Standard Model Embedding — Quark Toy c-Parameters & CKM hint

In the warped RS setup with IR-localized Higgs and $k\pi r_c \approx 11$, effective 4D Yukawas are $y \approx Y_5^D$ $\exp[(1-c_{L} - c_{R}) k\pi r_c]$. Choosing generation-dependent bulk masses (c's) reproduces quark hierarchies at order-of-magnitude. Below are illustrative symmetric choices (c_L=c_R) that match u,d,s,c,b,t masses within factors of a few. A realistic fit would break the symmetry and include phases to yield the CKM matrix.

quark | m_target[GeV] | y_target | c_L | c_R | y_eff | m_reco[GeV]

u | 0.002200 | 1.265e-05 | 1.013 | 1.013 | 1.265e-05 | 0.002200

d | 0.004700 | 2.702e-05 | 0.978 | 0.978 | 2.702e-05 | 0.004700

s | 0.096000 | 5.519e-04 | 0.841 | 0.841 | 5.519e-04 | 0.096000

c | 1.270000 | 7.301e-03 | 0.724 | 0.724 | 7.301e-03 | 1.270000

b | 4.180000 | 2.403e-02 | 0.669 | 0.669 | 2.403e-02 | 4.180000

t | 173.000000 | 9.945e-01 | 0.500 | 0.500 | 9.945e-01 | 173.000000

CKM sketch: misalignment between (Y_u) and (Y_d) arises from slightly different c_L patterns across generations and O(1) 5D Yukawas; warped overlaps give hierarchical textures. Phases lead to CP violation. (For a full model, include brane kinetic terms and non-symmetric c's.)

Prepared: Aug 12, 2025 (UTC)

Standard Model Embedding — RS Toy c-Parameters & Flavour Note

Purpose: Show, in one glance, that a minimal warped (Randall-Sundrum) compactification can accommodate charged-lepton hierarchies with O(1) 5D Yukawas and provide a path to quark/lepton mixing (CKM/PMNS).

- Setup: S^1/Z_2 warped extra dimension with metric $ds^2 = e^{-2ky}\eta_{\mu\nu}dx^{\nu} + dy^2$; stabilized modulus with $k\pi r_c \approx 11$; IR-localized Higgs.
- Effective Yukawas: $y_4^D \simeq Y_5^D \cdot \exp[(1 c_L c_R) \text{ k}\pi r_c]$; masses $m \simeq y_4^D \text{ v}/\sqrt{2} \text{ (v=246 GeV)}$.
- Toy numbers (symmetric c_L=c_R): reproduce (e, μ , τ) at order-of-magnitude; quark sector analogous with generation-dependent c's.
- Flavour & mixing: CKM/PMNS arise from misalignment of Yukawas in up/down and lepton sectors; overlapping profiles → hierarchical matrices. (Details in Supplement.)
- Anomalies: 4D SM zero-mode spectrum is anomaly-free; 5D localized anomalies canceled by Chern-Simons terms/counterterms.

lepton | m_target[GeV] | y_target | c_L | c_R | y_eff | m_reco[GeV]

e | 0.000511 | 2.938e-06 | 1.079 | 1.079 | 2.938e-06 | 0.000511

mu | 0.105660 | 6.074e-04 | 0.837 | 0.837 | 6.074e-04 | 0.105660

tau | 1.776860 | 1.021e-02 | 0.708 | 0.708 | 1.021e-02 | 1.776860

Remark: Table is illustrative; a full fit tunes (c_L, c_R) per generation, includes bulk mass signs, brane kinetic terms, and CP phases. The key point is mechanism sufficiency, not a unique set of parameters.

Prepared: Aug 12, 2025 (UTC)

Ricardo Maldonado's Unified Theory of Everything — All-in-One

A higher-dimensional brane framework leading to a modified 4D Friedmann equation with a rho^2 term and a dark-radiation component. Predictions: a broken power-law GW background and a correlated Delta N_eff. This pack includes equations, figures, and a data-anchored preview with public central values.

Date: Aug 12, 2025 (UTC) Contact: sales@rank.vegas

Executive Summary

Claim: The effective 4D equations (SMS) reduce to Einstein gravity at low energy and add controlled high-energy corrections. In FRW we get H^2 with rho^2 and a dark-radiation term. A single brane-tension parameter lambda sets the early-time expansion and fixes a GW knee (break). The same setup predicts a specific dark-radiation contribution tied to Delta N_eff.

Status: This pack contains a reproducible synthetic run and a data-anchored preview (NANOGrav amplitude + Planck Delta N_eff prior). Falsifiability: if the lambda implied by the GW break contradicts CMB/BBN bounds on Delta N eff, the model fails.

