```
opts_chunk$set (warning = FALSE, message = FALSE, tidy=TRUE, echo=TRUE)
options(warn = -1)
rm(list=ls())
library(survival)
library(knitr)
library(kableExtra)
library(glmnet)
## Loading required package: Matrix
## Loaded glmnet 4.1-7
library(ggplot2)
# Following loaded in "forest_search_v0.R"
suppressMessages(library(randomForest))
#library(SPlit)
library(grf)
library(policytree)
library(DiagrammeR)
#library(cowplot)
library(data.table)
library(plyr)
library(aVirtualTwins)
# Not sure formatR is needed?
#library(formatR)
suppressMessages(library(gridExtra))
library(speff2trial)
## Loading required package: leaps
# Location where code is stored
# Modified for MAC
codepath<-c("/Users/larryleon/Documents/GitHub/forestSearch/R/")</pre>
source(paste0(codepath, "source_forestsearch_v0.R"))
source_fs_functions(file_loc=codepath)
# Output grf, fs, and fs bootstrap
#outgrf<-c("output/actg_2v3_grf.Rdata")</pre>
#outfs<-c("output/actg_2v3_fs.Rdata")</pre>
# Boots=10000
outfsboot<-c("output/actg_2v3_fsboot_B=10k.Rdata")</pre>
# Set to null if not outputting
outgrf<-NULL
outfs<-NULL
#outfsboot<-NULL
```

```
t.start.all <- proc.time()[3]
# GRF analysis To guide selection of binary cutpoints</pre>
```

```
df.analysis <- subset(ACTG175, arms %in% c(2, 3))</pre>
df.analysis <- within(df.analysis, {</pre>
   id <- as.numeric(c(1:nrow(df.analysis)))</pre>
   time_days <- days
   treat <- ifelse(arms == 2, 1, 0)
})
# plot(survfit(Surv(time_days,cens)~treat,data=df.analysis))
coxph(Surv(time_days, cens) ~ treat, data = df.analysis)
## Call:
## coxph(formula = Surv(time_days, cens) ~ treat, data = df.analysis)
##
           coef exp(coef) se(coef)
## Likelihood ratio test=0.72 on 1 df, p=0.3974
## n= 1085, number of events= 237
confounders.name <- c("age", "wtkg", "karnof", "cd40", "cd80", "hemo", "homo", "drugs",
    "race", "gender", "oprior", "symptom")
outcome.name <- c("time_days")</pre>
event.name <- c("cens")</pre>
id.name <- c("id")</pre>
treat.name <- c("treat")</pre>
n.min < -60
dmin.grf <- 12
frac.tau <- 0.8
grf.est <- grf.subg.harm.survival(data = df.analysis, confounders.name = confounders.name,
   outcome.name = outcome.name, event.name = event.name, id.name = id.name, treat.name = treat.name,
   n.min = n.min, dmin.grf = dmin.grf, frac.tau = frac.tau, details = TRUE)
## tau= 816.8
     leaf.node control.mean control.size control.se treated.mean treated.size
## 1
          2 -22.534852 827.000000 9.297449 22.534852 827.000000
## 2
            3
                21.827794 258.000000 20.578104 -21.827794
                                                               258.000000
## 3
            4 17.855279 172.000000 18.338238 -17.855279 172.000000
## 4
           5 -81.423480 126.000000 28.077435 81.423480 126.000000
            6 -30.446957 518.000000 11.140013
                                                  30.446957 518.000000
## 5
            7 37.007518 269.000000 20.531196 -37.007518 269.000000
## 6
## 31
           10 -39.907373 456.000000 12.953776 39.907373 456.000000
## 41
           11
                 8.402547 181.000000 10.438682 -8.402547 181.000000
            12
               -82.936355 112.000000 29.182517
                                                    82.936355
## 51
                                                               112.000000
## 61
           13 73.841749 124.000000 25.966441 -73.841749
                                                              124.000000
## 7
           14 104.097341
                           64.000000 56.110380 -104.097341
                                                              64.000000
          15 -72.389931
                           81.000000 30.391589
                                                  72.389931
## 8
                                                               81.000000
##
      treated.se
                      diff depth
## 1
       9.297449 -45.06970
                             1
## 2
     20.578104 43.65559
                              1
       18.338238 35.71056
                               2
## 3
## 4
       28.077435 -162.84696
                               2
## 5
       11.140013 -60.89391
                               2
## 6
       20.531196 74.01504
                               2
```

```
## 31 12.953776 -79.81475
## 41 10.438682 16.80509
                                3
