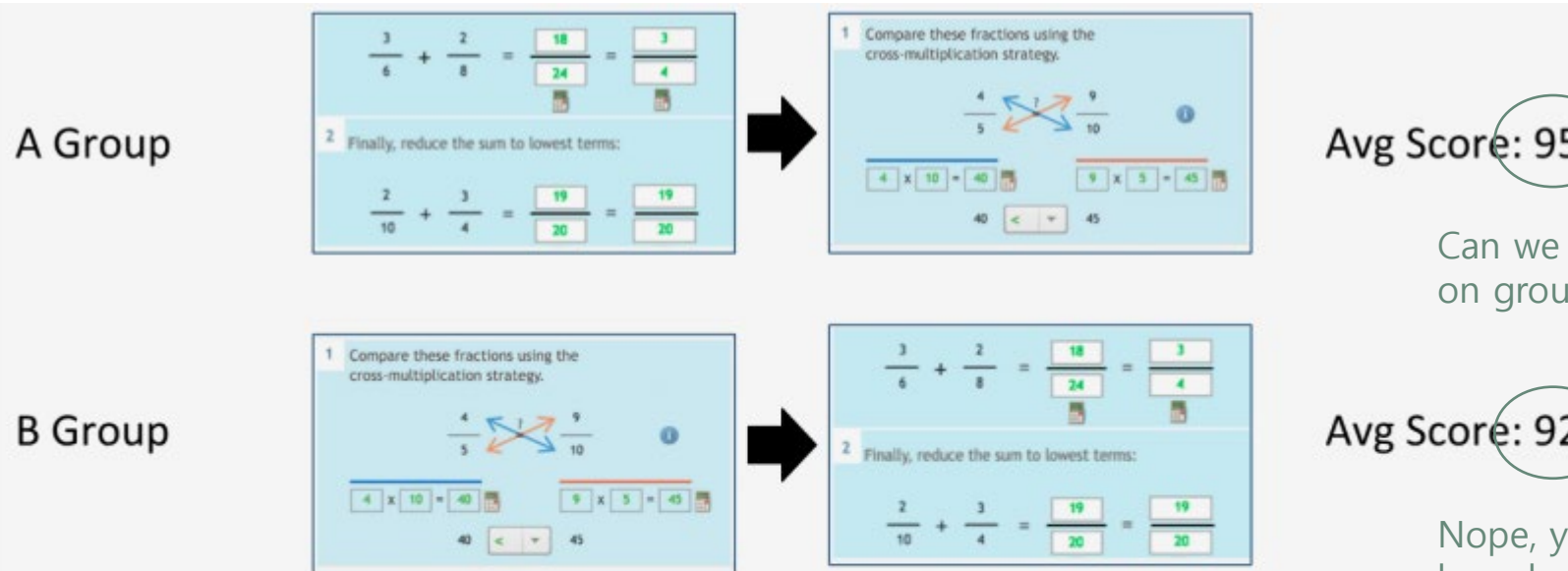


Lecture 15 : Batch RL

Why



Avg Score: 95

Can we say that method applied on group A is good enough?




Avg Score: 92

Nope, you don't know what would have happened if group B went through same sequence of interventions as group A