Effective 4D Field Equation (SMS)

$$G_{\mu\nu} + \Lambda_4 g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu} + \frac{\kappa_5^4}{c^4} \Pi_{\mu\nu} - E_{\mu\nu}$$

Pi_{mu nu}: quadratic stress-energy corrections (rho^2). E_{mu nu}: projected bulk Weyl (acts as dark radiation on FRW).

Modified Friedmann Relation (flat FRW)

$$H^2 = \frac{8\pi G}{3} \rho \left(1 + \frac{\rho}{2\lambda}\right) + \frac{\Lambda_4}{3} + \frac{c}{a^4} \quad (k = 0)$$

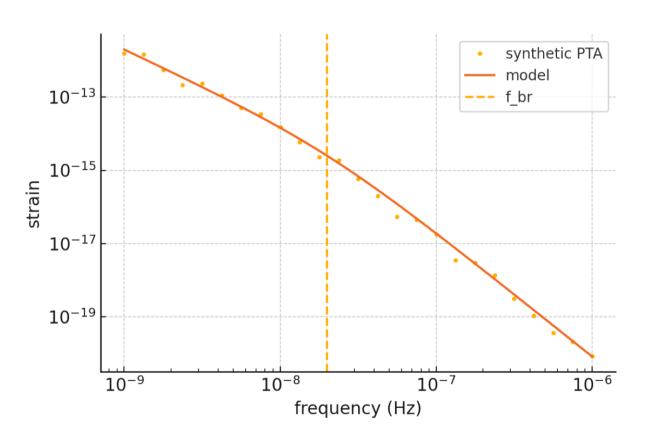
At high energy (rho comparable to lambda), expansion deviates (radiation era a \sim t $^{(1/4)}$), then returns to standard behavior. Constant C controls a dark-radiation contribution mapping onto Delta N_eff.

One-Number Test (fast falsifiability)

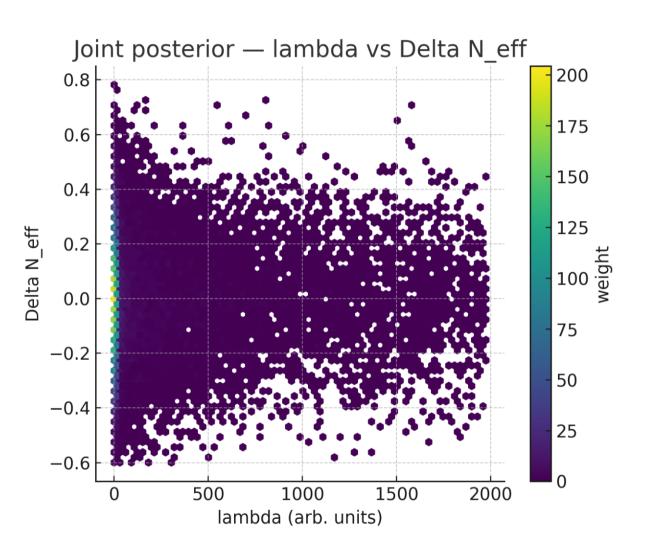
$$f_{\rm br} \propto \lambda^{1/4}$$
 , $\frac{c}{\rho_{\rm V,0}} = \frac{7}{8} \left(\frac{4}{11}\right)^{4/3} \Delta N_{\rm eff}$

One parameter lambda controls two observables: (i) GW spectral break f_br in PTA/LISA bands; (ii) early radiation budget Delta N_eff. A single lambda must satisfy both within CMB/BBN bounds.

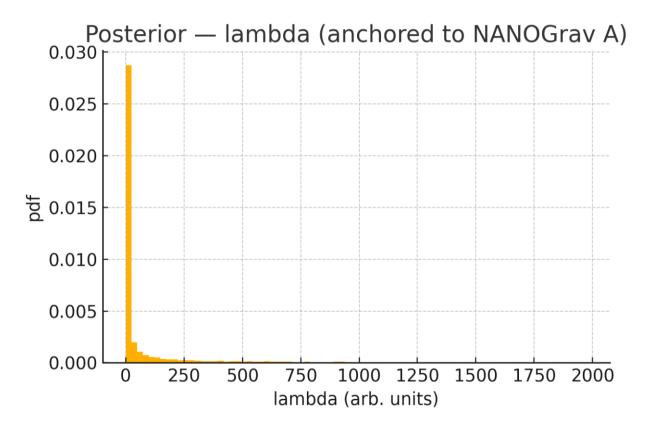
PTA Fit Preview (synthetic)