## 51 29.182517 -165.87271
                                3
                                3
## 61 25.966441 147.68350
       56.110380 208.19468
## 7
                                3
## 8
       30.391589 -144.77986
                                3
## leaf.node control.mean control.size control.se treated.mean treated.size
## 7
      14 104.09734 64.00000 56.11038 -104.09734 64.00000
## treated.se
                  diff depth
## 7 56.11038 208.1947
cat("Truncation point for RMST:", c(grf.est$tau.rmst), "\n")
## Truncation point for RMST: 816.8
# Plot manually
# plot(qrf.est£tree) plot(qrf.est£tree1) plot(qrf.est£tree2)
# plot(grf.est£tree3)
df0.grf <- subset(grf.est$data, treat.recommend == 0)</pre>
df1.grf <- subset(grf.est$data, treat.recommend == 1)</pre>
# Terminal leaf corresponding to selected SG
cat("Terminal leaf:", c(grf.est$sg.harm.id), "\n")
## Terminal leaf: karnof <= 90
# action=1 --> recommend control
# Manually identify the subgroup looking at tree and terminal leaf
print(dim(df0.grf))
## [1] 64 34
check <- subset(df.analysis, karnof <= 90 & cd80 > 1034 & age > 37)
print(dim(check))
## [1] 64 29
# plot(survfit(Surv(time_days,cens)~treat,data=df.analysis))
# coxph(Surv(time_days,cens)~treat,data=df.analysis)
if (!is.null(outgrf)) save(grf.est, file = outgrf)
t.done <- proc.time()[3]</pre>
t.min \leftarrow (t.done - t.start.all)/60
cat("Minutes and hours for GRF estimation", c(t.min, t.min/60), "\n")
## Minutes and hours for GRF estimation 2.917367 0.04862278
t.start <- proc.time()[3]</pre>
cat("GRF variables in selected tree", "\n")
## GRF variables in selected tree
```

```
print(grf.est$tree.names)
## [1] "age"
                "cd80"
                         "wtkg"
                                 "cd40"
                                            "karnof"
cat("GRF cuts wrt selected tree:", "\n")
## GRF cuts wrt selected tree:
print(grf.est$tree.cuts)
## [1] "age <= 37"
                       "cd80 <= 499"
                                        "cd80 <= 1034" "wtkg <= 64.64"
## [5] "cd40 <= 417"
                       "cd80 <= 680"
                                        "karnof <= 90"
# Reduce dimension via Cox lasso
xx <- as.matrix(df.analysis[, confounders.name])</pre>
yy <- as.matrix(df.analysis[, c("time_days", "cens")])</pre>
colnames(yy) <- c("time", "status")</pre>
cvfit <- cv.glmnet(xx, yy, family = "cox") #first do 10-fold cross-validation to select lambda
m <- glmnet(xx, yy, family = "cox", lambda = cvfit$lambda.min) #plugin the optimal lambda
conflasso.name <- confounders.name[which(m$beta != 0)]
cat("Cox-LASSO selected:", c(conflasso.name), "\n")
## Cox-LASSO selected: age wtkg karnof cd40 cd80 drugs oprior symptom
cat("GRF cuts wrt selected tree:", "\n")
## GRF cuts wrt selected tree:
print(grf.est$tree.cuts)
## [1] "age <= 37"
                       "cd80 <= 499" "cd80 <= 1034" "wtkg <= 64.64"
## [5] "cd40 <= 417" "cd80 <= 680" "karnof <= 90"
# Considering continuous factors per GRF cuts Only *also* considering drugs and
# symptom per lasso
df.analysis <- within(df.analysis, {</pre>
   z1a <- ifelse(age <= 37, 1, 0)
    z1b <- ifelse(age <= median(age), 1, 0)</pre>
    z2 <- ifelse(wtkg <= 65, 1, 0)
    z3 <- ifelse(karnof <= 90, 1, 0)
   z4 <- ifelse(cd40 <= 417, 1, 0)
    z5a <- ifelse(cd80 <= 499, 1, 0)
    z5b \leftarrow ifelse(cd80 \leftarrow 680, 1, 0)
    z5c <- ifelse(cd80 <= 1034, 1, 0)
   # z6<-hemo z7<-homo
   z8 <- drugs
    # z9<-race z10<-gender z11<-oprior
   z12 <- symptom
   # Convert to factors
    v1a <- as.factor(z1a)
   v1b <- as.factor(z1b)</pre>
   v2 <- as.factor(z2)</pre>
```

```
v5b <- as.factor(z5b)
    v5c <- as.factor(z5c)
    v6 <- as.factor(z8)
    v7 <- as.factor(z12)
})
FSconfounders.name <- c("v1a", "v1b", "v2", "v3", "v4", "v5a", "v5b", "v5c", "v6",
    "v7")
outcome.name <- c("time_days")</pre>
event.name <- c("cens")</pre>
id.name <- c("id")</pre>
treat.name <- c("treat")</pre>
df.confounders <- df.analysis[, FSconfounders.name]</pre>
df.confounders <- dummy(df.confounders)</pre>
hr.threshold <- 1.5 # Initital candidates</pre>
hr.consistency <- 1.25 # Candidates for many splits
pconsistency.threshold <- 0.9</pre>
maxk <- 4
# maxk is max # of covariates in combination Since we want to allow generation
# of intervals for single covariate allowing for 4 can yield v1, v2 (say), and
# v3,v4 with v3 and v4 generating intervals for a single covariate
# Limit timing for forestsearch
max.minutes <- 60
