Analogical classification in formal grammar

Matías Guzmán Naraaj



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Matías Guzmán Naranjo

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4 Methodological notes

In this chapter I present, somewhat informally, the statistical and data visualization tools I will use in the rest of this book. Readers interested in the mathematical details should consult the cited sources, since detailed descriptions and explanations of these techniques would merit a short book and a strong statistical background. My intention is only to provide the reader with a good intuition of what these methods do.

4.1 On the general methodology

Many of the phenomena I discuss in the following case studies have been studied exhaustively before, and it is not my intention to develop complete analyses for any of these cases. Moreover, in several instances, I will use sub-optimal models that ignore semantics or other possible strong predictors, this should only make the main point stronger: formal analogy occurs even in unexpected cases, and it follows the grammatical hierarchy of the language. Similarly, I do not provide full formal linguistic analyses, but rather only sketches to motivate a plausible type hierarchy. It is my intention that the ideas proposed in this book can be formally implemented in different linguistic theories (Construction Grammar, Cognitive Grammar, Paradigm Function Morphology, HPSG or similar). This is why theoretical assumptions are kept to a minimum.

I make no strong claims concerning the psycho-linguistic reality to these models. The fact that we can predict, to a greater or lesser degree, word classes from formal properties of words, does not mean that speakers necessarily do the same. It is possible that the way speakers perform class assignment in some of the languages studied has some parallels to the models proposed here, but it is also possible that speakers do rely on different aspects of cognition. These are related but independent questions. The patterns I will present could be productive, or vestiges of previous systems, but not any less real. I will, however, make some connections with some ideas about cognitive aspects of language during the final discussion.

There are two main reasons for the choice of languages in this study: theoreti-

cal relevance and data availability. I have not tried to compile a representative typological sample. Far from it, most examples are from Indo-European languages of various subfamilies, and only a few are taken from African languages. The analogical models require an electronic, morphologically annotated dictionary, which are still very rare for languages spoken by smaller language communities. The theoretical relevance relates to the classes a language has and how they are organized.

4.2 Statistical models and methodology

For all the cases to follow I use the same general method for building the analogical models. From the stem of the words (nouns or verbs) I extract predictors which might be at play in the analogical relations and fit a neural network with the nnet package (Venables & Ripley 2002)¹ in R (R Development Core Team 2008). The use of neural networks has a long history in linguistics, and they are usually linked to connectionist models (Bechtel & Abrahamsen 2002; Churchland 1989; McClelland & Rumelhart 1986; Rumelhart & McClelland 1986a). However, I do not make any claims about the underlying linguistic system, or the rightness or wrongness of connectionism. The use of neural networks for the following analogical models is purely practical. Similar effects could probably be achieved using different algorithms like Random Forest (Breiman 2001) or Support Vector Machines (Smola & Schölkopf 1998; Scholkopf & Smola 2001). For the present book, the actual technology is not important, only the concept behind it². My aim is to show that prediction is possible, not to find the best possible method.

The *stems* in the models are not theoretical objects, and the ideas in these models should be compatible with word-based models. The idea is that there is a distinction between the phonological material that expresses some property like MASCULINE, and the phonological material that expresses the meaning 'cat'. I take the *stem* to be the full word minus the phonological material that marks the category at hand. In a trivial Spanish example, the stem of *gato* ('male cat') is /*gat*/, since the /o/ segment is the gender correlate, and we have the opposing form *gata* ('female cat'). For many non-trivial cases some compromise had to

¹For all models I used the softmax linking function and the maximum number of weights and iterations set in a way that the models converge. Whether a hidden layer was present or not, and the number of hidden units, varied from model to model.

²The next subsection provides a simple illustration of how the analogical models work, but the interested reader should consult Venables & Ripley (2002) for a rigorous mathematical explanation of neural networks and the nnet package.

be reached, and it will be described in detail. Crucially, this approach does not consider underlying representations, only surface forms. Of course, one could compare the results of a model based on some sort of underlying representation with the results of more surface oriented models.

