

# Letter: A testable brane-world unification with early-time $\rho^2$ and dark radiation

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## Abstract

We obtain an effective 4-D cosmology with a  $\rho^2$  correction and a dark-radiation term from a higher-D brane setup. The brane tension  $\lambda$  sets a GW spectral break ( $f_{\text{br}} \propto \lambda^{1/4}$ ) and correlates with  $\Delta N_{\text{eff}}$ , enabling a falsifiable joint test using PTA→LISA and CMB/BBN. We provide posteriors using the official NANOGrav 15-yr KDE spectrum with a Planck-2018 prior and include LISA sensitivity context.

$$f_{\text{br}}(\lambda) \propto \lambda^{1/4}, \quad C/\rho_{Y,0} = \frac{7}{8} \left(\frac{4}{11}\right)^{4/3} \Delta N_{\text{eff}}$$