## Cover Letter — Physical Review Letters

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Subject: Presubmission: Brane-cosmology GW break  $f_br(\lambda) \leftrightarrow \Delta N_eff$  (testable, single-parameter) Dear Editors,

Please consider the manuscript "Unified Brane-Cosmology: A Testable Route to Unification."

We show that a higher-D brane setup yields a 4D Friedmann equation with a high-energy  $\rho^2$  correction and a dark-radiation term (C/a<sup>4</sup>). A single parameter (brane tension  $\lambda$ ) sets a stochastic-GW spectral break f\_br  $\propto \lambda^{1/4}$  and correlates with  $\Delta N_{eff}$ , providing a falsifiable bridge from theory to data (PTA $\rightarrow$ LISA with CMB/BBN priors).

## Highlights:

- Concise, general-interest result: one parameter ( $\lambda$ ) links a GW spectral break to early-universe  $\Delta N_{\rm eff}$ .
- Near-term falsifiability across PTA→LISA; consistency with CMB/BBN required.

We attach an 18-page All-in-One summary (Unicode), a Results Two-Pager with a real-anchored preview fit, and a small DataKit for reproducibility. We will submit the full manuscript via your online system.

Sincerely,

Ricardo Maldonado (sales@rank.vegas)