ML Evaluation → Classification

CMSC 473/673 - NATURAL LANGUAGE PROCESSING

Slides modified from Dr. Frank Ferraro

Learning Objectives

Develop an intuition about precision & recall

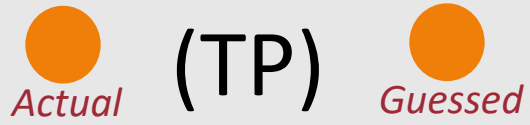
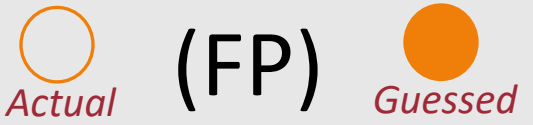
Extend P/R to multi-class problems

Identify when you might want certain evaluation metrics over others

Model classification problems using logistic regression

Define appropriate features for a logistic regression problem

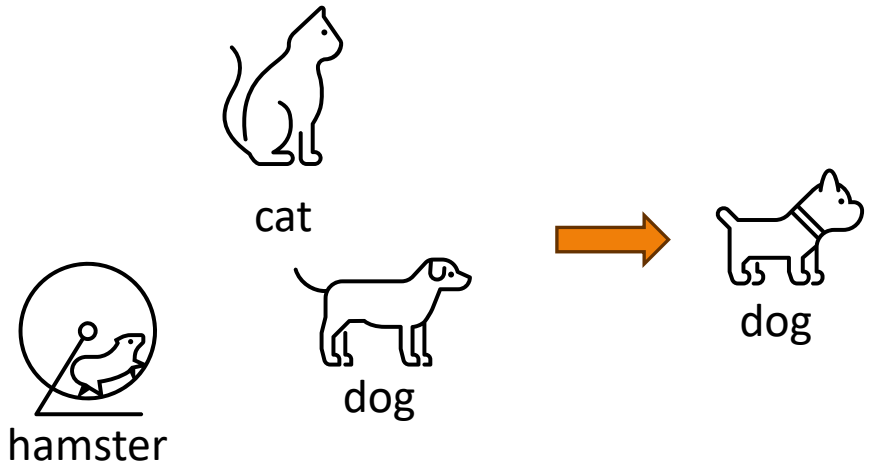
Review: Classification Evaluation: the 2-by-2 contingency table

	What is the actual label?	
What label does our system predict? (↓)	**Actual Target Class (“●”)**	**Not Target Class (“○”)**
Selected/ Guessed (“●”)	True Positive (TP) 	False Positive (FP) 
Not selected/ not guessed (“○”)	False Negative (FN) 	True Negative (TN) 

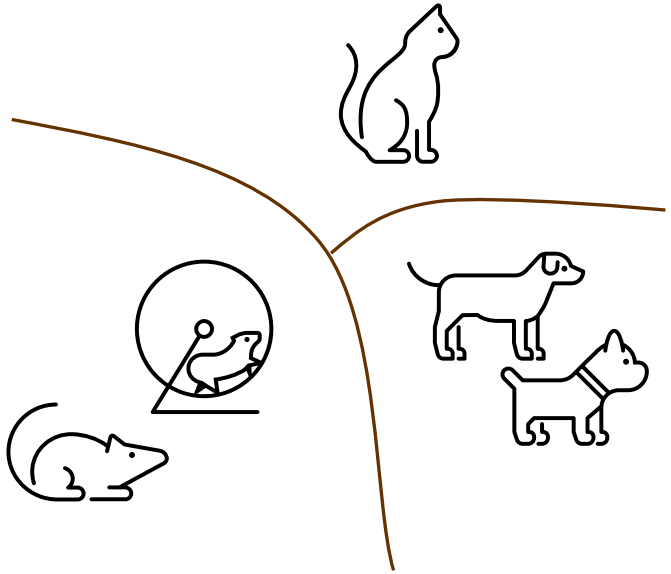
Construct this table by *counting* the number of TPs, FPs, FNs, TNs

Review: Types of Learning

SUPERVISED LEARNING

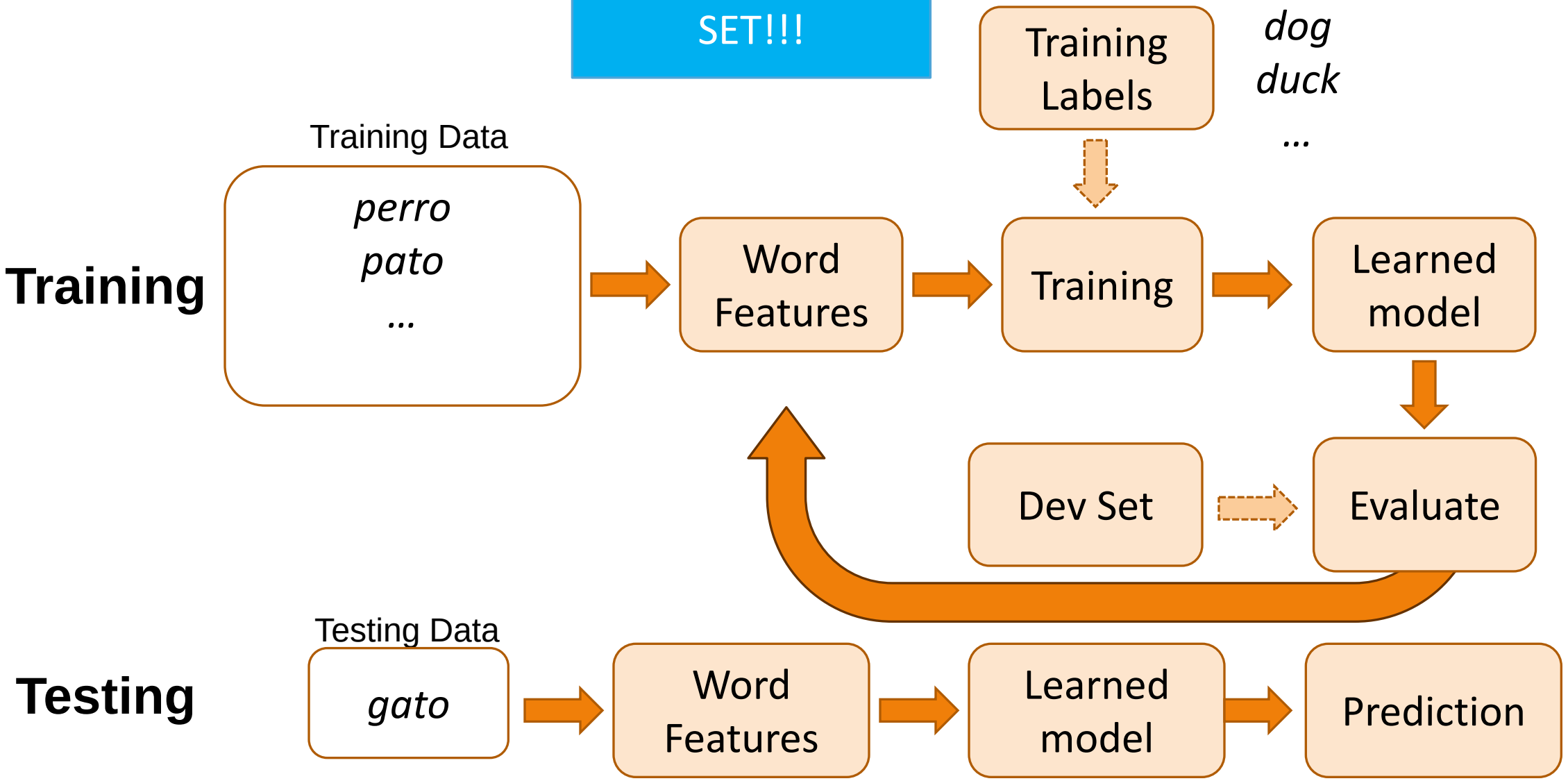


UNSUPERVISED LEARNING

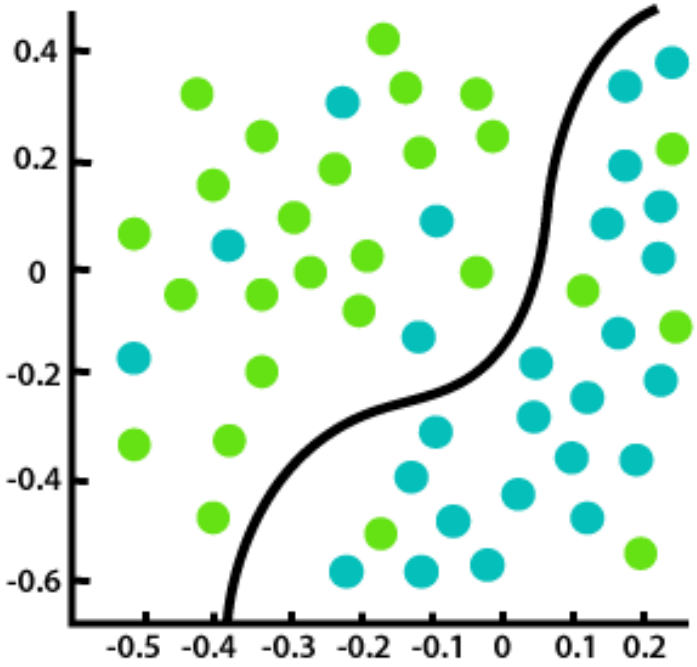


Review: Steps

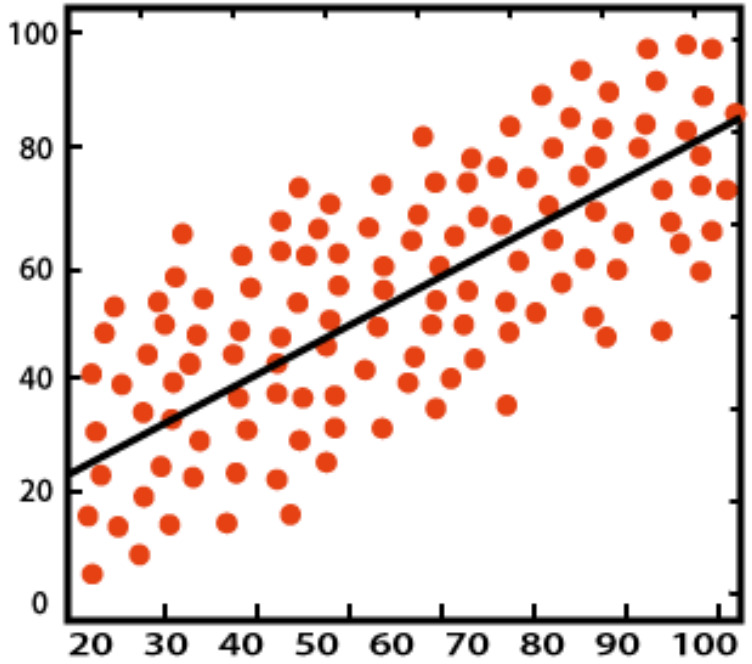
DO NOT ITERATE ON THE TESTING SET!!!



