



The VCL model of Secure Simple Bank

Nuno Amálio Laboratory for Advanced Software Systems University of Luxembourg 6, rue R. Coudenhove-Kalergi L-1359 Luxembourg

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Version	Date	Description							
0.1	01/10/2010	1st release							
0.2	30/09/2011	Uses VCL diagrams produced with the Visual Contract Builder Tool.							
0.3	21/11/2012	Updates VCL diagrams to reflect changes to the syntax.							
0.4	23/09/2013	Slight changes to case study, diagrams and resulting Z.							

Table 1: Document Revision History

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Chapter 1

Introduction

The Visual Contract Language (VCL) [AK10a, AKMG10, AK10b, AKM10] expresses software designs. Its approach to modelling is akin to object-oriented modelling. VCL's semantic basis is set theory; design by contract (pre- and post-conditions) is used to model behaviour. VCL is supported by a tool, the Visual Contract Builder (VCB) [AGK11]¹.

This document presents the VCL model of the secure simple Bank case study together with the Z specification generated from the VCL model. The next section describes the requirements of this case study. Chapter 2 presents the VCL model. The Z specification that is generated from the VCL model is given in chapter 3.

1.1 Case Study

The secure simple bank case study extends the simple Bank case study used in [APS05, Amá07, AKM10, AK10a]. The extension covers the security concerns of authentication and access-control. The requirements of this system are listed in table 1.1.

Table 1.1: Requirements of the secure simple bank system.

R1	The bank system shall keep information of customers and their Bank accounts.
	A customer may hold many accounts; an account is held by one customer only.
R2	A customer record comprises a customer number, a name, an address and a
	type (either <i>corporate</i> or <i>personal</i>). Each customer has its own unique customer
	number.
R3	A Bank account shall have an account number, a balance indicating how much
	money there is in it, and its type (either <i>current</i> or <i>savings</i>). Each account has
	its own unique account number.
R4	Accounts of type savings cannot have negative balances.
R5	Customers of type corporate cannot hold savings accounts.
R6	Customers may hold savings accounts provided they also hold a current account
	with the Bank.

¹http://vcl.gforge.uni.lu

R7	The system shall provide an operation to create customers records. This takes
	as input the customer's name, address and type; the customer number is to be
	assigned internally by the system.
R8	The system shall provide an operation to open bank accounts for some customer.
	This takes as input a customer number and a type of account; the account number
	is to be assigned internally by the system.
R9	The system shall provide an operation to deposit money into a bank account.
	This takes as input an account number and an amount to be deposited.
R10	The system shall provide an operation to withdraw money from some bank ac-
	count. This takes as input an account number and an amount to be withdrawn.
R11	The system shall provide an operation to view the balance of some bank account.
	This takes as input an account number and outputs the account's balance.
R12	The system shall provide an operation to obtain a list of all accounts of some
	customer. This takes as input a customer number and outputs the set of accounts
	numbers corresponding to accounts held in the bank by the customer.
R13	The system shall provide an operation to view a list of all accounts that are in
	debt in the bank. This outputs the set of accounts numbers corresponding to
	accounts held in the bank that are in debt.
R14	The system shall provide an operation to delete accounts from the system. This
	takes as an input the number of the account to be deleted. A bank account may
	be deleted provided its balance is 0.
R15	Users have to authenticate themselves prior to opening a system session (login),
	which needs to be closed when they no longer need the system's services $(logout)$.
R16	Users have their access to the system suspended if they miss a password for three
	consecutive times.
R17	There are two kinds of users: <i>clerks</i> and <i>managers</i> . Managers can execute <i>create</i>
	customer records, open accounts and delete accounts. Clerks can execute deposit
	and withdraw. Both managers and clerks can execute get balance, get customer
	accounts and get accounts in debt.
R18	A system service or operation may be used provided users have an open session
	and they have the required permissions to execute task.
R19	The system shall provide a functionality to suspend transactions for security
	reasons. If transactions are suspended, no deposits and withdrawals are allowed.
	The system shall allow transactions to be resumed once they have been suspended.

Chapter 2

The VCL Model

This chapter presents the VCL model of the secure simple Bank case study, which is divided in VCL packages. All diagrams presented here were drawn using the VCB tool. The following presents each packages of the VCL model.

2.1 Package CommonTypes

The container package CommonTypes encapsulates common structures of the VCL model. Figure 2.1 presents this package's package and structural diagrams. It introduces the set Name representing a set of names.

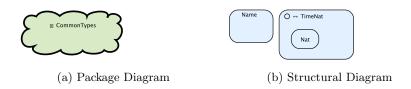


Figure 2.1: Package and structural diagrams of package CommonTypes

2.2 Package Bank

The ensemble package Bank localises the problem domain concern of banking. It introduces structures related with customer and their bank accounts. Figure 2.2 presents the package and structural diagrams of this package. Bank is an ensemble package that extends (or incorporates) the package CommonTypes (Fig. 2.2a).

2.2.1 Structural Diagrams

The VCL SD of package Bank (Fig. 2.2b) is as follows:

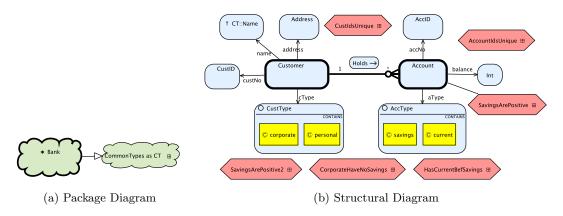


Figure 2.2: Package and structural diagrams of package Bank

- Values sets CustID and AccID represent the set of customer and account identifiers. Blob Address represents a set of postal addresses.
- Blobs CustType and AccType define customer and account types, respectivelly.
 They are defined by enumeration. CustType has elements corporate and personal; AccType has elements savings and current.
- Domain sets Customer and Account represent the main problem domain concepts (requirement R1). Property edges name, cType, address and custNo hold information of customers (Requirement R2); accNo, balance and aType hold information of accounts (Requirement R3).
- Relational edge Holds relates customers and their accounts. UML-style multiplicity constraints say that a customer may have many accounts and that an account is held by one Customer (Requirement R1).
- Several assertions represent constraints on the state space of the system. SavingsArePositive is local; it represents requirement R4. Remaining assertions are global: CorporateHaveNoSavings (represents requirement R5) and HasCurrent-BefSavings (represents requirement R6).

2.2.2 Assertion Diagrams of Invariants

The invariants identified in the SD of Fig. 2.2b are defined using VCL Assertion Diagrams (ADs) in Figs. 2.3 and 2.4.

Figure 2.3a presents the AD of local invariant SavingsArePositive (of set Account), which says that savings accounts have positive balances. The declarations compartment is empty; no extra declarations of names are required to describe the assertion. The predicate compartment expresses the required constraint as an implication formula: if the account's type is savings then the balance must be greater or equal than 0. The same

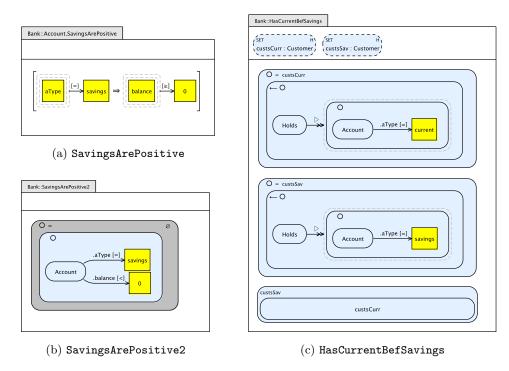


Figure 2.3: ADs of invariants SavingsArePositive, SavingsArePositive2 and Has-CurrentBefSavings

invariant is expressed globally using sets in Fig.2.3b; this defines the set of accounts with negative balances and then says that this set must be empty (outer set is shaded to say that it is empty).

The global invariant HasCurrentBefSavings is described in AD of Fig. 2.3c. The AD defines two hidden variables to hold the set of customers with current accounts (custsCurr) and set of customers with savings accounts (custsSav) and then says that the latter is a subset of former. Sets custsCurr and custsSav are defined by extracting the domain of the relation Holds restricted on the range to either current or savings accounts (the domain operator is \leftarrow and the range restriction operator is \triangleright).

