

188: Best time to Buy and Sell Stock

prices = [2, 4, 1] \Rightarrow integer array with stock prices day wise
k - transactions, \Rightarrow buy at most k times and sell k times.

In above case for k=2, answer is 2.

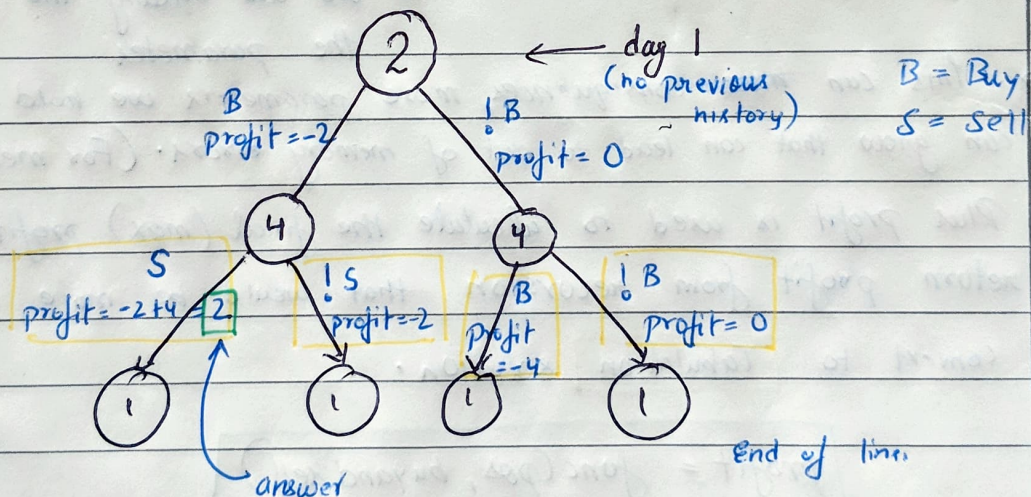
(buy on 1st day and sell on 2nd day)

Note:- Cannot purchase multiple stocks on same day.

Logic

At any day:-

Buy / Not buy (If last transaction was sell)
Sell / Not sell (If last transaction was buy)



We can create a recursive solution from this approach.

Steps

- 1) Figure out how many parameters are required in the recursive solution.

func (pos, buy, sell, last_trans, profit)

- pos \uparrow current position in prices array
- buy \uparrow Increase buy count
- sell \uparrow You buy or sell depends on last transaction
- last_trans \uparrow How many times sold
- profit \uparrow profit upto current recursion.

2) See if the number of parameters can be reduced.

buy
sell
last-trans } All can be represented by only one variable.

buy and sell When we buy we increment it by 1
When we sell we increment it by 1

Buy is only possible when last transaction was sell
and Sell is only possible when last transaction was buy.

∴ When $\text{buyand sell} \% 2 == 0$ You Buy
else: You sell

3) func(pos, buyand sell, profit)

↑ we are holding the profit in the parameter.

→ This can have consequences, more parameters we hold, stack size can grow that can lead to out of memory errors. (For memorization)

→ Plus profit is used to calculate the final (max) profit, if we return profit from recursion, that would be more easy to convert to Tabulation solution.

profit = func(pos, buyand sell)

4) Base cases:

if $\text{pos} \geq \text{len}(\text{prices})$ or $\text{buyand sell} \geq 2 * k$: return 0

5) Recurrence relation:

Options are do nothing (move to next day) OR
Buy or sell and move to next day.

$F(\text{pos}, \text{buyand sell}) = F(\text{pos} + 1, \text{buyand sell})$

if $\text{buyand sell} \% 2 == 0$
 $F(\text{pos}, \text{buyan$

do-nothing = $F(\text{pos} + 1, \text{buy and sell})$

do-something = 0

if buyandsell % 2 == 0:

do-something = $F(\text{pos} + 1, \text{buyandsell} + 1) - \text{prices}[\text{pos}]$

else:

do-something = $F(\text{pos} + 1, \text{buyandsell} + 1) + \text{prices}[\text{pos}]$

~~return~~

$F(\text{pos}, \text{buyandsell}) = \max(\text{do-nothing}, \text{do-something})$