Why

| | | | |
|---------|--|--|---|
| A Group | $\frac{3}{6} + \frac{2}{8} = \frac{18}{24} = \frac{3}{4}$ <p>2 Finally, reduce the sum to lowest terms:</p> $\frac{2}{10} + \frac{3}{4} = \frac{19}{20} = \frac{19}{20}$ | <p>1 Compare these fractions using the cross-multiplication strategy:</p> $\frac{4}{5} \text{ ? } \frac{9}{10}$ <p>4 x 10 = 40 9 x 5 = 45</p> <p>40 < 45</p> | Avg Score: 95 |
| B Group | <p>1 Compare these fractions using the cross-multiplication strategy:</p> $\frac{4}{5} \text{ ? } \frac{9}{10}$ <p>4 x 10 = 40 9 x 5 = 45</p> <p>40 < 45</p> | <p>2 Finally, reduce the sum to lowest terms:</p> $\frac{2}{10} + \frac{3}{4} = \frac{19}{20} = \frac{19}{20}$ | Avg Score: 92 |
| B Group | $\frac{3}{6} + \frac{2}{8} = \frac{18}{24} = \frac{3}{4}$ <p>2 Finally, reduce the sum to lowest terms:</p> $\frac{2}{10} + \frac{3}{4} = \frac{19}{20} = \frac{19}{20}$ | <p>1 Compare these fractions using the cross-multiplication strategy:</p> $\frac{4}{5} \text{ ? } \frac{9}{10}$ <p>4 x 10 = 40 9 x 5 = 45</p> <p>40 < 45</p> | <p>???</p> <p>Test the first method by trying it and comparing it to what group B previously had done</p> |

Why

| | | | | |
|---------|--|---|--|---|
| A Group | $\frac{3}{6} + \frac{2}{8} = \frac{18}{24} = \frac{3}{4}$ <p>2 Finally, reduce the sum to lowest terms:</p> $\frac{2}{10} + \frac{3}{4} = \frac{19}{20} = \frac{19}{20}$ |  | <p>1 Compare these fractions using the cross-multiplication strategy.</p> $\frac{4}{5} \text{ ? } \frac{9}{10}$ <p>4 x 10 = 40 9 x 5 = 45</p> <p>40 < 45</p> | Avg Score: 95 |
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Why

| | | | | |
|---------|--|---|--|---|
| A Group | $\frac{3}{6} + \frac{2}{8} = \frac{18}{24} = \frac{3}{4}$ <p>2 Finally, reduce the sum to lowest terms:</p> $\frac{2}{10} + \frac{3}{4} = \frac{19}{20} = \frac{19}{20}$ |  | <p>1 Compare these fractions using the cross-multiplication strategy.</p> $\frac{4}{5} \text{ ? } \frac{9}{10}$ <p>4 x 10 = 40 9 x 5 = 45</p> <p>40 < 45</p> | Avg Score: 95 |
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Why

Generalization

Fair, but can improve

Q1. check on the meaning

In this case, generalization would mean making sure all candidate methods have been used to all possible groups to get rid of that factor that certain methods return unusual results when applied on certain groups

So, we want to reach towards a point where we know that all candidate methods can be generalized: know what averaged return they will give when applied to almost all of the possible groups to be tested on.

Improvement would include testing group A in the sequence that group B originally has gone through.

B Group

The diagram illustrates a transition from a traditional fraction addition method to a cross-multiplication method. On the left, under the label "B Group", two examples of fraction addition are shown. The first example is $\frac{3}{6} + \frac{2}{8} = \frac{18}{24} = \frac{3}{4}$, and the second is $\frac{2}{10} + \frac{3}{4} = \frac{19}{20} = \frac{19}{20}$. A large black arrow points from this section to the right. On the right, a box labeled "1" contains the instruction "Compare these fractions using the cross-multiplication strategy." It shows the fractions $\frac{4}{5}$ and $\frac{9}{10}$ with arrows indicating cross-multiplication: $4 \times 10 = 40$ and $9 \times 5 = 45$. Below this, it shows $40 < 45$. To the right of this box are three question marks "???".

Why

Generalization

Connects...

The idea of using the data that already has been collected and making the most out of it to make decisions on moving forward

Especially when making bad decisions can be costly or dangerous

Similarly if obtaining more data itself is costly or not possible

Q2 Would this mean: obtaining the most generalized result from given data?

Why

Generalization

Connects...

