
CS2040 Lecture Note #2: **Abstract Data Type**

Walls

Lecture Note #2: ADT

■ Objectives:

- Able to understand the need of data abstraction
- Able to define ADT with Java Interface
(Java Interface: A group of related methods with empty bodies)
- Able to implement data structure given a Java interface

1 Software Engineering Issues

Motivation

1. Software Engineering Issues (1/4)

□ Program Design Principles

- **Abstraction**

- Concentrate on what it can be done and not how it can be done
- Use of Java Interface

- **Coupling**

- Restrict interdependent relationship among classes to the minimum

- **Coherent**

- A class should be about a single entity only
- There should be a clear logical grouping of all functionalities

- **Information Hiding**

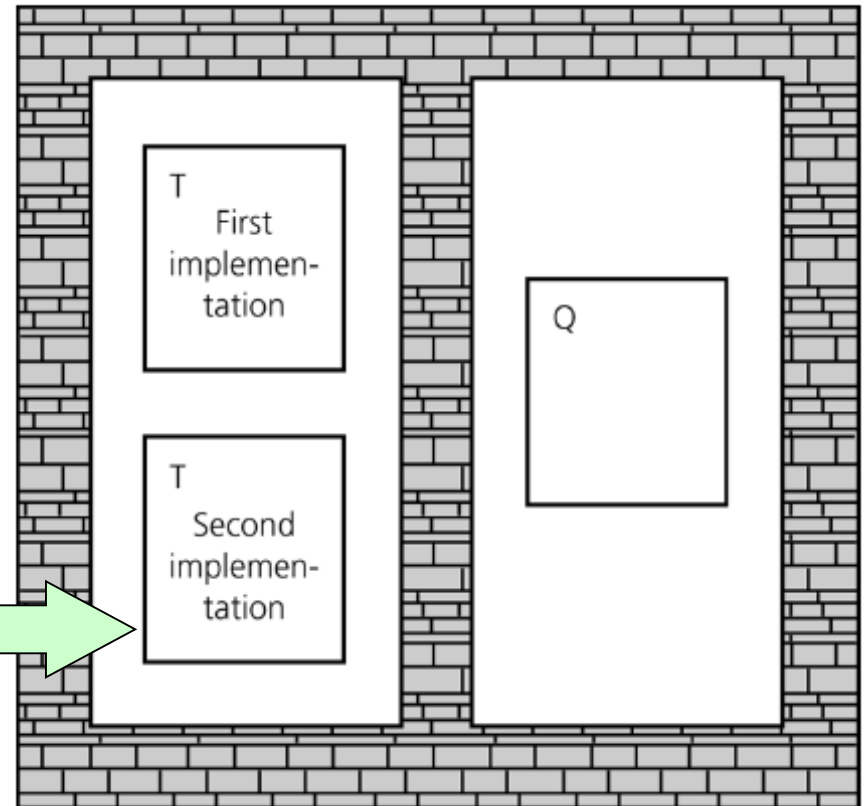
- Only expose necessary information to outside

1. Software Engineering Issues (2/4)

❏ Information Hiding

- Information hiding is like walls building around the various classes of a program.
- The wall around each class T prevents the other classes from seeing how T works.
- Thus, if class Q uses T , and if the approach for performing T changes, class Q will not be affected.

Makes it easy to substitute new, improved versions of how to do a task later



1. Software Engineering Issues (3/4)

- ❑ Information Hiding is not complete isolation of the classes
 - Q does not know how T does the work, but needs to know how to **invoke** T and what T **produces**
 - What goes in and comes out is governed by the terms of the **method's specifications**
 - If you use this method in this way, this is exactly what it will do for you.