Figure 2.4c presents AD of global invariant CorporateHaveNoSavings. Again, the declarations compartment is empty. The predicate compartment describes this assertion by saying that the set of of all corporate customers with savings accounts (outer set) is empty (shading says that some set is empty), which gives the required meaning. This involves two sets that are then used to constrain the relation Holds. The first set restricts Customer to those objects whose property cType has value corporate. The second set restricts Account to those objects whose property aType has value savings. The two property edge modifiers are then used to restrict the relation Holds according to these two sets.

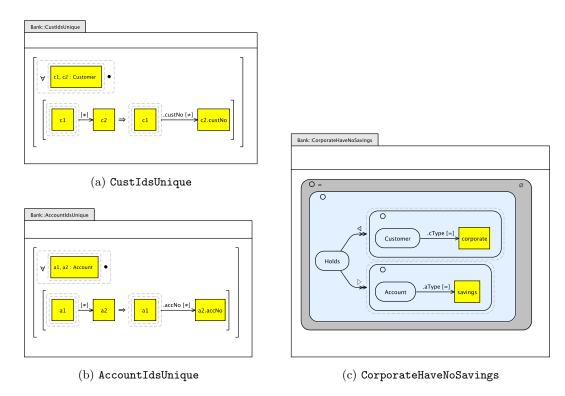


Figure 2.4: ADs of invariants CustIdsUnique, AccountIdsUnique and Corporate-HaveNoSavings

2.2.3 Behaviour

The behaviour diagram (BD) of package Bank is given in Fig. 2.5. It introduces the following operations:

- The update operation New of set Customer, which creates customer objects (a constructor, denoted by symbol \mathbb{N}).
- The local operations of set Account. This includes the update operation New to create Account objects, the update operations Deposit and Withdraw to deposit and withdraw money from some account (update or modifier operations, symbol U), the delete operation Delete to delete account objects (symbol D), and the observe operation GetBalance to retrieve the current balance of some account.
- The global update operations CreateCustomer to create customer records in the system (requirement R7), OpenAccount to create new customer accounts (requirement R8), AccDeposit to deposit money onto some account (requirement R9), AccWithdraw to withdraw money from account (requirement R10) and AccDelete to delete money from some account (requirement R14).

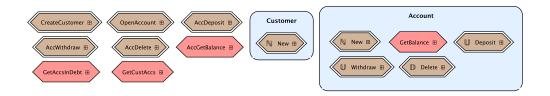


Figure 2.5: Behavioural diagram for the Bank package

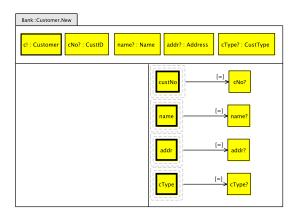


Figure 2.6: Contract diagram of operation New of set Customer

• The global observe operations AccGetBalance to get the balance of some account (requirement R11), GetAccsInDebt to retrieve the accounts that are in debt (requirement R13), and GetCustAccs to retrieve the accounts of some customer (requirement R12).

We now describe the operations of the operations of the BD of Fig. 2.5 using contract and assertion diagrams.

The CD of operation New of set Customer (Fig. 2.6) declares the output c! of type Customer (marked in bold) to represents the Customer object that is returned as a result of the operation. It declares inputs cNo? of type CustID, name? of type Name, addr? of type Address and cType? of type CustType, which represent, respectively, the identifier, name, address and type of the new customer. The predicate assigns in the post-condition the properties custNo, name, address and cType to the declared inputs.

The CD of operation New of set Account (Fig. 2.7a) declares the output a! of type Account (marked in bold), which represents the Account object returned as a result of the operation. It declares inputs accNo? of type AccID and aType? of type AccType, which represent, respectively, the identifier and type of the new account. The predicate assigns in the post-condition the properties accNo to the input accNo?, balance to 0 and aType to the input aType?.

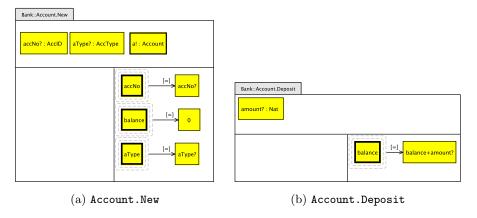


Figure 2.7: Contract diagrams of operations New and Deposit of set Account

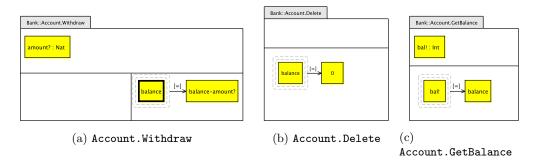


Figure 2.8: Operations Withdraw, Delete and GetBalance of set Account

The CD of operation Deposit of set Account (Fig. 2.7b) declares the input amount of the primitive type Nat (Natural numbers). The post-condition says that the property balance becomes the previous value of balance minus the amount given as input.

The CD of operation Withdraw of set Account (Fig. 2.8a) declares the input amount of the primitive type Nat (Natural numbers). The post-condition says that the property balance becomes the previous value of balance added with the amount given as input.

The AD of operation Delete of set Account (Fig. 2.8b) says that objects may be deleted provided its balance is 0.

The AD of operation GetBalance of set Account (Fig. 2.8c) gives the output bal! the value of the property balance.

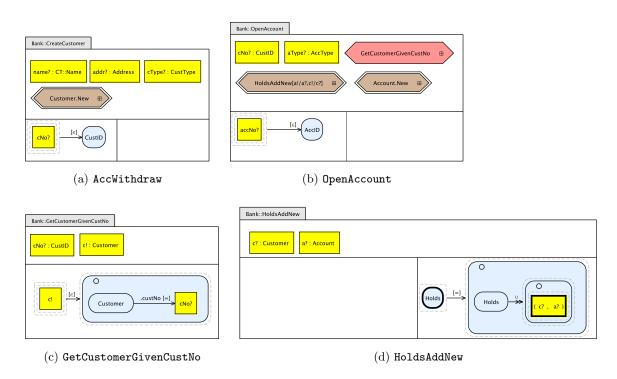


Figure 2.9: Contract diagrams of global operations ${\tt CreateCustomer}$, ${\tt OpenAccount}$ and auxiliary operations

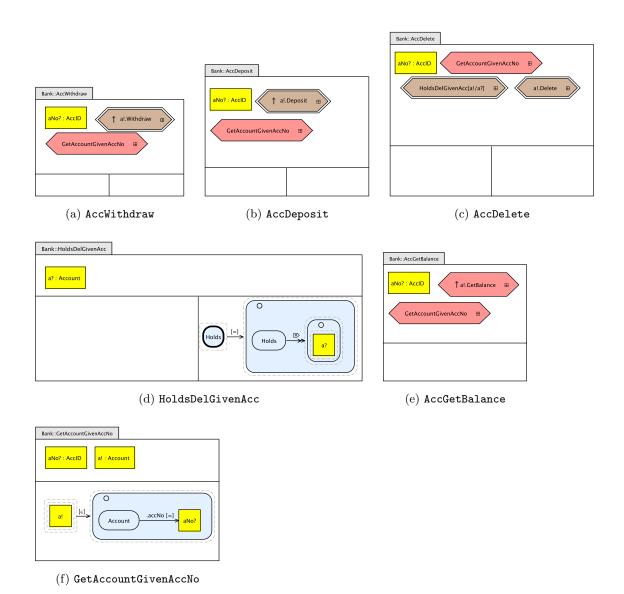


Figure 2.10: Contract diagrams of global operations AccWithdraw, AccDeposit and AccDelete and auxiliary operations

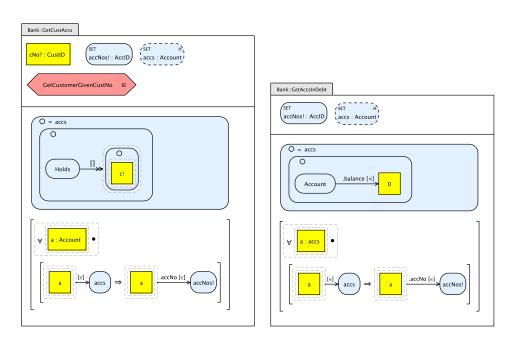


Figure 2.11: Assertion diagrams of global query operations GetCustAccs and GetAccsInDebt

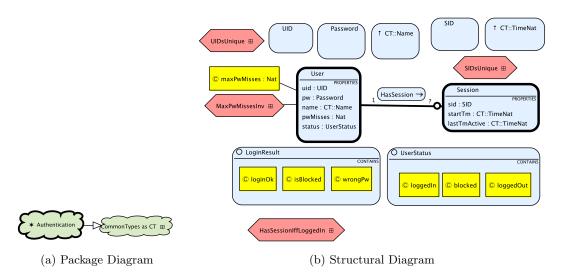


Figure 2.12: Package and structural diagrams of package Authentication

2.3 Package Authentication

The VCL package Authentication defines the core of a general solution to the concern of user authentication. This addresses requirement R15 of Table 1.1. Package Authentication is to be extended by other packages to define authentication-related functionality.

