

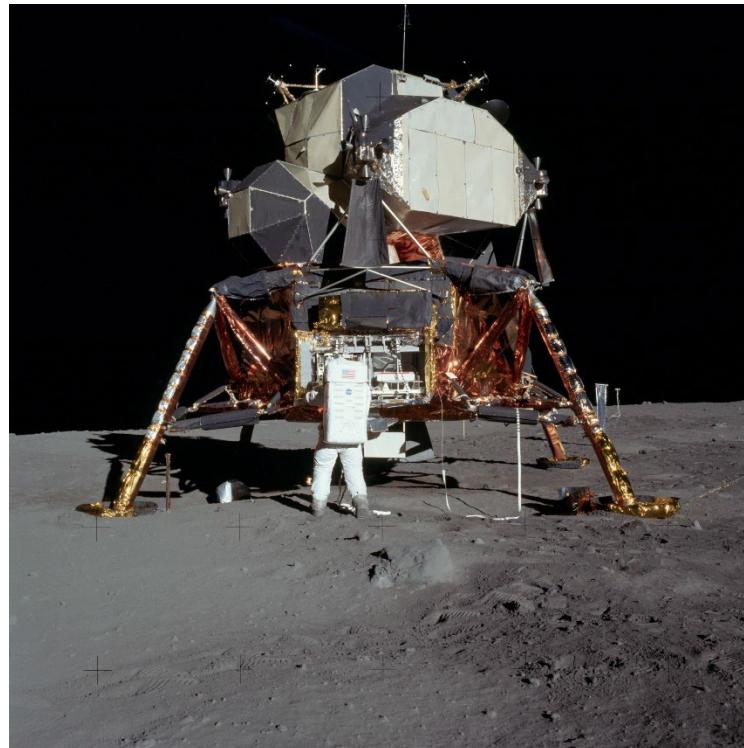
## Lunar Lander Simulation

### Background

This project simulates a greatly simplified version of the lunar lander from the Apollo 11 mission in 1969. The program should implement two modes:

1. “Game” mode, in which the user repeatedly enters a value representing the throttle on the rocket thrusters slowing the vehicle down as it descends.
2. Autopilot mode, in which a control function calculates the needed thrust automatically.

In both modes, the goal is to make a soft landing on the lunar surface before fuel runs out.



Apollo 11 lunar lander on the Moon. (Photo: NASA)

### Suggested Approach

For sake of simplicity, make the simulation run at one second intervals. Note: This is not one second of real time, but each step should represent one second of simulated time. This provides reasonable granularity without too much detail. The simulation will generally last no more than 150 steps (i.e. simulated seconds). The math required is very basic physics and is in discrete time, not continuous time.

The premise is this: The vehicle is descending straight down from given initial altitude and velocity. Negative values for velocity and acceleration indicate downward motion, while positive values indicate upward motion. The user or the control function (depending on mode: “game mode” or “autopilot”) can choose any amount of thrust, up to a maximum of 45 kN (kiloNewtons). The gravity of the moon causes

a constant acceleration of  $-1.6 \text{ m/s}^2$  on the vehicle. A soft landing is one where the velocity at touchdown is one meter per second or less.

For the game mode, it is suggested that the thrust input be in kN and the value be converted to Newtons by multiplying by 1000. You'll find that you need to run full thrust for several seconds, so entering 45 over and over is easier than entering 45000. The autopilot control function will most easily be implemented in Newtons, not kN, however.

Each kilogram of fuel produces 3000 N of force for one second, so the chosen thrust is divided by 3000 to determine how much fuel was burned in that one-second step. If the chosen thrust is greater than 3000 times the amount of fuel remaining, the thrust needs to be limited to consume only the remaining fuel and no more thrust can be produced after that.

As each simulated second passes, the current altitude, acceleration, velocity, mass, and fuel remaining need to be updated with new values reflecting the effects of the chosen thrust. These values should be printed to the screen and an output file in .csv format for later plotting. You can use the following pseudocode to update those values:

```
// Calculate acceleration
acceleration = (thrust/mass + gravity) * timeStep

// Update mass and fuel
mass -= thrust / 3000
fuel -= thrust / 3000

// Update velocity and height
velocity += acceleration * timeStep
altitude += velocity * timeStep
```

NOTE: Since `timeStep = 1` in the above pseudocode, it can be omitted entirely.

The autopilot control function should take current altitude, mass, and velocity as parameters and return a thrust value that is designed to land the vehicle safely.

## Requirements

Create a structure that represents the current state, i.e. altitude, velocity, acceleration, mass, and fuel. Use this structure throughout your code.

You should include separate functions for the following tasks:

- Checking that the desired thrust does not exceed the maximum (45 kN) and is limited by the remaining fuel. This function should return the actual thrust allowed.
- Updating all of the state values (altitude, velocity, acceleration, mass, and fuel) with each step.
- The autopilot control: Determining a thrust based on the current state (this function is not called in game mode).
- Main function: Asks the user which mode (game mode or autopilot mode), opens the file for writing, runs the simulation loop, prints the state to the screen and to the file.

## Physical Details

$H_0$  (initial altitude): 15000 m  
 $v_0$  (initial velocity): -325 m/s  
Initial fuel remaining: 1800 kg  
 $m_0$  (initial mass): 9000 kg (including fuel)  
 $g_m$  (Lunar gravity): -1.6 m/s<sup>2</sup>  
Allowable thrust: 0 - 45 kN  
Fuel consumption:  $(T / 3000 \text{ m/s}) \text{ kg/s}$   
Soft landing:  $-1 \leq v_f \leq 0 \text{ m/s}$

$H$  represents the current altitude (e.g. height),  $v$  is the current velocity, and  $T$  is the thrust.

## Suggested control formulas for autopilot

Try  $H_f = 5$  and  $v_f = -0.9$ . You are free to experiment with other values and control formulas.

For higher altitudes ( $H > H_f$ ):

$$a_d = \frac{(v^2 - v_f^2)}{2(H - H_f)}$$

$$T = m(a_d - g_m)$$

Near landing ( $H < H_f$ ):

$$T = -mg_m \left( \frac{v}{v_f} \right)$$

Note:  $a_d$  is just a temporary variable representing the “desired” acceleration. The actual acceleration is calculated from the actual thrust.

## Example Output (in autopilot mode)

```
Thrust: 25636 Altitude: 11 Velocity: -4.5 Mass: 7691.5 Fuel: 491.52
Thrust: 21496 Altitude: 8 Velocity: -2.7 Mass: 7683.0 Fuel: 482.98
Thrust: 17103 Altitude: 6 Velocity: -1.5 Mass: 7675.8 Fuel: 475.81
Thrust: 12651 Altitude: 5 Velocity: -0.9 Mass: 7670.1 Fuel: 470.11
Thrust: 11844 Altitude: 4 Velocity: -0.9 Mass: 7665.9 Fuel: 465.90
Thrust: 12586 Altitude: 4 Velocity: -0.9 Mass: 7661.9 Fuel: 461.95
Thrust: 11998 Altitude: 3 Velocity: -0.9 Mass: 7657.8 Fuel: 457.75
Thrust: 12444 Altitude: 2 Velocity: -0.9 Mass: 7653.8 Fuel: 453.75
Thrust: 12086 Altitude: 1 Velocity: -0.9 Mass: 7649.6 Fuel: 449.60
Thrust: 12086 Altitude: -0 Velocity: -0.9 Mass: 7645.6 Fuel: 445.58

Soft landing!
```