

## Before we begin

```
cd 00_setup && make  
# Windows users: see setup.md
```

(setup)

# Haskell 101

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- ▶ 101
  - ▶ **Concepts and generalities**
  - ▶ **Syntax overview**
  - ▶ **Data structures**
  - ▶ **Declaring functions**



- ▶ **Project environment**
  - ▶ **Cabal? Stack?**
  - ▶ **Hackage? Stackage?**
  - ▶ **Haskell at Google?**
- ▶ **Advanced stuff**
  - ▶ **Functors?**
  - ▶ **Monads?**
  - ▶ **Monad Transformers?**
  - ▶ **...**

- ▶ **Programming knowledge**
  - ▶ **Imperative programming is enough**
  - ▶ **Functional programming is a plus**

## A programming language

- ▶ General purpose



## A programming language

- ▶ General purpose
- ▶ Purely functional



## A programming language

- ▶ General purpose
- ▶ Purely functional
- ▶ Lazily evaluated





## A programming language

- ▶ General purpose
- ▶ Purely functional
- ▶ Lazily evaluated
- ▶ Strongly statically typed



- ▶ A silver bullet
- ▶ Only for category theorists

- ▶ A silver bullet
- ▶ Only for category theorists
- ▶ Hard!

- ▶ A silver bullet
- ▶ Only for category theorists
- ▶ Hard! Just different...

## ▶ Computation method is function application

```
sum [1 .. 10]
```

(Haskell)

- ▶ Computation method is function application
- ▶ Contrast with variable assignment

```
sum [1 .. 10]
```

(Haskell)

```
int total = 0;  
for (int i = 1; i < 10; i++)  
    total += i;
```

(C++)

- ▶ Computation method is function application
- ▶ Contrast with variable assignment
- ▶ Lambda calculus  $\rightarrow \dots \rightarrow$  Haskell

```
sum [1 .. 10]
```

(Haskell)

```
int total = 0;  
for (int i = 1; i < 10; i++)  
    total += i;
```

(C++)

## ► Similar to math

```
f :: Int -> Int  
f x = x + 1
```

(Haskell)

$$f : \mathbb{Z} \rightarrow \mathbb{Z}$$

$$f(x) = x + 1$$



## ► Similar to math

Math	Haskell
$f(x)$	<code>f x</code>
$f(x, y)$	<code>f x y</code>
$f(g(x))$	<code>f (g x)</code>
$f(g(x), h(y))$	<code>f (g x) (h y)</code>
$f(x)g(y)$	<code>f x * g y</code>

- ▶ Similar to math
- ▶ most common thing  $\Rightarrow$  easiest to type

Math	Haskell
$f(x)$	<code>f x</code>
$f(x, y)$	<code>f x y</code>
$f(g(x))$	<code>f (g x)</code>
$f(g(x), h(y))$	<code>f (g x) (h y)</code>
$f(x)g(y)$	<code>f x * g y</code>

## ▶ No more statement vs expression differences

```
int a = 3;  
int b = 5;  
int c = f(a + b, a + 2 * b);
```

(C++)

## ▶ No more statement vs expression differences

```
1 + 2
```

```
(Haskell)
```

## ▶ No more statement vs expression differences

```
let a = 1  
in a + 2
```

(Haskell)

- ▶ No more statement vs expression differences
- ▶ Textual substitution as **model** for evaluation (reduction)

```
let a = 1  
in  a + 2
```

(Haskell)

```
1 + 2
```

(eval)

- ▶ No more statement vs expression differences
- ▶ Textual substitution as **model** for evaluation (reduction)

```
let a = 1  
in  a + 2
```

(Haskell)

3

(eval)

- ▶ No more statement vs expression differences
- ▶ Textual substitution as **model** for evaluation (reduction)

```
let a = if someBool then 1 else 0
in  a + 2
```

(Haskell)



- ▶ No more statement vs expression differences
- ▶ Textual substitution as **model** for evaluation (reduction)

```
let a = if someBool then 1 else 0  
in a + 2
```

(Haskell)

```
(if someBool then 1 else 0) + 2
```

(eval)

