•all(iterable) -> bool

any(iterable) -> bool

```
List & dictionary mutation:
                                                List comprehensions:
 Numeric types in Python:
                                                                                                                    |>>> a = [10]
                                                                                                                                          >>> a = [10]
                                                  [<map exp> for <name> in <iter exp> if <filter exp>]
 >>> type(2)
                     Represents
                                                                                                                                          >>> b = [10]
                                                                                                                    |>>> b = a
 <class 'int'> ____ integers exactly
                                                  Short version: [<map exp> for <name> in <iter exp>]
                                                                                                                                          >>> a == b
                                                                                                                    >>> a == b
 >>> type(1.5)
                     Represents real
                                                                                                                    True
                                                                                                                                          True
 <class 'float'>≺
                                               A combined expression that evaluates to a list using this
                      numbers with
                                                                                                                    >>> a append(20)
                                                                                                                                          >>> b.append(20)
                                               evaluation procedure:
                    finite precision
                                                                                                                    >>> a == b
                                                                                                                                          >>> a
                                                1. Add a new frame with the current frame as its parent
                                                                                                                                           [10]
                                                                                                                    True
                                               2. Create an empty result list that is the value of the
 Rational implementation using functions:
                                                                                                                                          >>> b
                                                                                                                    >>> a
                                                  expression
                                                                                                                     [10, 20]
                                                                                                                                          [10, 20]
 def rational(n, d):
                                               3. For each element in the iterable value of <iter exp>:
                                                                                                                    >>> b
                                                                                                                                          >>> a == b
      def select(name):
                                                  A. Bind <name> to that element in the new frame from step 1
                                                                                                                     [10, 20]
                                                                                                                                          False
                                      This
           if name == 'n':
                                                  B. If <filter exp> evaluates to a true value, then add
                                    function
                                                                                                                    >>> nums = {'I': 1.0, 'V': 5, 'X': 10}
                                                     the value of <map exp> to the result list
                return n
                                   represents
                                                                                                                     >>> nums['X']
           elif name == 'd': a rational
                                               The result of calling repr on a value is
                                    number
                return d
                                                                                                                    >>> nums['I'] = 1
                                                what Python prints in an interactive session
                                                                                                                    >>> nums['L'] = 50
      return select
                                               The result of calling str on a value is
                                                                                                                     >>> nums
def numer(x):
                                                what Python prints using the print function
                                                                                                                     {'X': 10, 'L': 50, 'V': 5, 'I': 1}
                          Constructor is a
     return x('n')
                                                                                                                     >>> sum(nums.values())
                                                 >>> 12e12
                       higher-order function
                                                                           >>> print(today)
def denom(x):
                                                 1200000000000000.0
                                                                           2014-10-13
     return x('d')
                                                                                                                     >>> dict([(3, 9), (4, 16), (5, 25)])
                                                 >>> print(repr(12e12))
                          Selector calls x
                                                                                                                     {3: 9, 4: 16, 5: 25}
                                                 1200000000000000.0
                                                                                                                     >>> nums get('A', 0)
Lists:
                                                str and repr are both polymorphic; they apply to any object
>>> digits = [1, 8, 2, 8]
                                                                                                                     >>> nums.get('V', 0)
                                                repr invokes a zero-argument method ___repr__ on its argument
>>> len(digits)
                                                                                 >>> today.__str__()
                                                >>> today.__repr__()
                                                                                                                     >>> {x: x*x for x in range(3,6)}
                |digits| -----
>>> digits[3]
                                                'datetime.date(2014, 10, 13)'
                                                                                 '2014-10-13'
                                                                                                                     {3: 9, 4: 16, 5: 25}
                                                                                        def memo(f):
                                                                                                                    >>> suits = ['coin', 'string', 'myriad']
                                                Memoization:
>>> [2, 7] + digits * 2
                                                                                            cache = \{\}
                                                                fib(5)
                                                                                                                     >>> suits.pop() —————
                                                                                                                                                Remove and return
[2, 7, 1, 8, 2, 8, 1, 8, 2, 8]
                                                                                            def memoized(n):
                                                                                                                     'myriad'
                                                                                                                                                 the last element
                                                                                                if n not in cache: |>>> suits remove('string')√
