- 4. Understanding A3C
- 3. Before that, understand A-C or A2C
- 2. Before that, understand REINFORCE with baseline and see how it differs with A-C
- 1. Before that, understand REINFORCE: how policy gradient method works

Sum(of the rewards?) over states weighted by how often the states occur under policy pi

$$\nabla J(\boldsymbol{\theta}) \propto \sum_{s} \mu(s) \sum_{a} q_{\pi}(s, a) \nabla \pi(a|s, \boldsymbol{\theta})$$
$$= \mathbb{E}_{\pi} \left[ \sum_{a} q_{\pi}(S_{t}, a) \nabla \pi(a|S_{t}, \boldsymbol{\theta}) \right].$$

This starts from objective function...

$$J(\boldsymbol{\theta}) \doteq v_{\pi_{\boldsymbol{\theta}}}(s_0),$$

= true value function for policy pi determined by theta

This starts from objective function...

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$$= \mathbb{E}_{\pi} \left[ \sum_{a} q_{\pi}(S_{t}, a) \nabla \pi(a|S_{t}, \boldsymbol{\theta}) \right].$$



$$\boldsymbol{\theta}_{t+1} \doteq \boldsymbol{\theta}_t + \alpha \sum_{a} \hat{q}(S_t, a, \mathbf{w}) \nabla \pi(a|S_t, \boldsymbol{\theta}),$$

So then the update for parameters defining the policy would be like this

$$\nabla J(\boldsymbol{\theta}) \propto \sum_{s} \mu(s) \sum_{a} q_{\pi}(s, a) \nabla \pi(a|s, \boldsymbol{\theta})$$
$$= \mathbb{E}_{\pi} \left[ \sum_{a} q_{\pi}(S_{t}, a) \nabla \pi(a|S_{t}, \boldsymbol{\theta}) \right].$$



But then to simplify

$$\nabla J(\boldsymbol{\theta}) = \mathbb{E}_{\pi} \left[ \sum_{a} \pi(a|S_{t}, \boldsymbol{\theta}) q_{\pi}(S_{t}, a) \frac{\nabla \pi(a|S_{t}, \boldsymbol{\theta})}{\pi(a|S_{t}, \boldsymbol{\theta})} \right]$$

$$= \mathbb{E}_{\pi} \left[ q_{\pi}(S_{t}, A_{t}) \frac{\nabla \pi(A_{t}|S_{t}, \boldsymbol{\theta})}{\pi(A_{t}|S_{t}, \boldsymbol{\theta})} \right] \qquad \text{(replacing } a \text{ by the sample } A_{t} \sim \pi \text{)}$$

$$= \mathbb{E}_{\pi} \left[ G_{\iota} \frac{\nabla \pi(A_{t}|S_{t}, \boldsymbol{\theta})}{\pi(A_{t}|S_{t}, \boldsymbol{\theta})} \right], \qquad \text{(because } \mathbb{E}_{\pi}[G_{\iota}|S_{\iota}, A_{\iota}] = q_{\pi}(S_{\iota}, A_{\iota}) \text{)}$$



Then to update is

$$\boldsymbol{\theta}_{t+1} \doteq \boldsymbol{\theta}_t + \alpha G_t \frac{\nabla \pi(A_t|S_t, \boldsymbol{\theta}_t)}{\pi(A_t|S_t, \boldsymbol{\theta}_t)}.$$
  $\nabla \ln x = \frac{\nabla x}{x}$ 

## REINFORCE: Monte-Carlo Policy-Gradient Control (episodic) for $\pi_*$

Input: a differentiable policy parameterization  $\pi(a|s, \theta)$ 

Algorithm parameter: step size  $\alpha > 0$ 

Initialize policy parameter  $\boldsymbol{\theta} \in \mathbb{R}^{d'}$  (e.g., to **0**)

Loop forever (for each episode):

Generate an episode  $S_0, A_0, R_1, \ldots, S_{T-1}, A_{T-1}, R_T$ , following  $\pi(\cdot|\cdot, \boldsymbol{\theta})$ 

Loop for each step of the episode t = 0, 1, ..., T - 1:

$$G \leftarrow \sum_{k=t+1}^{T} \gamma^{k-t-1} R_k \\ \theta \leftarrow \theta + \alpha \gamma^t G \nabla \ln \pi (A_t | S_t, \theta)$$
 (G<sub>t</sub>)

## Why baseline helps

Ex) if there is a state where all actions return high values, the baseline can help differentiate the higher valued action out of them.

