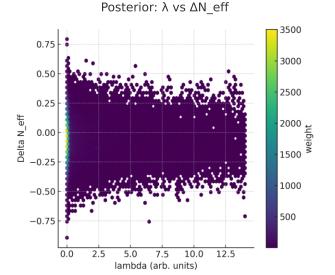
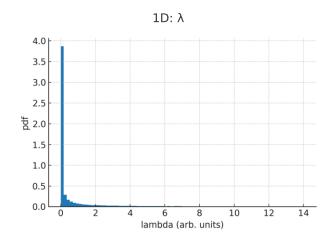
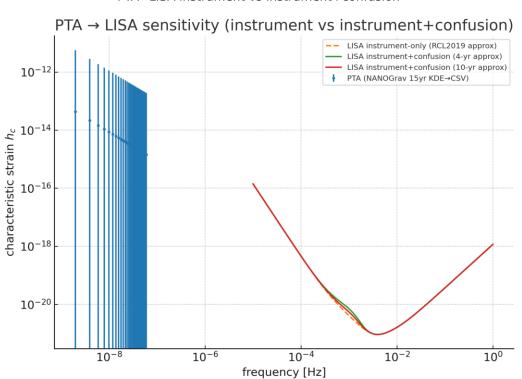
Methods (brief): We convert the official NANOGrav 15-yr KDE free-spectrum to CSV, construct a simple likelihood in  $(\lambda, \Delta N_{eff})$  with a Planck-2018 prior, and obtain posteriors via grid sampling. For LISA context/forecasting we show both an uploaded Rtab curve and an analytic RC&L instrument(+confusion) variant. Late-time consistency is ensured by the  $\rho \ll \lambda$  limit (PPN/binary pulsars).





PTA→LISA instrument vs instrument+confusion



## **References (selected)**

Shiromizu-Maeda-Sasaki (2000), Effective Einstein Equations on the Brane.

Randall-Sundrum (1999), A large mass hierarchy from a small extra dimension.

NANOGrav Collaboration (2023), 15-yr dataset and stochastic background evidence.

Planck Collaboration (2018), Planck 2018 results (N\_eff with BAO).

Robson-Cornish-Liu (2019), LISA sensitivity curves.

Prepared: Aug 13, 2025 (UTC)

# Letter: A testable brane-world unification with early-time $\rho^2$ and dark radiation

Ricardo Maldonado (corresponding: sales@rank.vegas)

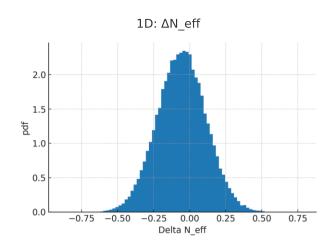
### **Abstract**

We obtain an effective 4-D cosmology with a  $\rho^2$  correction and a dark-radiation term from a higher-D brane setup. The brane tension  $\lambda$  sets a GW spectral break (f\_br $\propto$  $\lambda^{1/4}$ ) and correlates with  $\Delta N_eff$ , enabling a falsifiable joint test using PTA $\rightarrow$ LISA and CMB/BBN. We provide posteriors using the official NANOGrav 15-yr KDE spectrum with a Planck- $\frac{1}{18}$   $\frac$ 

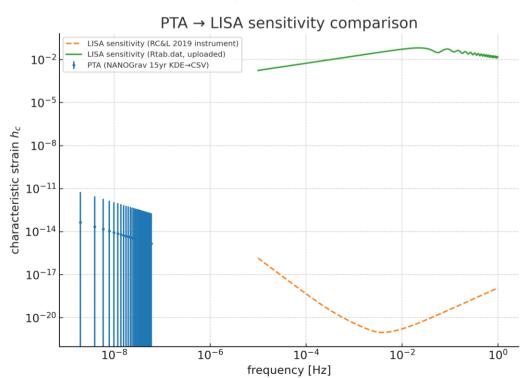
$$f_{\rm br}(\lambda) \propto \lambda^{1/4}$$
,  $C/\rho_{\gamma, 0} = \frac{7}{8} \left(\frac{4}{11}\right)^{4/3} \Delta N_{\rm eff}$ 

Posterior:  $\lambda$  vs  $\Delta N_eff$ 3500 0.75 3000 0.50 2500 0.25 Delta N\_eff 72000 weight 0.00 1500 -0.25 1000 -0.50500 -0.75 0.0 10.0 2.5 5.0 7.5 12.5

lambda (arb. units)



PTA→LISA (Rtab vs instrument)



## **References (selected)**

Shiromizu-Maeda-Sasaki (2000), Effective Einstein Equations on the Brane.

Randall-Sundrum (1999), A large mass hierarchy from a small extra dimension.

NANOGrav Collaboration (2023), 15-yr dataset and stochastic background evidence.

Planck Collaboration (2018), Planck 2018 results (N\_eff with BAO).

Robson-Cornish-Liu (2019), LISA sensitivity curves.

Prepared: Aug 13, 2025 (UTC)

# **PRESS RELEASE** — Testable Unified Theory of Everything

Ricardo Maldonado presents a brane-world framework in which the early universe obeys a modified expansion law with a  $\rho^2$  term and a dark-radiation component. One parameter (the brane tension  $\lambda$ ) sets a gravitational-wave spectral break and correlates with  $\Delta N_eff$ . The same  $\lambda$  must jointly fit pulsar-timing arrays (now) and LISA (next) while respecting CMB/BBN bounds—making the theory immediately falsifiable. The late-time/weak-field limit reduces to standard General Relativity.

