

JCAP Letter — Title & Abstract

Title: A testable brane-world unification: ρ^2 cosmology, dark radiation, and a GW spectral break

Abstract: We present a minimal higher-dimensional (brane-world) framework that yields a modified 4D Friedmann equation $H^2 = (8\pi G/3) \rho (1 + \rho/2\lambda) + \lambda/4 + C/a^4$ (flat FRW). A single physical scale—the brane tension λ —controls two independent observables: a broken-power-law stochastic gravitational-wave background with break frequency $f_{\text{br}} \propto \lambda^{1/4}$, and an early-universe radiation excess parameterized by ΔN_{eff} via C . Using the public NANOGrav 15-year KDE free-spectrum (HD, 30 frequencies) and a loose Planck-2018 prior on ΔN_{eff} , we demonstrate a data-anchored fit and provide a small reproducibility pack (CSV + script). The claim is falsifiable: one value of λ must simultaneously place the GW break and satisfy CMB/BBN bounds. We outline an explicit RS-type toy embedding of the Standard Model on the brane and show the GR/PPN limit for $\rho \ll \lambda$.

JCAP Letter — Equations & Setup

SMS: $G_{\mu\nu} + \Lambda g_{\mu\nu} = (8\pi G) T_{\mu\nu} + (\kappa_5^4) \Pi_{\mu\nu} - E_{\mu\nu}.$

FRW (flat): $H^2 = (8\pi G/3) \rho (1 + \rho/2\Lambda) + \Lambda/3 + C/a^4.$

Early-time scale factor: $a(t) \sim t^{(1/4)} (\rho^2 \text{ era}).$

JCAP Letter — Predictions & Falsifiability

GW break: $f_{\text{br}} \propto \lambda^{1/4}$; dark radiation: C maps to ΔN_{eff} .

One λ must fit both PTA→LISA context and CMB/BBN bounds.

JCAP Letter — Data-Anchored Two-Pager Summary

NANOGrav 15yr KDE (HD, 30f) + Planck-2018 Delta N_{eff} prior.

Broken-power-law fit; best-fit table in SM; LISA appendix for sensitivity context.

JCAP Letter — Discussion & Outlook

RS toy embedding (anomaly checklist, Yukawas via localization, radion stabilization).

PPN/GR consistency for $\rho \ll \lambda$; next steps: full likelihood and compactification.