>>> pairs = [[10, 20], [30, 40]]
                                                                                                                                                  Remove a value
                                                                                                    cache[n] = f(n)|>>> suits.append('cup')
                                                                               fib(4)
>>> pairs[1]
                pairs | ---> 0
                                                                                                return cache[n]
                                                                                                                    >>> suits.extend(['sword', 'club'])
[30, 40]
                                               fib(1)
                                    10
                                                        fib(2)
                                                                                                                    >>> suits[2] = 'spade'
>>> pairs[1][0]
                                                                                            return memoized
                                                                                                                                                          Add all
                                                                                                                     >>> suits
30
                                                                       fib(2)
                                                                                      fib(3)
                                                                                                                                                          values
                                                    fib(0)
                                                            fib(1)
                                                                                                                     ['coin', 'cup', 'spade', 'club']
                                                                                                                                                        Replace a
Executing a for statement:
                                                                                                                     >>> suits[0:2] = ['diamond'] <--
                                                                           fib(1)
                                                                                          fib(2)
                                                                                 fib(1)
                                                                   fib(0)
                                                                                                                                                       slice with
for <name> in <expression>:
                                                                                                                     >>> suits
                                    30
                                         40
                                                                                                                                                         values
    <suite>
                                                                                      fib(0)
                                                                                              fib(1)
                                                                                                                     ['diamond', 'spade', 'club']
                                               Call to fib
                                                                                                                    >>> suits insert(0, 'heart') Add an element
 1. Evaluate the header <expression>,
                                               Found in cache
                                                                                                                                                    at an index
   which must yield an iterable value
                                                                                                                     >>> suits
                                               O Skipped
                                                                                                                     ['heart', 'diamond', 'spade', 'club']
   (a sequence)
                                               Type dispatching: Look up a cross-type implementation of an
2. For each element in that sequence,
                                                                                                                     Identity:
                                               operation based on the types of its arguments
   in order:
                                                                                                                     <exp0> is <exp1>
                                               Type coercion: Look up a function for converting one type to
  A. Bind <name> to that element in
                                                                                                                     evaluates to True if both <exp0> and
                                               another, then apply a type-specific implementation.
      the current frame
                                                                                                                     <exp1> evaluate to the same object
  B. Execute the <suite>
                                                                      Exponential growth. Recursive fib takes
                                                             \Theta(b^n)
                                                                                                                     Equality:
                                                                     \Theta(\phi^n) steps, where \phi=\frac{1+\sqrt{5}}{2}pprox 1.61828
                                                                                                                     <exp0> == <exp1>
 Unpacking in a
                        A sequence of
                                                                                                                     evaluates to True if both <exp0> and
 for statement:
                   fixed-length sequences
                                                                                                                     <exp1> evaluate to equal values
                                                                     Incrementing the problem scales R(n)
                                                                                                                     Identical objects are always equal values
                                                  k_2
                                                                      by a factor
>>> pairs=[[1, 2], [2, 2], [3, 2], [4, 4]]
                                                             \Theta(n^2)
                                                                      Quadratic growth. E.g., overlap
>>> same_count = 0
                                                                                                                     You can copy a list by calling the list
                                                                      Incrementing n increases R(n) by the
                                                                                                                     constructor or slicing the list from the
      A name for each element in a
                                                                      problem size n
                                                                                                                     beginning to the end.
          fixed-length sequence
                                                              \Theta(n)
                                                                     Linear growth. E.g., factors or exp
                                                                                                                     Constants: Constant terms do not affect
>>> for (x, y) in pairs:
                                                                                                                     the order of growth of a progess
                                                          \Theta(\log n)
        if x == y:
                                                                      Logarithmic growth. E.g., exp_fast
                                                                                                                                \Theta(500 \cdot n)
                                                                                                                                              \Theta(\frac{1}{500} \cdot n)
                                                                                                                      \Theta(n)
             same_count = same_count + 1
                                                                      Doubling the problem only increments R(n)
                                                                                                                     Logarithms: The base of a logarithm does
>>> same_count
                                                              \Theta(1)
                                                                                                                     not affect the order of growth of a process
