

MATH 753.01 - Fall 2020

Homework 01

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Section 0.4

Ex 1

Identify which values of x that there is subtraction of nearly equal numbers - Find an equivalent expression.

- (a)

$$\frac{1 - \sec(x)}{\tan^2(x)} \quad (1)$$

The $\sec(x)$ function is very near $+1$ for values of $x \approx 2n\pi$, this would create subtraction of nearly equal numbers. We can use trigonometric rules:

$$\frac{1 - 1/\cos(x)}{\tan^2(x)} = \quad (2)$$

- (b)

$$\frac{1 - (1 - x)^3}{x} \quad (3)$$

For $x \approx 0$, the numerator evaluated roughly to $1 - 1$, thus we have subtraction of nearly equal numbers. Additionally, this would likely raise a *zero-division error* if $x = 0$ exactly. We can expand the numerator, and find the algebraic equivalent:

$$\frac{1 - (-x^3 + 3x^2 - 3x + 1)}{x} = \frac{x^3 - 3x^2 + 3x}{x} = x^2 - 3x + 3 \quad (4)$$

- (c)

$$\frac{1}{1+x} - \frac{1}{1-x} \quad (5)$$

For $x \approx 0$, both terms will evaluate to approximately $1/1$. This would create subtraction of nearly equal numbers.

Ex 2

Find the roots of $x^2 + 3x - 8^{-14} = 0$ with three-digit accuracy.

Ex 4

Evaluate $x\sqrt{x^2 + 17} - x^2$ where $x = 9^{10}$ to three decimals.

We multiply the function by it's conjugate:

$$x\sqrt{x^2 + 17} - x^2 = \frac{(x\sqrt{x^2 + 17} - x^2)(x\sqrt{x^2 + 17} + x^2)}{1(x\sqrt{x^2 + 17} + x^2)} = \frac{(x^2(x^2 + 17) - x^4)}{(x\sqrt{x^2 + 17} + x^2)} \quad (6)$$

0.5**Ex 4****Ex 6****Ex 8****Ex 9****1.1****Ex 2****Ex 4**