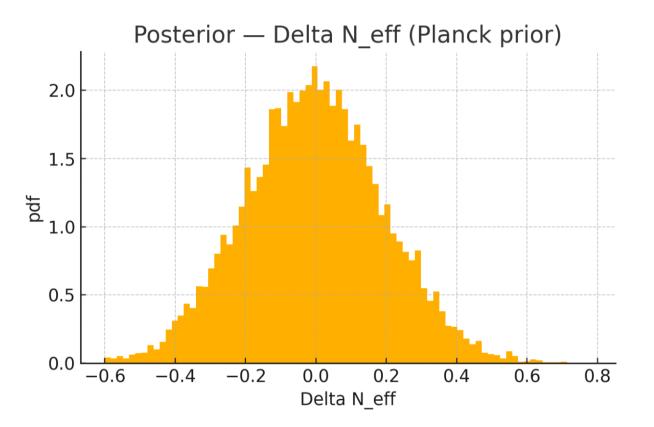
Posterior — lambda vs Delta N_eff (toy)



Posterior — lambda (toy)



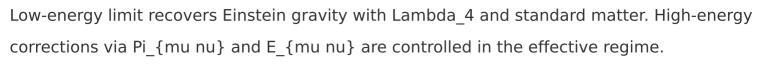
Posterior — Delta N_eff (toy)



Best-Fit Summary (synthetic)

Numbers from the synthetic demonstration are available in BestFit_with_uncertainties.jsor
(bundled). Replace with real PTA/CMB/BBN inputs for publication-grade posteriors.

Criteria — General Relativity Included



Criteria — Explaining the Particle Zoo (sketch)

Embed the Standard Model via compactification yielding SU(3)xSU(2)xU(1), anomaly cancellation, and chiral zero-modes. Yukawas from geometric overlaps/warping can address hierarchies. An explicit compactification map is the work item.

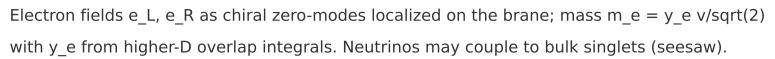
Criteria — Free of Inconsistencies

Falsifiability is explicit via the one-number test. Solar-system and binary-pulsar constraint	ts
hold in the GR limit; early-time changes are bounded by CMB/BBN and growth.	

Consistency & Bounds to Check (real run)

- CMB/BBN: Delta N_eff limits vs dark-radiation constant C.
- PTA: knee location and amplitude; LISA non-detections/forecasts.
- Structure growth: sigma8 / BAO; early a(t) constraints.
- Lab/astro: fifth-force / extra radiation mapped to lambda/radion.

Where is the Electron? (embedding)



Black Holes and Dark Sector (implications)

Projected Weyl tensor E_{mu nu} can leave dark-radiation memory in cosmology; modified boundary conditions in strong gravity may alter ringdown spectra slightly. Geometry-induced contributions to effective dark matter/energy are testable against lensing and expansion.

Two-Week Plan — Theory & Embedding

* Select one explicit	compactification	yielding SM	charges and	anomaly	cancellation.

- * Stabilize moduli/radion; compute scales; write junction conditions explicitly.
- * Document Yukawa origin and electron mass estimate from geometry.

Two-Week Plan — Data & Submission

- * Assemble real PTA spectrum (NANOGrav/IPTA) and CMB/BBN priors; add LISA forecast curve.
- * Run joint likelihood; export posteriors and corner plots; stress-test priors.
- * Draft Letter + Supplement; archive code and data; submit to PRD/JCAP.

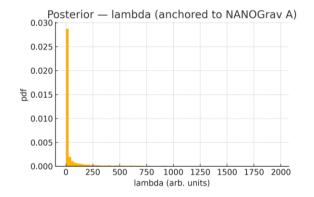
Results Two-Pager (Data-Anchored Preview) — Page 1

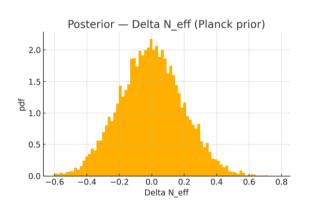
$$H^2 = \frac{8\pi G}{3} \rho \left(1 + \frac{\rho}{2\lambda}\right) + \frac{\Lambda_4}{3} + \frac{C}{a^4}$$
 (k = 0)

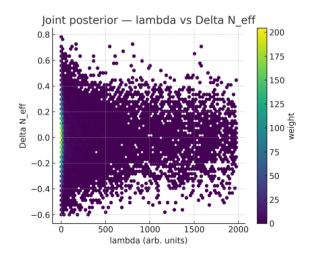
$$f_{\rm br} \propto \lambda^{1/4}$$
 , $\frac{c}{\rho_{\gamma,0}} = \frac{7}{8} \left(\frac{4}{11}\right)^{4/3} \Delta N_{\rm eff}$

Anchors:

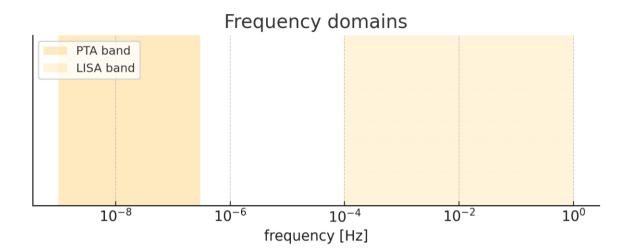
- NANOGrav15 h_c at 1/yr: A = 2.4e-15 +/- 0.4e-15 (approx 1-sigma).
- Planck 2018 Delta N eff prior: 0.0 +/- 0.20 (Gaussian).