The predictors used to fit the analogical models vary slightly from model to model, but they always contain phonological information about the shape of the word. The most straightforward way to do this is to simply take a set number of letters at the end (or beginning) of the stems and use them (together with their position) as predictors. What the positional information does is to make a distinction between, say, a t at the end of the stem and a t in the third to last position. This way of specifying phonological shape has advantages and disadvantages. A good aspect of this approach is that the model can, on its own, infer classes between phonemes as represented by letters. If x and h share some phonological feature which makes them into a natural class, and are thus predictive of the same inflection class or gender, the model will simply assign the corresponding weights to said inflection class. This means that we do not need a rich phonological representation to arrive at phonological analogies. Another possible issue, which might unfairly benefit or harm the models, is that in cases of low correspondence between the phonology and the orthography, certain spelling rules might contain some additional information not directly available to speakers, or some important information might be missing. There is no easy way to solve this problem, short of using detailed phonological transcriptions, which are unavailable for most of the languages under consideration. Any sort of phonological process like methathesis, which could be easily captured by a rule-based approach, will be invisible to the model, thus reducing the amount of information available. To reduce loss of information due to some spelling systems representing a single phoneme with a character sequence (e.g. Spanish and German), I simplified spelling assigning special characters to those regular sequences. Some phonological information is, however, non-recoverable from the orthography (e.g. some vowel length/quality information in German, or the difference between long and double vowels in Kasem).

To prevent overfitting³ the models I apply ten-fold cross-validation to every model. This is done by splitting the dataset into ten groups. The general model is then fitted using nine of the groups as training data and testing the predictions of the model on the group not used for fitting it. The process is repeated for

³Overfitting happens when models predict the same items they learned from. This is a problem because if a model is overfitted, it does not really tell us much about how good the predictors are on novel items.

each of the ten subgroups. This way we can look at all the data while preventing overfitting (Kohavi 1995).

In section §2.2 I discussed four possible ways of implementing analogy, and argued that the difference is a gradient rather than a truly categorical one. The present models fall somewhere between a weighted multiple-rule-based model like those presented by Albright & Hayes (2003) and Albright (2009) and a purely stochastic model like NDL (Arppe et al. 2014; Baayen 2011; Baayen et al. 2011) or AM (Skousen 1989; Skousen et al. 2002; Skousen 1992; Arndt-Lappe 2011; 2014). The difference between the present model and a weighted rule-based model is that I consider all possible patterns within some structurally defined positions in the word (e.g. the last two segments, the last consonant, the number of syllables, etc.), and do not attempt to predefine the rules of the model, or decide to include or exclude some patterns. The difference to a completely stochastic system lies in the same property: the current model is sensitive to structural properties of the lexemes it sees, while NDL and AM are "blind" or completely amorphous. Like AM, and unlike some previous connectionist systems (Bechtel & Abrahamsen 2002; Churchland 1989; McClelland & Rumelhart 1986; Rumelhart & McClelland 1986a), the analogical model used here sees linguistically defined categories as the outputs. In traditional connectionist systems the networks directly paired semantics to sounds (Matthews 2005).

The similarities between these kinds of systems have been observed before:

Connectionist networks themselves further illustrate the problem, in that they might be seen to fall in both camps. Back-propagation networks are often described as depending on similarity...However, they are also often described as using 'implicit rules' which can be extracted using appropriate analysis...Therefore, back-propagation networks appear rule- and similarity-based (Hahn & Chater 1998: p. 200)

In any case, it should be clear that I am not arguing for neural networks as a necessarily better implementation of analogical systems, or as a psychologically plausible system. Neural networks as used here are just one of the many alternatives we have to model analogy.

All this being said, a more clever and carefully designed model similar to the weighted multiple-rule-based model like those presented by Albright & Hayes (2003) and Albright (2009), or that of Beniamine & Bonami (2016), would probably perform better for any particular case and be more psychologically plausible. These models have some downsides, however. The most important one is that

they require much better structured datasets, with complete phonological information. This requirement is harder to fulfill than the rough, semi-phonemic transcriptions required for the neural network models. A second difficulty of these models is that they are extremely slow to fit because the rule inference step is computationally intensive. This makes it impossible in practice to fit many different models for each case and hence impractical to test various combinations of predictors.

4.3 Analogical models using neural networks

The easiest way to explain the intuition behind the models, and the tools I use for evaluating them, is with concrete examples. Suppose a language has two inflection classes, A and B. The dataset in (1) presents stems for lexemes belonging two said inflection classes.

(1) a. A: lama, lara, lado, laso, pama, ra, dal, kar, tsar, sek, cessb. B: egrr, liz, lo, loi, lu, lip, roop, oppe, toi, olor, gin, grip, wik

There is no single (simple) rule which can predict to what class a given lexical item belongs. However, intuitively, the first vowel seems to be a strong indicator. All items for which the first vowel is a belong to class A, while items for which the first vowel is a or a belong to class B. Items with a are found in both groups. Because there are only a few lexical items, and the pattern is fairly simple, this generalization is fairly evident, but in a more complex system it would be much harder. These observations could also be inferred with a statistical model.

