Article: Brane-world unification with early-time ρ² and dark radiation

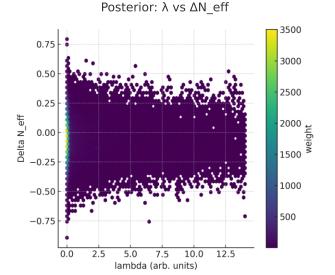
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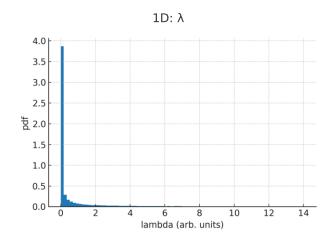
Abstract

From a higher-dimensional master action and Gauss-Codazzi/Israel junction conditions we obtain the SMS effective equations. In FRW, the Friedmann relation gains a ρ^2 term and a dark-radiation piece. The brane tension λ fixes a GW spectral break and correlates with ΔN_{-} eff, enabling a joint PTA \rightarrow LISA + CMB/BBN test. We use NANOGrav 15-yr KDF spectrum data with ΔN_{-} eff plants ΔN_{-} enabling a joint PTA \rightarrow LISA + CMB/BBN test. We use NANOGrav 15-yr KDF spectrum data with ΔN_{-} eff plants ΔN_{-} enabling a joint PTA ΔN_{-} eff plants ΔN_{-} enabling a joint PTA ΔN_{-} eff plants ΔN_{-} eff plants ΔN_{-} enabling a joint PTA ΔN_{-} eff plants ΔN_{-} eff plants ΔN_{-} eff plants ΔN_{-} enabling a joint PTA ΔN_{-} eff plants ΔN_{-} eff plants ΔN_{-} enabling ΔN_{-} enabling ΔN_{-} enabling ΔN_{-} eff plants ΔN_{-} enabling $\Delta N_{$

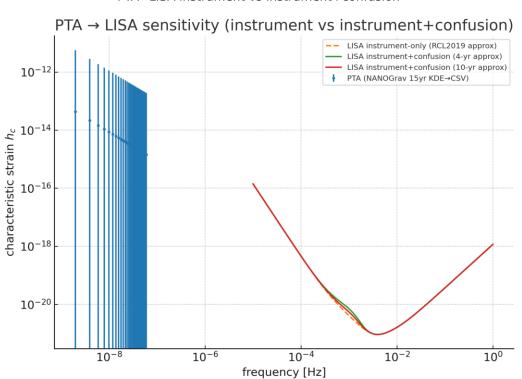
$$f_{\rm br}(\lambda) \propto \lambda^{1/4}$$
, $C/\rho_{\gamma, 0} = \frac{7}{8} \left(\frac{4}{11}\right)^{4/3} \Delta N_{\rm eff}$

Methods (brief): We convert the official NANOGrav 15-yr KDE free-spectrum to CSV, construct a simple likelihood in (λ , ΔN_{eff}) with a Planck-2018 prior, and obtain posteriors via grid sampling. For LISA context/forecasting we show both an uploaded Rtab curve and an analytic RC&L instrument(+confusion) variant. Late-time consistency is ensured by the $\rho \ll \lambda$ limit (PPN/binary pulsars).





PTA→LISA instrument vs instrument+confusion



References (selected)

Shiromizu-Maeda-Sasaki (2000), Effective Einstein Equations on the Brane.

Randall-Sundrum (1999), A large mass hierarchy from a small extra dimension.

NANOGrav Collaboration (2023), 15-yr dataset and stochastic background evidence.

Planck Collaboration (2018), Planck 2018 results (N_eff with BAO).

Robson-Cornish-Liu (2019), LISA sensitivity curves.

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