

Communication

Concurrency and Distributed Systems

November 2023

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- Indexed parallel

Channels

Parameters in event names can serve two purposes:

- to represent data being passed;
- to indicate an event performed by a process instance.

They are written after a dot: `c.v`

Parameter expressions can take values from built-in or user-defined datatypes.

Built-in datatypes include sets and sequences.

compare: process parameters

Declarations

If c is a name and T is a type-valued expression, then

$$\text{channel } c : T$$

introduces the set of all events of the form $c.t$, where t is a value of type T .

We may introduce more than one channel in the same declaration: for example,

$$\text{channel } c, d : T$$

would introduce two channels c and d , both of type T .

Built-in datatypes

The built-in type `Int` represents the set of positive and negative integers: $-2^{31} + 1 \dots 2^{31} - 1$.

The built-in type `Bool` represents the set of Boolean values: `True` and `False`.

Example

The following declaration introduces a channel `insert` that can carry any integer value

```
channel insert : Int
```

User-defined datatypes

The declaration

```
datatype NewType = name1 | name2 | name3
```

introduces

- a new datatype NewType
- three constants, name1, name2, and name3, as values of that datatype

Constructors

The declaration

```
datatype NewType = name1 | name2 | label.OtherType
```

introduces

- a new datatype NewType
- two constants, name1 and name2, as values of that datatype
- a set of values of the form label.t, where t is any value of the datatype Type

types may be recursive – Type may be NewType

Example

```
datatype Tree = Leaf.Int | Node.Int.Tree.Tree
```

```
Leaf.3 :: Tree
```

```
Node.5.(Leaf.3).(Leaf.5) :: Tree
```

More components

An event on a channel may have several components. The definition

`channel c : T . U`

introduces a set of events

`{ c.t.u | t <- T, u <- U }`

Example

Floor = {0..2}

datatype Person = pA | pB | pC

channel call : Floor . Person

Productions

If we wish to refer to the set of all events associated with a channel, then we may use the **productions** operator. If c is a channel, then

$$\{ \mid c \mid \}$$

is the set of all events $c.x$ matching the declaration of c .

More generally, if c is a channel with multiple components, then

$$\{ \mid c.t \mid \}$$

is the set of all events $c.t.x$ matching the declaration.

Example

```
{ | floorRequest | } =  
  { floorRequest.0.pA, floorRequest.0.pB,  
    floorRequest.0.pC, floorRequest.0.pD,  
    floorRequest.1.pA, floorRequest.1.pB,  
    floorRequest.1.pC, floorRequest.3.pD,  
    ... }
```

Input and output

If two or more processes share a channel then, for each component:

- some processes may allow any value
- some processes may insist on exactly one value

Input and output

If the transaction described by the channel occurs, then for each component

- all participating processes agree on the value chosen
- their future behaviour may depend upon that value

Input

If the transaction described by the channel occurs, then a process allowing any value for some component

- now has a value for that component to work with
- a value arising from the behaviour of the other components

Input

We may use an indexed external choice to describe a process that allows any value for a component.

If c is a channel declared as

$$\text{channel } c : V$$

and P is a process parameterised by values of type V , then

$$[] v : V @ c.v \rightarrow P(v)$$

allows any event of the form $c.v$, and may be referred to as **input** on channel c .

Example

LiftController = ...

call?f?p -> ...

Input

We may use $?$ to indicate an indexed external choice for a particular component of a channel.

If c is a channel declared as

$$\text{channel } c : V$$

and P is a process parameterised by values of type V , then

$$c?v \rightarrow P(v)$$

allows any event of the form $c.v$, and may be referred to as **input** on channel c .

if we want to allow only $c.v$ for some subset W of V , then we can write $c?v:W \rightarrow P(v)$

Output

We may use $!$ to indicate insistence upon a particular value for a particular component:

If c is a channel declared as

$$\text{channel } c : V$$

and P is a process, and E is an expression with value val of type V

$$c!E \rightarrow P$$

will allow only the event $c.val$, and may be referred to as **output** on channel c .