nmin.fs <- 60
# stop.threshold<-0.60 # If any sg meets this, then choose this (stop here);</pre>
m1.threshold <- Inf # Turning this off (Default)
stop.threshold <- 1
# =1 will run through all sq's meeting HR criteria
fs.splits <- 1000 # How many times to split for consistency
# vi is % factor is selected in cross-validation --> higher more important
vi.grf.min <- 0.2
# Null, turns off grf screening Set to 5 for this heavily censored data
d.min <- 5 # Min number of events for both arms (d0.min=d1.min=d.min)
# default=5
sg_focus <- "hr"
split_method <- "Random"</pre>
pstop_futile <- 0.3
# Stops the consistency evaluation after first subgroup with consistency below
# pstop_futile With idea that since SG's are sorted by hazard ratio estimates,
# once consistency is below pstop_futile it seems unlikely that SG's with lower
# hr's will reach the required consistency criterion
fs.est <- forestsearch(df = df.analysis, confounders.name = FSconfounders.name, df.predict = df.analysi
    details = TRUE, sg_focus = sg_focus, split_method = split_method, pstop_futile = pstop_futile,
    outcome.name = outcome.name, treat.name = treat.name, event.name = event.name,
```

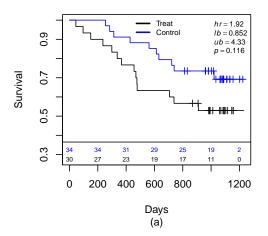
v3 <- as.factor(z3)
v4 <- as.factor(z4)
v5a <- as.factor(z5a)</pre>

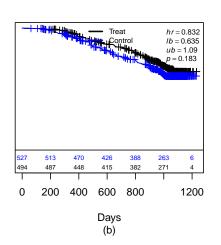
```
id.name = id.name, n.min = nmin.fs, hr.threshold = hr.threshold, hr.consistency = hr.consistency,
    fs.splits = fs.splits, stop.threshold = stop.threshold, d0.min = d.min, d1.min = d.min,
    pconsistency.threshold = pconsistency.threshold, max.minutes = max.minutes, maxk = maxk,
    plot.sg = FALSE, vi.grf.min = vi.grf.min)
## Confounders per grf screening v2 v1a v7 v3 v5b v6 v5c v1b v5a v4
## Number of possible subgroups= 1048575
## Number of possible subgroups (in millions) = 1.048575
## # of subgroups based on # variables > k.max and excluded 1042380
## k.max = 4
## Events criteria for control, exp= 5 5
## # of subgroups with events less than criteria: control, experimental 3623 3913
## # of subgroups meeting all criteria = 1441
## # of subgroups fitted (Cox model estimable) = 1441
## Minutes= 0.1167
## Number of criteria not met for subgroup evaluation
## crit.failure
##
         0
                                           4
               287
                       3237
                                         751
## 1043821
                                479
## Number of subgroups meeting HR threshold 91
## Subgroups (1st 10) meeting overall screening thresholds (HR, m1) sorted by focus: (m1,sg_focus)= Inf
          n E d1 m1 m0 HR L(HR) U(HR) v2.0 v2.1 v1a.0 v1a.1 v7.0 v7.1 v3.0
   1: 4 106 21 15 Inf Inf 3.01 1.17
                                        7.77
                                                 0
                                                       0
                                                                   \cap
                                                                         0
                                                             1
    2: 4 99 16 11 Inf Inf 2.72 0.95
                                        7.84
                                                                   0
                                                 1
                                                       0
                                                             1
   3: 3 124 23 16 Inf Inf 2.62 1.08 6.36
                                                 0
                                                       \cap
                                                             1
                                                                   0
                                                                              \cap
                                                                                   0
   4: 4 88 30 20 Inf Inf 2.49 1.17
                                         5.34
                                                 0
                                                             1
   5: 4 97 29 18 Inf Inf 2.22 1.05
                                         4.70
                                                                   0
                                                                                   0
                                                 0