Review: Types of models



Classification



Regression

https://medium.com/unpackai/classification-regression-in-machine-learning-7cf3b13b0b09

Review: Classification Evaluation: the 2-by-2 contingency table

	What is the actual label?	
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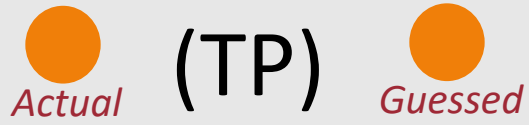
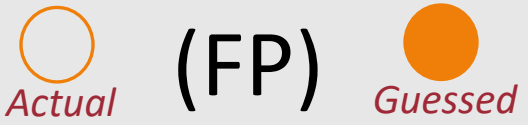
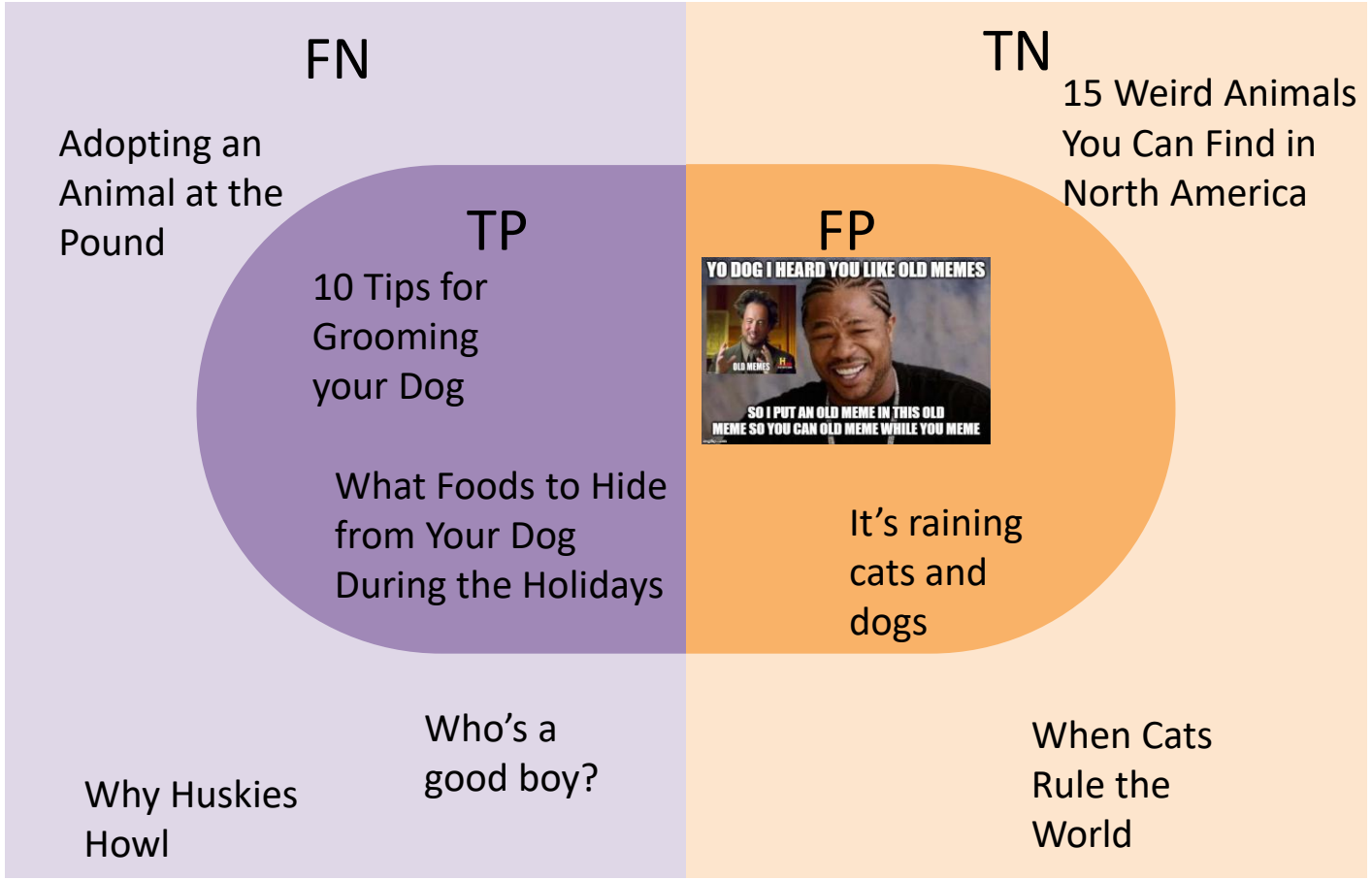
Selected/ Guessed (“●”)	True Positive (TP) 	False Positive (FP) 
Not selected/ not guessed (“○”)	False Negative (FN) 	True Negative (TN) 

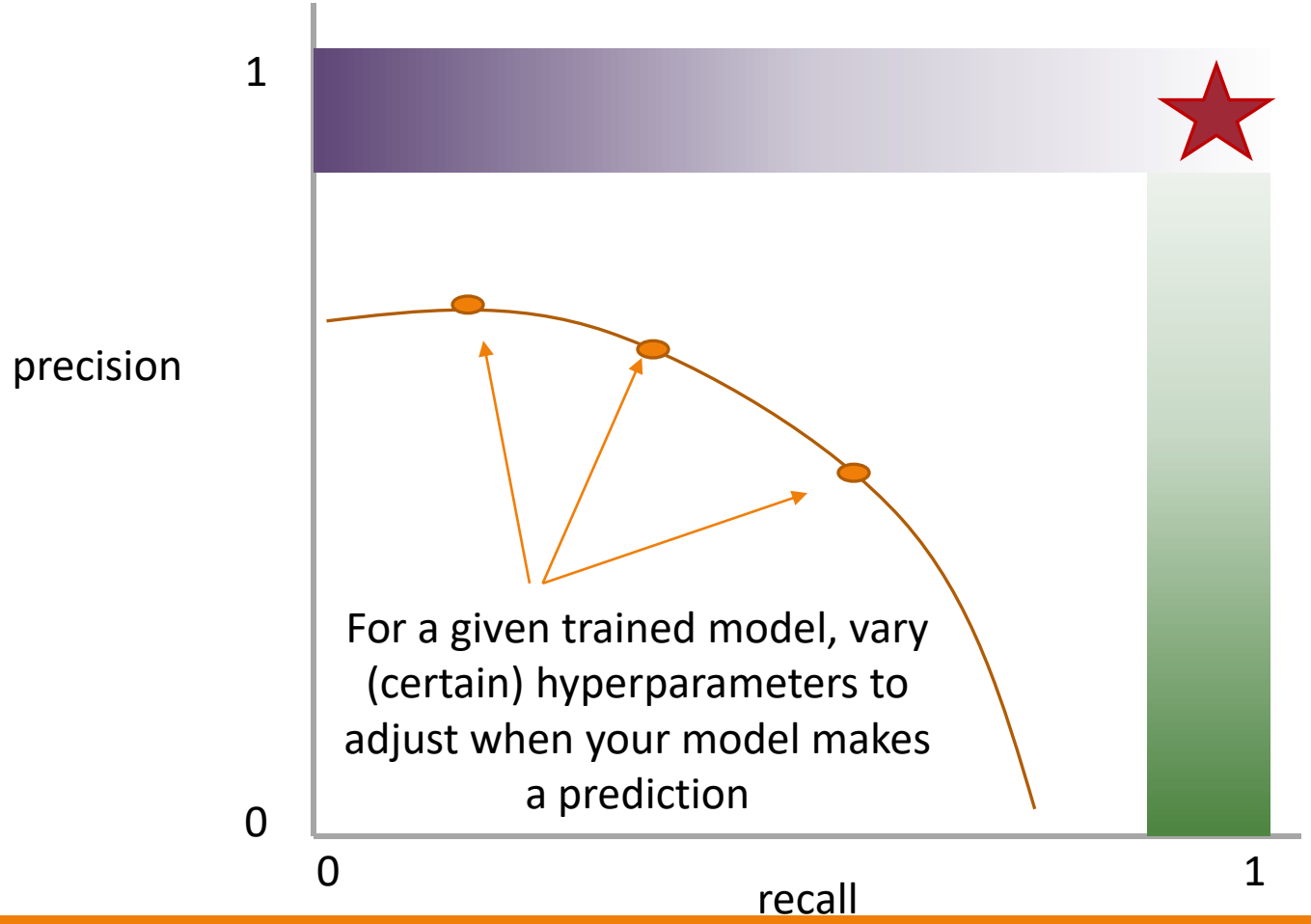
Contingency Table (out of table form)

Query:
Articles about dogs



Meme from: https://www.reddit.com/r/AdviceAnimals/comments/ck8xh0/yo_dawg_i_heard_you_like_old_memes/