1. Software Engineering Issues (4/4)

❑ Information Hiding CAN apply to data

- **Data abstraction** asks that you think in terms of **what** you can do to a collection of data independently of **how** you do it
- **Data structure** is a construct that can be defined within a programming language to store a **collection of data**
- **Abstract data type (ADT)** is a **collection of data** & a **specification on the set of operations** on that data
 - Typical **operations** on data are: *add*, *remove*, and *query* (in general, **management of data**)
 - Specification indicates what ADT operations **do**, **but not how** to implement them

2 Abstract Data Type

Collection of data + set of operations on the data

2. Data Structure

- ❑ **Data structure** is a construct that can be defined within a programming language to store a collection of data
 - **Arrays**, which are built into Java, are data structure
 - We can **create** other data structures. For example, we want a data structure (a collection of data) to store both the names and salaries of a collection of employees

```
static final int MAX_NUMBER = 500; // static final means "constant"
String [] names = new String [MAX_NUMBER];
double [] salaries = new double [MAX_NUMBER];
// employee names[i] has a salary of salaries[i]
```

or
(better choice)

```
class Employee {
    static final int MAX_NUMBER = 500;
    private String names;
    private double salaries;
}

.....
Employee[ ] workers = new Employee[Employee.MAX_NUMBER];
```

2. Abstract Data Type (ADT) (1/4)

- ❑ **ADT** is a collection of data together with a specification of a set of operations on that data
 - Specifications indicate what ADT operations do, but not how to implement them
 - Data structures are part of an ADT's implementation
- ❑ **When a program needs data operations that are not directly supported by a language, you need to create your own ADT**
- ❑ You should first design the ADT by carefully specifying the operations before implementation

2. Abstract Data Type (ADT) (2/4)

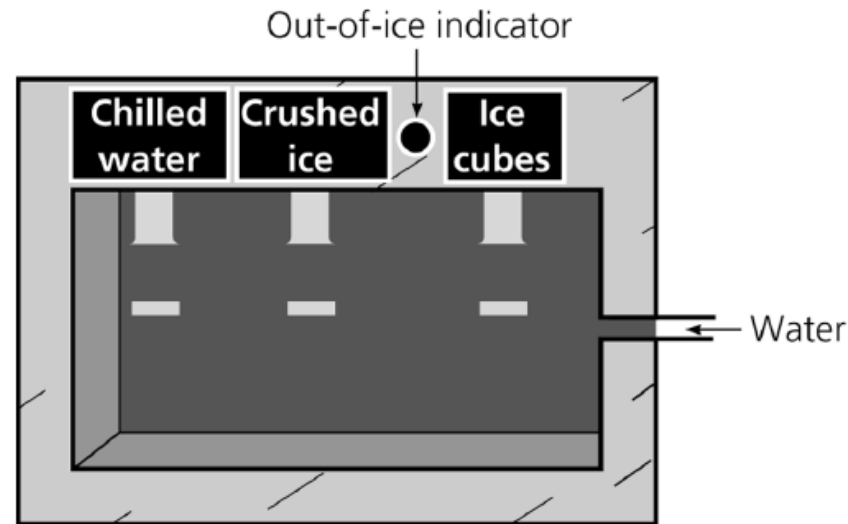
■ Example: A water dispenser as an ADT

- Data: **water**
- Operations: *chill*, *crush*, *cube*, and *isEmpty*
- Data structure: the internal structure of the dispenser
- Walls: made of steel

The only slits in the walls:

- ☐ Input: **water**
- ☐ Output: **chilled water, crushed ice, or ice cubes.**

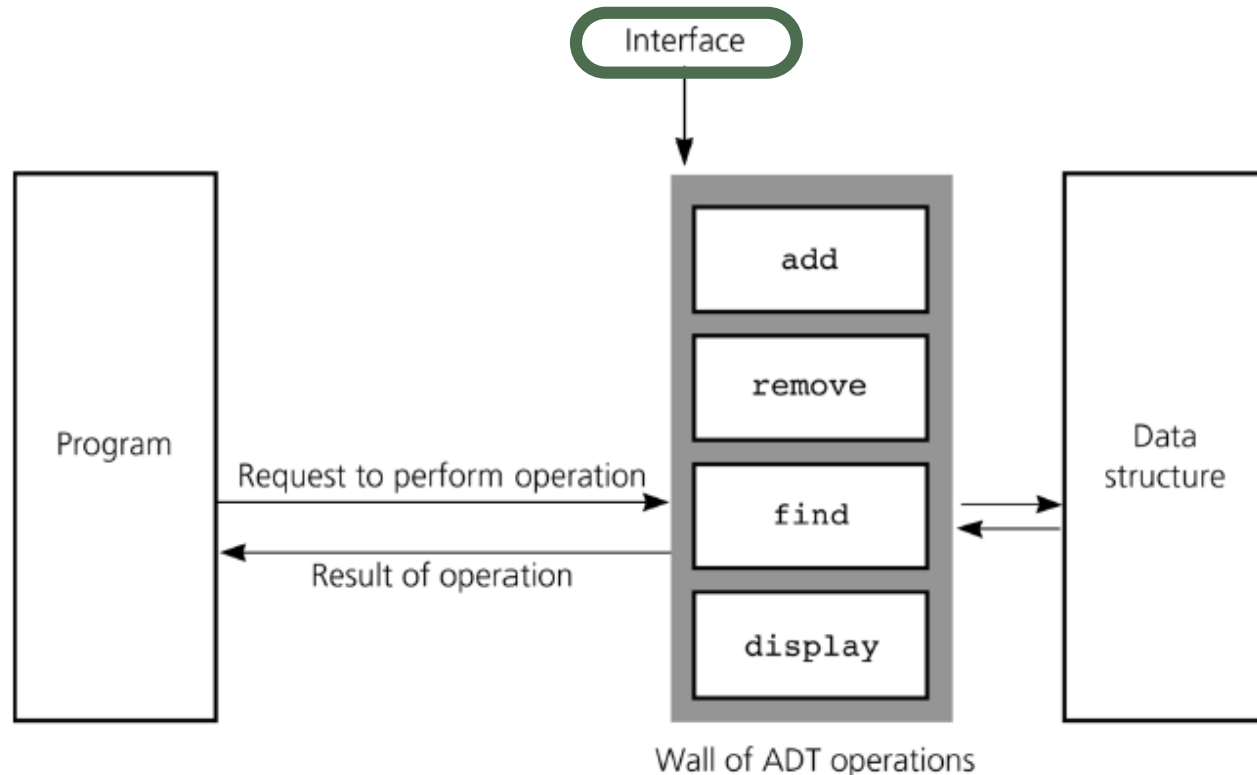
Crushed ice can be made in many different ways.
We don't care how it was made



- Using an ADT is like using a vending machine.

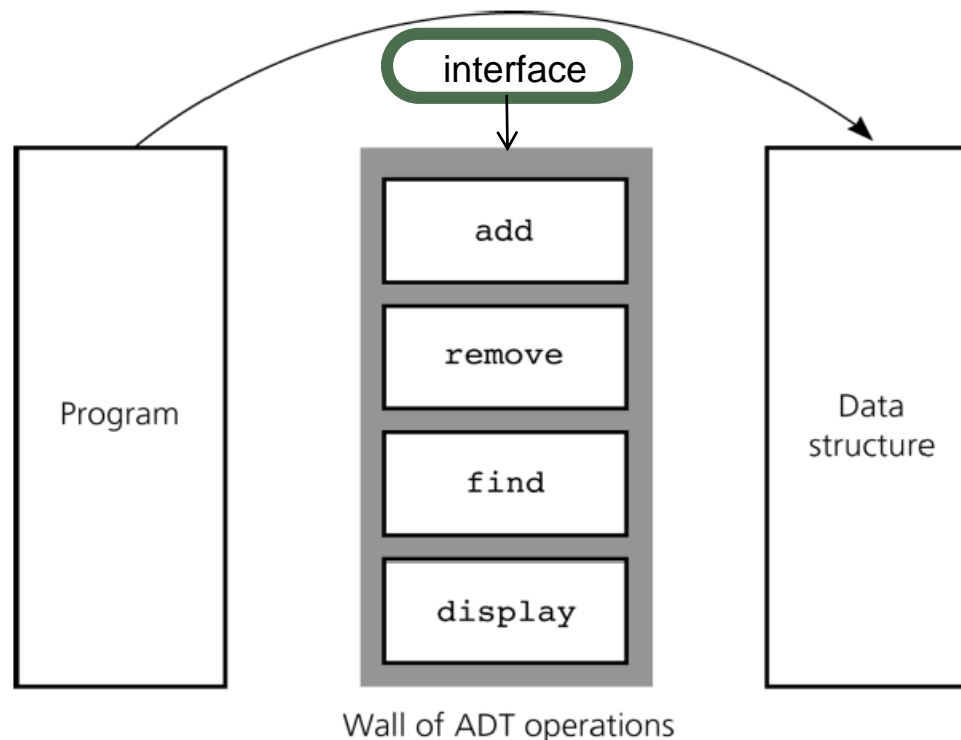
2. Abstract Data Type (ADT) (3/4)

