

7.2

4.

$$E(X) = 1$$

$$E(X^2) = \int_0^{+\infty} x^2 f(x) dx = \int_0^{+\infty} x^2 e^{-x} dx = - \int_0^{+\infty} x^2 d(e^{-x}) = x^2 e^{-x} \Big|_0^{+\infty} + 2 \int_0^{+\infty} x e^{-x} dx = 2 \int_0^{+\infty} x e^{-x} dx = 2$$

$$D(X) = E(X^2) - E^2(X) = 1$$

5.

$$D(X) = E(X^2) - E^2(X) \quad E(X) = 0.5 \quad E(X^2) = 0.5 \quad D(X) = 0.5 - 0.25 = 0.25$$

$$D(Y) = E(Y^2) - E^2(Y) \quad E(Y) = E(X) = 0.3 \quad D(Y) = 0.3 - 0.09 = 0.21$$

$$8. E(X^2) = D(X) + E^2(X) = 2 + 1 = 3 \quad E(Y^2) = D(Y) + E^2(Y) = 3 + 1 = 4$$

$$\begin{aligned} D(XY) &= E(XY - E(XY))^2 = E((XY)^2 - 2XYE(XY) + E^2(XY)) \\ &= E(XY)^2 - 2E^2(XY) + E^2(XY) \\ &= E(XY)^2 - E^2(XY) \end{aligned}$$

$$E(X^2Y^2) = E(X^2)E(Y^2) = 12$$

$$E(XY) = E(X)E(Y) = 0.1$$

$$\therefore D(XY) = 11$$

$$9. E(X) = \mu^2 + \sigma^2 \quad E(X) = \mu \quad E(Y) = \mu^2 + \sigma^2 \quad E(Y) = \mu$$

$$= 2$$

$$= 1$$

$$= 5$$

$$= -2$$

$$E(2X+Y) = 2E(X) + E(Y) = 0 \quad E((2X+Y)^2) = E(4X^2 + 4XY + Y^2)$$

$$= 4E(X^2) + 4E(XY) + E(Y^2)$$

$$= 4E(X^2) + 4E(X)E(Y) + E(Y^2)$$

$$= 8 + -8 + 5 = 5$$

$$D(2X+Y) = E((2X+Y)^2) - E^2(2X+Y) = 5 - 0 = 5$$