Figure 2.12 presents Authentication's package and structural diagrams. Package Authentication extends package CommonTypes (Fig. 2.12a). The four invariants introduced in the SD of package Authentication (Fig. 2.12b) are given in Fig. 2.13.

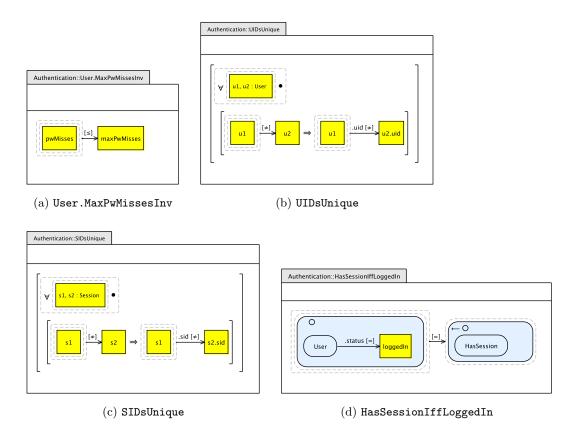


Figure 2.13: Assertion diagrams of package Authentication

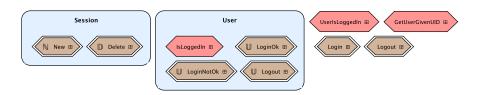


Figure 2.14: Behaviour diagrams of package Authentication

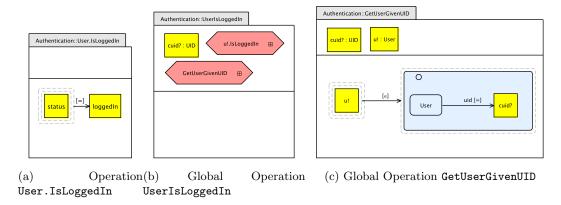


Figure 2.15: Assertion diagrams of observe operations of package Authentication

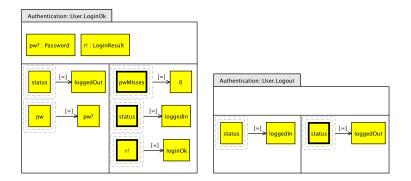
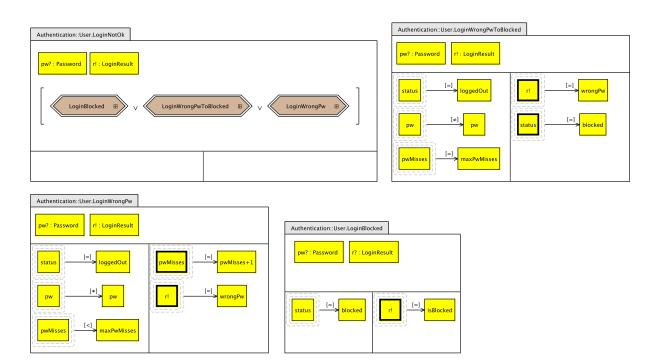


Figure 2.16: Contract Diagrams for local operations LoginOk and Logout of set User.



 $Figure \ 2.17: \ Contract \ Diagrams \ describing \ local \ operation \ \texttt{LoginNotOk} \ of \ set \ \texttt{User}$

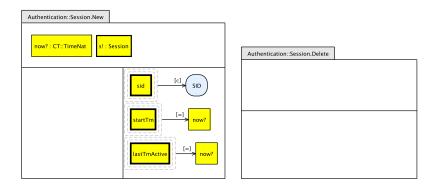


Figure 2.18: Contract Diagrams for local operations New and Delete of set Session.

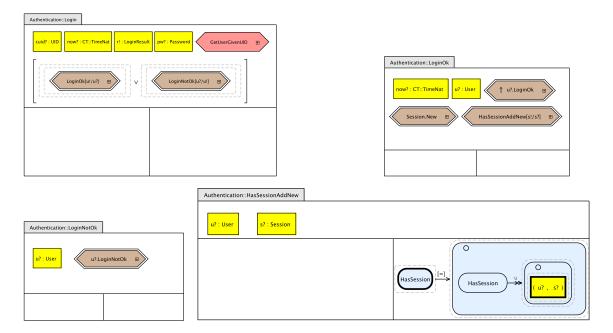


Figure 2.19: Contract Diagrams defining global operations Login

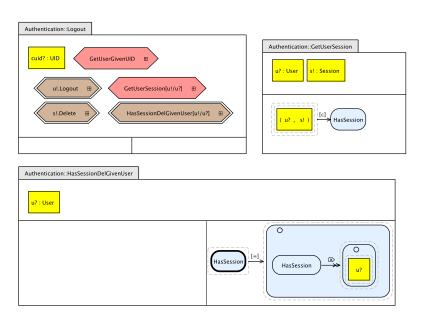


Figure 2.20: Contract Diagrams of global operation Logout and auxiliary definitions

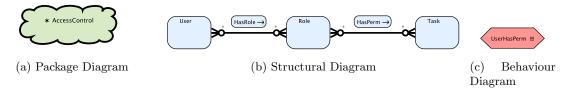
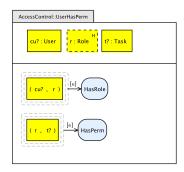


Figure 2.21: Package structural and behaviour diagrams of package AccessControl



(a) Operation UserHasPerm

Figure 2.22: Assertion diagrams of global observe operation UserHasPerm

2.4 Package AccessControl

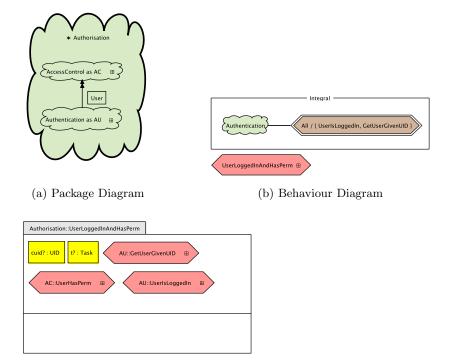
The VCL package AccessControl (Fig. 2.21a) defines the core of a general solution to the concern of access control following a rôle-based access control [SCFY96] scheme. This addresses requirement R16 of secure simple Bank (Table 1.1).

Figure 2.21 presents AccessControl's package, structural and behaviour diagrams. Figure 2.22 presents the AD that defines observe operation UserHasPerm.

2.5 Package Authorisation

VCL Package Authorisation puts together the concerns of authentication and acess-control. This is naturally expressed in the package's PD (Fig. 2.23a); the ensemble package Authorisation extends both Authentication and AccessControl.

Authorisation's BD (Fig. 2.23b) introduces observe operation UserLoggedInAnd-HasPerm, which checks if some user is logged in the system and has permission to execute some task. This is defined in the AD of Fig. 2.23c, which puts together the operations UserIsLoggedIn of package Authentication and UserHasPerm of package AccessControl.



