

The Importance of Cell Connectivity for Efficient and Accurate Modeling of Flow through Dipping Aquifers with MODFLOW 6

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Abstract

Groundwater flow through a dipping aquifer is often modeled using a single layer of model cells to represent the aquifer. The layer of cells is “deformed” to follow the top and bottom elevations of the aquifer. When this approach is used in MODFLOW, adjacent cells within the model layer are vertically offset from one another, and the standard conductance-based (two-point) formulation for flow between cells does not rigorously account for these offsets. The XT3D multi-point flow formulation introduced in

MODFLOW 6 is designed to account for geometric irregularities in the grid, including vertical offsets, and to provide accurate results for both isotropic and anisotropic groundwater flow. A recent study evaluated the performance of the standard formulation and XT3D using a simple, synthetic benchmark model of a steeply dipping aquifer. Although XT3D generally improved the accuracy of flow simulations relative to the standard formulation as expected, neither formulation produced accurate flows in cases that involved large vertical offsets. In this paper, we explain that the inability of XT3D to produce accurate flows in the steeply dipping aquifer benchmark was not due to an inherent limitation of the flow formulation, but to the limited cell connectivity inherent in the most commonly used discretization packages in MODFLOW 6. Furthermore, we demonstrate that XT3D is able to produce the expected accuracy when adequate cell connectivity is introduced using MODFLOW’s unstructured grid type and the aquifer is discretized vertically using at least two model layers.

1 Introduction

Numerical simulation of layered aquifer systems can involve a tradeoff between efficiency and accuracy. A traditional approach to discretizing layered aquifer systems, called the “grid overlay” method by Hoaglund and Pollard (2003), maps the heterogeneous hydrologic properties onto a rectilinear grid (McDonald and Harbaugh, 1984). While this method preserves the benefits of the rectilinear grid structure, it can require a large number of model grid layers to adequately discretize hydrogeologic layers of variable dip and thickness (Zyvoloski and Vesselinov, 2006).

An alternative approach, called the “boundary-matching” method by Hoaglund and Pollard (2003), allows model grid layers to “deform” vertically to follow the undulations of hydrogeologic layers. This method “minimize[s] the number of model [grid] layers required to simulate an aquifer system” (McDonald and Harbaugh, 1984). In fact, it is common practice to represent each hydrogeologic layer using a single, boundary-matching model grid layer. However, the non-orthogonality of the resulting grid can be a source of significant model error (Hoaglund and Pollard, 2003).

In models based on the Control Volume Finite Difference method, which is the method used in the MODFLOW family of hydrologic simulation codes (Langevin et al., 2017, 2024), the loss of accuracy associated with the boundary-matching approach results from the use of a “two-point” formulation to calculate flows between adjacent grid cells. In the two-point formulation, the flow between two cells is proportional to the difference between the heads calculated in those two cells. For simulations of flow through isotropic porous media, the two-point flow formulation is most accurate when the grid satisfies the so-called “CVFD requirement” (Langevin et al., 2017) that the straight-line connection between two cell centers must intersect the midpoint of the cell interface at a right angle (Narasimhan and Witherspoon, 1976). However, boundary-

matching grids violate the CVFD requirement at vertical interfaces between cells in the same model layer because the corresponding cell connections are not strictly horizontal.

In MODFLOW, the top and bottom surfaces of model cells are horizontal (Langevin et al., 2017). Thus, when boundary matching is implemented in a two-dimensional (2D) cross-sectional or three-dimensional (3D) MODFLOW model, the tops of laterally adjacent cells are vertically offset from each other (as are the cell bottoms) and can follow the undulations of the aquifer boundaries only on average. Following Bardot et al. (2022), we call this type of grid “vertically offset.” In a vertically offset grid, subhorizontal cell connections across vertical cell interfaces violate the CVFD requirement, which reduces the accuracy of two-point flow formulation. For an isotropic aquifer, Hoaglund and Pollard (2003) note that “the error range is smaller for smaller dips, generally $< 20\%$ within 10° of dip.”

The introduction of unstructured grids into MODFLOW (Panday et al., 2013; Langevin et al., 2017) presented new ways for a grid to violate the CVFD requirements. To help overcome the limitations of the two-point flow formulation on geometrically irregular grids, MODFLOW-USG and MODFLOW 6 offer a Ghost-Node Correction (GNC) Package (Panday et al., 2013; Langevin et al., 2017). However, configuration of optimal ghost node locations and interpolation weights is highly problem-dependent, and we are not aware of guidelines for handling general unstructured grids or arbitrarily oriented 3D anisotropy.

The optional XT3D flow formulation (Provost et al., 2017) introduced in MODFLOW 6 offers a more “automatic” alternative to ghost nodes. XT3D is a multi-point flow formulation (Edwards and Rogers, 1998; Aavatsmark, 2002) based on gradient reconstruction (Mavriplis, 2003; Diskin and Thomas, 2008). By performing flow calculations using Darcy’s Law in its tensorial form using a multi-point approximation of the head gradient vector, XT3D accounts for both arbitrarily oriented anisotropy and geometric irregularity of the grid. In theory, XT3D should be able to compensate for the geometric irregularity introduced by vertical offsets between adjacent cells in the same grid layer.

