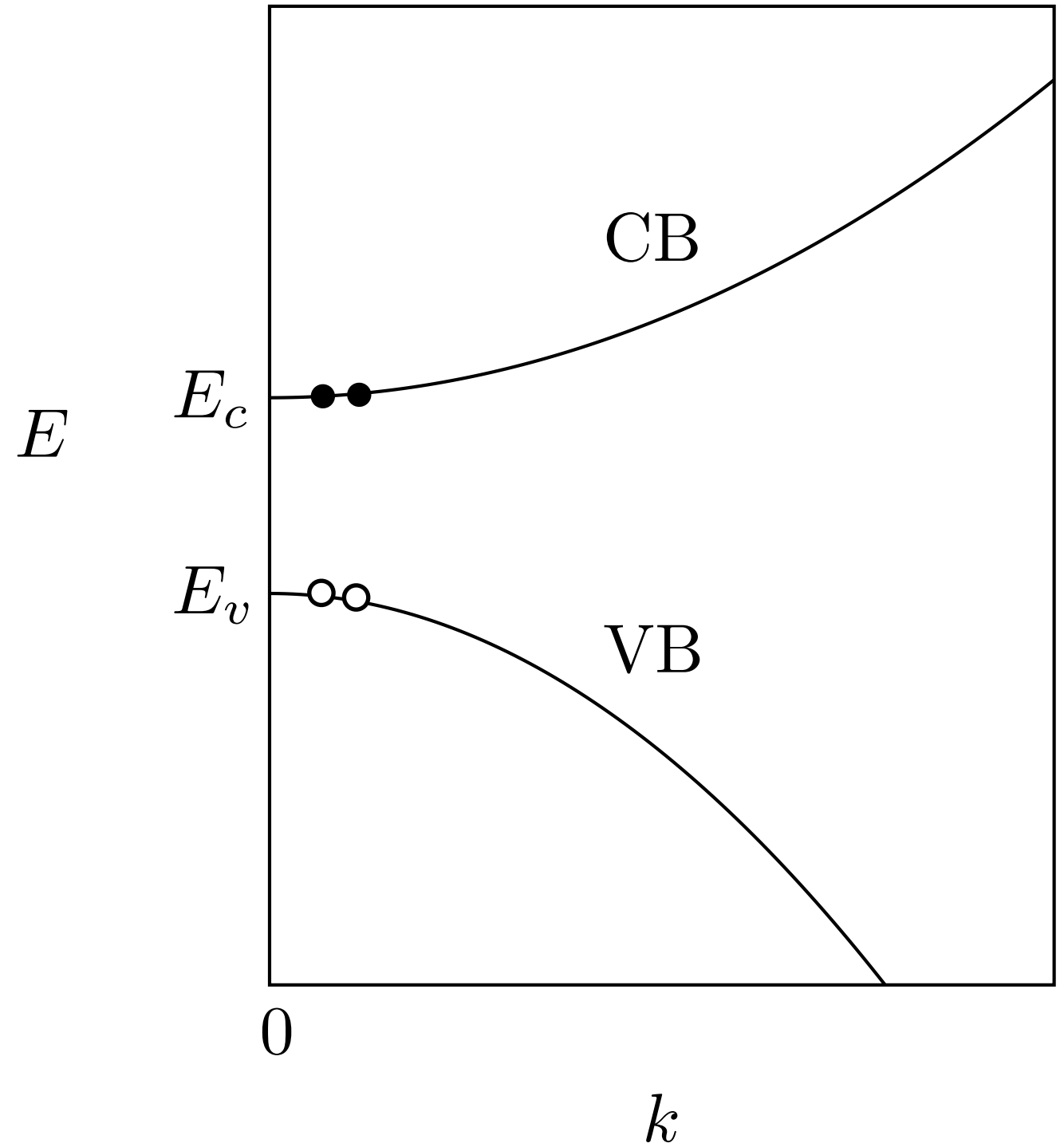
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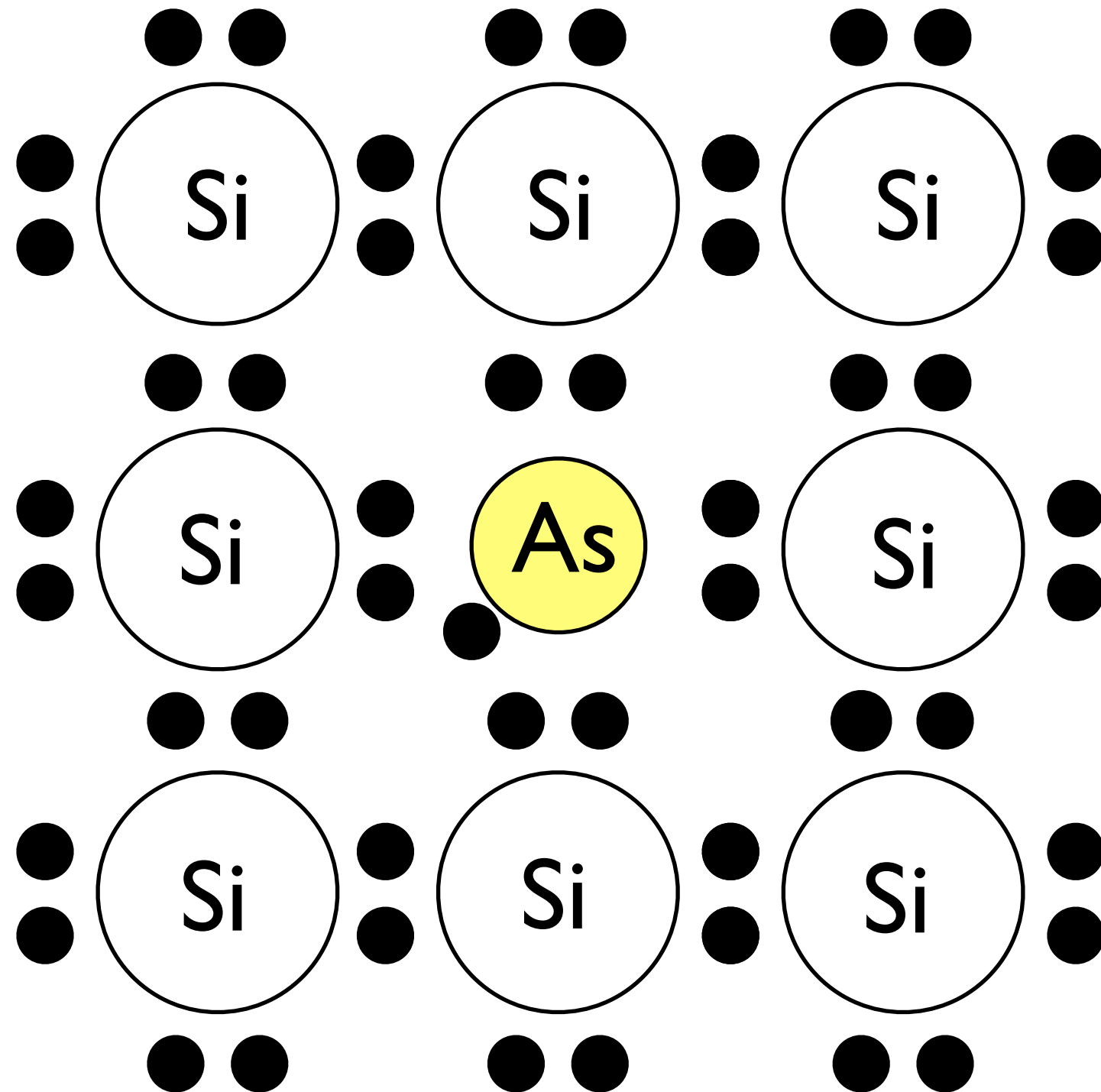
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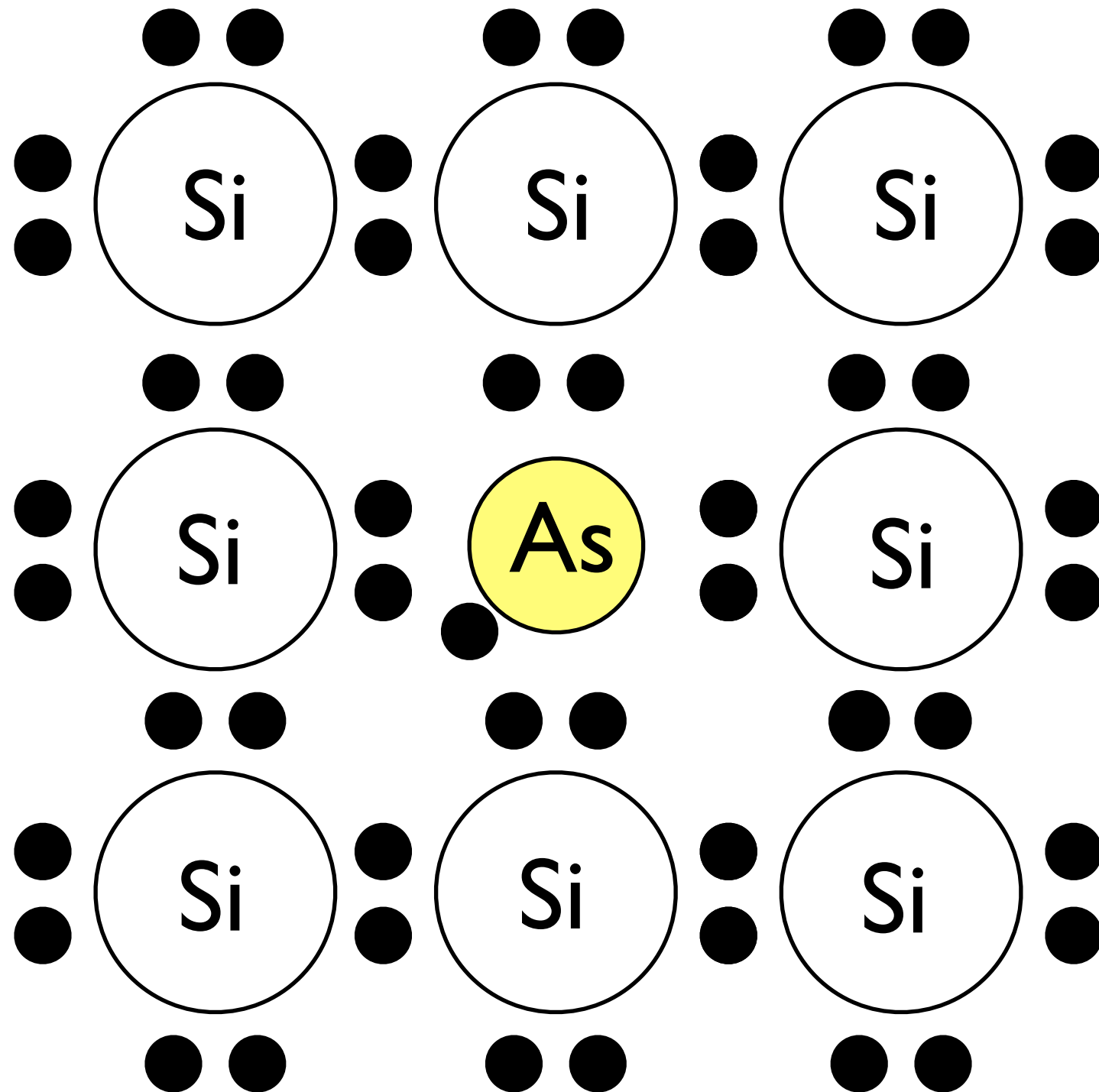