- ❑ A WALL of ADT operations isolates a data structure from the program that uses it
- ❑ An **interface** is what a program/module/class should understand and use the ADT



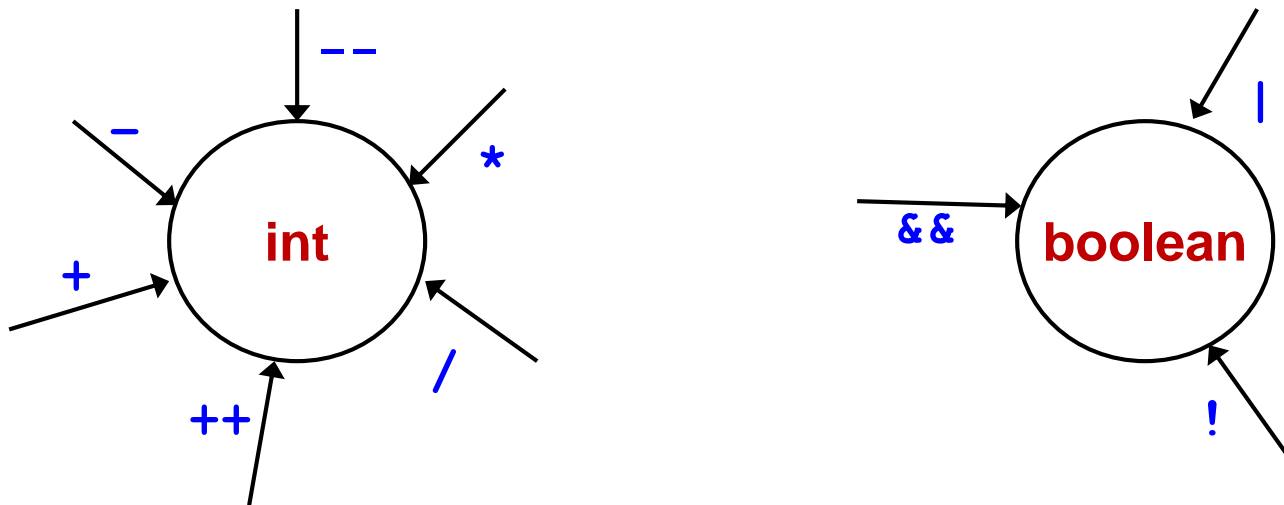
2. Abstract Data Type (ADT) (4/4)

- ❑ An **interface** is what a program/module/class should understand and use the ADT
- ❑ The following bypasses the interface to access the data structure. This violates the wall of ADT operations.



2. Example: Primitive Types as ADTs (1/2)

- Java's predefined data types are ADTs
- Representation details are hidden which aids portability as well
- Examples: **int**, **boolean**, **String**, **double**