                                                       0
                                                             1
   6: 4 110 19 13 Inf Inf 2.20 0.84
                                         5.80
                                                 0
                                                       0
                                                             1
                                                                   0
                                                                              0
                                                                                   1
                                         4.22
  7: 4 98 31 19 Inf Inf 2.05 0.99
                                                 1
                                                             1
   8: 4 146 33 18 Inf Inf 2.02 1.02 4.01
                                                 1
   9: 3 120 36 22 Inf Inf 2.02 1.03 3.94
                                                 0
                                                                                    0
                                                       0
                                                             1
                                                                   0
                                                                              0
## 10: 4 157 33 22 Inf Inf 2.01 0.97 4.14
                                                 0
                                                       0
                                                             1
                                                                   0
                                                                         1
                                                                              0
##
       v3.1 v5b.0 v5b.1 v6.0 v6.1 v5c.0 v5c.1 v1b.0 v1b.1 v5a.0 v5a.1 v4.0 v4.1
##
   1:
                1
                       0
                            1
                                 0
                                        0
                                              1
                                                     0
                                                           0
                                                                 0
                                                                        \cap
##
    2:
          0
                 1
                       0
                            0
                                 0
                                        0
                                              1
                                                     0
                                                           0
                                                                 0
                                                                        0
                                                                             0
                                                                                  0
##
   3:
          \cap
                       0
                            0
                                 0
                                        0
                                                     \cap
                                                           \cap
                                                                 \cap
                                                                        \cap
                                                                                  \cap
                1
                                              1
##
   4:
                       0
                                 0
                                                     0
                                                                        0
##
   5:
                       0
                                 0
                                        0
                                              0
                                                     0
                                                           0
                                                                 0
                                                                        0
          1
                1
                            1
##
    6:
          0
                 0
                       0
                            0
                                 0