A doped semiconductor



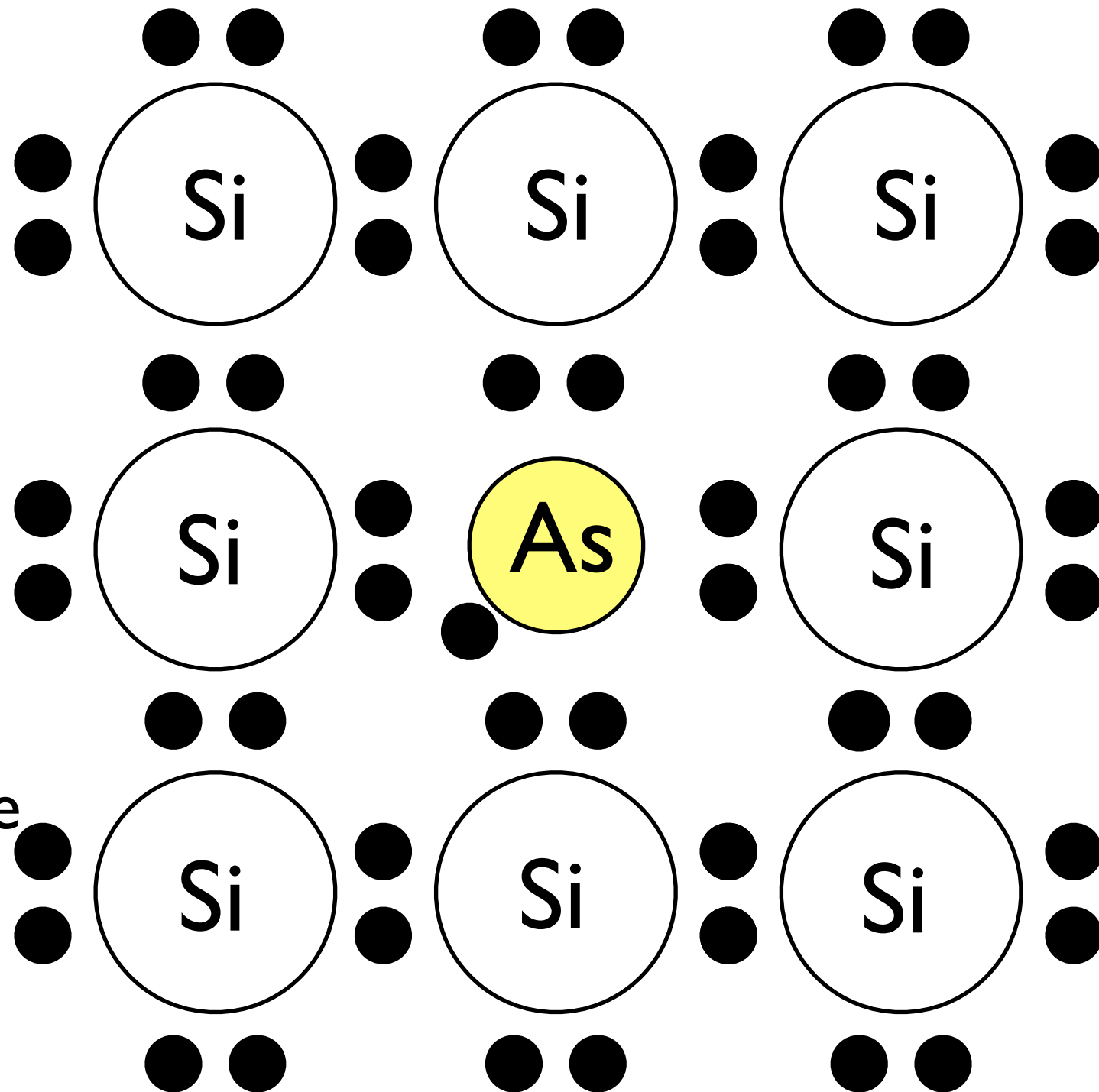
A doped semiconductor

Why is there
an “extra”
electron?



A doped semiconductor

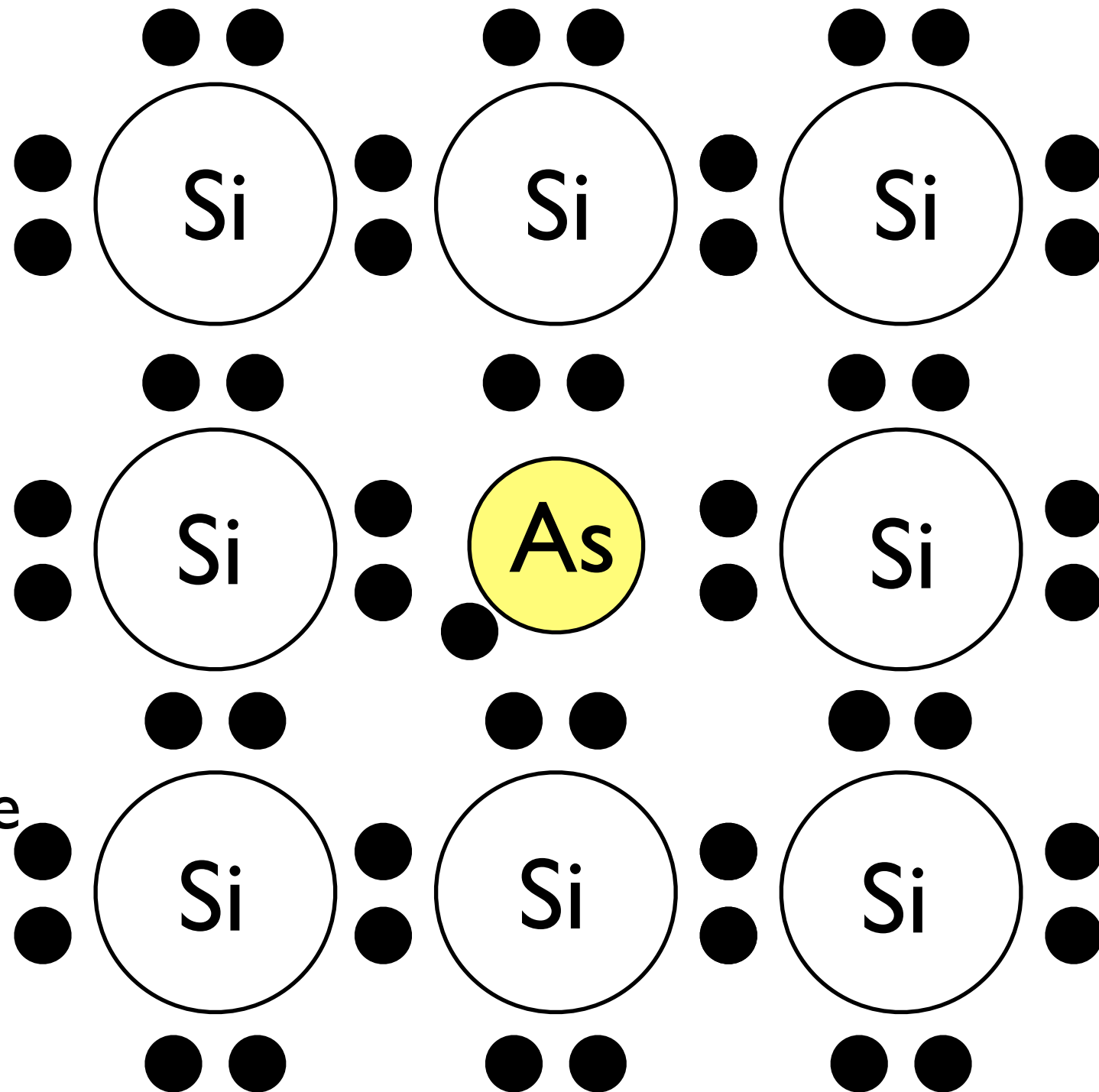
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Why does it
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arsenic atom?
(The bonds are
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A doped semiconductor

Why is there an “extra” electron?

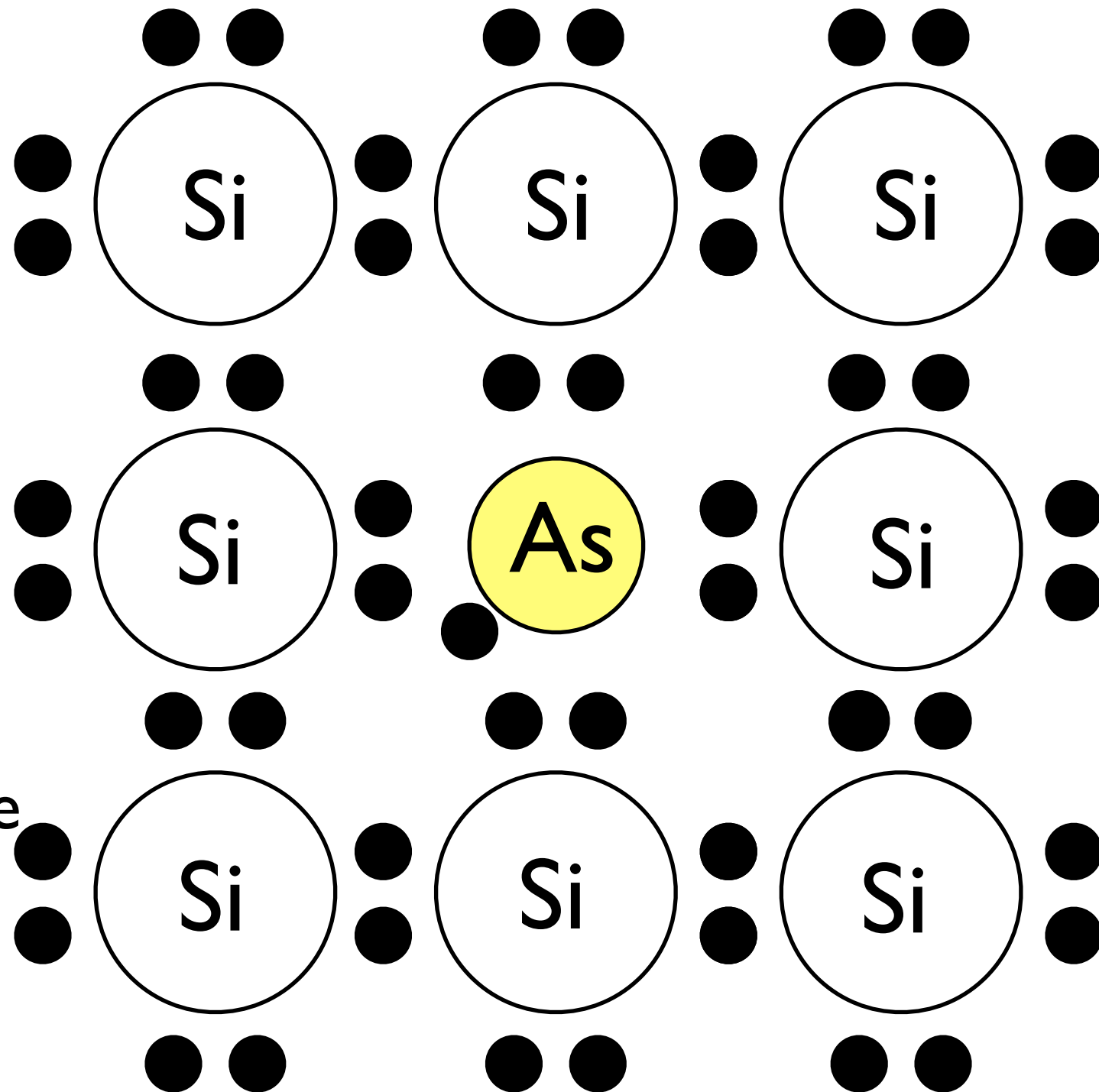


What role does temperature play?

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A doped semiconductor

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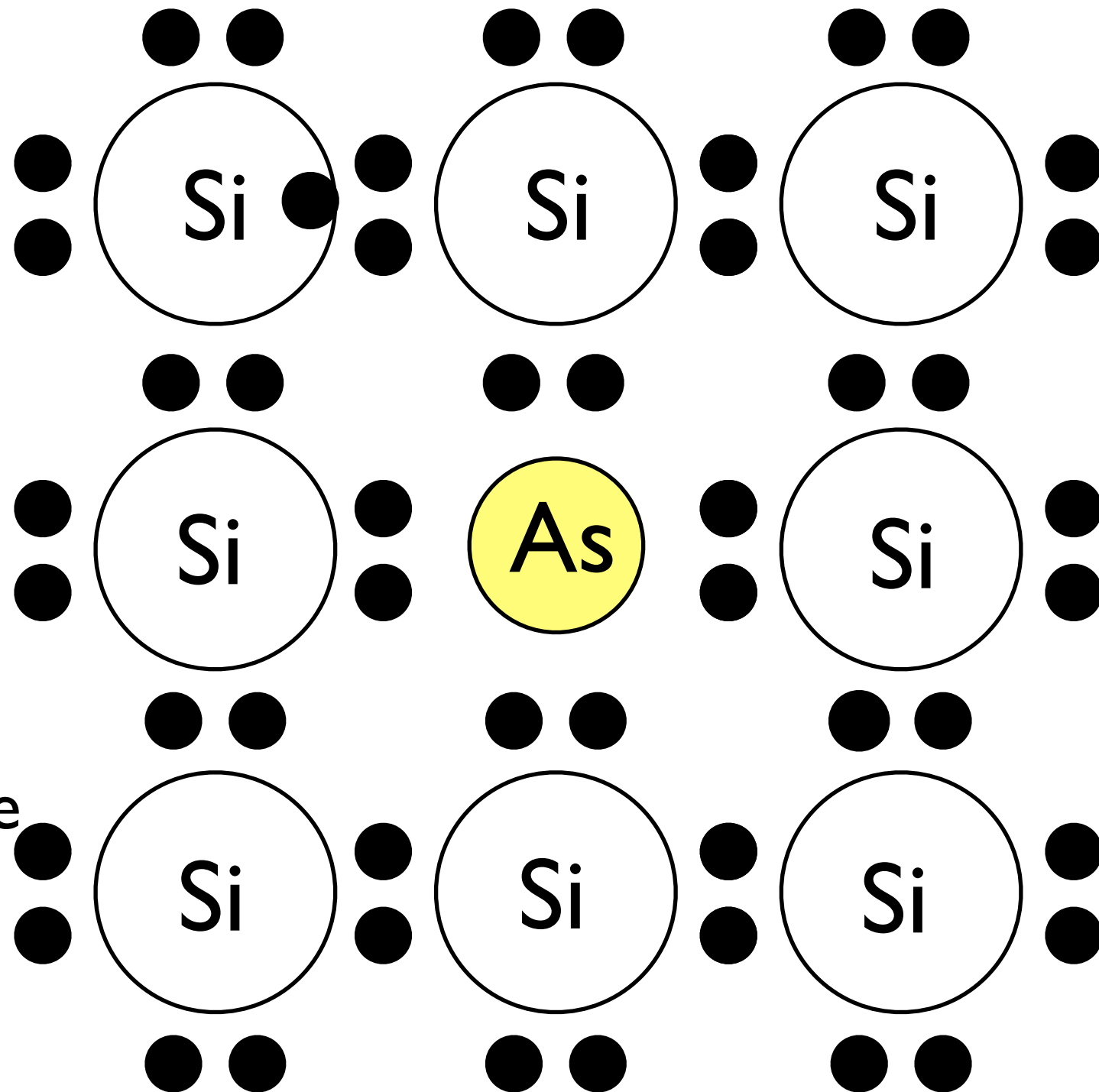
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How is this different from the case of pure silicon?