                                                                      Constant. The problem size doesn't matter
                                                                                                                      \Theta(\log_2 n) \quad \Theta(\log_{10} n)
                                                                                                                                               \Theta(\ln n)
    -3, -2, -1, 0, 1, 2, 3, 4, \dots
                                               Global frame

►func make_withdraw(balance) [parent=Global]
                                                                                                                    Nesting: When an inner process is repeated
                                                             make_withdraw
                                                                                                                     for each step in an outer process, multiply
                                                                                 func withdraw(amount) [parent=f1]
                                                                                                                     the steps in the outer and inner processes
                                                                 withdraw
                                                                                >>> withdraw = make withdraw(100)
                                                                                                                     to find the total number of steps
             range(-2, 2)
                                                                                >>> withdraw(25)
                                                                                                                     def overlap(a, b):
                                               f1: make_withdraw [parent=Global]
                                                                                                                         count = 0
 Length: ending value — starting value
                                                                                                                                             Outer: length of a
                                                                 balance 50
                                                                                >>> withdraw(25)
                                                  The parent
                                                                                                                         for item in a: <
 Element selection: starting value + index
                                                                withdraw
                                                                                                                             if item in b:<
                                                frame contains
                                                                                def make_withdraw(balance):
                                                                                                                                             Inner: length of b
                                                                  Return
                                                                                                                                 count += 1
                                                the balance of
 >>> list(range(-2, 2))
                           List constructor
                                                                   value
                                                                                  def withdraw(amount):
                                                                                                                         return count
                                                   withdraw
 [-2, -1, 0, 1]
                                                                                        nonlocal balance
                                                                                                                    If a and b are both length n,
                                                f2: withdraw [parent=f1]
                                                                                        if amount > balance:
                                                                                                                     then overlap takes \Theta(n^2) steps
                       Range with a 0
 >>> list(range(4))
                                                                                            return 'No funds'
                                                                 amount 25
                                                                                                                     Lower-order terms: The fastest-growing part
                       starting value
                                                  Every call
 [0, 1, 2, 3]
                                                                                        balance = balance - amount
                                                                  Return 75
                                                                                                                    of the computation dominates the total
                                                 decreases the
                                                                  value '
                                                                                        return balance
Membership:
                           Slicing:
                                                 same balance
                                                                                                                     \Theta(n^2) \Theta(n^2 + n) \Theta(n^2 + 500 \cdot n + \log_2 n + 1000)
                                                                                    return withdraw
                           >>> digits[0:2]
>>> digits = [1, 8, 2, 8]
                                               f3: withdraw [parent=f1]
                            [1, 8]
>>> 2 in digits
                                                                                                     |x = 2|
                                                                                                                Effect
                                                                                   Status
                           >>> digits[1:]
                                                                 amount 25
True

    No nonlocal statement

                                                                                                              Create a new binding from name "x" to number 2
                                                                 Return 50
                           [8, 2, 8]
>>> 1828 not in digits
                                                                                                              in the first frame of the current environment
                                                                                 •"x" is not bound locally
                                                                   value
True
                            Slicing creates

    No nonlocal statement

                                                                                                              Re-bind name "x" to object 2 in the first frame
                                                Strings as sequences:
                              a new object
                                                                                                              of the current environment
                                                                                 •"x" is bound locally
                                                >>> city = 'Berkeley'
                                                                                 •nonlocal x
                                                                                                              Re-bind "x" to 2 in the first non-local frame of
Functions that aggregate iterable arguments
                                                >>> len(city)
                                                                                 •"x" is bound in a
                                                                                                              the current environment in which "x" is bound
•sum(iterable[, start]) -> value
                                                                                 non-local frame
                                                >>> city[3]
•max(iterable[, key=func]) -> value
                                                                                 nonlocal x
                                                                                                              SyntaxError: no binding for nonlocal 'x' found
 max(a, b, c, ...[, key=func]) -> value
                                                                                 •"x" is not bound in
                                               >>> 'here' in "Where's Waldo?"
min(iterable[, key=func]) -> value
                                                                                 a non-local frame
                                               True
 min(a, b, c, ...[, key=func]) -> value
                                                                                 nonlocal x
```