- ▶ No more statement vs expression differences
- ▶ Textual substitution as **model** for evaluation (reduction)

```
let a = if someBool then 1 else 0
in a + (let b = 2 in b)
```

(Haskell)

- ▶ No more statement vs expression differences
- ▶ Textual substitution as **model** for evaluation (reduction)

```
let a = if someBool then 1 else 0  
in a + (let b = 2 in b)
```

(Haskell)

```
(if someBool then 1 else 0) + (let b = 2 in b)
```

(eval)

- ▶ No more statement vs expression differences
- ▶ Textual substitution as **model** for evaluation (reduction)

```
let a = if someBool then 1 else 0  
in a + (let b = 2 in b)
```

(Haskell)

```
(if someBool then 1 else 0) + 2
```

(eval)

- ▶ No more statement vs expression differences
- ▶ Textual substitution as **model** for evaluation (reduction)

```
let offset = case color of
    Red    -> 0
    Green  -> 8
    Blue   -> 16
in baseValue + offset
```

(Haskell)

► Do we have variables?

```
let a = 3  
in  a = a + 1
```

(Haskell)

## ► Do we have variables?

```
let a = 3  
in  a = a + 1
```

(Haskell)

```
3 = 3 + 1
```

(eval)

## ► Do we have variables?

```
let a = 3  
in  a = a + 1
```

(Haskell)

```
3 = 4 -- this is bad
```

(eval)



- ▶ Do we have variables?
- ▶ **No:** Everything is immutable

```
let a = 3  
in a = a + 1 -- compile error
```

(Haskell)

```
3 = 4 -- compile error
```

(eval)

- ▶ Do we have variables?
- ▶ **No:** Everything is immutable

```
let a = 3  
in a = a + 1 -- compile error
```

(Haskell)

```
let a = 3  
    b = a + 1  
in b -- this is ok
```

(Haskell)

- ▶ Do we have variables?
- ▶ **No:** Everything is immutable
- ▶ No side effects!

```
numberToWords :: Int -> String
```

(Haskell)

- ▶ Do we have variables?
- ▶ **No**: Everything is immutable
- ▶ No side effects **unless explicitly stated**

```
numberToWords :: Int -> String  
readFile     :: String -> IO String
```

(Haskell)

```
numberToWords :: Int -> String -- pure function  
readFile      :: String -> IO String -- impure function (Haskell)
```

▶  $\exists f :: a \rightarrow \text{IO } a$  (from pure to impure)

▶  $\nexists f :: \text{IO } a \rightarrow a$  (from impure to pure)

▶  $\exists f :: a \rightarrow \text{IO } a$  (from pure to impure)

▶  $\nexists f :: \text{IO } a \rightarrow a$  (from impure to pure)

IO corrupts.

### ► Which order for textual substitution?

```
add x y = x + y
```

(Haskell)

```
add (12 + 8) (20 + 2)
```

(eval)



### ► Which order for textual substitution?

```
add x y = x + y
```

(Haskell)

```
-- arguments first  
add (12 + 8) (20 + 2)
```

```
| -- function body first  
| add (12 + 8) (20 + 2)
```

```
|  
|  
|
```

(eval)

### ► Which order for textual substitution?

```
add x y = x + y
```

(Haskell)

```
-- arguments first  
add (12 + 8) (20 + 2)  
add 20 22  
20 + 22  
42
```

```
| -- function body first  
| add (12 + 8) (20 + 2)  
| (12 + 8) + (20 + 2)  
| 20 + 22  
| 42
```

(eval)

## Let's talk about evaluation order

- ▶ Which order for textual substitution?
- ▶ Are they always equivalent?

```
add x y = x + y
```

(Haskell)

```
-- arguments first  
add (12 + 8) (20 + 2)  
add 20 22  
20 + 22  
42
```

```
| -- function body first  
| add (12 + 8) (20 + 2)  
| (12 + 8) + (20 + 2)  
| 20 + 22  
| 42
```

(eval)

## Let's talk about evaluation order

- ▶ Which order for textual substitution?
- ▶ Are they always equivalent?

```
const x y = x
```