A doped semiconductor

Why is there an “extra” electron?



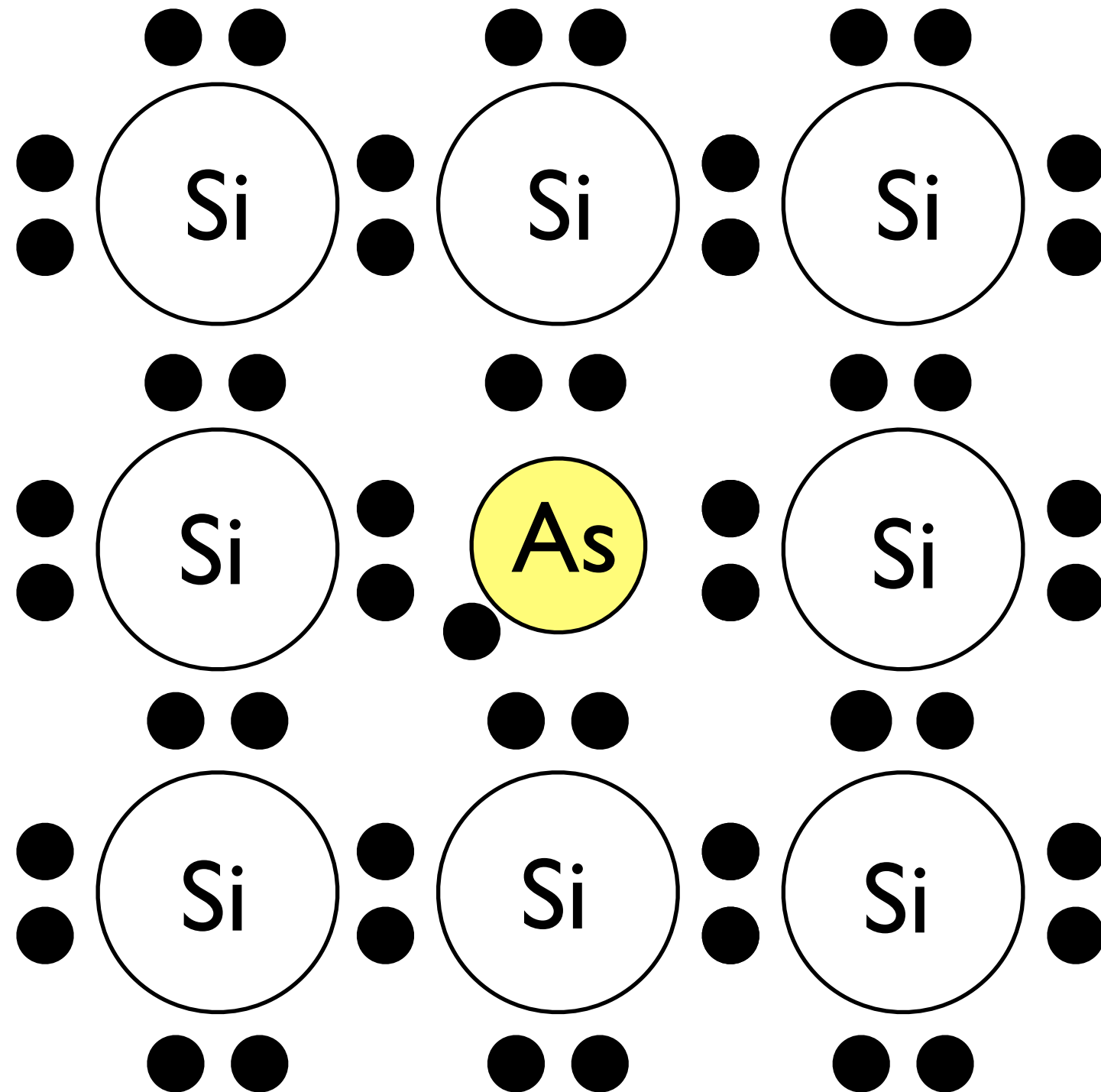
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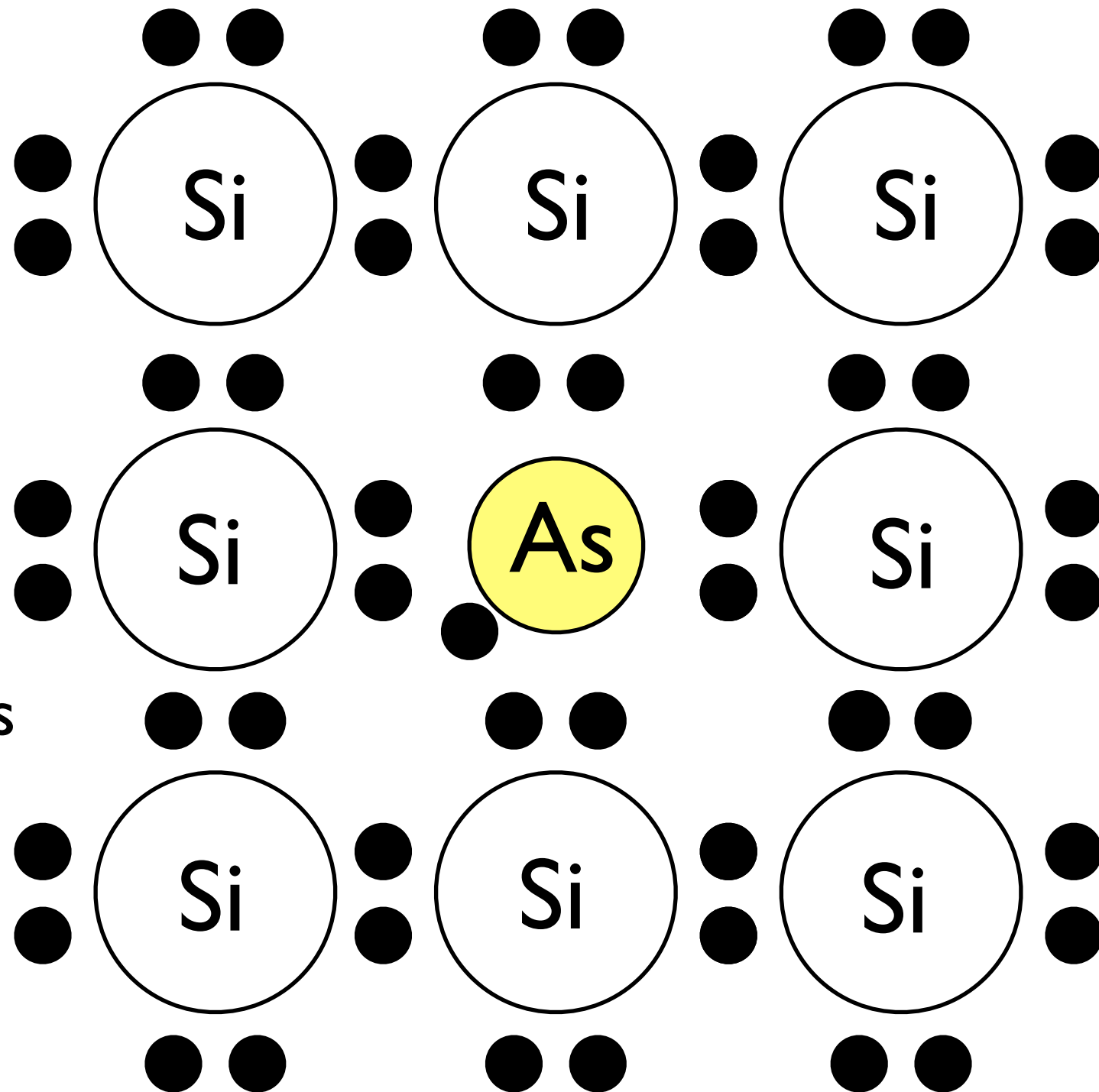
A doped semiconductor

What about
holes?

