

EX.0.1.2, Sauer

Rewrite the following polynomials in nested form and evaluate at $x = -1/2$.

a. $p(x) = 6x^3 - 2x^2 - 3x + 7$

b. $p(x) = 8x^5 - x^4 - 3x^3 + x^2 - 3x + 1$

c. $p(x) = 4x^6 - 2x^4 - 2x + 4$

$$\begin{aligned} \text{a. } p(x) &= 6x^3 - 2x^2 - 3x + 7 \\ &= (6x^2 - 2x - 3)x + 7 \\ &= ((6x - 2)x - 3)x + 7 \quad \text{nested form} \end{aligned}$$

$$p(-\frac{1}{2}) = 7.25 \quad \text{with both formula}$$

$$\begin{aligned} \text{b. } p(x) &= 8x^5 - x^4 - 3x^3 + x^2 - 3x + 1 \\ &= (8x^4 - x^3 - 3x^2 + x - 3)x + 1 \\ &= ((8x^3 - x^2 - 3x + 1)x - 3)x + 1 \\ &= (((8x^2 - x - 3)x + 1)x - 3)x + 1 \\ &= (((((8x - 1)x - 3)x + 1)x - 3)x + 1) \quad \text{nested form} \end{aligned}$$

$$p(-\frac{1}{2}) = 2.8125 \quad \text{with both formula}$$

$$\begin{aligned} \text{c. } p(x) &= 4x^6 - 2x^4 - 2x + 4 \\ &= (4x^5 - 2x^3 - 2)x + 4 \\ &= ((4x^4 - 2x^2)x - 2)x + 4 \\ &= (((4x^3 - 2x)x)x - 2)x + 4 \\ &= (((((4x^2 - 2)x)x)x - 2)x + 4) \quad \text{nested form} \end{aligned}$$

$$p(-\frac{1}{2}) = 4.9375 \quad \text{with both formula}$$