Bardot et al. (2022) tested the ability of MODFLOW 6 to accurately simulate flow through sedimentary structures, both with and without XT3D. The simplest 2D cross-sectional (“transect”) version of their benchmark model simulated flow through a steeply dipping, homogeneous, isotropic aquifer of uniform thickness embedded between two confining units. In test runs that used the boundary-matching method on a vertically offset grid, both the two-point flow formulation and XT3D produced flows that differed markedly from the expected magnitude and direction throughout the aquifer, regardless of how finely the aquifer was discretized. They noted, however, that a preliminary analysis by two authors of the present work (Provost and Langevin) suggested that the limited cell connectivity offered by the layered, vertically offset grids was inadequate to allow an accurate flow solution.

To our knowledge, the implications of limited cell connectivity in layered, vertically offset grids for the

accuracy of simulated flows, and the potential to improve accuracy using enhanced connectivity between model layers, have not been previously recognized or investigated. In this paper, we present theoretical explanations for why “layered” connectivity in a vertically offset grid is inadequate for accurate simulation of flows in steeply dipping hydrogeologic layers, and why using what we call “full” cell connectivity together with XT3D should improve accuracy. Then, in a set of test problems similar to those of Bardot et al. (2022), we demonstrate the effectiveness of using full connectivity with XT3D. Finally, we discuss the implications of our findings for practical groundwater problems involving steeply dipping hydrogeologic layers.

2 Theory

Versions of MODFLOW prior to MODFLOW-USG (Panday et al., 2013) supported only structured grids composed of rows, columns, and layers of cells, which could be vertically offset. This grid type, called “DIS,” continues to be supported in MODFLOW-USG and MODFLOW 6, which also offer an unstructured grid type called “DISU” (Panday et al., 2013; Langevin et al., 2017). In addition, MODFLOW 6 offers an unstructured grid type called “DISV,” which is based on specification of cell vertices (Langevin et al., 2017). The DIS and DISV grid types are based on model layers, with the same horizontal grid structure within each layer. The DISU grid type is more flexible and does not depend on the concept of model layers.

Figure 1a illustrates what we refer to as “layered” and “full” cell connectivity. The focus is on a group of four cells in a two-grid-layer, vertically offset MODFLOW 6 model of fully saturated flow through a permeable hydrogeologic layer (aquifer) with impermeable top and bottom boundaries. If the grid is represented using a layered grid type (DIS or DISV), the grid has what we call “layered connectivity”: a cell is hydraulically connected to each laterally adjacent cell in the same grid layer (regardless of whether or not the cell faces actually overlap), and with each overlying and underlying cell, as indicated by the blue lines that connect cell centers in Figure 1a. In layered connectivity, two cells that have overlapping vertical faces but are in different grid layers (e.g., cells 1A and 2B) notably do not have a direct hydraulic connection. The addition of such connections between cells in different grid layers, as indicated by the red lines that connect cell centers in Figure 1a, results in a grid with what we call “full connectivity.” Implementation of full connectivity in MODFLOW 6 requires that the vertically offset grid be represented using the fully unstructured (DISU) grid type.

The role of full cell connectivity in enabling accurate simulation of flow along a dipping hydrogeologic layer can be understood by considering Figure 1b. Components of the groundwater flux (specific discharge) vector are displayed on each cell-cell interface and are representative of steady, uniform flow along the hydrogeologic layer. Gray vectors represent the uniform flux oriented along the hydrogeologic layer, which

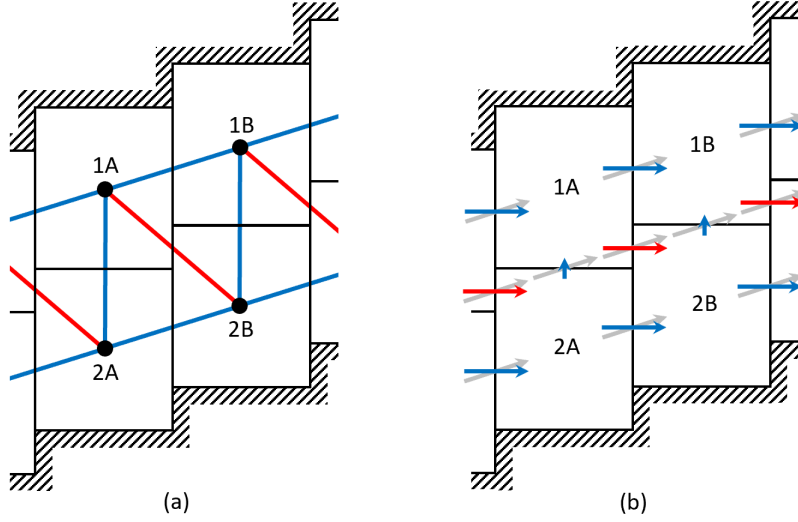


Figure 1: Schematics showing (a) cell connectivity and (b) cell-cell interface fluxes in a two-grid-layer model of a dipping hydrogeologic layer. Hatching denotes impermeable boundaries along the top and bottom of the hydrogeologic layer. In (a), black circles represent cell centers. Blue lines represent hydraulic connections between cells in a layered-connectivity grid. Red lines represent additional connections that must be made to achieve full connectivity. In (b), gray arrows represent the uniform groundwater flux the model is attempting to simulate. Blue arrows represent components of the uniform groundwater flux normal to the horizontal and vertical cell-cell interfaces in the layered-connectivity grid. Red arrows represent components of the uniform groundwater flux normal to the additional vertical cell-cell interfaces introduced to represent the full connectivity.

