

$$\mathbf{G} = m_1 \mathbf{b}_1 + m_2 \mathbf{b}_2 + m_3 \mathbf{b}_3 \quad (2-24)$$

$$\mathbf{b}_i = \frac{2\pi \mathbf{a}_j \times \mathbf{a}_k}{\mathbf{a}_i \cdot (\mathbf{a}_j \times \mathbf{a}_k)} \quad (2-25)$$

$$G = 2k \sin \theta \quad (2-26)$$

$$\sin \theta = G/2k \quad (2-27)$$

$$F = -\alpha(r - r_0) \quad (3-1)$$

$$r = r_0 + A \sin \omega t \quad (3-2)$$

$$x_n = na \quad (3-3)$$

$$F_n = -\alpha(2u_n - u_{n+1} - u_{n-1}) \quad (3-4)$$

$$a_n = \frac{d^2 u_n}{dt^2} \quad (3-5)$$

$$-\alpha(2u_n - u_{n+1} - u_{n-1}) = m \frac{d^2 u_n}{dt^2} \quad (3-6)$$

$$u_n = A \sin(kx_n - \omega t) \quad (3-7)$$

$$\omega^2 = \omega_m^2 \sin^2(ka/2) \quad (3-8)$$

$$\omega = \omega_m |\sin(ka/2)| \quad (3-9)$$

$$\omega_m = \sqrt{4\alpha/m} \quad (3-10)$$

$$\omega = vk \quad (3-11)$$

$$\omega \approx (\omega_m a/2)|k| \quad (3-12)$$

$$v = \omega_m a/2 \quad (3-13)$$

$$-\alpha(2u_{2n} - u_{2n+1} - u_{2n-1}) = m_1 \frac{d^2 u_{2n}}{dt^2} \quad (3-14)$$

$$-\alpha(2u_{2n+1} - u_{2n+2} - u_{2n}) = m_2 \frac{d^2 u_{2n+1}}{dt^2} \quad (3-15)$$

$$u_{2n} = A_1 \sin(kx_{2n} - \omega t) \quad (3-16)$$

$$u_{2n+1} = A_2 \sin(kx_{2n+1} - \omega t) \quad (3-17)$$

$$\omega^2 = \alpha \left(\frac{1}{m_1} + \frac{1}{m_2} \right)$$

$$\pm \alpha \sqrt{\left(\frac{1}{m_1} + \frac{1}{m_2} \right)^2 - \frac{4 \sin^2(ka/2)}{m_1 m_2}} \quad (3-18)$$

$$A_2 = A_1(1 - m_1 \omega^2 / 2\alpha) \sec(ka/2) \quad (3-19)$$

$$\omega \approx ka \sqrt{\frac{\alpha}{2(m_1 + m_2)}} \quad (3-20)$$

$$\omega \approx \sqrt{2\alpha \left(\frac{1}{m_1} + \frac{1}{m_2} \right)} \quad (3-21)$$

$$v = a \sqrt{\frac{\alpha}{2(m_1 + m_2)}} \quad (3-22)$$

$$\omega = \sqrt{2\alpha/m_1} \quad (\text{acoustic branch}) \quad (3-23)$$

$$\omega = \sqrt{2\alpha/m_2} \quad (\text{optical branch}) \quad (3-24)$$

$$\mathbf{u}_n = \mathbf{A} \sin(\mathbf{k} \cdot \mathbf{r}_n - \omega t) \quad (3-25)$$

$$U = - \int_{r_0}^r F dr \quad (3-26)$$

$$U = \frac{1}{2} \alpha (r - r_0)^2 \quad (3-27)$$

$$\mathbf{F} = -e\mathbf{E} \quad (4-1)$$

$$\mathbf{a} = -(e/m)\mathbf{E} \quad (4-2)$$

$$\mathbf{r} = \frac{1}{2} \mathbf{a} t^2 + \mathbf{v}_0 t \quad (4-3)$$

$$\langle \mathbf{r} \rangle = \frac{1}{2} \mathbf{a} \langle t^2 \rangle \quad (4-4)$$

$$\mathbf{v}_d = \frac{1}{2} \mathbf{a} \langle t^2 \rangle / \tau \quad (4-5)$$

$$\mathbf{v}_d = -(e\tau/m)\mathbf{E} \quad (4-6)$$

$$\mathbf{J} = -ne\mathbf{v}_d \quad (4-7)$$

$$\mathbf{J} = (ne^2\tau/m)\mathbf{E} \quad (4-8)$$

$$\mathbf{J} = \sigma \mathbf{E} \quad (4-9)$$

$$\sigma = ne^2\tau/m \quad (4-10)$$

$$V = IR \quad (4-11)$$

$$R = L/A\sigma \quad (4-12)$$

$$\mathcal{E} = V/L$$

$$\mathbf{F} = -e\mathbf{v}_d \times \mathbf{B} \quad (4-13)$$

$$\mathbf{F} = -e(\mathbf{v}_d \times \mathbf{B}) - e\mathbf{E}_H \quad (4-14)$$

$$\mathbf{E}_H = -\mathbf{v}_d \times \mathbf{B} \quad (4-15)$$

$$\mathbf{E}_H = \frac{1}{ne} \mathbf{J} \times \mathbf{B} \quad (4-16)$$

$$\mathbf{E}_H = -R_H \mathbf{J} \times \mathbf{B} \quad (4-17)$$

$$R_H = -1/ne \quad (4-18)$$

$$\mathbf{F} = -e\mathbf{v} \times \mathbf{B} \quad (4-19)$$

$$evB = mv^2/r \quad (4-20)$$

$$\omega = eB/m \quad (4-21)$$

$$E = hf \quad (5-1)$$

$$p = h/\lambda \quad (5-2)$$

$$E = \hbar\omega \quad (5-3)$$

$$\mathbf{p} = \hbar\mathbf{k} \quad (5-4)$$

$$\hbar\omega_i = \hbar\omega_f + E \quad (5-5)$$

$$\hbar\mathbf{k}_i = \hbar\mathbf{k}_f + \mathbf{p} \quad (5-6)$$

$$E_f = E_i + \hbar\omega \quad (5-7)$$

$$\mathbf{p}_f = \mathbf{p}_i + \hbar\mathbf{k} \quad (5-8)$$

$$E_f = E_i - \hbar\omega \quad (5-9)$$

$$\mathbf{p}_f = \mathbf{p}_i - \hbar\mathbf{k} \quad (5-10)$$

$$\omega_f = \omega_i + \omega \quad (5-11)$$

$$\mathbf{k}_f = \mathbf{k}_i + \mathbf{k} \quad (5-12)$$

$$\omega_f = \omega_i - \omega \quad (5-13)$$

$$\mathbf{k}_f = \mathbf{k}_i - \mathbf{k} \quad (5-14)$$

$$k = k_i \sqrt{2} \quad (5-15)$$

$$\lambda = h/p \quad (5-16)$$

$$|z| = \sqrt{x^2 + y^2} \quad (6-1)$$

$$\exp(ix) = 1 + (ix) + \frac{1}{2}(ix)^2 + \frac{1}{6}(ix)^3 + \dots$$

$$= \sum_{n=0}^{\infty} \frac{1}{n!} (ix)^n \quad (6-2)$$

$$\exp(ix) = (1 - \frac{1}{2}x^2 + \dots) + i(x - \frac{1}{6}x^3 + \dots)$$

$$= \cos x + i \sin x \quad (6-3)$$

$$|\exp(ix)| = 1 \quad (6-4)$$

$$\psi = A \exp(ikx - i\omega t) \quad (6-5)$$

$$\psi = A \cos(kx - \omega t) + iA \sin(kx - \omega t) \quad (6-6)$$

$$\mathbf{R} = n_1 \mathbf{a}_1 + n_2 \mathbf{a}_2 + n_3 \mathbf{a}_3 \quad (1-6)$$