Put in simple terms, given a training dataset with items, and a series of predictors for each item, the neural network model learns from these items and assigns weights to the predictors. When presented with new data (the testing dataset), the network calculates from the weights the probability of each outcome for each item in the dataset. This is achieved the following way. The neural network sets a baseline for the prediction, based on one of the levels for each predictor. For each predictor, the first level (alphabetically) is chosen for the baseline node (in this case thus: s1=c, s2=a). This baseline has a weight for each outcome (the classes to be predicted). To each other level of each predictor, it assigns a weight for each outcome. The weights of the predictors are added to the baseline to calculate the probability of each outcome given some input.

We can apply this to our previous example. We split the data set into a training and a small testing dataset. For the testing dataset we randomly select the items:

lama, *lara*, *kar*, *egrr*, *liz*, *oppe*, *grip*, and we assign the rest of the items to the training dataset. For illustration, we can fit two different models. In Model 1, we set two predictors s1 and s2, which correspond to the first and second letter in the items, respectively. For Model 2 we set v1 and c1, which correspond to the first vowel and first consonant of the items, respectively. We can then train Model 1 and Model 2.

Figure 4.1 shows the structure of the neural network for Model 1. As can be seen, there is a direct connection between the predictors and the outcomes (a skip layer), and there are no intermediate steps (hidden layers). We can see how each letter predicts A or B. The thickness of the line represents the absolute value of the weight (thicker lines have larger absolute values), and the color represents whether the weight is positive (dark gray) and favors the outcome, or negative (light gray) and disfavours the outcome. In the node marked as B1 we have the baseline (the bias node) made up of the combination of the levels c for s1 and a for s2⁴. This combination clearly favours A, as we would expect. If any of these levels changes in the input, then the nodes in the skip layer activate and counteract the baseline. If, say, the input contains an u, i or o instead of an a in s2, then the corresponding node will strongly activate the outcome B, as we, again, would expect from the data set. The complete set of weights from the inputs to the outcomes for Model 1 is given in Table 4.1.

To calculate the actual class probabilities from the output weights, we use the softmax function. The intuition of this function is that, given a vector of weights, it will transform that vector into a vector of probabilities, where the element with the highest weight will receive the highest probability, and all probabilities add up to 1. The general form of this function is given in equation (4.2). In prose, we exponentiate each weight, and divide by the sum of all exponentiated weights.

$$S(y_i) = \frac{e^{y_i}}{\sum_{i}^{e^{y_j}}} \tag{4.2}$$

As an example, assume the weight vector [2, 1, 0.1]. Exponentiating each member we get the vector [7.4, 2.7, 1.1], and their sum is 11.21. Dividing the exponentiated weights by the sum we get the probabilities [0.66, 0.24, 0.1].

To know how well the model performs, we predict the outcomes of the testing dataset, build a confusion matrix and calculate different accuracy scores. The corresponding confusion matrix for this model is shown in Table 4.3. Here we see the predictions that the model made for each testing item. There were two

⁴The models chooses the baseline levels purely on alphabetical order.

4.3 Analogical models using neural networks

Figure 4.1: Representation of Model 1.

Table 4.1: Weight table for Model 1.

	weight	predictor	response	variable
1	5.42	c-a	A	baseline
2	3.43	d	A	s1
3	-0.29	e	A	s1
4	-3.21	g	Α	s1
5	0.58	k	A	s1
6	2.89	1	A	s1
7	-7.13	O	Α	s1
8	4.37	p	A	s1
9	1.89	r	A	s1
10	2.24	S	A	s1
11	0.81	t	A	s1
12	-2.62	w	A	s1
13	4.67	e	A	s1
14	0.61	g	A	s1
15	-13.22	i	A	s1
16	-8.12	1	A	s1
17	-14.45	O	A	s1
18	0.03	p	A	s1
19	-0.33	r	A	s1
20	4.25	S	A	s1
21	-18.31	u	Α	s1
22	-5.43	c-a	В	baseline
23	-3.88	d	В	s2
24	-0.35	e	В	s2
25	3.28	g	В	s2
26	0.49	k	В	s2
27	-2.19	1	В	s2
28	7.49	O	В	s2
29	-4.96	p	В	s2
30	-2.67	r	В	s2
31	-2.02	S	В	s2
32	-0.49	t	В	s2
33	2.95	w	В	s2
34	-5.20	e	В	s2
35	-0.48	g	В	s2
36	12.77	i	В	s2
37	8.35	1	В	s2
38	13.70	o	В	s2
39	-0.38	р	В	s2
40	-0.11	r	В	s2
41	-3.81	s	В	s2
42	17.85	u	В	s2

errors in total: *egrr* and *grip*. It is easy to see why these errors happen: there are no comparable items in the training dataset, *grip* starts with a *gr* sequence and *egrr* is the only item with an *e* as first letter and *g* as second letter.