Better if baseline can have roughly median or average of the possible value for all the actionsc

## REINFORCE with Baseline (episodic), for estimating $\pi_{\theta} \approx \pi_*$

Input: a differentiable policy parameterization  $\pi(a|s, \theta)$ 

Input: a differentiable state-value function parameterization  $\hat{v}(s, \mathbf{w})$ 

Algorithm parameters: step sizes  $\alpha^{\theta} > 0$ ,  $\alpha^{\mathbf{w}} > 0$ 

Initialize policy parameter  $\boldsymbol{\theta} \in \mathbb{R}^{d'}$  and state-value weights  $\mathbf{w} \in \mathbb{R}^{d}$  (e.g., to 0)

Loop forever (for each episode):

Generate an episode  $S_0, A_0, R_1, \ldots, S_{T-1}, A_{T-1}, R_T$ , following  $\pi(\cdot|\cdot, \boldsymbol{\theta})$ 

Loop for each step of the episode t = 0, 1, ..., T - 1:

$$G \leftarrow \sum_{k=t+1}^{T} \gamma^{k-t-1} R_k$$

$$\delta \leftarrow G \left( \hat{v}(S_t, \mathbf{w}) \right) \text{ baseline}$$

$$\mathbf{w} \leftarrow \mathbf{w} + \alpha^{\mathbf{w}} \delta \nabla \hat{v}(S_t, \mathbf{w})$$

$$(G_t)$$

$$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha^{\boldsymbol{\theta}} \gamma^t \delta \nabla \ln \pi(A_t | S_t, \boldsymbol{\theta})$$

So why need to compare A-C and baseline REINFORCE?

From the idea that the baseline is the state-value function...

And updating parameters for state-value function

And updating another set of parameters for the policy

Seems similar to Actor(policy) and critic (state-value func)

BUT IT IS NOT A-C

Baseline REINFORCE is not A-C because

State-value func in baseline REINFORCE is not a critic because

State-value func is not used for bootstrapping but only as a baseline

Policy gradient method with bootstrapping critic

Temporal-difference method (it was Monte Carlo for REINFORCE)

So faster and more suitable for online problems

## From just a state-value func for baseline

$$\boldsymbol{\theta}_{t+1} \doteq \boldsymbol{\theta}_t + \alpha \left( G_{t:t+1} - \hat{v}(S_t, \mathbf{w}) \right) \frac{\nabla \pi(A_t | S_t, \boldsymbol{\theta}_t)}{\pi(A_t | S_t, \boldsymbol{\theta}_t)}$$

$$= \boldsymbol{\theta}_t + \alpha \left( R_{t+1} + \left( \hat{v}(S_{t+1}, \mathbf{w}) - \hat{v}(S_t, \mathbf{w}) \right) \frac{\nabla \pi(A_t | S_t, \boldsymbol{\theta}_t)}{\pi(A_t | S_t, \boldsymbol{\theta}_t)} \right)$$

$$= (13.12)$$

bootstrapping

```
One-step Actor-Critic (episodic), for estimating \pi_{\theta} \approx \pi_*
Input: a differentiable policy parameterization \pi(a|s, \theta)
Input: a differentiable state-value function parameterization \hat{v}(s, \mathbf{w})
Parameters: step sizes \alpha^{\theta} > 0, \alpha^{\mathbf{w}} > 0
Initialize policy parameter \boldsymbol{\theta} \in \mathbb{R}^{d'} and state-value weights \mathbf{w} \in \mathbb{R}^{d} (e.g., to 0)
Loop forever (for each episode):
    Initialize S (first state of episode)
    I \leftarrow 1
    Loop while S is not terminal (for each time step):
         A \sim \pi(\cdot|S, \boldsymbol{\theta})
          Take action A, observe S', R
          \delta \leftarrow R + \gamma \hat{v}(S', \mathbf{w}) - \hat{v}(S, \mathbf{w}) (if S' is terminal, then \hat{v}(S', \mathbf{w}) \doteq 0)
         \mathbf{w} \leftarrow \mathbf{w} + \alpha^{\mathbf{w}} \delta \nabla \hat{v}(S, \mathbf{w}) Note that delta can be seen as \boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha^{\boldsymbol{\theta}} I \delta \nabla \ln \pi(A|S, \boldsymbol{\theta}) advantage = Advantage Actor Critic
          I \leftarrow \gamma I
                                                                 = A2C
          S \leftarrow S'
```