Review: Precision and Recall Present a Tradeoff



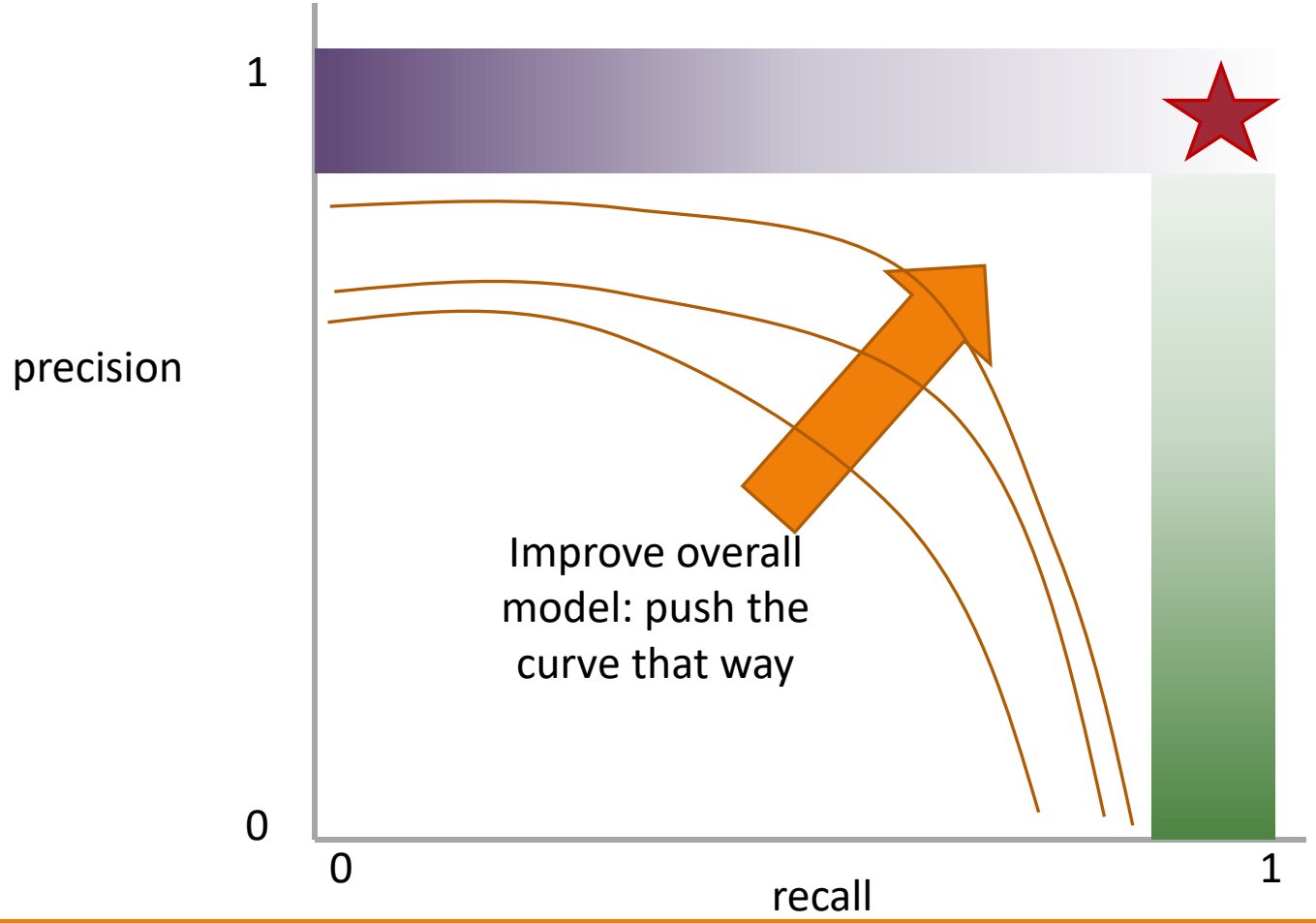
Q: Where do you want your ideal model ?

Q: You have a model that always identifies correct instances. Where on this graph is it?

Q: You have a model that only make correct predictions. Where on this graph is it?

Idea: measure the tradeoff between precision and recall

Review: Precision and Recall Present a Tradeoff



Q: Where do you want your ideal model ?

Q: You have a model that always identifies correct instances. Where on this graph is it?

Q: You have a model that only make correct predictions. Where on this graph is it?

Idea: measure the tradeoff between precision and recall

Review: A combined measure: F-score

Weighted (harmonic) average of **P**recision & **R**ecall

F1 measure: equal weighting between precision and recall

$$F_1 = \frac{2 * P * R}{P + R} = \frac{2 * TP}{2 * TP + FP + FN}$$

(useful when $P = R = 0$)

Classification Evaluation: Accuracy, Precision, and Recall

Accuracy: % of items correct

$$\frac{\text{TP} + \text{TN}}{\text{TP} + \text{FP} + \text{FN} + \text{TN}}$$

$$F_1 = \frac{2 * P * R}{P + R} = \frac{2 * TP}{2 * TP + FP + FN}$$

When would you want to use accuracy vs F1?

Accuracy works better if the dataset is balanced

Accuracy takes everything in consideration

F-Score is focused on TP

	Actually Target	Actually Not Target
Selected/Guessed	True Positive (TP)	False Positive (FP)
Not select/not guessed	False Negative (FN)	True Negative (TN)

P/R/F in a Multi-class Setting: Micro- vs. Macro-Averaging

Macroaveraging: Compute performance for each class, then average.

$$\text{macroprecision} = \frac{1}{C}\sum_{c}\frac{\text{TP}_c}{\text{TP}_c + \text{FP}_c} = \frac{1}{C}\sum_{c}\text{precision}_c$$

$$\text{macrorecall} = \frac{1}{C}\sum_{c}\frac{\text{TP}_c}{\text{TP}_c + \text{FN}_c} = \frac{1}{C}\sum_{c}\text{recall}_c$$

when to prefer macroaveraging?

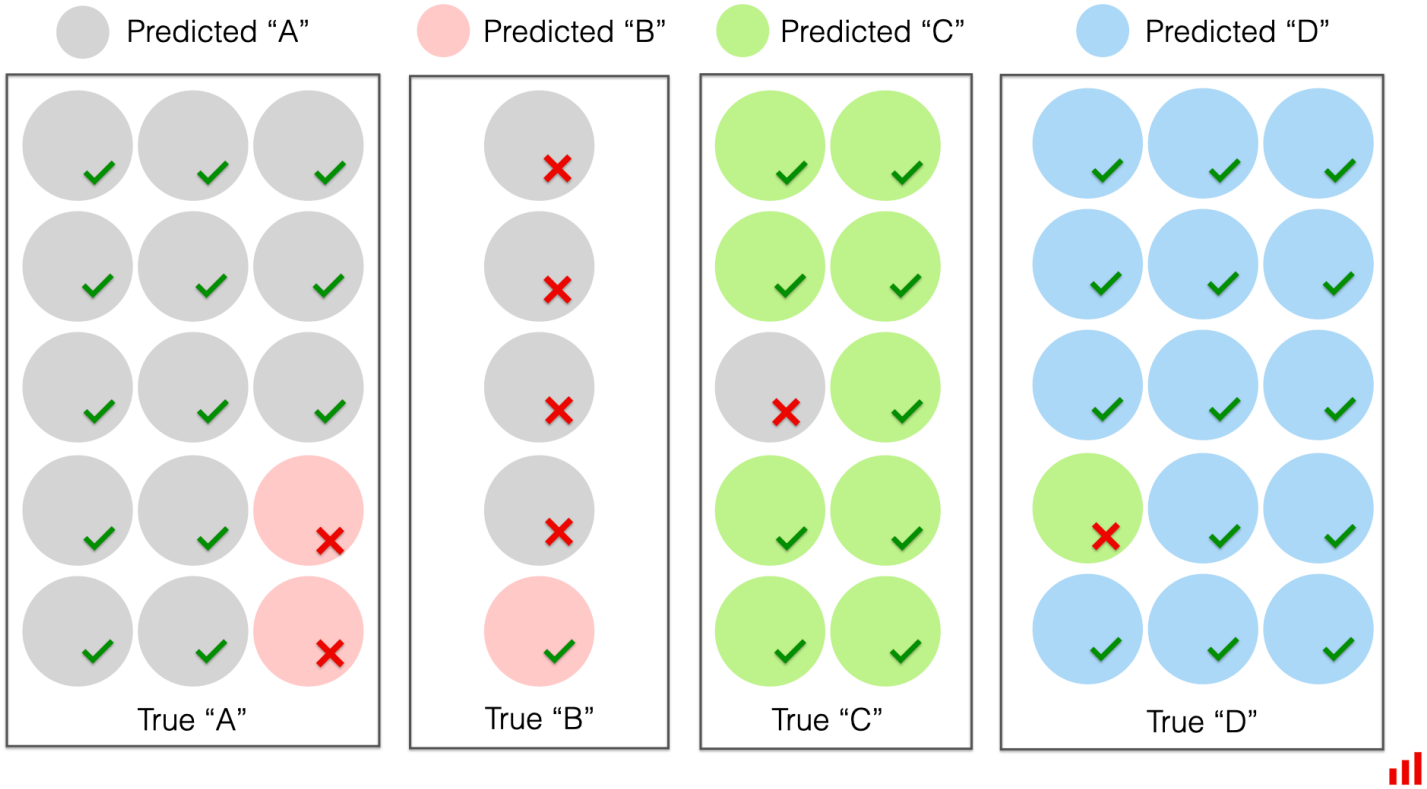
Microaveraging: Collect decisions for all classes, compute contingency table, evaluate.

$$\text{microprecision} = \frac{\sum_c \text{TP}_c}{\sum_c \text{TP}_c + \sum_c \text{FP}_c}$$

$$\text{microrecall} = \frac{\sum_c \text{TP}_c}{\sum_c \text{TP}_c + \sum_c \text{FN}_c}$$

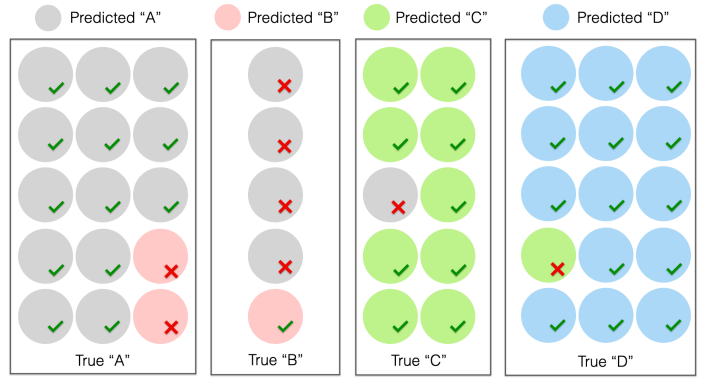
when to prefer microaveraging?