Table 4.3 shows the confusion matrix for the predictions of Model 1, and Table 4.4 shows a matrix with the positions of True Positives (TP), True Negatives (TN), False Positives (FP) and False Negatives (FN). The TP and TN are cases where the class predicted by the model match the real class of the items. FP and FN are the cases where the class predicted by the model does not match the real class of the items. The total population N is the sum of all these values: TP + TN + FP + FN.

	Predicted	Observed	Word
1	A	A	lama
2	A	A	lara
3	A	A	kar
4	A	В	egrr
5	В	В	liz
6	В	В	oppe
7	A	В	grip

Table 4.2: Predictions Model 1.

Table 4.3: Confusion matrix for Model 1.

	Reference		
Prediction	A	В	
A	3	2	
В	0	2	

The accuracy is the number of correct predictions divided by the total number of items. Additionally, we can calculate the confidence interval (CI) of the accuracy by using a binomial test (Clopper & Pearson 1934; Newcombe 1998). The No Information Rate (or accuracy of a model under a no information situation) is calculated as the largest class percentage in the data. In this case, A's class percentage is 0.4286 and B's is 0.5714, thus the latter is taken to be the No Information Rate. In other words, the No Information Rate is the accuracy of a

Table 4.4: Diagram of True Positives, False Positives, True Negatives and False Negatives.

	Refe	rence
Prediction	A	В
A	TP	FP
В	FN	TN

model that always predicts the most frequent outcome. In our example data $\bf B$ is the most frequent outcome. If the model predicted all outcomes to be $\bf B$, then it would reach an accuracy of 4/7 = 0.5714. Models where all predictors have no information regarding the outcomes (i.e. they are poor predictors) tend to have an accuracy close to the No Information Rate, because always predicting the most frequent outcome guarantees the highest possible accuracy under a no information situation. The model is then said to perform above chance if the No Information Rate is less than the lower limit of the accuracy confidence interval.

There are three additional statistical values I will use in certain cases are: *Specificity, Sensitivity* and *Negative Predictive Value*. Specificity is the proportion of negatives that are identified as such (= TN/(TN + FP)), while sensitivity is the proportion of positives that are identified as such (= TP/(TP + FN)). The negative predictive value (= TN/(TN + FN)) will help us identify the class to which more items from other class are misclassified. These three statistics are not relevant for this particular example because we only have two classes here, but can be used, by class, in models with more than two outcomes.

Finally, the kappa statistic compares the observed accuracy with the expected accuracy (under random chance). The expected accuracy is calculated as follows. We multiply the observed frequency of **A** by the predicted frequency of **A**, and the observed frequency of **B** by the predicted frequency of **B**. We then divide these numbers by N, add them together and divide again by N. Thus, we get:

Expected.Accuracy =
$$\frac{\frac{(\text{TP+FN})*(\text{TP+FP})}{N} + \frac{(\text{TN+FP})*(\text{TN+FN})}{N}}{N}$$
 (4.3)

Finally to calculate the kappa statistic we use the following equation:

$$Kappa = \frac{observed.accuracy - expected.accuracy}{1 - expected.accuracy}$$
(4.4)

Kappa scores⁵ go from 0 (in a perfectly random model) to 1 (in a perfectly accurate model), a kappa of 0.5 is halfway between the expected accuracy and 1. The advantage of using kappa is that it tells us how well above random chance the model is performing, and, to a degree, it allows to make model comparisons. The disadvantage is that there is no standarized interpretation and no objective cutoff point. A model with a kappa of 0.2 is not inherently bad, nor can it be said that it is at chance level. However, we can say that a model with a kappa of 0.7 is better than a model with a kappa of 0.5.

Table 4.5 shows the relevant statistics for Model 1. In this case, because our dataset is so small, the model's accuracy can not be said to be better than chance.

Overall statistics:						
Accuracy	0.7143					
95% CI	(0.2904, 0.9633)					
No Information Rate	0.5714					
Карра	0.3593					

Table 4.5: Overall statistics for Model 1.