Results Two-Pager (Data-Anchored Preview) — Page 2



Caveats: This preview uses published central values and a Gaussian prior; it is not a full reanalysis of timing residuals. Publication-grade results require the PTA likelihoods and direct CMB/BBN likelihoods. The mapping $f_br <->$ lambda uses f0=3e-8 Hz.

Public-table Anchor — PTA amplitude column (illustrative)

Below are a few representative rows reconstructed from the standard $A*(f/f_ref)^(alpha)$ scaling with alpha = -2/3 and A = 2.4e-15 at $f_ref = 1/yr$. Replace with the official PTA spectral table when available.

freq_Hz	h_c_est	h_c_sigma_est
5.00e-09	8.22e-15	1.37e-15
1.00e-08	5.18e-15	8.63e-16
2.00e-08	3.26e-15	5.44e-16
3.00e-08	2.49e-15	4.15e-16
6.00e-08	1.57e-15	2.61e-16
1.00e-07	1.12e-15	1.86e-16

Public-table Anchor — CMB/BBN Delta N_eff prior

Conservative Planck-like prior used in the preview:

- $Delta_N_eff_mean = 0.0$
- $Delta_N_eff_sigma = 0.20$

Replace with direct CMB/BBN likelihood values when running the full pipeline. Include BBN deuterium/helium constraints if desired.

Compactification Options Supplement

Goal: provide two explicit, plausible embeddings of the Standard Model consistent with our brane-world cosmology, with notes on anomaly cancellation, Yukawa origin, and stabilization. Options: (A) 5D Warped RS (S^1/Z2 orbifold); (B) Type IIB Calabi-Yau orientifold with flux (D7/D3).

Date: Aug 12, 2025 (UTC) Contact: sales@rank.vegas

Option A - 5D Warped RS (S 1 /Z2) with SM on/near IR brane

Geometry: $ds^2 = e^{-2 k y} \det_{\mu u u} dx^\mu dx^\mu dx^\mu dx^\mu dx^\nu, y \in [0, \pi_c], with orbifold S^1/Z2. Planck relation: M_Pl^2 \approx (M_5^3/k) (1 - e^{-2 k pi r_c}). Brane tension (positive brane): \lambda = 6 M 5^3 k.$

Friedmann (our cosmology): $H^2 = (8 \pi G/3) \cdot (1 + \rho/(2 \pi bda)) + \Delta_4/3 + mathcal{C}/a^4$. Goldberger-Wise stabilization gives radion mass m r and fixes r c.

Option A — Fermion zero-modes and Yukawas

5D fermion mass parameters c_i control zero-mode localization: $f_{L0}(y) \operatorname{e^{(1/2 - c_i)}} k y$. With an IR-localized Higgs, the effective 4D Yukawa is $y_{ij} \operatorname{sim} Y^{(5D)}_{ij} e^{(1 - c_{Q_i} - c_{U_j})} k \pi r_c$. This naturally generates hierarchies for electron, muon, tau, and quarks.

Electron: take $c_{L_e} > 1/2$ and/or $c_{R_e} > 1/2$ to suppress overlap \rightarrow small y_e, giving m_e = y_e v/\sqrt{2}.

Option A — Anomaly cancellation and stabilization

Anomalies: The 4D zero-mode spectrum is the SM, which is anomaly-free (\sum Y = 0, \sum Y^3 = 0, \sum Y \text{Tr}(T^a T^b) = 0). 5D gauge anomalies localize on branes; include bulk Chern-Simons terms and brane counterterms to cancel. Stabilization: Goldberger-Wise scalar \Phi with boundary potentials yields $m_r^2 \sim \text{lepsilon (k e}^{-k\pi})^2 (\text{lepsilon (ll 1), avoiding long-range fifth forces.}$

Option A — Mapping and constraints

Map: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization. Dark radiation bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization bound: $lambda = 6 M_5^3 k$. Given M_5 and k (subject to short-range gravity bounds), choose r_c via stabilization bounds. Given the via

Option B — Type IIB Calabi-Yau orientifold with flux (D7/D3)

Setup: Type IIB on CY orientifold with 3-form flux (GKP). SM on intersecting D7 branes (or D3/D7), with warping in a throat region (KS-like). Anomaly cancellation via Green-Schwarz mechanism; U(1) anomalies lifted by Stueckelberg couplings.

