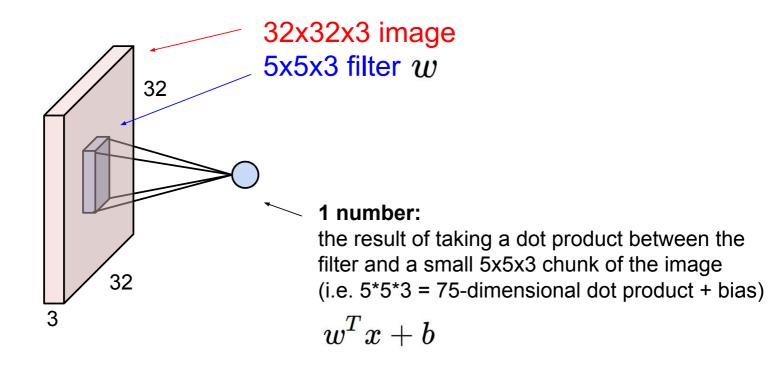
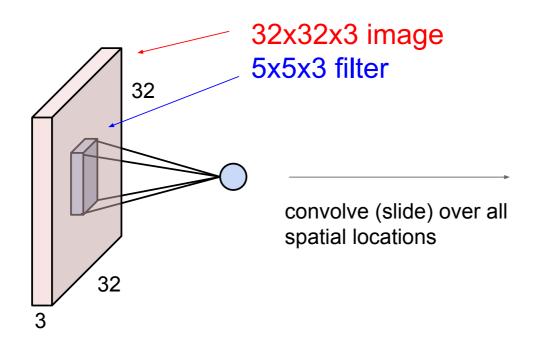
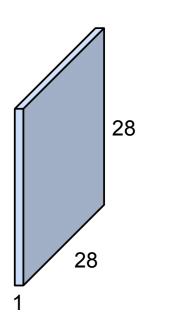
Convolution Layer



Convolution Layer

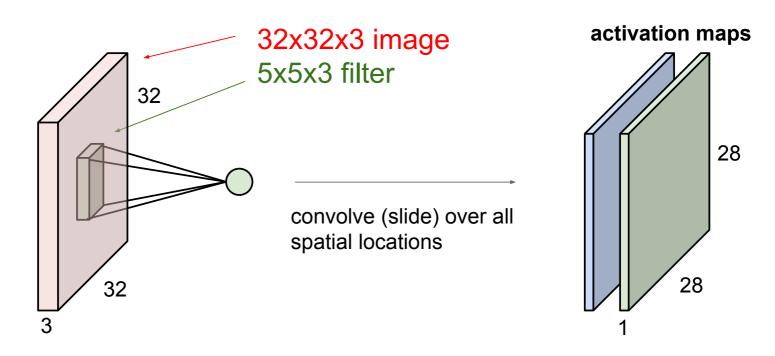


activation map

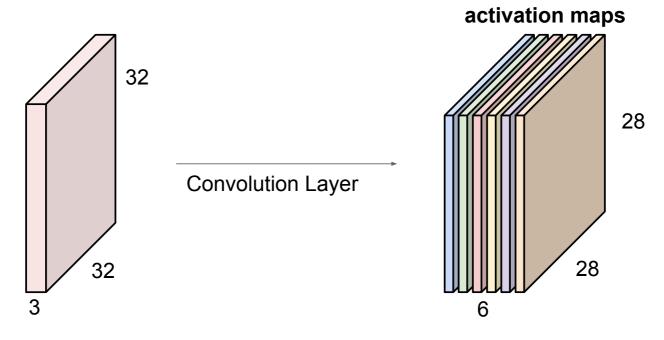


Convolution Layer

consider a second, green filter

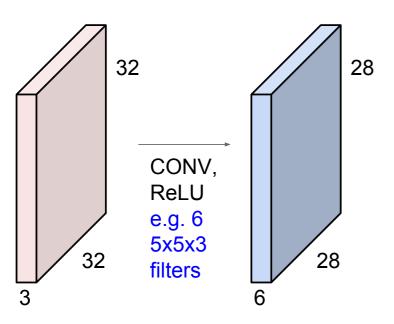


For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:

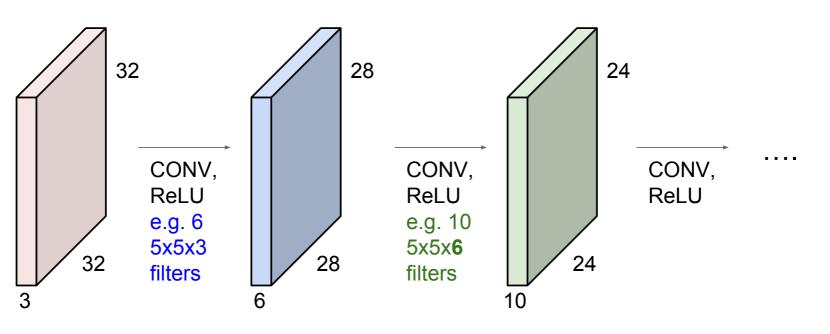


We stack these up to get a "new image" of size 28x28x6!