$$\mathbf{R} = a\hat{\mathbf{i}} \quad \text{or} \quad [100],$$

$$\mathbf{R} = a\hat{\mathbf{i}} + a\hat{\mathbf{j}} \quad \text{or} \quad [110], \quad (1-7)$$

$$\mathbf{R} = a\hat{\mathbf{i}} + a\hat{\mathbf{j}} + a\hat{\mathbf{k}} \quad \text{or} \quad [111].$$

$$\mathbf{a}_1 = -\frac{1}{2}a\hat{\mathbf{i}} + \frac{1}{2}a\hat{\mathbf{j}} + \frac{1}{2}a\hat{\mathbf{k}},$$

$$\mathbf{a}_2 = \frac{1}{2}a\hat{\mathbf{i}} - \frac{1}{2}a\hat{\mathbf{j}} + \frac{1}{2}a\hat{\mathbf{k}}, \quad (1-8)$$

$$\mathbf{a}_3 = \frac{1}{2}a\hat{\mathbf{i}} + \frac{1}{2}a\hat{\mathbf{j}} - \frac{1}{2}a\hat{\mathbf{k}}.$$

$$\mathbf{a}_1 = \frac{1}{2}a\hat{\mathbf{j}} + \frac{1}{2}a\hat{\mathbf{k}},$$

$$\mathbf{a}_2 = \frac{1}{2}a\hat{\mathbf{i}} + \frac{1}{2}a\hat{\mathbf{k}}, \quad (1-9)$$

$$\mathbf{a}_3 = \frac{1}{2}a\hat{\mathbf{i}} + \frac{1}{2}a\hat{\mathbf{j}}.$$

$$F = -\frac{e^2}{4\pi\epsilon_0 r^2} \quad (1-10)$$

$$F = Be^{-r/R},$$

$$y = A \sin(kx - \omega t) \quad (2-1)$$

$$k = 2\pi/\lambda \quad (2-2)$$

$$T = 1/f \quad (2-3)$$

$$\omega = 2\pi f \quad (2-4)$$

$$v = \lambda f \quad (2-5)$$

$$\omega = vk \quad (2-6)$$

$$x_2 - x_1 = n\lambda \quad (2-7)$$

$$x_2 - x_1 = (n + \frac{1}{2})\lambda \quad (2-8)$$

$$d \sin \theta = n\lambda \quad (2-9)$$

$$2d \sin \theta = n\lambda \quad (2-10)$$

$$\Delta x = R \cos \theta_1 + R \cos \theta_2 \quad (2-11)$$

$$R \cos \theta_1 + R \cos \theta_2 = n\lambda \quad (2-12)$$

$$\mathbf{R} \cdot \mathbf{k}_1 = Rk \cos(\pi - \theta_1) = -Rk \cos \theta_1 \quad (2-13)$$

$$\mathbf{R} \cdot \mathbf{k}_2 = Rk \cos \theta_2 \quad (2-14)$$

$$\mathbf{R} \cdot (\mathbf{k}_2 - \mathbf{k}_1) = nk\lambda = 2\pi n \quad (2-15)$$

$$\mathbf{R} \cdot \mathbf{G} = 2\pi n, \quad (2-16)$$

$$\mathbf{G} = \mathbf{k}_2 - \mathbf{k}_1 \quad (2-17)$$

$$\mathbf{R} = n_1 \mathbf{a}_1 + n_2 \mathbf{a}_2 + n_3 \mathbf{a}_3 \quad (2-18)$$

$$\mathbf{a}_1 \cdot \mathbf{G} = 2\pi m_1,$$

$$\mathbf{a}_2 \cdot \mathbf{G} = 2\pi m_2, \quad (2-19)$$

$$\mathbf{a}_3 \cdot \mathbf{G} = 2\pi m_3,$$

$$\mathbf{a}_1 = a\hat{\mathbf{i}}, \mathbf{a}_2 = a\hat{\mathbf{j}}, \mathbf{a}_3 = a\hat{\mathbf{k}} \quad (2-20)$$

$$G_x = m_1(2\pi/a), \quad G_y = m_2(2\pi/a),$$

$$G_z = m_3(2\pi/a) \quad (2-21)$$

$$\mathbf{G} = m_1 \frac{2\pi}{a} \hat{\mathbf{i}} + m_2 \frac{2\pi}{a} \hat{\mathbf{j}} + m_3 \frac{2\pi}{a} \hat{\mathbf{k}} \quad (2-22)$$

$$\mathbf{b}_1 = (2\pi/a)\hat{\mathbf{i}},$$

$$\mathbf{b}_2 = (2\pi/a)\hat{\mathbf{j}}, \quad (2-23)$$

$$\mathbf{b}_3 = (2\pi/a)\hat{\mathbf{k}},$$

$$-i\hbar \frac{\partial \psi}{\partial x} = p\psi, \quad (6-7)$$

$$i\hbar \frac{\partial \psi}{\partial t} = E\psi. \quad (6-8)$$

$$-\frac{\hbar^2}{2m} \frac{\partial^2 \psi}{\partial x^2} = i\hbar \frac{\partial \psi}{\partial t} \quad (6-9)$$

$$-\frac{\hbar^2}{2m} \frac{\partial^2 \psi}{\partial x^2} + U\psi = i\hbar \frac{\partial \psi}{\partial t} \quad (6-10)$$

$$|\psi|^2 = A^2 \quad (6-11)$$

$$\psi = A \int_{k_1}^{k_2} \exp(ikx - i\omega t) dk \quad (6-12)$$

$$\omega(k) \approx \omega(\bar{k}) + \left. \frac{d\omega}{dk} \right|_{k=\bar{k}} (k - \bar{k}) \quad (6-13)$$

