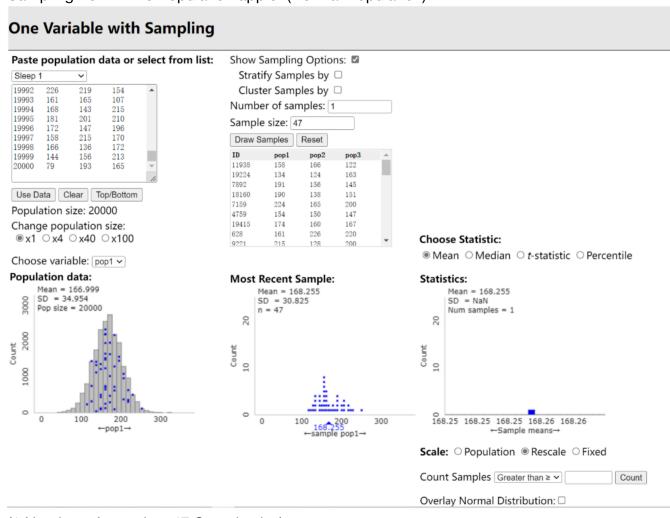
# Chapter 2 Summary

Tina Wang, Paul Luo, Jackson Cong

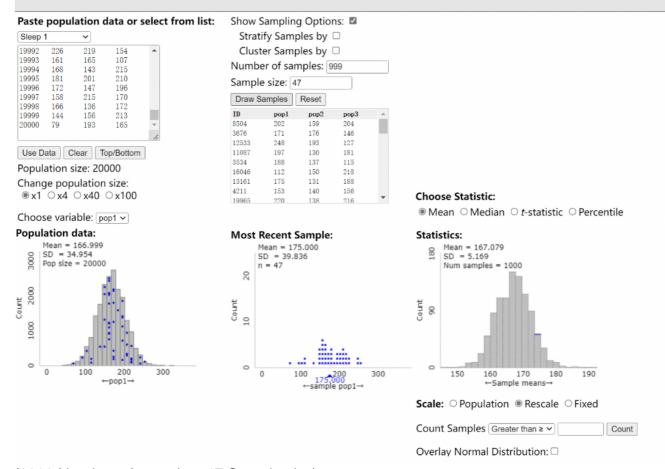
## Investigation 2.4: Population Mean

• Sampling from Finite Population applet (Normal Population)



(1 Number of samples, 47 Sample size)

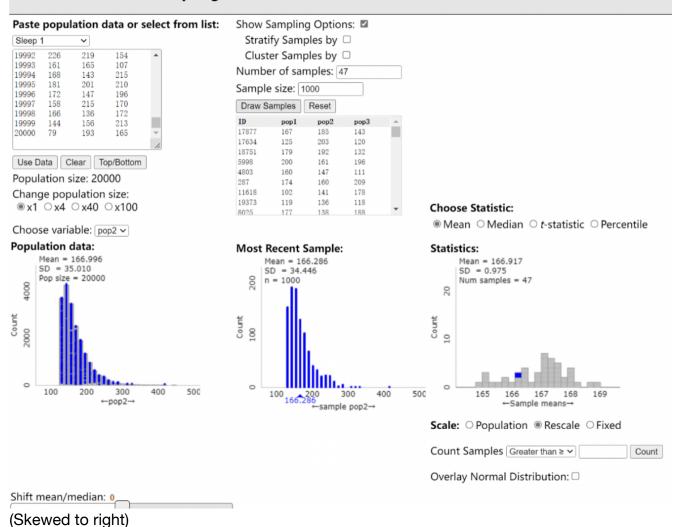
#### One Variable with Sampling



(1000 Number of samples, 47 Sample size)