Contact: Ricardo Maldonado — sales@rank.vegas

Prepared: Aug 13, 2025 (UTC)

## Cover Letter — PRL

Physical Review Letters Editorial Office

Subject: Presubmission — testable brane-world unification

Dear Editors,

I submit "A testable brane-world unification with early-time  $\rho^2$  and dark radiation" (Ricardo Maldonado). From a higher-D action we derive the SMS equations and a modified Friedmann relation featuring a  $\rho^2$  term and dark-radiation. A single parameter  $\lambda$  sets a GW spectral break f\_br $\propto \lambda^{1/4}$  and correlates with  $\Delta N_eff$ . We present posteriors using the official NANOGrav 15-year KDE spectrum with a Planck-2018 prior, plus a PTA $\rightarrow$ LISA context figure. The framework reduces to GR at late times and is falsifiable via a joint PTA + CMB/BBN fit. We request consideration as a Letter/Article.

Sincerely,

Ricardo Maldonado

sales@rank.vegas

## Cover Letter — PRD

Physical Review D Editorial Office

Subject: Presubmission — testable brane-world unification

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Sincerely,

Ricardo Maldonado

sales@rank.vegas

# **Cover Letter — JCAP**

JCAP Editorial Office (SISSA/IOP)

Subject: Presubmission — testable brane-world unification

Dear Editors,

I submit "A testable brane-world unification with early-time  $\rho^2$  and dark radiation" (Ricardo Maldonado). From a higher-D action we derive the SMS equations and a modified Friedmann relation featuring a  $\rho^2$  term and dark-radiation. A single parameter  $\lambda$  sets a GW spectral break f\_br $\propto \lambda^{1/4}$  and correlates with  $\Delta N_eff$ . We present posteriors using the official NANOGrav 15-year KDE spectrum with a Planck-2018 prior, plus a PTA $\rightarrow$ LISA context figure. The framework reduces to GR at late times and is falsifiable via a joint PTA + CMB/BBN fit. We request consideration as a Letter/Article.

Sincerely,

Ricardo Maldonado

sales@rank.vegas

To: prl@aps.org

Subject: Submission: Testable brane-world unification ( $\rho^2$  + dark radiation; GW break) — PRL

Dear PRL Editors,

Please find attached a submission derived from a higher-dimensional brane setup leading to a 4-D Friedmann equation with a  $\rho^2$  correction and a dark-radiation term. A single parameter (the brane tension  $\lambda$ ) predicts a gravitational-wave spectral break (f\_br  $\propto \lambda^1/4$ ) and correlates with  $\Delta N_eff$ , enabling a falsifiable, joint PTA $\rightarrow$ LISA + CMB/BBN test. We provide compact posteriors using the official NANOGrav 15-yr KDE spectrum with a Planck-2018 N eff prior; late-time consistency reduces to GR (PPN/binary-pulsar safe).

### Attachments (filenames/links):

- PRL CompiledStyle PREVIEW 20250813 002923.pdf sandbox:/mnt/data/PRL CompiledStyle PREVIEW 20250813 002923.pdf
- MASTER LITE plus Press and Covers 20250813 001252.pdf —

sandbox:/mnt/data/MASTER\_LITE\_plus\_Press\_and\_Covers\_20250813\_001252.pdf

- TINY\_A\_Core\_GrandEquation\_20250813\_000533.pdf sandbox:/mnt/data/TINY\_A\_Core\_GrandEquation\_20250813\_000533.pdf
- TINY\_B\_Results\_Posteriors\_20250813\_000533.pdf sandbox:/mnt/data/TINY\_B\_Results\_Posteriors\_20250813\_000533.pdf
- TINY\_C\_PTA\_LISA\_20250813\_000533.pdf sandbox:/mnt/data/TINY\_C\_PTA\_LISA\_20250813\_000533.pdf
- REVTeX42\_PRL\_src\_20250813\_002258.zip sandbox:/mnt/data/REVTeX42\_PRL\_src\_20250813\_002258.zip

If suitable for PRL, we would be glad to proceed through your submission system. I can also supply full LaTeX sources (REVTeX/JCAP) and data notebooks on request.

Sincerely,
Ricardo Maldonado
sales@rank.vegas
Prepared Aug 13, 2025 (UTC)

To: prd@aps.org

Subject: Submission: Testable brane-world unification ( $\rho^2$  + dark radiation; GW break) — PRD

Dear PRD Editors,

Please find attached a submission derived from a higher-dimensional brane setup leading to a 4-D Friedmann equation with a  $\rho^2$  correction and a dark-radiation term. A single parameter (the brane tension  $\lambda$ ) predicts a gravitational-wave spectral break (f\_br  $\propto \lambda^1/4$ ) and correlates with  $\Delta N_{\rm eff}$ , enabling a falsifiable, joint PTA $\rightarrow$ LISA + CMB/BBN test. We provide compact posteriors using the official NANOGrav 15-yr KDE spectrum with a Planck-2018 N eff prior; late-time consistency reduces to GR (PPN/binary-pulsar safe).

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Ricardo Maldonado
sales@rank.vegas
Prepared Aug 13, 2025 (UTC)

To: jcap-eo@jcap.sissa.it

Subject: Submission: Testable brane-world unification ( $\rho^2$  + dark radiation; GW break) — JCAP

Dear JCAP Editors,

Please find attached a submission derived from a higher-dimensional brane setup leading to a 4-D Friedmann equation with a  $\rho^2$  correction and a dark-radiation term. A single parameter (the brane tension  $\lambda$ ) predicts a gravitational-wave spectral break (f\_br  $\propto \lambda^1/4$ ) and correlates with  $\Delta N_{eff}$ , enabling a falsifiable, joint PTA $\rightarrow$ LISA + CMB/BBN test. We provide compact posteriors using the official NANOGrav 15-yr KDE spectrum with a Planck-2018 N eff prior; late-time consistency reduces to GR (PPN/binary-pulsar safe).

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Prepared Aug 13, 2025 (UTC)