

ALGORITHM LABORATORY

ASSIGNMENT - 1

PROBLEM STATEMENT: Given a set of records R_1, \dots, R_n identified by keys K_1, \dots, K_n and a key K , decide whether the record corresponding to key K exists or not.

SCENARIOS: Write a program to implement the searching algorithms for each of the following situations:

1. *The input records are not sorted based on the keys and each key has equal probability of getting searched.*

ALGORITHM (LINEAR SEARCH):

- a. Start from the first element of the array.
- b. Compare the current element with the key to be searched.
- c. If a match is found, return the index of the element.
- d. If the end of the array is reached without finding the key, return -1 (indicating key not found).
- e. The algorithm terminates after either finding the key or scanning all elements.

PROGRAM CODE:

```
#include <bits/stdc++.h>
using namespace std;
using namespace std::chrono;

pair<int,int> linearSearch(vector<int> &records, int key,int n) {
    int comp = 0;
    comp = 2;
    for (int i = 0; i < n; i++) {
        if (key == records[i]) {
            return {i,comp};
        }
    }
```

```

        comp+=2;
    }
    return {-1,comp};
}

int main() {
    srand(time(NULL));
    for (int k = 10; k <= 10000; k *= 10) {
        unordered_set<int> records;
        unordered_set<int> search_string;

        while (records.size() < k) {
            int random = rand() % (5 * k);
            records.insert(random);
            search_string.insert(random);
        }

        while (search_string.size() < ((3 * k) >> 1)) {
            int random = (5 * k) + (rand() % (5 * k));
            search_string.insert(random);
        }

        vector<int> record(records.begin(), records.end());
        vector<int> search_strings(search_string.begin(),
search_string.end());
        random_shuffle(search_strings.begin(), search_strings.end());

        double time_key_found = 0;
        double avg_comparisions = 0;
        double time_key_not_found = 0;
        int key_found = 0, key_not_found = 0;
        int num_trials = 0;
        if(k<=100){
            num_trials=100000;
        }
        else if(k==1000) num_trials = 100;
        else num_trials = 10;

        for (int trial = 0; trial < num_trials; trial++) {
            for(int i=0;i<search_strings.size();i+=1){
                record.push_back(search_strings[i]);
                auto start = high_resolution_clock::now();
                pair<int,int> p;
                p= linearSearch(record, search_strings[i],k);
                int f = p.first;
                auto end = high_resolution_clock::now();
                record.pop_back();
                auto time = duration_cast<nanoseconds>(end - start);
            }
        }
    }
}