                                        0
                                                     0
                                                           0
                                                                 0
                                                                        0
                                                                             0
##
   7:
          1
                       \cap
                            \cap
                                 \cap
                                        \cap
                                              \cap
                                                     \cap
                                                           \cap
                                                                 \cap
                                                                        \cap
                                                                             \cap
                                                                                  \cap
                 1
   8:
                                                     0
                                                     0
                                                           0
                                                                 0
                                                                        \cap
                                                                                  0
##
  9:
                       0
                            0
                                 0
                                        0
                                              0
                                                                             0
          1
                 1
## 10:
          0
                0
## Consistency 0.95
## Splitting method, # of splits= Random 1000
## Model, % Consistency Met= v1a.0 v5b.0 v6.0 v5c.1 0.95
## Consistency 0.631
## Consistency 0.913
## Splitting method, # of splits= Random 1000
## Model, % Consistency Met= v1a.0 v5b.0 v5c.1 0.913
## Consistency 0.941
## Splitting method, # of splits= Random 1000
## Model, % Consistency Met= v1a.0 v3.1 v5b.0 v4.1 0.941
## Consistency 0.641
```

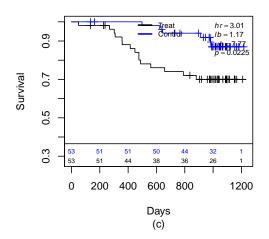
Consistency 0.333

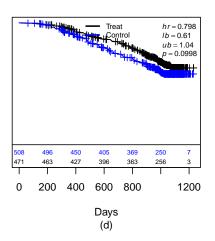
```
## Consistency 0.533
## Consistency 0.542
## Consistency 0.493
## Consistency 0.404
## Consistency 0.501
## Consistency 0.835
## Consistency 0.835
## Consistency 0.17
## Number of subgroups meeting consistency criteria= 3
     p.consistency Nsg group.id m.index K M.1 M.2 M.3 M.4
## 1:
             0.95 106 21 1 4 v1a.0 v5b.0 v6.0 v5c.1
## 2:
            0.913 124
                           23
                                   3 3 v1a.0 v5b.0 v5c.1
## 3:
           0.941 88
                          91
                                   4 4 v1a.0 v3.1 v5b.0 v4.1
## p.consistency Nsg group.id m.index K M.1 M.2 M.3 M.4
## 1: 0.950 106 21 1 4 v1a.0 v5b.0 v6.0 v5c.1
## 2:
            0.941 88
                           91
                                    4 4 v1a.0 v3.1 v5b.0 v4.1
## 3:
            0.913 124
                          23
                                    3 3 v1a.0 v5b.0 v5c.1
xx <- fs.est$find.grps$out.found$hr.subgroups
covs.found \leftarrow xx[, -c(1:10)]
covs.most <- apply(covs.found, 2, sum)</pre>
covs.most <- covs.most[covs.most > 0]
print(covs.most)
## v2.0 v1a.0 v1a.1 v7.0 v7.1 v3.0 v3.1 v5b.0 v5b.1 v6.0 v5c.0 v5c.1 v1b.0
                                7 50 23 17 31 19 15 5
## 37 22 16 17 1
## v1b.1 v5a.0 v5a.1 v4.0 v4.1
     33 12
                3
                    11
print(fs.est$grp.consistency$result)
     p.consistency Nsg group.id m.index K M.1 M.2 M.3 M.4
## 1:
        0.950 106 21 1 4 v1a.0 v5b.0 v6.0 v5c.1
## 2:
             0.941 88
                            91
                                    4 4 v1a.0 v3.1 v5b.0 v4.1
## 3:
             0.913 124
                            23
                                    3 3 v1a.0 v5b.0 v5c.1
df0.fs <- subset(fs.est$df.pred, treat.recommend == 0)</pre>
df1.fs <- subset(fs.est$df.pred, treat.recommend == 1)
if (!is.null(outfs)) save(fs.est, df.analysis, FSconfounders.name, file = outfs)
t.done <- proc.time()[3]</pre>
t.min \leftarrow (t.done - t.start)/60
cat("Minutes and hours for FS estimation", c(t.min, t.min/60), "\n")
