Spanning Tree

```
Root:
                        loop
                            \mathbf{for}\ m := 1\ \mathbf{to}\ \delta\ \mathbf{do}
                                write r_{\rm mi} := r_{\rm im} := \langle 0, 0 \rangle
                            end for
                         end loop
Others:
                        loop
                            \mathbf{for}\ m := 1\ \mathbf{to}\ \delta\ \mathbf{do}
                                lr_{\min} := \operatorname{read}(r_{\min})
                                FirstFound := false
                                dist := 1 + \min\{lr_{mi}.dis \mid 1 \le m \le \delta\}
                                for m := 1 to \delta do
                                    if FirstFound and lr_{\rm mi}.{\rm dis}={\rm dist} - 1 then
                                        write r_{\rm im} := \langle 1, \, \text{dist} \rangle
                                       FirstFound := true
                                    else
                                       write r_{\rm im} := \langle 0, \, {\rm dist} \rangle
                                    end if
                                end for
                            end for
                         end loop
```

Dijkstras mutual exclusion

```
P_1: \\ \textbf{loop} \\ \textbf{if } x_1 = x_n \textbf{ then} \\ x_1 := (x_1+1) \bmod (n+1) \\ \textbf{end if} \\ \textbf{end loop} \\ \\ P_i \ (i \neq 1): \\ \\ \textbf{loop} \\ \textbf{if } x_i \neq x_{i\text{-}1} \textbf{ then} \\ x_i := x_{i\text{-}1} \\ \textbf{end if} \\ \textbf{end loop} \\ \\ \end{cases}
```

Mutual exclusion for tree structure

Root:

```
\begin{aligned} &\mathbf{loop} \\ & \mathrm{read}\ lr_{1,\mathrm{i}} := \mathrm{read}(r_{1,\mathrm{i}}) \\ & \mathbf{if}\ lr_{\delta,\mathrm{i}} = r_{\mathrm{i},1}\ \mathbf{then} \\ & \mathrm{write}\ r_{\mathrm{i},2} := (lr_{1,\mathrm{i}} + 1)\ \mathrm{mod}\ (4n + 5) \\ & \mathbf{end}\ \mathbf{if} \end{aligned} & \mathbf{for}\ m := 2\ \mathbf{to}\ \delta\ \mathbf{do} \\ & lr_{\mathrm{m},\mathrm{i}} := \mathrm{read}(r_{\mathrm{m},\mathrm{i}}) \\ & \mathrm{write}\ r_{\mathrm{i},\mathrm{m}+1} := lr_{\mathrm{m},\mathrm{i}} \\ & \mathbf{end}\ \mathbf{for} \end{aligned}
```

Others:

```
\begin{aligned} &\mathbf{loop} \\ & \mathrm{read}\ lr_{1,\mathrm{i}} := \mathrm{read}(r_{1,\mathrm{i}}) \\ & \mathbf{if}\ lr_{1,\mathrm{i}} \neq r_{\mathrm{i},2}\ \mathbf{then} \\ & \mathrm{write}\ r_{\mathrm{i},2} := lr_{1,\mathrm{i}} \\ & \mathbf{end}\ \mathbf{if} \end{aligned} \mathbf{for}\ m := 2\ \mathbf{to}\ \delta\ \mathbf{do} \\ & lr_{\mathrm{m},\mathrm{i}} := \mathrm{read}(r_{\mathrm{m},\mathrm{i}}) \\ & \mathrm{write}\ r_{\mathrm{i},\mathrm{m}+1} := lr_{\mathrm{m},\mathrm{i}} \\ & \mathbf{end}\ \mathbf{for} \end{aligned}
```