Example

```
datatype MotorInstruction = up | down | stop
```

```
channel motor : MotorInstruction
```

```
LiftController =
```

```
...
```

```
motor!down -> ...
```

Output

For a single component, ! behaves exactly as (.).

However, for a channel with multiple components, the expression

$$c?x.y \rightarrow \dots$$

denotes a process that will allow any value of x and any value of y : that is, an external choice over pairs of values.

If we wish to describe a process that will allow any value of one component but will insist upon a particular value for the next, then we need to use !.

$$c?x!y \rightarrow \dots$$

Example

Person(pA) = ...

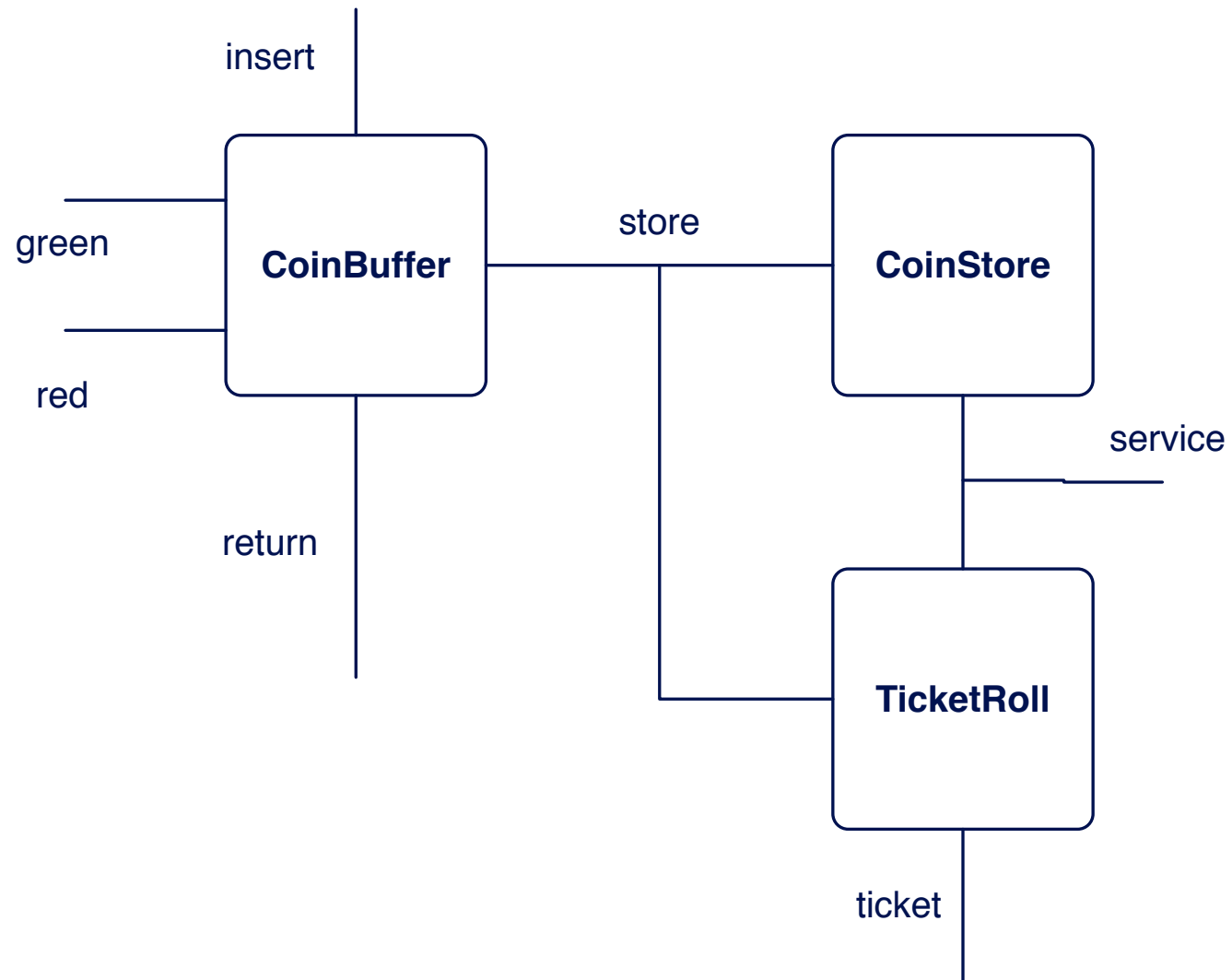
call?f!pA -> ...