the model is attempting to simulate. Blue vectors represent the flux components normal to cell-cell interfaces that correspond to blue connections in Figure 1a, which are common to both the layered-connectivity and full-connectivity grids. Red vectors represent the flux components normal to cell-cell interfaces that correspond to red connections in Figure 1a, which are lacking in the layered-connectivity grid.

The blue vectors in Figure 1b show that to simulate steady, uniform flow along the dipping hydrogeologic layer, cells must exchange water not only “horizontally” with neighboring cells in the same grid layer, but also vertically with cells in the adjacent grid layer. Specifically, there must be flow from cells in the bottom grid layer to cells in the top grid layer, which corresponds to the vertical component of the groundwater flux. Note, however, that the blue vectors alone are incompatible with steady, uniform flow along the hydrogeologic layer because the exchange of water between the two grid layers is in one direction only: upward. Such a steady-state flow configuration would imply continuous depletion of flow within the bottom grid layer and accumulation of flow within the top grid layer as one moves along the hydrogeologic layer in the direction of flow. Thus, steady, uniform flow along the hydrogeologic layer cannot be simulated accurately without some mechanism for returning flow from the top grid layer to the bottom grid layer. The full-connectivity grid provides such a mechanism by offering additional connections between cells in adjacent grid layers. Vertical flows from the bottom grid layer to the top grid layer, represented by vertical blue vectors in Figure 1b, can be returned to the bottom grid layer by nominally “horizontal” flows, represented by red vectors in Figure 1b. Although this concept has been illustrated using a two-grid-layer model for simplicity, the same reasoning applies given any number of grid layers.

Note how the vertically offset grid violates the CFVD requirement because nominally “horizontal” connections between cell centers in the same grid layer are not strictly horizontal and therefore not perpendicular to the vertical cell-cell interfaces they intersect. For example, in Figure 1a, the connection between cells 1A and 1B is not perpendicular to the cell-cell interface, which reduces the accuracy of the conductance-based formulation.

Once the full connectivity is established, it is the role of the flow formulation to account properly for the geometry of the grid, a task for which XT3D was specifically designed. However, XT3D alone cannot compensate for cell connectivity that does not provide adequate pathways for flow. This explains why using XT3D did not improve the simulation results substantially on the layered-connectivity grid in the benchmark tests of Bardot et al. (2022). In the middle section of the hydrogeologic layer, away from the end boundary conditions, the flow solution approached steady, uniform flow the only way that it could given the limited connectivity: by suppressing vertical flows between grid layers, thereby rendering the overall flow approximately horizontal.

The arguments presented in this section suggest that, in addition to the use of XT3D, full connectivity

can be important for obtaining an accurate flow solution in MODFLOW 6 simulations that involve steeply dipping hydrogeologic layers. The next section presents results of simulations designed to test this hypothesis.

3 Description of Test Problem

The test problem is patterned after the cross-sectional (transect) benchmark of Bardot et al. (2022). It attempts to simulate uniform flow in an inclined permeable hydrogeologic layer (“aquifer”) embedded in less permeable material (the “domain”).

To simulate flow along an aquifer of uniform thickness inclined at angle θ relative to the horizontal (30° for the base case), heads are specified at the centers of cells along the perimeter of the model using a formula that corresponds to a uniform, unit head gradient:

$$h = -x \cos \theta - z \sin \theta, \quad (1)$$

where h is head in meters and x and z are the horizontal and vertical model coordinates, respectively, in meters. The hydraulic conductivity of the aquifer is set to 1 m/d (meter per day) so that the analytical flow solution is a groundwater flux of 1 m/d along the aquifer. In the base case, the conductivity of the domain surrounding the aquifer is set to 10^{-6} m/d to effectively isolate the aquifer hydraulically.

The test simulations use grids of MODFLOW 6 DISU (unstructured) type, which offers the flexibility to implement either layered or full connectivity. In all cases, a grid of MODFLOW 6 DIS (structured) type is first created and then converted a DISU grid. In simulations that use layered connectivity, the DISU grid is formulated to have the same cell geometry and connectivity as the original DIS grid. In simulations that use full connectivity, additional connections between adjacent layers are added during the conversion process. The base case uses grids consisting of 11 columns and 9 layers of cells, with 3 layers within the aquifer, 3 layers in the domain above the aquifer, and 3 layers in the domain below the aquifer. The model is 11 m wide, and each column is 1 m wide. Cells within the aquifer are square (1 m x 1 m). Corner cells in the lower left and upper right corner were also set to be the same dimension as the aquifer cells. The resulting base model vertical height is 14.77 m.