## Minutes and hours for FS estimation 0.4066333 0.006777222
t.start <- proc.time()[3]</pre>
# Note, the elements above will need to be re-initiated if running separate
# from above E.q., outcome.names, event.name, ... hr.threshold, etc.
library(doParallel)
registerDoParallel(parallel::detectCores(logical = FALSE))
```

```
# Compare with GRF
layout(matrix(c(1, 2, 3, 4), 2, 2, byrow = TRUE))
plot.subgroup(sub1 = df0.grf, sub1C = df1.grf, tte.name = "time_days", event.name = "cens",
    treat.name = "treat", fix.rows = FALSE, byrisk = 200, show.med = FALSE, ymin = 0.4,
    subtitle1 = "(a)", subtitle2 = "(b)", xlab = "Days")
plot.subgroup(sub1 = df0.fs, sub1C = df1.fs, tte.name = "time_days", event.name = "cens",
    treat.name = "treat", fix.rows = FALSE, byrisk = 200, show.med = FALSE, ymin = 0.4,
    subtitle1 = "(c)", subtitle2 = "(d)", xlab = "Days")
```









```
cox.formula.boot <- as.formula(paste("Surv(time_days,cens)~treat"))
split_method <- "Random"
est.loghr <- TRUE

confounders.name <- FSconfounders.name
stop.threshold <- 0.99
fs.splits <- 1000
max.minutes <- 6

# Suggest running 50, first ... to get timing estimate</pre>
```

```
NB <- 10 * 1000
df_temp <- fs.est$df.pred[, c("id", "treat.recommend")]</pre>
dfa <- merge(df.analysis, df_temp, by = "id")</pre>
df_boot_analysis <- dfa</pre>
fitH <- get_Cox_sg(df_sg = subset(df_boot_analysis, treat.recommend == 0), cox.formula = cox.formula.bo
    est.loghr = est.loghr)
H_obs <- fitH$est_obs # log(hr) scale</pre>
seH_obs <- fitH$se_obs
# Hc observed estimates
fitHc <- get_Cox_sg(df_sg = subset(df_boot_analysis, treat.recommend == 1), cox.formula = cox.formula.b
    est.loghr = est.loghr)
Hc_obs <- fitHc$est_obs</pre>
seHc_obs <- fitHc$se_obs</pre>
rm("fitH", "fitHc")
Ystar_mat <- bootYstar({</pre>
   ystar <- get_Ystar(boot)</pre>
}, boots = NB, seed = 8316951, counter = "boot", export = fun_arg_list_boot)
# Check dimension
if (dim(Ystar_mat)[1] != NB | dim(Ystar_mat)[2] != nrow(df_boot_analysis)) stop("Dimension of Ystar_mat
tB.start <- proc.time()[3]</pre>
# Bootstraps
resB <- bootPar({</pre>
    ans <- fsboot_forparallel(boot)</pre>
}, boots = NB, seed = 8316951, counter = "boot", export = fun_arg_list_boot)
tB.now <- proc.time()[3]
tB.min <- (tB.now - tB.start)/60
doParallel::stopImplicitCluster()
cat("Minutes for Boots", c(NB, tB.min), "\n")
## Minutes for Boots 10000 409.168
cat("Projection per 100", c(tB.min * (100/NB)), "\n")
## Projection per 100 4.09168
cat("Propn bootstrap subgroups found =", c(sum(!is.na(resB$H_biasadj_1))/NB), "\n")
## Propn bootstrap subgroups found = 0.9806
# How many timmed out
cat("Number timmed out=", c(sum(is.na(resB$H_biasadj_1) & resB$tmins_search > max.minutes)),
    "\n")
## Number timmed out= 0
H_estimates <- get_dfRes(Hobs = H_obs, seHobs = seH_obs, H1_adj = resB$H_biasadj_1,</pre>
    ystar = Ystar_mat, cov_method = "standard", cov_trim = 0.05)
Hc_estimates <- get_dfRes(Hobs = Hc_obs, seHobs = seHc_obs, H1_adj = resB$Hc_biasadj_1,</pre>
    ystar = Ystar_mat, cov_method = "standard", cov_trim = 0.05)
print(H_estimates)
```

```
