AdvStDaAn, Worksheet, Week 2

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05.04.2022

Contents

Exercise 1

```
path <- file.path('Datasets', 'sniffer.dat')
df <- read.table(path, header=TRUE)
summary(df)</pre>
```

Dataset loading and sanity check:

```
##
      Temp.Tank
                       Temp.Gas
                                       Vapor.Tank
                                                     Vapor.Dispensed
           :31.00
                           :35.00
                                                            :2.590
##
   Min.
                    Min.
                                    Min.
                                            :2.590
                                                     Min.
   1st Qu.:37.00
                    1st Qu.:41.00
                                     1st Qu.:3.290
                                                     1st Qu.:3.373
  Median :60.00
                    Median :60.00
                                    Median :4.285
                                                     Median :4.090
##
##
  Mean
           :57.91
                    Mean
                           :55.91
                                    Mean
                                            :4.422
                                                     Mean
                                                            :4.324
##
   3rd Qu.:62.00
                    3rd Qu.:62.00
                                     3rd Qu.:4.630
                                                     3rd Qu.:4.540
   Max.
           :92.00
                    Max.
                           :92.00
                                    Max.
                                            :7.450
                                                     Max.
                                                            :7.450
          Y
##
           :16.00
##
  Min.
##
  1st Qu.:23.75
## Median :31.50
## Mean
           :31.12
##
   3rd Qu.:34.50
## Max.
           :55.00
dim(df)
```

```
## [1] 32 5
```

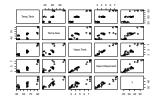
head(df)

```
Temp.Tank Temp.Gas Vapor.Tank Vapor.Dispensed Y
##
## 1
             33
                      53
                                3.32
                                                 3.42 29
## 2
             31
                                3.10
                                                 3.26 24
                      36
## 3
             33
                      51
                                3.18
                                                 3.18 26
## 4
             37
                      51
                                3.39
                                                 3.08 22
## 5
             36
                      54
                                3.20
                                                 3.41 27
## 6
             35
                      35
                                3.03
                                                 3.03 21
```

tail(df)

##		Temp.Tank	Temp.Gas	Vapor.Tank	Vapor.Dispensed	Y
##	27	60	62	4.02	3.89	33
##	28	59	62	3.98	4.02	27
##	29	59	62	4.39	4.53	34
##	30	37	35	2.75	2.64	19
##	31	35	35	2.59	2.59	16
##	32	37	37	2.73	2.59	22

plot(df)



Data looks like it is highly correlated with each other. But we keep it this way

for the first exercises.

Exercise 1.a)

Fitting a first model without any transformations to the data:

```
lm1.1 \leftarrow lm(Y \sim ., data = df)
```

The model looks initially not too bad. For a proper evaluation one would need to perform a residual and sensitivity analysis to investigate the adequacy of the model. But for this exercise we keep the track of the worksheet.

E1.a)(I) Estimated coefficients

```
coef(lm1.1)
```

```
## (Intercept) Temp.Tank Temp.Gas Vapor.Tank Vapor.Dispensed
## 1.01501756 -0.02860886 0.21581693 -4.32005167 8.97488928
```

E1.a)(II) F-statistic

```
summary(lm1.1)
```

```
##
## Call:
## lm(formula = Y ~ ., data = df)
##
## Residuals:
              1Q Median
##
      Min
                            3Q
                                  Max
  -5.586 -1.221 -0.118 1.320
##
                                5.106
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
##
  (Intercept)
                    1.01502
                               1.86131
                                         0.545 0.59001
## Temp.Tank
                   -0.02861
                               0.09060
                                        -0.316
                                                0.75461
## Temp.Gas
                    0.21582
                               0.06772
                                         3.187
                                                0.00362 **
## Vapor.Tank
                   -4.32005
                               2.85097
                                        -1.515
                                                0.14132
                   8.97489
## Vapor.Dispensed
                                         3.237
                                                0.00319 **
                               2.77263
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.73 on 27 degrees of freedom
## Multiple R-squared: 0.9261, Adjusted R-squared: 0.9151
## F-statistic: 84.54 on 4 and 27 DF, p-value: 7.249e-15
```

The p-value of the F-statistic is « 0.05 indicating that at least one of the variables can not be 0 and therfore are important to describe the response value. Even though, the p-values of the t-test indicate that not all of them are of the same importance. In this case are only 2 explanatory variables significantly important (Temp.Gas & Vapor.Dispensed). E1.a)(III) Variance Inflation Factor (VIF) Inspecting multicollinearity with the Variance Inflation Factor (VIF):

```
library(car)
```

```
## Loading required package: carData
```

```
vif(lm1.1)
```

```
## Temp.Tank Temp.Gas Vapor.Tank Vapor.Dispensed
## 12.997379 4.720998 71.301491 61.932647
```

A vif above 5 to 10 indicates problems with multicollinearity. According to this guideline all variables but Temp.Gas have too high vif factors and therewith problems with multicollinearity. Vapor.Tank is affected the most.