(Haskell)

```
-- arguments first  
const expr1 expr2
```

```
| -- function body first  
| const expr1 expr2
```

```
|  
|  
|
```

(eval)

## Let's talk about evaluation order

- ▶ Which order for textual substitution?
- ▶ Are they always equivalent?

```
const x y = x
```

(Haskell)

```
-- arguments first
```

```
const (40 + 2) (20 + 2)
```

```
const 42 22
```

```
42
```

```
| -- function body first
```

```
| const (40 + 2) (20 + 2)
```

```
| (40 + 2)
```

```
| 42
```

```
|
```

(eval)

## Let's talk about evaluation order

- ▶ Which order for textual substitution?
- ▶ Are they always equivalent?

```
const x y = x
```

(Haskell)

```
-- arguments first
```

```
const (4+2) (error "Crash")
```

```
| -- function body first
```

```
| const (4+2) (error "Crash")
```

```
|  
|  
|
```

(eval)

## Let's talk about evaluation order

- ▶ Which order for textual substitution?
- ▶ Are they always equivalent?

```
const x y = x
```

(Haskell)

```
-- arguments first
```

```
const (4+2) (error "Crash")
```

```
error: Crash
```

```
| -- function body first
```

```
| const (4+2) (error "Crash")
```

```
| (4 + 2)
```

```
| 6
```

```
|
```

(eval)

- ▶ Deferred expression evaluation
- ▶ Not used  $\Rightarrow$  not computed



- ▶ Deferred expression evaluation
- ▶ Not used  $\Rightarrow$  not computed

QUIZ

- ▶ Deferred expression evaluation
- ▶ Not used  $\Rightarrow$  not computed

```
if (obj != nullptr && obj->value > 0)
```

(C++)

- Memory pitfalls

Delayed computations (but escape hatches)

- Memory pitfalls
- IO and parallelism pitfalls

Delayed computations (but escape hatches)

- Memory pitfalls
- IO and parallelism pitfalls
- + Huge optimizations

Equation reduction and short-circuiting

- Memory pitfalls
- IO and parallelism pitfalls
- + Huge optimizations
- + Greater expressivity (e.g. infinite structures)

```
> naturalNumbers = [0,1..]  
> squaredNumbers = map (^2) naturalNumbers  
> take 5 squaredNumbers  
[0,1,4,9,16]
```

(Haskell)

## ► Untyped

```
mov rax, r8  
mov rbx, r9  
add rax, rbx
```

(asm)

- ▶ Untyped
- ▶ Dynamically typed

```
def add(a, b):  
    return a + b
```

(Python)



- ▶ Untyped
- ▶ Dynamically typed
- ▶ Statically typed

```
int add(int a, int b) {  
    return a + b;  
}
```

(C++)

- ▶ Untyped
- ▶ Dynamically typed
- ▶ Statically typed
- ▶ Haskell: strongly statically typed with type inference

```
-- add :: Int -> Int -> Int  
add x y = x + y
```

(Haskell)

- ▶ Read-Eval-Print-Loop interpreter
- ▶ Your new best friend
- ▶ Fast iteration time

- ▶ Read-Eval-Print-Loop interpreter
- ▶ Your new best friend
- ▶ Fast iteration time
- ▶ Desktop calculator

```
Prelude> 2 + 3
```

```
5
```

```
Prelude> sqrt (3 ^ 2 + 4 ^ 2)
```

```
5.0
```

(Haskell)

- ▶ Read-Eval-Print-Loop interpreter
- ▶ Your new best friend
- ▶ Fast iteration time
- ▶ Desktop calculator
- ▶ Type inference using `:type (:t)`
- ▶ . . .