```

```

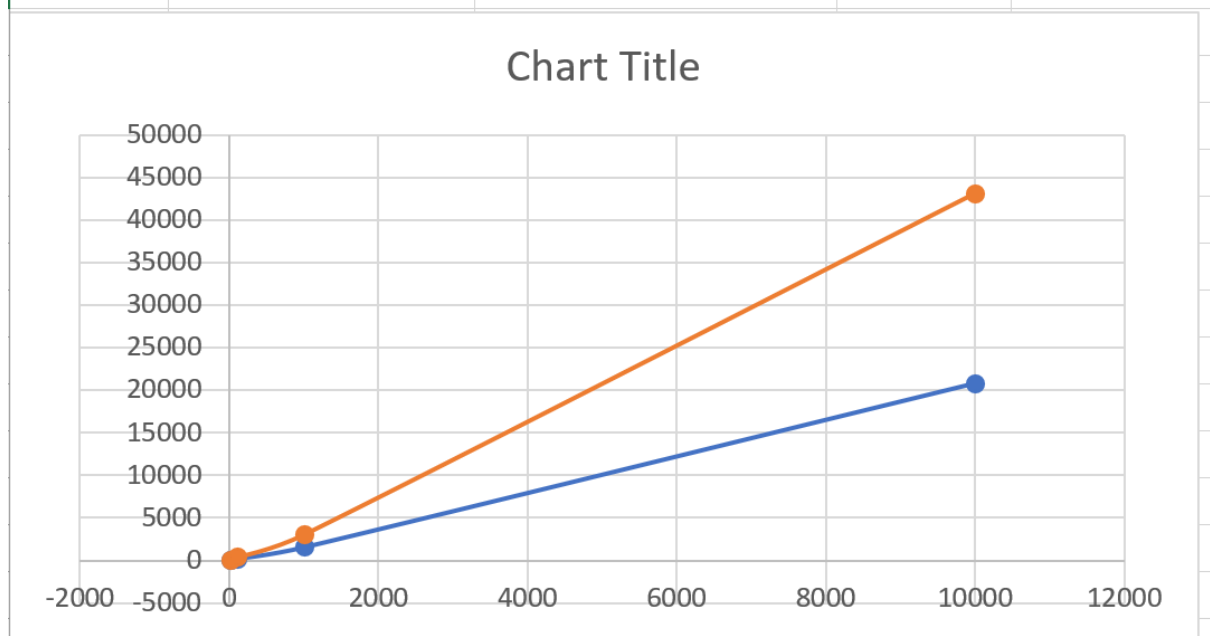
        avg_comparisions+=p.second;
        if (f == -1) {
            time_key_not_found += time.count();
            key_not_found++;
        } else {
            time_key_found += time.count();
            key_found++;
        }
    }
    avg_comparisions/=(key_not_found+key_found);
    double avg_key_found = (key_found > 0) ? time_key_found / key_found :
0;
    double avg_key_not_found = (key_not_found > 0) ? time_key_not_found /
key_not_found : 0;

    cout << "N = " << k << " | Key Found Avg = " << avg_key_found << "
nanoseconds"
        << " | Key Not Found Avg = " << avg_key_not_found << " nanoseconds" <<
" | Avg_num_of_comparisions = "<<avg_comparisions<<endl;
    }
    return 0;
}

```

OUTPUT and PLOT:

| N value | Time key found (ns) | Time key not found (ns) | Avg_comp | |
|---------|---------------------|-------------------------|----------|--|
| 10 | 110.788 | 99.2362 | 14.6667 | |
| 100 | 230.512 | 400.489 | 134.667 | |
| 1000 | 1577.98 | 3053.93 | 1334.67 | |
| 10000 | 20777.5 | 43102.7 | 13334.7 | |



2. The input records are not sorted based on the keys, but each key, $K_i, 1 \leq i \leq n - 1$, has a probability p_i of getting searched.

ALGORITHM (LINEAR SEARCH):

- Start from the first element of the array.
- Compare the current element with the key to be searched.
- If a match is found, return the index of the element.
- If the end of the array is reached without finding the key, return -1 (indicating key not found).
- The algorithm terminates after either finding the key or scanning all elements.

PROGRAM CODE:

```
#include <bits/stdc++.h>
using namespace std;
using namespace std::chrono;

pair<int,int> linearSearch(vector<int> &records, int key,int n) {
    int comp = 0;
    comp = 2;
    for (int i = 0; i < n; i++) {
        if (key == records[i]) {
            return {i,comp};
        }
        comp+=2;
    }
    return {-1,comp};
}

int main() {
    srand(time(NULL));
    for (int k = 10; k <= 10000; k *= 10) {
        unordered_set<int> records;
        unordered_set<int> search_string;

        while (records.size() < k) {
            int random = rand() % (5 * k);
            records.insert(random);
            search_string.insert(random);
        }

        while (search_string.size() < ((3 * k) >> 1)) {
```

```

        int random = (5 * k) + (rand() % (5 * k));
        search_string.insert(random);
    }

    vector<int> record(records.begin(), records.end());
    vector<int> search_strings(search_string.begin(),
search_string.end());
    random_shuffle(search_strings.begin(), search_strings.end());

    double time_key_found = 0;
    double avg_comparisions = 0;
    double time_key_not_found = 0;
    int key_found = 0, key_not_found = 0;
    int num_trials = 0;
    if(k<=100){
        num_trials=100000;
    }
    else if(k==1000) num_trials = 100;
    else num_trials = 10;

    for (int trial = 0; trial < num_trials; trial++) {
        for(int i=0;i<search_strings.size();i+=1){
            record.push_back(search_strings[i]);
            auto start = high_resolution_clock::now();
            pair<int,int> p;
            p= linearSearch(record, search_strings[i],k);
            int f = p.first;
            auto end = high_resolution_clock::now();
            record.pop_back();
            auto time = duration_cast<nanoseconds>(end - start);
            avg_comparisions+=p.second;
            if (f == -1) {
                time_key_not_found += time.count();
                key_not_found++;
            } else {
                time_key_found += time.count();
                key_found++;
            }
        }
    }
    avg_comparisions/=(key_not_found+key_found);
    double avg_key_found = (key_found > 0) ? time_key_found / key_found :
0;
    double avg_key_not_found = (key_not_found > 0) ? time_key_not_found /
key_not_found : 0;

    cout << "N = " << k << " | Key Found Avg = " << avg_key_found << "
nanoseconds"