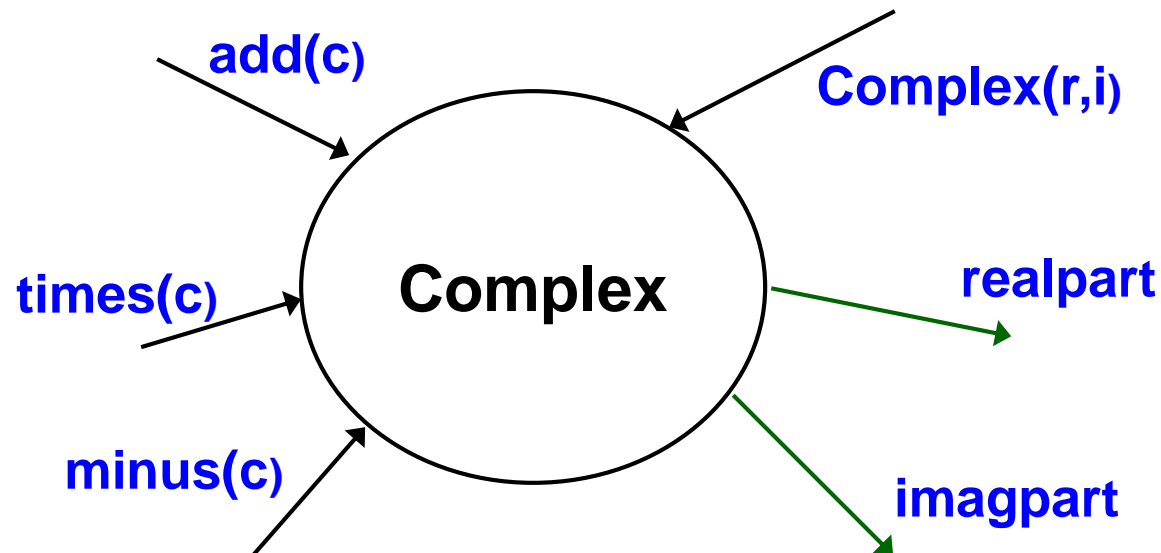


2. Example: Primitive Types as ADTs (2/2)

- Broadly classified as:
(here the example uses the array ADT)
 - **Constructors** (to add, create objects)
 - `int[] x = { 2,4,6,8 };`
 - **Mutators** (to update objects)
 - `x[3] = 10;`
 - **Accessors** (to query about state of objects)
 - `int y = x[3] + x[2];`

2. Example: Complex Number ADT (1/5)

- User-defined data types can also be organized as ADTs



Note: `add(c)` means to add `c` to itself, etc.

2. Example: Complex Number ADT (2/5)

■ A possible Complex ADT class:

```
class Complex {  
    private ...                // data members  
    public Complex(double r, double i) { ... } // create a new object  
    public void add(Complex c) { ... }         // this = this + c  
    public void minus(Complex c) { ... }        // this = this - c  
    public void times(Complex c) { ... }        // this = this * c  
    public double realpart() { ... }            // returns this.real  
    public double imagpart() { ... }            // returns this.imag  
}
```

■ Using the Complex ADT:

```
Complex c = new Complex(1,2); // c = (1,2)  
Complex d = new Complex(3,5); // d = (3,5)  
c.add(d); // c = c+d  
d.minus(new Complex(1,1)); // d = d-(1,1)  
  
c.times(d); // c = c*d
```

2. Example: Complex Number ADT (3/5)

■ 1st implementation: Cartesian

```
class Complex {  
    private double real;  
    private double imag;  
  
    // CONSTRUCTOR  
    public Complex(double r, double i) { real = r; imag = i; }  
  
    // ACCESSORS  
    public double realpart() { return real; }  
    public double imagpart() { return imag; }  
  
    // MUTATORS  
    public void add (Complex c) {    // this = this + c  
        real += c.realpart();  
        imag += c.imagpart();  
    }  
    public void minus (Complex c) {    // this = this - c  
        real -= c.realpart();  
        imag -= c.imagpart();  
    }  
    public void times (Complex c) {    // this = this * c  
        real = real*c.realpart() - imag*c.imagpart();  
        imag = real*c.imagpart() + imag*c.realpart();  
    }  
}
```

2. Example: Complex Number ADT (4/5)

■ 2nd implementation: Polar

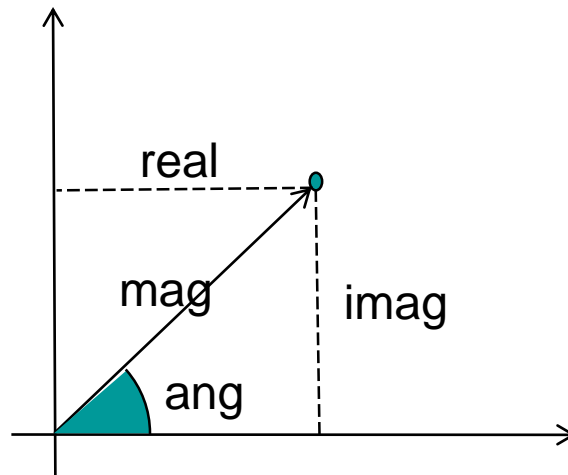
```
class Complex {  
    private double ang; // the angle of the vector  
    private double mag; // the magnitude of the vector  
    :  
    :  
    public times(Complex c) { // this = this * c  
        ang += c.angle();  
        mag *= c.mag();  
    }  
    :  
    :  
}
```