· Non-normal Population

### One Variable with Sampling



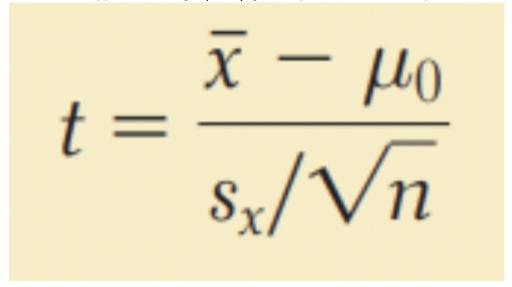
#### One Variable with Sampling



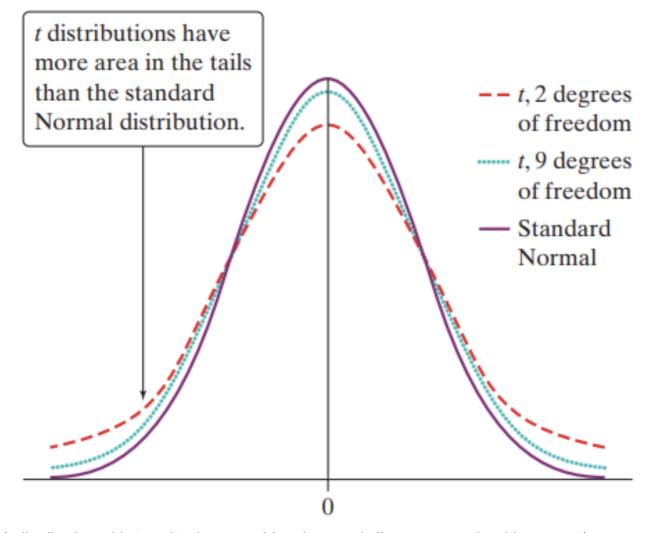
- (Uniform)
  - The sample data come from a well-designed random population or randomized experiment of size n with mean μ and standard deviation, the sampling distribution of sample means has following characters:
    - **Shape**: If the population distribution is **normal**, then so is the sampling distribution of  $\bar{x}$ ; If the population distribution **isn't normal**, the sampling distribution of  $\bar{x}$  will be approximately **normal** if the sample size is large enough by the central limit theorem (CLT).
    - Center:  $\mu_{\bar{x}} = \mu$  (The sampling mean equals to the population mean)
    - **Spread**:  $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$  (The sampling standard deviation equal to  $\frac{\sigma}{\sqrt{n}}$  of the population SD)
  - Central Limit Theorem: The population has a normal distribution or the sample size is large (n ≥ 30), the shape of sampling distribution will be normal. If the population distribution has unknown shape and n < 30, use a graph of the sample data to assess the Normality of the population. Do not use t procedures if the graph shows strong skewness or outliers.

# Investigation 2.5: t-test

- Standard deviation of statistic:  $SE(\bar{x}) = \frac{s}{\sqrt{n}}$
- To test the hypothesis  $H_0: \mu = \mu_0$ , compute the one-sample t statistic.

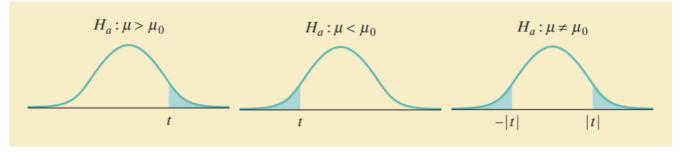


 When we perform inference about a population mean m using a t distribution, the appropriate degrees of freedom are found by subtracting 1 from the sample size n, making df (degrees of freedom) = n − 1.



(t distribution with 2 and 9 degrees of freedom, and all are symmetric with center 0)

• Then find the P-value by calculating the probability of getting a t statistic this large or larger in the direction specified by the alternative hypothesis  $H_a$  in a t distribution with df= n - 1:

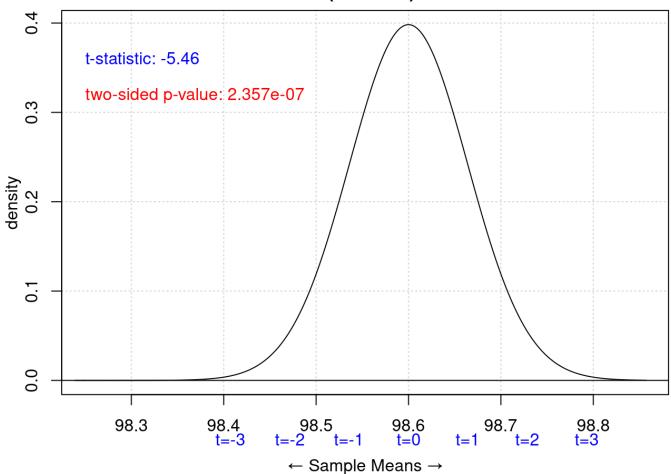


- **P-Value**: The P-value is based on a t-distribution with n 1 degrees of freedom. This value can be estimated in R.
- In R:
  - t.test(x, mu =  $\mu_0$ , alternative = "two.sided", conf.level = .95)
  - iscamonesamplet(xbar, sample standard deviation(s), n, hypothesized, alternative, conf.level)

```
iscamonesamplet(xbar = 98.249, sd = .733, n = 130, hypothesized = 98.6, alter
native = "two.sided", conf.level = .95)
```

```
##
## One Sample t test
##
## mean = 98.249, sd = 0.733, sample size = 130
## Null hypothesis : mu = 98.6
## Alternative hypothesis: mu <> 98.6
## t-statistic: -5.46
```

### t (df= 129)



```
## 95 % Confidence interval for mu: ( 98.1218 , 98.3762 )
## p-value: 2.35666e-07
```

- If  $P < \alpha$ , then Reject the  $H_0$ , otherwise Fail to Reject  $H_0$ .
- Confidence Interval for  $\mu$ . (Check the percentage of confidence interval to corresponding t-value)

$$\circ \ \bar{x} \pm t_{n-1}^* \times (\frac{s}{\sqrt{n}})$$

• In R: t.test(x, y = NULL, alternative = ("two.sided", "less", "greater"), mu = 0, conf.level = 0.95)

```
B3FD <- read.csv("~/math247/Project/B3FDAgeGender.csv")
age_diff <- abs(B3FD$difference)
t.test(age_diff, mu = 3, alt = "greater")</pre>
```

```
##
## One Sample t-test
##
## data: age_diff
## t = -3.3465, df = 498, p-value = 0.9996
## alternative hypothesis: true mean is greater than 3
## 95 percent confidence interval:
## 2.560345    Inf
## sample estimates:
## mean of x
## 2.705411
```

```
t.test(age_diff, mu = 3, conf.level = 0.95)
```

```
##
## One Sample t-test
##
## data: age_diff
## t = -3.3465, df = 498, p-value = 0.0008803
## alternative hypothesis: true mean is not equal to 3
## 95 percent confidence interval:
## 2.532456 2.878366
## sample estimates:
## mean of x
## 2.705411
```