Macro/Micro Example

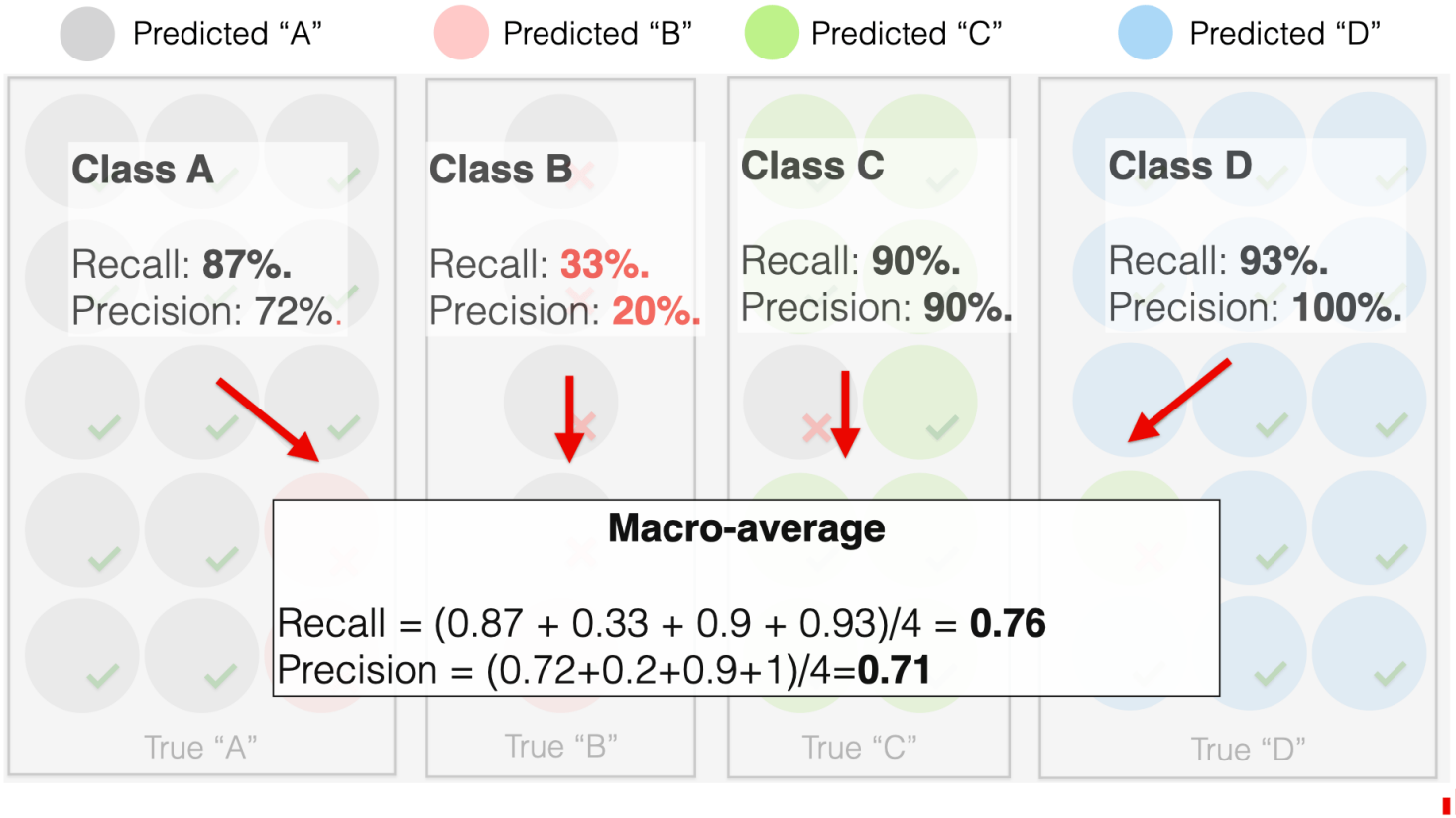


https://www.evidentlyai.com/classification-metrics/multi-class-metrics

Each *class* has equal weight



Macro-Average

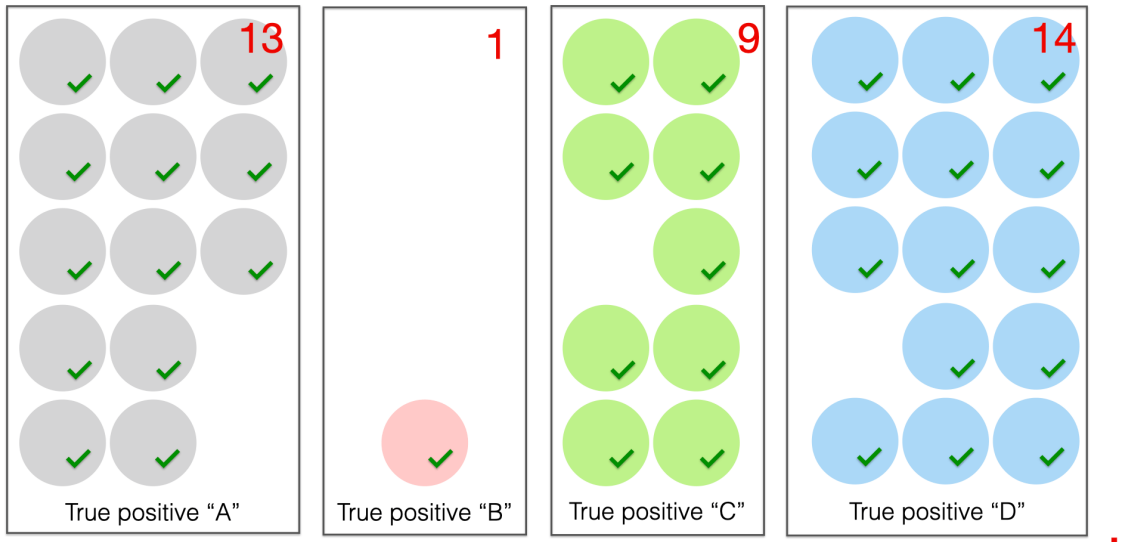


https://www.evidentlyai.com/classification-metrics/multi-class-metrics

Each *instance* has equal weight

Micro-Average

All true positives



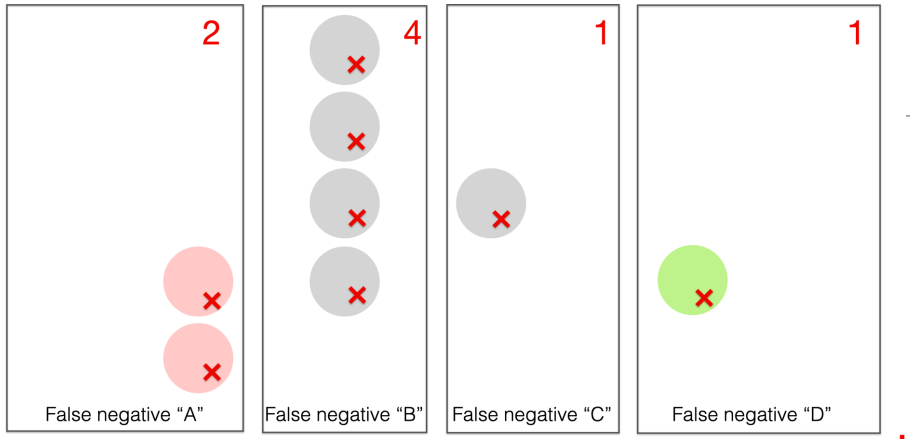
Total TP | Total FP | Total FN

$$\text{Precision}_{\text{Micro-average}} = \frac{13 + 1 + 9 + 14}{13 + 1 + 9 + 14 + \boxed{2 + 5 + 1 + 0}} = 0.82$$

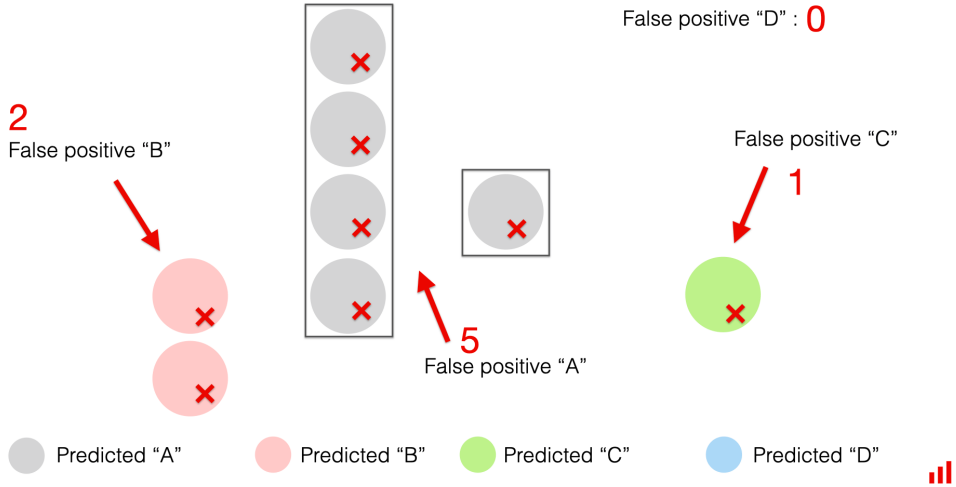
$$\text{Recall}_{\text{Micro-average}} = \frac{13 + 1 + 9 + 14}{13 + 1 + 9 + 14 + 2 + 4 + 1 + 1} = 0.82$$

https://www.evidentlyai.com/classification-metrics/multi-class-metrics

All false negatives



All false positives



Micro- vs Macro-Average

So when would we want to prefer micro-averaging vs macro-averaging?

$$\text{macroprecision} = \frac{1}{C}\sum_{c}\frac{\text{TP}_c}{\text{TP}_c + \text{FP}_c} = \frac{1}{C}\sum_{c}\text{precision}_c$$

$$\text{macrorecall} = \frac{1}{C}\sum_{c}\frac{\text{TP}_c}{\text{TP}_c + \text{FN}_c} = \frac{1}{C}\sum_{c}\text{recall}_c$$

$$\text{microprecision} = \frac{\sum_c \text{TP}_c}{\sum_c \text{TP}_c + \sum_c \text{FP}_c}$$

$$\text{microrecall} = \frac{\sum_c \text{TP}_c}{\sum_c \text{TP}_c + \sum_c \text{FN}_c}$$

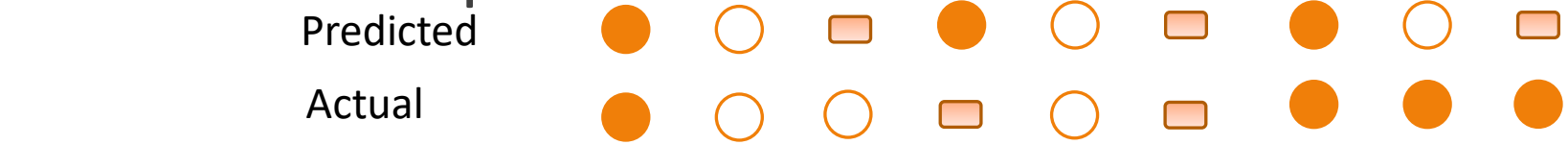
But how do we compute stats for multiple classes?