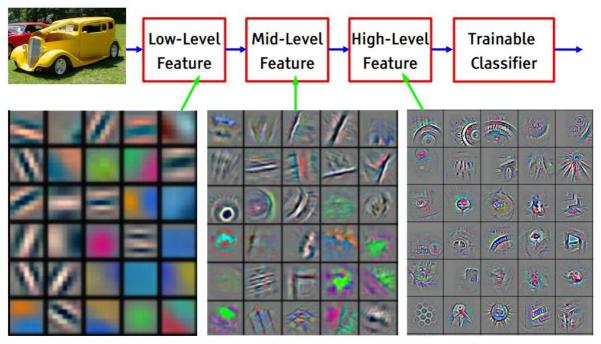
Preview: ConvNet is a sequence of Convolution Layers, interspersed with activation functions



Preview: ConvNet is a sequence of Convolutional Layers, interspersed with activation functions

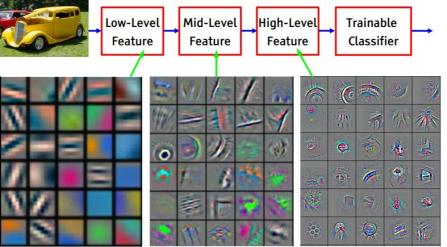


Preview

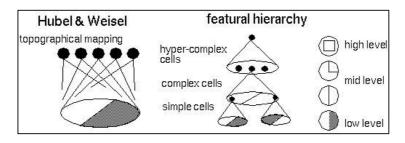


Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

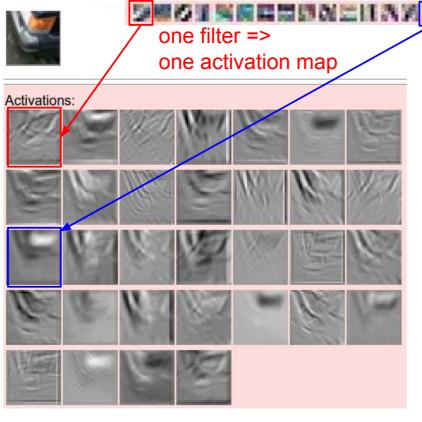
Preview



Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]



[From recent Yann LeCun slides]

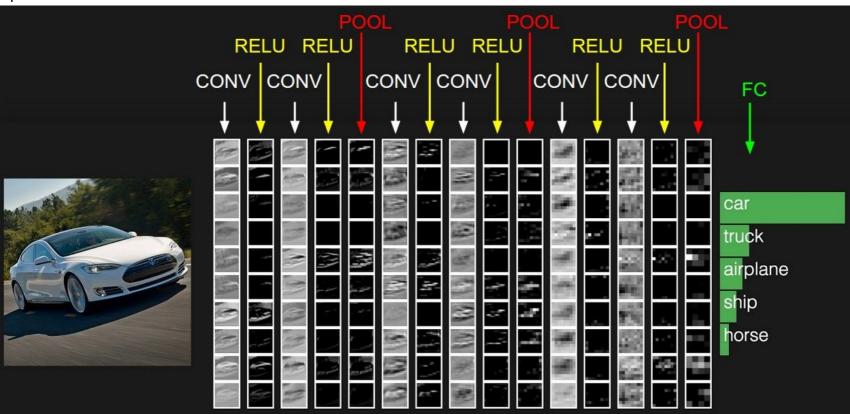


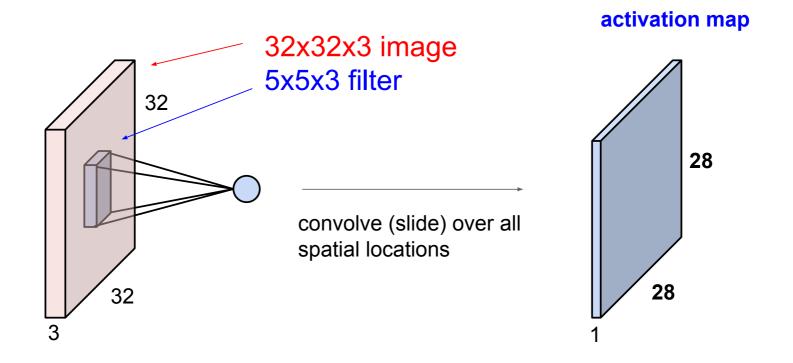
example 5x5 filters (32 total)