A second possible model for our dataset is to specify more linguistic information in the predictors. In Model 1 all we have is information about position of the segments, but not information about their nature. An alternative would be to set a model where the predictors are not selected by position only, but also by class. Instead of using the first and second letters in the pseudo words, we will now use the first consonant (c1) and the first vowel (v1). Figure 4.2 shows the structure of Model 2 as before. By selecting more structural predictors we have somewhat reduced the complexity of the model⁶, but the same generalization remains: the main predictor is the first vowel of the word. The full set of weights for the model is given in Table 4.6.

⁵In our case: Expected.Accuracy = $\frac{\frac{3\cdot(3+2)}{7} + \frac{2\cdot(2+2)}{7}}{\frac{2\cdot(3+2)}{7}} = \frac{\frac{15}{7} + \frac{4}{7}}{7} = 0.4694$. The accuracy is 5/7 = 0.7143. Thus, we have that kappa = $\frac{0.7143 - 0.4694}{1 - 0.4694} = 0.4615$. Notice that the Expected Accuracy is different from the No Information Path Accuracy 11 C

Thus, we have that kappa = $\frac{0.7143-0.4694}{1-0.4694}$ = 0.4615. Notice that the Expected Accuracy is different from the No Information Rate because the former is taken from a model that knows about the distribution of the outcomes in the training dataset, while the latter is a completely random assignment of outcomes to inputs in the testing dataset.

⁶Notice this is only the case because of the characteristics of this dataset. In more complex datasets a more structured model will usually be more complex than a less structured one because it requires more information.

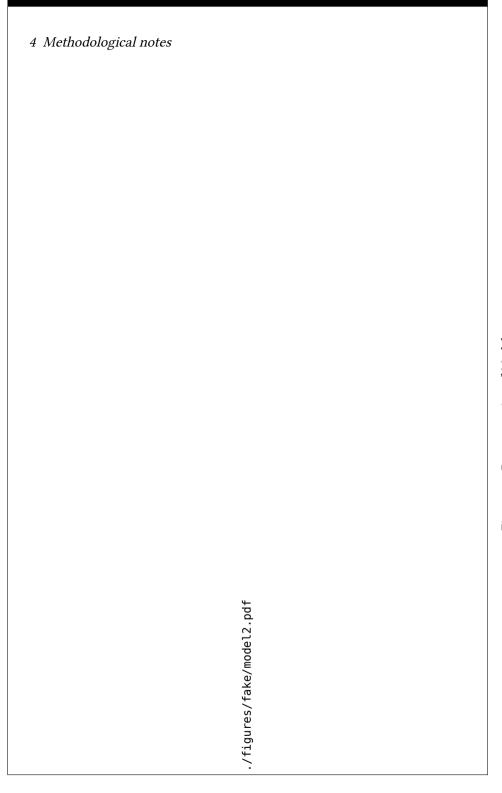


Figure 4.2: Representation of Model 2.

Table 4.6: Weight table for Model 2.

	weight	predictor	response	variable
1	7.43	a-c	A	baseline
2	11.87	e	A	v1
3	-21.81	i	A	v1
4	-24.18	0	A	v1
5	-34.05	u	A	v1
6	5.77	d	A	c1
7	-6.66	g	A	c1
8	0.34	k	A	c1
9	6.80	1	A	c1
10	5.68	p	A	c1
11	-2.33	r	A	c1
12	5.48	S	A	c1
13	-3.36	t	A	c1
14	-8.98	W	A	c1
15	-8.19	a-c	В	baseline
16	-12.23	e	В	v1
17	22.95	i	В	v1
18	25.17	0	В	v1
19	34.15	u	В	v1
20	-5.20	d	В	v1
21	7.28	g	В	c1
22	0.09	k	В	c1
23	-6.61	1	В	c1
24	-5.82	p	В	c1
25	2.02	r	В	c1
26	-6.57	S	В	c1
27	2.48	t	В	c1
28	9.22	W	В	c1

4 Methodological notes

In Table 4.7 we see now the results of the predictions. This time the model only made one mistake: egrr. The reason why grip is correctly classified this time is that the model finds it similar enough to liz, lip and gin, because it now knows what its vowel is. Trying to reconstruct the evaluation of egrr is instructive. For obtaining the weight for A we add to the baseline (7.43) the weight for cl=g(-6.66) and cl=g(11.87), which gives us 12.64, and we do the same for cl=g(-6.66) and we get -13.14. This clearly makes cl=grr with the node for cl=grr was pulling, in both cases, for cl=grr B. This means that even though the model made the wrong choice, it did see a similarity between egrr and other cl=grr between cl=grr and other cl=grr belonging to class cl=grr bad the highest (even if small) probability of belonging to class cl=grr between classes.