We already saw how the “polarity” affects the stats we compute…

Two main approaches. Either:

1. Compute “one-vs-all” 2x2 tables. OR
2. Generalize the 2x2 tables and compute per-class TP / FP / FN based on the diagonals and off-diagonals

1. Compute “one-vs-all” 2x2 tables

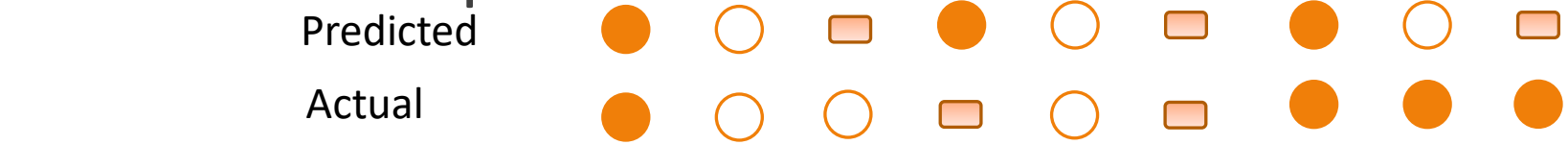


Look for ●	Actually Target	Actually Not Target
Selected/Guessed	True Positive (TP)	False Positive (FP)
Not select/not guessed	False Negative (FN)	True Negative (TN)

Look for ○	Actually Target	Actually Not Target
Selected/Guessed	True Positive (TP)	False Positive (FP)
Not select/not guessed	False Negative (FN)	True Negative (TN)

Look for ▭	Actually Target	Actually Not Target
Selected/Guessed	True Positive (TP)	False Positive (FP)
Not select/not guessed	False Negative (FN)	True Negative (TN)

1. Compute “one-vs-all” 2x2 tables

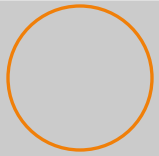
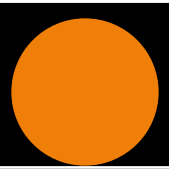
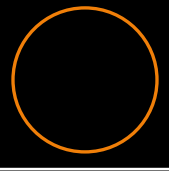


Look for ●	Actually Target	Actually Not Target
Selected/Guessed	2	1
Not select/not guessed	2	4

Look for ○	Actually Target	Actually Not Target
Selected/Guessed	2	1
Not select/not guessed	1	5

Look for ▭	Actually Target	Actually Not Target
Selected/Guessed	1	2
Not select/not guessed	1	5

2. Generalizing the 2-by-2 contingency table

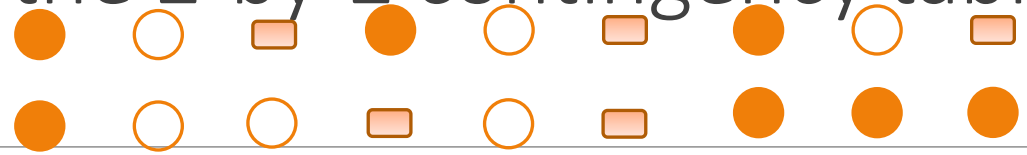
		Correct Value		
				
Guessed Value		#	#	#
		#	#	#
		#	#	#

This is also called a **Confusion Matrix**

2. Generalizing the 2-by-2 contingency table

Predicted

Actual

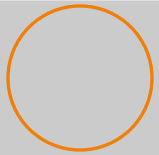
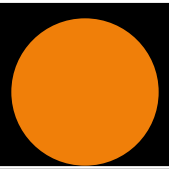
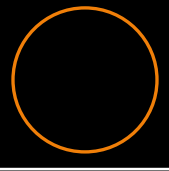


Guessed Value	Correct Value		
	●	○	▭
●	#	#	#
○	#	#	#
▭	#	#	#

2. Generalizing the 2-by-2 contingency table

Predicted

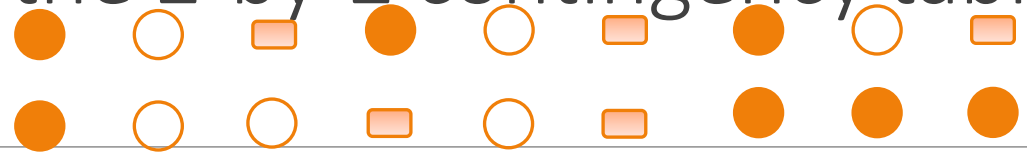
Actual

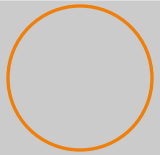
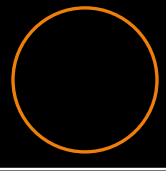
		Correct Value		
				
Guessed Value		2	0	1
		1	2	0
		1	1	1

2. Generalizing the 2-by-2 contingency table

Predicted

Actual



Guessed Value	Correct Value		
			
	A 2	B 0	C 1
	D 1	E 2	F 0
	G 1	H 1	I 1

How do you compute TP  ?

2. Generalizing the 2-by-2 contingency table

Predicted

Actual

Guessed Value	Correct Value		
	A 2	B 0	C 1
	D 1	E 2	F 0
	G 1	H 1	I 1

How do you compute TP ?

2. Generalizing the 2-by-2 contingency table

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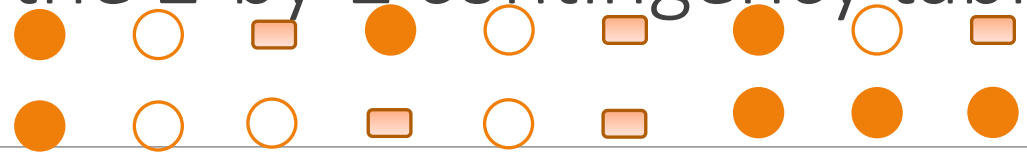
Actual



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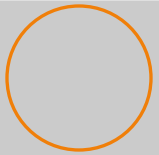
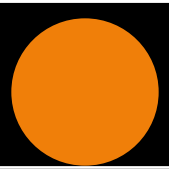
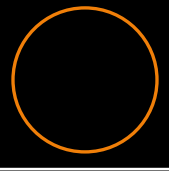
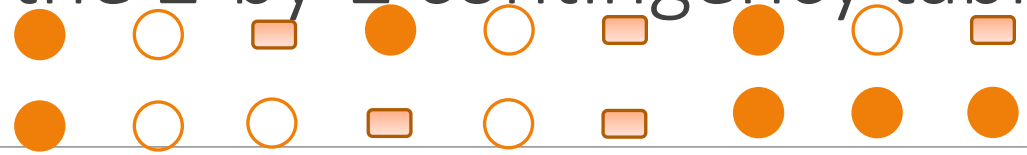
			
	A 2	B 0	C 1
	D 1	E 2	F 0
	G 1	H 1	I 1

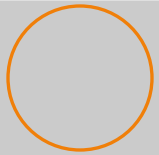
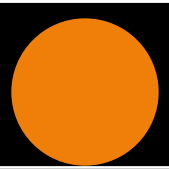
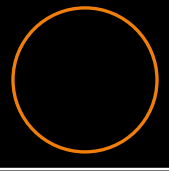
How do you compute FN  ?

2. Generalizing the 2-by-2 contingency table

Predicted

Actual



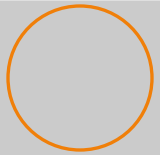
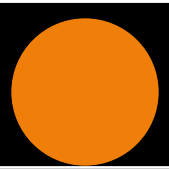
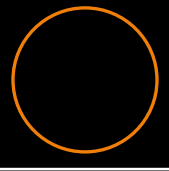
Guessed Value	Correct Value		
			
	A 2	B 0	C 1
	D 1	E 2	F 0
	G 1	H 1	I 1

How do you compute FN  ?

2. Generalizing the 2-by-2 contingency table

Predicted

Actual

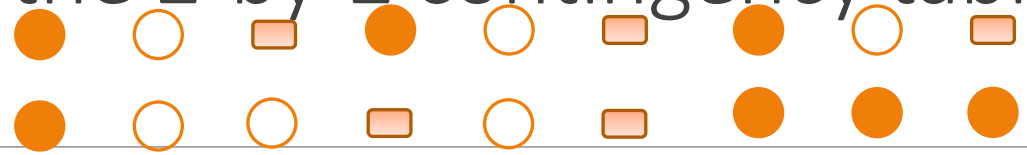
		Correct Value		
				
Guessed Value		A 2	B 0	C 1
		D 1	E 2	F 0
		G 1	H 1	I 1

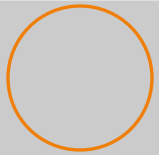
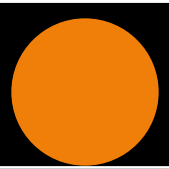
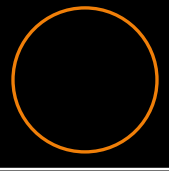
How do you compute $FP_{\square}$?

2. Generalizing the 2-by-2 contingency table

Predicted

Actual

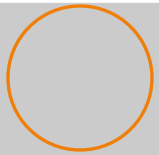
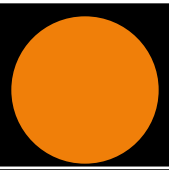
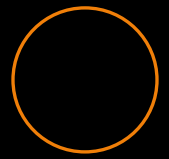


Guessed Value	Correct Value		
			
	A 2	B 0	C 1
	D 1	E 2	F 0
	G 1	H 1	I 1

How do you compute $FP_{\square}$?

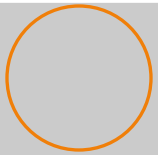
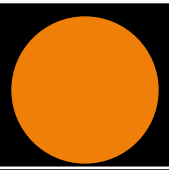
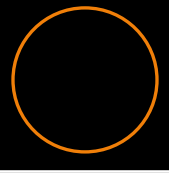
Generalizing the 2-by-2 contingency table

Q: Is this a good result?

		Correct Value		
				
Guessed Value		80	9	11
		7	86	7
		2	8	9

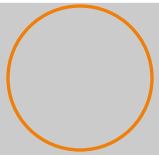
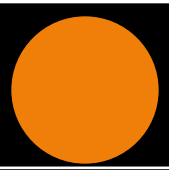
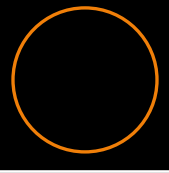
Generalizing the 2-by-2 contingency table

Q: Is this a good result?

