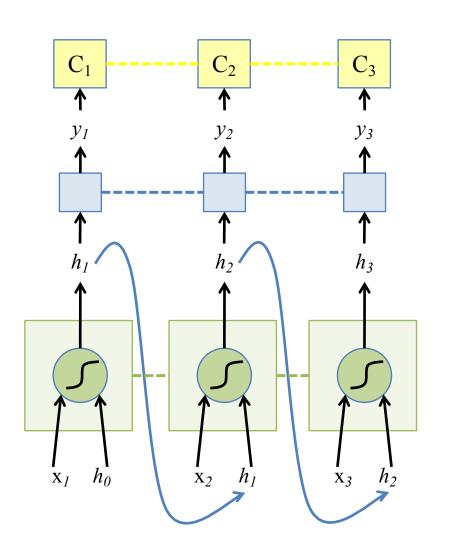
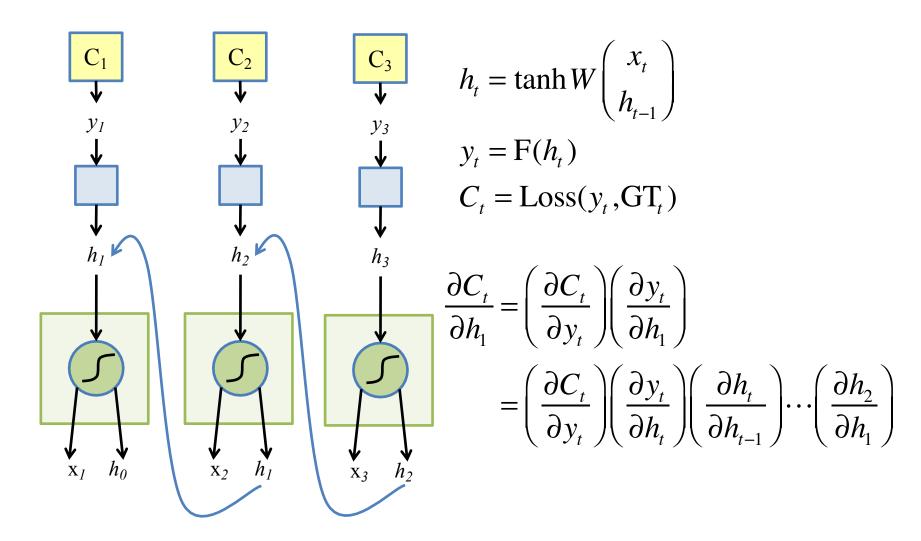
The Vanilla RNN Forward



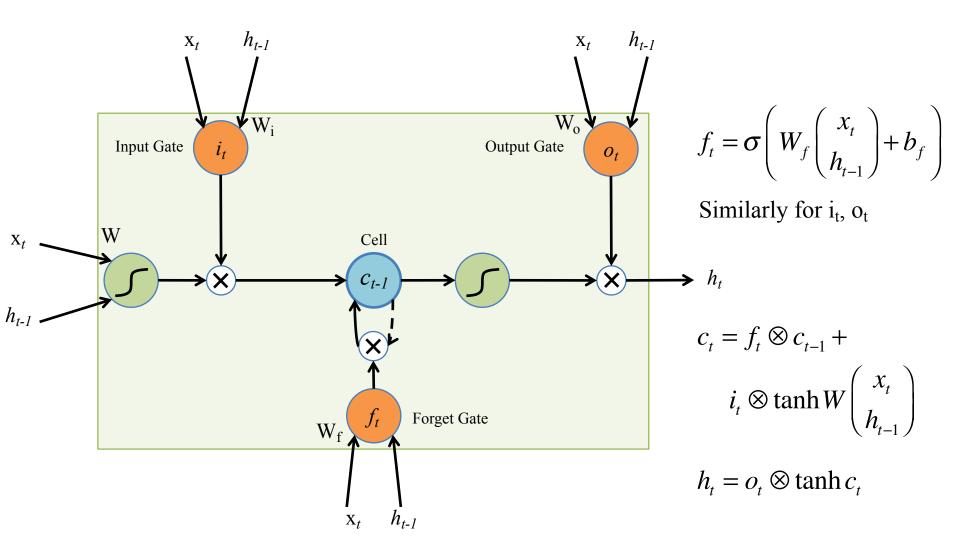
$$h_{t} = \tanh W \begin{pmatrix} x_{t} \\ h_{t-1} \end{pmatrix}$$
$$y_{t} = F(h_{t})$$
$$C_{t} = Loss(y_{t}, GT_{t})$$