>>> 234 in [1, 2, 3, 4, 5]

>>> [2, 3, 4] in [1, 2, 3, 4]

False

False

•"x" **is** bound in a

• "x" also bound locally

non-local frame

SyntaxError: name 'x' is parameter and nonlocal

def right(self):

return self.branches[1]

```
Root or Root Node
                                                                            Python object system:
 Recursive description:
                                                                            Idea: All bank accounts have a balance and an account holder;
                                  Root label - 3
  •A tree has a root label
                                                                            the Account class should add those attributes to each of its instances
  and a list of branches
                                Branch-
                                                                                                    >>>> a = Account('Jim')
  Each branch is a tree
                                                                               A new instance is
                                                                                                     >>> a.holder
 •A tree with zero branches
                                                                             created by calling a
                                                                                                     'Jim'
   is called a leaf
                                                                                     class
                                                                                                     >>> a balance
 Relative description:
                                                                                                                             An account instance
  Each location is a node
                                                                           When a class is called:
                                                                                                                                      holder: 'Jim'
                                                                                                                        balance: 0
  Each node has a label
                                                                            1.A new instance of that class is created:
 •One node can be the
                                                                           2. The __init__ method of the class is called with the new object as its first
  parent/child of another
                                                                              argument (named self), along with any additional arguments provided in the
                                                                              call expression.
  def tree(label, branches=[]):
                                     Verifies the
      for branch in branches:
                                                                                                 class Account:
                                    tree definition
          assert is_tree(branch);
                                                                                                     >def ___init___(self, account_holder):
                                                                               _init__ is called a
                                                                                                         self.balance = 0
      return [label] + list(branches)
                                                                                  constructor
                                                                                                         self.holder = account_holder
  def label(tree):
                                                                                                     def deposit(self, amount):
                        Creates a list from a
      return tree[0]
                                                                                                         .self.balance = self.balance + amount
                         sequence of branches
                                                                                                         return self.balance
  def branches(tree):
                                                                              self should always be
                                                                                                     def withdraw(self, amount):
                       Verifies that tree is
                                                                             bound to an instance of
      return tree[1:]
                                                                                                         if amount > self.balance:
                          bound to a list
                                                                             the Account class or a
                                                                                                             return 'Insufficient funds'
  def is_tree(tree):
                                                                               subclass of Account
                                                                                                         self.balance = self.balance - amount
      if type(tree) != list or len(tree) < 1:</pre>
                                                                                                         return self.balance
          return False
                                                                                                  >>> type(Account deposit)
      for branch in branches(tree):
                                                                                                  <class 'function'>
                                                                             Function call: all
                                       >>> tree(3, [tree(1),
          if not is_tree(branch):
                                                                                                  >>> type(a.deposit)
                                                                              arguments within
                                                    tree(2, [tree(1),
              return False
                                        . . .
                                                                                                  <class 'method'>
                                                                                 parentheses
                                                              tree(1)])])
      return True
                                        [3, [1], [2, [1], [1]]]
  def is_leaf(tree):
                                                                                                  >>> Account deposit(a, 5)
                                                                             Method invocation:
      return not branches(tree) | def fib_tree(n):
                                                                              One object before
  def leaves(t):
                                    if n == 0 or n == 1:
                                                                                                  >>> a.deposit(2)
                                                                              the dot and other
                                                                                                                              Call expression
      """The leaf values in t.
                                        return tree(n)
                                                                               arguments within
      >>> leaves(fib_tree(5))
                                    else:
                                                                                 parentheses
      [1, 0, 1, 0, 1, 1, 0, 1]
                                                                                                        Dot expression
                                         left = fib tree(n-2),
                                         right = fib_tree(n-1)
      if is_leaf(t):
                                         fib n = label(left) + label(right)
                                                                                                       <expression> . <name>
          return [label(t)]
                                         return tree(fib_n, [left, right])
                                                                             The <expression> can be any valid Python expression.
      else:
                                                                             The <name> must be a simple name.
          return sum([leaves(b) for b in branches(t)], [])
                                                                             Evaluates to the value of the attribute looked up by <name> in the object
 class Tree:
                                                                            that is the value of the <expression>.
     def ___init___(self, label, branches=[]):
                                                  Built-in isinstance
                                                                            To evaluate a dot expression:
          self.label = label
                                               function: returns True if
                                                                            1. Evaluate the <expression> to the left of the dot, which yields
          for branch in branches:
                                                branch has a class that
                                                                                 the object of the dot expression
             assert isinstance(branch, Tree) < is or inherits from Tree
                                                                            2. <name> is matched against the instance attributes of that object;
          self.branches = list(branches)
                                                                                 if an attribute with that name exists, its value is returned
                                    def fib_tree(n):
     def is_leaf(self):
                                                                            3. If not, <name> is looked up in the class, which yields a class
                                        if n == 0 or n == 1:
         return not self.branches
                                                                                 attribute value