Maximal matching

```
\begin{aligned} &\textbf{loop} \\ &\textbf{if pointer}_i = \textbf{null and } (\exists \ P_j \in N(i) \ | \ \textbf{pointer}_j = i) \ \textbf{then} \\ &\textbf{pointer}_i := j \\ &\textbf{end if} \end{aligned} &\textbf{if pointer}_i = \textbf{null and } (\forall \ P_j \in N(i) \ | \ \textbf{pointer}_j \neq i) \ \textbf{and } (\exists \ P_j \in N(i) \ | \ \textbf{pointer}_j \\ &= \textbf{null) then} \\ &\textbf{pointer}_i := j \\ &\textbf{end if} \end{aligned} &\textbf{if pointer}_i = j \ \textbf{and pointer}_j = k \ \textbf{and } k \neq i \ \textbf{then} \\ &\textbf{pointer}_i := \textbf{null} \\ &\textbf{end if} \end{aligned} &\textbf{end if}
```

Leader election in general graph

```
\begin{aligned} & | \text{loop} \\ & \langle \text{candidate, distance} \rangle := \langle \text{ID}(i,0) \rangle \\ & \text{for all $P_j \in N(i)$ do} \\ & \langle \text{leader}_i[j], \, \text{dist}_i[j] \rangle := \text{read}(\langle \text{leader}_i, \, \text{dist}_i \rangle \ ) \end{aligned} & \text{if } ((\text{dist}_i[j] < N) \text{ and } (\text{leader}_i[j] < \text{candidate})) \text{ or } ((\text{leader}_i[j] = \text{candidate}) \text{ and } (\text{dist}_i[j] < \text{distance})) \text{ then} \\ & \langle \text{candidate, distance} \rangle := \text{read}(\langle \text{leader}_i, \, \text{dist}_i \rangle) \\ & \text{end if} \end{aligned} & \text{end for} \\ & \text{write } \langle \text{leader}_i, \, \text{dist}_i \rangle := \langle \text{candidate, distance} \rangle \\ & \text{end loop} \end{aligned}
```

Self-stabilizing counting

Root:

```
\begin{aligned} & \textbf{loop} \\ & \text{sum} := 0 \\ & \textbf{for all } P_j \in \text{children}(i) \textbf{ do} \\ & \textit{lr}_{j,i} := \text{read}(r_{j,i}) \\ & \text{sum} := \text{sum} + \textit{lr}_{j,i}.\text{count} \\ & \textbf{end for} \\ & \text{count}_i := \text{sum} + 1 \\ & \textbf{end loop} \end{aligned}
```

Others:

```
\begin{split} & \mathbf{loop} \\ & \mathbf{sum} := 0 \\ & \mathbf{for} \ \mathbf{all} \ P_j \in \mathrm{children}(i) \ \mathbf{do} \\ & \mathit{lr}_{j,i} := \mathrm{read}(r_{j,i}) \\ & \mathbf{sum} := \mathbf{sum} + \mathit{lr}_{j,i}.\mathrm{count} \\ & \mathbf{end} \ \mathbf{for} \\ & \mathbf{count}_i := \mathbf{sum} + 1 \\ & \mathbf{write} \ r_{i, \ parent}.\mathbf{count} := \mathbf{count}_i \\ & \mathbf{end} \ \mathbf{loop} \end{split}
```

Self-stabilizing naming

Root:

```
\begin{aligned} & \mathbf{loop} \\ & \mathbf{ID_i} := 1 \\ & \mathbf{sum} := 0 \\ & \mathbf{for\ all}\ P_j \in \mathbf{children}(i)\ \mathbf{do} \\ & \mathit{lr_{j,i}} := \mathbf{read}(\mathbf{r_{j,i}}) \\ & \mathit{lr_{j,i}} := \mathbf{ID_i} + \mathbf{sum} + 1 \\ & \mathbf{sum} := \mathbf{sum}\ \mathit{lr_{j,i}}.\mathbf{count} \\ & \mathbf{end\ for} \\ & \mathbf{end\ loop} \end{aligned}
```

