Multi-Feature Super-Resolution Network for Cloth Wrinkle Synthesis Supplementary Material

The supplementary material of the paper "Multi-Feature Super-Resolution Network for Cloth Wrinkle Synthesis" consists of the following components:

- (1) This document provides the details about feature descriptors in geometry images, rigid motion transformation and the kinematics-based loss function.
- (2) The supplemental video shows a range of different examples of synthesized results, as well as comparisons with [13], including animated sequences.

1 Feature descriptors

The state of a cloth mesh \mathbf{M} , when embedded in 3D space, can be denoted as the positions of vertices $\mathbf{x} = [\mathbf{x}(q_1), \mathbf{x}(q_2), \cdots, \mathbf{x}(q_m)] \in \mathbb{R}^{3m}$. A physical simulation usually starts from a 3D space embedding \mathbf{x}_0 of the rest state mesh \mathbf{M}_0 . Then we generate a sequence of cloth meshes, denoted as $\mathbf{x}_0, \mathbf{x}_1, \cdots, \mathbf{x}_N$. We design a feature descriptor by considering the *position*, the *normal* and the *velocity* of a sampling point.

The displacement. The geometry images technique [18] converts world space coordinates into three grayscale values (as RGB values). The work of [13] followed this paradigm. However as we are only interested in the intrinsic shape of the mesh but not its spatial locations, directly encoding the absolute coordinates is not recommended. We make an adaption by encoding displacement vectors instead.

The displacement vector $\mathbf{d}_k(q_i)$ is defined, for the i-th vertex, as the difference between its position at the frame k and its starting position: $\mathbf{d}_k(q_i) = \mathbf{x}_k(q_i) - \mathbf{x}_0(q_i)$. This vector is then converted into another format such as RGB values. Displacement for any sample

point inside a triangle face is interpolated from mesh vertices.

The normal. Wrinkles are closely related to dihedral angles, which are defined as the angle between two normal vectors of adjacent faces. In this sense, normals are also very important features in describing a shape. We compute the normal for vertex q_i as area-weighted average of normals of the faces adjacent to q_i :

$$\mathbf{n}(q_i) = \frac{\sum_{T \in \mathcal{N}(q_i)} \alpha_T \mathbf{n}(T)}{\left\| \sum_{T \in \mathcal{N}(q_i)} \alpha_T \mathbf{n}(T) \right\|},$$
 (1)

where $\mathcal{N}(q_i)$ denotes the set of faces incident to vertex q_i , T is a triangle belonging to $\mathcal{N}(q_i)$, α_T is the area of triangle T and $\mathbf{n}(T) \in \mathbb{R}^3$ is the unit vector for triangle normal.

The velocity. In an animation, the wrinkling behavior exhibits smooth transition from frame to frame. Temporal coherence needs to be considered, otherwise cloth motion will show obvious jittering effects. Temporally coherent features should not vary dramatically from frame to frame, so extra constraints are needed to achieve this goal. Fortunately, for physically simulated cloth frame data, there is a natural connection between two consecutive frames: the vertex velocities. Velocities at the frame k predict the positions at the frame k+1, which are computed as:

$$\mathbf{v}_k = (\mathbf{x}_{k+1} - \mathbf{x}_k)/\Delta t. \tag{2}$$

Thus velocity is added to the feature vector. As above the velocity of arbitrary sample point is interpolated from the velocity of vertices.

2 Rigid motion invariant features

When a mesh changes its state from \mathbf{x}_0 to \mathbf{x}_k , the position change can be decomposed into a rigid motion and an intra-mesh non-rigid deformation. The rigid motion, represented by an optimal rotation \mathbf{R} and translation \mathbf{t} , has no contribution to the wrinkling behavior thus is to be culled off. The Kabsch Algorithm [47] is used to find the \mathbf{R} and \mathbf{t} which minimize the mean-square-error between two point sets at the frame k and its starting state:

$$\operatorname{argmin} \sum_{i=1}^{m} \| (\mathbf{R} \mathbf{x}_{k}(q_{i}) + \mathbf{t}) - \mathbf{x}_{0}(q_{i}) \|^{2} \text{ s.t. det } (\mathbf{R}) = 1.$$
(3)

To reduce computation cost, we only compute rigid motion of LR meshes at each frame and apply the same (\mathbf{R}, \mathbf{t}) to the corresponding HR meshes. With the computed \mathbf{R} and \mathbf{t} , the rigid motion invariant features in the paper are calculated of the form

$$\mathbf{d}' = (\mathbf{R}\mathbf{x} + \mathbf{t}) - \mathbf{x}_0, \mathbf{n}' = \mathbf{R}\mathbf{n}, \mathbf{v}' = \mathbf{R}\mathbf{v}. \tag{4}$$

This process actually aligns a newly deformed mesh state \mathbf{x} with its rest state \mathbf{x}_0 .

3 Kinematics-based loss function

We minimize a kinematics-based loss to constrain the relationship between the synthesized velocities and positions, as

$$\mathcal{L}_{kine} = \sum_{k=1}^{n} ||(\mathbf{x}_{k}^{s} - (\mathbf{x}^{s} + (\sum_{j=1}^{k} \mathbf{v}_{k-j}^{s}) * \Delta t)||^{2}, \quad (5)$$

where n is the length of frames associated to the input frame, and Δt represents the time step between consecutive frames. The \mathbf{x} in this formula can be replaced by displacement. Moreover, we add a rigid motion transformation to displacement and velocity in the equation (4). Replace the \mathbf{x} and \mathbf{v} in the formula (5) by equation (4), the kinematics-based loss can be written as

$$\mathcal{L}_{kine} = \sum_{k=1}^{n} ||\mathbf{R}_{k}^{-1} (\mathbf{d'}_{k}^{s} - (\mathbf{d'}^{s} + (\sum_{j=1}^{k} \mathbf{v'}_{k-j}^{s}) * \Delta t)||^{2}, (6)$$

Since the time step is really small and the the neighbouring n frames of meshes only have small scale deformation, we share the rotation matrix in (6) and get

$$\mathcal{L}_{kine} = \sum_{k=1}^{n} ||\mathbf{R}^{-1} (\mathbf{d'}_{k}^{s} - (\mathbf{d'}^{s} + (\sum_{j=1}^{k} \mathbf{v'}_{k-j}^{s}) * \Delta t)||^{2}.$$
 (7)

To define the notifications in an easily understood manner, we use the $(\mathbf{d}, \mathbf{n}, \mathbf{v})$ to replace the $(\mathbf{d}', \mathbf{n}', \mathbf{v}')$ in our paper.

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