Table 4.7: Predictions Model 2, including the probabilities for class ${\bf A}$ and ${\bf B}$.

	Predicted	Probability A	Probability B	Observed	Word
1	A	9.99e-01	3.25e-07	A	lama
2	A	9.99e-01	3.25e-07	A	lara
3	A	9.99e-01	5.20e-07	A	kar
4	A	9.99e-01	3.18e-06	В	egrr
5	В	5.14e-05	9.99e-01	В	liz
6	В	1.83e-04	9.99e-01	В	oppe
7	В	5.55e-09	1.00e+00	В	grip

The corresponding confusion matrix and statistics for Model 2 are given in Table 4.8 and Table 4.9, respectively.

Table 4.8: Confusion matrix for Model 2.

	Ref	ference
Prediction	A	В
A	3	1
В	0	3

Table 4.9: Overall statistics for Model 2.

Overall statistics:				
Accuracy	0.8571			
95% CI	(0.4213, 0.9664)			
No Information Rate	0.5714			
Карра	0.72			

One final important point is that we see how the CI and the Kappa are partially independent of each other. In Model 2, we obtained a Kappa of 0.72, which is considerably higher than what we would get in a random model, but because this metric is not sensitive to sample size, it fails to take into account the fact that there are only seven observations. The CI information, on the other hand, does take this into account and rightly tells us that we cannot draw any conclusion from this tiny dataset. I will use both metrics together when evaluating models.

The models in the following chapters are too large and complex to either plot, or explore by hand. For this reason I will only make use of confusion matrices and accuracy scores to evaluate them, but in principle it would be possible for someone to inspect any of the analogical models presented here.

4.4 Measuring variable importance

An issue with neural networks is the fact that it is relatively difficult to interpret the exact importance that the different factors have on the overall model. Unlike linear or logistic regression, we cannot directly explore the coefficients. However, in some cases, it is important to understand which factor plays a more or less important role predicting some dataset. To address this question we can make use of additive and subtractive modelling. The idea is very simple. For subtractive modelling we start with the complete model (with all predictors), and we compare its accuracy and kappa scores to models leaving one predictor out. This technique allows us to compare the relative importance of each individual predictor in the context of the complete model, each individual predictor is. The additive variant of this idea consists of starting with a null model without predictors, and one by one, adding the original predictors back and comparing at each step the accuracy and kappa scores.

4.5 Clustering and distances between classes

The second important method I will use throughout this book is that of clustering and measuring class similarity. Imagine the new made up set of stems whose inflectional class we want to predict as shown in (5):

- (5) a. A: lama, lara, lado, laso, tama, ga, gal, tar, tsar, tek, tess
 - b. B: egrr, liz, lo, loi, le, lep, loop, olpe, toi, olor, gen, grap, tak
 - c. C: yrro, yrto, yro, undo, ujo, jyr, juk, juz, ryk

In this new example we have three classes (A, B and C) which are easily described in terms of their first vowels and consonants. Words in A have an a, or an e preceded by a t, s or g. Words in B have an o, i, a, or an e not preceded by a t (except for tak). Words in C have a y or u, usually with an r or j. Additionally, we can observe that there is a much greater similarity between A and B, than C to the other two. A and B can appear with an l or e, and to a lesser degree t or g, while C does not.

We can fit a new model using again the predictors c1 and v1 to this new dataset (Model 3), and because the system is much more regular now, it should predict perfectly the class of an item. What we really want to achieve now is measuring the similarity between the three classes based on the analogical model. This can be done in different ways. In a model with few classes and lots of errors between the classes, we could look at the degree of confusion between any two classes and set classes with more confusion as more similar. In models with many classes this is less practical because class size is Zipf distributed (Blevins et al. 2016), which means that many classes will have very few members. In highly accurate models with very few errors, the measured similarity for small classes will be much less reliable. An alternative I will use in this situation is to directly use the probabilities predicted by the model.

The probabilities for Model 3 can be seen in Table 4.10⁷. In this table, each line shows the probabilities a stem has of belonging to either of the three classes. So, for *lama*, the probabilities are 0.8496 for class **A**, 0.1503 for class **B**, and 6.225e-09 for class **C**. From these probabilities we can build a (negative) correlation distance matrix⁸ and from this, a distance matrix as shown in Table 4.11.

