

Übung 3

1 a)

$$U_L = U_X + U_L$$

$$U_L = U_L - U_X = U_L - \frac{R_X}{R_X + R_L} U_L$$

$$\underline{U_L = U_L \left(1 - \frac{R_X}{R_X + R_L}\right)}$$

1 b)

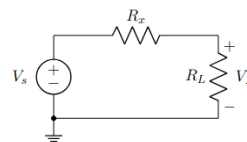
$$U_L = U_X + U_L$$

$$U_X = U_L - U_L$$

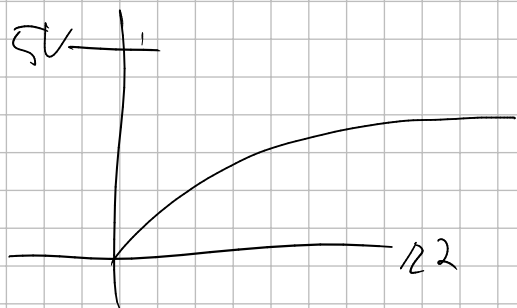
$$U_X = U_L - \frac{R_L}{R_X + R_L} U_L = \underline{U_L \left(1 - \frac{R_L}{R_X + R_L}\right)}$$

$$U_X + U_L = U_L \left(1 - \frac{R_X}{R_L + R_X}\right) + U_L \left(1 - \frac{R_L}{R_L + R_X}\right) = U_L \left(1 - \frac{R_X}{R_X + R_L} + 1 - \frac{R_L}{R_X + R_L}\right)$$

$$= U_L \left(2 - \frac{R_X + R_L}{R_X + R_L}\right) = U_L (2 - 1) = \underline{U_L}$$



2 a)



2b) $R_2 = [4,00, 12,0] \text{ k}\Omega$ $U_2 = 5 \text{ V}$

$$U_5 = \frac{R_2}{R_1 + R_2} U_2$$

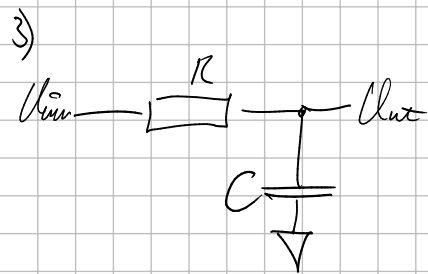
$$U_5 \in [1,43, 2,73] \text{ V}$$

$$a = \frac{2,73 \text{ V} - 1,43 \text{ V}}{12,0 \text{ k}\Omega - 4,00 \text{ k}\Omega} = 0,00016 \frac{\text{V}}{\Omega} = 0,16 \text{ V/k}\Omega$$

$$U(R_2) = 1,43 \text{ V} + 0,16 \text{ V/k}\Omega \cdot (R_2 - 4 \text{ k}\Omega)$$

$$= 1,43 \text{ V} - 0,65 \text{ V} + 0,16 \text{ V/k}\Omega \cdot R_2$$

$$= \underline{\underline{0,79 \text{ V} + 0,16 \text{ V/k}\Omega \cdot R_2}}$$



$$\left| \frac{U_{\text{out}}}{U_{\text{in}}} \right| = \frac{1}{\sqrt{1 + \left(\frac{f}{f_c} \right)^2}} \quad f_c = \frac{1}{2\pi RC} \quad f = 0,5 \text{ MHz}, 0,03 \text{ abfall slope gegeben}$$

$$\left| \frac{U_{\text{out}}}{U_{\text{in}}} \right| = 0,03$$

$$\frac{1}{\sqrt{1 + \left(\frac{0,5 \text{ MHz}}{f_c} \right)^2}} = 0,03$$

$$\left(\frac{0,5 \text{ MHz}}{f_c} \right)^2 = \left(\frac{1}{0,03} \right)^2 - 1$$

$$\frac{f}{f_c} = \sqrt{\left(\frac{1}{0,03} \right)^2 - 1}$$

$$f_c = \frac{f}{\sqrt{\frac{1}{0,03^2} - 1}} = \frac{1}{2\pi RC}$$

$$RC = \frac{\sqrt{\frac{1}{0,03^2} - 1}}{2\pi f}$$

$$RC = 1,06 \cdot 10^{-5}$$

$$f = 400 \text{ Hz} \quad f_c = \frac{1}{2\pi RC} = 15000 \text{ Hz}$$

$$\frac{1}{\sqrt{1 + \left(\frac{f}{f_c} \right)^2}} = \frac{1}{\sqrt{1 + \left(\frac{400 \text{ Hz}}{15000 \text{ Hz}} \right)^2}} = 0,9996$$

Abfall nur 0,04%

4 a)

$$m = 0,00 \text{ kg} \rightarrow R_w = 119 \Omega \quad m = 135,62 \text{ kg} \rightarrow R_w = 127 \Omega$$

$$R_z = (0, 200) \Omega$$

$$a = b$$

$$R_w = 119 \Omega$$

$$R_1 R_3 = R_2 R_4$$

$$(100 \Omega + \frac{(24 \Omega)(70 \Omega + R_z)}{94 \Omega + R_z}) R_w = (120 \Omega)^2$$

$$\frac{(24 \Omega)(70 \Omega + R_z)}{94 \Omega + R_z} = \frac{(120 \Omega)^2}{R_w} - 100 \Omega$$

$$(24 \Omega)(70 \Omega + R_z) \left(\frac{(120 \Omega)^2}{R_w} - 100 \Omega \right) / (94 \Omega + R_z)$$

$$24 - 70 \Omega^2 + R_z = 24 \Omega = 21,0084 \cdot 94 \Omega^2 + 21,0084 \Omega \cdot R_z$$

$$R_z(24 \Omega - 21,0084 \Omega) = 21,0084 \cdot 94 \Omega^2 - 70 \cdot 24 \Omega^2$$

$$R_z = \underline{\underline{98,5391 \Omega}}$$

4 b) $(100 \Omega + \frac{(24 \Omega)(70 \Omega + R_z)}{94 \Omega + R_z}) R_w = (120 \Omega)^2$

$$R_w = \frac{(120 \Omega)^2}{100 \Omega + \frac{(24 \Omega)(70 \Omega + R_z)}{94 \Omega + R_z}}$$

$$R_w = [117, 122]$$

4 c) $R_z = 98,5391 \Omega \quad R_w = 127 \Omega$

$$a - b = U \left(\frac{120 \Omega}{(120 \Omega + \frac{(24 \Omega)(70 \Omega + 98 \Omega)}{94 \Omega + 98 \Omega})} - \frac{127 \Omega}{120 \Omega + 127 \Omega} \right) =$$

