

CP.2.3.1, Sauer3

For the n -by- n matrix with entries $a_{ij} = 5/(i + 2j - 1)$, set $x = (1, \dots, 1)^T$ and $b = Ax$. Use the python program from CP.2.2.2 or Numpy's `numpy.linalg.solve` command to compute `x_c`, the double precision computed solution. Find the infinity norm of the forward error and the error magnification factor of the problem $Ax = b$, and compare it with the condition number of A : (a) $n = 6$, (b) $n = 10$.

Hint: Be careful with Python's indexing that starts at 0, and Sauer's and Matlab's indexing that starts at 1. With zero-based indexing the formula for a_{ij} is $a_{ij} = 5/(i + 2j + 2)$. Here is a code snippet to generate A with $n = 5$.

```
n = 5
A = np.zeros( [ n, n ], dtype=float )
for i in range(0,n):
    for j in range(0,n):
        A[i,j] = 5 / ( i + 2*j + 2.)
print(A)
```

```
[[2.66666667 2.          1.71428571 1.55555556 1.45454545]
 [2.25        1.83333333 1.625        1.5         1.41666667]
 [2.          1.71428571 1.55555556 1.45454545 1.38461538]
 [1.83333333 1.625        1.5         1.41666667 1.35714286]
 [1.71428571 1.55555556 1.45454545 1.38461538 1.33333333]]
```