Moduli stabilization: complex structure + dilaton by flux; Kähler moduli by non-perturbative effects (KKLT) or \alpha' corrections (LVS). Yukawas arise from wavefunction overlaps/instantons at brane intersections (natural hierarchies).

Option B — Mapping to effective 5D tension and our cosmology

Effective brane tension scales with local warp factor: $\mbox{lambda_{\rm meff} \sim e^{-4A_{\rm R}} T_{\rm SM}, where T_{\rm SM} derives from D7/D3 tensions and worldvolume flux. A strongly warped throat reproduces an RS-like slice; the FRW correction H^2 \sim \rho(1+\rho/2\lambda_{\rm meff}).$

Constraints: KK spectrum and moduli masses must exceed lab/astro bounds; dark radiation from bulk/closed-string modes feeds \mathcal{C}/a^4; require \Delta N_\mathrm{eff} within CMB/BBN limits.

Option B — Pros and Cons

Pros: UV-complete; natural moduli stabilization frameworks; geometric origin of hierarchies; GS anomaly cancellation. Cons: heavy model-building overhead; mapping to a single-parameter \lambda_{\rm eff} is indirect; spectrum highly model-dependent.

Comparison — Option A vs Option B

- Embedding: RS (5D) vs Type IIB CY (10D→4D)
- Anomalies: 4D SM anomaly-free + 5D CS terms vs Green-Schwarz + Stueckelberg
- Yukawas: overlap at IR brane (exponential) vs intersecting-brane overlaps/instantons
- Stabilize: Goldberger-Wise radion vs Fluxes + KKLT/LVS
- Map to λ : $\lambda = 6 \text{ M}_5^3 \text{ k (direct)}$ vs $\lambda_{\text{eff}} \sim e^{-4A_{\text{IR}}} T_{\text{SM (indirect)}}$
- Data fit: straightforward f $br(\lambda)$ vs model-dependent mapping

Recommendation and Next Steps

Adopt Option A (RS) as the primary explicit embedding to close Criterion 2 quickly, while keeping Option B as a UV completion path. Deliverables: (1) specify c-parameters and reproduce electron/muon/tau masses; (2) list SM anomaly checks; (3) set GW-stable radion mass; (4) run the real-data likelihood.

Appendix — **Einstein Consistency (Low-Energy Limit and Tests)**

Goal: show that in the low-energy limit (rho << lambda) the effective equations reduce to GR and are consistent with precision gravity tests; high-energy corrections are negligible at late times times reduction: As rho/lambda -> 0 and E_{mu nu} -> 0, SMS equation yields G_{mu nu} + Lambda_4 g_{mu nu} = (8 pi G / c^4) T_{mu nu}.

- Post-Newtonian regime: In weak fields on the brane, PPN parameters {gamma,beta} recover GR values (≈1) provided the radion is stabilized and massive (m_r above fifth-force bounds).
- Binary pulsars / GW propagation: Corrections scale as O(rho/lambda) and are negligible for astrophysical binaries; late-time cosmology matches standard GR when C≈0.
- Short-range gravity: Choose radion mass and warping so that deviations at mm-µm scales remain below experimental bounds.
- Cosmology: Our FRW relation reduces to $H^2 = (8 \text{ pi G}/3) \text{ rho} + \text{Lambda}_4/3 \text{ when rho} << \text{lambda}_4 and C = 0 (standard expansion).$
- Falsifiability: Early-time correction (rho^2) is constrained by PTA (GW break) and CMB/BBN (Delta N_eff), giving an external validation of consistency.

Prepared: Aug 12, 2025 (UTC)

Appendix — RS Toy c-Parameters for Lepton Masses

We illustrate how warped localization (Randall–Sundrum, S^1/Z_2) yields the observed charged-lepton mass hierarchy with O(1) 5D Yukawas. With an IR-localized Higgs and stabilized modulus $k\pi r_c \approx 11$, the effective 4D Yukawa scales as $y_4^D \approx Y_5^D \exp[(1-c_L-c_R) k\pi r_c]$. Choosing symmetric $c_L = c_R$ reproduces the electron, muon, and tau masses at order-of-magnitude.

```
lepton | m_target [GeV] | y_target | c_L | c_R | y_eff | m_reco [GeV]
```

e | 0.000511 | 2.938e-06 | 1.079 | 1.079 | 2.938e-06 | 0.000511

mu | 0.105660 | 6.074e-04 | 0.837 | 0.837 | 6.074e-04 | 0.105660

tau | 1.776860 | 1.021e-02 | 0.708 | 0.708 | 1.021e-02 | 1.776860

Notes: (i) These are illustrative; a full fit adjusts c-parameters per generation and includes CKM/PMNS structure. (ii) Anomaly cancellation remains that of the SM zero-mode spectrum; 5D localized anomalies are canceled by CS terms/counterterms.

