

# Cover Letter — Physical Review D

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Subject: Presubmission: Unified brane-cosmology with  $\rho^2 + C/a^4 \rightarrow$  GW break  $f_{\text{br}}(\lambda)$  and  $\Delta N_{\text{eff}}$  correlation

Dear Editors,

Please consider the manuscript “Unified Brane-Cosmology: A Testable Route to Unification.”

We show that a higher-D brane setup yields a 4D Friedmann equation with a high-energy  $\rho^2$  correction and a dark-radiation term ( $C/a^4$ ). A single parameter (brane tension  $\lambda$ ) sets a stochastic-GW spectral break  $f_{\text{br}} \propto \lambda^{\{1/4\}}$  and correlates with  $\Delta N_{\text{eff}}$ , providing a falsifiable bridge from theory to data (PTA→LISA with CMB/BBN priors).

Highlights:

- Full exposition of the effective 4D equations, cosmology reduction, and minimal likelihood.
- Real-anchored preview fit and DataKit for immediate reproducibility.

We attach an 18-page All-in-One summary (Unicode), a Results Two-Pager with a real-anchored preview fit, and a small DataKit for reproducibility. We will submit the full manuscript via your online system.

Sincerely,

Ricardo Maldonado (sales@rank.vegas)