The idea of using the data that already has been collected and making the most out of it to make decisions on moving forward

Especially when making bad decisions can be costly or dangerous

Similarly if obtaining more data itself is costly or not possible



Safe batch reinforcement learning

Safe Batch Reinforcement Learning

Some probability that the new policy will not be worse than the old policy

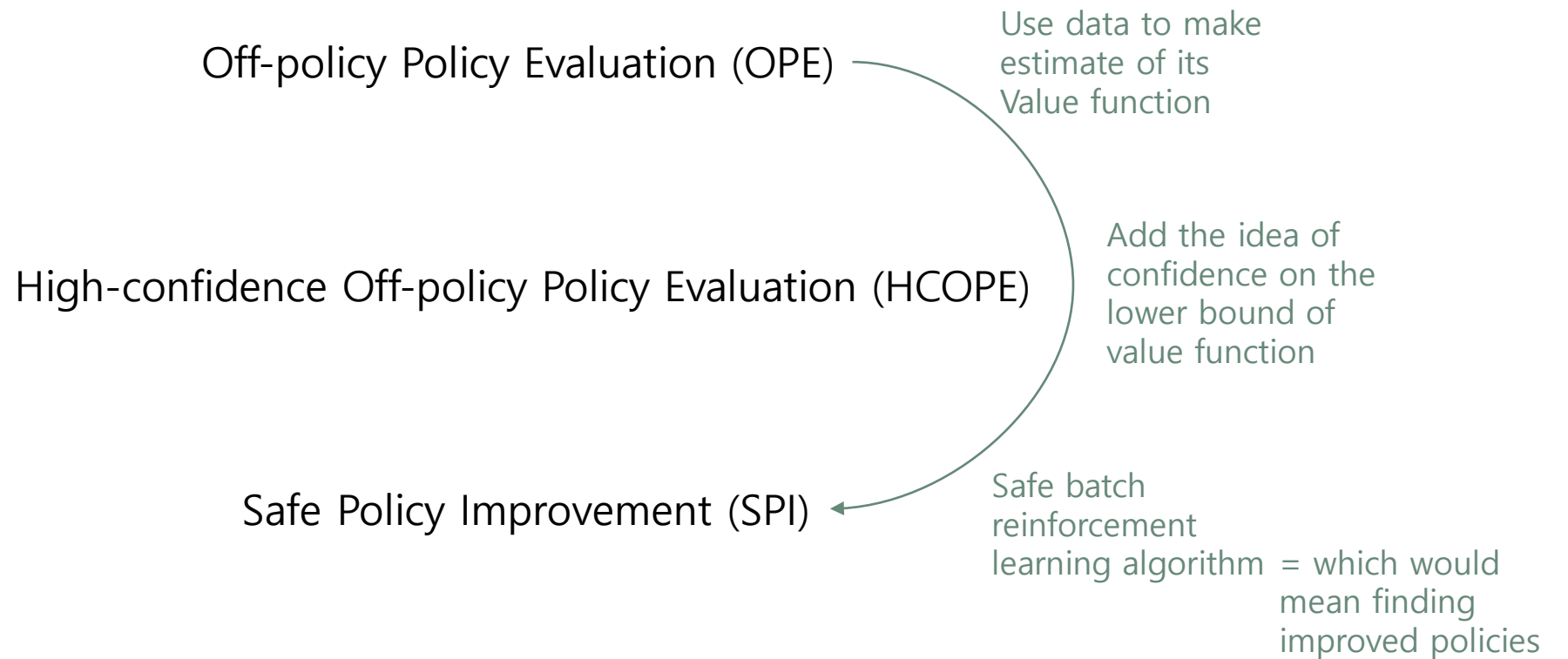
$$\Pr(V^{\mathcal{A}(\mathcal{D})} \geq V^{\pi_b}) \geq 1 - \delta$$

