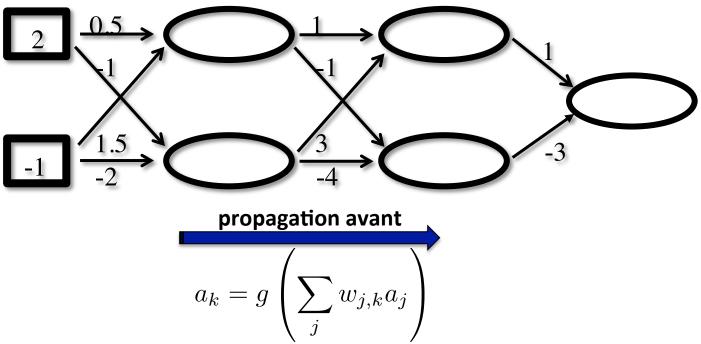
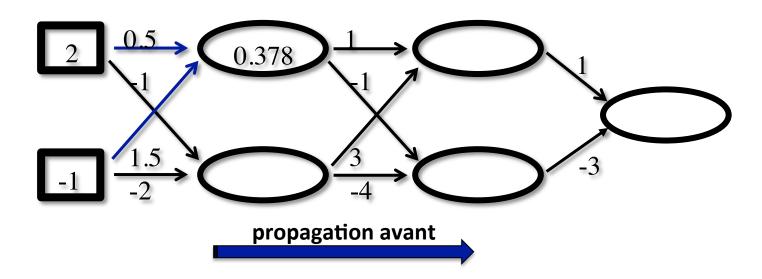
```
function BACK-PROP-LEARNING(examples, network) returns a neural network
  inputs: examples, a set of examples, each with input vector x and output vector y
           network, a multilayer network with L layers, weights w_{i,j}, activation function g
  local variables: \Delta, a vector of errors, indexed by network node
    for each weight w_{i,j} in network do
        w_{i,j} \leftarrow a small random number
   repeat
       for each example (x, y) in examples do
           /* Propagate the inputs forward to compute the outputs */
           for each node i in the input layer do
               a_i \leftarrow x_i
           for \ell = 2 to L do
               for each node j in layer \ell do
                   in_j \leftarrow \sum_i w_{i,j} a_i
                   a_i \leftarrow q(in_i)
           /* Propagate deltas backward from output layer to input layer */
           for each node j in the output layer do
               \Delta[j] \leftarrow y_j - a_j \quad (= -\partial Loss/\partial in_j)
           for \ell = L - 1 to 1 do
               for each node i in layer \ell do
                   \Delta[i] \leftarrow g(in_i)(1 - g(in_i)) \sum_{i} w_{i,j} \Delta[j]
           /* Update every weight in network using deltas */
           for each weight w_{i,j} in network do
              w_{i,j} \leftarrow w_{i,j} + \alpha \times a_i \times \Delta[j]
  until some stopping criterion is satisfied
  return network
```

 $Logistic(\cdot) \equiv g(\cdot)$ (pour simplifier notation)

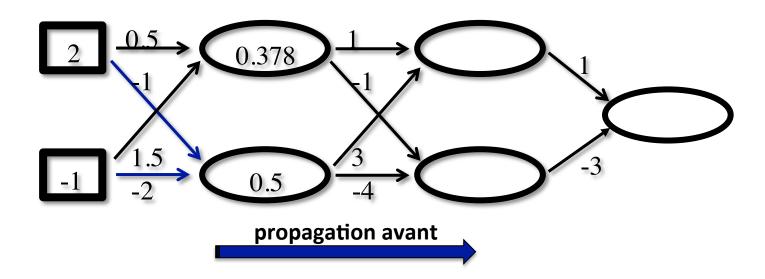
• Exemple: x = [2, -1], y = 1



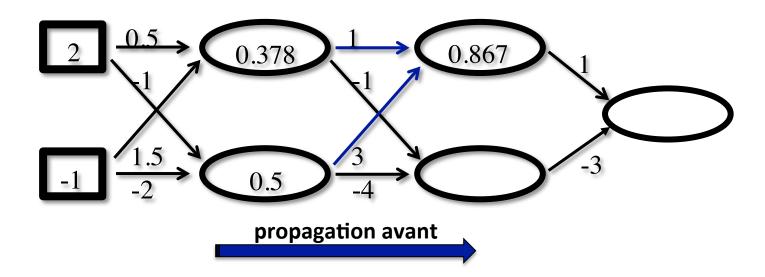
Hugo Larochelle et Froduald Kabanza



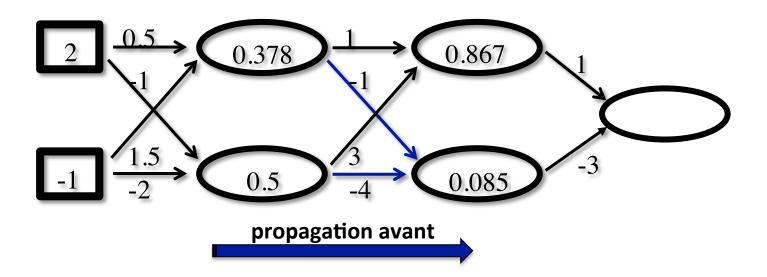
$$Logistic(0.5 * 2 + 1.5 * -1) = Logistic(-0.5) = 0.378$$