Guessed Value	Correct Value: 		
	30	40	30
	25	30	50
	30	35	35

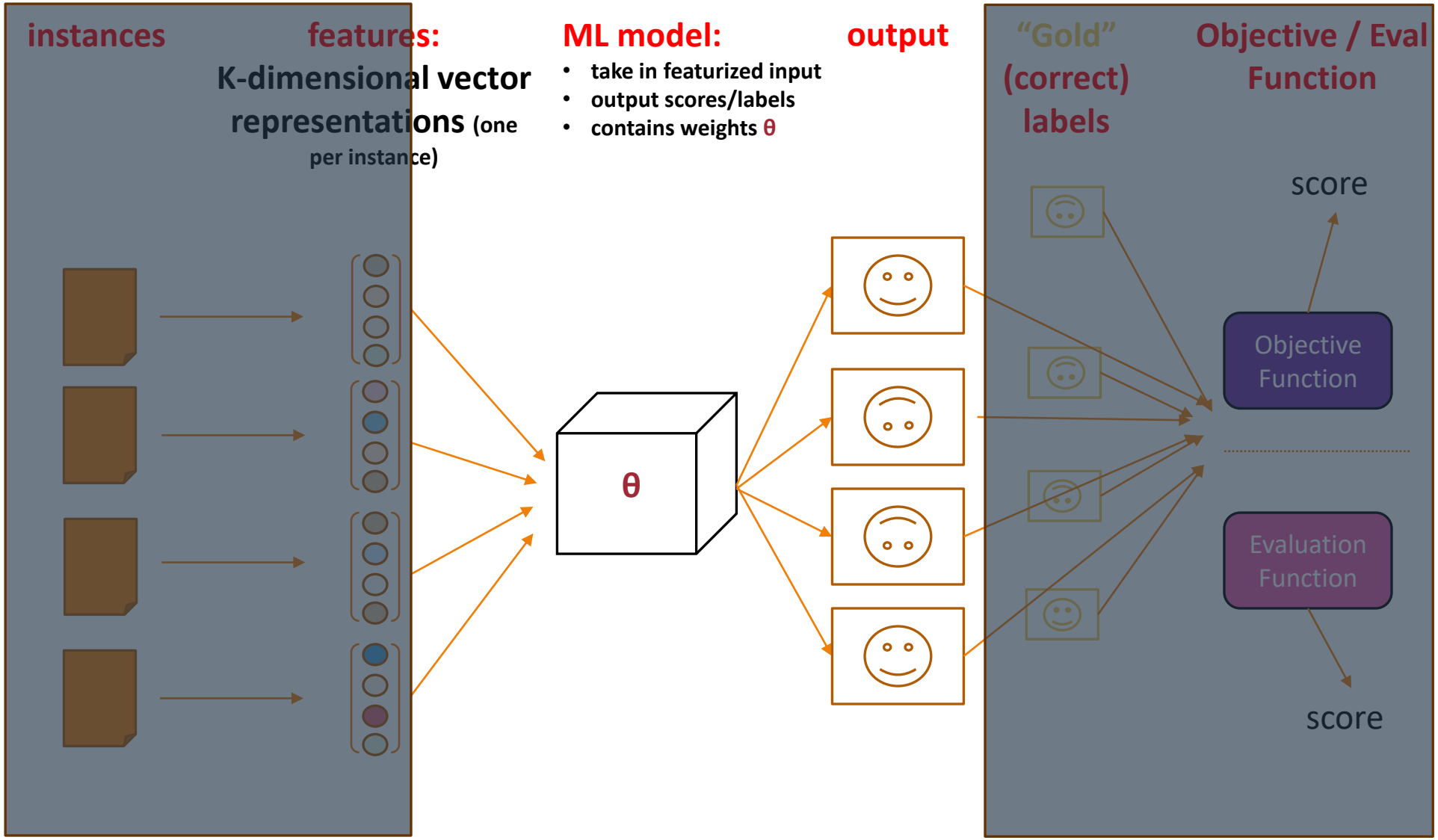
Generalizing the 2-by-2 contingency table

Q: Is this a good result?

		Correct Value		
				
Guessed Value		7	3	90
		4	8	88
		3	7	90

Classification

Defining the Model



Terminology

common NLP term	Log-Linear Models
as statistical regression	(Multinomial) logistic regression
	Softmax regression
based in information theory	Maximum Entropy models (MaxEnt)
a form of	Generalized Linear Models
viewed as	Discriminative Naïve Bayes
to be cool today	Very shallow (sigmoidal) neural nets

Maxent Models are Flexible

Maxent models can be used:

- to design discriminatively trained classifiers, or
- to create featureful language models

(among other approaches in NLP and ML more broadly)

Examining Assumption 3 Made for Classification Evaluation

Given X, our classifier produces a score for each possible label

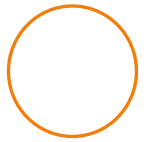
Normally (*but this can be adjusted!)

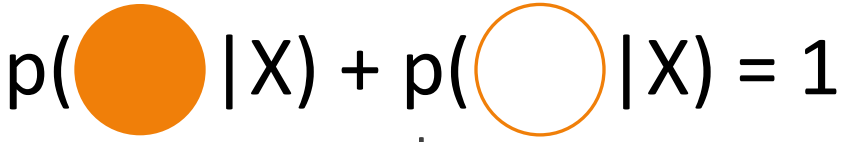
$$\text{best label} = \arg\max_{\text{label}} P(\text{label}|\text{example})$$

Terminology: Posterior Probability

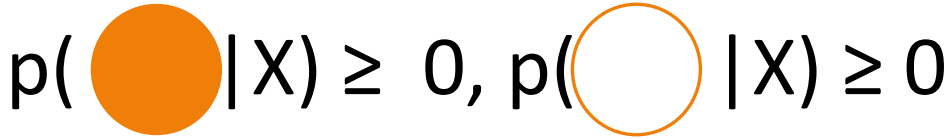
Posterior probability:

These are conditional probabilities

- If  and  are the only two options:



and



Bayes' Rule

Likelihood Prior

$$\frac{P(X|Y)\cdot P(Y)}{P(X)}$$

Posterior: $P(Y|X)$

Posterior probability: probability of event Y with knowledge that X has occurred

NLP pg. 450

Terminology (with variables)

Posterior probability:

$$p(Y = \text{label}_1 \mid X) \text{ vs. } p(Y = \text{label}_0 \mid X)$$

Conditional probabilities:

$$p(Y = \text{label}_1 \mid X) + p(Y = \text{label}_0 \mid X) = 1$$

$$p(Y = \text{label}_1 \mid X) \geq 0,$$
$$p(Y = \text{label}_0 \mid X) \geq 0$$

Conditional probability: probability of event Y, assuming event X happens too

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💡 Key Take-away 💡

We will ***learn*** this

$$p(Y \mid X)$$

Maxent Models for Classification: Discriminatively or …

Directly model the posterior

$$p(Y \mid X) = \mathbf{maxent}(X; Y)$$

Discriminatively trained classifier

Maxent Models for Classification: Discriminatively or Generatively Trained

Directly model the posterior

$$p(Y \mid X) = \mathbf{maxent}(X; Y)$$

Discriminatively trained classifier

Model the posterior with Bayes rule

$$p(Y \mid X) \propto \mathbf{maxent}(X \mid Y)p(Y)$$

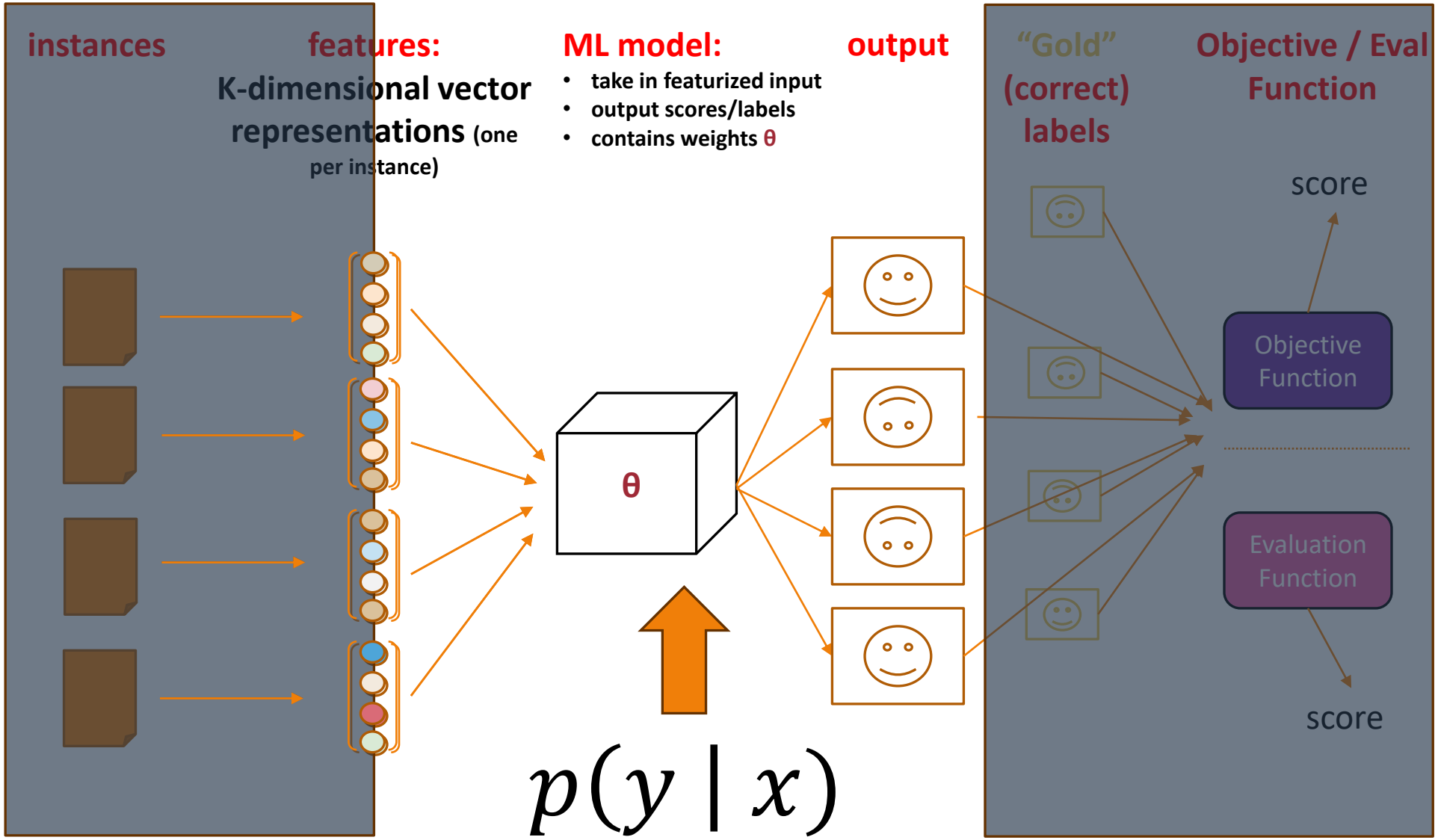
Generatively trained classifier with maxent-based language model

Maximum Entropy (Log-linear) Models For Discriminatively Trained Classifiers

(we'll start with this one)

$$p(y \mid x) = \text{maxent}(x, y)$$

discriminatively trained:
classify in one go



$$p(y \mid x) = \text{maxent}(x, y)$$

Core Aspects to Maxent Classifier p(y|x)

We need to define:

- **features** $f(x)$ from x that are meaningful;
- **weights** θ (at least one per feature, often one per feature/label combination) to say how important each feature is; and
- a way to **form probabilities** from f and θ

Overview of Featurization

Common goal: probabilistic classifier p(y | x)

Often done by defining **features** between x and y that are meaningful

- Denoted by a **general vector of K features**

$$f(x) = (f_1(x), \dots, f_K(x))$$

Features can be thought of as "soft" rules

- **E.g., POSITIVE sentiments tweets *may* be more likely to have the word "happy"**

Review: Document Classification via Bag-of-Words Features (Example)

Amazon acquired MGM in 2022, taking over a sprawling library that includes more than 4,000 feature films and 17,000 television shows. The tech behemoth also earned the rights to distribute all the Bond movies, but the new deal solidifies the company's oversight of Bond's big-screen future.