Example

```
channel insert : Coin  
channel green, red, ticket  
channel store, return : {0..400}  
channel service
```

```
Coin = {10,20,50,100}  
price = 100  
bufferCap = 4  
storeCap = 8  
rollSize = 2
```

we write 0..400 rather than Int...



Example

```
aCoinBuffer = {| insert, green, red, store, return |}
```

```
CoinBuffer =
```

```
  let
```

```
    Holding(n,v) =
```

```
      n < bufferCap &
```

```
        insert?c -> Holding(n+1,v+c)
```

```
    []
```

```
    green -> ( if v >= price then
```

```
                Purchasing(n,v)
```

```
            else
```

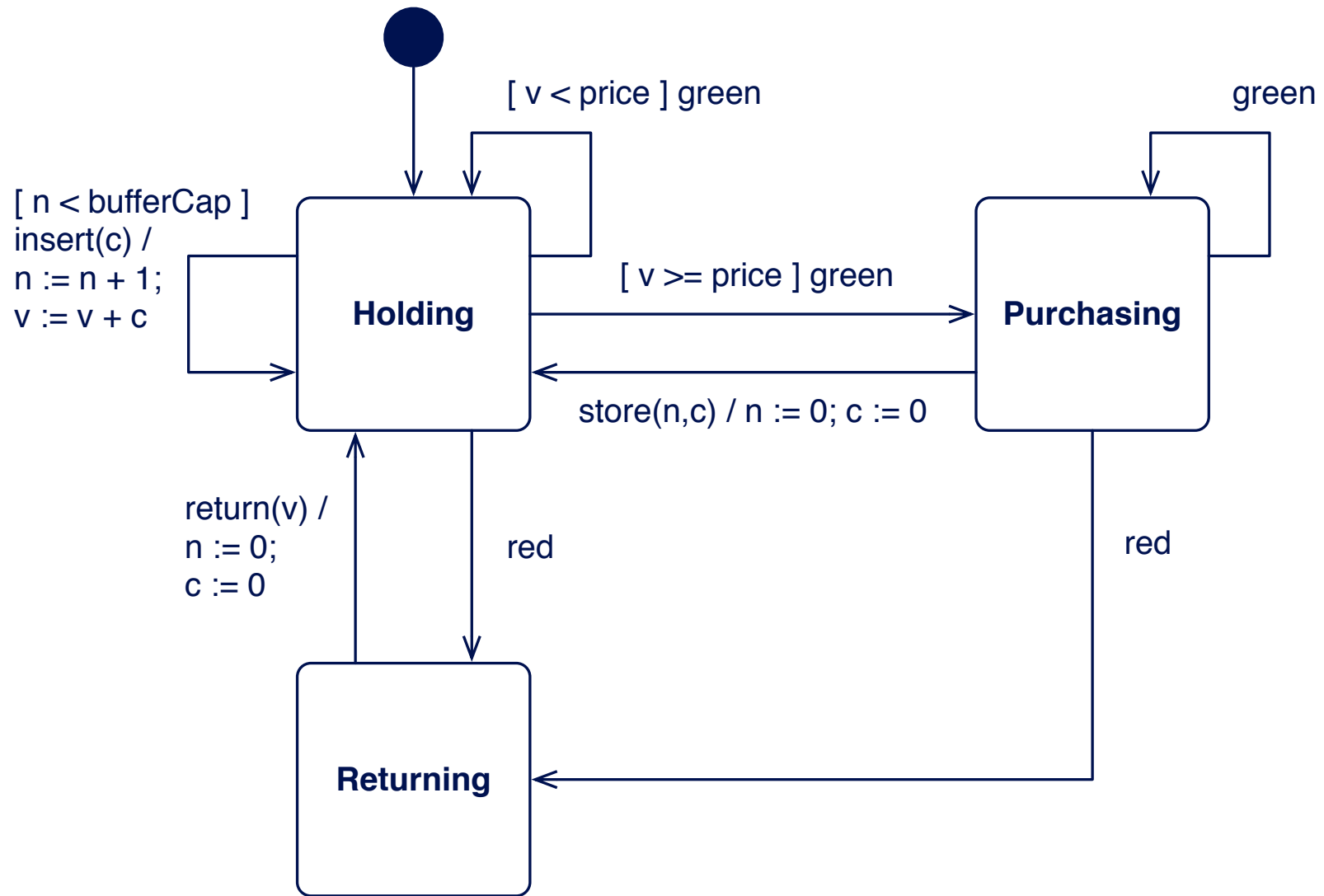
```
                Holding(n,v) )
```

```
    []
```

```
    red -> Returning(v)
```

```
Purchasing(n,v) =  
  green -> Purchasing(n,v)  
  []  
  red -> Returning(v)  
  []  
  store!n -> Holding(0,0)
```

```
Returning(v) =  
  return!v -> Holding(0,0)  
within  
  Holding(0,0)
```



```
aCoinStore = {| store, service |}
```

```
CoinStore =
```

```
  let
```

```
    Holding(m) =
```

```
      store?n:{1..(storeCap-m)} -> Holding(m+n)
```

```
      []
```

```
      service -> Holding(0)
```

```
  within
```

```
    Holding(0)
```

```
aTicketRoll = {| store, service, ticket |}
```

```
TicketRoll =
```

```
  let
```

```
    Holding(t) =
```

```
      (t > 0) & store?n -> ticket -> Holding(t-1)
