

# MATH 753.01 - Fall 2020

## Homework 01

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### Section 0.4

#### Ex 1

Identify which values of  $x$  that there is subtraction of nearly equal numbers - Find an equivalent expression.

- (a)

$$\frac{1 - \sec(x)}{\tan^2(x)} \quad (1)$$

The  $\sec(x)$  function is very near  $+1$  for values of  $x \approx 2n\pi$ , this would create subtraction of nearly equal numbers. We can use trigonometric rules:

$$\frac{1 - 1/\cos(x)}{\tan^2(x)} = \quad (2)$$

- (b)

$$\frac{1 - (1 - x)^3}{x} \quad (3)$$

For  $x \approx 0$ , the numerator evaluated roughly to  $1 - 1$ , thus we have subtraction of nearly equal numbers. Additionally, this would likely raise a *zero-division error* if  $x = 0$  exactly. We can expand the numerator, and find the algebraic equivalent:

$$\frac{1 - (-x^3 + 3x^2 - 3x + 1)}{x} = \frac{x^3 - 3x^2 + 3x}{x} = x^2 - 3x + 3 \quad (4)$$

- (c)

$$\frac{1}{1+x} - \frac{1}{1-x} \quad (5)$$

For  $x \approx 0$ , both terms will evaluate to approximately  $1/1$ . This would create subtraction of nearly equal numbers.

**Ex 2**

Find the roots of  $x^2 + 3x - 8^{-14} = 0$  with three-digit accuracy.

**Ex 4**

Evaluate  $x\sqrt{x^2 + 17} - x^2$  where  $x = 9^{10}$  to three decimals.

We multiply the function by it's conjugate:

$$x\sqrt{x^2 + 17} - x^2 = \frac{(x\sqrt{x^2 + 17} - x^2)(x\sqrt{x^2 + 17} + x^2)}{1(x\sqrt{x^2 + 17} + x^2)} = \frac{(x^2(x^2 + 17) - x^4)}{(x\sqrt{x^2 + 17} + x^2)} \quad (6)$$

**0.5****Ex 4****Ex 6****Ex 8****Ex 9****1.1****Ex 2****Ex 4**