

## POST-PROCESSING ASSIGNMENT

ME765 - Special Topics in Fluid Mechanics  
High-speed and compressible flows  
Fall 2018

**Submission deadline: November 1st at 11:59pm**

### Description:

You are provided with an under-resolved Direct Numerical Simulation (DNS) of a compressible channel flow with differentially heated walls. The single snapshot of the three-dimensional simulation takes up about 700 Mb with a structured grid of just over 31 million grid points ( $512 \times 240 \times 256$ ). For reference, the resolved simulation required just over 3 billion grid points. The grid is homogeneous in the streamwise,  $x$ , and spanwise,  $z$ , directions; in these homogeneous directions, the boundaries assumes periodicity. A wall-clustering is used in the wall-normal direction,  $y$ ; the grid locations in  $y$  are provided and should be used. The data is provided in Matlab format and binary format with a python script to access the data. You are provided with the following three-dimensional data:  $\rho$ ,  $\rho U$ ,  $\rho V$ ,  $\rho W$ ,  $\rho E$ . Note that  $\rho E = \rho(e + \frac{1}{2}(U^2 + V^2 + W^2))$ . The data is fully non-dimensionalized. The following information is provided:

- $(Lx, Ly, Lz) = (6\pi, 2, 2\pi)$
- $\gamma = 1.4$  and  $Pr = 0.72$
- Universal gas constant  $R = 0.31745$  (with consistent non-dimensionalization)

### Accessing the database:

- Matlab format (about 700 Mb):  
<https://drive.google.com/file/d/1uk90r885yJoVvTpG0-uGucWgD3g7RfHu/view?usp=sharing>
- Generic binary format (about 700 Mb):  
<https://drive.google.com/file/d/1eiTqiBQvjIpo6VdJbJzt00Q6ZS2c1S-I/view?usp=sharing>
- Python script to read generic binary:  
<https://drive.google.com/file/d/15GkZA4EBQbHbZtu57KQE3LUGBWzU1-bq/view?usp=sharing>
- Grid locations in the wall-normal direction:  
<https://drive.google.com/file/d/11TMxvNLx08IWe-PUm7TMfIvZQ1CdfP3U/view?usp=sharing>

## Questions:

1. Plot the average streamwise velocities (all in one figure):  $\overline{U}(y)$ ,  $\overline{V}(y)$ , and  $\overline{W}(y)$ .
2. Plot the following turbulence statistics (all in one figure):  $\overline{u'u'}(y)$ ,  $\overline{v'v'}(y)$ ,  $\overline{w'w'}(y)$ ,  $\overline{u'v'}(y)$ ,  $\overline{u'w'}(y)$ , and  $\overline{v'w'}(y)$ .
3. Plot the average Mach number:  $\overline{M}(y)$ .
4. Plot the average temperature profile:  $\overline{T}(y)$ .
5. Compute the average temperature gradient at the bottom and top wall.
6. Compute the average centerline and bulk Mach number.
7. Compute the planar average dilatation and show, at each  $y$  location, the minimum and maximum dilatation.
8. Plot the spectrum of the turbulent kinetic energy and dilatation at given  $y$  location.
9. Compute the ratio of grid spacing to the local Kolmogorov length scale.