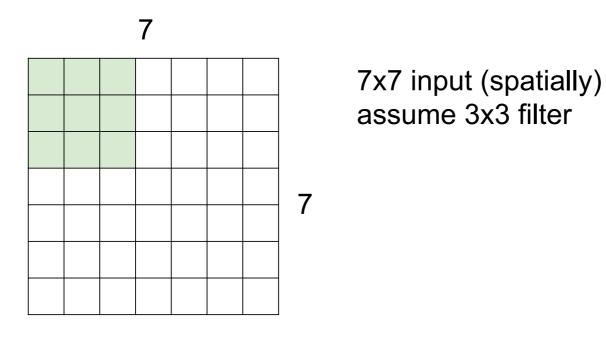
We call the layer convolutional because it is related to convolution of two signals:

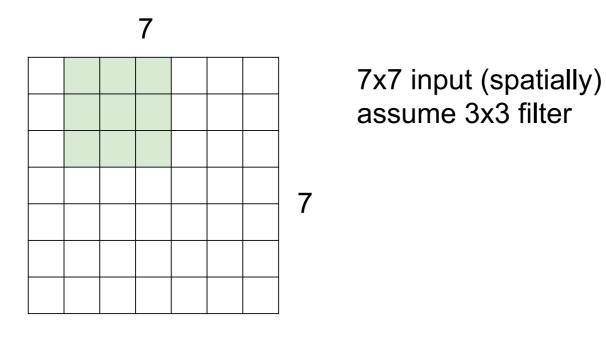
$$f[x,y] * g[x,y] = \sum_{n_1 = -\infty}^{\infty} \sum_{n_2 = -\infty}^{\infty} f[n_1, n_2] \cdot g[x - n_1, y - n_2]$$

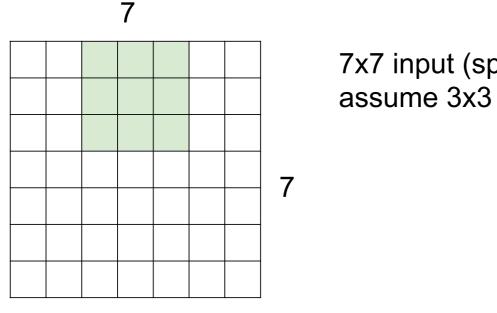
elementwise multiplication and sum of a filter and the signal (image) preview:



