

### EX.1.1.7, Langou

Let  $(f : \mathbb{R} \rightarrow \mathbb{R})$  be continuous. Let  $a$  and  $b$ , and **tol**. Let  $k$  be the smallest number of iterations of the Bisection Method that guarantees a forward error bound on the approximate solution within **tol**. Let **numevals** be the smallest number of iterations of the Bisection Method that guarantees a forward error bound on the approximate solution within **tol**.

- a. Derive a formula that relates  $a$ ,  $b$ ,  $k$  and **tol**.
- b. Solve for  $k$  as a function of  $a$ ,  $b$ , and **tol**.
- c. Derive a formula that relates  $k$  and **numevals**.

Let  $a$ ,  $b$ , and **tol** as given below. How many function evaluations of the Bisection Method are required to guarantee a forward error bound on the approximate solution within **tol**? Answer with an integer.

- d.  $a = -11$ ,  $b = 28$ , **tol**  $= 10^{-9}$
- e.  $a = 0.5$ ,  $b = 0.7$ , **tol**  $= 10^{-14}$