                                            return Tree(n)
                                                                            4. That value is returned unless it is a function, in which case a
                                        else:
 def leaves(tree):
                                                                                 bound method is returned instead
                                            left = fib_Tree(n-2)
    "The leaf values in a tree."
                                            right = fib_Tree(n-1)
                                                                             Assignment statements with a dot expression on their left-hand side affect
    if tree.is_leaf():
                                            fib_n = left.label+right.label
                                                                             attributes for the object of that dot expression
         return [tree.label]
                                            return Tree(fib_n,[left, right])
                                                                             • If the object is an instance, then assignment sets an instance attribute
     else:

    If the object is a class, then assignment sets a class attribute

         return sum([leaves(b) for b in tree.branches], [])
class Link:
                  Some zero
                                               Link(4, Link(5))
                                                                                      Account class
                                                                                                         interest: 0.02 0.04 0.05
    empty = () < length sequence
                                               Link instance
                                                              Link instance
                                                                                        attributes
                                                                                                         (withdraw, deposit, ___init___)
    def ___init___(self, first, rest=empty):
                                                first:
                                                              first:
        self.first = first
                                                                                                                                    balance:
                                                                                                balance: 0
                                                                                                                      Instance
                                                                                 Instance
        self.rest = rest
                                                                                                                                    holder:
                                                                                                                                               'Tom'
                                                                                                holder:
                                                                                                          'Jim'
                                                                              attributes of
                                                                                                                   attributes of
                                                rest:
                                                               rest:
    def __getitem__(self, i):
                                                                                                interest: 0.08
                                                                               jim_account
                                                                                                                    tom_account
        if i == 0:
           return self.first
                                                                             >>> jim_account = Account('Jim')
                                                                                                                    >>> jim_account.interest = 0.08
                                    Sequence abstraction special names:
        else:
                                                                                                                     >>> jim_account.interest
                                                                             >>> tom_account = Account('Tom')
             return self.rest[i-1]
                                                                                                                     0.08
                                                                             >>> tom_account.interest
                                                 Element selection []
                                      getitem
                                                                                                                     >>> tom_account.interest
    def ___len__(self):
                                                                             0.02
         return 1 + len(self.rest)
                                                                                                                     0.04
                                                                             >>> jim_account.interest
                                                 Built-in len function
                                     ___len___
                                                                                                                     >>> Account interest = 0.05
                                                                             0.02
     def ___repr__(self):
                                                                                                                     >>> tom_account.interest
                                                                             >>> Account interest = 0.04
         if self.rest:
                                                              Contents of
                                                                                                                     0.05
                                                                             >>> tom_account.interest
             rest_str = ', ' + repr(self.rest)
                                                               the repr
                                                                                                                     >>> jim_account.interest
                                                                             0.04
         else:
                                                              string of a
                                                                                                                     0.08
                                                                             >>> jim_account.interest
             rest_str = 🔼
                                                             Link instance
         return 'Link({0}{1})'.format(self.first, rest_str)
                                                                             0.04
def extend_link(s, t):
                                    >>> s = Link(3, Link(4))
                                                                            class CheckingAccount(Account):
    if s is Link.empty:
                                    >>> extend_link(s, s)
                                                                                 """A bank account that charges for withdrawals."""
        return t
                                    _ink(3, Link(4, Link(3, Link(4))))
                                                                                 withdraw_fee = 1
    else:
                                                                                 interest = 0.01
        return Link(s.first, extend_link(s.rest, t))
                                                                                 def withdraw(self, amount):
Python built-in sets:
                                         >>> s.union({1, 5})
                          >>> <mark>3</mark> in s
                                                                                     return Account.withdraw(self, amount + self.withdraw_fee)
                                         \{1, 2, 3, 4, 5\}
>>> s = \{3, 2, 1, 4, 4\}
                          True
                          >>> len(s)
                                         >>> s.intersection({6, 5, 4, 3})
>>> S
                                                                                     return (super()) withdraw(
                                                                                                                   amount + self.withdraw_fee)
{1, 2, 3, 4}
                                          {3, 4}
A binary search tree is a binary tree where each root is larger than all
                                                                             To look up a name in a class:
values in its left branch and smaller than all values in its right branch
                                                                             1. If it names an attribute in the class, return the attribute value.
class BTree(Tree):
                                                                             2. Otherwise, look up the name in the base class, if there is one.
    empty = Tree(None)
                                                                             >>> ch = CheckingAccount('Tom') # Calls Account.__init__
    def ___init___(self, label, left=empty, right=empty):
                                                                             >>> ch.interest # Found in CheckingAccount
        Tree.___init__(self, label, [left, right])
                                                                             0.01
    @property
                                                                             >>> ch.deposit(20) # Found in Account
    def left(self):
                                                                             20
        return self.branches[0]
                                                                             >>> ch.withdraw(5) # Found in CheckingAccount
    @property
                                                                             14
```