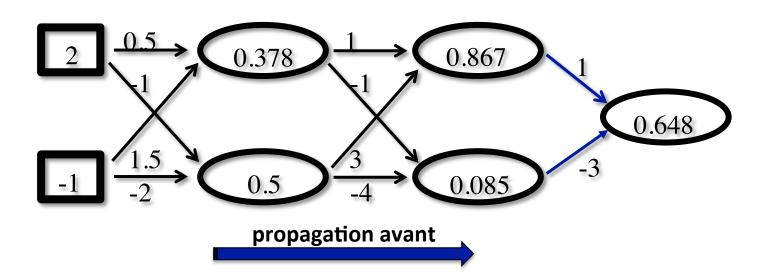
$$Logistic(-1 * 2 + -2 * -1) = Logistic(0) = 0.5$$



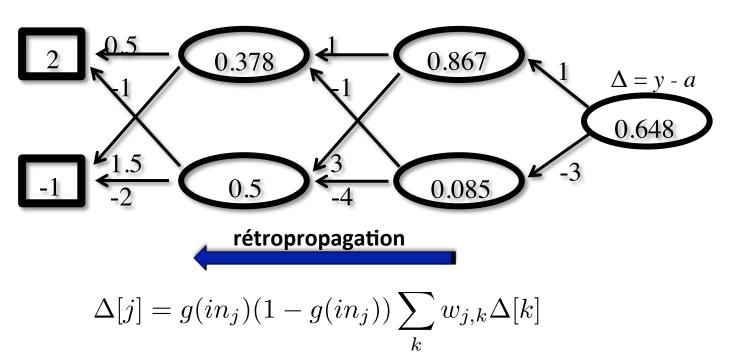
$$Logistic(1 * 0.378 + 3 * 0.5) = Logistic(1.878) = 0.867$$

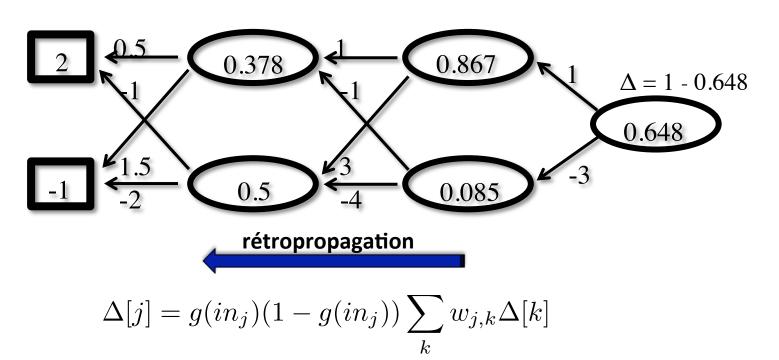


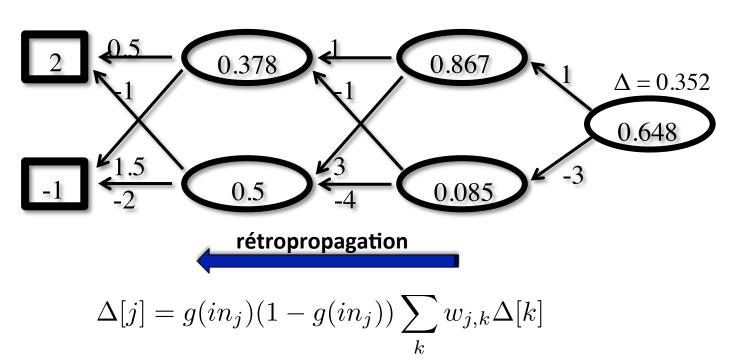
$$Logistic(-1 * 0.378 + -4 * 0.5) = Logistic(-2.378) = 0.085$$