 ${\rm (c)} \ {\rm Query} \ {\rm operation} \ {\tt UserLoggedInAndHasPerm}$

Figure 2.23: VCL diagrams of package Authorisation

2.6 Package RolesAndTasksBank

The VCL package RolesAndTasksBank makes some customisations concerning access control. Package RolesAndTasksBank is an ensemble package (Fig. 2.24a). Its SD (Fig. 2.24b) defines the sets Task and Role according to the needs of the secure simple bank system. In addition, it defines the derived sets ManagerTasks and ClerkTasks (subsets of Tasks), which describe the tasks to be executed by clerks and managers.

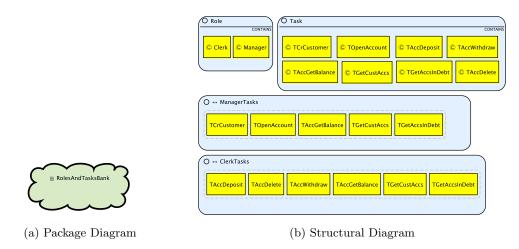


Figure 2.24: Package and structural diagrams of package RolesAndTasksBank

2.7 Package SecForBank

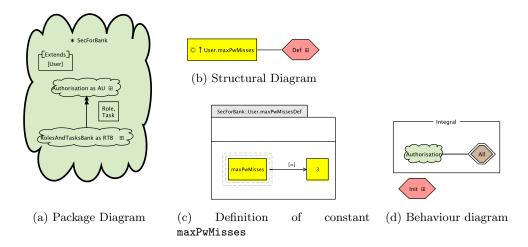


Figure 2.25: VCL Diagrams of package SecForBank

Package SecForBank customises generic package Authorisation for the purpose of secure simple bank.

SecForBank's PD (Fig. 2.25a) says that the ensemble package Authorisation extends the packages Authorisation and RolesAndTasksBak, and that the package RolesAndTasksBak overrides Authorisation on sets Role and Task. This basically says that the access control scheme defined in package AccessControl (incorporated in Authorisation) is to use the sets Role and Task from package RolesAndTasksBak. The SD (Fig. 2.25b) introduces a definition of the constant maxPwMisses defined in package Authentication (incorporated in Authorisation); the value for this constant is defined in the AD of Fig. 2.25c.

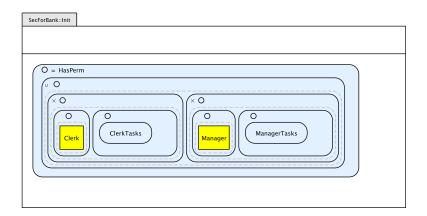


Figure 2.26: Assertion diagram describing Init, the initialisation of package SecForBank

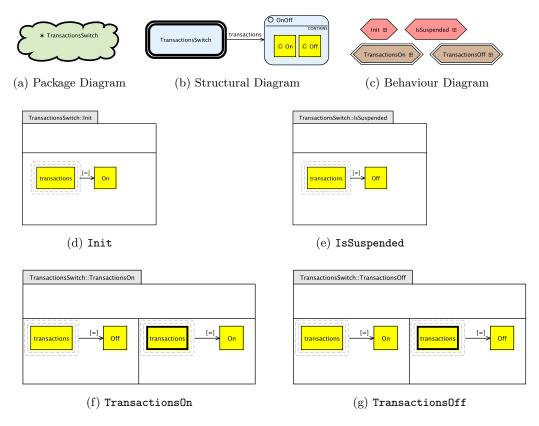


Figure 2.27: VCL diagrams of package TransactionsSwitch

The BD of package SecForBank (Fig. 2.25d) uses an integral extension to say that all global operations of package Authorisation are to be used unaltered in the context of SecForBank. In addition, SecForBank introduces Init, which defines the packages initialisation. Init is defined in the AD of Fig. 2.26; this says that the relation-edge HasPerm of AccessControl is initialised to the union of two sets: (a) the cross product of the set with object Clerk and the set ClerkTasks (the tasks of Clerk are those defined in ClerkTasks) and the cross product of the set with object Manager and the set ManagerTasks (the tasks of Manager are those defined in ManagerTasks).

2.8 Package TransactionsSwitch

This package defines a switch to turn transactions on and off. This addresses requirement R17 of secure simple Bank (Table 1.1).

The PD of TransactionsSwitch (Fig. 2.27a) introduces this ensemble package. The SD (Fig. 2.27a) introduces the package set TransactionsSwitch (singleton representing the whole package) and its property transactions of type OnOff (an enumeration with values On and Off).

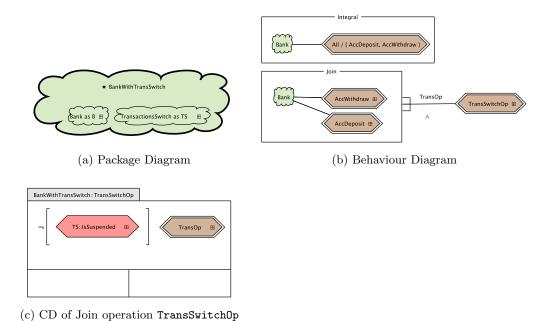


Figure 2.28: VCL diagrams of package BankWithTransSwitch

The package's BD (Fig. 2.27c) introduces Init (the package's initialisation), the observe operation IsSuspended (says whether transactions are suspended), and the updates operations TransactionsOn (turns transactions on) and TransactionsOff (turns transactions off).

The initialisation (Fig. 2.27d) says that initially transactions are not suspended. Operation IsSuspended (Fig. 2.27e) defines a predicate that is true when transactions are suspended. Finally, operations TransactionsOn (Fig. 2.27f) and TransactionsOff (Fig. 2.27g) turn transactions on and off.

2.9 Package BankWithTransSwitch

VCL package BankWithTransSwitch adds the transactions switch mechanism to the package Bank. This ensures that transactions are executed only if they have not been suspended.

BankWithTransSwitch's PD (Fig. 2.28a) says that the ensemble package BankWithTransSwitch extends both Bank and TransactionsSwitch. The BD (Fig. 2.28b) says that all operations of Bank except AccDeposit and AccWithdraw are to be integrally extended (brought into the new context unaltered), and that the Bank operations AccDeposit and AccWithdraw are to be composed with the contract TransSwitchOp (Fig. 2.28c), which adds a precondition to these operations: they may be executed provided transactions are not suspended.

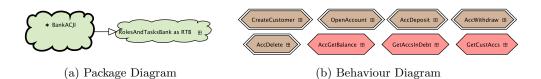


Figure 2.29: Package and behaviour diagram of package BankACJI

2.10 Package BankACJI

This section introduces package BankACJI (Bank Access-Control Join Interface), which defines the interface of package Bank (section 2.2) to the access control concern. This consists of defining an outer interface to be merged with package Bank that will enable composition with the access control concern.

The ensemble package BankACJI (Fig. 2.29a) extends package RolesAndTasksBank. BankACJI's BD (Fig. 2.29a) comprises the same global operations of package Bank. The CD of these operations are defined in CDs of Figs .2.30a to 2.30h.

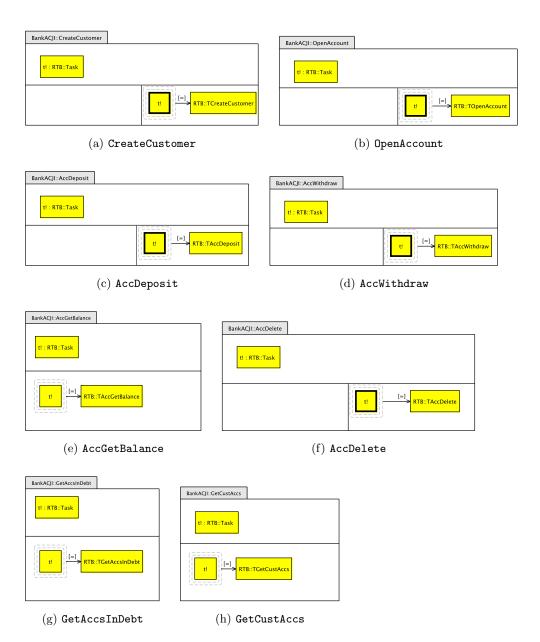


Figure 2.30: Operations of package BankACJI

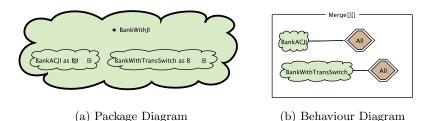


Figure 2.31: Package and behaviour diagrams of package BankWithJI

2.11 Package BankWithJI

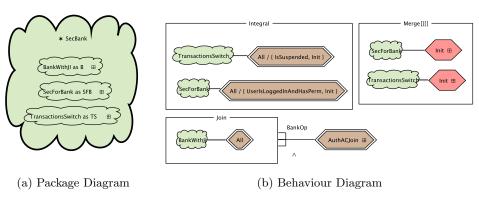
This section introduces package BankWithJI (Bank With Join Interfaces), which adds the access-control join interface, package BankACJI, to the package BankWithTransS-witch.