---- indicates shared weights

The Vanilla RNN Backward



The Popular LSTM Cell



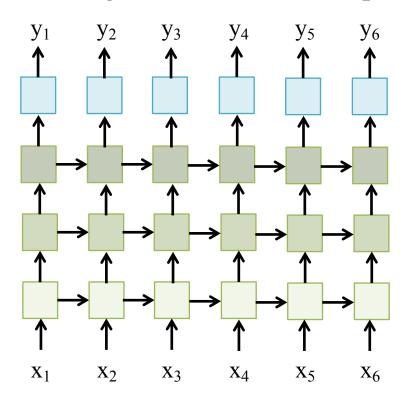
^{*} Dashed line indicates time-lag

LSTM – Forward/Backward

Go To: http://arunmallya.github.io/writeups/nn/lstm/index.html#/

Multi-layer RNNs

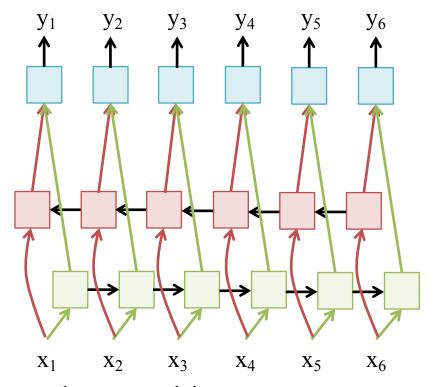
• We can of course design RNNs with multiple hidden layers



• Think exotic: Skip connections across layers, across time, ...