$$\bar{k} = \frac{1}{2}(k_1 + k_2) \quad (6-14)$$

$$\bar{\omega} = \omega(\bar{k}) \quad (6-15)$$

$$v_g = \left. \frac{d\omega}{dk} \right|_{k=\bar{k}} \quad (6-16)$$

$$\omega = \bar{\omega} + (k - \bar{k})v_g \quad (6-17)$$

$$\psi = 2A \frac{\sin[(x - v_g t)\Delta k/2]}{x - v_g t} \exp(i\bar{k}x - i\bar{\omega}t) \quad (6-18)$$

$$\Delta k = k_2 - k_1 \quad (6-19)$$

$$|\psi|^2 = 4A^2 \frac{\sin^2[(x - v_g t)\Delta k/2]}{(x - v_g t)^2} \quad (6-20)$$

$$\omega = \frac{\hbar}{2m} k^2 \quad (6-21)$$

$$v_g = \frac{d\omega}{dk} = \frac{d}{dk} \left(\frac{\hbar}{2m} k^2 \right) = \frac{\hbar k}{m} = v \quad (6-22)$$

$$\text{Re } \psi = 2A \frac{\sin[(x - v_g t)\Delta k/2]}{x - v_g t} \cos(\bar{k}x - \bar{\omega}t) \quad (6-23)$$

$$\Delta x \Delta p \approx \hbar \quad (6-24)$$

$$\psi = A \exp(ikx - i\omega t) - A \exp(-ikx - i\omega t) \quad (6-25)$$

$$\psi(x, t) = 2iA \sin(kx) \exp(-i\omega t) \quad (6-26)$$

$$k = n(\pi/L) \quad (6-27)$$

$$\psi = \begin{cases} 2iA \sin(n\pi x/L) \exp(-i\omega t), & 0 \leq x \leq L, \\ 0, & x \leq 0 \text{ or } x \geq L. \end{cases} \quad (6-28)$$

$$|\psi|^2 = 4A^2 \sin^2(n\pi x/L) \quad (6-29)$$

$$\hbar^2 k^2 / 2m + U = \hbar\omega \quad (6-30)$$

$$k = \sqrt{\frac{2m(E - U)}{\hbar^2}} \quad (6-31)$$

$$k = i\alpha \quad (6-32)$$

$$\alpha = \sqrt{\frac{2m(U - E)}{\hbar^2}} \quad (6-33)$$

$$\psi = A \exp(-\alpha x) \exp(-i\omega t) \quad (6-34)$$

$$|\psi|^2 = A^2 \exp(-2\alpha x) \quad (6-35)$$

$$-\frac{\hbar^2}{2m} \left(\frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial y^2} + \frac{\partial^2 \psi}{\partial z^2} \right) + U\psi = i\hbar \frac{\partial \psi}{\partial t} \quad (6-36)$$

$$\psi = A \exp(i\mathbf{k} \cdot \mathbf{r} - i\omega t) \quad (6-37)$$

$$\mathbf{r} = x\hat{\mathbf{i}} + y\hat{\mathbf{j}} + z\hat{\mathbf{k}} \quad (6-38)$$

$$\mathbf{k} = k_x\hat{\mathbf{i}} + k_y\hat{\mathbf{j}} + k_z\hat{\mathbf{k}} \quad (6-39)$$

$$\mathbf{v}_g = \frac{\partial \omega}{\partial k_x} \hat{\mathbf{i}} + \frac{\partial \omega}{\partial k_y} \hat{\mathbf{j}} + \frac{\partial \omega}{\partial k_z} \hat{\mathbf{k}} \quad (6-40)$$

$$\psi(x, y, z, t) = A \sin(k_x x) \sin(k_y y) \sin(k_z z) \exp(-i\omega t), \quad (7-2)$$

$$\mathbf{k} = k_x\hat{\mathbf{i}} + k_y\hat{\mathbf{j}} + k_z\hat{\mathbf{k}} \quad (7-3)$$

$$k_x = n_x(\pi/L), \quad (7-4)$$

$$k_y = n_y(\pi/L), \quad (7-4)$$

$$k_z = n_z(\pi/L), \quad (7-4)$$

$$\psi(x + L, y, z, t) = \psi(x, y, z, t), \quad (7-5)$$

$$\psi(x, y + L, z, t) = \psi(x, y, z, t), \quad (7-5)$$

$$\psi(x, y, z + L, t) = \psi(x, y, z, t). \quad (7-5)$$

$$\psi(x, y, z, t) = A \exp(ik_x x + ik_y y + ik_z z - i\omega t) \quad (7-6)$$

$$k_x = n_x(2\pi/L), \quad (7-7)$$

$$k_y = n_y(2\pi/L), \quad (7-7)$$

$$k_z = n_z(2\pi/L). \quad (7-7)$$

$$\mathbf{k} = (2\pi/L)(n_x\hat{\mathbf{i}} + n_y\hat{\mathbf{j}} + n_z\hat{\mathbf{k}}) \quad (7-8)$$

$$g(\mathbf{k}) = 2V/(2\pi)^3 \quad (7-9)$$

$$E = p^2/2m = \hbar^2 k^2/2m \quad (7-10)$$

$$k = \sqrt{2mE/\hbar^2} \quad (7-11)$$

$$V_k = \frac{4}{3}\pi k^3 = \frac{4}{3}\pi(2mE/\hbar^2)^{3/2} \quad (7-12)$$

$$N(E) = V_k g(\mathbf{k}) = (V/3\pi^2)(2mE/\hbar^2)^{3/2} \quad (7-13)$$

$$N(E) = \int_0^E g(E) dE \quad (7-14)$$

$$g(E) = \frac{dN(E)}{dE} \quad (7-15)$$

$$g(E) = (V/2\pi^2)(2m/\hbar^2)^{3/2} E^{1/2} \quad (7-16)$$

$$N = V_k g(\mathbf{k}) = (V/3\pi^2)(2mE_F/\hbar^2)^{3/2}. \quad (7-17)$$

$$E_F = (\hbar^2/2m)(3\pi^2 n)^{2/3} \quad (7-18)$$

$$W_{21} = W_{12} \exp\left(\frac{E_2 - E_1}{k_B T}\right) \quad (7-19)$$

$$N = V_k g(\mathbf{k}) = (V/3\pi^2)(2mE_F/\hbar^2)^{3/2}. \quad (7-17)$$

$$W'_{21} = W_{21} P_2(1 - P_1) \quad (7-21)$$

$$W_{12} P_1(1 - P_2) = W_{21} P_2(1 - P_1) \quad (7-22)$$

$$\frac{P_1}{1 - P_1} \exp(E_1/k_B T) = \frac{P_2}{1 - P_2} \exp(E_2/k_B T). \quad (7-23)$$