```

```
      []
```

```
      service -> Holding(rollSize)
```

```
  within
```

```
    Holding(rollSize)
```

```
TicketMachine =  
  CoinBuffer  
  [ aCoinBuffer || union(aCoinStore,aTicketRoll) ]  
  ( CoinStore [ aCoinStore || aTicketRoll ] TicketRoll )  
  
assert TicketMachine :[deadlock free]  
  
TicketMachineWithoutService =  
  TicketMachine [ aTicketMachine || {service} ] STOP  
  
assert TicketMachineWithoutService :[deadlock free]
```

Scope

Our language of processes is **declarative**.

Each variable gets its value at the point at which it is declared, and retains that value for the **scope** of that declaration.

Example

Copy = in?x -> out!x -> Copy

Indexed parallel

If $P(x)$ is a process-valued expression with parameter x , and $aP(x)$ is a set-valued expression with the same parameter, then

$$|| \ x : X \ @ \ [aP(x)] \ P(x)$$

is a process that behaves as a combination of processes $P(x)$, one for each value of x in X , in which

- events from $aP(x)$ are allowed only when $P(x)$ allows them

Example

```
channel enterLift, exitLift : Floor . Person
```

```
aFloor(i) = { | enterLift.i, exitLift.i, ... | }
```

```
Floor(i) =
```

```
  let
```

```
    Holding(P) =
```

```
      enterLift!i?p:P -> ...
```

```
    ...
```

```
Floors = || i : {0..10} @ [aFloor(i)] Floor(i)
```