Bi-directional RNNs

• RNNs can process the input sequence in forward and in the reverse direction

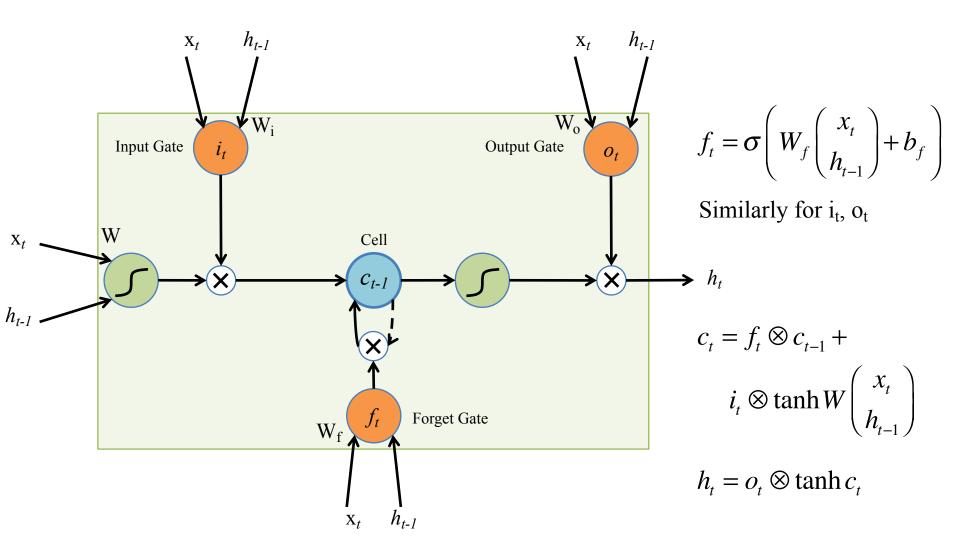


Popular in speech recognition

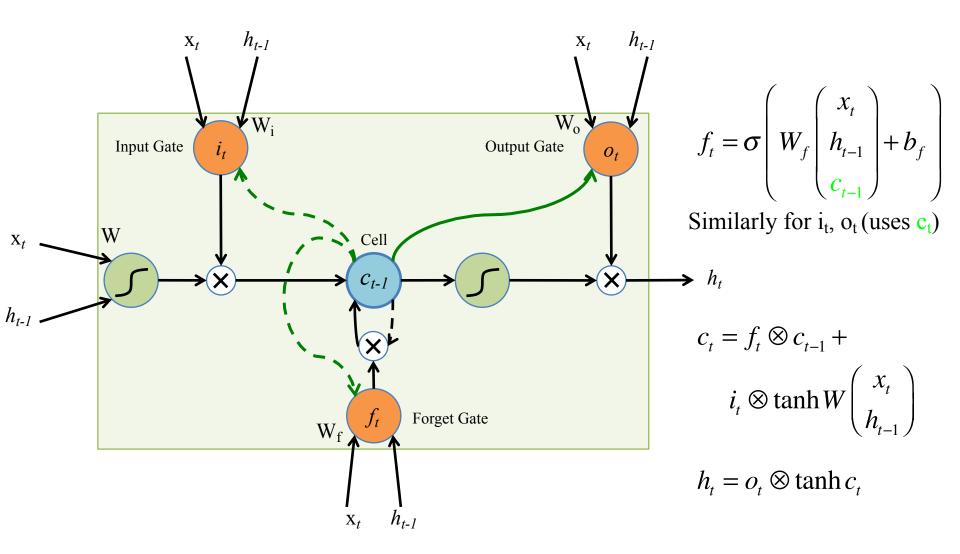
Recap

- RNNs allow for processing of variable length inputs and outputs by maintaining state information across time steps
- Various Input-Output scenarios are possible (Single/Multiple)
- RNNs can be stacked, or bi-directional
- Vanilla RNNs are improved upon by LSTMs which address the vanishing gradient problem through the CEC
- Exploding gradients are handled by gradient clipping

The Popular LSTM Cell

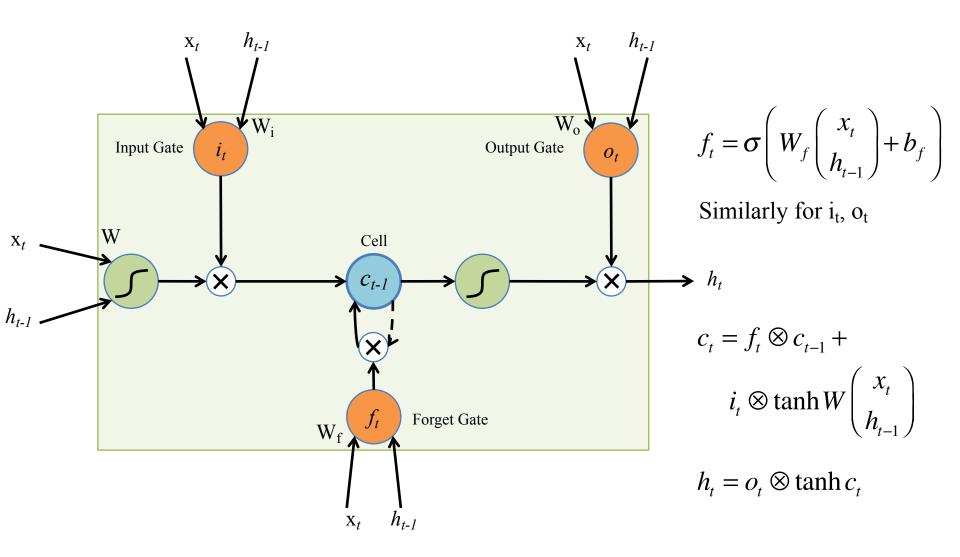


Extension I: Peephole LSTM



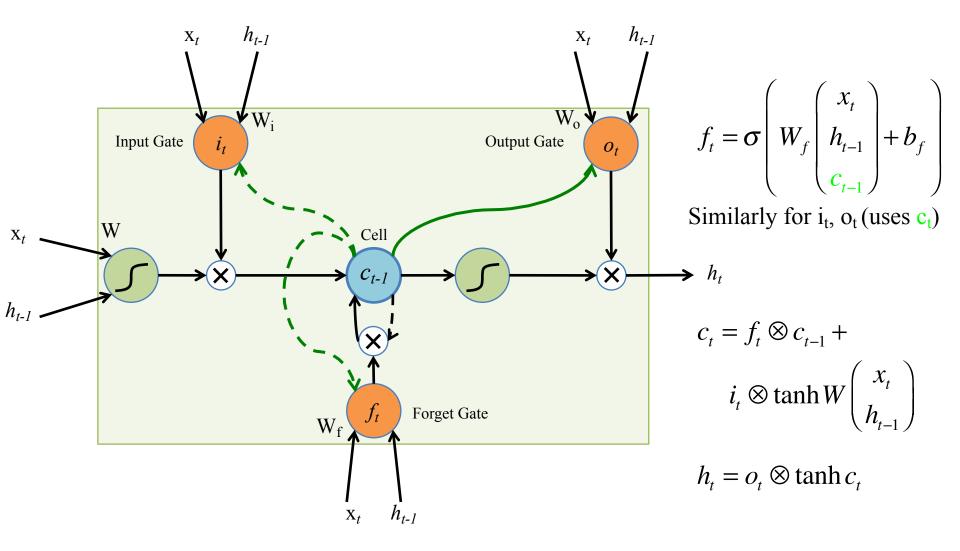
^{*} Dashed line indicates time-lag

The Popular LSTM Cell



¹⁰

Extension I: Peephole LSTM



¹¹

Peephole LSTM

- Gates can only see the output from the previous time step, which is close to 0 if the output gate is closed. However, these gates control the CEC cell.
- Helped the LSTM learn better timing for the problems tested –
 Spike timing and Counting spike time delays

