

With  $k = 3$  (Fort Boyard version), the first player loses.