## Asynchronous advantage actor-critic

### Algorithm S3 Asynchronous advantage actor-critic - pseudocode for each actor-learner thread.

```
// Assume global shared parameter vectors \theta and \theta_v and global shared counter T=0
                                                                                                                     Difference from just A-C:
// Assume thread-specific parameter vectors \theta' and \theta'_{v}
Initialize thread step counter t \leftarrow 1
                                                                                                                     Multiple A-C agents with a global
repeat
                                                                                                                     shared parameter
     Reset gradients: d\theta \leftarrow 0 and d\theta_v \leftarrow 0.
     Synchronize thread-specific parameters \theta' = \theta and \theta'_v = \theta_v
    t_{start} = t
    Get state s_t
     repeat
         Perform a_t according to policy \pi(a_t|s_t;\theta')
         Receive reward r_t and new state s_{t+1}
         t \leftarrow t + 1
         T \leftarrow T + 1
    until terminal s_t or t - t_{start} == t_{max}
    R = \begin{cases} 0 & \text{for terminal } s_t \\ V(s_t, \theta'_v) & \text{for non-terminal } s_t \text{// Bootstrap from last state} \end{cases}
                                                                                                      Paper says that this is same as
    for i \in \{t - 1, ..., t_{start}\} do
                                                                                                      advantage
         R \leftarrow r_i + \gamma R
         Accumulate gradients wrt \theta': d\theta \leftarrow d\theta + \nabla_{\theta'} \log \pi(a_i|s_i;\theta')(R - V(s_i;\theta'_v))
                                                                                                              Accumulate gradient over multiple
         Accumulate gradients wrt \theta'_v: d\theta_v \leftarrow d\theta_v + \partial (R - V(s_i; \theta'_v))^2 / \partial \overline{\theta'_v}
                                                                                                              timesteps before applying
    end for
    Perform asynchronous update of \theta using d\theta and of \theta_v using d\theta_v.
until T > T_{max}
```

## Further things to take note

## Q. Reason for being asynchronous?

### Algorithm S3 Asynchronous advantage actor-critic - pseudocode for each actor-learner thread.

// Assume global shared parameter vectors  $\theta$  and  $\theta_v$  and global shared counter T=0// Assume thread-specific parameter vectors  $\theta'$  and  $\theta'_{v}$ Initialize thread step counter  $t \leftarrow 1$ repeat Reset gradients:  $d\theta \leftarrow 0$  and  $d\theta_v \leftarrow 0$ . Synchronize thread-specific parameters  $\theta' = \theta$  and  $\theta'_v = \theta_v$  $t_{start} = t$ Get state s<sub>t</sub> repeat Perform  $a_t$  according to policy  $\pi(a_t|s_t;\theta')$ Receive reward  $r_t$  and new state  $s_{t+1}$  $t \leftarrow t + 1$  $T \leftarrow T + 1$ **until** terminal  $s_t$  or  $t - t_{start} == t_{max}$ for terminal  $s_t$  $V(s_t, \theta'_v)$  for non-terminal  $s_t$ // Bootstrap from last state for  $i \in \{t-1, \ldots, t_{start}\}$  do In reverse order for proper bootstrapping  $R \leftarrow r_i + \gamma R$ Accumulate gradients wrt  $\theta'$ :  $d\theta \leftarrow d\theta + \nabla_{\theta'} \log \pi(a_i|s_i;\theta')(R - V(s_i;\theta'_v))$ Accumulate gradients wrt  $\theta'_v$ :  $d\theta_v \leftarrow d\theta_v + \partial (R - V(s_i; \theta'_v))^2 / \partial \theta'_v$ 

Input Input Decoder Decoder Decoder Critic Critic Actor Actor Network Network Network Network  $\pi(s,a)$ V(s)  $\pi(s,a)$ V(s) Actor-Critic Type #1 Actor-Critic Type #2

Really depends on the model but this ones seems to be this

#### end for

Perform asynchronous update of  $\theta$  using  $d\theta$  and of  $\theta_v$  using  $d\theta_v$ .

until 
$$T > T_{max}$$

Possible idea: incorporating experience replay into the asynchronous reinforcement learning framework to increase data efficiency

Debatable if it will get faster

코드!

https://github.com/laphisboy/RL\_fall/tree/master/fall\_week\_4