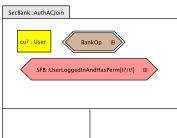
PD of package BankWithJI (Fig 2.31a) says that the ensemble package BankWithJI extends packages BankACJI and BankWithTransSwitch. The BD (Fig:BankWithJI:BD) specifies the merge by saying that all operations of package BankWithJI are to be merged with all operations of package BankACJI; this means that all operations with the same name are merged into a single operation.

2.12 Package SecBank

The package SecBank encapsulates the overall secure simple bank system with all its concerns.

PD of package SecBank (Fig. 2.32a) says that the ensemble package SecBank extends packages SecForBank, AuthenticationOps, BankWithJI and TransactionsSwitch. The BD (Fig. 2.32b) says that all operations of packages TransactionsSwitch and AuthenticationOps are to be used integrally in the new context, and that all operations of package BankWithJI are to be joined with the behaviour specified in the join contract AuthACJoin. The join contract AuthACJoin (Fig. 2.32c) adds a precondition to the joined operation; it says that the operation may be executed provided the current user is logged in and has permissions to execute some given task.





(c) Join contract AuthACJoin

Figure 2.32: VCL diagrams of package SecBank

Chapter 3

Z Specification generated from the VCL model of secure simple Bank

This chapter presents the Z specification generated from the VCL model of secure simple Bank. Appendix A presents some Z definitions from the ZOO toolkit that are used in the Z specifications presented here. The Z specification presented here has been type-checked using the CZT (Community Z Tools) Z type-checker.

3.1 Preamble

```
CLASS ::= CustomerCl \mid AccountCl \mid UserCl \mid SessionCl
```

```
subCl: CLASS \leftrightarrow CLASS
abstractCl: \mathbb{P} \ CLASS
rootCl: \mathbb{P} \ CLASS
subCl = \{\}
abstractCl = \{\}
rootCl = CLASS \setminus \text{dom } subCl
```

3.2 Package CommonTypes

section CommonTypes parents ZOO_Toolkit, Model_Preamble

[Name]

 $TimeNat == \mathbb{N}$

3.3 Package Bank

This section presents Z specification generated for the VCL package Bank (section 2.2).

section Bank parents ZOO_Toolkit, Model_Preamble, CommonTypes

 ${f Set}$ CustType

 $CustType ::= corporate \mid personal$

Set Address

[Address]

Set CustID

[CustID]

Set Customer

Customer0
name: Name
address: Address
custNo: CustID
cType: CustType
Customer
Customer0
$_SCustomer$ $__$
$sCustomer: \mathbb{P}(\mathbb{O}CustomerCl)$
$stCustomer: \mathbb{O}CustomerCl \rightarrow Customer$
dom stCustomer = sCustomer
SCustomerInit
SCustomer'
$sCustomer' = \varnothing$
$stCustomer' = \varnothing$
CustomerNew
Customer'
name?:Name
address?:Address
cType?:CustType
name' = name?
address' = address?
cType' = cType?

```
\Phi BankSCustomerN ___
         \Delta SCustomer
         Customer'
         c!: \mathbb{O}\ CustomerCl
         c! \in \mathbb{O}_x \ CustomerCl \setminus sCustomer
         sCustomer' = sCustomer \cup \{c!\}
         stCustomer' = stCustomer \cup \{(c! \mapsto \theta \ Customer')\}
      SCustomerNew == \exists Customer' \bullet \Phi BankSCustomerN \wedge CustomerNew
Set AccID
      [AccID]
Set AccType
      AccType ::= savings \mid current
Set Account
        Account0
         accNo:AccID
         a\,Type:Acc\,Type
         balance: \mathbb{Z}
        Account Savings Are Positive \_\_\_
         Account0
         (aType = savings) \Rightarrow (balance \ge 0)
        Account_{-}
         Account0
         Account Savings Are Positive
```

```
SAccount ___
 sAccount : \mathbb{P}(\mathbb{O}|AccountCl)
 stAccount: \mathbb{O} \ Account Cl \rightarrow Account
 dom stAccount = sAccount
SAccountInit\_
 SAccount'
 sAccount' = \emptyset
 stAccount' = \emptyset
AccountNew _____
 Account'
 accNo?:ACCID
 aType? : AccType
 accNo' = accNo?
 aType' = aType?
 balance' = 0
AccountDelete
 Account
 balance = 0
AccountDeposit\_
 \Delta Account
 amount?: \mathbb{N}
 accNo' = accNo'
 a\mathit{Type}' = a\mathit{Type}'
 balance' = balance + amount?
```

```
Account Withdraw ___
 \Delta Account
 amount?:\mathbb{N}
 accNo' = accNo'
 aType' = aType'
 balance' = balance - amount?
AccountGetBalance
 \Xi Account
 accBal!: \mathbb{Z}
 accBal! = balance
\Phi BankSAccountN _____
 \Delta SAccount
 Account'
 a!: \mathbb{O} AccountCl
 a! \in \mathbb{O}_x AccountCl \setminus sAccount
 sAccount' = sAccount \cup \{a!\}
 stAccount' = stAccount \cup \{(a! \mapsto \theta \ Account')\}
\Phi BankSAccount U
 \Delta SAccount
 \Delta Account
 a?: \mathbb{O} AccountCl
 a? \in sAccount
 \theta \ Account = stAccount \ a?
 sAccount' = sAccount
 stAccount' = stAccount \oplus \{(a? \mapsto \theta \ Account')\}
\Phi BankSAccountO ___
 \Xi SAccount
\Xi Account
 a?: \mathbb{O} AccountCl
 a? \in sAccount
 \theta \ Account = stAccount \ a?
```

```
\Phi BankSAccountD ____
           \Delta SAccount
           Account
           a?: \mathbb{O} AccountCl
           a? \in sAccount
           \theta Account = stAccount \ a?
           sAccount' = sAccount \setminus \{a?\}
           stAccount' = \{a?\} \lessdot stAccount
       SAccountNew == \exists Account' \bullet \Phi BankSAccountN \wedge AccountNew
       SAccountDelete == \exists Account \bullet \Phi BankSAccountD \land AccountDelete
       SAccountDeposit == \exists \Delta Account \bullet \Phi BankSAccountU \wedge AccountDeposit
       SAccountWithdraw == \exists \Delta Account \bullet \Phi BankSAccountU \wedge AccountWithdraw
       SAccountGetBalance == \exists \Delta Account \bullet \Phi BankSAccountO \wedge AccountGetBalance
Relational Edge Holds
           rHolds: \mathbb{O}\ CustomerCl \leftrightarrow \mathbb{O}\ AccountCl
         . HoldsInit _
           Holds'
           rHolds' = \emptyset
          HoldsAddNew\_
           \Delta Holds
           a?: \mathbb{O} AccountCl
           c?: \mathbb{O} \ CustomerCl
```

A Holds Del Given Account $\Delta Holds$ $a?: \mathbb{O} Account Cl$ $r Holds' = r Holds \Rightarrow \{a?\}$