Others:

```
\begin{aligned} & \mathbf{loop} \\ & \mathbf{sum} := 0 \\ & \mathit{lr}_{\mathrm{parent},i} := \mathrm{read}(\mathbf{r}_{\mathrm{parent},i}) \\ & \mathrm{ID}_{i} := \mathit{lr}_{\mathrm{parent},i}.\mathrm{identifier} \\ & \mathbf{for} \ \mathbf{all} \ P_{j} \in \mathrm{children}(i) \ \mathbf{do} \\ & \mathit{lr}_{j,i} := \mathrm{read}(\mathbf{r}_{j,i}) \\ & \mathit{lr}_{j,i} := \mathrm{ID}_{i} + \mathrm{sum} + 1 \\ & \mathrm{sum} := \mathrm{sum} \ \mathit{lr}_{j,i}.\mathrm{count} \\ & \mathbf{end} \ \mathbf{for} \end{aligned}
```

Digital clock synchronization (bounded)

Upon a pulse:

```
\begin{split} & \textbf{for all } P_j \in N(i) \ \textbf{do} \\ & \quad send(j, \operatorname{clock}_i) \\ & \textbf{end for} \\ & \quad max := \operatorname{clock}_i \\ & \textbf{for all } P_j \in N(i) \ \textbf{do} \\ & \quad \operatorname{receive}(\operatorname{clock}_j) \\ & \quad \textbf{if } \max < \operatorname{clock}_j \ \textbf{then} \\ & \quad \max := \operatorname{clock}_j \\ & \quad \textbf{end if} \\ & \quad \textbf{end for} \operatorname{clock}_i := (\max + 1) \ \operatorname{mod} \ ((n+1)d+1) \end{split}
```

Self-stabilizing counting in non-rooted tree

```
loop
   for all P_j \in N(i) do
       lr_{j,i} := read(r_{j,i})
       \operatorname{sum}_i := 0
       for all P_j \in N(i) do
          \operatorname{sum}_i := 0
          for all P_k \in N(i) do
              if P_j \neq P_k then
                  \operatorname{sum}_{i} := \operatorname{sum}_{i} + lr_{ki}.\operatorname{count}
              end if
          end for
       end for
       \operatorname{count}_{\mathbf{i}}[j] := \operatorname{sum}_{\mathbf{j}} + 1
       sum_i := sum_i + sum_i
       write r_{ij}.count := count_i[j]
   end for
   count_i := sum_i \, + \, 1
end loop
```

Update algorithm for P_i

```
\begin{aligned} & \textbf{loop} \\ & \text{Readset} := \emptyset \\ & \textbf{for all } P_j \in N(i) \textbf{ do} \\ & \text{Readset}_i := \text{Readset}_i \cup \text{read}(\text{Processors}_j) \\ & \textbf{end for} \\ & \text{Readset}_i := \text{Readset}_i \setminus \setminus \langle i, * \rangle \\ & \text{Readset}_i := \text{Readset}_i + + \langle *, 1 \rangle \\ & \text{Readset}_i := \text{Readset}_i \cup \langle i, 0 \rangle \\ & \textbf{for all } P_j \in \text{Processors}(\text{Readset}_i) \textbf{ do} \\ & \text{Readset}_i := \text{Readset}_i \setminus \setminus \text{NotMinDis}(P_j, \text{Readset}_i) \\ & \textbf{end for} \\ & \text{write Processors}_i := \text{ConPrefix}(\text{Readset}_i) \\ & \textbf{end loop} \end{aligned}
```

Superstabilizing coloring

```
loop
                                \mathsf{AColors} := \emptyset
                                \operatorname{GColors} := \emptyset
                                for m := 1 to \delta do
                                   lr_{\rm m} := {\rm read}(r_{\rm m})
                                    AColors = Acolors \cup lr_m.color
                                    if ID(m) > i then
                                       GColors = Gcolors \cup lr_m.color
                                    end if
                                end for
                                \mathbf{if}\ \mathrm{colors}_i = \bot\ \mathbf{or}\ \mathrm{color}_i \in \mathrm{GColor}\ \mathbf{then}
                                    color_i = choose(\ \ AColor)
                                end if
                                \mathrm{write}\;\mathrm{color}_i := \mathrm{color}\;
                             end loop
Interrupt section
                             if receiver_{ij} and j > i then
                                colors_i = \bot
                                write\ colors_i = \bot
                             end if
```