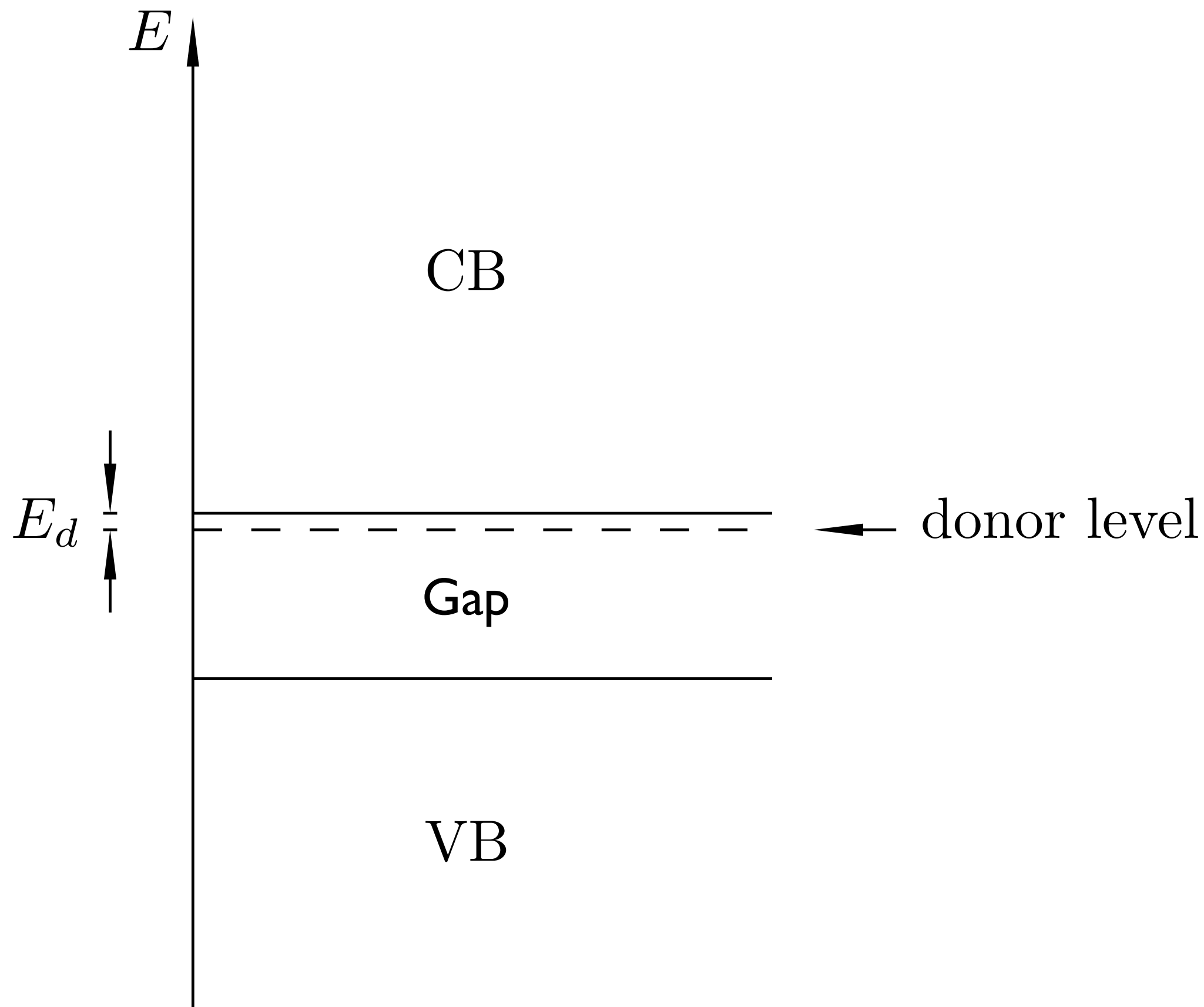


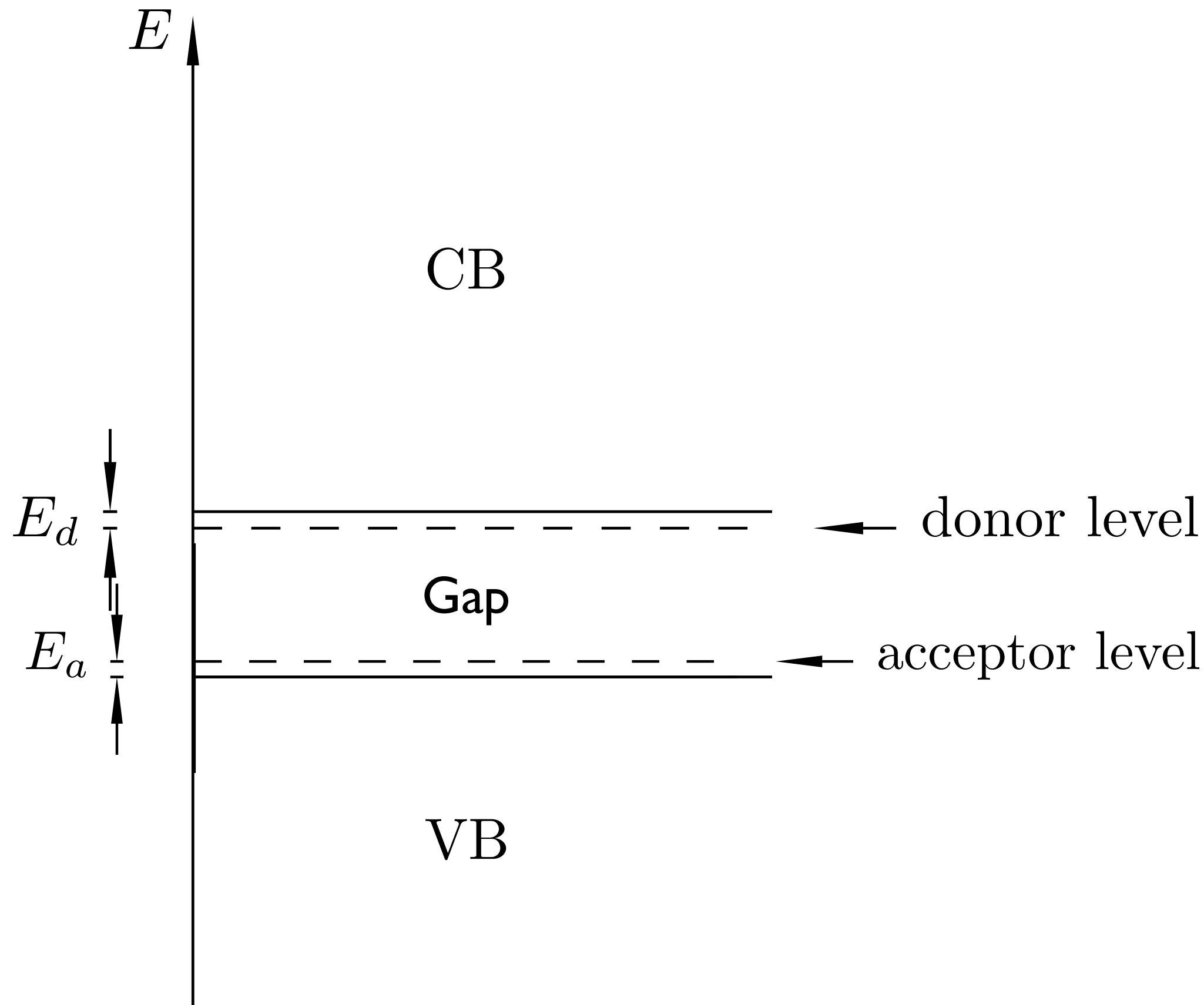
A doped semiconductor

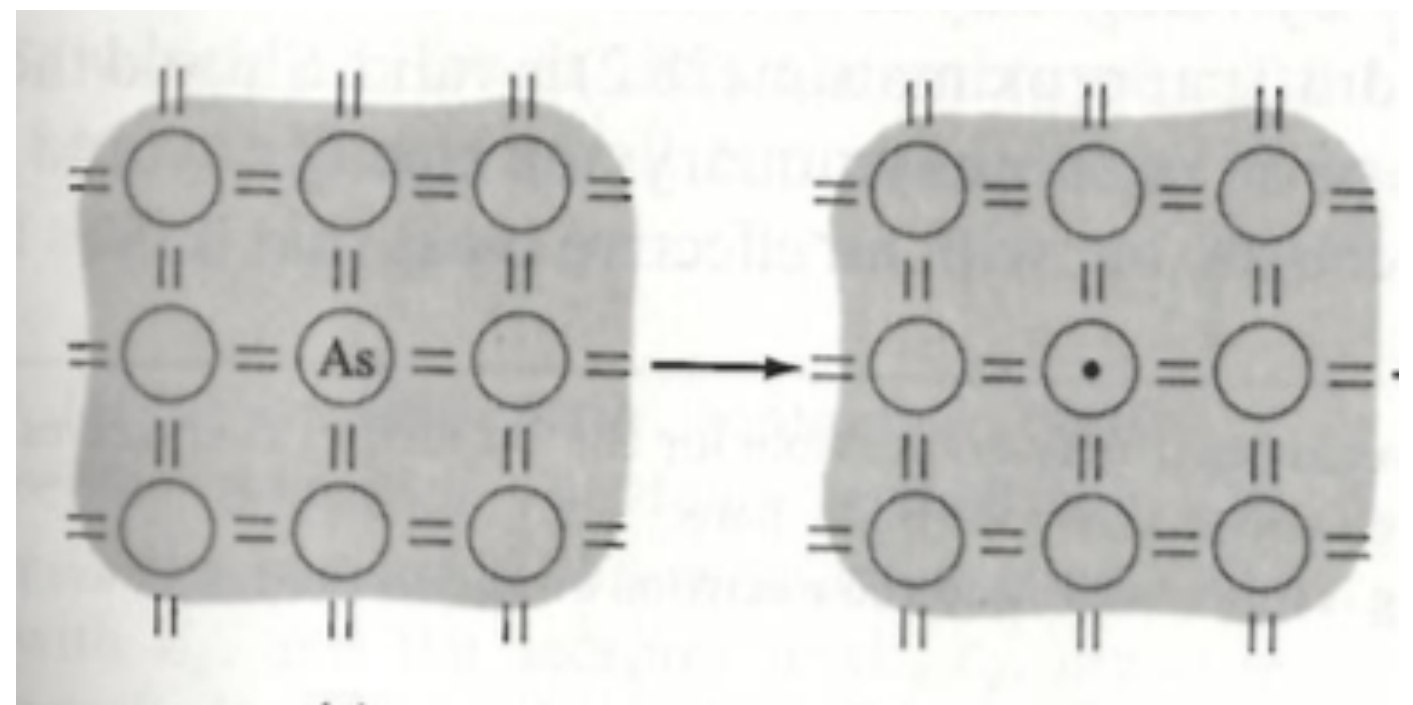
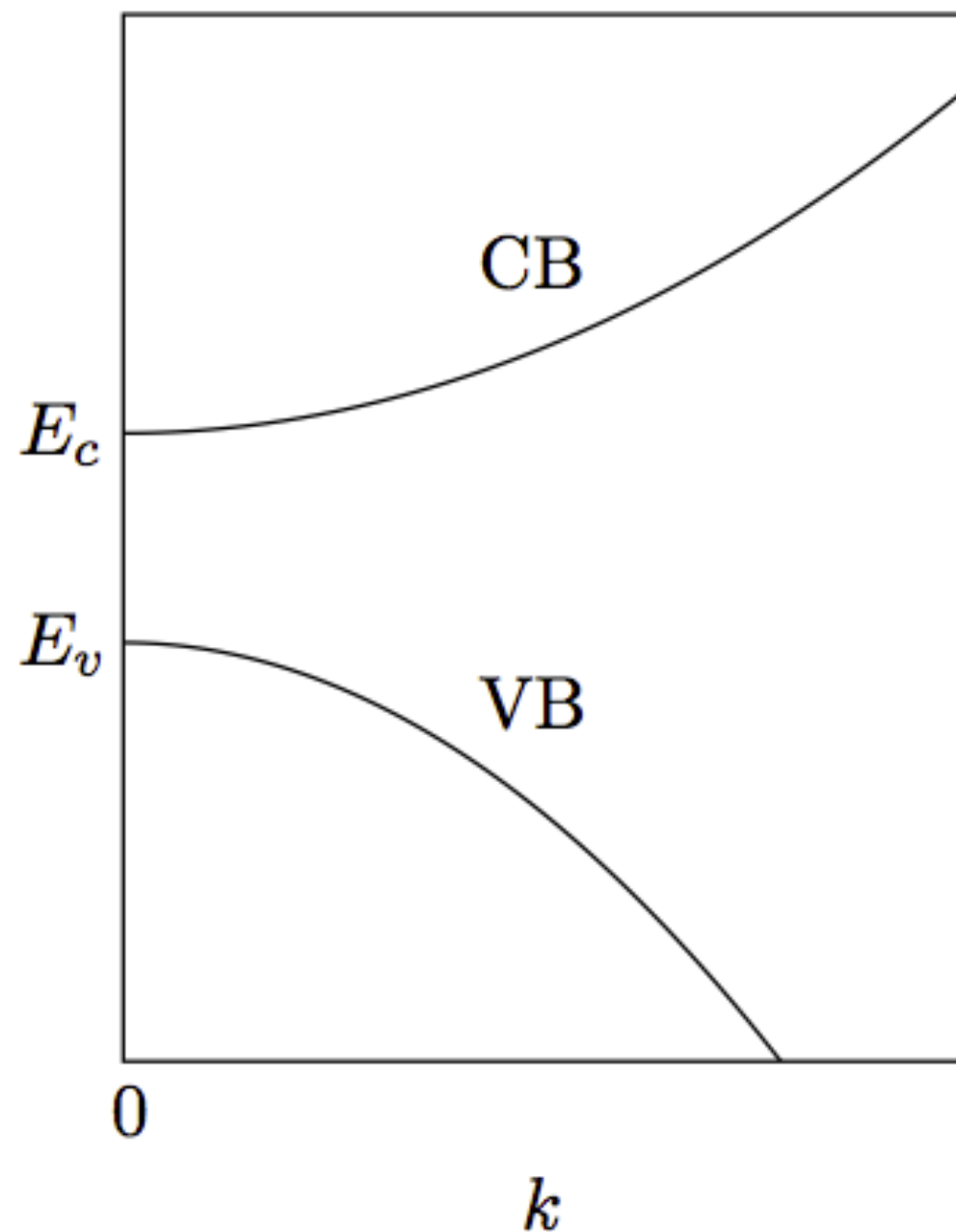
What about
holes?