$$\frac{P_n}{1 - P_n} \exp(E_n/k_B T) = \text{constant} \quad (7-24)$$

$$\text{constant} = \exp(E_F/k_B T) \quad (7-25)$$

$$P_n = \frac{1}{\exp\left(\frac{E_n - E_F}{k_B T}\right) + 1} \quad (7-26)$$

$$f_D(E) = \frac{1}{\exp\left(\frac{E - E_F}{k_B T}\right) + 1} \quad (7-27)$$

$$f_D(E) = \begin{cases} 1, & E < E_F, \\ 0, & E > E_F. \end{cases} \quad (7-28)$$

$$N = \int_0^\infty f_D(E) g(E) dE \quad (7-29)$$

$$\Delta \mathbf{k} = (1/\hbar) \Delta \mathbf{p} = (m/\hbar) \mathbf{v}_d \quad (7-30)$$

$$J \approx (nv_d/v_F) e v_F = n e v_d \quad (7-31)$$

$$v_d = e \tau_F \mathcal{E} / m \quad (7-32)$$

$$\sigma = n e^2 \tau_F / m \quad (7-33)$$

$$\ell = v_F \tau_F \quad (7-34)$$

$$E = (\hbar^2/2m) k^2 \quad (8-1)$$

$$\psi = A \exp(\pm i\pi x/a - i\omega t) \quad (8-2)$$

$$\psi_1 = 2A \cos(\pi x/a) \exp(-i\omega t) \quad (8-3)$$

$$\psi_2 = 2iA \sin(\pi x/a) \exp(-i\omega t) \quad (8-3)$$

$$|\psi_1|^2 = 4A^2 \cos^2(\pi x/a) \quad (8-4)$$

$$|\psi_2|^2 = 4A^2 \sin^2(\pi x/a) \quad (8-4)$$

$$\psi = u_k(x) \exp(ikx - i\omega t) \quad (8-5)$$

$$u_k(x + a) = u_k(x) \quad (8-6)$$

$$\psi = u_{k'}(x) \exp(ik'x - i\omega t) \quad (8-7)$$

$$\psi = u_{n,k}(x) \exp(ikx - i\omega t) \quad (8-8)$$

$$u_{n,k}(x) = u_{k'}(x) \exp(-i2\pi n x/a) \quad (8-9)$$

$$\psi = u_{\mathbf{k}}(\mathbf{r}) \exp(i\mathbf{k} \cdot \mathbf{r} - i\omega t), \quad (8-10)$$

$$\mathbf{r} = x\hat{\mathbf{i}} + y\hat{\mathbf{j}} + z\hat{\mathbf{k}} \quad (8-11)$$

$$\mathbf{k} = k_x\hat{\mathbf{i}} + k_y\hat{\mathbf{j}} + k_z\hat{\mathbf{k}} \quad (8-12)$$

$$u_{\mathbf{k}}(\mathbf{r} + \mathbf{R}) = u_{\mathbf{k}}(\mathbf{r}) \quad (8-13)$$

$$V_k = (2\pi)^3/V_c \quad (8-14)$$

$$V_k g(\mathbf{k}) = [(2\pi)^3/V_c] [2V/(2\pi)^3] = 2V/V_c \quad (8-15)$$

$$v = \frac{d\omega}{dk} = \frac{1}{\hbar} \frac{dE}{dk} \quad (9-1)$$

$$dE = F_{\text{ext}} dx \quad (9-2)$$

$$dE = F_{\text{ext}} v dt \quad (9-3)$$

$$\frac{dE}{dt} = F_{\text{ext}} v \quad (9-4)$$

$$\frac{dE}{dt} = F_{\text{ext}} \frac{1}{\hbar} \frac{dE}{dk} \quad (9-5)$$

$$F_{\text{ext}} = \hbar \frac{dk}{dt} \quad (9-6)$$

$$F = \frac{d(\hbar k)}{dt} = \frac{dp}{dt} = m \frac{dv}{dt} = ma. \quad (9-7)$$

$$\mathbf{F}_{\text{ext}} = \hbar \frac{d\mathbf{k}}{dt} \quad (9-8)$$

$$\frac{d\mathbf{k}}{dt} = -(e/\hbar) \mathcal{E} \quad (9-9)$$

$$a = \frac{dv}{dt} = \frac{dv}{dk} \frac{dk}{dt} \quad (9-10)$$

$$a = \left(\frac{1}{\hbar} \frac{d^2 E}{dk^2} \right) \left(\frac{1}{\hbar} F_{\text{ext}} \right) \quad (9-11)$$

$$m^* = \left(\frac{1}{\hbar^2} \frac{d^2 E}{dk^2} \right)^{-1} \quad (9-12)$$

$$a = F_{\text{ext}}/m^* \quad (9-13)$$

$$E_p = -E_n \quad (9-14)$$

$$\mathbf{k}_p = -\mathbf{k}_n \quad (9-15)$$

$$q_p = -q_n = +e \quad (9-16)$$

$$\mathbf{a} = \mathbf{F}_{\text{ext}}/m_p^* \quad (9-17)$$

$$m_p^* = \left(\frac{1}{\hbar^2} \frac{d^2 E_p}{dk_p^2} \right)^{-1}. \quad (9-18)$$

$$m_p^* = -m_n^* \quad (9-19)$$

$$\mathbf{\mathcal{E}}_H = -R_H \mathbf{J} \times \mathbf{B} \quad (9-20)$$

$$R_H = -1/ne \quad (9-21)$$

$$R_H = +1/pe \quad (9-22)$$

$$\omega = eB/m^* \quad (9-23)$$

$$E_g = E_c - E_v \quad (10-1)$$

$$E(k) = E(0) + \left. \frac{dE}{dk} \right|_{k=0} k + \frac{1}{2} \left. \frac{d^2 E}{dk^2} \right|_{k=0} k^2 + \dots \quad (10-2)$$

$$E = E_c + \frac{\hbar^2}{2m_n^*} k^2 \quad (10-3)$$

$$E = E_v - \frac{\hbar^2}{2m_p^*} k^2 \quad (10-4)$$

$$g(E) = \frac{V}{2\pi^2} (2m_n^*/\hbar^2)^{3/2} (E - E_c)^{1/2}. \quad (10-5)$$

$$g(E) = \frac{V}{2\pi^2} (2m_p^*/\hbar^2)^{3/2} (E_v - E)^{1/2}. \quad (10-6)$$

$$f_D(E) = \frac{1}{\exp\left(\frac{E - E_F}{k_B T}\right) + 1} \quad (10-7)$$

$$N = \int_{E_c}^{\infty} f_D(E) g(E) dE \quad (10-8)$$

$$n = \frac{1}{V} \int_{E_c}^{\infty} f_D(E) g(E) dE \quad (10-9)$$

$$f_D(E) \approx \exp\left(-\frac{E - E_F}{k_B T}\right) \quad (10-10)$$

$$n = N_c \exp\left(-\frac{E_c - E_F}{k_B T}\right) \quad (10-11)$$

$$N_c = 2 \left(\frac{m_n^* k_B T}{2\pi \hbar^2} \right)^{3/2}. \quad (10-12)$$

$$\int_0^{\infty} \sqrt{x} e^{-x} dx = \frac{1}{2} \sqrt{\pi},$$

$$p = \frac{1}{V} \int_{-E_v}^{E_v} [1 - f_D(E)] g(E) dE \quad (10-13)$$

$$1 - f_D(E) \approx \exp\left(-\frac{E_F - E}{k_B T}\right) \quad (10-14)$$

$$p = N_v \exp\left(-\frac{E_F - E_v}{k_B T}\right) \quad (10-15)$$

$$N_v = 2 \left(\frac{m_p^* k_B T}{2\pi \hbar^2} \right)^{3/2}. \quad (10-16)$$

$$E_F = \frac{1}{2} (E_c + E_v) + \frac{1}{2} k_B T \ln(N_v/N_c) \quad (10-17)$$

$$n_i = p_i = \sqrt{N_c N_v} \exp\left(-\frac{E_g}{2k_B T}\right). \quad (10-18)$$

