

## 1 Day 2: Operators and Expectation Values

1. The momentum operator is defined as:

$$\hat{p} = -i\hbar \frac{\partial}{\partial x} \quad (1)$$

Find the eigenstates and eigenvalues for this operator.

2. A particle's wavefunction is given by:

$$\psi(x) = A(a^2 - x^2) \quad (2)$$

for  $-a \leq x \leq +a$  and  $\psi(x) = 0$  elsewhere

1. Find the normalization constant  $A$ .
2. Find the expectation values of  $x$ ,  $x^2$ ,  $p$ , and  $p^2$ .
3. Find  $\sigma_x$  and  $\sigma_p$  and verify that Heisenberg's uncertainty relation holds:  
 $\sigma_x \sigma_p \geq \frac{\hbar}{2}$