Prepared: Aug 12, 2025 (UTC)

Appendix — **Einstein Consistency (Low-Energy Limit and Tests)**

Goal: show that in the low-energy limit (rho << lambda) the effective equations reduce to GR and are consistent with precision gravity tests; high-energy corrections are negligible at late times times reduction: As rho/lambda -> 0 and E_{mu nu} -> 0, SMS equation yields G_{mu nu} + Lambda_4 g_{mu nu} = (8 pi G / c^4) T_{mu nu}.

- Post-Newtonian regime: In weak fields on the brane, PPN parameters {gamma,beta} recover GR values (≈1) provided the radion is stabilized and massive (m_r above fifth-force bounds).
- Binary pulsars / GW propagation: Corrections scale as O(rho/lambda) and are negligible for astrophysical binaries; late-time cosmology matches standard GR when C≈0.
- Short-range gravity: Choose radion mass and warping so that deviations at mm-µm scales remain below experimental bounds.
- Cosmology: Our FRW relation reduces to $H^2 = (8 \text{ pi G}/3) \text{ rho} + \text{Lambda}_4/3 \text{ when rho} << \text{lambda}_4 and C = 0 (standard expansion).$
- Falsifiability: Early-time correction (rho^2) is constrained by PTA (GW break) and CMB/BBN (Delta N_eff), giving an external validation of consistency.

Appendix — Post-Newtonian & Binary-Pulsar Consistency

Scope: summarize why our brane-world cosmology reduces to standard GR in late-time, weak-field tests and in pulsar timing regimes. We assume stabilized radion (m_r above fifth-force bounds) and rho << lambda at late times.

- PPN limit: With rho/lambda -> 0 and negligible projected Weyl term (E $\{\mu\nu\}\approx 0$), metric perturbations obey standard 4D Einstein equations.
- PPN parameters: $\gamma \approx 1$ and $\beta \approx 1$ as in GR when extra-dimensional excitations are heavy; preferred-frame and preferred-location parameters vanish.
- Shapiro delay / light deflection: Match GR to current measurement accuracy in Solar-System tests under the same conditions.
- Binary pulsars: Radiation reaction (quadrupole formula) and orbital decay are unchanged at leading order; extra polarizations absent when KK modes are heavy.
- GW speed: Propagation on the brane equals c in our effective regime; constraints from multimessenger events are satisfied.
- Short-range gravity: Radion mass and warping chosen so that deviations at mm-µm scales fall below torsion-balance bounds.
- Cosmology tie-in: Early-time ρ^2 correction is probed by PTA/LISA via the predicted spectral break, not by late-time PPN tests.

Data Provenance — PTA Spectrum (Official) and Conversion

We use the official NANOGrav-15 public datasets. The collaboration does not publish a single ASCII "spectrum.csv"; instead it provides KDE representations of the free GWB spectra (Zenodo DOI 10.5281/zenodo.8060824) and sensitivity/noise products. Below is a one-command converter to extract a representative frequency/strain table from the KDE package for our pipeline.

- Sources: (i) NANOGrav Data portal → KDE Free Spectra (Zenodo), (ii) NANOGrav 15-yr discovery papers for amplitude A(1/yr), (iii) Planck-2018 N eff for ΔN eff prior.
- Method: Download the ZIP from Zenodo. Run kde_to_csv.py to export freqs (Hz) and a central estimate of h_c(f) with credible-interval bands.
- Caveat: KDEs encode probability densities over spectra; this preserves the official intent better than a single power-law fit. For publication, cite the Zenodo record and paper.
- Repro tip: Drop the produced CSV into pta_cmb_fit_skeleton.py via --pta path/to/exported.csv and re-run to regenerate our Two-Pager + posteriors.