Example

```
Node(i,j) =  
  h.i.j?x -> v.i.(j+1)?y -> v.i.j!min(x,y) ->  
    if i + j == N then  
      v.(i+1).j!max(x,y) -> Node(i,j)  
    else  
      h.(i+1).j!max(x,y) -> Node(i,j)
```

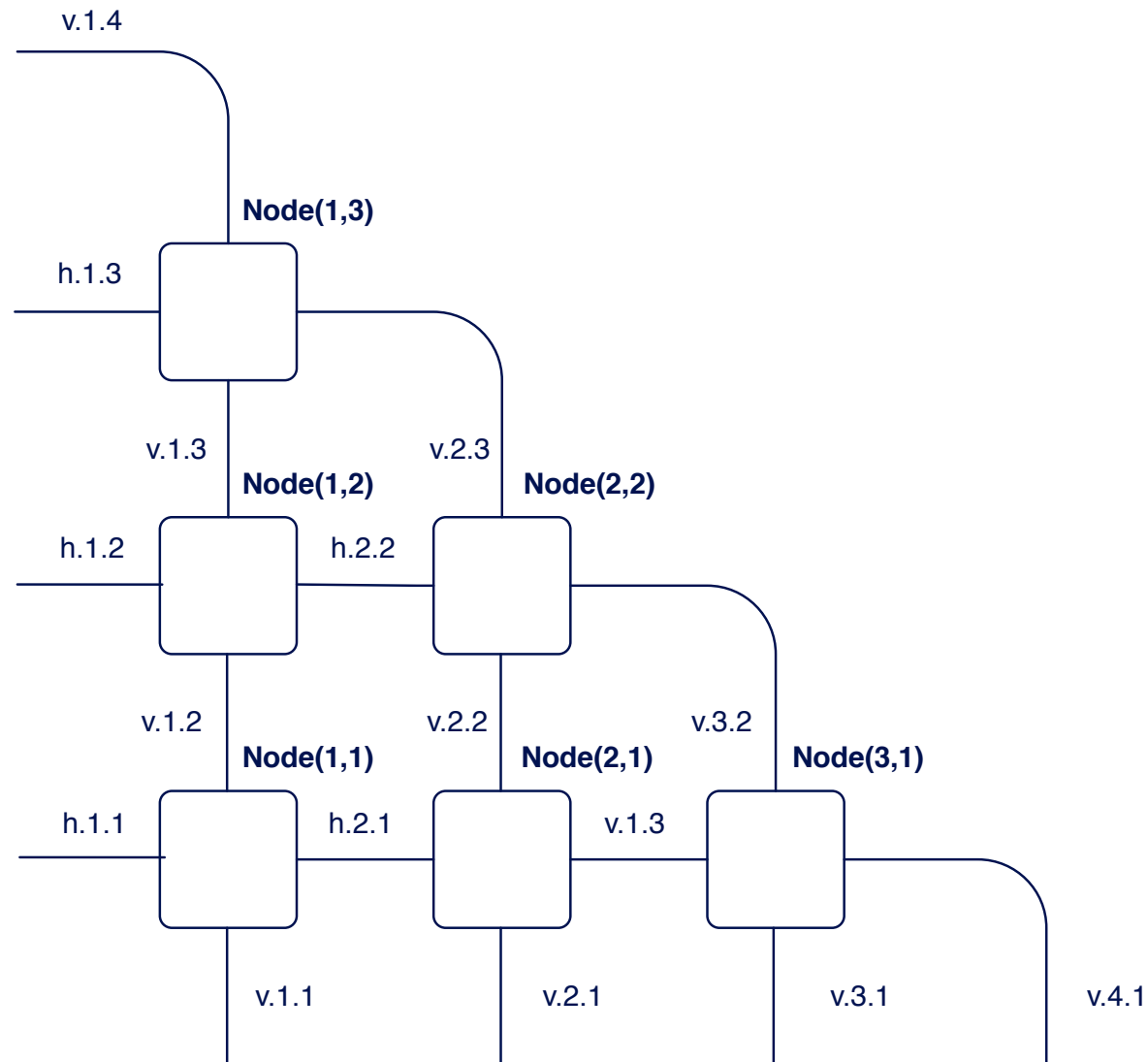
original

Example

```
aNode(i,j) =  
  { | h.i.j, v.i.(j+1), v.i.j,  
    if i + j == N then v.(i+1).j else h.(i+1).j | }
```

```
Array(N) =  
  || i : {1..N}, j : {1..N}, i+j <= N @ [aNode(i,j)] Node(i,j)
```