```

```

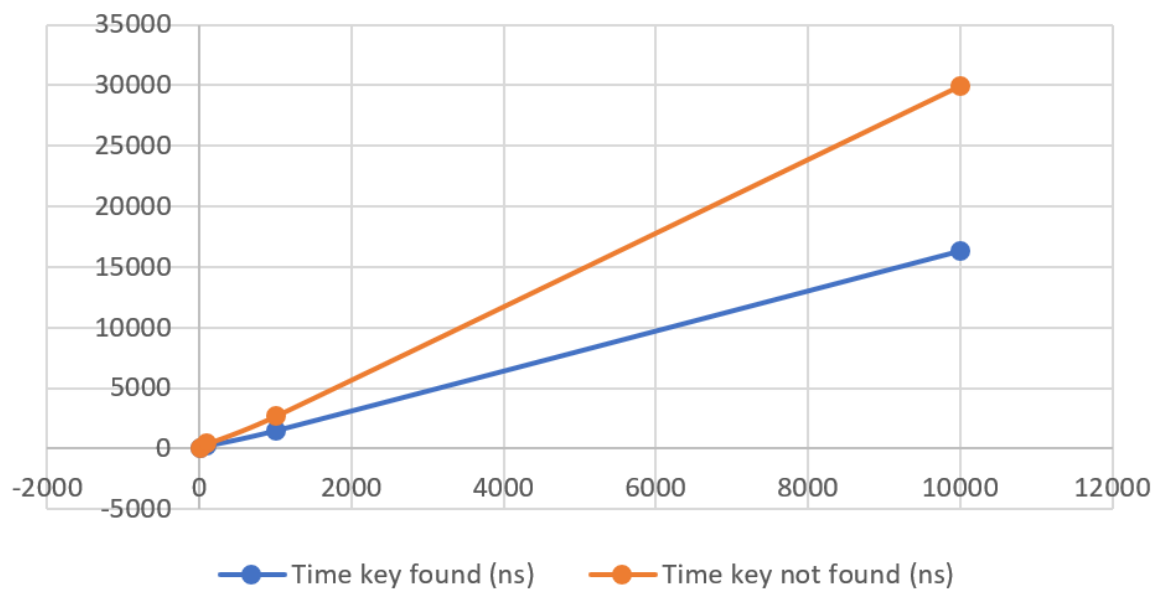
    << " | Key Not Found Avg = " << avg_key_not_found << " nanoseconds" <<
" | Avg_num_of_comparisions = "<<avg_comparisions<<endl;
}
return 0;
}

```

OUTPUT and PLOT:

| N value | Time key found (ns) | Time key not found (ns) | Avg_comp |
|---------|---------------------|-------------------------|----------|
| 10 | 62.9787 | 73.2813 | 14.4 |
| 100 | 248.572 | 411.016 | 133.787 |
| 1000 | 1499.23 | 2685.66 | 1326.35 |
| 10000 | 16367.5 | 29984.5 | 13261.4 |