⁷For the purposes of this example I am not splitting the dataset into training and testing sets. For the actual case studies the probabilities used come from the same cross-validation process.

⁸When using errors instead of probabilities the process is the same, but we take the negative correlation measures for the confusion matrix instead.

Table 4.10: Predicted probabilities for Model 3.

	Probability A	Probability B	Probability C	Word
1	8.496e-01	1.503e-01	6.225e-09	lama
2	8.496e-01	1.503e-01	6.225e-09	lara
3	8.496e-01	1.503e-01	6.225e-09	lado
4	8.496e-01	1.503e-01	6.225e-09	laso
5	9.512e-01	4.873e-02	5.017e-12	tama
6	5.987e-01	4.012e-01	3.328e-11	ga
7	5.987e-01	4.012e-01	3.328e-11	gal
8	9.512e-01	4.873e-02	5.017e-12	tar
9	9.512e-01	4.873e-02	5.017e-12	tsar
10	5.974e-01	4.025e-01	1.745e-11	tek
11	5.974e-01	4.025e-01	1.745e-11	tess
12	1.018e-01	8.981e-01	3.138e-11	egrr
13	5.833e-23	1.000e+00	1.999e-19	liz
14	2.353e-17	1.000e+00	4.455e-15	lo
15	2.353e-17	1.000e+00	4.455e-15	loi
16	3.006e-01	6.993e-01	1.220e-08	le
17	3.006e-01	6.993e-01	1.220e-08	lep
18	2.353e-17	1.000e+00	4.455e-15	loop
19	2.353e-17	1.000e+00	4.455e-15	olpe
20	8.127e-17	1.000e+00	1.107e-17	toi
21	2.353e-17	1.000e+00	4.455e-15	olor
22	1.018e-01	8.981e-01	3.138e-11	gen
23	5.987e-01	4.012e-01	3.328e-11	grap
24	9.512e-01	4.873e-02	5.017e-12	tak
25	6.060e-11	7.044e-14	1.000e+00	yrro
26	6.060e-11	7.044e-14	1.000e+00	yrto
27	6.060e-11	7.044e-14	1.000e+00	yro
28	1.308e-11	1.154e-13	1.000e+00	undo
29	5.052e-12	7.686e-15	1.000e+00	ujo
30	1.162e-09	1.756e-12	1.000e+00	jyr
31	5.052e-12	7.686e-15	1.000e+00	juk
32	5.052e-12	7.686e-15	1.000e+00	juz
33	6.060e-11	7.044e-14	1.000e+00	ryk

Correlation matrix						
	A	В	С			
Α	0.000	-1.359	-1.533			
В	-1.359	0.000	-1.598			
C	-1.533	-1.597	0.000			
As distances						
	A	В				
В	0.359					
C	0.533	0.598				

Table 4.11: Correlation distances for Model 3.

From the distance matrix we can see that A is closest (has the smaller distance) to B, and that the greater distance is between B and C. Using the distance matrix we can then build a dendrogram using hierarchical clustering (Rokach & Maimon 2005) as in Figure 4.3. Similarly, we can compress the information given in the correlation matrix from three to two dimensions using multidimensional scaling (MDS) (Borg & Groenen 2005; Cysouw 2007). Informally, MDS is a way of visualizing highly dimensional data in a two-dimensional plot. It tries to preserve as much of the original distance between two objects as possible. There is an inherent data loss when using MDS, which means the plots are an approximation, and there is dimensional data in the original distance matrix being lost. Using this two-dimensional representation of the data we can plot the categories on a two-dimensional plane as in Figure 4.4.

In this case, both representations agree with the observation from before: A and B are closer to each other than to C. Additionally, Figure 4.3 shows that A is somewhat closer to C than B is. For simple cases with only three groups I will only make use of dendrograms, but for cases with many classes I will also use MDS.

⁹For the clustering I use the Ward's linkage method. Although Ward's method (Murtagh & Legendre 2014) is designed to be applied to Euclidean distances, some recent studies have shown it performs formidably with other distance metrics (Meyniel et al. 2010; Strauss & von Maltitz 2017).