Having donors
kills all the
holes



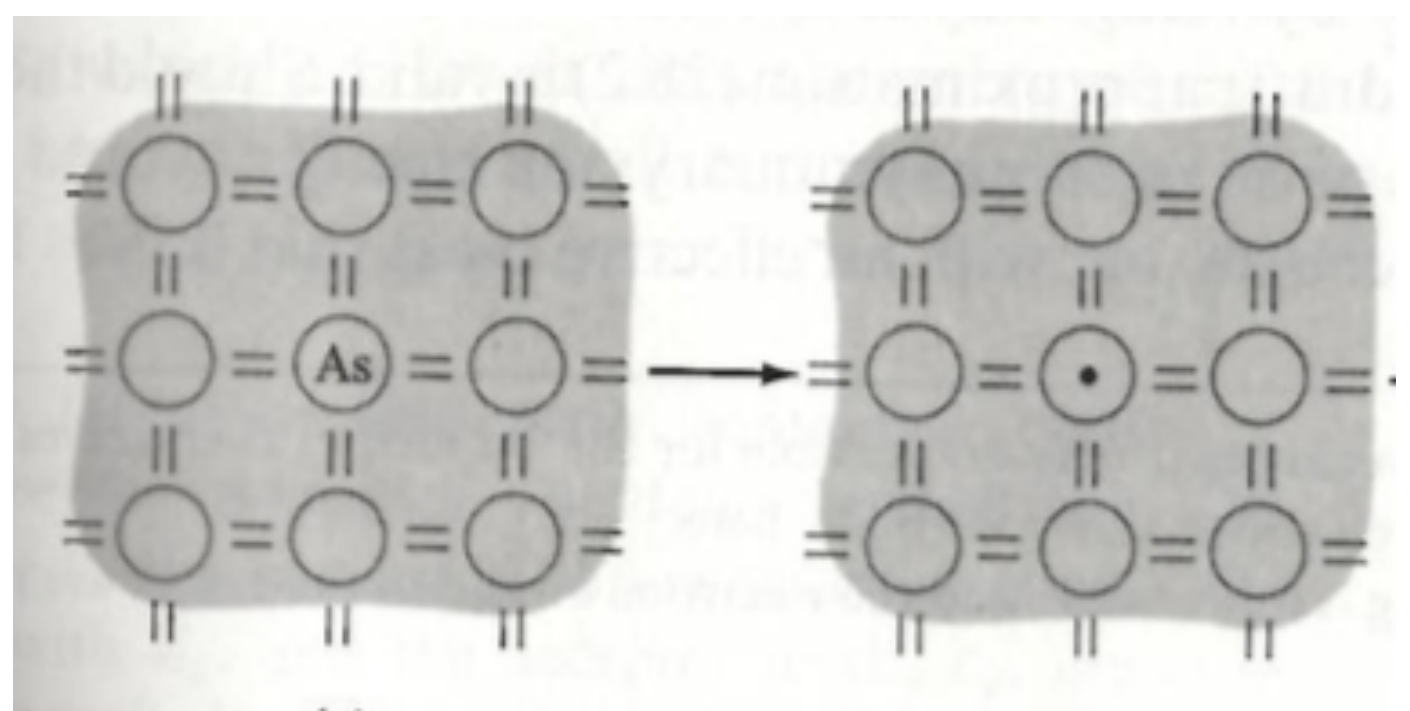
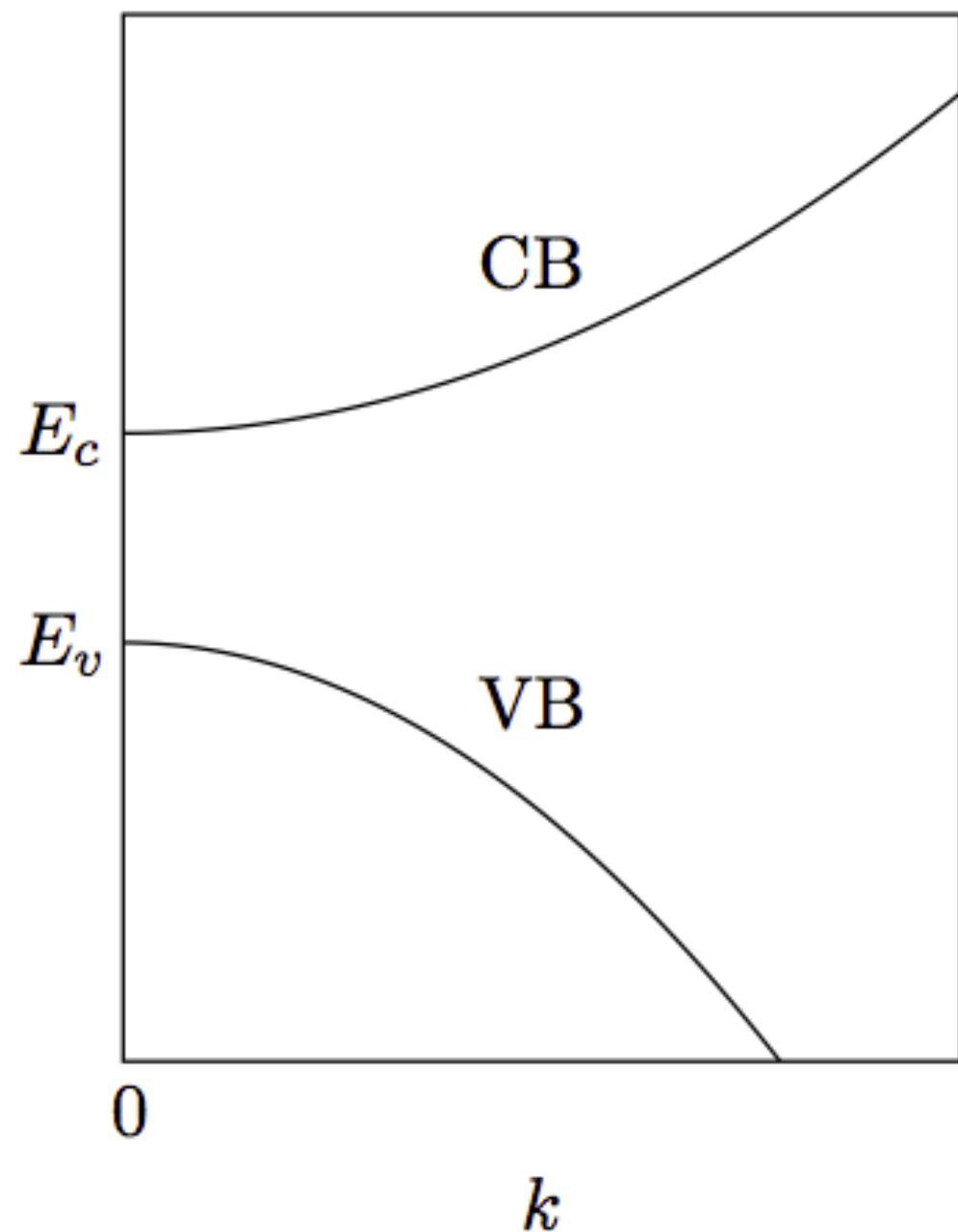




○=Silicon atom

1 H																	2 He
3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
55 Cs	56 Ba	57 La *	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra	89 Ac *	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og

Now these aren't equal to each other!



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37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe				
55 Cs	56 Ba	57 La	*	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn			
87 Fr	88 Ra	89 Ac	*	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og			

$$n = 2 \left(\frac{m_n^* k_B T}{2\pi \hbar^2} \right)^{3/2} e^{-\frac{E_c - E_F}{k_B T}} \quad p = 2 \left(\frac{m_p^* k_B T}{2\pi \hbar^2} \right)^{3/2} e^{-\frac{E_F - E_v}{k_B T}}$$

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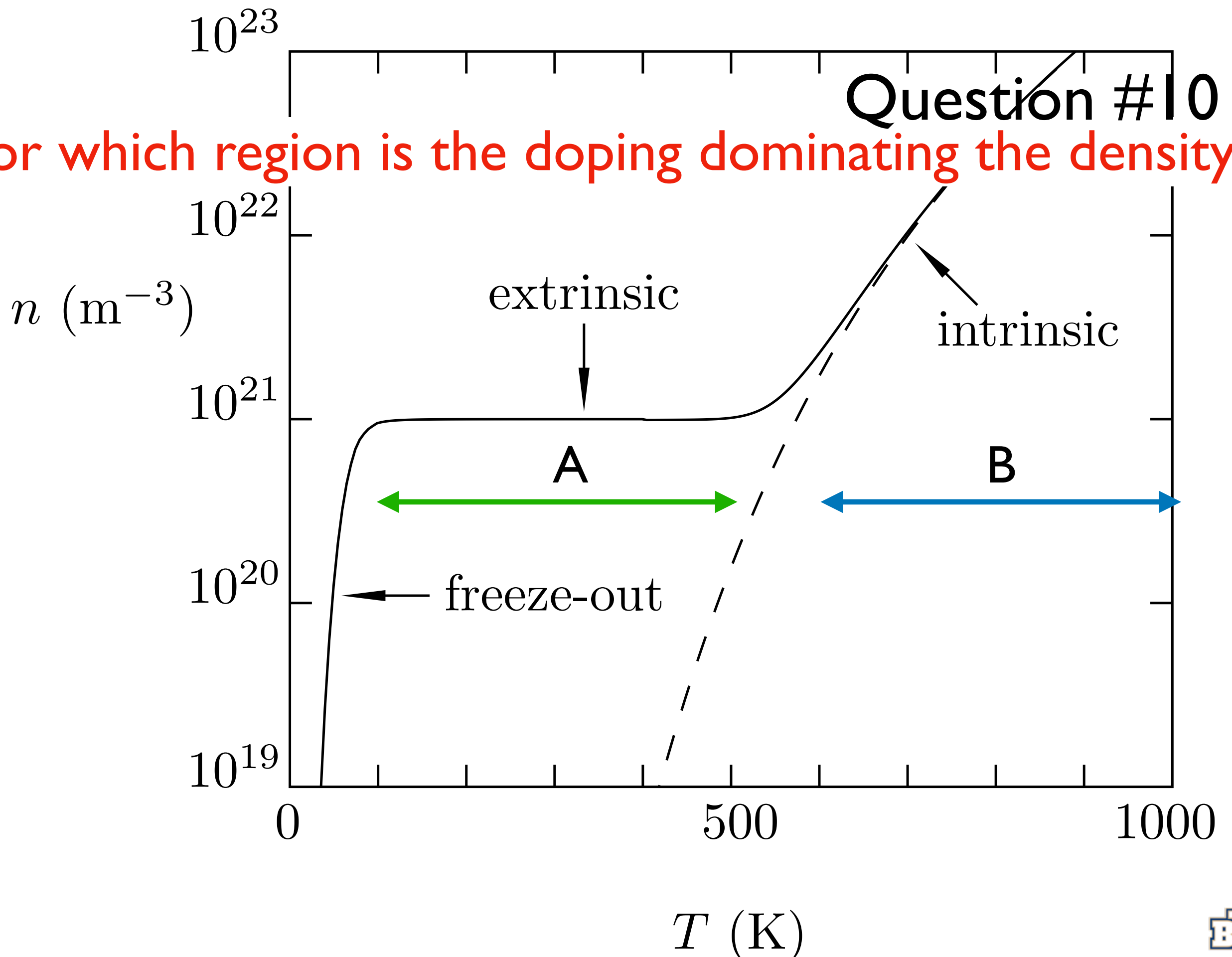
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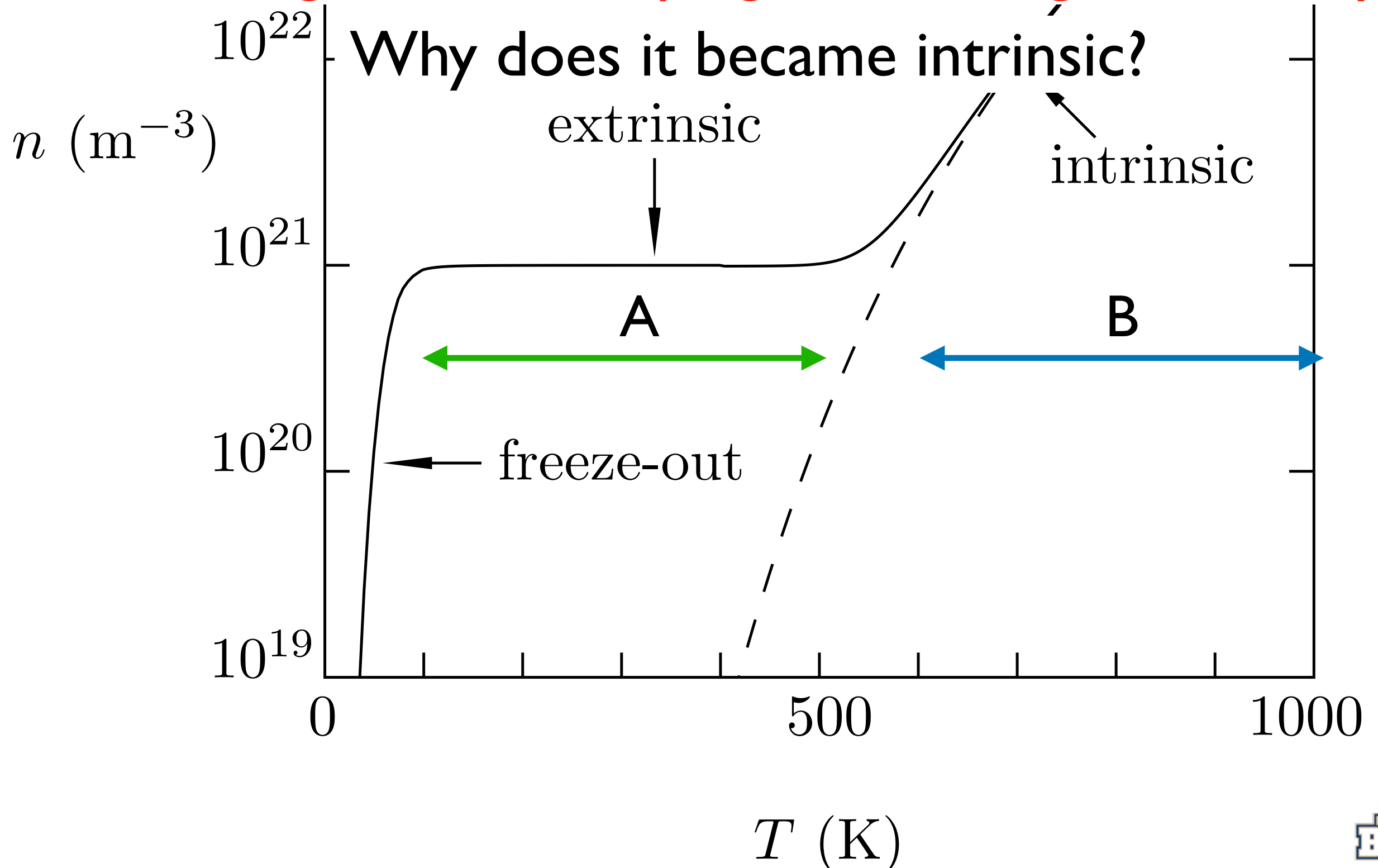
$$np = N_c N_v e^{-\frac{E_g}{k_B T}}$$

Question #10
For which region is the doping dominating the density?



Question #10

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How big of an affect is it?

1 atom in 5×10^7

$$n_i = 10^{16} \text{ m}^{-3} \rightarrow$$

How big of an affect is it?