Example



Example

```
aInput = {| h.1.1, h.1.2, h.1.3, v.1.4 |}
```

```
Input = h.1.1!4 -> h.1.2!3 -> h.1.3!2 -> v.1.4!1 -> Input
```

```
aOutput = {| v.1.1, v.2.1, v.3.1, v.4.1 |}
```

```
Output = v.1.1!1 -> v.2.1!2 -> v.3.1!3 -> v.4.1!4 -> Output
```

```
aArray = {| v.i.j, h.i.j | i <- {1..4}, j <- {1..4} |}
```

```
ArrayIO = (Input [ aInput || aArray ] Array(4))  
          [ aArray || aOutput ] Output
```

```
assert ArrayIO :[deadlock free]
```

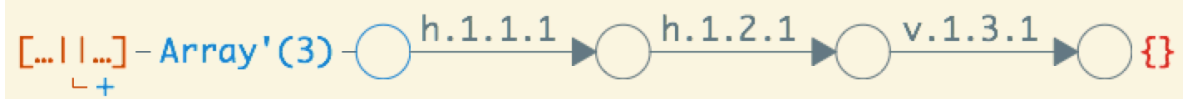
Example

```
Node'(i,j) =  
  h.i.j?x -> v.i.(j+1)?y ->  
    if i + j == N then  
      v.(i+1).j!max(x,y) -> v.i.j!min(x,y) -> Node'(i,j)  
    else  
      h.(i+1).j!max(x,y) -> v.i.j!min(x,y) -> Node'(i,j)
```

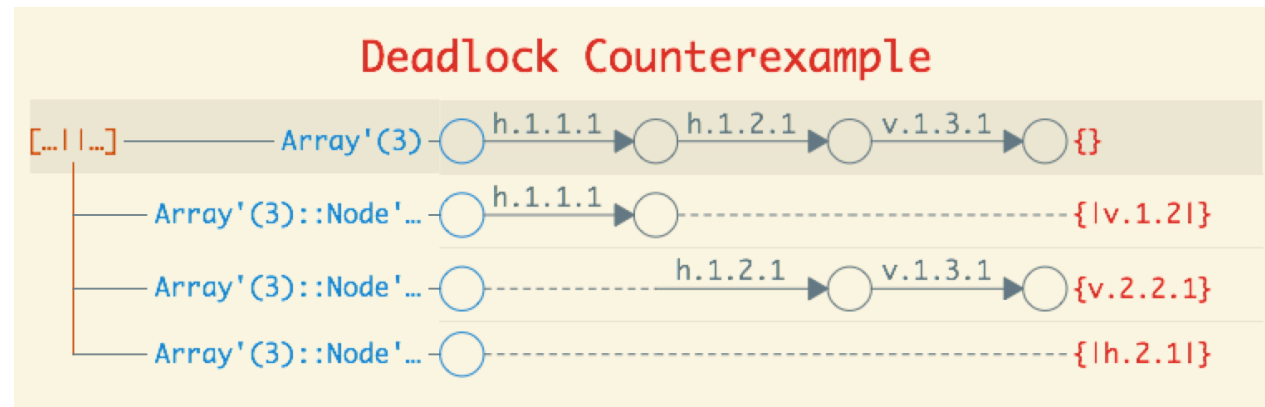
alternative

Example

Deadlock Counterexample



Example



Summary

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- Input and output
- Indexed parallel

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