

# Appendix — Post-Newtonian & Binary-Pulsar Consistency

Scope: summarize why our brane-world cosmology reduces to standard GR in late-time, weak-field tests and in pulsar timing regimes. We assume stabilized radion ( $m_r$  above fifth-force bounds) and  $\rho \ll \lambda$  at late times.

- PPN limit: With  $\rho/\lambda \rightarrow 0$  and negligible projected Weyl term ( $E_{\{\mu\nu\}} \approx 0$ ), metric perturbations obey standard 4D Einstein equations.
- PPN parameters:  $\gamma \approx 1$  and  $\beta \approx 1$  as in GR when extra-dimensional excitations are heavy; preferred-frame and preferred-location parameters vanish.
- Shapiro delay / light deflection: Match GR to current measurement accuracy in Solar-System tests under the same conditions.
- Binary pulsars: Radiation reaction (quadrupole formula) and orbital decay are unchanged at leading order; extra polarizations absent when KK modes are heavy.
- GW speed: Propagation on the brane equals  $c$  in our effective regime; constraints from multimessenger events are satisfied.
- Short-range gravity: Radion mass and warping chosen so that deviations at mm- $\mu$ m scales fall below torsion-balance bounds.
- Cosmology tie-in: Early-time  $p^2$  correction is probed by PTA/LISA via the predicted spectral break, not by late-time PPN tests.