 $rHolds' = rHolds \cup \{(a?, c?)\}$

Global State

```
BankGblSt \_
SCustomer
SAccount
Holds
BankHoldsGCnt __
BankGblSt
mult(rHolds, sCustomer, sAccount, om, \varnothing, \varnothing)
Bank Savings Are Positive 2
BankGblSt
\{o: sAccount \mid (stAccount \ o).aType = savings \land (stAccount \ o).balance < 0\} = \emptyset
BankCustIdsUnique _____
BankGblSt
\forall c1, c2 : \mathbb{O} \ CustomerCl \bullet
   ((c1 \neq c2) \Rightarrow ((stCustomer\ c1).custNo \neq (stCustomer\ c2).custNo))
BankAccountIdsUnique\_\_\_
BankGblSt
\forall a1, a2 : \mathbb{O} \ AccountCl \bullet
   ((a1 \neq a2) \Rightarrow ((stAccount \ a1).accNo \neq (stAccount \ a2).accNo))
BankCorporateHaveNoSavings\_
BankGblSt
(\{o: sCustomer \mid (stCustomer o).cType = corporate\}
   \triangleleft rHolds) \triangleright \{o : sAccount \mid (stAccount \ o) . aType = savings\} = \emptyset
```

```
BankHasCurrentBefSavings0
   BankGblSt
   custsCurr: \mathbb{PO} CustomerCl
   custsSav : \mathbb{PO} CustomerCl
   custsCurr = dom(rHolds > \{o : sAccount \mid (stAccount o).aType = current\})
   custsSav = dom(rHolds \triangleright \{o : sAccount \mid (stAccount o).aType = savings\})
   custsCurr \subseteq custsSav
BankHasCurrentBefSavings == BankHasCurrentBefSavings0 \setminus (custsCurr, custsSav)
  BankGbl.
   BankGblSt
   BankHoldsGCnt
   Bank Corporate Have No Savings \\
   Bank Cust Ids Unique \\
   BankHasCurrentBefSavings
   Bank Account Ids Unique \\
   Bank Savings Are Positive 2\\
  BankAHoldsGCnt _
```

 $\operatorname{mult}(rHolds,sCustomer,sAccount,om,\{\},\{\})$

 $BankInit == Bank' \land SCustomerInit \land SAccountInit \land HoldsInit$

Operation CreateCustomer

BankSt

 $\Psi BankCreateCustomer == \Delta Bank \wedge \Xi SAccount \wedge \Xi Holds$ $BankCreateCustomer == \Psi BankCreateCustomer \wedge SCustomerNew$

Operation GetCustomerGivenCustNo

```
BankGetCustomerGivenCustNo\_
BankGblSt
cNo?: CustID
c!: \bigcirc CustomerCl
c! \in \{o: sCustomer \mid (stCustomer \ o).custNo = cNo?\}
```

Operation OpenAccount

Operation GetAccountGivenAccNo

```
BankGetAccountGivenAccNo\_
BankGblSt
aNo? : AccID
a! : \mathbb{O} \ AccountCl
a! \in \{o : sAccount \mid (stAccount \ o) . accNo = aNo?\}
```

Operation AccDelete

```
\begin{split} \Psi BankAccDelete =&= \Delta \ Bank \ \land \Xi \ Customer \\ BankAccDelete =&= \Psi BankAccDelete \ \land \ GetAccountGivenAccNo \ \land \ SAccountDelete \\ \land \ HoldsDelGivenAccount \ \backslash \ (a?) \end{split}
```

Operation AccDeposit

```
\Psi BankAccDeposit == \Delta Bank \wedge \Xi Customer \wedge \Xi Holds
BankAccDeposit == \Psi BankAccDeposit \wedge GetAccountGivenAccNo \wedge SAccountDeposit \setminus (a?)
```

Operation AccWithdraw

```
\Psi BankAccWithdraw == \Delta Bank \wedge \Xi Customer \wedge \Xi Holds
BankAccWithdraw = \Psi BankAccWithdraw \land GetAccountGivenAccNo \land SAccountWithdraw \setminus (a?)
```

Operation AccGetBalance

 $BankAccGetBalance == \Xi Bank \land \land GetAccountGivenAccNo \land SAccountGetBalance \setminus (a?)$

Operations GetAccsInDebt and GetCustAccounts

```
BankGetAccsInDebt0 ___
BankGbl
accs: \mathbb{P} \mathbb{O} AccountCl
accNos!: \mathbb{P} AccID
accs = \{o : sAccount \mid (stAccount o).balance < 0\}
\forall a : \mathbb{O} \ AccountCl \bullet
   ((a \in accs) \Rightarrow ((stAccount \ a).accNo \in accNos!))
```

 $BankGetAccsInDebt == BankGetAccsInDebt0 \setminus (accs)$

```
BankGetCustomerGivenCustNo\_
BankGblSt
cNo?: CustID
c! : \mathbb{O} \ CustomerCl
c! \in \{o : sCustomer \mid (stCustomer o).custNo = cNo?\}
```

```
BankGetCustAccs0
```

```
BankGbl
cNo? : \mathit{CustID}
accs: \mathbb{PO} AccountCl
c! : \mathbb{O} \ CustomerCl
accNos!: \mathbb{P} AccID
BankGetCustomerGivenCustNo\\
accs = rHolds (\{c!\})
\forall a : \mathbb{O} \ AccountCl \bullet
  ((a \in accs) \Rightarrow ((stAccount \ a).accNo \in accNos!))
```

```
BankGetCustAccs == BankGetCustAccs0 \setminus (accs, c!)
```

3.4 Package Authentication

The following presents the Z specification that is generated for VCL package Authentication (section 2.3).

 ${f section}\ Authentication\ {f parents}\ ZOO_Toolkit,\ Model_Preamble,\ CommonTypes$

Set LoginResult

```
LoginResult ::= loginOK \mid wrongPW \mid isBlocked
```

Set UID

[SID]

Set Session

```
Session0 \\ sid : SID \\ startTm : TimeNat \\ lastTmActive : TimeNat
Session \\ Session0
Session : \mathbb{P}(\mathbb{O} \ SessionCl) \\ stSession : \mathbb{O} \ SessionCl \Rightarrow Session \\ dom \ stSession = sSession
```

```
SSessionInit\_
 SSession
 sSession = \emptyset \land stSession = \emptyset
. SessionNew\_
 Session'
 sid?:SID
 now?:\mathit{Time}
 sid' = sid?
 startTm' = now?
 lastTmActive' = now?
SessionDelete _____
 Session
\Phi SSessionNew ___
 \Delta SSession
 Session'
 s!: \mathbb{O} \, SessionCl
 s! \in \mathbb{O}_x \ SessionCl \setminus sSession
 sSession' = sSession \cup \{s!\}
 stSession' = stSession \cup \{(s! \mapsto \theta \ Session')\}
\Phi SSession Upd
 \Delta SSession
 \Delta Session
s?: \mathbb{O} SessionCl
 s? \in sSession
 \theta Session = stSession s?
 \mathit{sSession'} = \mathit{sSession}
 stSession' = stSession \oplus \{(s?, \theta Session')\}
```

```
 \begin{array}{l} \Phi SSessionO \\ SSession \\ Session \\ s?: \mathbb{O} \ SessionCl \\ \hline s? \in sSession \\ \theta \ Session = stSession \ s? \end{array}
```

```
SSessionNew == \exists Session' \bullet \Phi SSessionNew \land SessionNew
SSessionDelete == \exists Session \bullet \Phi SSessionDel \land SessionDelete
```

Set UserStatus

```
UserStatus ::= loggedIn \mid blocked \mid loggedOut
```

Set Password

[Password]

Set UID

[UID]

Set User

This defines constant maxPWMisses.

