For example, if 1000! has n zeroes at the end, what does that imply?

 $1000! = y \times 10^n$ for some y where y does not end in a zero.