2. Example: Complex Number ADT (5/5)

■ “Relationship” between Cartesian and Polar

From Polar to Cartesian: $\text{real} = \text{mag} * \cos(\text{ang});$
 $\text{imag} = \text{mag} * \sin(\text{ang});$

From Cartesian to Polar: $\text{ang} = \tan^{-1}(\text{imag}/\text{real});$
 $\text{mag} = \text{real} / \cos(\text{ang});$



3 Java Interface

Related methods

3 Java Interface

- Java interfaces provide a way to specify common behaviour for a set of (perhaps unrelated) classes
- Java interface can be used for ADT
 - It allows further abstraction / generalization
 - It uses the keyword **interface**, rather than **class**
 - It specifies methods to be implemented by subclasses
 - **A Java interface is a group of related methods with empty bodies**
 - It can have constant definition (which are implicitly **public static final**)
- A class is said to implement the interface if it provides implementations for all of the methods in the interface

3 Example #1

```
// package in java.lang;  
public interface Comparable <T> {  
    int compareTo (T other);  
}
```

```
class Shape implements Comparable <Shape> {  
    static final double PI = 3.14;  
    double area() {...};  
    double circumference() { ... };  
    int compareTo(Shape x) {  
        if (this.area() == x.area())  
            return 0;  
        else if (this.area() > x.area())  
            return 1;  
        else  
            return -1;  
    }  
}
```

3 Example #2: Interface for Complex

E.g. Complex ADT interface

- anticipate both Cartesian and Polar approach

```
public interface Complex {  
    public double realpart(); // returns this.real  
    public double imagpart(); // returns this.imag  
    public double angle();    // returns this.ang  
    public double mag();      // returns this.mag  
    public void add(Complex c); // this = this + c  
    public void minus(Complex c); // this = this - c  
    public void times(Complex c); // this = this * c  
}
```

Complex.java

- In interface, methods have signatures but no implementation

3 Example #2: ComplexCart (1/2)

■ Cartesian Implementation (Part 1 of 2)

ComplexCart.java

```
class ComplexCart implements Complex {  
    private double real;  
    private double imag;  
  
    // CONSTRUCTOR  
    public ComplexCart(double r, double i) { real = r; imag = i; }  
  
    // ACCESSORS  
    public double realpart() { return this.real; }  
    public double imagpart() { return this.imag; }  
    public double mag() { return Math.sqrt(real*real + imag*imag); }  
    public double angle() {  
        if (real != 0) {  
            if (real < 0) return (Math.PI + Math.atan(imag/real));  
            return Math.atan(imag/real);  
        }  
        else if (imag == 0) return 0;  
        else if (imag > 0) return Math.PI/2;  
        else return -Math.PI/2;  
    }  
}
```

3 Example #2: ComplexCart (2/2)

■ Cartesian Implementation (Part 2 of 2)

ComplexCart.java

```
// MUTATORS
public void add(Complex c) {
    this.real += c.realpart();
    this.imag += c.imagpart();
}

public void minus(Complex c) {
    this.real -= c.realpart();
    this.imag -= c.imagpart();
}

public void times(Complex c) {
    double tempReal = real * c.realpart() - imag * c.imagpart();
    imag = real * c.imagpart() + imag * c.realpart();
    real = tempReal;
}

public String toString() {
    if (imag == 0) return (real + "");
    else if (imag < 0) return (real + "" + imag + "i");
    else return (real + "+" + imag + "i");
}
```

Why can't we write the following?

```
if (imag == 0) return (real);
```



3 Example #2 : ComplexPolar (1/3)

■ Polar Implementation (Part 1 of 3)

ComplexPolar.java

```
class ComplexPolar implements Complex {
    private double mag; // magnitude
    private double ang; // angle
    // CONSTRUCTOR
    public ComplexPolar(double m, double a) { mag = m; ang = a; }
    // ACCESSORS
    public double realpart() { return mag * Math.cos(ang); }
    public double imagpart() { return mag * Math.sin(ang); }
    public double mag() { return mag; }
    public double angle() { return ang; }
    // MUTATORS
    public void add(Complex c) { // this = this + c
        double real = this.realpart() + c.realpart();
        double imag = this.imagpart() + c.imagpart();
        mag = Math.sqrt(real*real + imag*imag);
        if (real != 0) {
            if (real < 0) ang = (Math.PI + Math.atan(imag/real));
            else ang = Math.atan(imag/real);
        }
        else if (imag == 0) ang = 0;
        else if (imag > 0) ang = Math.PI/2;
        else ang = -Math.PI/2;
    }
}
```