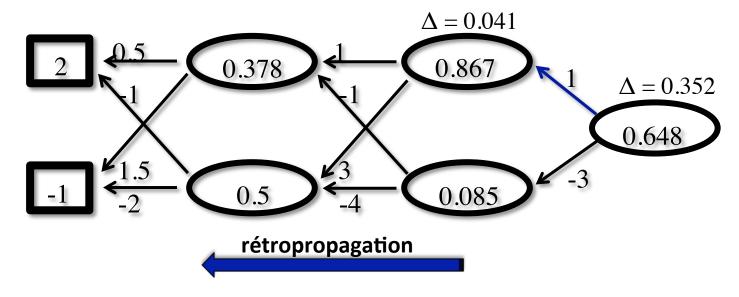


$$Logistic(1 * 0.867 + -3 * 0.085) = Logistic(0.612) = 0.648$$

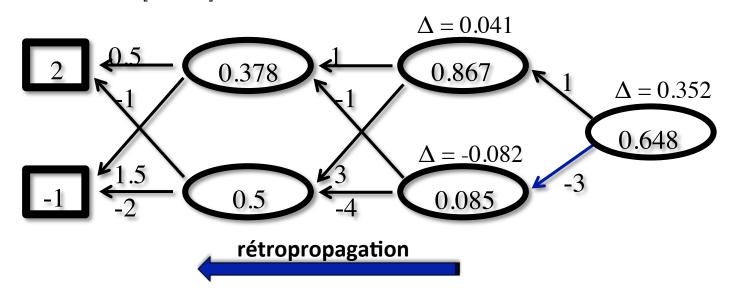




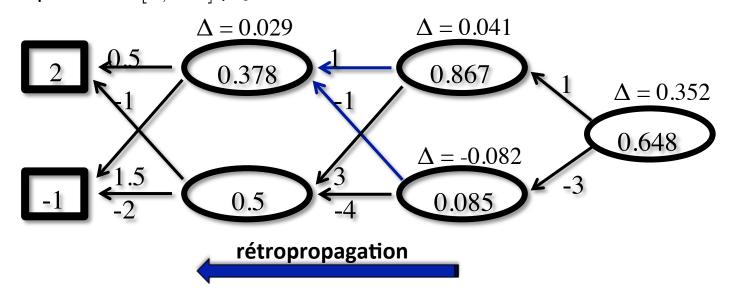




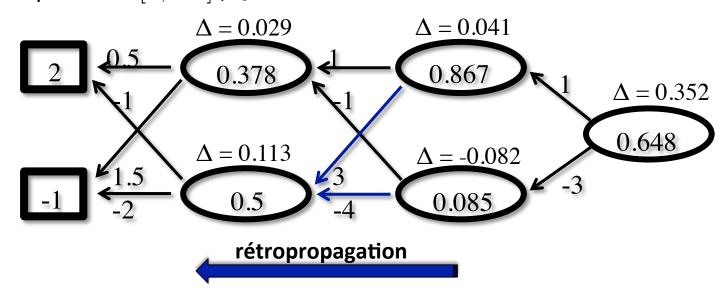
$$\Delta = 0.867 * (1-0.867) * 1 * 0.352 = 0.041$$



$$\Delta = 0.085 * (1-0.085) * -3 * 0.352 = -0.082$$

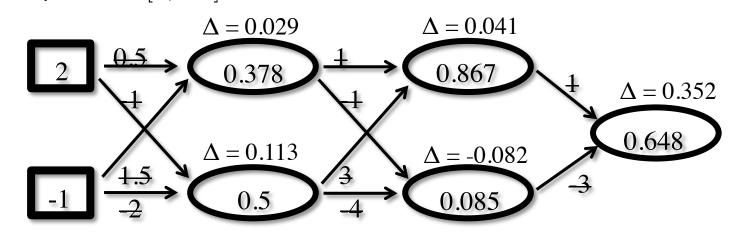


$$\Delta = 0.378 * (1-0.378) * (1 * 0.041 + -1 * -0.082) = 0.029$$



$$\Delta = 0.5 * (1-0.5) * (3 * 0.041 + -4 * -0.082) = 0.113$$

• Exemple: $\mathbf{x} = [2, -1]$, y = 1



$$w_{1,3} \leftarrow 0.5 + 0.1 * 2 * 0.029 = 0.506$$

 $w_{1,4} \leftarrow -1 + 0.1 * 2 * 0.113 = -0.977$
 $w_{2,3} \leftarrow 1.5 + 0.1 * -1 * 0.029 = 1.497$

 $w_{3.6} \leftarrow -1 + 0.1 * 0.378 * -0.082 = -1.003$ $w_{4.5} \leftarrow 3 + 0.1 * 0.5 * 0.041 = 3.002$ $w_{24} \leftarrow -2 + 0.1 * -1 * 0.113 = -2.011$ $w_{4.6} \leftarrow -4 + 0.1 * 0.5 * -0.082 = -4.004$

mise à jour (α =0.1)

 $w_{3.5} \leftarrow 1 + 0.1 * 0.378 * 0.041 = 1.002$

15 Hugo Larochelle et Froduald Kabanza $w_{57} \leftarrow 1 + 0.1 * 0.867 * 0.352 = 1.031$ $w_{67} \leftarrow -3 + 0.1 * 0.085 * 0.352 = -2.997$