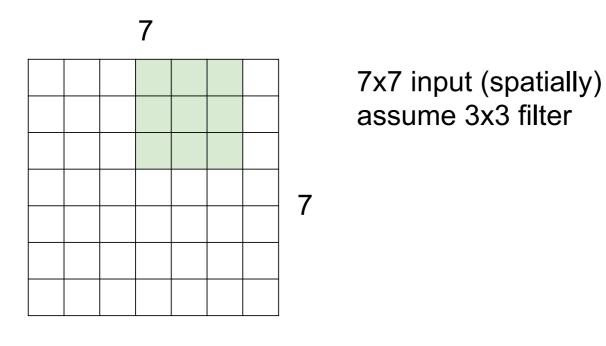


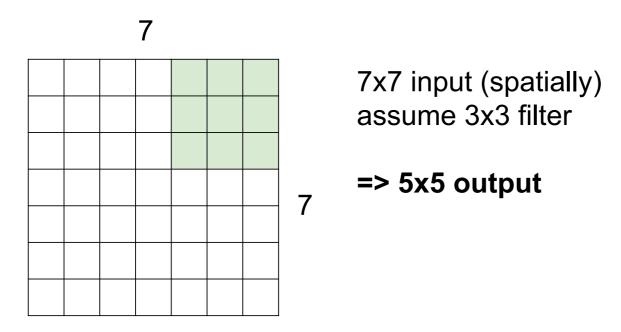


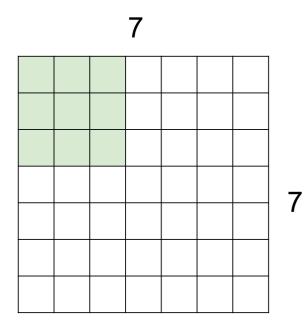




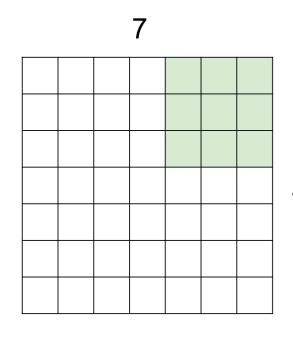
7x7 input (spatially) assume 3x3 filter



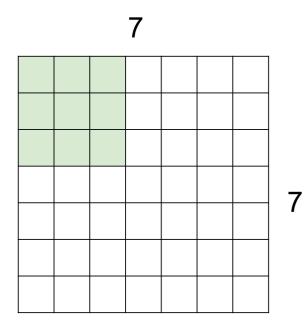




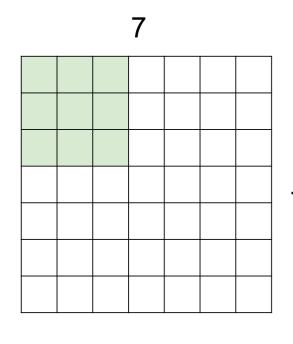
7x7 input (spatially) assume 3x3 filter applied with stride 2



7x7 input (spatially) assume 3x3 filter applied with stride 2 => 3x3 output!



7x7 input (spatially) assume 3x3 filter applied with stride 3?



7x7 input (spatially) assume 3x3 filter applied with stride 3?

doesn't fit! cannot apply 3x3 filter on 7x7 input with stride 3.

N

	F		
F			

Output size: (N - F) / stride + 1

e.g. N = 7, F = 3: stride $1 \Rightarrow (7 - 3)/1 + 1 = 5$ stride $2 \Rightarrow (7 - 3)/2 + 1 = 3$ stride $3 \Rightarrow (7 - 3)/3 + 1 = 2.33$:

In practice: Common to zero pad the border

0	0	0	0	0	0		
0							
0							
0							
0							

e.g. input 7x7
3x3 filter, applied with stride 1
pad with 1 pixel border => what is the output?

```
(recall:)
(N - F) / stride + 1
```

In practice: Common to zero pad the border

0	0	0	0	0	0		
0							
0							
0							
0							

e.g. input 7x7
3x3 filter, applied with stride 1
pad with 1 pixel border => what is the output?

7x7 output!

In practice: Common to zero pad the border

0	0	0	0	0	0		
0							
0							
0							
0							

e.g. input 7x7
3x3 filter, applied with stride 1
pad with 1 pixel border => what is the output?

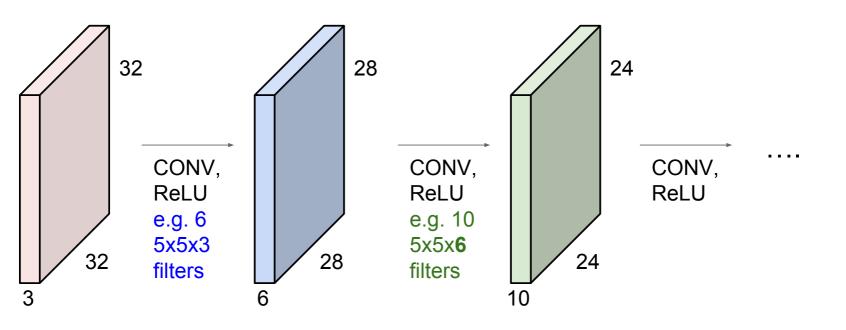
7x7 output!

in general, common to see CONV layers with stride 1, filters of size FxF, and zero-padding with (F-1)/2. (will preserve size spatially)

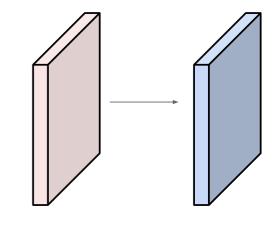
e.g. F = 3 => zero pad with 1 F = 5 => zero pad with 2 F = 7 => zero pad with 3

Remember back to...

E.g. 32x32 input convolved repeatedly with 5x5 filters shrinks volumes spatially! (32 -> 28 -> 24 ...). Shrinking too fast is not good, doesn't work well.



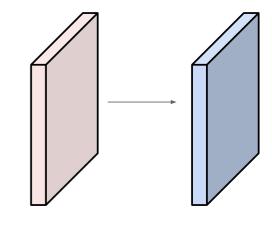
Input volume: **32x32x3**10 5x5 filters with stride 1, pad 2



Output volume size: ?

