

Practice Problem 2.10 (solution page 182)

As an application of the property that $a \wedge a = 0$ for any bit vector a , consider the following program:

```

1 void inplace_swap(int *x, int *y) {
2     *y = *x ^ *y; /* Step 1 */
3     *x = *x ^ *y; /* Step 2 */
4     *y = *x ^ *y; /* Step 3 */
5 }

```

As the name implies, we claim that the effect of this procedure is to swap the values stored at the locations denoted by pointer variables x and y . Note that unlike the usual technique for swapping two values, we do not need a third location to temporarily store one value while we are moving the other. There is no performance advantage to this way of swapping; it is merely an intellectual amusement.

Starting with values a and b in the locations pointed to by x and y , respectively, fill in the table that follows, giving the values stored at the two locations after each step of the procedure. Use the properties of \wedge to show that the desired effect is achieved. Recall that every element is its own additive inverse (that is, $a \wedge a = 0$).

Step	*x	*y
Initially	a	b
Step 1	a	$a \wedge b$
Step 2	b	$a \wedge b$
Step 3	b	a

$$\text{Step 1. } *y = *x \wedge *y = a \wedge b$$

$$\begin{aligned} \text{Step 2. } *x &= *x \wedge *y = a \wedge (a \wedge b) \\ &= (a \wedge a) \wedge b \\ &= 0 \wedge b \\ &= b \end{aligned}$$

$$\begin{aligned} \text{Step 3. } *y &= *x \wedge *y = b \wedge (a \wedge b) \\ &= a \wedge (b \wedge b) \\ &= a \wedge 0 \\ &= a \end{aligned}$$