The above description represents the base-case test problem. However, the results also include simulations designed to investigate the effects of varying the gridding resolution, the dip angle of the aquifer, the conductivity contrast between the aquifer and the domain, and the anisotropy of the conductivity tensor.

Jupyter notebooks created for the test problem are available in the Supporting Information that accompanies this paper (best place???). The notebooks leverage the capabilities of FloPy (Bakker et al.,

2016; Hughes et al., 2023) to assist in setting up input for and processing results from the MODFLOW 6 simulations. A Python script for converting structured, DIS grids to unstructured, DISU grids with full connectivity is included.

4 Results and Discussion

To demonstrate the effect of cell connectivity on the accuracy of simulated flow through a steeply dipping aquifer, results for the base case described in the previous section are compared for simulations that use either layered or full connectivity, and either the two-point flow formulation (also known as the "standard conductance-based formulation" in MODFLOW 6) or the XT3D flow formulation. The base case is then modified to further investigate the effects of grid resolution, aquifer dip angle, conductivity contrast between the aquifer and the surrounding domain, and anisotropic hydraulic conductivity.

Plots of specific discharge (groundwater flux) at cell centers and flows across cell-cell interfaces (face flows) calculated by MODFLOW 6 are used to illustrate the accuracy of the simulated flows. The magnitude and direction of specific discharge at the cell in the center of the aquifer, at which boundary effects are presumably minimized, and the total volumetric flow rate entering the aquifer through the left-hand boundary, which consists of constant-head (CHD) cells, are also reported as representative values of flow. Maximum head errors are also reported for the base case.

Specific discharge at cell centers is calculated in a postprocessing step using distance-weighted interpolation of face flows calculated by MODFLOW 6 and reported in the binary budget output file. For the purpose of illustrating and evaluating the results of this idealized benchmark, specific discharge in cells within the aquifer is calculated using only face flows between cells within the aquifer. Likewise, specific discharge in cells within the surrounding domain is calculated using only face flows between cells within the domain. Specific discharge values reported in the binary budget output file by MODFLOW 6 are different than the values reported here for cells that are adjacent to the boundary between the aquifer and the domain. This is because MODFLOW interpolates specific discharge in a cell using all of the face flows for that cell, including flows across cell faces on the aquifer-domain boundary. Those flows represent an "average" of the different flows on either side of the aquifer-domain boundary. Therefore, specific discharge calculated in a cell adjacent to the aquifer-domain boundary is affected by the different flow rate on the other side of the boundary. While this is an unavoidable consequence of vertically offset discretization in practical applications, and not necessarily a problem, users should be aware of these effects when interpreting the results of MODFLOW 6 dispersive-transport and MODPATH particle-tracking simulations.

4.1 Effects of Cell Connectivity and Flow Formulation

The numerical solution for the layered-connectivity grid confirms the findings of Bardot et al. (2022) in that fluxes are predominantly horizontal (Figure 2a). We see that despite an enforced hydraulic gradient of 30° , the vertical component of the flux cannot propagate through the aquifer given that cells along the aquifer top are hydraulically disconnected from the low permeability domain, hence forcing flow horizontally (red arrows on right panel). The numerical solution for this grid type is a problem of cell connectivity, and thus the XT3D formulation does not resolve this issue (Figure 2b). Results for the full-connectivity grid with the standard conductance-based formulation shows an improvement in the flow solution (Figure 2c), with the XT3D formulation successfully reproducing the analytical solution (Figure 2d). We see that the grid with full connectivity allows incorporation of the vertical flow component, thus permitting cross-connection between grid layers.

The results shown in Figures 2a and b, which are based on a vertically offset grid with layered connectivity, are consistent with the findings of Bardot et al. (2022). Despite boundary heads designed to induce specific discharge of 1 m/d along the 30° incline of the aquifer, the simulated flow within the aquifer is predominantly horizontal, and the magnitude of the specific discharge at the center of the aquifer and the total flow entering the aquifer are both overestimated. The XT3D flow formulation is unable to compensate for the inadequate cell connectivity (Figure 2b), which does not allow flow between laterally adjacent cells in different grid layers.

The vertically offset grid with full connectivity (Figures 2c and d) shows significantly improved results, even for the standard flow formulation (Figure 2c). Using the XT3D flow formulation provides the most accurate results, as expected (Figure 2d).

4.2 Effects of Grid Resolution

Layered-connectivity grids, which are commonly used in groundwater models (Reilly and Harbaugh, 2004), are often configured using one model grid layer per hydrogeologic unit when simulating groundwater flow. The simulations in this subsection investigate the effect of vertically discretizing the aquifer using multiple grid layers (Figure 3). The base case uses three grid layers to represent the aquifer. When the number of grid layers is altered, the horizontal discretization is also adjusted to maintain square cells inside the aquifer, thus, maintaining a constant cell aspect ratio. We compare modeled flux magnitude and direction in cell at the center of the aquifer, as well as volumetric flow through the aquifer, against the analytical solution.