Input volume: 32x32x3

10 5x5 filters with stride 1, pad 2

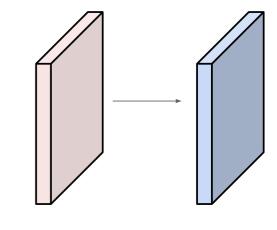


Output volume size:

$$(32+2*2-5)/1+1 = 32$$
 spatially, so

32x32x10

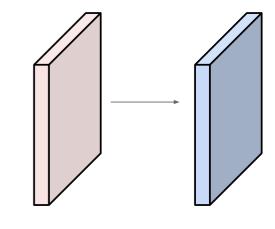
Input volume: **32x32x3**10 5x5 filters with stride 1, pad 2



Number of parameters in this layer?

Input volume: 32x32x3

10 5x5 filters with stride 1, pad 2



(+1 for bias)

Number of parameters in this layer? each filter has 5*5*3 + 1 = 76 params

=> 76*10 = **760**

Summary. To summarize, the Conv Layer:

- Accepts a volume of size $W_1 \times H_1 \times D_1$
- · Requires four hyperparameters:
 - Number of filters K,
 - their spatial extent F,
 - the stride S,
 - \circ the amount of zero padding P.
- Produces a volume of size $W_2 \times H_2 \times D_2$ where:
 - $W_2 = (W_1 F + 2P)/S + 1$
 - $H_2 = (H_1 F + 2P)/S + 1$ (i.e. width and height are computed equally by symmetry)
 - $D_2 = K$
- With parameter sharing, it introduces $F \cdot F \cdot D_1$ weights per filter, for a total of $(F \cdot F \cdot D_1) \cdot K$ weights and K biases.
- In the output volume, the d-th depth slice (of size $W_2 \times H_2$) is the result of performing a valid convolution of the d-th filter over the input volume with a stride of S, and then offset by d-th bias.

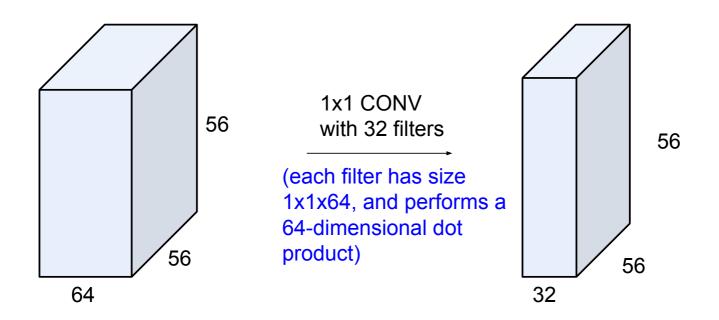
Common settings:

Summary. To summarize, the Conv Layer:

- Accepts a volume of size $W_1 imes H_1 imes D_1$
- Requires four hyperparameters:
 - Number of filters K,
 - \circ their spatial extent F,
 - the stride S,
 - \circ the amount of zero padding P.

- K = (powers of 2, e.g. 32, 64, 128, 512)
 - F = 3, S = 1, P = 1
 - F = 5, S = 1, P = 2
 - F = 5, S = 2, P = ? (whatever fits)
 - F = 1, S = 1, P = 0
- Produces a volume of size $W_2 \times H_2 \times D_2$ where:
 - $W_2 = (W_1 F + 2P)/S + 1$
 - $H_2 = (H_1 F + 2P)/S + 1$ (i.e. width and height are computed equally by symmetry)
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(btw, 1x1 convolution layers make perfect sense)





Summary. To summarize, the Conv Layer:

- Accepts a volume of size $W_1 imes H_1 imes D_1$
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 - Number of filters K,
 - \circ their spatial extent F,
 - the stride S.
 - the amount of zero padding P.

class torch.nn.Conv2d(in_channels, out_channels, kernel_size, stride=1, padding=0, dilation=1, groups=1, bias=True) [source]

Applies a 2D convolution over an input signal composed of several input planes.

In the simplest case, the output value of the layer with input size (N, C_{in}, H, W) and output $(N, C_{out}, H_{out}, W_{out})$ can be precisely described as:

$$\operatorname{out}(N_i, C_{out_j}) = \operatorname{bias}(C_{out_j}) + \sum_{k=0}^{C_{in}-1} \operatorname{weight}(C_{out_j}, k) \star \operatorname{input}(N_i, k),$$

where \star is the valid 2D cross-correlation operator, N is a batch size, C denotes a number of channels, H is a height of input planes in pixels, and W is width in pixels.

