

Simulation of chemical reaction kinetics

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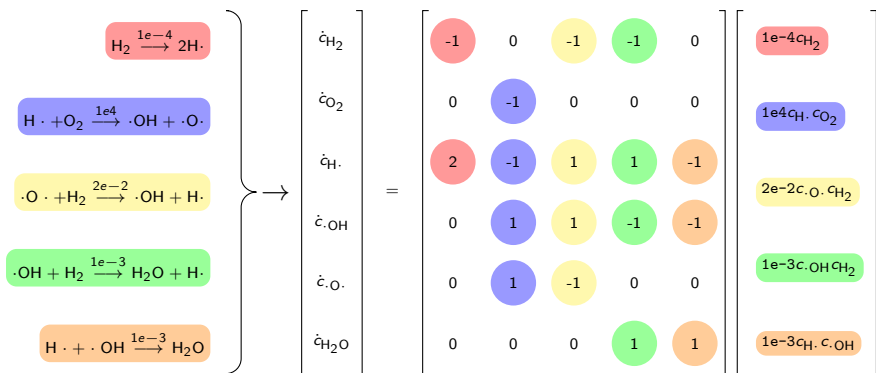
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Simulation of a oxyhydrogen reaction
with the given initial conditions and

chemical equations: $\rightarrow \dot{\mathbf{c}} = f(\mathbf{c})$, $\mathbf{c}_0 = [100 \ 50 \ 0 \ 0 \ 0 \ 0]^T$



- Since the problem is *stiff*, we have to choose an implicit multi-step method to obtain a large domain of stability (A-stable).
- Try *Adams-Moulton*-method and *BDF*-method with $k = 1$ steps and a step size $h = 1e-2$:

$$\sum_{j=0}^k a_j y_{n+j} = h \sum_{j=0}^k b_j f_{n+j} \quad (1)$$

Adams-Moulton:

k	a_0	a_1	b_0	b_1
1	-1	1	0.5	0.5

$$F(y_{n+1}) = y_n + \frac{h}{2} (f_n + f_{n+1}) - y_{n+1}$$

BDF:

k	a_0	a_1	b_0	b_1
1	-1	1	0	1

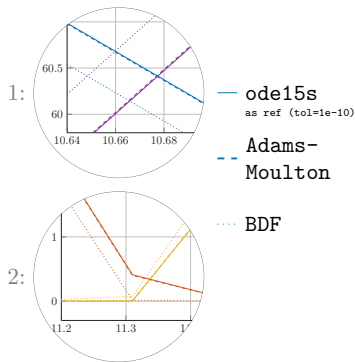
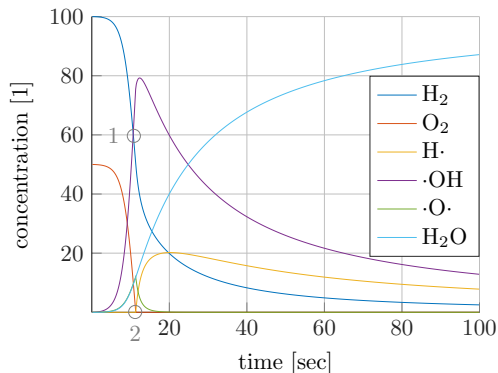
$$F(y_{n+1}) = y_n + h f_{n+1} - y_{n+1}$$

```
% Classic Iteration Loop
while (n+k-1)*h < tend
    % Newton-method
    [...] % initializing
    Fi = F(y(n+k-1));
    while norm(Fi) > tol
        [...] % calculate JFi
        yi(i+1) = yi(i) - JFi \ Fi;
        Fi = F(yi(i+1));
        i = i+1;
    end
    y(n+k) = yi(i);
    n = n+1;
end
```

To calculate the Jacobian:

$$JF(y) = \begin{bmatrix} \frac{\delta F(y)}{\delta y_1} & \dots & \frac{\delta F(y)}{\delta y_N} \end{bmatrix}$$

$$\frac{\delta F(y)}{\delta y_i} = \frac{F(y + \hat{h}e_i) - F(y)}{\hat{h}}$$



method	fun eval	max NS	average NS	ct [sec]	err
A-M	91016	7	1.0145	4.0205	0.0347
BDF	80476	7	1.0068	5.7835	13.5788
ode15s	988	-	-	0.4859	ref