Other minor variants

Coupled Input and Forget Gate

$$f_t = 1 - i_t$$

• Full Gate Recurrence

$$f_t = \sigma \begin{pmatrix} x_t \\ h_{t-1} \\ c_{t-1} \\ \vdots \\ f_{t-1} \\ f_{t-1} \\ o_{t-1} \end{pmatrix} + b_f$$

LSTM: A Search Space Odyssey

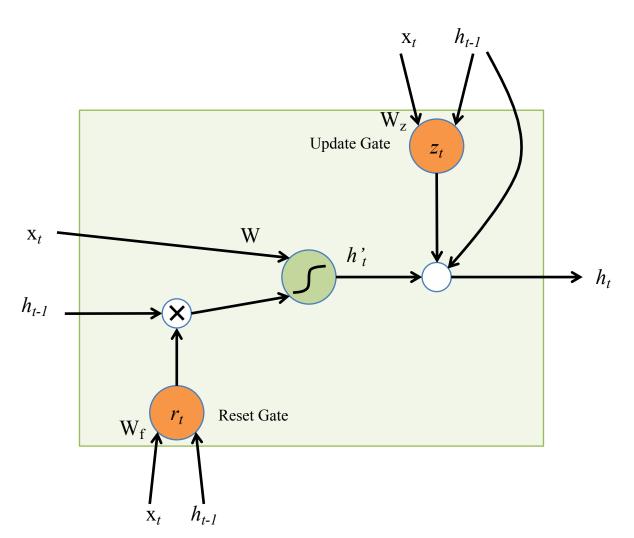
- Tested the following variants, using Peephole LSTM as standard:
 - 1. No Input Gate (NIG)
 - 2. No Forget Gate (NFG)
 - 3. No Output Gate (NOG)
 - 4. No Input Activation Function (NIAF)
 - 5. No Output Activation Function (NOAF)
 - 6. No Peepholes (NP)
 - 7. Coupled Input and Forget Gate (CIFG)
 - 8. Full Gate Recurrence (FGR)
- On the tasks of:
 - Timit Speech Recognition: Audio frame to 1 of 61 phonemes
 - IAM Online Handwriting Recognition: Sketch to characters
 - JSB Chorales: Next-step music frame prediction

LSTM: A Search Space Odyssey

- The standard LSTM performed reasonably well on multiple datasets and none of the modifications significantly improved the performance
- Coupling gates and removing peephole connections simplified the LSTM without hurting performance much
- The forget gate and output activation are crucial
- Found interaction between learning rate and network size to be minimal – indicates calibration can be done using a small network first

Gated Recurrent Unit (GRU)

- A very simplified version of the LSTM
 - Merges forget and input gate into a single 'update' gate
 - Merges cell and hidden state
- Has fewer parameters than an LSTM and has been shown to outperform LSTM on some tasks

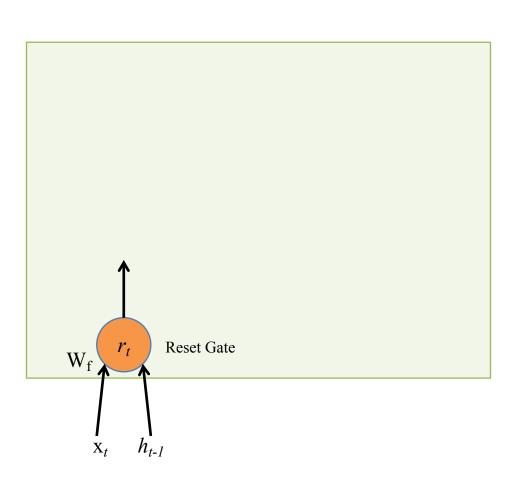


$$r_{t} = \sigma \left(W_{r} \begin{pmatrix} x_{t} \\ h_{t-1} \end{pmatrix} + b_{f} \right)$$