TECH

NOT TECH

Core assumption: the label can be predicted from counts of individual word types

With V word types, define V feature functions $f_i(x)$ as

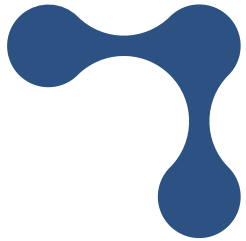
$f_i(x)$ =# of times word type *i* appears in document x

$$f(x) = \left(f_i(x)\right)_i^V$$

feature $f_i(x)$	value
Amazon	1
acquired	1
behemoth	1
Bond	2
…	
sniffle	0
…	

Adapted from https://www.nbcnews.com/pop-culture/movies/amazon-taking-control-james-bond-movie-franchise-rcna192967

Example Classification Tasks



GLUE
https://gluebenchmark.com/
🤗datasets: glue

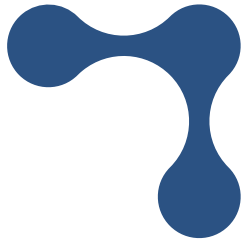
GLUE Tasks

Name	Download
The Corpus of Linguistic Acceptability	
The Stanford Sentiment Treebank	
Microsoft Research Paraphrase Corpus	
Semantic Textual Similarity Benchmark	
Quora Question Pairs	
MultiNLI Matched	
MultiNLI Mismatched	
Question NLI	
Recognizing Textual Entailment	
Winograd NLI	
Diagnostics Main	

SuperGLUE T

Name	Identifier
Broadcoverage Diagnostics	AX-b
CommitmentBank	CB
Choice of Plausible Alternatives	COPA
Multi-Sentence Reading Comprehension	MultiRC
Recognizing Textual Entailment	RTE
Words in Context	WiC
The Winograd Schema Challenge	WSC
BoolQ	BoolQ
Reading Comprehension with Commonsense Reasoning	ReCoRD
Winogender Schema Diagnostics	AX-g

SuperGLUE
https://super.gluebenchmark.com/
🤗datasets: super_glue

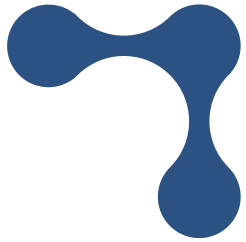


Recognizing Textual Entailment (RTE)

Given a premise sentence s and hypothesis sentence h, determine if h "follows from" s

ENTAILMENT (yes):

NOT ENTAILED (no):



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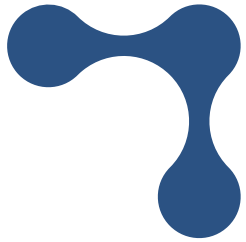
ENTAILMENT (yes):

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

h: The Bulls basketball team is based in Chicago.

NOT ENTAILED (no):



Recognizing Textual Entailment (RTE)

Given a premise sentence s and hypothesis sentence h, determine if h "follows from" s

ENTAILMENT (yes):

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

h: The Bulls basketball team is based in Chicago.

NOT ENTAILED (no):

s: Based on a worldwide study of smoking-related fire and disaster data, UC Davis epidemiologists show smoking is a leading cause of fires and death from fires globally.

h: Domestic fires are the major cause of fire death.

RTE

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
h: The Bulls basketball team is based in Chicago.

ENTAILED

p(ENTAILED | s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships. h: The Bulls basketball team is based in Chicago.)

Discriminative Document Classification

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

h: The Bulls basketball team is based in Chicago.

ENTAILED

Discriminative Document Classification

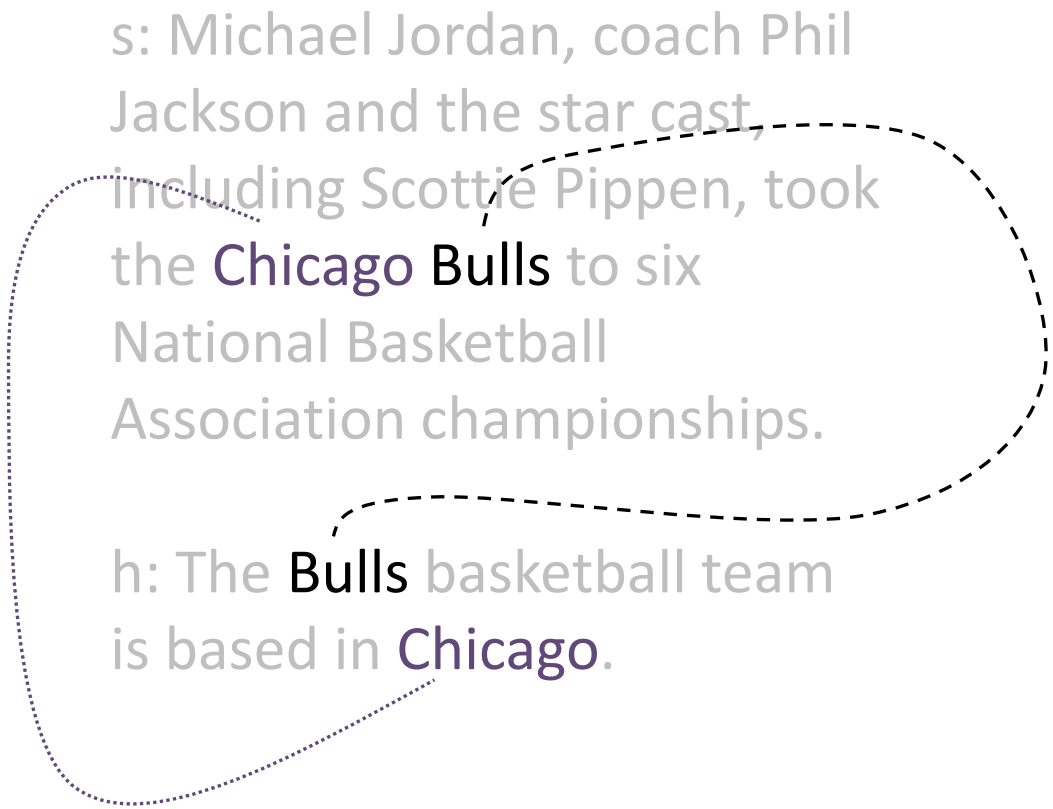
s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.

h: The Bulls basketball team is based in Chicago.

ENTAILED

These extractions are all **features** that have **fired** (likely have some significance)

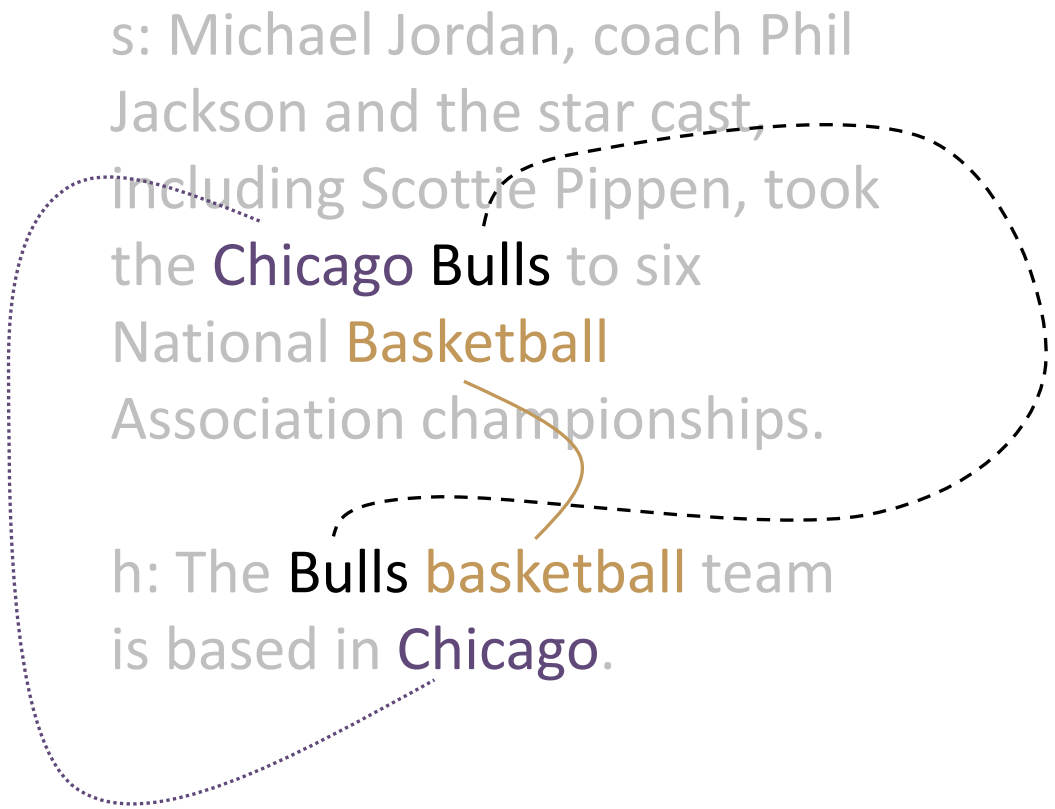
Discriminative Document Classification



ENTAILED

These extractions are all **features** that have **fired** (likely have some significance)

