

Règles de la déduction naturelle

$$\begin{array}{c}
 \frac{A \in \Gamma}{\Gamma \vdash A} \quad (ax) \qquad \qquad \frac{}{\Gamma \vdash \top} \quad (\top_i) \\
 \\
 \frac{\Gamma, \neg A \vdash \perp}{\Gamma \vdash A} \quad (RAA) \qquad \qquad ou \qquad \qquad \frac{\Gamma \vdash \perp}{\Gamma \vdash A} \quad (\perp_e) \\
 \\
 \frac{\Gamma, A \vdash B}{\Gamma \vdash A \rightarrow B} \quad (\rightarrow_i) \qquad \qquad \frac{\Gamma \vdash A \rightarrow B \quad \Gamma \vdash A}{\Gamma \vdash B} \quad (\rightarrow_e) \\
 \\
 \frac{\Gamma, A \vdash \perp}{\Gamma \vdash \neg A} \quad (\neg_i) \qquad \qquad \frac{\Gamma \vdash \neg A \quad \Gamma \vdash A}{\Gamma \vdash \perp} \quad (\neg_e) \\
 \\
 \frac{\Gamma \vdash A \quad \Gamma \vdash B}{\Gamma \vdash A \wedge B} \quad (\wedge_i) \qquad \frac{\Gamma \vdash A \wedge B}{\Gamma \vdash A} \quad (\wedge_{eg}) \qquad \frac{\Gamma \vdash A \wedge B}{\Gamma \vdash B} \quad (\wedge_{ed}) \\
 \\
 \frac{\Gamma \vdash A}{\Gamma \vdash A \vee B} \quad (\vee_{ig}) \qquad \frac{\Gamma \vdash B}{\Gamma \vdash A \vee B} \quad (\vee_{id}) \qquad \frac{\Gamma \vdash A \vee B \quad \Gamma, A \vdash C \quad \Gamma, B \vdash C}{\Gamma \vdash C} \quad (\vee_e) \\
 \\
 \frac{\Gamma \vdash A \quad x \notin FV(\Gamma)}{\Gamma \vdash \forall x A} \quad (\forall_i) \qquad \qquad \frac{\Gamma \vdash \forall x A}{\Gamma \vdash A[x := t]} \quad (\forall_e) \\
 \\
 \frac{\Gamma \vdash A[x := t]}{\Gamma \vdash \exists x A} \quad (\exists_i) \qquad \qquad \frac{\Gamma \vdash \exists x A \quad \Gamma, A \vdash B \quad x \notin FV(\Gamma, B)}{\Gamma \vdash B} \quad (\exists_e)
 \end{array}$$