$$np = N_c N_v \exp\left(-\frac{E_g}{k_B T}\right) \quad (10-19)$$

$$np = n_i p_i = n_i^2 \quad (10-20)$$

$$n \approx N_d, \quad (10-21)$$

$$p \approx n_i^2/N_d.$$

$$p \approx N_a, \quad (10-22)$$

$$n \approx n_i^2/N_a.$$

$$\sigma_n = ne^2 \tau_n / m_n^* \quad (10-23)$$

$$\mathbf{J} = \sigma_n \mathbf{\mathcal{E}} \quad (10-24)$$

$$\mathbf{J} = -ne \mathbf{v}_d \quad (10-25)$$

$$\mathbf{v}_d = -\frac{\sigma_n}{ne} \mathbf{\mathcal{E}} = -\frac{e \tau_n}{m_n^*} \mathbf{\mathcal{E}} \quad (10-26)$$

$$\mu_n = e \tau_n / m_n^* \quad (10-27)$$

$$\mathbf{v}_d = -\mu_n \mathbf{\mathcal{E}} \quad (10-28)$$

$$\sigma_n = ne \mu_n \quad (10-29)$$

$$\sigma_p = pe^2 \tau_p / m_p^* \quad (10-30)$$

$$\mu_p = e \tau_p / m_p^* \quad (10-31)$$

$$\mathbf{v}_d = \mu_p \mathbf{\mathcal{E}} \quad (10-32)$$

$$\sigma_p = pe \mu_p \quad (10-33)$$

$$\sigma = \sigma_n + \sigma_p \quad (10-34)$$

$$\mathbf{\mathcal{E}}_H = -R_H \mathbf{J} \times \mathbf{B} \quad (10-35)$$

$$R_H = -1/ne \quad (10-36)$$

$$R_H = +1/pe \quad (10-37)$$

$$\mu_n = -\sigma R_H \quad (10-38)$$

$$\mu_p = \sigma R_H \quad (10-39)$$

$$E_F = \frac{1}{2} (E_c + E_v) + \frac{1}{2} k_B T \ln \left[(N_v/N_c)^{1/2} (N_d/n_i) \right] \quad (11-1)$$

$$E_F = \frac{1}{2} (E_{cn} + E_{vn}) + \frac{1}{2} k_B T \ln \left[(N_v/N_c)^{1/2} (N_d/n_i) \right] \quad (11-2)$$

$$E_F = \frac{1}{2} (E_{cp} + E_{vp}) - \frac{1}{2} k_B T \ln \left[(N_c/N_v)^{1/2} (N_a/n_i) \right] \quad (11-3)$$

$$E_{vp} - E_{vn} = k_B T \ln(N_d N_a / n_i^2) \quad (11-4)$$

$$e\phi = E_{vp} - E_{vn} \quad (11-5)$$

$$\phi = (k_B T / e) \ln(N_d N_a / n_i^2) \quad (11-6)$$

$$\oint \mathbf{\mathcal{E}} \cdot d\mathbf{S} = Q/\epsilon \quad (11-7)$$

$$\epsilon = \epsilon_r \epsilon_0 \quad (11-8)$$

$$\mathbf{\mathcal{E}} = \mathcal{E} \hat{\mathbf{i}} \quad (11-9)$$

$$\frac{d\mathcal{E}}{dx} = \frac{\rho}{\epsilon_r \epsilon_0} \quad (11-10)$$

$$\mathcal{E} = \frac{1}{\epsilon_r \epsilon_0} \int_{-\infty}^x \rho dx. \quad (11-11)$$

$$\mathcal{E} = \begin{cases} -(eN_d/\epsilon_r \epsilon_0)(\frac{1}{2}x_d + x), & -\frac{1}{2}x_d \leq x \leq 0, \\ -(eN_d/\epsilon_r \epsilon_0)(\frac{1}{2}x_d - x), & 0 \leq x \leq \frac{1}{2}x_d, \\ 0, & \text{otherwise.} \end{cases} \quad (11-12)$$

$$\mathcal{E}_{\max} = eN_d x_d / 2\epsilon_r \epsilon_0 \quad (11-13)$$

$$\Delta U = - \int_{-\infty}^{\infty} F dx \quad (11-14)$$

$$\Delta U = e \int_{-x_d/2}^{x_d/2} \mathcal{E} dx \quad (11-15)$$

$$\Delta U = -e^2 N_d x_d^2 / 4\epsilon_r \epsilon_0 \quad (11-16)$$

$$\phi = eN_d x_d^2 / 4\epsilon_r \epsilon_0 \quad (11-17)$$

$$x_d = \sqrt{4\epsilon_r \epsilon_0 \phi / eN_d} \quad (11-18)$$

$$\mathcal{E}_{\max} = \sqrt{eN_d \phi / \epsilon_r \epsilon_0} \quad (11-19)$$

$$I_{nr0} = I_{ng0} \quad (11-20)$$

$$I_{pr0} = I_{pg0} \quad (11-21)$$

$$E_{cp} = E_{vn} + E_g + e(\phi - V_a) \quad (11-22)$$

$$n(V_a) = \frac{1}{V} \int_{E_{cp}}^{\infty} f_D(E) g(E) dE \quad (11-23)$$

$$n(V_a) = N_c \exp\left(-\frac{E_{cp} - E_F}{k_B T}\right) \quad (11-24)$$

$$n(V_a) = N_c \times \exp\left(-\frac{E_{vn} + E_g + e(\phi - V_a) - E_F}{k_B T}\right) \quad (11-25)$$