Easier
to calc

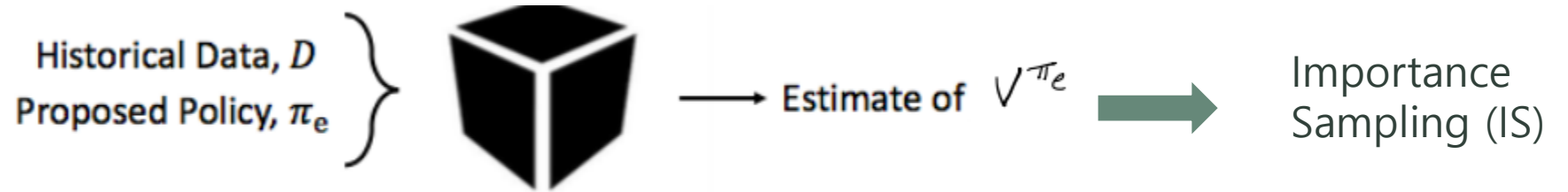
$$\Pr(V^{\mathcal{A}(\mathcal{D})} \geq V_{min}) \geq 1 - \delta$$

Safe batch
reinforcement
learning

Safe Batch Reinforcement Learning



Safe Batch Reinforcement Learning




Importance Sampling

$$IS(D) = \frac{1}{n} \sum_{i=1}^n \left(\prod_{t=1}^L \frac{\pi_e(a_t | s_t)}{\pi_b(a_t | s_t)} \right) \left(\sum_{t=1}^L \gamma^t R_t^i \right)$$


Importance
Sampling (IS)

Importance Sampling

$$IS(D) = \frac{1}{n} \sum_{i=1}^n \left(\prod_{t=1}^L \frac{\pi_e(a_t | s_t)}{\pi_b(a_t | s_t)} \right) \left(\sum_{t=1}^L \gamma^t R_t^i \right)$$



$$\prod \frac{p(a_j | s_j)^{\pi_e}}{p(a_j | s_j)^{\pi_b}}$$



$$G(h_j)$$

Importance Sampling

$$IS(D) = \frac{1}{n} \sum_{i=1}^n \left(\prod_{t=1}^L \frac{\pi_e(a_t | s_t)}{\pi_b(a_t | s_t)} \right) \left(\sum_{t=1}^L \gamma^t R_t^i \right)$$

Q3.

n = number of batches (epochs?)

L = number of timesteps within batch(epoch?)

Importance Sampling

$$IS(D) = \frac{1}{n} \sum_{i=1}^n \left(\prod_{t=1}^L \frac{\pi_e(a_t | s_t)}{\pi_b(a_t | s_t)} \right) \left(\sum_{t=1}^L \gamma^t R_t^i \right)$$

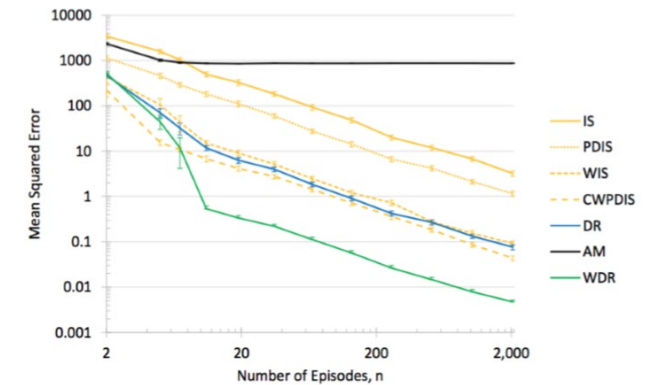
$$PSID(D) = \sum_{t=1}^L \gamma^t \frac{1}{n} \sum_{i=1}^n \left(\prod_{\tau=1}^t \frac{\pi_e(a_\tau | s_\tau)}{\pi_b(a_\tau | s_\tau)} \right) R_t^i$$

$$WIS(D) = \frac{1}{\sum_{i=1}^n w_i} \sum_{i=1}^n w_i \left(\sum_{t=1}^L \gamma^t R_t^i \right)$$


$$DR(\pi_e | D) = \frac{1}{n} \sum_{i=1}^n \sum_{t=0}^{\infty} \gamma^t w_t^i (R_t^i - \hat{q}^{\pi_e}(S_t^i, A_t^i)) + \gamma^t \rho_{t-1}^i \hat{v}^{\pi_e}(S_t^i)$$

