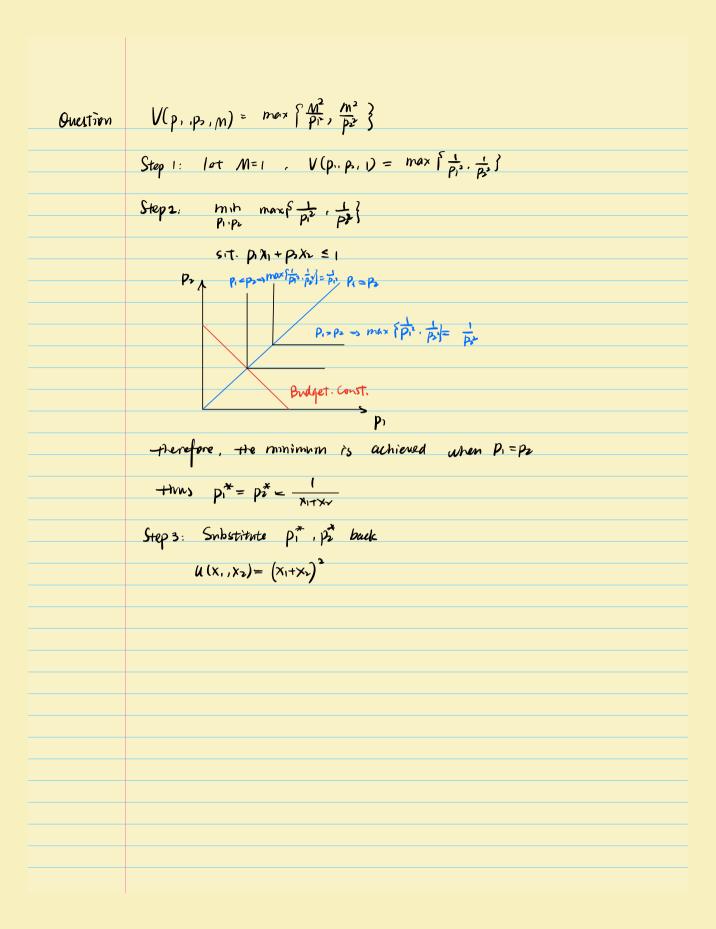
	Sep. 13.
Question	(a) man X1 x2
2003 Midtern	
	94. (~ 94. ,
	$L = x_1^{\alpha} x_2^{1-\alpha} - x(p_1 x_1 + p_2 x_2 - M)$ Here, since MU1>0. MU2>0
	Foc. Il = axi = 221-a-xp1=0 the constraint must be bindly
	Foc. de = axi x2 (-a - xp1 =0) the constraint must be binding.
	$\frac{\partial \ell}{\partial x} = (1-d) \chi_1^{\alpha} \chi_2^{-\alpha} - \lambda \rho_2 = 0$
	dx = 1 / m = 3 f / m
	>(PIXI+P2X2-M)=0. >>0. => PIXI+P=X>=M
	$\frac{\times \chi_2}{(1-\alpha)\chi_1} = \frac{p_1}{p_2} \iff \alpha p_2 \chi_2 = (1-\alpha)p_1 \chi_1$
	(1-d) X1 P2
	substitute this back to the budget constraint.
	$M = \frac{2M}{M} M = \frac{(1-d)M}{M}$
	$\chi_1^M(\rho,M) = \frac{2M}{\rho_1} \qquad \chi_2^M(\rho,M) = \frac{(1-\alpha)M}{\rho_2}$
	(b) Indirect uplitus function
	(b) Indirect utility function. $V(p_1, p_2, M) = (x_1^M)^{\alpha} (x_2^M)^{1-\alpha}$
	$= \left(\frac{\alpha N}{P_1}\right)^{\alpha} \left(\frac{(1-\alpha)N}{P_2}\right)^{\alpha}$
	$= \left(\frac{\Delta}{P_1}\right)^{\alpha} \left(\frac{1-\alpha}{P_2}\right)^{1-\alpha} M$
	(PI) (P)
	ca) Verify The Roy's identity:
	$m = \frac{4V}{C} \left(-\frac{\alpha}{C} \right)^{\alpha} \left(\frac{1-\alpha}{C} \right)^{\frac{\alpha}{2}} \left(\frac{1-\alpha}{C} \right)^{\frac{\alpha}{2}}$
	$\chi_{1}^{m} = -\frac{\frac{\partial V}{\partial p_{1}}}{\frac{\partial V}{\partial M}} = -\frac{\left(-\alpha\right)\left(\frac{\alpha}{p_{1}}\right)^{\alpha}\left(\frac{1-\alpha}{p_{2}}\right)^{\frac{\alpha}{p_{1}}}}{\left(\frac{1-\alpha}{p_{1}}\right)^{\alpha}\left(\frac{1-\alpha}{p_{2}}\right)^{\frac{\alpha}{p_{1}}}} = \frac{\alpha m}{p_{1}}$ Verified.
	on (pi) (pi)
	x could be verified in the same way.
	~,,,.