Like the results in Figure 2, the results in Figure 3 show that the use of full connectivity and the XT3D flow formulation reduces the errors in calculated flows, provided at least two grid layers are used

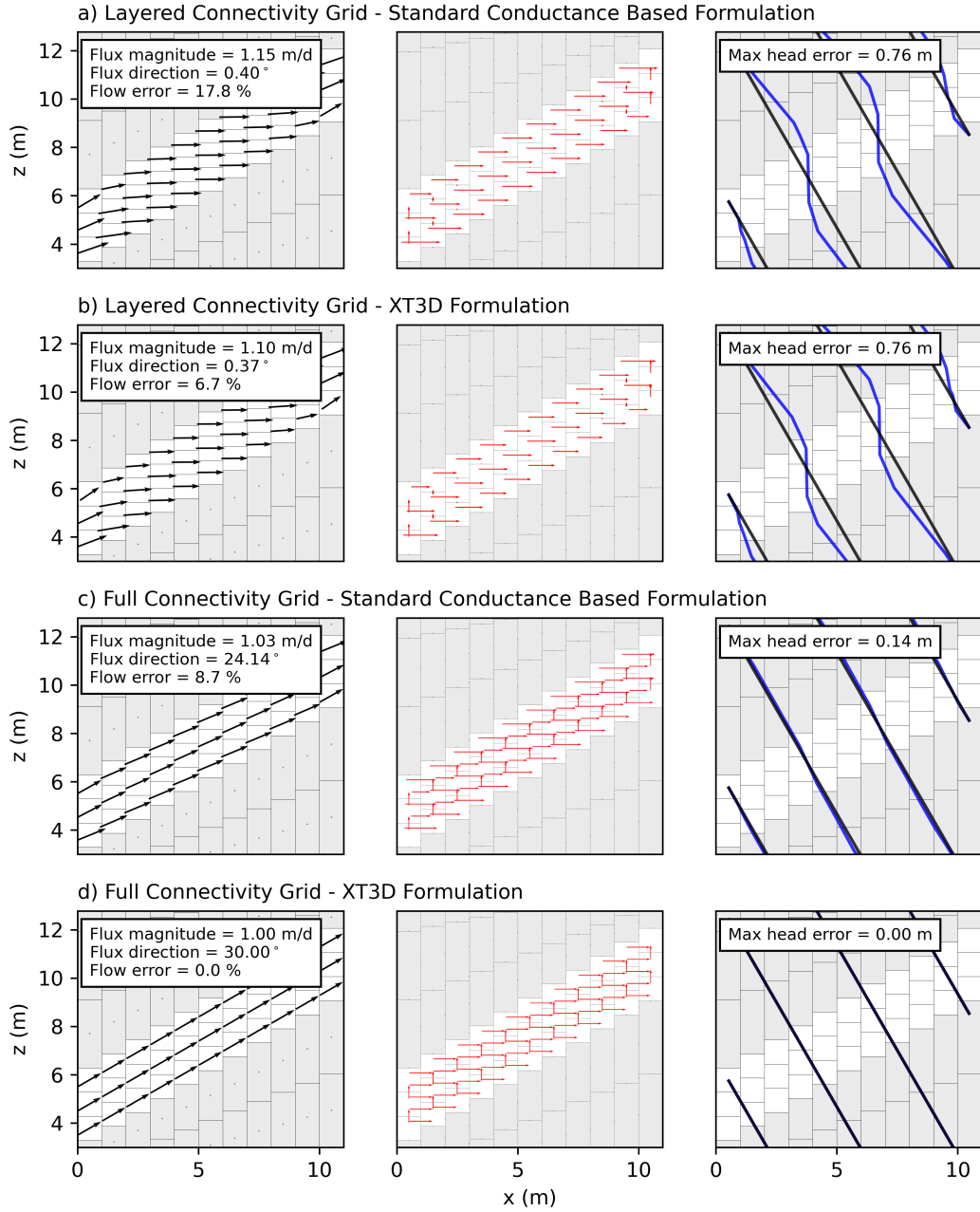


Figure 2: Numerical results for the test problem using base-case settings for layered-connectivity and full-connectivity grids, with the standard conductance-based formulation as well as the XT3D formulation. The left panel of each scenario shows the calculated specific discharge at each cell center (arrows). The middle panel shows the face flows (arrows). The right panel shows head contours for the analytical solution (black) as well as the numerical solution (blue).