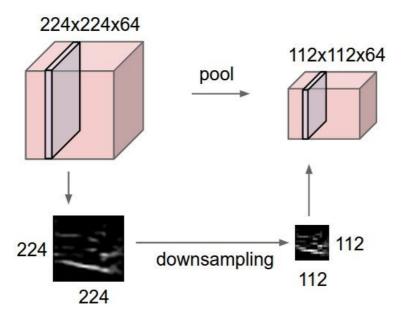
- stride controls the stride for the cross-correlation, a single number or a tuple.
- padding controls the amount of implicit zero-paddings on both sides for padding number of points for each dimension.
- dilation controls the spacing between the kernel points; also known as the à trous
 algorithm. It is harder to describe, but this link has a nice visualization of what dilation does.
- groups controls the connections between inputs and outputs. in_channels and out_channels must both be divisible by groups. For example,
 - At groups=1, all inputs are convolved to all outputs.
 - At groups=2, the operation becomes equivalent to having two conv layers side by side, each seeing half the input channels, and producing half the output channels, and both subsequently concatenated.
 - At groups= in_channels , each input channel is convolved with its own set of filters (of size | out_channels in channels |).

The parameters kernel_size , stride , padding , dilation can either be:

• a single int - in which case the same value is used for the height and width dimension

Pooling layer

- makes the representations smaller and more manageable
- operates over each activation map independently:



MAX POOLING

Single depth slice

X	\	1	1	2	4
		5	6	7	8
		3	2	1	0
		1	2	3	4

max pool with 2x2 filters and stride 2

6	8
3	4

У

- Accepts a volume of size $W_1 \times H_1 \times D_1$
- · Requires three hyperparameters:
- \circ their spatial extent F,
 - \circ the stride S.
- Produces a volume of size $W_2 imes H_2 imes D_2$ where:

$$W = (W - E)/C + 1$$

- $\circ \ \ W_2=(W_1-F)/S+1$
- $H_2 = (H_1 F)/S + 1$ $D_2 = D_1$
- Introduces zero parameters since it computes a fixed function of the input
- Note that it is not common to use zero-padding for Pooling layers

Common settings:

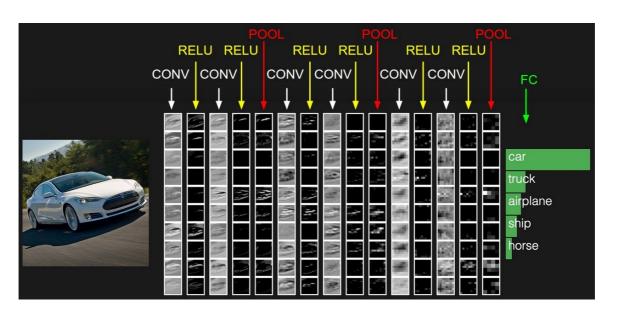
- Accepts a volume of size $W_1 imes H_1 imes D_1$
- Requires three hyperparameters:
 - \circ their spatial extent F,
 - the stride S.
- Produces a volume of size $W_2 \times H_2 \times D_2$ where:

$$W_2 = (W_1 - F)/S + 1$$

- $H_2 = (H_1 F)/S + 1$
- $Ooldsymbol{0} O_2 = D_1$
- · Introduces zero parameters since it computes a fixed function of the input
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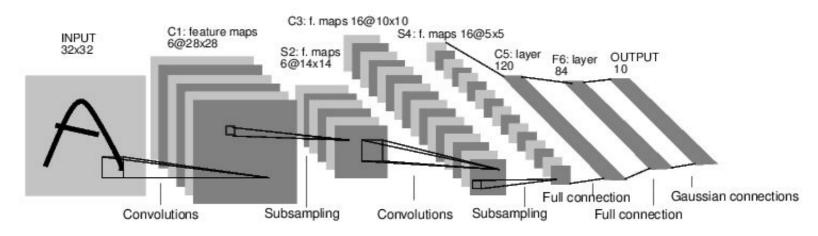
Fully Connected Layer (FC layer)

 Contains neurons that connect to the entire input volume, as in ordinary Neural Networks



Case Study: LeNet-5

[LeCun et al., 1998]



Conv filters were 5x5, applied at stride 1 Subsampling (Pooling) layers were 2x2 applied at stride 2 i.e. architecture is [CONV-POOL-CONV-POOL-CONV-FC]