Question	V(priprim) = M(pi+pr) . Recover the corresponding almost utility
	$V(p_1, p_2, M) = M(p_1 + p_2)$. Recover the corresponding acres of thing
JR Example 2.1	Step 1: let $M=1$. $V(p_1, p_2, 1) = (p_1^r + p_2^r)^{-\frac{1}{r}}$
	Step 1: let /11=1. V(pi, ps,1) = (pi ps,1)
	Step 2: min V(pipz) sit. pix+pxx =1
	1 = - (pir+pzr) - > (pizi+pzzz-1)
	foc: [ρ,7: -(-f)(ρ,σ+ρ,σ)-1-1 ρ,σ-1 - x, x =0
	[pz]: -(-+)(pi+psr)-+-18psr-1-25x=0
	λ(p1×1+p2/5-1)=0
	$\Rightarrow (\frac{p_1}{p_2})^{r-1} = \frac{z_1}{z_{22}} \qquad \frac{p_1}{p_2} = (\frac{\chi_1}{\chi_2})^{r-1} \Rightarrow p_1 = (\frac{\chi_1}{\chi_2})^{r-1} p_2$
	Substitute into pix1+pax2=1
	$\left(\frac{\chi_1}{\chi_2}\right)^{\frac{1}{p-1}} p_2 \chi_1 + p_2 \chi_2 = 1$ Substitute into $p_1 x_1 + p_2 x_2 = 1$
	$\Rightarrow p_2\left[\left(\frac{x_1}{k_2}\right)^{\frac{1}{p-1}} \cdot x_1 + x_2\right] = 1$
	* XzH
	$\Rightarrow p^* = \frac{\chi_2 \vec{r}}{\chi_1 \vec{r}_1 + \chi_2 \vec{r}_1}$
	and $\rho_1^* = \frac{x_1 \frac{r}{r}}{x_1 \frac{r}{r} + x_2 \frac{r}{r}}$
	χ ₁ (=) + χ ₂ r-ι
	Step 3: substate pt. pt back
	$\mathcal{U}(x_1, x_2) = \mathcal{V}(p_1^{-1}, p_2^{-1}) = \left(x_1^{\frac{1}{d-1}} + x_2^{\frac{1}{1-1}}\right)^{\frac{1}{1-1}}$



Multi3Cb.
$$u(x) = (\alpha_1 \times \beta_1 + \alpha_2 \times x_3)^{\frac{1}{p}}, \text{ assume } \alpha_1 + \alpha_2 = 1$$

$$(a) \quad \rho \to 1 \quad \Rightarrow \quad u(x) = \alpha_1 \times_1 + \alpha_2 \times x_3$$

$$(b) \quad \rho \to 0.$$

$$u(x) = \exp\left(\frac{1}{p}\log(\alpha_1 x_1^p + \alpha_2 x_3^p)\right)$$

$$f(x) = f(x) + f'(x)(x - x_3)$$

$$+ \text{the Consider the first order Taylor exponsion centered at } \rho = 0$$

$$\text{for the term Possible (symfrim. with respect to } \rho.$$

$$\phi_1 x_1^1 + \alpha_2 x_2^2 = \alpha_1 x_1^2 + \alpha_3 x_2^2 + \alpha_1 p_1 f' \ln x_1 + \alpha_2 f_2 f' \ln x_2 + O(p^2)$$

$$= \alpha_1 + \alpha_2 + \beta_1 (\ln x_1 + \beta_2 x_1 \ln x_2 + o(p^2))$$

$$= \alpha_1 + \alpha_2 + \beta_1 (\ln x_1 + \beta_2 x_1 \ln x_2 + o(p^2))$$

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$$= \alpha_1 + \alpha_2 + \beta_1 (\ln x_1 + o(p^2) + o(p^2))$$

$$= \alpha_1 + \alpha_2 + \alpha_3 + o(p^2)$$

$$= \alpha_1 + \alpha_2 +$$

$$= \lim_{\rho \to -\rho^*} \chi_z \left(\alpha_1 \left(\frac{\chi_1}{\chi_2} \right)^{\rho} + \alpha_z \right)^{\frac{1}{\rho}}$$

let
$$r = \frac{x_1}{x_2}$$

1>1 => Inr >0

Let
$$r = \frac{x_1}{x_2} > 1$$

$$\lim_{\rho \to 0} x_2 \left(x_1 r^{\rho} + x_2 \right)^{\frac{1}{\rho}}$$

$$= \lim_{\rho \to \infty} e^{x} p \left[\ln(\alpha_1 r^{\rho} + \alpha_2) + \ln x_2 \right]$$

Similarly . we can prove when x1<x2.

Sometimes we let $f = \frac{\sigma}{\sigma}$ and $\sigma = \frac{1}{1-\rho}$, where σ has a meaning of the elasticity of substitution.

Hence, the CES utility function is given by

$$\mu(x) = \left(\propto_1 \chi_1 \frac{\sigma_{-1}}{\sigma} + \sim_2 \chi_2 \frac{\sigma_{-1}}{\sigma} \right)^{\frac{\sigma}{\sigma-1}}$$

when P-1, 5-10, perfect substitute