## Basic Haskell types

```
Prelude> :t anInt
anInt :: Int
Prelude> :t aDouble
aDouble :: Double
Prelude> :t 'a'
'a' :: Char
Prelude> :t "this is a string"
"this is a string" :: String -- or [Char]
Prelude> :t [anInt, anInt + 2, 2 * anInt]
[anInt, anInt + 2, 2 * anInt] :: [Int]
Prelude> :t (anInt, aDouble)
(anInt, aDouble) :: (Int, Double)
```

(Haskell)

`f :: Int -> Int -> Int`

`f :: Int -> Int -> Int`

`f x y = x + y`



```
f      ::  Int -> Int -> Int
```

```
f x y = x + y
```

```
f 1 2  ::                               Int
```

```
f      :: Int -> Int -> Int
```

```
f x y = x + y
```

```
f 1 2  :: Int
```

```
3
```

▶ What is the type of `length` below?

```
Prelude> length [1 .. 5]  
5  
Prelude> length "this is some string"  
19
```

(Haskell)

▶ What is the type of `length` below?

▶ `length :: [a] -> Int`

```
Prelude> length [1 .. 5]
```

```
5
```

```
Prelude> length "this is some string"
```

```
19
```

(Haskell)

- ▶ What is the type of `length` below?
- ▶ `length :: [a] -> Int`
- ▶ `a` is a type variable: stand-in for **any** type

```
Prelude> length [1 .. 5]
5
Prelude> length "this is some string"
19
```

(Haskell)

# First letter rule

Context	Capital letter	Lowercase letter
	Fixed type	Type variable
Type	( <code>Int</code> , ...)	( <code>a</code> , ...)
Value	????	Functions, arguments, names, ...

- ▶ Type of a function determine what the function can do?
- ▶ There can be only one  $a \rightarrow b \rightarrow a$  function
- ▶ (modulo assumptions)

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- ▶ `djinn`: Generate Haskell code from a type

- ▶ Type of a function determine what the function can do?
- ▶ There can be only one  $a \rightarrow b \rightarrow a$  function
- ▶ (modulo assumptions)
- ▶ Can we get to the function given the type signature?
- ▶ `djinn`: Generate Haskell code from a type
- ▶ Hoogle, Hayoo

- ▶ Haskell code is immutable
- ▶ But our code needs variables

```
sumList :: [Int] -> Int  
sumList list = ???
```

(Haskell)

- ▶ Haskell code is immutable
- ▶ But our code needs variables
- ▶ Recursion is our friend

```
sumList :: [Int] -> Int
sumList list =
  if null list
  then 0
  else head list + sumList (tail list)
```

(Haskell)

**directory** : 01\_functions

**change** : src/Codelab.hs

(replace `codelab` with implementation)

**check with** : make

```
type Point    = (Int, Int)  -- tuple
```

(Haskell)

```
type Point    = (Int, Int)  -- tuple
type Polygon  = [Point]     -- list
```

(Haskell)

```
type Point    = (Int, Int)  -- tuple
type Polygon  = [Point]     -- list
type Map k v   = [(k, v)]   -- type parameters
```

(Haskell)



What do they consist of?

What do they consist of?

- ▶ No private members...

What do they consist of?

- ▶ No private members...
- ▶ No modifiers...

What do they consist of?

- ▶ No private members...
- ▶ No modifiers...
- ▶ No methods...

What do they consist of?

- ▶ No private members...
- ▶ No modifiers...
- ▶ No methods...
- ▶ Only **constructors**

```
class C {  
    public:  
        C(string name, int age);  
        virtual ~C ();  
        string getName();  
        int getAge();  
        int getAgeIn(int n);  
        void setName(string name);  
        void setAge(int age);  
    private:  
        string name;  
        int age;  
};
```

(C++)

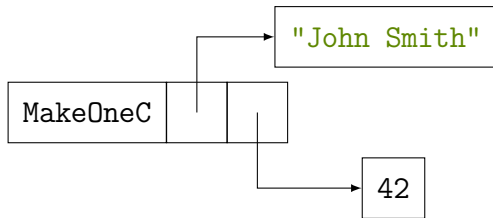
name
age
C()
~C()
getName()
getAge()
getAgeIn()
setName()
setAge()

```
data C = MakeOneC String Int
```

```
person :: C
```

```
person = MakeOneC "John Smith" 42
```

(Haskell)