 $UsermaxPwMisses: \mathbb{N}$

<i>User</i> 0
uid:UID
pw: Password
name: Name
$pwMisses: \mathbb{N}$
status : UserStatus
UserMaxPwMissesInv
User0
$pwMisses \le UsermaxPwMisses$
User
User0
$\overline{UserMaxPwMissesInv}$
$sUser: \mathbb{P}(\mathbb{O}\ UserCl)$ $stUser: \mathbb{O}\ UserCl \rightarrow User$
$stUser: \cup UserUl \rightarrow User$
$dom \ stUser = sUser$
SUserInit
SUser
$sUser = \varnothing \wedge stUser = \varnothing$
Hoomfol opposite
$_$ UserIsLoggedIn $_$ User
USET
status = logaedIn


```
UserLoginNotOk == UserLoginBlocked \lor UserLoginWrongPW \\ \lor UserLoginWrongPWToBlocked SUserLoginOk == \exists \Delta User \bullet \Phi SUserUpd \land UserLoginOk SUserLogout == \exists \Delta User \bullet \Phi SUserUpd \land UserLogout SUserLoginNotOk == \exists \Delta User \bullet \Phi SUserUpd \land UserLoginNotOk
```

Relation Edge HasSession

```
HasSessionAddNew\_
        \Delta Has Session
        u?: \mathbb{O}\ UserCl
        s?: \mathbb{O} \operatorname{SessionCl}
        rHasSession' = rHasSession \cup \{(u?, s?)\}
       Has Session Del Given User \_
        \Delta HasSession
        u?: \mathbb{O}\ UserCl
       rHasSession' = \{u?\} \leqslant rHasSession
       Has Session Get User Session
        HasSession
        u?: \mathbb{O}\ UserCl
        s!: \mathbb{O} SessionCl
        (u?, s!) \in rHasSession
Global State
       Authentication GblSt
        SUser
        SSession
        AHas Session
       Authentication Has Session GCnt
        Authentication GblSt
        mult\ (rHasSession,\ sUser,\ sSession,\ ozo,\varnothing,\varnothing)
       Authentication Has Session Iff Logged In \_\_\_\_
        Authentication GblSt\\
        \{o: sUser \mid (stUser \ o).status = loggedIn\} = dom(rHasSession)
```

 $AuthenticationInit == AuthenticationGbl' \land SUserInit \land SSesionInit \land HasSessionInit$

Global Behaviour

```
SUserOF.
   SUser
   User
   o?: \mathbb{O} \ UserCl
   o? \in sUser
   \theta \ User = stUser o?
SUserIsLoggedIn == \exists User \bullet
  SUserOF \land UserIsLoggedIn
  Authentication User Is Logged In 0 _
   AuthenticationGbl
   cuid?:UID
   u! : \mathbb{O} \ \mathit{UserCl}
   SUserIsLoggedIn[u!/o?]
   Authentication Get User Given UID \\
AuthenticationUserIsLoggedIn == AuthenticationUserIsLoggedIn0 \setminus (u!)
\Psi Authentication Login Ok == \Delta Authentication Ops
AuthenticationLoginOk == \Psi AuthenticationLoginOk \wedge SUserLoginOk
  \land SSessionNew \land HasSessionAddNew[s!/s?] \setminus (sid?, s!)
\Psi Authentication Login Not Ok ==
  \Delta Authentication \wedge \Xi SSession \wedge \Xi HasSession
AuthenticationLoginNotOk ==
  \Psi Authentication Login Not Ok \wedge SUser Login Not Ok
AuthenticationLogin == SUserGetUserGivenID[u?/u!] \land
  (AuthenticationLoginOk \lor AuthenticationLoginNotOk) \setminus (u?)
\Psi Authentication Logout == \Delta Authentication Ops
AuthenticationLogout == \Psi AuthenticationLogout
  \land SUserGetUserGivenID[u?/u!]
  \land SUserLogout \land HasSessionDelGivenUser
  \land HasSessionGetUserSession[s?/s!]
  \land SessionDelete \setminus (u?, s?)
```

3.5 Package AccessControl

The following presents the Z specification that is generated for VCL package Access-Control (section 2.4).

 ${\bf section} \ Access Control \ {\bf parents} \ ZOO_Toolkit, \ Model_Preamble$

Set	User
	$[\mathit{User}]$
Set	Role
	[Role]
Set	Task
	$[\mathit{Task}]$
\mathbf{Rel}	ation Edge HasPerm
	$HasPerm _$ $rHasPerm : Role \leftrightarrow Task$
	HasPermInit
	HasPerm'
	$rHasPerm' = \varnothing$
Rel	ation Edge HasRole
	HasRole
	$rHasRole: User \leftrightarrow Role$

HasRoleInit
HasRole'
$rHasRole' = \varnothing$
Global State
$_AccessControlGblSt__$
HasPerm
HasRole
$_Access Control Has Perm GCnt ___$
AccessControlGblSt
$\overline{mult\left(rHasPerm,Role,Task,mm,\varnothing,\varnothing\right)}$
$_AccessControlHasRoleGCnt$
AccessControlGblSt
$\overline{ mult (rHasRole, User, Role, mm, \varnothing, \varnothing) }$
$_AccessControlGbl$
AccessControlGblSt
Access Control Has Perm GCnt

 $AccessControlInit == AccessControlGbl' \wedge HasRoleInit \wedge HasPermInit$

3.5.1 Global Behaviour

Access Control Has Role GCnt

 $AccessControlUserHasPerm == AccessControlUserHasPerm0 \setminus (r)$

3.6 Package RolesAndTasksBank

The following presents the Z specification that is generated for VCL package RolesAnd-TasksBank (section 2.6).

3.6.1 Blob *Role*

 $Role ::= Clerk \mid Manager$

3.6.2 Blob *Task*

```
Task ::= TCreateCustomer \mid TOpenAccount \mid TAccDeposit \mid TAccWithdraw \mid TAccGetBalance \mid TAccDelete \mid TGetAccsInDebt \mid TGetCustAccs
```

3.7 Package Authorisation

The following presents the Z specification that is generated for VCL package Authorisation (section 2.5).

3.7.1 Global State

$_Authorisation$ $__$		
Authentication		
Access Control		

3.7.2 Global Behaviour

```
\_AuthorisationUserLoggedInAndHasPerm\_\_\_\_\_
Authorisation
AccessControlUserHasPerm
AuthenticationUserIsLoggedIn
```

3.8 Package SecForBank

The following presents the Z specification that is generated for VCL package SecForBank (section 2.7).

3.8.1 Global State

This gives a value to constant maxPwMisses of package Users:

```
maxPwMisses = 3
SecForBank \_
Authorisation
AccessControlInitMod == AccessControlInit \ (rHasPerm')
```

3.8.2 Global Behaviour

 $SecForBankUserLoggedInAndHasPerm == SecForBank \\ \land AuthorisationUserLoggedInAndHasPerm$

3.9 Package BankACJI

The following presents the Z specification that is generated for VCL package ${\tt BankACJI}$ (section 2.10).

3.9.1 Global Behaviour

BankACJICreateCustomer
t!: Task
t! = TCreateCustomer
BankACJIOpenAccount
t!: Task
t! = TOpenAccount
$_Bank ACJIAcc Deposit ___$
$t!: \mathit{Task}$
t! = TAccDeposit
BankACJIAccWithdraw
t!: Task
t! = TAccWithdraw
BankACJIAccGetBalance
t!: Task
t! = TAccGetBalance



3.10 Package BankWithJI

The following presents the Z specification that is generated for VCL package BankWithJI (section 2.11).

3.10.1 Global State



 $BankWithJIInit == BankWithJI' \land BankInit$

3.10.2 Global Behaviour

Defines the frame for *update* operations.

```
Common With Bank == Bank With JI \upharpoonright Bank Bank With JI Without Bank == \exists \ Common With Bank \bullet \ Bank With JI \Psi Bank With JI Merge Ops == \Delta Bank With JI \land \Xi Bank With JI Without Bank
```

BankWithJICreateCustomer
$\Psi BankWithJIMergeOps$
BankCreateCustomer
Bank ACJIC reate Customer
$_Bank With JIO pen Account ___$
$\Psi BankWithJIMergeOps$
BankOpenAccount
Bank ACJIOpen Account
BankWithJIAccDeposit
$\Psi BankWithJIMergeOps$
BankAccDeposit
BankACJIAccDeposit
2 a.w. 200112002 opcoor
BankWithJIAccWithdraw
BankAccWithdraw
Bank ACJIAccWith draw
BankWithJIAccGetBalance
BankWithJI
BankAccGetBalance
BankACJIAccGetBalance
Danimit Confidence
BankWithJIAccDelete
$\Psi BankWithJIMergeOps$
BankAccDelete
Bank ACJIAccDelete
BankWithJIGetAccsInDebt
BankWithJI
BankGetAccsInDebt
Bank ACJI Get Accs In Debt

$_BankWithJIGetC$	<i>CustAccs</i>	
BankWithJI		
BankGetCustAcc	cs	
BankACJIGetCu	istAccs	

3.11 Package SecBank

The following presents the Z specification that is generated for VCL package SecBank (section 2.12).