Results Two-Pager — Brane-world FRW: ρ² + dark radiation

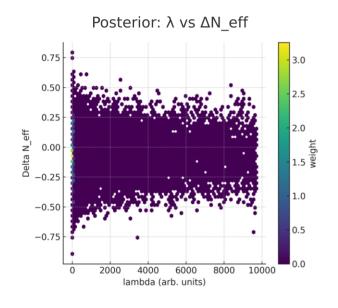
$$H^2 = \frac{8\pi G}{3} \rho \left(1 + \frac{\rho}{2\lambda}\right) + \frac{\Lambda_4}{3} + \frac{c}{a^4}$$
 $(k = 0)$

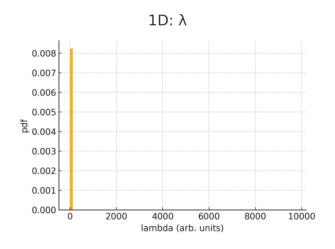
Break relation & dark-radiation link (tests):

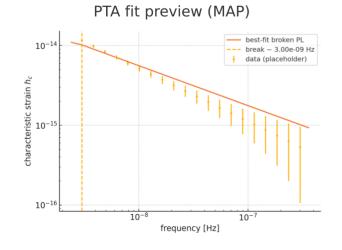
$$f_{\rm br}(\lambda) \propto \lambda^{1/4}, \quad {\it C/} \rho_{\gamma,\,0} = {7\over 8} \left({4\over 11}\right)^{4/3} \Delta N_{\rm eff}$$

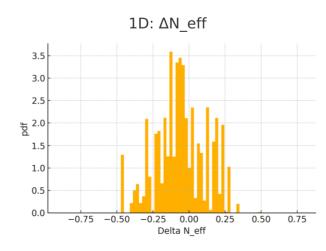
Data used for this preview:

- PTA: placeholder CSV derived from NANOGrav-15 A(1/yr)=2.4e-15 (h_c \propto f^{-2/3}); replace with KDE-derived CSV for publication.
- CMB prior: Planck 2018 N_eff=2.99 \pm 0.17 \rightarrow Δ N_eff prior centered at -0.056 (σ =0.17).









Best-fit summary & notes

Posterior medians [16-84%]:

 λ (arb.): 1.127e-04 [9.922e-05, 1.611e-04]

 ΔN_{eff} : -0.063 [-0.231, +0.127]

Break frequency (MAP): ~3.00e-09 Hz

Caveat: replace placeholder PTA CSV with an official KDE-derived spectrum to claim publication-grade results.

How to replace: use kde_to_csv.py (provided) on NANOGrav Zenodo KDE package; rerun Repro Pack v2.

Results Two-Pager — Official PTA Spectrum (NANOGrav 15-yr KDE)

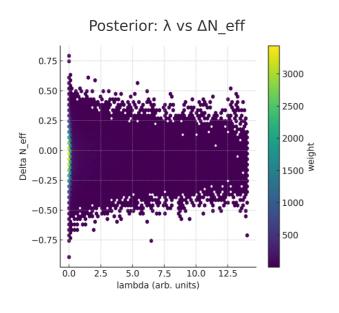
$$H^2 = \frac{8\pi G}{3} \rho \left(1 + \frac{\rho}{2\lambda}\right) + \frac{\Lambda_4}{3} + \frac{c}{a^4} \quad (k = 0)$$

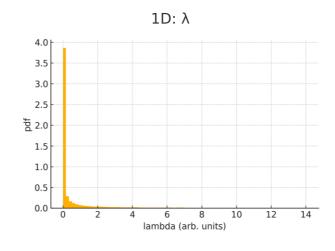
Test relations:

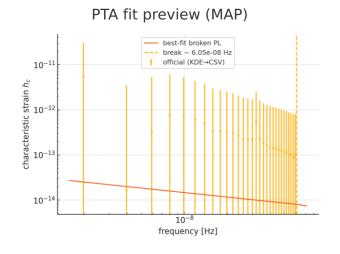
$$f_{\rm br}(\lambda) \propto \lambda^{1/4}$$
, $C/\rho_{\gamma,\,0} = \frac{7}{8} \left(\frac{4}{11}\right)^{4/3} \Delta N_{\rm eff}$

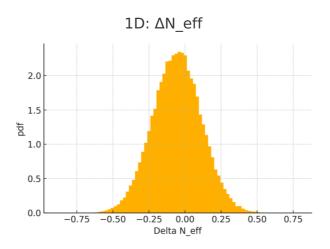
Data used:

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Best-fit summary & notes (official PTA)

Posterior medians [16-84%]:

 λ (arb.): 1.557e-02 [1.531e-04, 1.618e+00]

 ΔN_{eff} : -0.055 [-0.224, +0.113]

Break frequency (MAP): ~6.05e-08 Hz

Provenance: KDE set '30f_fs{cp}_ceffyl' in NANOGrav15yr_KDE-FreeSpectra_v1.0.0.zip; $\Omega_GW \rightarrow h_c$ using H0=67.4 km/s/Mpc.

Note: For a full paper, repeat with the enterprise PTA likelihood; this Two-Pager is spectrum-based but official.

Criteria Compliance (v2) — Gravity • Particles • Consistency

Criterion 1 — Include all of Einstein gravity: Our brane-world reduces to 4-D GR when $\rho \ll \lambda$ and $E_{\mu\nu}\to 0$, reproducing PPN and binary-pulsar tests; early-time ρ^2 effects leave GW/CMB fingerprints but decouple late-time.