# The almighty "data" keyword

```
data Bool      = False | True
```

(Haskell)

```
True  :: Bool  
False :: Bool
```

(types)



## The almighty "data" keyword

```
data Bool      = False | True
data None      = None
```

(Haskell)

```
None :: None
```

(types)

# The mighty "data" keyword

```
data Bool      = False | True
data None      = None
data Minutes = Minutes Int
```

(Haskell)

```
Minutes      :: Int -> Minutes
Minutes 42 :: Minutes
```

(types)

Context	Capital letter	Lowercase letter
	Fixed type	Type variable
Type	( <code>Int</code> , ...)	( <code>a</code> , ...)
Value	Constructors ( <code>True</code> , <code>False</code> )	Functions, arguments, names, ...

# Not

```
data Bool = False | True
```

```
not :: Bool -> Bool
```

```
not x = ???
```

(Haskell)

# Not

```
data Bool = False | True
```

```
not :: Bool -> Bool
```

```
not x = if x then False else True
```

(Haskell)

```
data Bool = False | True
```

```
not :: Bool -> Bool
```

```
not x = if x then False else True
```

(Haskell)

Only for built-in type(s)

# Not

```
data Bool = False | True
```

```
not :: Bool -> Bool
```

```
not True  = False
```

```
not False = True
```

(Haskell)

## #PatternMatching

# And

```
data Bool = False | True
```

```
(&&) :: Bool -> Bool -> Bool
```

```
x && y = ???
```

(Haskell)



```
data Bool = False | True
```

```
(&&) :: Bool -> Bool -> Bool
```

```
x && y = if x  
  then (if y then True else False)  
  else False
```

(Haskell)

```
data Bool = False | True
```

```
(&&) :: Bool -> Bool -> Bool
```

```
x && y = if x  
  then (if y then True else False)  
  else False
```

(Haskell)

Only for built-in type(s)

```
data Bool = False | True
```

```
(&&) :: Bool -> Bool -> Bool
```

```
True  && True   = True
```

```
True  && False  = False
```

```
False && True   = False
```

```
False && False  = False
```

(Haskell)

# And

```
data Bool = False | True
```

```
(&&) :: Bool -> Bool -> Bool
```

```
True && True = True
```

```
x    && y    = False
```

(Haskell)

```
data Bool = False | True
```

```
(&&) :: Bool -> Bool -> Bool
```

```
True && True = True
```

```
x    && y    = False
```

(Haskell)

Can you spot a problem?

```
data Bool = False | True
```

```
(&&) :: Bool -> Bool -> Bool
```

```
True && True = True
```

```
x    && y    = False
```

(Haskell)

Eager in the second argument :(

# And

```
data Bool = False | True
```

```
(&&) :: Bool -> Bool -> Bool
```

```
True && y = y
```

```
x    && y = False
```

(Haskell)

# And

```
data Bool = False | True
```

```
(&&) :: Bool -> Bool -> Bool
```

```
True && y = y
```

```
_ && _ = False
```

(Haskell)



# Deconstructors?

```
data Minutes = Minutes Int
```

```
add :: Minutes -> Minutes -> Minutes
```

```
add mx my = ???
```

(Haskell)

# Deconstructors?

```
data Minutes = Minutes Int
```

```
add :: Minutes -> Minutes -> Minutes
```

```
add mx my = mx + my
```

(Haskell)

# Deconstructors?

```
data Minutes = Minutes Int
```

```
add :: Minutes -> Minutes -> Minutes
```

```
add mx my = mx + my
```

(Haskell)

Needs overload for + to work on `Minutes` directly!