Chart Title



3. *The input records are sorted based on keys.*

ALGORITHM (BINARY SEARCH):

f. **Initialize pointers:**

- i. Set low = 0 (starting index).
- ii. Set high = n - 1 (ending index), where n is the number of records.

g. **Repeat the following steps while low <= high:**

- i. Calculate the middle index: $\text{mid} = (\text{low} + \text{high}) / 2$.
- ii. Compare the middle element with the key:
 1. If the middle element is **equal** to the key, return the index mid (key found).
 2. If the middle element is **less than** the key, set $\text{low} = \text{mid} + 1$ (search in the right half).
 3. If the middle element is **greater than** the key, set $\text{high} = \text{mid} - 1$ (search in the left half).

h. **End the search:**

- i. If the key is not found and $\text{low} > \text{high}$, return -1 (key not found).

PROGRAM CODE:

```
#include <bits/stdc++.h>
using namespace std;
using namespace std::chrono;

pair<int,int> binarySearch(vector<int> &records, int key) {
    int comp = 0;
    int low = 0;
    int high = records.size() - 1;
    while (low <= high) {
        comp++;
        int mid = (low + high) >> 1;
        if (records[mid] == key) return {mid,comp};
        else if (records[mid] > key) high = mid - 1;
        else low = mid + 1;
    }
    return {-1,comp};
}

int main() {
```

```

srand(time(NULL));

for (int k = 10; k <= 10000; k *= 10) {
    set<int> records;
    unordered_set<int> search_string;

    while (records.size() < k) {
        int random = rand() % (5 * k);
        records.insert(random);
        search_string.insert(random);
    }

    while (search_string.size() < ((3 * k) >> 1)) {
        int random = (5 * k) + (rand() % (5 * k));
        search_string.insert(random);
    }

    vector<int> record(records.begin(), records.end());
    vector<int> search_strings(search_string.begin(),
search_string.end());
    random_shuffle(search_strings.begin(), search_strings.end());

    double time_key_found = 0;
    double time_key_not_found = 0;
    int key_found = 0, key_not_found = 0;
    double avg_comp = 0;

    int num_trials = (k == 10000) ? 1000 : (k == 1000) ? 10000 : 100000;

    for (int trial = 0; trial < num_trials; trial++) {
        for (int i = 0; i < search_strings.size(); i++) {
            auto start = high_resolution_clock::now();
            pair<int,int> p;
            p = binarySearch(record, search_strings[i]);
            auto end = high_resolution_clock::now();
            auto time = duration_cast<nanoseconds>(end - start);
            int f = p.first;
            avg_comp += p.second;
            if (f == -1) {
                time_key_not_found += time.count();
                key_not_found++;
            } else {
                time_key_found += time.count();
                key_found++;
            }
        }
    }
}

```



```

    double avg_key_found = (key_found > 0) ? time_key_found / key_found :
0;
    double avg_key_not_found = (key_not_found > 0) ? time_key_not_found /
key_not_found : 0;
    avg_comp/=(key_found+key_not_found);
    cout << "N = " << k
        << " | Key Found Avg = " << avg_key_found << " nanoseconds"
        << " | Key Not Found Avg = " << avg_key_not_found << "
nanoseconds"
        << " | Avg_comp = "<<avg_comp<<" nanoseconds"
        << endl;
}
return 0;
}

```

OUTPUT and PLOT:

| N value | Time key found (ns) | Time key not found (ns) | Avg_comp |
|---------|---------------------|-------------------------|----------|
| 10 | 67.9453 | 73.5278 | 3.26667 |
| 100 | 97.7511 | 99.2095 | 6.2 |
| 1000 | 144.813 | 124.285 | 9.32467 |
| 10000 | 204.676 | 130.242 | 12.9087 |

