

Summer 2024

MATH 4650-E01

CSCI 4650-E01

MATH 5660-E01 (additional exercises will be assigned by email for 5660 students)

Homework 4

Due on Monday July 1st 2024

Exercises:

1. EX.3.1.1.b2c [handwritten](#)
2. EX.3.1.2.b2c [handwritten](#)
3. EX.3.1.4 [handwritten](#)
4. EX.3.1.6 [handwritten](#)
5. EX.3.1.8 [handwritten](#)
6. EX.3.1.10 [handwritten](#)
7. EX.3.1.18 [colab](#)
8. CP.3.1.4 [colab](#)
9. EX.3.2.2 [handwritten](#)

**EX.3.1.1.b2c, Sauer3**

Use Lagrange interpolation to find a polynomial that passes through the points

- b.  $(-1, 0), (2, 1), (3, 1), (5, 2)$ .
- c.  $(0, -2), (2, 1), (4, 4)$ .

**EX.3.1.2.b2c, Sauer3**

Use Newton's divided differences to find the interpolating polynomials of the points in EX.3.1.1.b2c, and verify agreement with the Lagrange interpolating polynomial.

b.  $(-1, 0)$ ,  $(2, 1)$ ,  $(3, 1)$ ,  $(5, 2)$ .

c.  $(0, -2)$ ,  $(2, 1)$ ,  $(4, 4)$ .

**EX.3.1.4, Sauer3**

- a. Find a polynomial  $p(x)$  of degree 3 or less whose graph passes through the points  $(0, 0)$ ,  $(1, 1)$ ,  $(2, 2)$ ,  $(3, 7)$ .
- b. Find two other polynomials (of any degree) that pass through these four points.
- c. Decide whether there exists a polynomial  $p(x)$  of degree 3 or less whose graph passes through the points  $(0, 0)$ ,  $(1, 1)$ ,  $(2, 2)$ ,  $(3, 7)$ , and  $(4, 2)$ .

**EX.3.1.6, Sauer3**

Write down a polynomial of degree exactly 5 that interpolates the four points  $(1, 1)$ ,  $(2, 3)$ ,  $(3, 3)$ ,  $(4, 4)$ .

**EX.3.1.8, Sauer3**

Let  $p(x)$  be the degree 9 polynomial that takes the value 112 at  $x = 1$ , takes the value 2 at  $x = 10$ , and equals zero for  $x = 2, \dots, 9$ . Calculate  $p(0)$ .

**EX.3.1.10, Sauer3**

Let  $p(x)$  be the degree 5 polynomial that takes the value 10 at  $x = 1, 2, 3, 4, 5$  and the value 15 at  $x = 6$ . Find  $p(7)$ .

**EX.3.1.18, Sauer3**

The expected lifetime of an industrial fan when operated at the listed temperature is shown in the table that follows. Estimate the lifetime at 70°C by using (a) the parabola from the last three data points (b) the degree-3 curve using all four points.

temp (°C)	hrs ( $\times 1000$ )
25	95
40	75
50	63
60	54

Please use COLAB for this problem.

No handwritten work! Please turn in a Colab Notebook



### CP.3.1.4, Sauer3

Remodel the `sin1` calculator key in Program 3.3 to build `cos1`, a cosine key that follows the same principles. First decide on the fundamental domain for cosine.

**EX.3.2.2, Sauer3**

- a. Given the data points  $(1, 0)$ ,  $(2, \ln(2))$ , and  $(4, \ln(4))$ , find the degree 2 interpolating polynomial.
- b. Use the result of (a) to approximate  $\ln(3)$ .
- c. Use Theorem 3.3 to give an error bound for the approximation in part (b).
- d. Compare the actual error to your error bound.