# Deconstructors?

```
data Minutes = Minutes Int
```

```
add :: Minutes -> Minutes -> Minutes
```

```
add (Minutes x) (Minutes y) = ???
```

(Haskell)

# Deconstructors?

```
data Minutes = Minutes Int
```

```
add :: Minutes -> Minutes -> Minutes
```

```
add (Minutes x) (Minutes y) = Minutes (x + y)
```

(Haskell)

# Deconstructors?

```
data Minutes = Minutes Int
```

```
add :: Minutes -> Minutes -> Minutes
```

```
add (Minutes x) (Minutes y) = Minutes $ x + y
```

(Haskell)

## Record syntax

```
data User = User String String Int
```

(Haskell)

```
User :: String -> String -> Int -> User
```

(types)

# Record syntax

```
data User = User {  
    userFirstName :: String,  
    userLastName  :: String,  
    userAge       :: Int  
}
```

(Haskell)

```
User      :: String -> String -> Int -> User
```

(types)



## Record syntax

```
data User = User {  
    userFirstName :: String,  
    userLastName  :: String,  
    userAge       :: Int  
}
```

(Haskell)

```
User           :: String -> String -> Int -> User  
userFirstName  :: User -> String  
userLastName   :: User -> String  
userAge        :: User -> Int
```

(types)

**directory** : 02\_datatypes

**change** : src/Codelab.hs

(replace `codelab` with implementation)

**check with** : make

## The almighty "data" keyword. Continued

```
data Bool      = False | True
data None      = None
data Minutes = Minutes Int
```

(Haskell)

## The mighty "data" keyword. Continued

```
data Bool      = False | True
data None      = None
data Minutes   = Minutes Int
data Maybe a   = Nothing | Just a
```

(Haskell)

```
Nothing ::      Maybe a
Just     :: a -> Maybe a
Just 42  ::      Maybe Int
```

(types)

## The mighty "data" keyword. Continued

```
data Bool      = False | True
data None      = None
data Minutes   = Minutes Int
data Maybe a   = Nothing | Just a
data List a    = Nil | Cell a (List a)
```

(Haskell)

```
      Nil ::      List a
      Cell :: a -> List a -> List a
Cell 0 (Cell 1 (Nil)) :: List Int
```

(types)

## The mighty "data" keyword. Continued

```
data Bool      = False | True
data None      = None
data Minutes   = Minutes Int
data Maybe a   = Nothing | Just a
data List a    = Nil | Cell a (List a)
```

(Haskell)

```
Nil :: List a
Cell :: a -> List a -> List a
Cell 0 $ Cell 1 $ Nil :: List Int
```

(types)

## The almighty "data" keyword. Continued

```
data Bool      = False | True
data None      = None
data Minutes   = Minutes Int
data Maybe a   = Nothing | Just a
data List a    = Nil | Cell a (List a)
data [a]       = [] | (a:[a])
```

(Haskell)

```
    [] :: [a]
    (:) :: a -> [a] -> [a]
0 : 1 : [] :: [Int]
```

(types)

## The almighty "data" keyword. Continued

```
data Bool      = False | True
data None      = None
data Minutes   = Minutes Int
data Maybe a   = Nothing | Just a
data List a    = Nil | Cell a (List a)
data [a]       = [] | (a:[a])
```

(Haskell)

```
[] :: [a]
(:) :: a -> [a] -> [a]
[0, 1] :: [Int]
```

(types)



# Length

```
data [a] = [] | (a:[a])
```

```
length :: [a] -> Int
```

```
length l = ???
```

(Haskell)

# Length

```
data [a] = [] | (a:[a])
```

```
length :: [a] -> Int
```

```
length []      = ???
```

```
length (x:xs) = ???
```

(Haskell)

# Length

```
data [a] = [] | (a:[a])
```

```
length :: [a] -> Int
```

```
length [] = 0
```

```
length (x:xs) = ???
```

(Haskell)

```
data [a] = [] | (a:[a])
```

```
length :: [a] -> Int
```

```
length [] = 0
```

```
length (_,xs) = 1 + length xs
```

(Haskell)

## #Recursion

**directory** : 03\_lists

**change** : src/Codelab.hs

(replace `codelab` with implementation)

**check with** : make

# Curried functions, partial application

```
f      :: Int ->   Int -> Int
```

(Haskell)

## Curried functions, partial application

```
f      :: Int -> ( Int -> Int )  
f      :: Int ->   Int -> Int
```

(Haskell)

## Curried functions, partial application

```
f      :: Int -> ( Int -> Int )  
f      :: Int ->   Int -> Int  
f 1    ::           Int -> Int
```