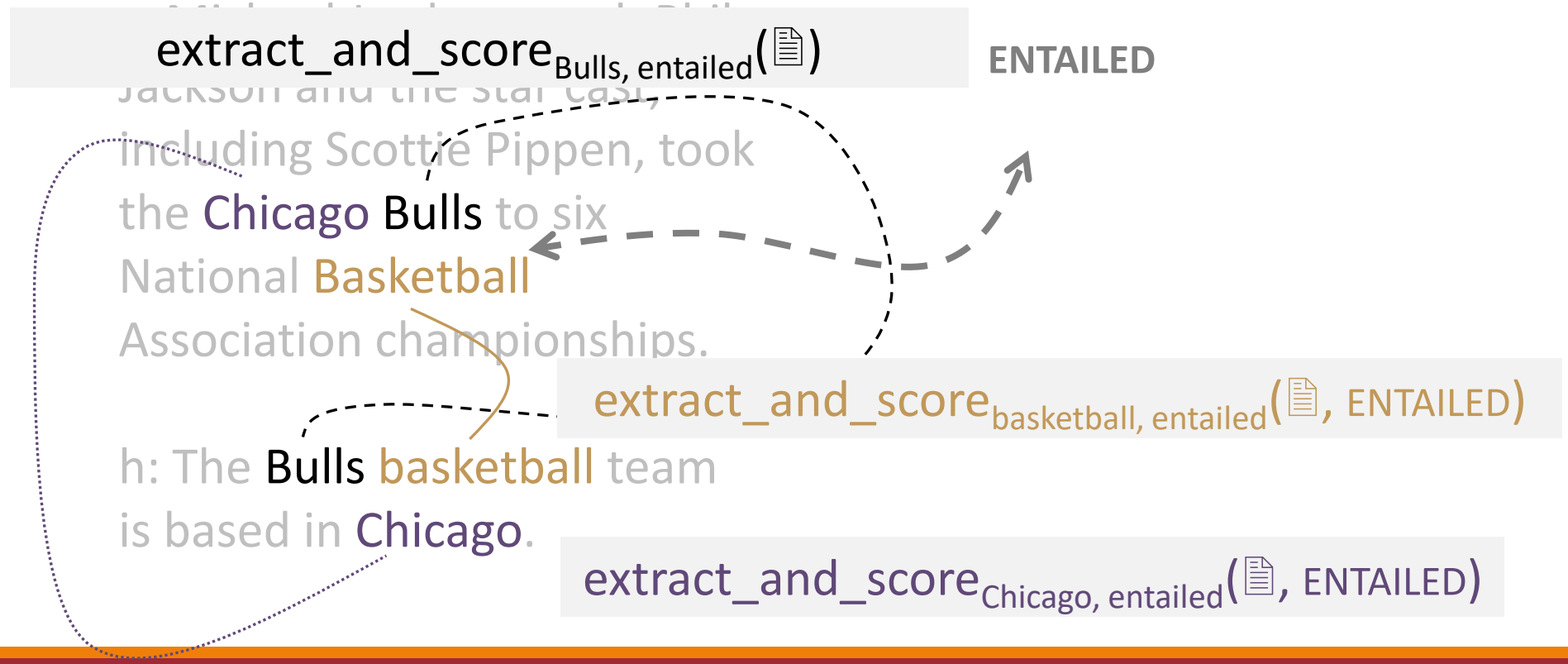
Discriminative Document Classification



ENTAILED

These extractions are all **features** that have **fired** (likely have some significance)

We need to *score* the different extracted clues.



Score and Combine Our Clues

$score_{1,\ Entailed}$(📄)

$score_{2\ ,\ Entailed}$(📄)

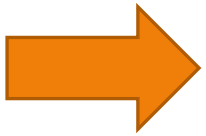
$score_{3\ ,\ Entailed}$(📄)

…

$score_{k\ ,\ Entailed}$(📄)

…

COMBINE



posterior probability of ENTAILED

Scoring Our Clues

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
h: The Bulls basketball team is based in Chicago.

$$\text{score}(\quad, \text{ENTAILED}) =$$

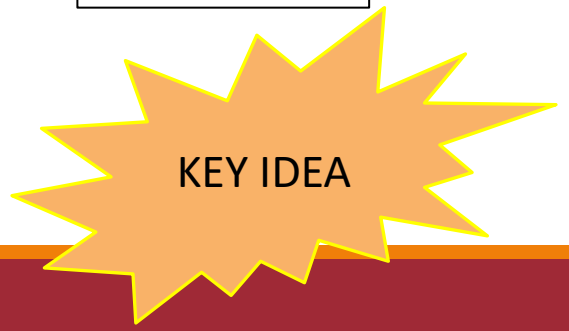
(ignore the feature indexing for now)

$$\text{score}_{1\ ,\ \text{Entailed}}(\text{📄}) +$$
$$\text{score}_{2\ ,\ \text{Entailed}}(\text{📄}) +$$
$$\text{score}_{3\ ,\ \text{Entailed}}(\text{📄}) +$$
$$\ldots$$

Turning Scores into Probabilities

score(s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships. h: The Bulls basketball team is based in Chicago. , ENTAILED) > score(s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships. h: The Bulls basketball team is based in Chicago. , NOT ENTAILED)

p(ENTAILED | s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships. h: The Bulls basketball team is based in Chicago.) > p(NOT ENTAILED | s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships. h: The Bulls basketball team is based in Chicago.)



Turning Scores into Probabilities (More Generally)

$$\text{score}(x, y_1) > \text{score}(x, y_2)$$

$$p(y_1 \mid x) > p(y_2 \mid x)$$

KEY IDEA

Maxent Modeling

What function G…

operates on any real number?

is never less than 0?

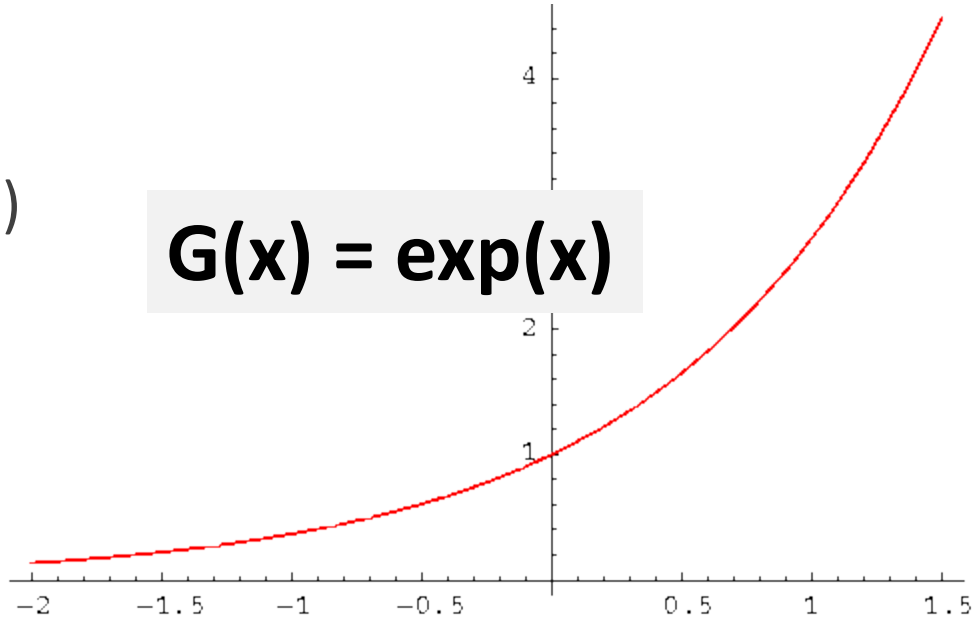
is monotonic? ($a < b \rightarrow G(a) < G(b)$)

What function G…

operates on any real number?

is never less than 0?

is monotonic? (a < b ➔ G(a) < G(b))



Maxent Modeling

$$p(\text{ENTAILED} \mid s, h) \propto$$

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
h: The Bulls basketball team is based in Chicago.

$$\exp(\text{score}(s, h, \text{ENTAILED}))$$

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
h: The Bulls basketball team is based in Chicago.

Maxent Modeling

$$p(\ \text{ENTAILED}\ |\ s\ )\propto$$

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
h: The Bulls basketball team is based in Chicago.

$$\exp(\ \text{score}_{1,\text{Entailed}}(\text{📄}) + \text{score}_{2,\text{Entailed}}(\text{📄}) + \text{score}_{3,\text{Entailed}}(\text{📄}) + \ldots\ ))$$

Maxent Modeling

$$p(\ \text{ENTAILED}\ |\ \text{s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships. h: The Bulls basketball team is based in Chicago.}\ ) \propto$$

$$\exp\Big(\ \text{weight}_{1,\ \text{Entailed}} * \text{applies}_1(\text{📄}) + \text{weight}_{2,\ \text{Entailed}} * \text{applies}_2(\text{📄}) + \text{weight}_{3,\ \text{Entailed}} * \text{applies}_3(\text{📄}) + \ldots\ \Big)$$

Maxent Modeling

$$p(\ \text{ENTAILED}\ |\ \text{s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships. h: The Bulls basketball team is based in Chicago.}\ ) \propto$$

$$\exp\Big(\ \text{weight}_{1,\ \text{Entailed}} * \text{applies}_1(\text{📄}) + \text{weight}_{2,\ \text{Entailed}} * \text{applies}_2(\text{📄}) + \text{weight}_{3,\ \text{Entailed}} * \text{applies}_3(\text{📄}) + \ldots\ \Big)$$

K different weights…

for K different features

Maxent Modeling

$$p(\text{ENTAILED} \mid \text{s, h}) \propto \exp\Big(\sum_{K} \text{weight}_{K,\text{Entailed}} * \text{applies}_{K}(\text{s, h})\Big)$$

s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships.
h: The Bulls basketball team is based in Chicago.

$$\text{weight}_{1,\text{Entailed}} * \text{applies}_1(\text{s, h}) + \text{weight}_{2,\text{Entailed}} * \text{applies}_2(\text{s, h}) + \text{weight}_{3,\text{Entailed}} * \text{applies}_3(\text{s, h}) + \dots$$

K different weights…

for K different features

multiplied and then summed

Maxent Modeling

$$p(\ \text{ENTAILED}\ |\ \text{s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships. h: The Bulls basketball team is based in Chicago.}\ ) \propto$$

$$\exp(\text{Dot\_product of Entailed weight\_vec feature\_vec(📄)})$$

K different weights…

for K different features

multiplied and then summed

Maxent Modeling

$$p(\ \text{ENTAILED} \mid \text{s: Michael Jordan, coach Phil Jackson and the star cast, including Scottie Pippen, took the Chicago Bulls to six National Basketball Association championships. h: The Bulls basketball team is based in Chicago.}\ ) \propto$$

$$\exp(\ \theta^T_{\text{ENTAILED}} f(\ \text{  }\ )\ )$$

K different weights…

for K different features

multiplied and then summed

Knowledge Check: Data Prep

https://colab.research.google.com/drive/19yg0EUXQtHozBiSuO6cKOBhoSPzQHgug?usp=sharing