## HO sdHO HO_lower HO_upper H1 sdH1 H1_lower H1_upper
## 1: 3.01229 1.456134 1.16796 7.769007 1.535403 0.2423926 1.126793 2.092189
print(Hc_estimates)
             HO sdHO HO_lower HO_upper H1 sdH1 H1_lower H1_upper
## 1: 0.7977977 0.1095 0.6096253 1.044053 0.8600442 0.1128287 0.6650466 1.112217
if (!is.null(outfsboot)) save(fs.est, Ystar_mat, resB, H_estimates, Hc_estimates,
    df_boot_analysis, file = outfsboot)
t.done <- proc.time()[3]
t.min \leftarrow (t.done - t.start)/60
cat("Minutes and hours for FS bootstrap", c(t.min, t.min/60), "\n")
## Minutes and hours for FS bootstrap 409.3363 6.822271
df0.fs <- subset(fs.est$df.pred, treat.recommend == 0)</pre>
df1.fs <- subset(fs.est$df.pred, treat.recommend == 1)</pre>
# ITT analysis
cox_itt <- summary(coxph(Surv(time_days, cens) ~ treat, data = fs.est$df.pred))$conf.int</pre>
# ITT estimates
resITT <- c(round(cox_itt[c(1, 3, 4)], 2), nrow(fs.est$df.pred))</pre>
# Forest Search Un-adjusted
Hstat <- c(unlist(H_estimates))[c(1, 3, 4)]</pre>
resH_obs <- c(c(Hstat), nrow(df0.fs))</pre>
# Bias-corrected
Hstat <- c(unlist(H_estimates))[c(5, 7, 8)]</pre>
resH_bc <- c(c(Hstat), nrow(df0.fs))</pre>
Hstat2 <- c(unlist(H_estimates))[c(5, 7, 8)]</pre>
Hstat2 <- round(Hstat2, 2)</pre>
a <- paste0(Hstat2[1], " [")
a <- paste0(a, Hstat2[2])
a <- paste0(a, ",")
a <- paste0(a, Hstat2[3])
a <- paste0(a, "]")
H_bc2 \leftarrow c(a)
# Un-adjusted
Hcstat <- c(unlist(Hc_estimates))[c(1, 3, 4)]</pre>
resHc_obs <- c(c(Hcstat), nrow(df1.fs))</pre>
# Bias-corrected
Hcstat <- c(unlist(Hc_estimates))[c(5, 7, 8)]</pre>
resHc_bc <- c(c(Hcstat), nrow(df1.fs))</pre>
Hcstat2 <- c(unlist(Hc_estimates))[c(5, 7, 8)]</pre>
Hcstat2 <- round(Hcstat2, 2)</pre>
a <- paste0(Hcstat2[1], " [")</pre>
a <- paste0(a, Hcstat2[2])
```

```
a <- paste0(a, ",")
a <- paste0(a, Hcstat2[3])
a <- paste0(a, "]")
Hc_bc2 <- c(a)

res <- rbind(resITT, resH_obs, resH_bc, resHc_obs, resHc_bc)

resf <- as.data.frame(res)

colnames(resf) <- c("HR Estimate", "Lower", "Upper", "$\\#$ Subjects")

rnH <- c("$\\hat{H}$$", "$\\hat{H}_{bc}$$")

rnHc <- c("$\\hat{H}^{c}$", "$\\hat{H}^{c}$")

rnItt <- c("ITT")

rownames(resf) <- c(rnItt, rnH, rnHc)</pre>
```

Table 1: ACTG-175 FS Analysis: Cox hazard ratio (HR) estimates for the ITT population and subgroups H and H^c . Cox model estimates are based on subgroups: The estimated subgroup \hat{H} ; and the bootstrap (B = 10,000) bias-correction to \hat{H} estimates, denoted \hat{H}_{bc} . Estimates for the complement H^c are defined analogously. The number of subjects in each population (# Subjects) are listed.

	HR Estimate	Lower	Upper	# Subjects
ITT				
ITT	0.900	0.690	1.160	1085
H subgroup estimates				
\hat{H}	3.012	1.168	7.769	106
\hat{H}_{bc}	1.535	1.127	2.092	106
H-complement subgroup estimates				
\hat{H}^c	0.798	0.610	1.044	979
\hat{H}^c_{bc}	0.860	0.665	1.112	979

```
t.done <- proc.time()[3]
t.min <- (t.done - t.start.all)/60
cat("Minutes and hours to finish", c(t.min, t.min/60), "\n")
## Minutes and hours to finish 412.6678 6.877797</pre>
```

```
cat("Machine=", c(Sys.info()[[4]]), "\n")

## Machine= Mac-Studio-3.local

cat("Number of cores=", c(detectCores(logical = FALSE)), "\n")

## Number of cores= 10
```