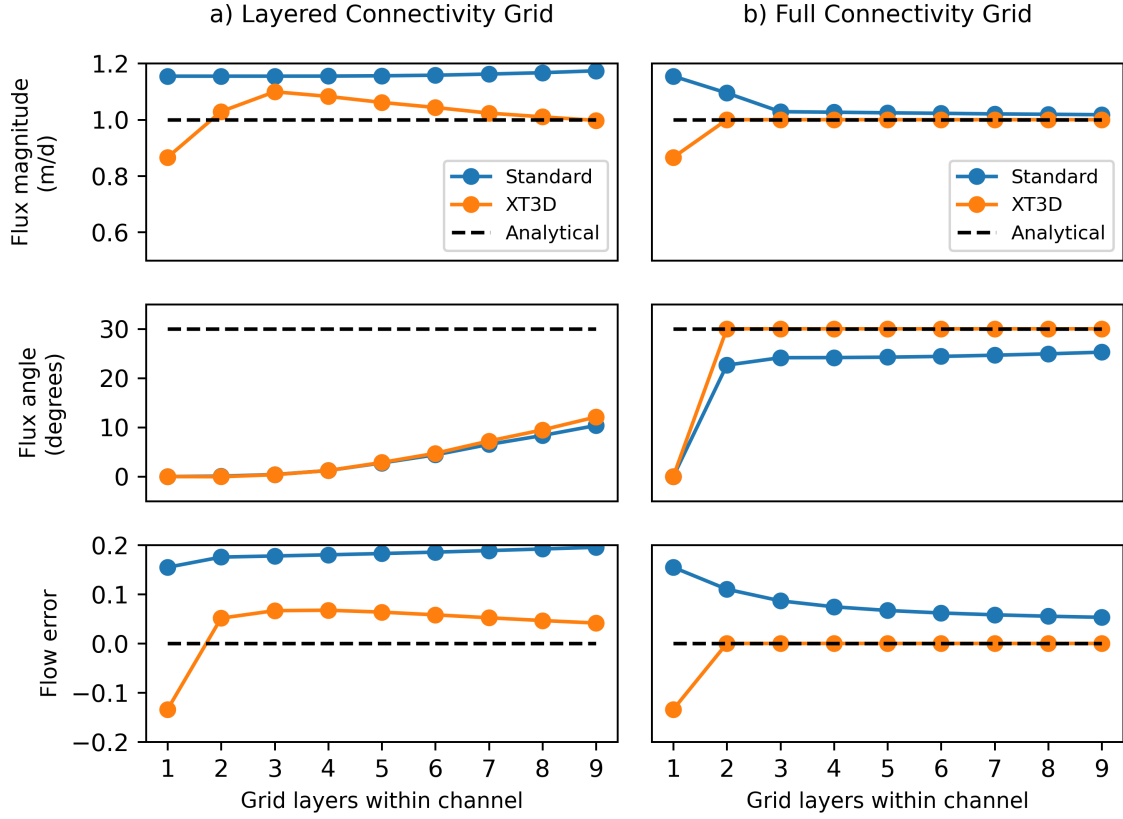


Figure 3: Graphs indicating how the number of grid layers within the aquifer affects the flux magnitude in the center cell (top), the flux direction in center cell (middle) and the volumetric flow through the aquifer (bottom). Errors are minimized by using full connectivity (right column), the XT3D flow formulation (orange lines) and at least two grids layers in the aquifer.

to vertically discretize the aquifer. When a single grid layer is used to represent the aquifer, the enhanced connectivity needed to achieve an accurate solution is not possible, and the XT3D flow formulation is unable to compensate for the inadequate connectivity.

4.3 Effects of Dip Angle and Conductivity Contrast

The base case uses an aquifer dip angle of 30° and a conductivity contrast between domain and aquifer of $10^{-6}:1$. In this subsection, we investigate the behavior of the flow solution for aquifer dip angles ranging from 0 to 80° . We also examine the behavior for a range of conductivity contrasts by setting the domain conductivity to $1/2$, $1/5$, $1/10$ and $1/100$ that of the aquifer. Simulated flux magnitude and direction at the center cell for all combinations are plotted against the analytical solution in Figure 4.

With layered connectivity and the standard conductance-based flow formulation (Figure 4a), the magnitude of the error in the flux magnitude (left panel) is similar for all of the conductivity ratios simulated and increases with increasing aquifer dip angle. The magnitude of the error in the flux direction (right panel) increases with decreasing conductivity ratio. As the surrounding domain becomes much less conductive than the aquifer, the flow direction tends toward horizontal.

With layered connectivity and the XT3D flow formulation (Figure 4b), the magnitude of the error in the flux magnitude (left panel) increases with decreasing conductivity ratio and increasing aquifer dip angle. The magnitude of the error in the flux direction (right panel) increases with decreasing conductivity ratio. As the surrounding domain becomes much less conductive than the aquifer, the flow direction tends toward horizontal, as with the standard flow formulation.

With full connectivity and the standard conductance-based flow formulation (Figure 4c), the magnitude of the error in the flux magnitude is less than 17% of the analytical solution of 1 m/d, and the magnitude of the error in the flux direction is less than 10° , at dip angles less than 40° for all of the conductivity ratios simulated. Given that the cells within the aquifer are square, cells that are nominally in the same grid layer within the aquifer no longer share any interfacial area, i.e., they become hydraulically disconnected, at a dip angle of 45° . A second transition in connectivity occurs at a dip angle of approximately 63° , and at a dip angle of approximately 72° the vertical columns of cells within the aquifer are completely disconnected from their neighbors to either side. When the discretization used to represent the aquifer becomes substantially disconnected, it cannot be expected to support accurate results. Note that for coarser horizontal discretization, transitions in connectivity within the aquifer would occur at smaller dip angles.

With full connectivity and the XT3D flow formulation (Figure 4d), the magnitude of the error in the flux magnitude is less than 3% of the analytical solution of 1 m/d, and the magnitude of the error in the flux

direction is less than 1° , at dip angles less than 40° for all of the conductivity ratios simulated. The effects of hydraulic disconnection of cells within the aquifer are evident at approximately 63° for the magnitude of the error in flow magnitude and at 45° for the magnitude of the error in flow direction. Overall, use of full connectivity with the XT3D flow formulation substantially reduces the error in calculated flows.