3 Example #2 : ComplexPolar (2/3)

■ Polar Implementation (Part 2 of 3)

ComplexPolar.java

```
public void minus(Complex c) {    // this = this - c
    double real = mag * Math.cos(ang) - c.realpart();
    double imag = mag * Math.sin(ang) - c.imagpart();
    mag = Math.sqrt(real*real + imag*imag);
    if (real != 0) {
        if (real < 0) ang = (Math.PI + Math.atan(imag/real));
        else ang = Math.atan(imag/real);
    }
    else if (imag == 0) ang = 0;
    else if (imag > 0) ang = Math.PI/2;
    else ang = -Math.PI/2;
}
```

3 Example #2 : ComplexPolar (3/3)

■ Polar Implementation (Part 3 of 3)

ComplexPolar.java

```
public void times(Complex c) {    // this = this * c
    mag *= c.mag();
    ang += c.angle();
}

public String toString() {
    if (imagpart() == 0)
        return (realpart() + "");
    else if (imagpart() < 0)
        return (realpart() + "" + imagpart() + "i");
    else
        return (realpart() + "+" + imagpart() + "i");
}
}
```

3 Example #2 : TestComplex (1/3)

■ Testing Complex class (Part 1 of 3)

TestComplex.java

```
class TestComplex {  
  
    public static void main(String[] args) {  
        // Testing ComplexCart  
        Complex a = new ComplexCart(10.0, 12.0);  
        Complex b = new ComplexCart(1.0, 2.0);  
  
        System.out.println("Testing ComplexCart:");  
        a.add(b);  
        System.out.println("a=a+b is " + a);  
        a.minus(b);  
        System.out.println("a-b (which is the original a) is " + a);  
        System.out.println("Angle of a is " + a.angle());  
        a.times(b);  
        System.out.println("a=a*b is " + a);  
    }  
}
```

```
Testing ComplexCart:  
a=a+b is 11.0+14.0i  
a-b (which is the original a) is 10.0+12.0i  
Angle of a is 0.8760580505981934  
a=a*b is -14.0+32.0i
```

3 Example #2 : TestComplex (2/3)

■ Testing Complex class (Part 2 of 3)

TestComplex.java

```
// Testing ComplexPolar
Complex c = new ComplexPolar(10.0, Math.PI/6.0);
Complex d = new ComplexPolar(1.0, Math.PI/3.0);

System.out.println("\nTesting ComplexPolar:");
System.out.println("c is " + c);
System.out.println("d is " + d);
c.add(d);
System.out.println("c=c+d is " + c);
c.minus(d);
System.out.println("c-d (which is the original c) is " + c);
c.times(d);
System.out.println("c=c*d is " + c);
```

```
Testing ComplexPolar:
c is 8.660254037844387+4.999999999999999i
d is 5.0000000000000001+8.660254037844386i
c=c+d is 13.660254037844393+13.660254037844387i
c-d (which is ... c) is 8.660254037844393+5.0000000000000002i
c=c*d is 2.83276944823992E-14+100.00000000000007i
```

3 Example #2 : TestComplex (3/3)

■ Testing Complex class (Part 3 of 3)

TestComplex.java

```
// Testing Combined
System.out.println("\nTesting Combined:");
System.out.println("a is " + a);
System.out.println("d is " + d);
a.minus(d);
System.out.println("a=a-d is " + a);
a.times(d);
System.out.println("a=a*d is " + a);
d.add(a);
System.out.println("d=d+a is " + d);
d.times(a);
System.out.println("d=d*a is " + d);
}
```

```
Testing Combined:
a is -14.0+32.0i
d is 5.0000000000000001+8.660254037844386i
a=a-d is -19.0+23.339745962155614i
a=a*d is -297.1281292110204-47.84609690826524i
d=d+a is -292.12812921102045-39.18584287042089i
d=d*a is 84924.59488697552+25620.40696350589i
```