

### Answers for Semantics Workshop 3

Q2

- (i) The set of all entities  $y$  such that Jo liked  $y$  and Ethel didn't like  $y$ .
- (ii) The set of all entities  $z$  such that  $z$  gave the cake to themselves.
- (iii) The set of all entities  $x$  that are identical to Jo.
- (iv) The set of all entities  $z$  such that  $z$  is a student and  $z$  liked Jo.

Q3

(i)  $\lambda y [(like(y))(jo) \ \& \ \sim((like(y))(ethel))]$  (the-dog)

$\gg (like(the-dog))(jo) \ \& \ \sim((like(the-dog))(ethel))$

(ii)  $\lambda z [(give(z)(the-cat))(z)]$  (bertie)

$\gg (give(bertie)(the-cat))(bertie)$

(iii)  $\lambda x [\sim(x = jo)]$  (bertie)

$\gg \sim(bertie = jo)$

(iv)  $\lambda y [(like(the-cat))(y) \vee \sim(like(the-dog))(y)]$  (bertie)

$\gg (like(the-cat))(bertie) \vee \sim(like(the-dog))(bertie)$

(v)  $\lambda x [\lambda y [crazy(x) \ \& \ (like(x))(y)] (jo) \vee \sim(crazy(x))]$  (bertie)

$\gg crazy(bertie) \ \& \ (like(bertie))(jo) \vee \sim(crazy(bertie))$

Q4

(i)  $\lambda x [(kick(x))(x)]$  (jo)

$\gg (kick(x))(jo)$

**Wrong – every variable  $x$  should be replaced by jo**

**Should be**  $(kick(jo))(jo)$

(ii)  $\lambda x [\lambda x [howl(x)] (the-cat)]$  (the-dog)

$\gg \lambda x [howl(the-dog)] (the-cat)$

**Wrong – same variable is bound by two instances of lambda, one should be replaced by a different variable eg  $y$  ALSO, there is only one instance of a variable in the formula – there is nothing for the second lambda expression to convert**

(iii)  $\lambda y [(like(jo))(x)]$  (bertie)

>> (like(jo))(bertie)

**Wrong – can't convert by replacing x with bertie as the variable bound by lambda is not x but y; variables need to be the same for conversion to take place**

(iv)  $\lambda z$  [crazy(z)] (ethel)  $\vee$  drunk(z)

>> crazy(ethel)  $\vee$  drunk(ethel)

**Wrong – second open formula is not within the scope of the lambda operator and can't be converted, needs to be  $\lambda z$  [crazy(z)  $\vee$  drunk(z)] (ethel) to get the desired result**

Q5

- |      |  |   |
|------|--|---|
| i.   | $\lambda R [(R(jo'))(bertie')]$ .                        | $\langle\langle e, \langle e, t \rangle \rangle, t \rangle$   |
| ii.  | $\lambda P [\lambda A [A(P)]]$ .                         | $\langle\langle e, t \rangle, \langle\langle\langle e, t \rangle, \langle e, t \rangle \rangle, \langle e, t \rangle \rangle \rangle$ |
| iii. | $\lambda Q [Q(ethel')]$ .                                | $\langle\langle e, t \rangle, t \rangle$  |
| iv.  | $\lambda x [\lambda y [\lambda z [(give'(x)(y))(z)]]]$ . | $\langle e, \langle e, \langle e, t \rangle \rangle \rangle$  |
| v.   | $\lambda p [p \leftrightarrow rain']$ .                  | $\langle t, t \rangle$  |
| vi.  | $\lambda p [\lambda q [p \leftrightarrow q]]$ .          | $\langle t, \langle t, t \rangle \rangle$   |