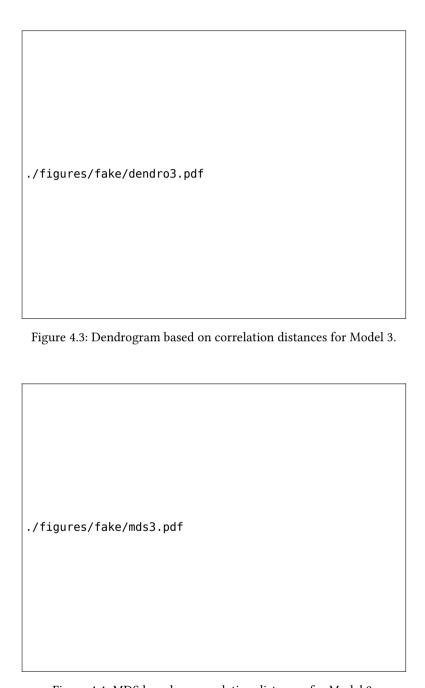


Figure 4.4: MDS based on correlation distances for Model 3.

4.6 Summing up

I have shown in this chapter that building analogical models with neural networks is not conceptually different from finding analogical relations by hand. The statistical models are, to a great extent, a notational variant of informal descriptions or schemas. They have the advantage that they require less manual work and can be easily applied to very large datasets. The clustering analysis with dendrograms and the MDS analysis for finding similar classes does not produce substantially different results from what a linguist would arrive at by inspecting the items manually. As stated before, there is no claim about the cognitive reality or psycholinguistic plausibility of the neural networks themselves. Neural networks are simply tools. The claim is that the analogical relations are present in the data, and speakers can thus make use of these relations.

In the next chapters I will use these tools to explore different analogical systems in various languages. Part II contains four chapters besides this one, each corresponding to a general topic and containing at least two case studies. Chapter §5 deals with some general gender issues in Latin and Romanian. This chapter introduces the basic claim, and shows how analogical relations that predict gender in nouns have a correlate with the hierarchy. Chapter §6 shows what happens in systems where simple trees are not enough and we need hybrid types in the hierarchy. This chapter deals with the topic of overabundance and affix competition in Russian and Croatian. Chapter §7 explores the claim that we need structural information in the analogical models. I present examples from prefixing languages (Swahili and Otomí de la Sierra), where the analogical process takes place on the first segments of the items, and Hausa, were the analogical specification requires more structure than for other languages. Chapter §8 presents three cases of complex inflectional systems: Spanish verb classes and Kasem number classes. This chapter provides the strongest evidence for the interaction between type hierarchies and analogical processes. Finally, Chapter §9 sums up the results and their implications for both usage-based and formal linguistics.

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some language, see some other lan-
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Analogical classification in formal grammar

The organization of the lexicon, and especially the relations between groups of lexemes is a strongly debated topic in linguistics. Some authors have insisted on the lack of any structure of the lexicon. In this vein, Di Sciullo Williams (1987: 3) claim that "[t]he lexicon is like a prison – it contains only the lawless, and the only thing that its inmates have in commonis lawlessness". In the alternative view, the lexicon is assumed to have a rich structure that captures all regularities and partial regularities that exist between lexical entries. Two very different schools of linguistics have insisted on the organization of the lexicon.

On the one hand, for theories like HPSG (Pollard Sag 1994), but also some versions of construction grammar (Fillmore Kay 1995), the lexicon is assumed to have a very rich structure which captures common grammatical properties between its members. In this approach, a type hierarchy organizes the lexicon according to common properties between items. For example, Koenig (1999: 4, among others), working from an HPSG perspective, claims that the lexicon "provides a unified model for partial regularties, medium-size generalizations, and truly productive processes".

On the other hand, from the perspective of usage-based linguistics, several authors have drawn attention to the fact that lexemes which share morphological or syntactic properties, tend to be organized in clusters of surface (phonological or semantic) similarity (Bybee Slobin 1982; Skousen 1989; Eddington 1996). This approach, often called analogical, has developed highly accurate computational and non-computational models that can predict the classes to which lexemes belong. Like the organization of lexemes in type hierarchies, analogical relations between items help speakers to make sense of intricate systems, and reduce apparent complexity (Köpcke Zubin 1984).

Despite this core commonality, and despite the fact that most linguists seem to agree that analogy plays an important role in language, there has been remarkably little work on bringing together these two approaches. Formal grammar traditions have been very successful in capturing grammatical behaviour, but, in the process, have downplayed the role analogy plays in linguistics (Anderson 2015). In this work, I aim to change this state of affairs. First, by providing an explicit formalization of how analogy interacts with grammar, and second, by showing that analogical effects and relations closely mirror the structures in the lexicon. I will show that both formal grammar approaches, and usage-based analogical models, capture mutually compatible relations in the lexicon.