WDR

MAGIC



Importance Sampling



$$IS(D) = \frac{1}{n} \sum_{i=1}^n \left(\prod_{t=1}^L \frac{\pi_e(a_t | s_t)}{\pi_b(a_t | s_t)} \right) \left(\sum_{t=1}^L \gamma^t R_t^i \right)$$

$$PSID(D) = \sum_{t=1}^L \gamma^t \frac{1}{n} \sum_{i=1}^n \left(\prod_{\tau=1}^t \frac{\pi_e(a_\tau | s_\tau)}{\pi_b(a_\tau | s_\tau)} \right) R_t^i \quad \text{temporal}$$

$$WIS(D) = \frac{1}{\sum_{i=1}^n w_i} \sum_{i=1}^n w_i \left(\sum_{t=1}^L \gamma^t R_t^i \right) \quad \text{weighted}$$

$$DR(\pi_e | D) = \frac{1}{n} \sum_{i=1}^n \sum_{t=0}^{\infty} \gamma^t w_t^i (R_t^i - \hat{q}^{\pi_e}(S_t^i, A_t^i)) + \gamma^t \rho_{t-1}^i \hat{v}^{\pi_e}(S_t^i) \quad \text{approximated model + IS}$$

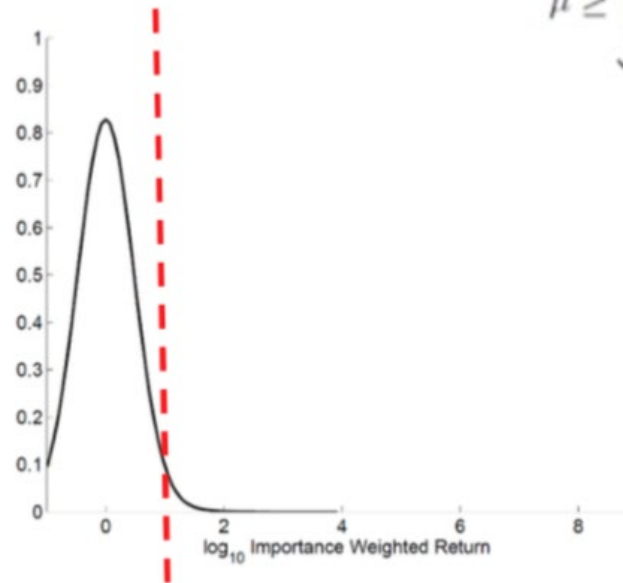
WDR weighted DR

MAGIC

High-confidence off-policy policy evaluation (HCOPE)



High-confidence off-policy policy evaluation (HCOPE)



$$\mu \geq \underbrace{\left(\sum_{i=1}^n \frac{1}{c_i}\right)^{-1} \sum_{i=1}^n \frac{Y_i}{c_i}}_{\text{empirical mean}} - \underbrace{\left(\sum_{i=1}^n \frac{1}{c_i}\right)^{-1} \frac{7n \ln(2/\delta)}{3(n-1)}}_{\text{term that goes to zero as } 1/n \text{ as } n \rightarrow \infty} - \underbrace{\left(\sum_{i=1}^n \frac{1}{c_i}\right)^{-1} \sqrt{\frac{\ln(2/\delta)}{n-1} \sum_{i,j=1}^n \left(\frac{Y_i}{c_i} - \frac{Y_j}{c_j}\right)^2}}_{\text{term that goes to zero as } 1/\sqrt{n} \text{ as } n \rightarrow \infty}.$$

1. Use some of the data to cutoff / tune the confidence interval
2. Compute lower bound (value function)

Frozen Lake

Used tensorflow and gym

Used e-greedy or random noise for just frozen lake (not slippery) *deterministic*



Used e-greedy or random noise for slippery and windy frozen lake *stochastic*

Used q-network for slippery and windy frozen lake