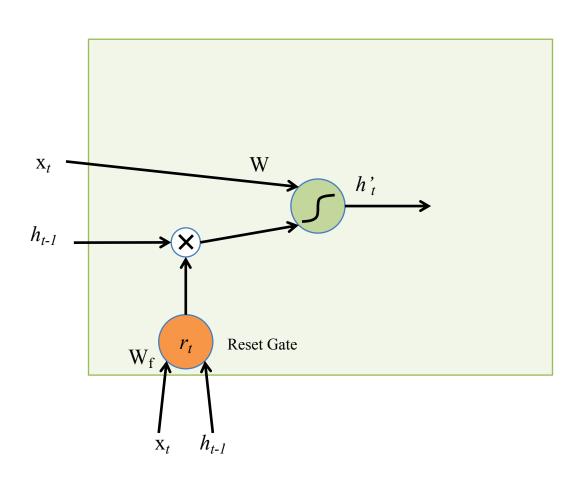
$$h'_{t} = \tanh W \begin{pmatrix} x_{t} \\ r_{t} \otimes h_{t-1} \end{pmatrix}$$

$$z_{t} = \sigma \left(W_{z} \begin{pmatrix} x_{t} \\ h_{t-1} \end{pmatrix} + b_{f} \right)$$

$$h_t = (1 - z_t) \otimes h_{t-1} + z_t \otimes h'_t$$

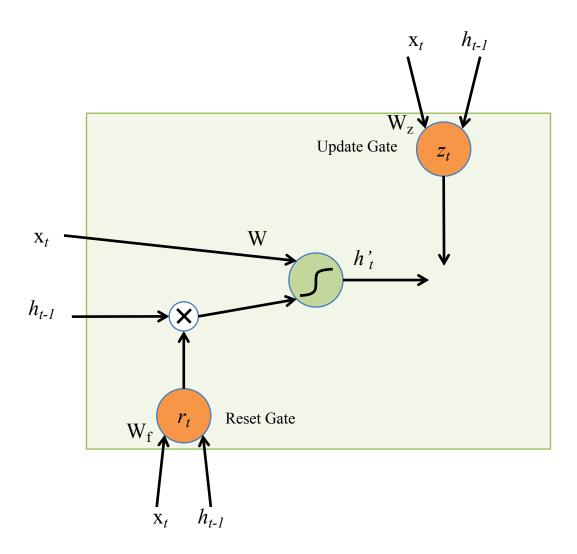


$$r_{t} = \sigma \left(W_{r} \begin{pmatrix} x_{t} \\ h_{t-1} \end{pmatrix} + b_{f} \right)$$



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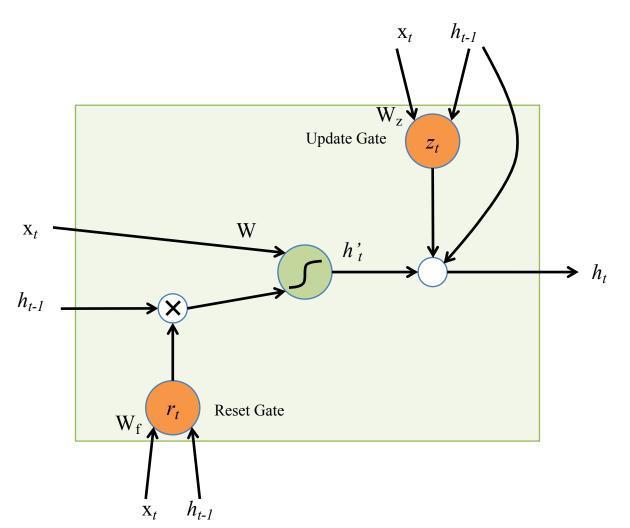
$$h'_{t} = \tanh W \begin{pmatrix} x_{t} \\ r_{t} \otimes h_{t-1} \end{pmatrix}$$



$$r_{t} = \sigma \left(W_{r} \begin{pmatrix} x_{t} \\ h_{t-1} \end{pmatrix} + b_{f} \right)$$

$$h'_{t} = \tanh W \begin{pmatrix} x_{t} \\ r_{t} \otimes h_{t-1} \end{pmatrix}$$

$$z_{t} = \sigma \left(W_{z} \begin{pmatrix} x_{t} \\ h_{t-1} \end{pmatrix} + b_{f} \right)$$



$$r_{t} = \sigma \left(W_{r} \begin{pmatrix} x_{t} \\ h_{t-1} \end{pmatrix} + b_{f} \right)$$

$$h'_{t} = \tanh W \begin{pmatrix} x_{t} \\ r_{t} \otimes h_{t-1} \end{pmatrix}$$

$$z_{t} = \sigma \left(W_{z} \begin{pmatrix} x_{t} \\ h_{t-1} \end{pmatrix} + b_{f} \right)$$

$$h_t = (1 - z_t) \otimes h_{t-1} + z_t \otimes h'_t$$

An Empirical Exploration of Recurrent Network Architectures

- Given the rather ad-hoc design of the LSTM, the authors try to determine if the architecture of the LSTM is optimal
- They use an evolutionary search for better architectures