$$n(V_a) = n(0) \exp(eV_a / k_B T) \quad (11-26)$$

$$I_{nr} = I_{nr0} \exp(eV_a / k_B T) \quad (11-27)$$

$$I_{pr} = I_{pr0} \exp(eV_a / k_B T) \quad (11-28)$$

$$I_{ng} = I_{ng0} \quad (11-29)$$

$$I_{pg} = I_{pg0} \quad (11-30)$$

$$I = I_{nr} - I_{ng} + I_{pr} - I_{pg} \quad (11-31)$$

$$I = I_0 [\exp(eV_a / k_B T) - 1] \quad (11-32)$$

$$I_0 = I_{ng0} + I_{pg0} \quad (11-33)$$

$$x_d = \sqrt{4\epsilon_r \epsilon_0 (\phi - V_a) / eN_d} \quad (11-34)$$

$$\mathcal{E}_{\max} = \sqrt{eN_d (\phi - V_a) / \epsilon_r \epsilon_0}. \quad (11-35)$$

$$C = \frac{\epsilon_r \epsilon_0 A}{x_d} \quad (11-36)$$

$$C = A \sqrt{eN_d \epsilon_r \epsilon_0 / 4(\phi - V_a)} \quad (11-37)$$

$$p = mv = \frac{m}{\hbar} \frac{dE}{dk} \quad (12-1)$$

$$\oint \mathbf{\mathcal{E}} \cdot d\mathbf{l} = -d\Phi_B / dt \quad (13-1)$$

$$\mathbf{B} = \mathbf{B}_0 \exp(-x/\lambda) \quad (13-2)$$

$$\lambda = \frac{\lambda_0}{\sqrt{1 - (T/T_c)^4}} \quad (13-3)$$

$$B_c(T) = B_c(0) [1 - (T/T_c)^2] \quad (13-4)$$

$$B = \mu_0 I / 2\pi R \quad (13-5)$$

$$I_c = 2\pi r B_c / \mu_0 \quad (13-6)$$

$$\mathbf{k}_{1f} = \mathbf{k}_{1i} - \mathbf{k} \quad (13-7)$$

$$\mathbf{k}_{2f} = \mathbf{k}_{2i} + \mathbf{k} \quad (13-7)$$

$$\mathbf{k}_{1f} + \mathbf{k}_{2f} = \mathbf{k}_{1i} + \mathbf{k}_{2i} \quad (13-8)$$

$$\mathbf{k}_1 + \mathbf{k}_2 = \text{constant} \quad (13-9)$$

$$\psi = \sum_{i,j} A_{ij} \psi_1(\mathbf{k}_i) \psi_2(\mathbf{k}_j) \quad (13-10)$$

$$2\Delta \approx 3.5 k_B T_c \quad (13-11)$$

$$\mathbf{k}_1 + \mathbf{k}_2 = \Delta \mathbf{k} \quad (13-12)$$

The Periodic Table of the Elements																		2 He 4.003				
1 H 1.008		1st line: atomic number 2nd line: atomic symbol 3rd line: atomic mass												5 B 10.81		6 C 12.01	7 N 14.01	8 O 16.00	9 F 19.00	10 Ne 20.18		
3 Li 6.941														4 Be 9.012		13 Al 26.98		14 Si 28.09	15 P 30.97	16 S 32.07	17 Cl 35.45	18 Ar 39.95
11 Na 22.99														12 Mg 24.31								
19 K 39.10		20 Ca 40.08	21 Sc 44.96	22 Ti 47.88	23 V 50.94	24 Cr 52.00	25 Mn 54.94	26 Fe 55.85	27 Co 58.93	28 Ni 58.69	29 Cu 63.55	30 Zn 65.39	31 Ga 69.72	32 Ge 72.59	33 As 74.92	34 Se 78.96	35 Br 79.90	36 Kr 83.80				
37 Rb 85.47		38 Sr 87.62	39 Y 88.91	40 Zr 91.22	41 Nb 92.91	42 Mo 95.94	43 Tc (98)	44 Ru 101.1	45 Rh 102.9	46 Pd 106.4	47 Ag 107.9	48 Cd 112.4	49 In 114.8	50 Sn 118.7	51 Sb 121.8	52 Te 127.6	53 I 126.9	54 Xe 131.3				
55 Cs 132.9		56 Ba 137.3	57 La 138.9	72 Hf 178.5	73 Ta 180.9	74 W 183.9	75 Re 186.2	76 Os 190.2	77 Ir 192.2	78 Pt 195.1	79 Au 197.0	80 Hg 200.6	81 Tl 204.4	82 Pb 207.2	83 Bi 209.0	84 Po (209)	85 At (210)	86 Rn (222)				
87 Fr (223)		88 Ra 226.0	89 Ac 227.0	104 Rf (261)	105 Db	106 Sg	107 Bh	108 Hs	109 Mt													

58 Ce 140.1	59 Pr 140.9	60 Nd 144.2	61 Pm (145)	62 Sm 150.4	63 Eu 152.0	64 Gd 157.3	65 Tb 158.9	66 Dy 162.5	67 Ho 164.9	68 Er 167.3	69 Tm 168.9	70 Yb 173.0	71 Lu 175.0
90 Th 232.0	91 Pa 231.0	92 U 238.0	93 Np 237.0	94 Pu (244)	95 Am (243)	96 Cm (247)	97 Bk (247)	98 Cf (251)	99 Es (252)	100 Fm (257)	101 Md (258)	102 No (259)	103 Lr (260)

89 Ac	actinium	68 Er	erbium	101 Md	mendelevium	104 Rf	rutherfordium
13 Al	aluminum	63 Eu	europium	80 Hg	mercury	62 Sm	samarium
95 Am	americium	100 Fm	fermium	42 Mo	molybdenum	21 Sc	scandium
51 Sb	antimony	9 F	fluorine	60 Nd	neodymium	106 Sg	seaborgium
18 Ar	argon	87 Fr	francium	10 Ne	neon	34 Se	selenium
33 As	arsenic	64 Gd	gadolinium	93 Np	neptunium	14 Si	silicon
85 At	astatine	31 Ga	gallium	28 Ni	nickel	47 Ag	silver
56 Ba	barium	32 Ge	germanium	41 Nb	niobium	11 Na	sodium
97 Bk	berkelium	79 Au	gold	7 N	nitrogen	38 Sr	strontium
4 Be	beryllium	72 Hf	hafnium	102 No	nobelium	16 S	sulfur
83 Bi	bismuth	108 Hs	hassium	76 Os	osmium	73 Ta	tantalum
107 Bh	bohrium	2 He	helium	8 O	oxygen	43 Tc	technetium
5 B	boron	67 Ho	holmium	46 Pd	palladium	52 Te	tellurium
35 Br	bromine	1 H	hydrogen	15 P	phosphorus	65 Tb	terbium
48 Cd	cadmium	49 In	indium	78 Pt	platinum	81 Tl	thallium
20 Ca	calcium	53 I	iodine	94 Pu	plutonium	90 Th	thorium
98 Cf	californium	77 Ir	iridium	84 Po	polonium	69 Tm	thulium
6 C	carbon	26 Fe	iron	19 K	potassium	50 Sn	tin
58 Ce	cerium	36 Kr	krypton	59 Pr	praseodymium	22 Ti	titanium
55 Cs	cesium	57 La	lanthanum	61 Pm	promethium	74 W	tungsten
17 Cl	chlorine	103 Lr	lawrencium	91 Pa	protactinium	92 U	uranium
24 Cr	chromium	82 Pb	lead	88 Ra	radium	23 V	vanadium
27 Co	cobalt	3 Li	lithium	86 Rn	radon	54 Xe	xenon
29 Cu	copper	71 Lu	lutetium	75 Re	rhenium	70 Yb	ytterbium
96 Cm	curium	12 Mg	magnesium	45 Rh	rhodium	39 Y	yttrium
105 Db	dubnium	25 Mn	manganese	37 Rb	rubidium	30 Zn	zinc
66 Dy	dysprosium	109 Mt	meitnerium	44 Ru	ruthenium	40 Zr	zirconium
99 Es	einsteinium						

Listed below are the crystal structures of various elements and compounds. The lattice parameters a in units of Å are also given.