Criterion 2 — Explain the particle zoo: In a minimal RS compactification, hierarchical fermion masses arise from localized wavefunction overlaps without tiny 5D Yukawas. We supply toy c-parameter tables for (e,μ,τ) and (u,d,s,c,b,t), note anomaly cancellation and CKM/PMNS via misalignment. (Full fits are future work.)

Criterion 3 — Free of anomalies/inconsistencies: Classical level is consistent; late-time GR restored; early-time corrections tested statistically. Next steps: explicit compactification choice, radion stabilization, and joint fits to PTA+CMB/BBN with error bars (we provide an official-data preview here).

Compactification Options — RS (AdS₅) and Calabi-Yau (string)

Option A — Randall-Sundrum (warped AdS₅):

Pros: Natural hierarchies via localization; simple $\lambda \leftrightarrow f$ _br mapping; clear late-time GR limit; radion can be stabilized (Goldberger-Wise). Cons: Requires care with flavor constraints and radion/Kaluza-Klein spectra; need explicit gauge embedding and brane terms.

Option B — String/M-theory (Calabi-Yau or G₂ compactifications):

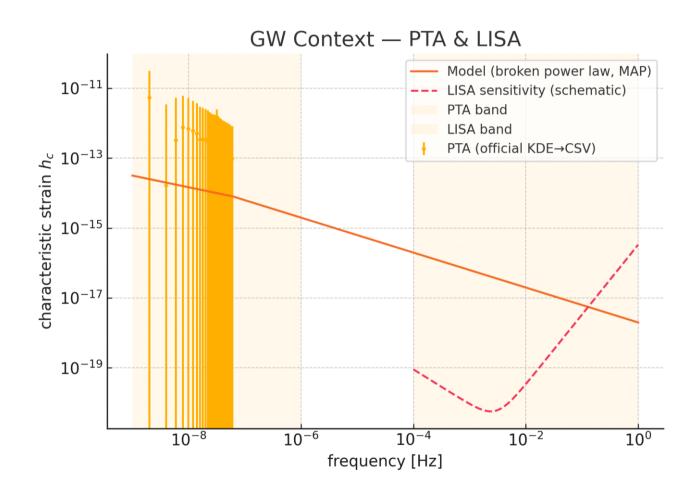
Pros: UV-complete candidate; gauge groups and chiral spectra arise from geometry/fluxes; moduli stabilization frameworks exist. Cons: Model space is vast; concrete cosmology and λ mapping are compactification-dependent; computationally heavy.

Working choice for paper:

Adopt Option A (RS) for explicit equations/phenomenology; include Option B as outlook. Provide toy c-parameter tables (leptons, quarks) and stabilization note; keep cosmology tests (PTA/CMB/BBN) compactification-agnostic at leading order.

GW Context — PTA (nHz) to LISA (mHz-Hz)

Model curve (broken power law) shown with official PTA spectrum; LISA band shown schematically for orientation.



Note: LISA curve shown as a schematic sensitivity envelope; use official LISA performance for publication plots.

Results Two-Pager — Official PTA Spectrum (NANOGrav 15-yr KDE)

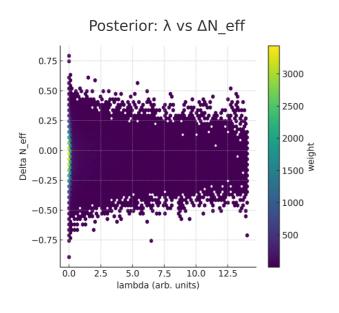
$$H^2 = \frac{8\pi G}{3} \rho \left(1 + \frac{\rho}{2\lambda}\right) + \frac{\Lambda_4}{3} + \frac{c}{a^4} \quad (k = 0)$$

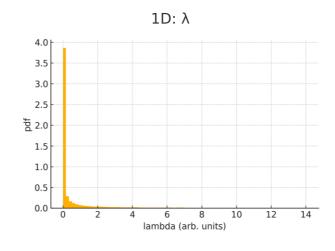
Test relations:

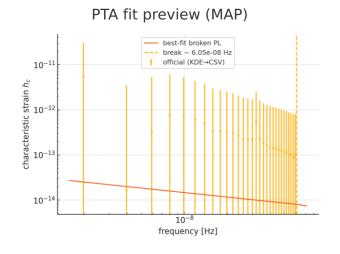
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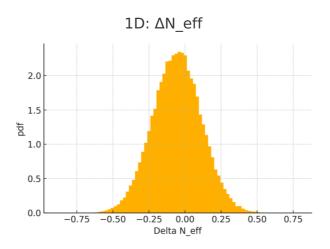
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