1 atom in 5×10^7

$$n_i = 10^{16} \text{ m}^{-3} \rightarrow n \approx 10^{21} \text{ m}^{-3}$$

$$\frac{dq}{dt} = I = -eNv \quad \boxed{1}$$

$$\vec{J} = -en\vec{v} = \sigma\vec{\mathcal{E}} = \frac{ne^2\tau}{m^*}\vec{\mathcal{E}} \quad \boxed{2} \quad \boxed{3} \quad \boxed{4}$$

$$\vec{v}_d = -\frac{e\tau}{m^*}\vec{\mathcal{E}} \Rightarrow \mu_n = \frac{e\tau}{m^*} \quad \boxed{5} \quad \boxed{6}$$

$$\boxed{7}$$

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Why bother with mobility?
How is it useful?

$\boxed{7}$

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$$\sigma_n = ne\mu_n \quad \boxed{7}$$

Which of the following are intrinsic
semiconductors

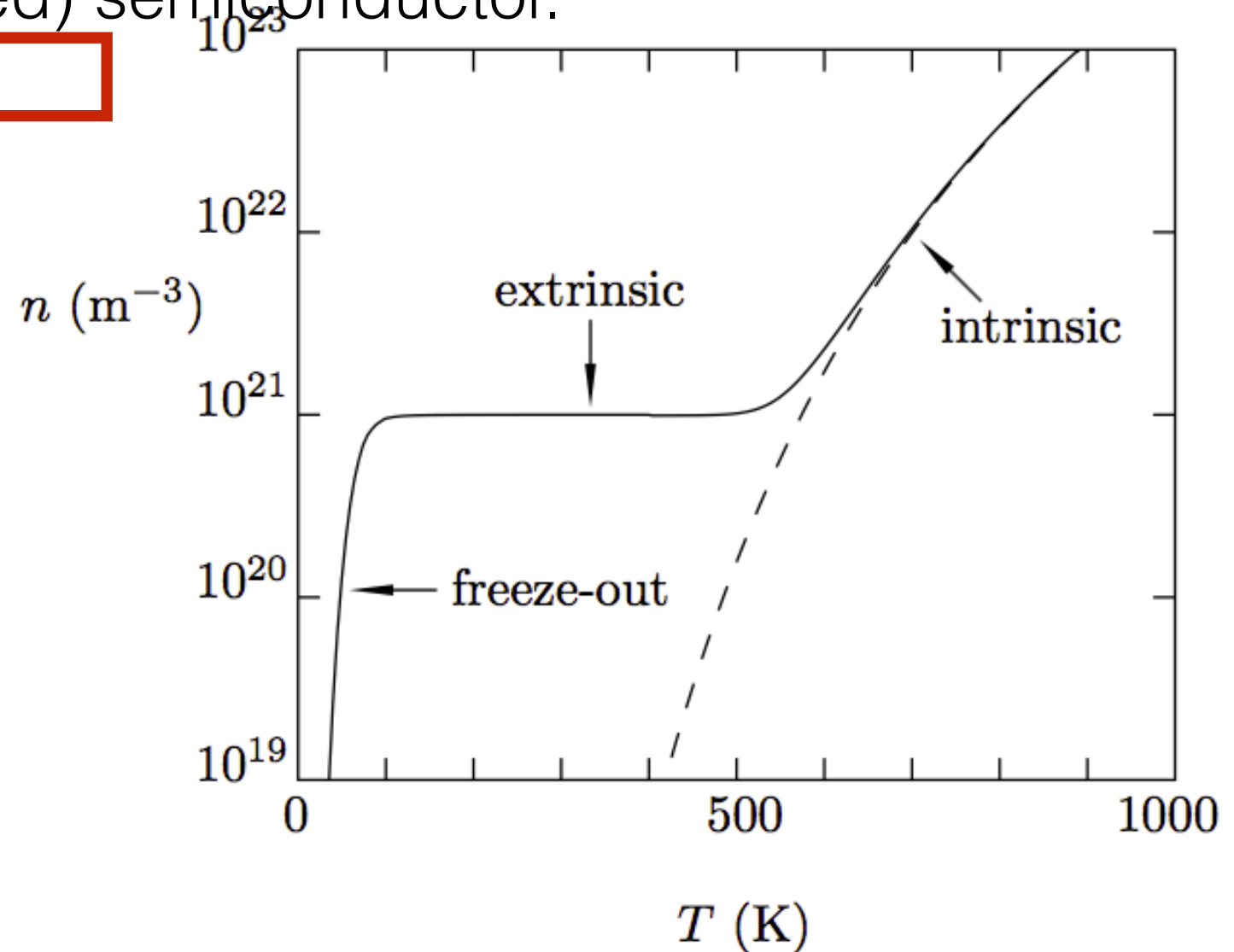
Question #12

- a) A cool doped semiconductor.
- b) A hot, doped semiconductor.
- c) A cool pure (undoped) semiconductor.
- d) A hot pure (undoped) semiconductor.
- e) b, c, and d.
- f) Both b and d.

Which of the following are intrinsic semiconductors

Question #12

- a) A cool doped semiconductor.
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- c) A cool pure (undoped) semiconductor.
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At low temperature, what kind of semiconductor has a higher electrical conductivity?

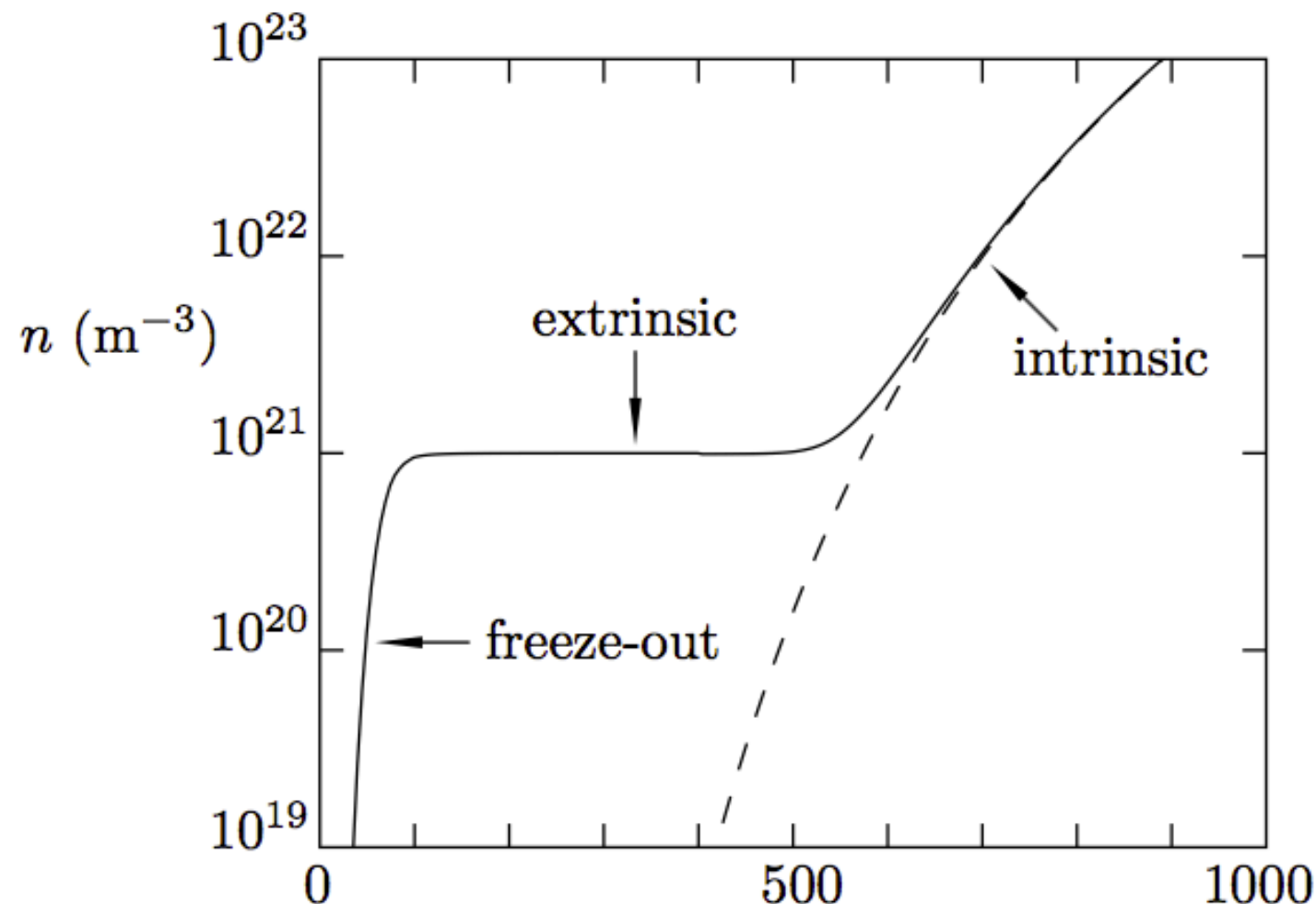
Question #13

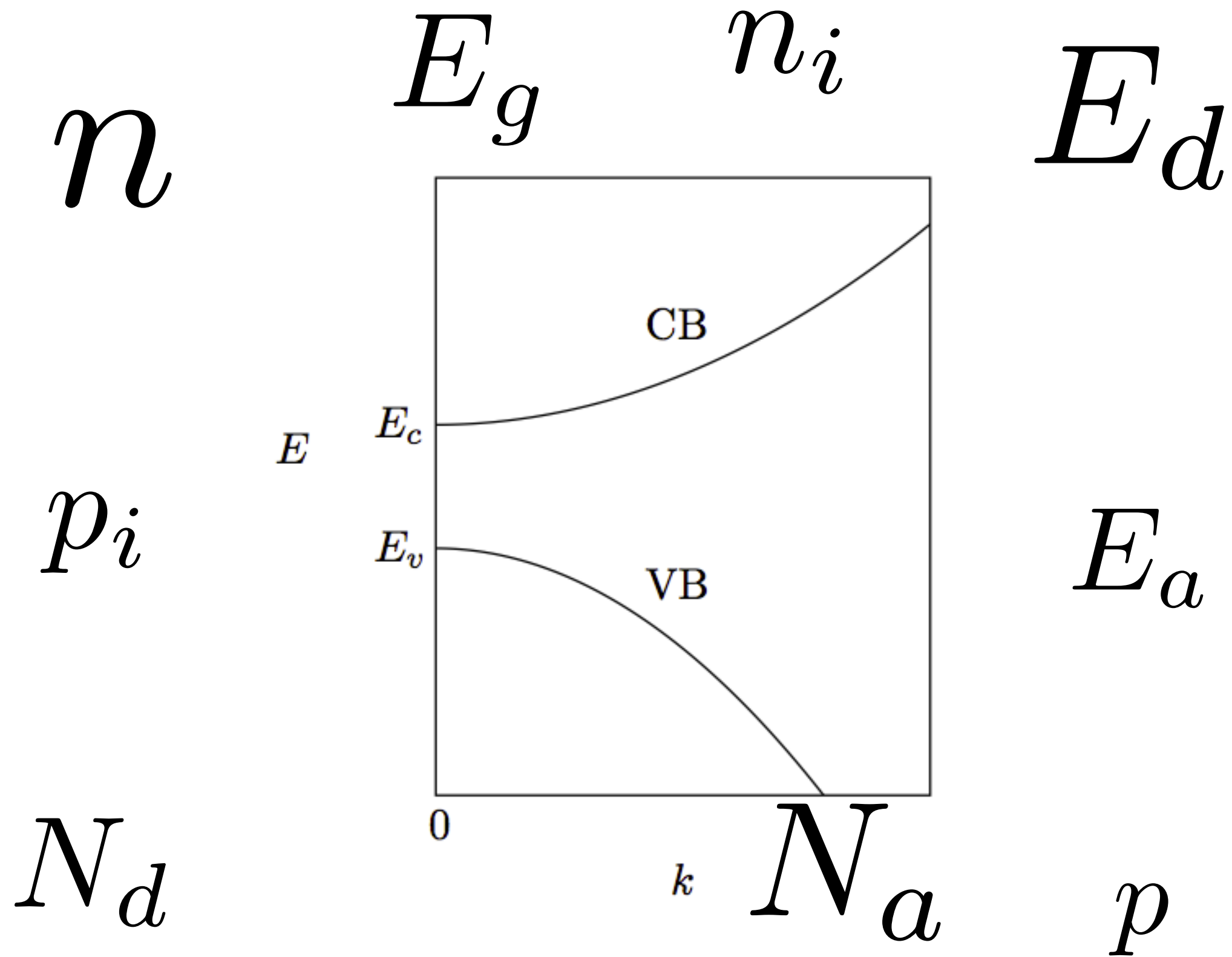
- a) Extrinsic because it has less charge carriers.
- b) Extrinsic because it has more charge carriers.
- c) Intrinsic because it has more charge carriers.
- d) Intrinsic because it has less charge carriers.
- e) They will have the same electrical conductivity.