Elements with a bcc lattice					
Li	3.50	Ba	5.02	Mo	3.14
Na	4.30	V	3.04	W	3.15
K	5.20	Nb	3.30	Fe	2.86
Rb	5.59	Ta	3.32	Eu	4.58
Cs	6.50	Cr	2.87		
Elements with an fcc lattice					
Ca	5.56	Pd	3.87	Al	4.04
Sr	6.08	Pt	3.90	Pb	4.93
Ac	5.31	Cu	3.61	Ce	5.12
Rh	3.80	Ag	4.07	Yb	5.48
Ir	3.82	Au	4.07	Th	5.08
Ni	3.52				
Elements with the diamond structure					
C	3.56	Ge	5.65	Sn	6.46
Si	5.42				
Compounds with the cesium chloride structure					
CsCl	4.11	TlI	4.18	CuPd	2.99
CsBr	4.28	TlSb	3.85	AgZn	3.16
CsI	4.56	TlBi	3.90	AuZn	3.15
TlCl	3.84	CuZn	2.95	AlNi	2.82
TlBr	3.97				

Compounds with the sodium chloride structure					
LiF	4.02	RbI	7.32	BaTe	6.99
LiCl	5.14	CsF	6.00	MnO	4.43
LiBr	5.49	MgO	4.20	MnS	5.21
LiI	6.00	MgS	5.19	MnSe	5.45
NaF	4.61	MgSe	5.45	FeO	4.28
NaCl	5.63	CaO	4.80	CoO	4.25
NaBr	5.96	CaS	5.68	NiO	4.17
NaI	6.46	CaSe	5.91	AgF	4.92
KF	5.36	CaTe	6.34	AgCl	5.54
KCl	6.27	SrO	5.15	AgBr	5.76
KBr	6.58	SrS	6.01	CdO	4.70
KI	7.05	SrSe	6.23	SnTe	6.28
RbF	5.63	SrTe	6.65	PbS	5.93
RbCl	6.53	BaO	5.53	PbSe	6.14
RbBr	6.85	BaSe	6.59	PbTe	6.44
Compounds with the zincblende structure					
BeS	4.86	ZnTe	6.09	GaP	5.44
CuCl	5.41	CdTe	6.46	GaAs	5.64
CuBr	5.68	AlP	5.45	GaSb	6.09
CuI	6.05	AlAs	5.63	InSb	6.45
ZnS	5.42	AlSb	6.10	SnSb	6.13
ZnSe	5.66				

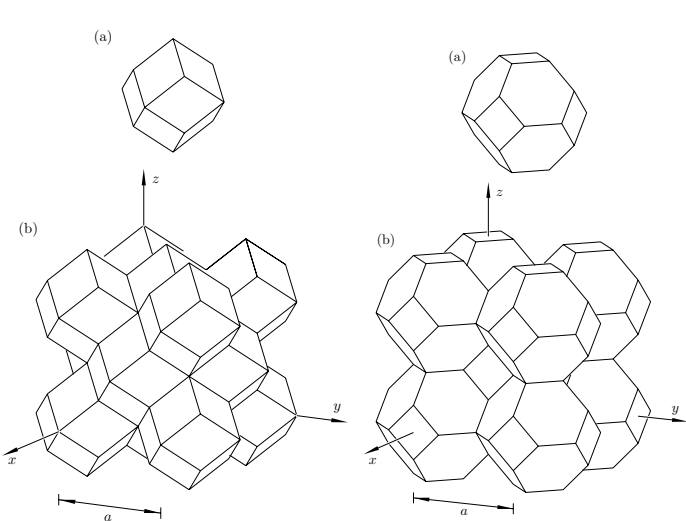


Fig. 1-19. (a) The Wigner-Seitz cell for the fcc lattice. (b) These cells fit together to fill all space.

Fig. 1-16. (a) The Wigner-Seitz cell for the bcc lattice. (b) These cells fit together to fill all space.

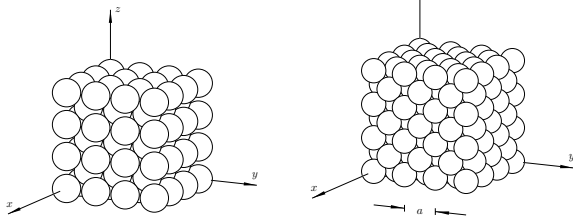


Fig. 1-12. Body-centered cubic arrangement of atoms.

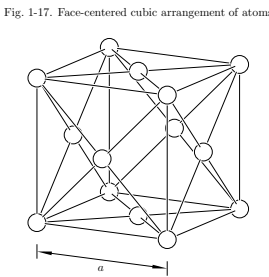


Fig. 1-18. The conventional unit cell of the fcc lattice.

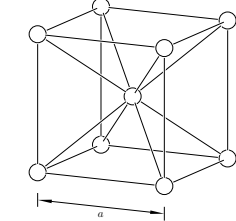


Fig. 1-13. The conventional unit cell of the bcc lattice.

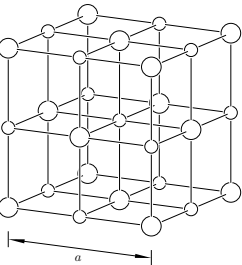


Fig. 1-21. The conventional unit cell for the sodium chloride structure. The large and small spheres represent two different types of atoms.

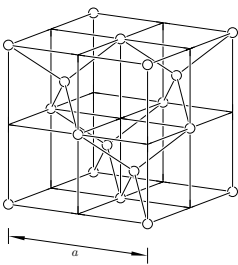


Fig. 1-27. The conventional unit cell of the diamond structure. All atoms are identical.

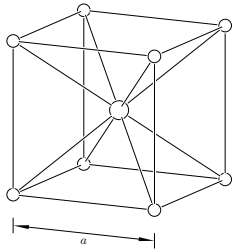


Fig. 1-25. The conventional unit cell of the cesium chloride structure. The large and small spheres represent two different types of atoms.