4.4 Effect of Anisotropy

The base case and variations up to this point have used isotropic hydraulic conductivity. However, sedimentary layers often exhibit anisotropic conductivity. Therefore, we examine the effect of anisotropic and dipping conductivity tensors within the aquifer, with conductivity perpendicular to the aquifer reduced by factors of 10, 100, 1000 and 10,000. We also include the isotropic scenario (anisotropy ratio of 1). Results are presented in Figure 5. Layered-connectivity grids produce results that deviate significantly from the analytical solution both with and without the XT3D formulation (Figure 5a), while full-connectivity grids with XT3D reproduce the analytical solution (Figure 5b, orange lines).

5 Conclusions

Bardot et al. (2022) revisited the capability of MODFLOW 6 to accurately simulate groundwater flow through sedimentary structures. They observed that calculated flows involved significant error in a benchmark problem that simulated flow through a steeply dipping hydrogeologic layer using vertically offset grids, whether or not the XT3D multi-point flow formulation was used. They hypothesized that inadequate lateral connectivity between model cells was responsible for the inability to obtain accurate flow results in their benchmark problem.

In this paper, we have confirmed that the layered lateral connectivity offered by DIS and DISV model grids can be inadequate for simulating groundwater flow through steeply dipping sedimentary structures, even when the XT3D multi-point flow formulation is used. However, when connections between laterally adjacent cells in different grid layers are added to comprise a grid with full connectivity, there can be a substantial increase in the accuracy of simulated flows. The additional connectivity is implemented using the fully unstructured (DISU) grid type in MODFLOW 6. This accuracy improvement requires that at least two grid layers be used to represent the dipping aquifers, with additional grid layers required for very steep dips.

Our benchmark results suggest that, given appropriate discretization and cell connectivity, the XT3D multi-point flow formulation implemented in MODFLOW 6 can be combined with vertically offset grids to efficiently and accurately model flows through steeply dipping sedimentary structures. Future work may

