Web Scale Data Mining homework 1

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2.1) You are analysing a stream which contains s singletons (items occurring once) and d pairs of items, in some random order. You are sampling the stream using Algorithm 2, which uses a pseudorandom number generator and takes each item for further processing with probability 1/100. What is the expected value of the fraction returned by the algorithm, as a function of s and d? Hint: follow the analysis in Section 4.2.1 of [10] (references in the textbook).

The correct answer would be: $\frac{d}{s+d}.$ The answer from algorithm 2:

• number of obtained singletons: $\frac{s}{100}$,

• number of doubles obtained twice: $\frac{d}{100*100} = \frac{d}{10000},$ • number of doubles obtained once: $d*2*\frac{1}{100}\frac{99}{100} = \frac{198d}{10000},$ • expected value of the fraction returned by the algorithm: $\frac{d}{100s+199d}.$