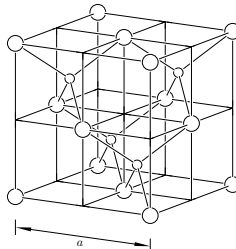


Fig. 1-26. The conventional unit cell for the zincblende structure. The large and small spheres represent two different types of atoms.

The SI units are given in parentheses. Other commonly used units are given in terms of the SI units. Symbols conform with the recommendations of the American National Standards Institute (ANSI) and the American Institute of Physics (AIP).

Commonly used multiples of SI units:

prefix	symbol	factor
tera	T	10^{12}
giga	G	10^9
mega	M	10^6
kilo	k	10^3
centi	c	10^{-2}
milli	m	10^{-3}
micro	μ	10^{-6}
nano	n	10^{-9}
pico	p	10^{-12}
femto	f	10^{-15}

length: meter (m)

angstrom	1 Å	$= 10^{-10}$ m
inch	1 in.	$= 2.54 \times 10^{-2}$ m
foot	1 ft	$= 0.3048$ m
mile	1 mi	$= 1609$ m

mass: kilogram (kg)

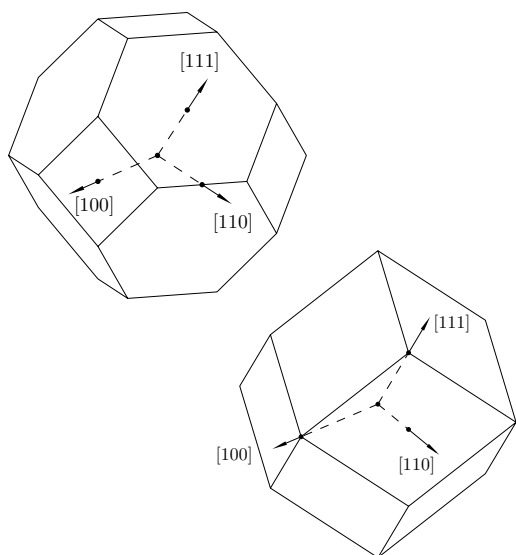
atomic mass unit	1 u	$= 1.661 \times 10^{-27}$ kg
slug	1 slug	$= 14.59$ kg

force: newton ($N = \text{kg} \cdot \text{m}/\text{s}^2$)

dyne	1 dyn	$= 10^{-5}$ N
pound	1 lb	$= 4.448$ N

pressure: pascal ($\text{Pa} = \text{kg}/\text{m} \cdot \text{s}^2$)

atmosphere	1 atm	$= 1.013 \times 10^5$ Pa
pounds/square inch	1 psi	$= 6895$ Pa
cm of mercury	1 cm Hg	$= 1333$ Pa
bar	1 bar	$= 1.000 \times 10^5$ Pa
torr	1 torr	$= 133.3$ Pa



time: second (s)

minute	1 min	$= 60$ s
hour	1 h	$= 3600$ s

frequency: hertz ($\text{Hz} = \text{s}^{-1}$)

radians/second	1 rad/s	$= 1/2\pi$ Hz
----------------	---------	---------------

energy: joule ($\text{J} = \text{kg} \cdot \text{m}^2/\text{s}^2$)

erg	1 erg	$= 10^{-7}$ J
electron volt	1 eV	$= 1.602 \times 10^{-19}$ J
calorie	1 cal	$= 4.187$ J
kilowatt-hour	1 kW·h	$= 3.6 \times 10^6$ J
British thermal unit	1 Btu	$= 1055$ J

power: watt ($\text{W} = \text{kg} \cdot \text{m}^2/\text{s}^3$)

horsepower	1 hp	$= 745.7$ W
------------	------	-------------

charge: coulomb ($\text{C} = \text{A} \cdot \text{s}$)

electric potential: volt ($\text{V} = \text{kg} \cdot \text{m}^2/\text{s}^3 \cdot \text{A}$)

current: ampere (A)

resistance: ohm ($\Omega = \text{kg} \cdot \text{m}^2/\text{s}^3 \cdot \text{A}^2$)

capacitance: farad ($\text{F} = \text{s}^4 \cdot \text{A}^2/\text{kg} \cdot \text{m}^2$)

magnetic field: tesla ($\text{T} = \text{kg}/\text{s}^2 \cdot \text{A}$)

gauss	1 G	$= 10^{-4}$ T
-------	-----	---------------

magnetic flux: weber ($\text{Wb} = \text{kg} \cdot \text{m}^2/\text{s}^2 \cdot \text{A}$)

maxwell	1 Mx	$= 10^{-8}$ Wb
---------	------	----------------

magnetic inductance: henry ($\text{H} = \text{kg} \cdot \text{m}^2/\text{s}^2 \cdot \text{A}^2$)

temperature: kelvin (K)

degrees Celsius	0°C	$= 273.15$ K
-----------------	-----	--------------

angle: radian (rad)

degree	1°	$= \pi/180$ rad
revolution	1 rev	$= 2\pi$ rad

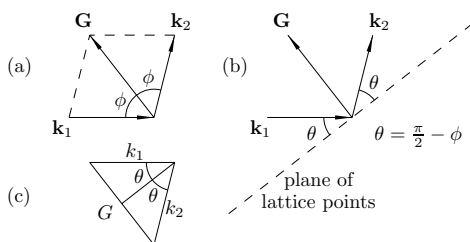


Fig. 2-14. (a) Diagram showing the relation, $\mathbf{G} = \mathbf{k}_2 - \mathbf{k}_1$. (b) \mathbf{G} is perpendicular to planes of lattice points in real space. (c) Diagram showing the relation between G , k , and θ .

SOME PHYSICAL CONSTANTS

electron charge	e	1.602×10^{-19} C
electron mass		9.11×10^{-31} kg
proton mass		1.673×10^{-27} kg
neutron mass		1.675×10^{-27} kg
Planck's constant	h	6.626×10^{-34} J·s
	\hbar	1.055×10^{-34} J·s
Boltzmann's constant	k_B	1.380×10^{-23} J/K
permittivity constant	ϵ_0	8.854×10^{-12} F/m
permeability constant	μ_0	1.257×10^{-6} H/m
speed of light	c	3.00×10^8 m/s
Avogadro's number		6.022×10^{23} /mol
Bohr magneton	μ_B	9.27×10^{-24} J/T

IMPURITY LEVELS IN SILICON AND GERMANIUM

All values are given for room temperature (300 K).

Donors	E_d in Si	E_d in Ge
P	0.044 eV	0.0120 eV
As	0.049	0.0127
Sb	0.039	0.0096
Bi	0.069	
Acceptors	E_a in Si	E_a in Ge
B	0.046 eV	0.0104 eV
Al	0.057	0.0102
Ga	0.065	0.0108
In	0.16	0.0112
Tl	0.26	0.01