3.11.1 Global State

SecBank	
SecForBank	
BankWithJI	
Authentication Ops	
SecBankInit	
SecForBankInit	
Bank With JIInit	
Authentication Ops In it	

3.11.2 Global Bebhaviour

 $SecBankWithoutBankWithJi == \exists CommonWithBankWithJI \bullet SecBank$ $\Psi SecBankOpsFromBankWithJI == \Delta SecBank \wedge \Xi SecBankWithoutBankWithJi$ CreateCustomer _ $\Psi SecBankOpsFromBankWithJI$ $cu?: \mathbb{O} \mathit{UserCl}$ Bank With JIC reate CustomerSecForBankUserLoggedInAndHasPerm[t!/t?]OpenAccount $\Psi SecBank Ops From Bank With JI$ $cu?: \mathbb{O} \mathit{UserCl}$ Bank With JIO pen AccountSecForBankUserLoggedInAndHasPerm[t!/t?] $AccDeposit_{-}$ $\Psi SecBankOpsFromBankWithJI$ $cu?: \mathbb{O} \mathit{UserCl}$ BankWithJIAccDepositSecForBankUserLoggedInAndHasPerm[t!/t?]AccWithdraw $\Psi SecBank Ops From Bank With JI$ $cu?: \mathbb{O} \mathit{UserCl}$ Bank With JIAcc With drawSecForBankUserLoggedInAndHasPerm[t!/t?]

 $CommonWithBankWithJI == SecBank \upharpoonright BankWithJI$

_AccGetBalance	
SecBank	
$cu?: \mathbb{O}\mathit{UserCl}$	
Bank With JIAcc Get Balance	
SecForBank User Logged In And Has Perm[t!/t?]	
. $AccDelete$	
$\Psi Sec Bank Ops From Bank With JI$	
$cu?: \mathbb{O} UserCl$	
Bank With JIAcc Delete	
$\overline{SecForBankUserLoggedInAndHasPerm[t!/t?]}$	
$AccGetAccsInDebt_$ $SecBank$ $cu?: @UserCl$ $BankWithJIAccDeposit$	
SecForBank User Logged In And Has Perm[t!/t?]	
. AccGetCustAccs	
$SecBank$ $cu?: \mathbb{O}UserCl$	
$cu:: \cup UserCt$ $BankWithJIAccWithdraw$	
SecForBankUserLoggedInAndHasPerm[t!/t?]	

Appendix A

ZOO Toolkit

 ${\bf section} \ ZOO_Toolkit \ {\bf parents} \ standard_toolkit$

[OBJ]

 $relation(opt_{-})$

```
[X] = \underbrace{opt_{-} : \mathbb{P}(\mathbb{P}X)}_{opt_{-} : \mathbb{P}X \to X}
\forall S : \mathbb{P}X \bullet opt S \Leftrightarrow (\exists x : X \bullet S = \{x\}) \lor S = \{\}
\forall x : X \bullet the \{x\} = x
```

```
 \begin{split} & [L] \\ & \Sigma : (L \nrightarrow \mathbb{Z}) \to \mathbb{Z} \\ & \Sigma \left\{\right\} = 0 \\ & \forall \, l : L; \, \, n : \mathbb{Z} \bullet \Sigma \left\{(l, n)\right\} = n \\ & \forall \, l : L; \, \, n : \mathbb{Z}; \, \, S : L \nrightarrow \mathbb{Z} \mid \neg \, l \in \mathrm{dom} \, \, S \bullet \Sigma \left(\left\{(l, n)\right\} \cup S\right) = n + \Sigma \, S \end{split}
```

 $\begin{aligned} & \textit{MultTy} ::= mm \mid mo \mid om \mid mzo \mid zom \mid mlo \mid lom \mid lolo \mid loo \mid olo \mid lozo \mid zolo \\ & \mid oo \mid zozo \mid zoo \mid ozo \mid ms \mid sm \mid ss \mid so \mid os \mid szo \mid zos \end{aligned}$

 $\mathbf{relation}(\mathit{mult}_{\,-})$

```
=[X, Y]_{=}
  mult_{-}: \mathbb{P}((X \leftrightarrow Y) \times \mathbb{P} \ X \times \mathbb{P} \ Y \times Mult Ty \times \mathbb{F} \mathbb{N} \times \mathbb{F} \mathbb{N})
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
       (mult(r, sx, sy, mm, s_1, s_2)) \Leftrightarrow r \in sx \leftrightarrow sy
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
       (mult(r, sx, sy, mo, s_1, s_2)) \Leftrightarrow r \in sx \rightarrow sy
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, om, s_1, s_2)) \Leftrightarrow r^{\sim} \in sy \to sx
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, mzo, s_1, s_2)) \Leftrightarrow r \in sx \rightarrow sy
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, zom, s_1, s_2)) \Leftrightarrow r^{\sim} \in sy \to sx
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, mlo, s_1, s_2)) \Leftrightarrow r \in sx \leftrightarrow sy \land dom \ r = sx
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, lom, s_1, s_2)) \Leftrightarrow r \in sx \leftrightarrow sy \land ran \ r = sy
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, lolo, s_1, s_2)) \Leftrightarrow r \in sx \leftrightarrow sy \land dom \ r = sx \land ran \ r = sy
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, loo, s_1, s_2)) \Leftrightarrow r \in sx \rightarrow sy
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, olo, s_1, s_2)) \Leftrightarrow r^{\sim} \in sy \twoheadrightarrow sx
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, lozo, s_1, s_2)) \Leftrightarrow r \in sx \rightarrow sy
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, zolo, s_1, s_2)) \Leftrightarrow r^{\sim} \in sy \twoheadrightarrow sx
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, oo, s_1, s_2)) \Leftrightarrow r \in sx \rightarrowtail sy
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, zozo, s_1, s_2)) \Leftrightarrow r \in sx \rightarrowtail sy
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, zoo, s_1, s_2)) \Leftrightarrow r \in sx \rightarrow sy
  \forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
   (mult(r, sx, sy, ozo, s_1, s_2)) \Leftrightarrow r^{\sim} \in sy \rightarrowtail sx
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\forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
(mult(r, sx, sy, ms, s_1, s_2)) \Leftrightarrow (mult(r, sx, sy, mm, s_1, s_2))
\wedge (\forall x : \operatorname{dom} r \bullet \#(\{x\} \lhd r) \in s_1)
\forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
(mult(r, sx, sy, sm, s_1, s_2)) \Leftrightarrow (mult(r, sx, sy, mm, s_1, s_2))
\wedge (\forall y : \operatorname{ran} r \bullet \# (r \rhd \{y\}) \in s_1)
\forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
(mult(r, sx, sy, ss, s_1, s_2)) \Leftrightarrow (mult(r, sx, sy, ms, s_1, \{\}))
\land (mult(r, sx, sy, sm, s_2, \{\}))
\forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
(mult(r, sx, sy, so, s_1, s_2)) \Leftrightarrow (mult(r, sx, sy, mo, s_1, s_2))
\land (mult(r, sx, sy, sm, s_1, s_2))
\forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
(mult(r, sx, sy, os, s_1, s_2)) \Leftrightarrow (mult(r, sx, sy, om, \{\}, \{\}))
\land (mult(r, sx, sy, ms, s_1, \{\}))
\forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
(mult(r, sx, sy, szo, s_1, s_2)) \Leftrightarrow (mult(r, sx, sy, mzo, \{\}, \{\}))
\land (mult(r, sx, sy, sm, s_1, \{\}))
\forall r: X \leftrightarrow Y; \ sx: \mathbb{P}X; \ sy: \mathbb{P}Y; \ s_1, s_2: \mathbb{FN} \bullet
(mult(r, sx, sy, zos, s_1, s_2)) \Leftrightarrow (mult(r, sx, sy, zom, \{\}, \{\}))
\wedge (mult(r, sx, sy, ms, s_1, \{\}))
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