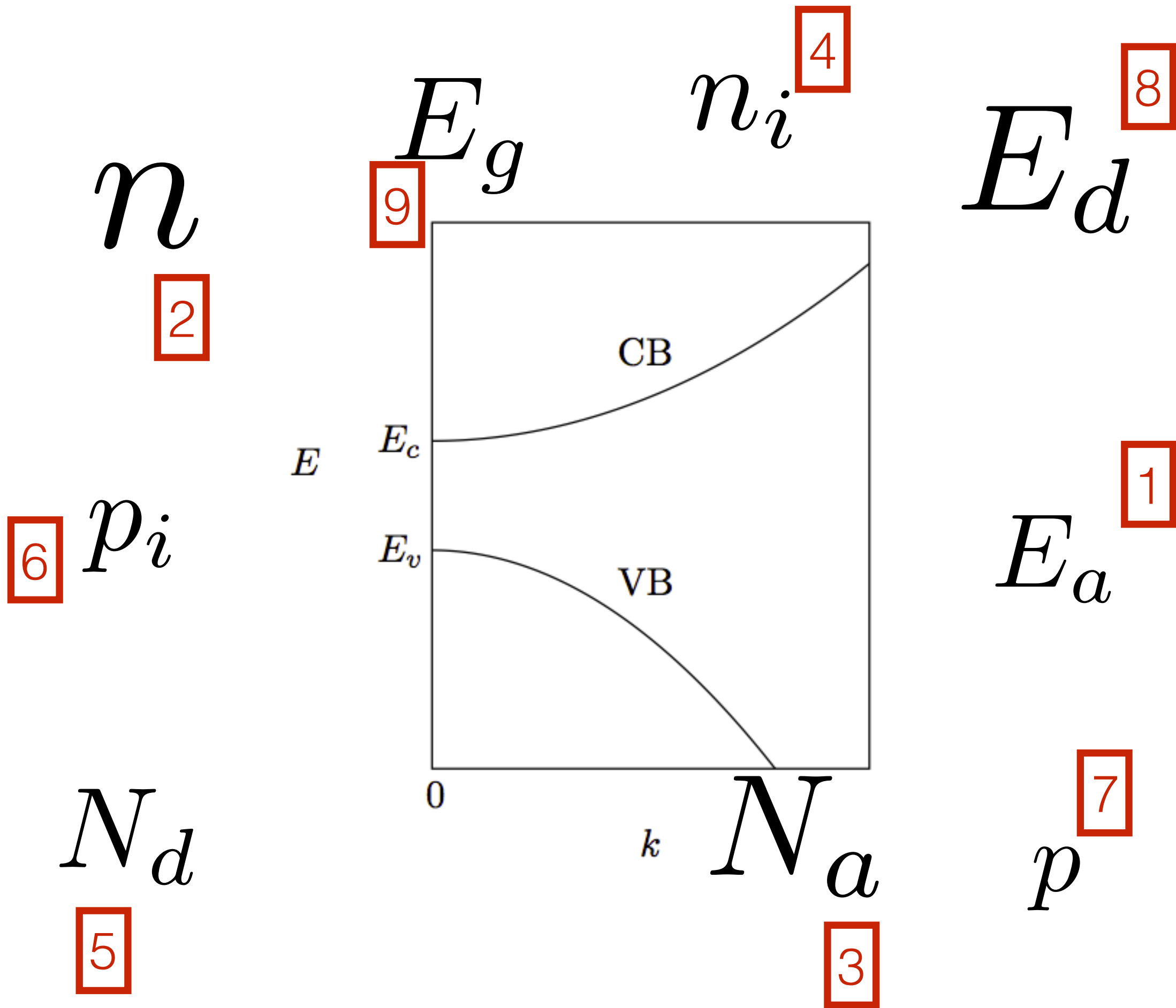
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- c) Intrinsic because it has more charge carriers.
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Consider an n-type semiconductor at low temperature (with donor density N_d), what will be the value of p ?

Question #14

- d) $p \approx 0$
- a) $p \approx n_i$
- c) $p \approx N_d$

Consider an n-type semiconductor at low temperature (with donor density N_d), what will be the value of p ?

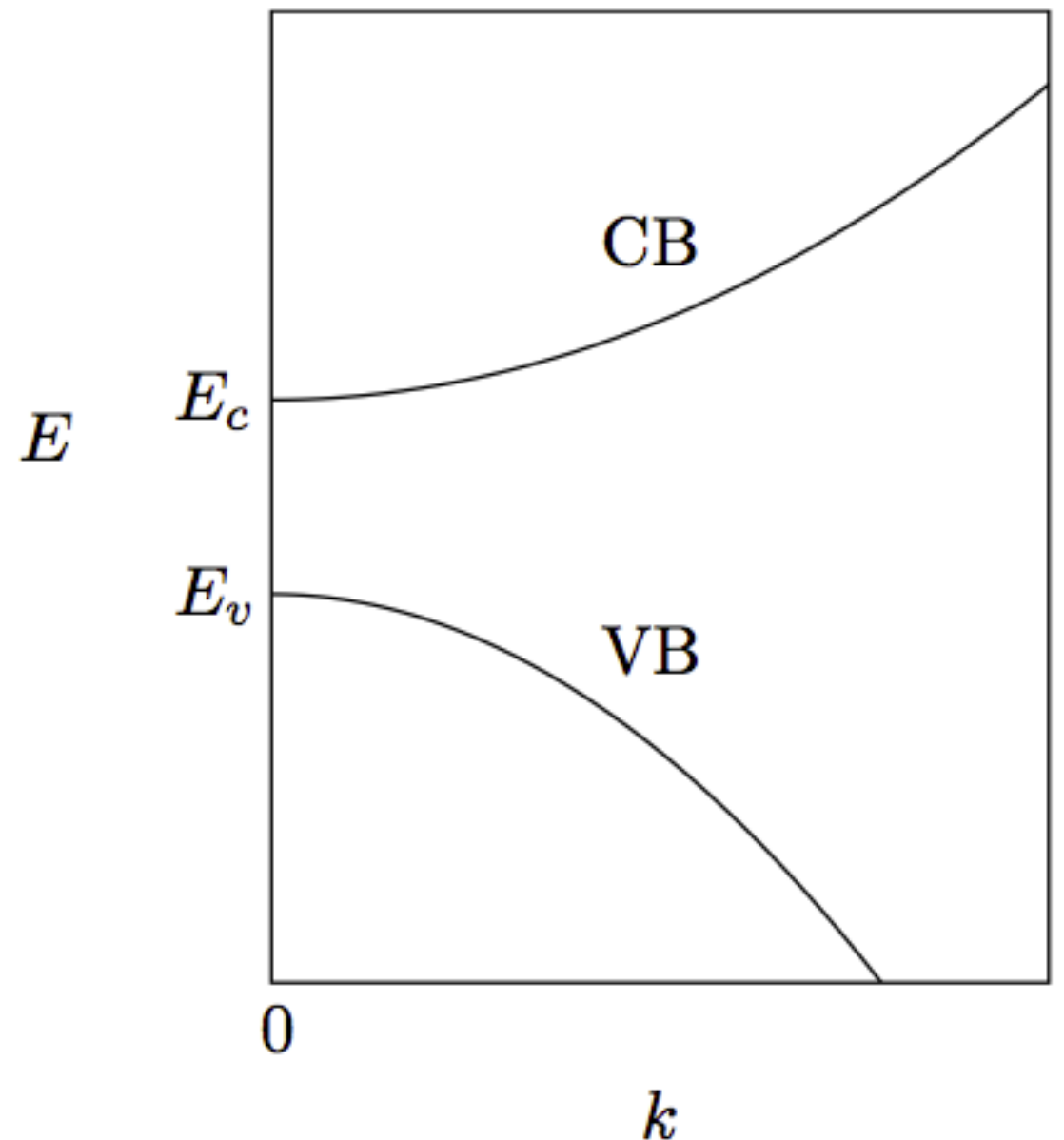
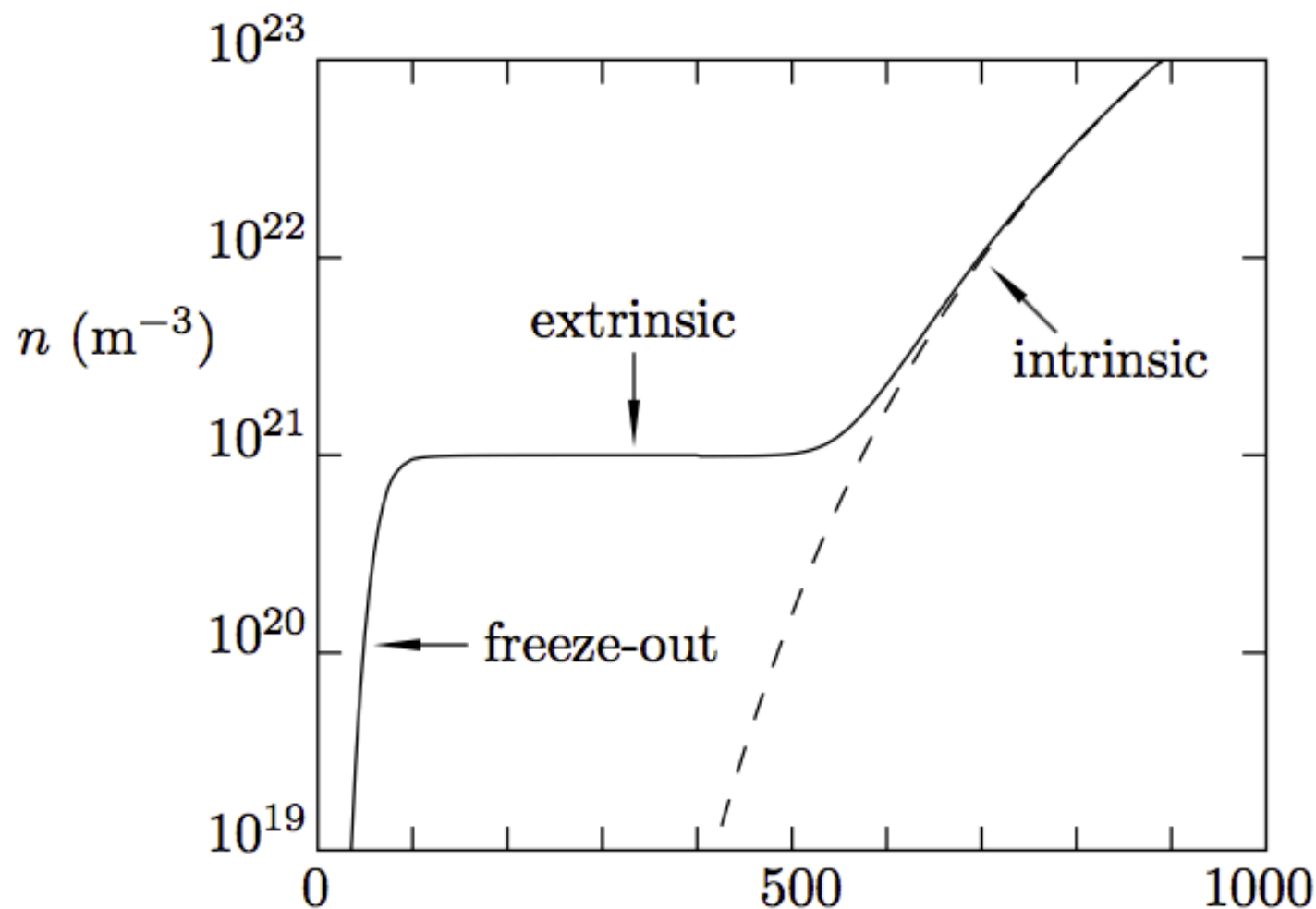
d) $p \approx 0$

a) $p \approx n_i$

c) $p \approx N_d$

Question #14

$$p \approx \frac{p_i^2}{N_d}$$



Consider a p-type semiconductor at high temperature (with donor density N_a), what will be the value of n ?

- c) $n \approx 0$
- d) $n \approx p_i$
- e) $n \approx N_a$

Question #15

Consider a p-type semiconductor at high temperature (with donor density N_a), what will be the value of n ?