Evolutionary Architecture Search

- A list of top-100 architectures so far is maintained, initialized with the LSTM and the GRU
- The GRU is considered as the baseline to beat
- New architectures are proposed, and retained based on performance ratio with GRU
- All architectures are evaluated on 3 problems
 - Arithmetic: Compute digits of sum or difference of two numbers provided as inputs. Inputs have distractors to increase difficulty 3e36d9-h1h39f94eeh43keg3c = 3369 13994433 = -13991064
 - XML Modeling: Predict next character in valid XML modeling
 - Penn Tree-Bank Language Modeling: Predict distributions over words

Evolutionary Architecture Search

At each step

- Select 1 architecture at random, evaluate on 20 randomly chosen hyperparameter settings.
- Alternatively, propose a new architecture by mutating an existing one.
 Choose probability p from [0,1] uniformly and apply a transformation to each node with probability p
 - If node is a non-linearity, replace with $\{tanh(x), sigmoid(x), ReLU(x), Linear(0, x), Linear(1, x), Linear(0, 9, x), Linear(1, 1, x)\}$
 - If node is an elementwise op, replace with {multiplication, addition, subtraction}
 - Insert random activation function between node and one of its parents
 - Replace node with one of its ancestors (remove node)
 - Randomly select a node (node A). Replace the current node with either the sum, product, or difference of a random ancestor of the current node and a random ancestor of A.
- Add architecture to list based on minimum relative accuracy wrt GRU on 3 different tasks

Evolutionary Architecture Search

- 3 novel architectures are presented in the paper
- Very similar to GRU, but slightly outperform it
- LSTM initialized with a large positive forget gate bias outperformed both the basic LSTM and the GRU!

LSTM initialized with large positive forget gate bias?

• Recall

$$f_{t} = \sigma \left(W_{f} \begin{pmatrix} x_{t} \\ h_{t-1} \end{pmatrix} + b_{f} \right)$$

$$c_{t} = f_{t} \otimes c_{t-1} + i_{t} \otimes \tanh W \begin{pmatrix} x_{t} \\ h_{t-1} \end{pmatrix}$$

$$\delta c_{t-1} = \delta c_{t} \otimes f_{t}$$

- Gradients will vanish if f is close to 0. Using a large positive bias ensures that f has values close to 1, especially when training begins
- Helps learn long-range dependencies
- Originally stated in <u>Learning to forget: Continual prediction with LSTM</u>, <u>Gers et al.</u>, 2000, but forgotten over time

Summary

- LSTMs can be modified with Peephole Connections, Full Gate Recurrence, etc. based on the specific task at hand
- Architectures like the GRU have fewer parameters than the LSTM and might perform better
- An LSTM with large positive forget gate bias works best!

Other Useful Resources / References

- http://cs231n.stanford.edu/slides/winter1516 lecture10.pdf
- http://www.cs.toronto.edu/~rgrosse/csc321/lec10.pdf
- R. Pascanu, T. Mikolov, and Y. Bengio, On the difficulty of training recurrent neural networks, ICML 2013
- S. Hochreiter, and J. Schmidhuber, <u>Long short-term memory</u>, Neural computation, 1997 9(8), pp.1735-1780
- F.A. Gers, and J. Schmidhuber, <u>Recurrent nets that time and count</u>, IJCNN 2000
- K. Greff, R.K. Srivastava, J. Koutník, B.R. Steunebrink, and J. Schmidhuber, <u>LSTM: A search space odyssey</u>, IEEE transactions on neural networks and learning systems, 2016
- K. Cho, B. Van Merrienboer, C. Gulcehre, D. Bahdanau, F. Bougares, H. Schwenk, and Y. Bengio, <u>Learning phrase representations using RNN encoder-decoder for statistical machine translation</u>, ACL 2014
- R. Jozefowicz, W. Zaremba, and I. Sutskever, <u>An empirical exploration of recurrent network architectures</u>, JMLR 2015