(Haskell)



## Curried functions, partial application

```
f      :: Int -> ( Int -> Int )
```

```
f      :: Int ->   Int -> Int
```

```
f 1    ::           Int -> Int
```

```
(f 1) 2 ::           Int
```

(Haskell)

## Curried functions, partial application

```
f      :: Int -> ( Int -> Int )  
f      :: Int ->   Int -> Int  
f 1    ::           Int -> Int  
f 1 2  ::           Int  
(f 1) 2 ::           Int
```

(Haskell)

??? :: (a -> b) -> [a] -> [b]

??? :: (a -> b) -> [a] -> [b]

(a -> b)    **function from type A to type B**

[a]        **list of values of type A**

[b]        **list of values of type B**

`map` :: (a -> b) -> [a] -> [b]

(a -> b)    **function from type A to type B**

[a]        **list of values of type A**

[b]        **list of values of type B**

```
map  ::  (a -> b) -> [a] -> [b]
```

```
add2 x = x + 2
```

```
map add2 [1, 2, 3] direct call, result [3, 4, 5]
```

```
map (\x -> x + 2) [1, 2, 3] lambda function (anonymous)
```

`map` :: (a -> b) -> [a] -> [b]

?????? :: (a -> Bool) -> [a] -> [a]

```
map    :: (a -> b) -> [a] -> [b]
filter :: (a -> Bool) -> [a] -> [a]
```



```
map    :: (a -> b) -> [a] -> [b]
filter :: (a -> Bool) -> [a] -> [a]
(.)    :: (b -> c) -> (a -> b) -> (a -> c)
```

```
map    :: (a -> b) -> [a] -> [b]
filter :: (a -> Bool) -> [a] -> [a]
(.)    :: (b -> c) -> (a -> b) -> (a -> c)
```

$$(f \circ g)(x) = f(g(x))$$

`map` :: (a -> b) -> [a] -> [b]

`filter` :: (a -> Bool) -> [a] -> [a]

`(.)` :: (b -> c) -> (a -> b) -> (a -> c)

`show` :: Stuff -> String

`length` :: String -> Int

`length . show` :: Stuff -> Int

```
map    :: (a -> b) -> [a] -> [b]
filter :: (a -> Bool) -> [a] -> [a]
(.)    :: (b -> c) -> (a -> b) -> (a -> c)
```

```
cat input | grep token | sed stuff | tee output
```

## Quiz with a vengeance!

????? :: (a -> b -> a) -> a -> [b] -> a

## Quiz with a vengeance!

????? :: (a -> b -> a) -> a -> [b] -> a

(a -> b -> a)    **combines accumulator and value**

a                **initial accumulator**

[b]              **list of values**

a                **result**

## Quiz with a vengeance!

`foldl1 :: (a -> b -> a) -> a -> [b] -> a`

`(a -> b -> a)` **combines accumulator and value**

`a` **initial accumulator**

`[b]` **list of values**

`a` **result**

## Quiz with a vengeance!

`foldl` :: (a -> b -> a) -> a -> [b] -> a

(a -> b -> a)    **combines accumulator and value**

a                **initial accumulator**

[b]              **list of values**

a                **result**

**"reduce"**



**directory** : 04\_abstractions

**change** : src/Codelab.hs

(replace `codelab` with implementation)

**check with** : make

Questions?

- ▶ [tryhaskell.org](https://tryhaskell.org)
- ▶ [learnyouahaskell.com](https://learnyouahaskell.com)
- ▶ [book.realworldhaskell.org](https://book.realworldhaskell.org)
- ▶ [haskellbook.com](https://haskellbook.com)
- ▶ [haskell.org/hoogle/](https://haskell.org/hoogle/)
- ▶ Pragmatic types: types vs tests
- ▶ Why functional programming matters

**directory** : 05\_maybe

**change** : src/Codelab.hs

(replace `codelab` with implementation)

**check with** : make

**directory** : 06\_rps

**change** : src/Codelab.hs

(replace `codelab` with implementation)

**check with** : make

Questions?