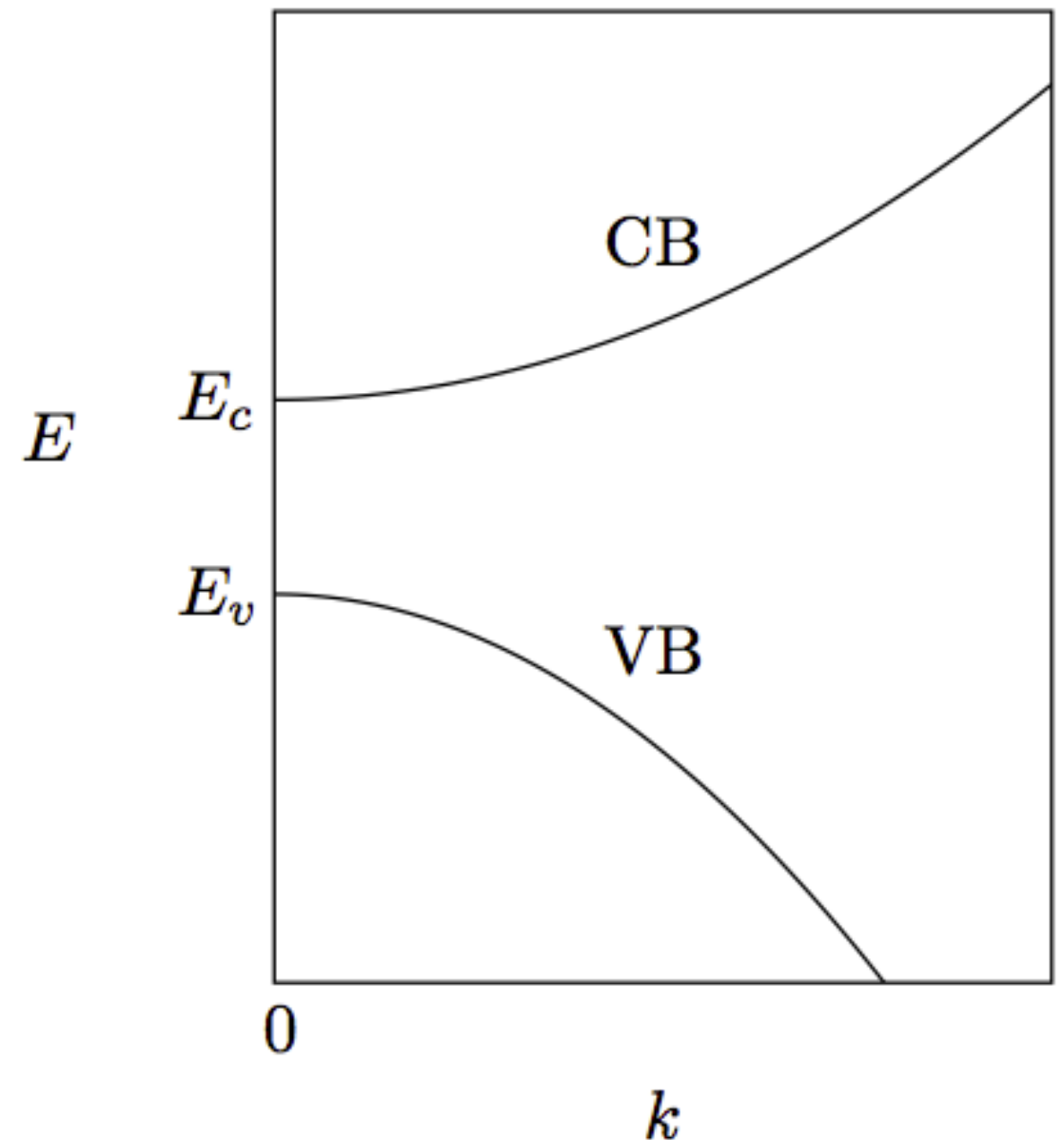
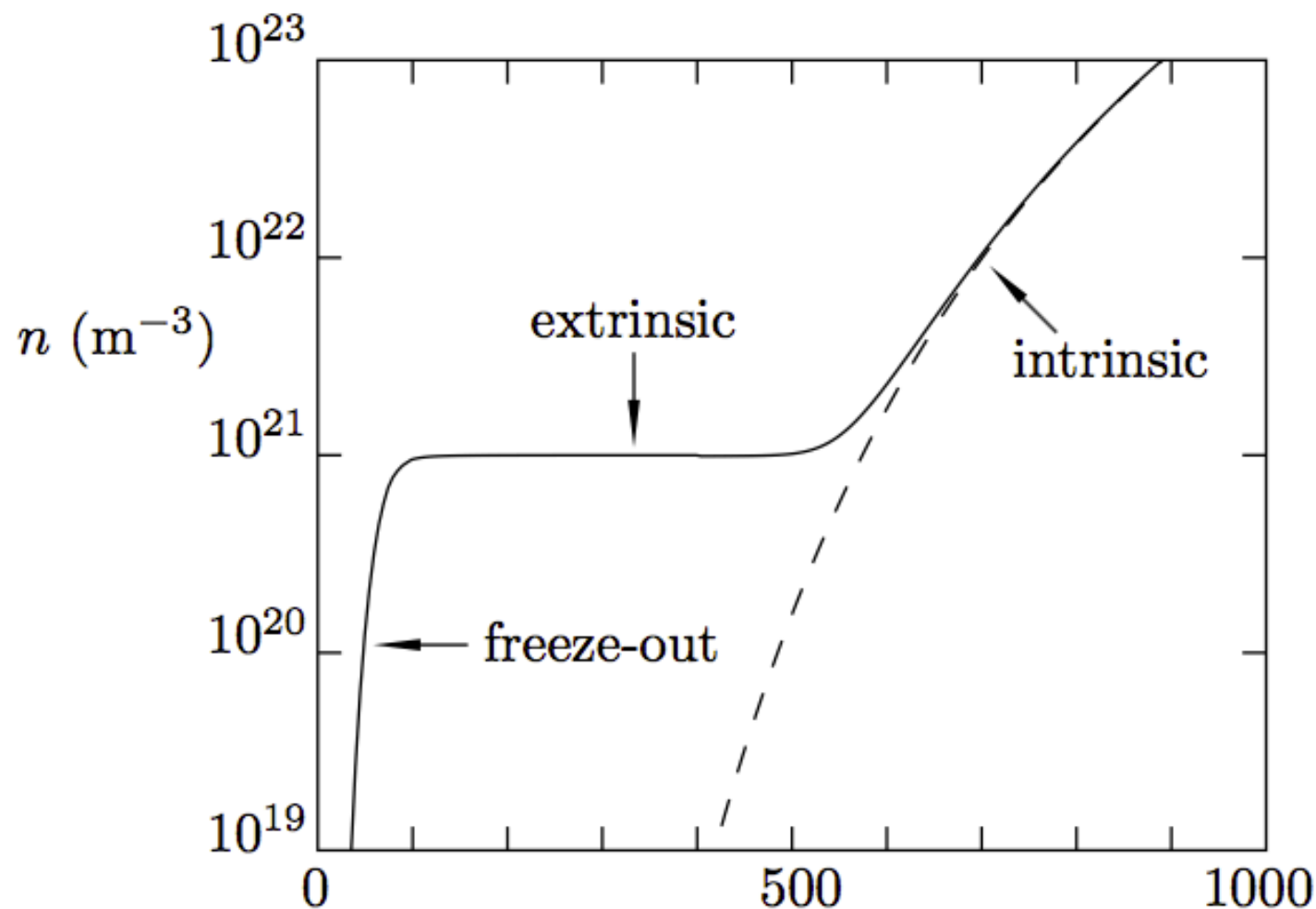
Question #15

c) $n \approx 0$

d) $n \approx p_i$

e) $n \approx N_a$

$$n \approx \frac{n_i^2}{N_a}$$



Question #16

If the we raise the temperature of a semiconductor, what happens to the mobility of the electrons and holes?

Question #16

If the we raise the temperature of a semiconductor, what happens to the mobility of the electrons and holes?

Question #16

- (A) Mobility of holes goes up; for electrons, goes down.
- (B) Mobility of holes goes down; for electrons, goes up.
- (C) both decrease.
- (D) both increase.
- (E) Nothing, unless the semiconductor is doped.

If the we raise the temperature of a semiconductor, what happens to the mobility of the electrons and holes?

If the we raise the temperature of a semiconductor, what happens to the mobility of the electrons and holes?

Answer: Mobility of both decreases

Why?

Question #17

Consider an n-type semiconductor at room temperature. If we increase the density of donor atoms, the mobility of the electrons in the conduction band

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Consider an n-type semiconductor at room temperature. If we increase the density of donor atoms, the mobility of the electrons in the conduction band

Question #17

- (A) remains the same.
- (B) decreases.
- (C) increases.
- (D) is irrelevant—only the holes are moving.

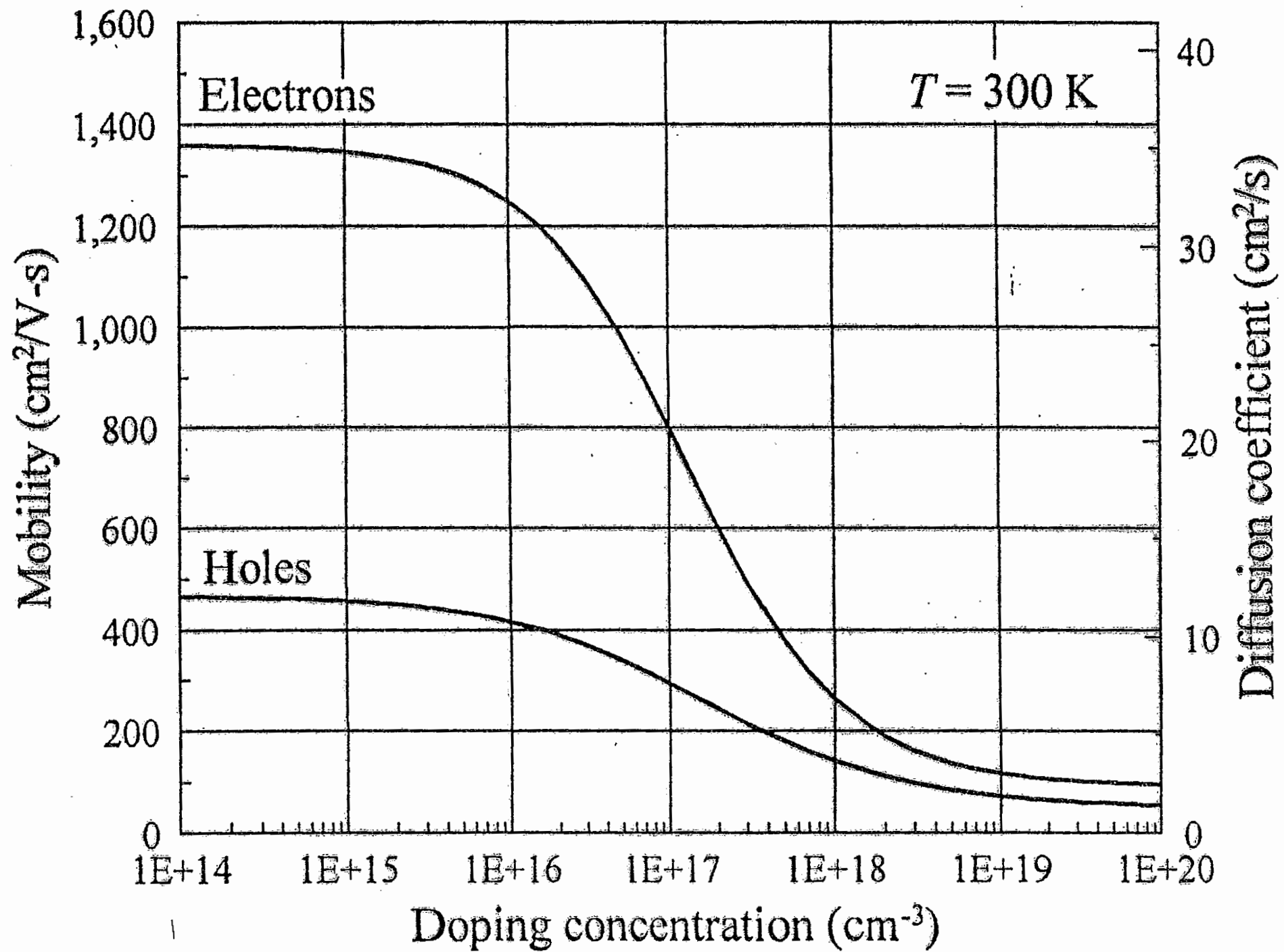


FIGURE 2.7. Electron and hole mobilities in bulk silicon at 300 K as a function of doping concentration.

Question #18

If we raise the temperature of an extrinsic semiconductor, what happens to its electrical conductivity? (Assume that the semiconductor remains extrinsic at the higher temperature.)

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- (D) Irrelevant, only the holes are moving.

If we raise the temperature of an extrinsic semiconductor, what happens to its electrical conductivity? (Assume that the semiconductor remains extrinsic at the higher temperature.) **Question #18**

- (A) conductivity remains the same.
- (B) conductivity increases.
- (C) conductivity decreases.
- (D) Irrelevant, only the holes are moving.

$$\mu_n = \frac{e\tau}{m^*}$$

$$\sigma_n = ne\mu_n$$

Question #19

If we raise the temperature of an intrinsic semiconductor, what happens to its electrical conductivity?

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If we raise the temperature of an intrinsic semiconductor, what happens to its electrical conductivity?

Question #19

- (A) conductivity remains the same.
- (B) conductivity increases.
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If we raise the temperature of an intrinsic semiconductor, what happens to its electrical conductivity?

Question #19

- (A) conductivity remains the same.
- (B) conductivity increases.
- (C) conductivity decreases.
- (D) Irrelevant, only the holes are moving.

$$\mu_n = \frac{e\tau}{m^*}$$

$$\sigma_n = ne\mu_n$$