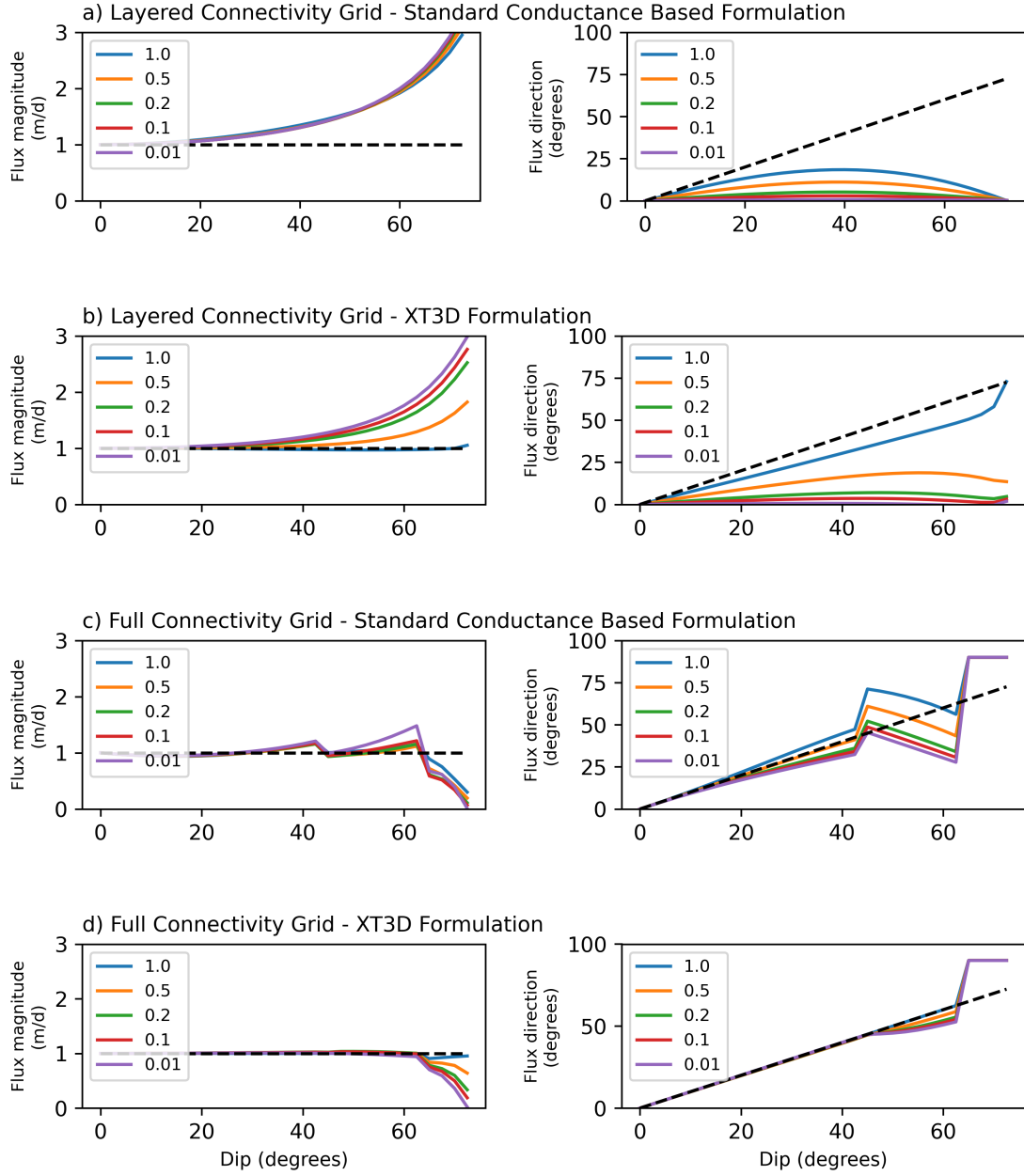


Figure 4: Flux magnitude and direction at the cell in the center of the aquifer as a function of aquifer dip angle for various ratios of domain to aquifer conductivity (blue, orange, green, red lines). The analytical solution is shown as a black dashed line.

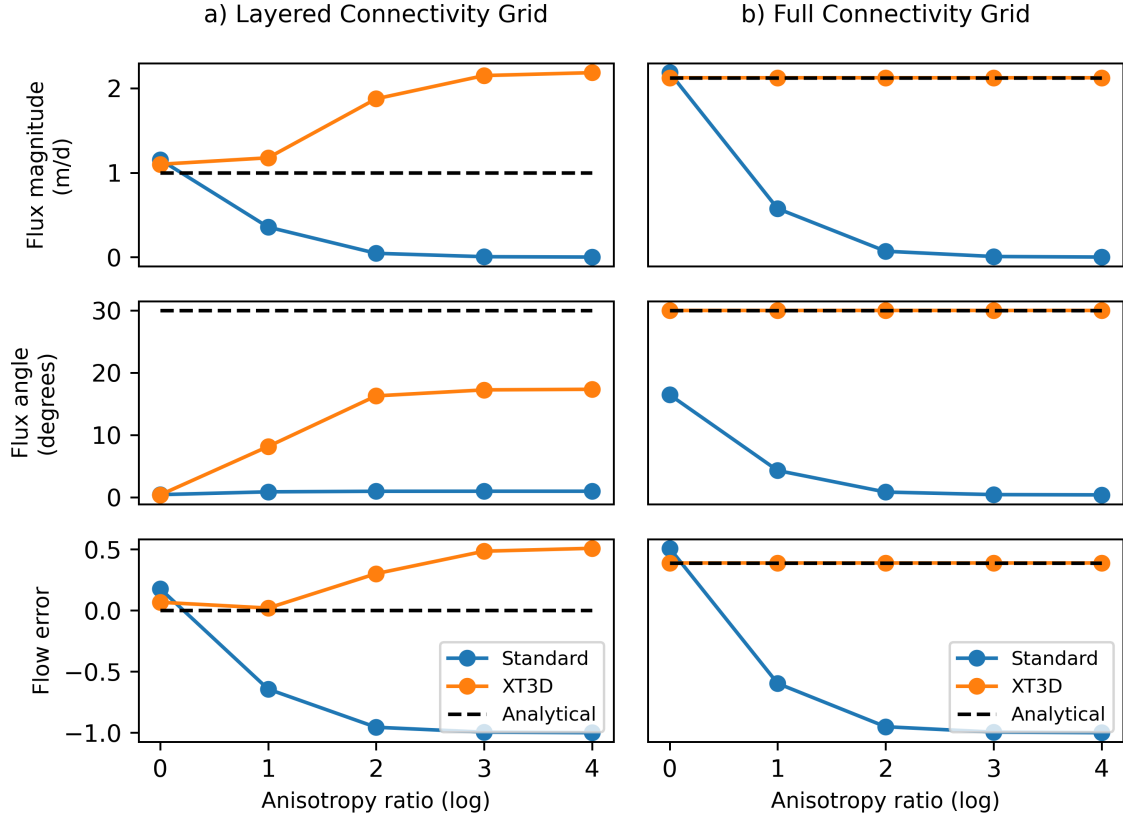


Figure 5: Graphs indicating how the anisotropy ratio within the aquifer affects the flux magnitude in the center cell (top), the flux direction in center cell (middle) and the volumetric flow through the aquifer (bottom). Errors are minimized by using full connectivity (right column) and the XT3D flow formulation (orange lines).

investigate the accuracy of calculated flows under different hydraulic gradients, as well as the implications of grid connectivity for more complex and realistic flow systems.

The importance of adequate grid connectivity has been explained and evaluated in this work specifically in terms of hydrogeologic layers that correspond to sedimentary structures. However, the impact of cell connectivity on the accuracy of simulated flows could be important in any MODFLOW application that models flow through a heterogeneous hydraulic conductivity field using a grid with large vertical offsets between laterally adjacent cells, whether or not the grid has an explicitly layered structure.

6 Acknowledgments

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7 Supporting Information

(To be determined)

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