

Quark Sector (Toy) — CKM/PMNS Sketch (ASCII-safe)

Toy quark sector note (qualitative):

- Bulk masses (c_Q , c_u , c_d) localize zero-mode profiles; effective 4D Yukawas $\sim \text{overlap}(H, Q, u/d)$.
- With $O(1)$ 5D Yukawas and modest spread in c -parameters, realize $m_u \ll m_c \ll m_t$ and $m_d \ll m_s \ll m_b$.
- CKM: small mixings from slight misalignment of left-handed doublet localizations (c_{Q1} , c_{Q2} , c_{Q3}).
- PMNS (leptons): larger mixings via different localization and/or a brane seesaw.
- Full anomaly-complete compactification remains future work; this page states a plausible toy path.

Appendix: LISA variants

LISA CSVs not found; please re-generate or re-upload.

Data Provenance — PTA Spectrum (Official) and Conversion

We use the official NANOGrav-15 public datasets. The collaboration does not publish a single ASCII “spectrum.csv”; instead it provides KDE representations of the free GWB spectra (Zenodo DOI 10.5281/zenodo.8060824) and sensitivity/noise products. Below is a one-command converter to extract a representative frequency/strain table from the KDE package for our pipeline.

- Sources: (i) NANOGrav Data portal → KDE Free Spectra (Zenodo), (ii) NANOGrav 15-yr discovery papers for amplitude $A(1/\text{yr})$, (iii) Planck-2018 N_{eff} for ΔN_{eff} prior.
- Method: Download the ZIP from Zenodo. Run `kde_to_csv.py` to export freqs (Hz) and a central estimate of $h_c(f)$ with credible-interval bands.
- Caveat: KDEs encode probability densities over spectra; this preserves the official intent better than a single power-law fit. For publication, cite the Zenodo record and paper.
- Repro tip: Drop the produced CSV into `pta_cmb_fit_skeleton.py` via `--pta path/to/exported.csv` and re-run to regenerate our Two-Pager + posteriors.

arXiv Title / Abstract / Supplemental Material (ASCII-safe)

Title: A testable brane-world unification: ρ^2 cosmology, dark radiation, and a GW spectral break

Abstract: We present a minimal higher-dimensional (brane-world) framework that yields a modified 4D Friedmann equation $H^2 = (8\pi G/3) \rho (1 + \rho/2\lambda) + \lambda^{4/3} + C/a^4$ (flat FRW). A single physical scale—the brane tension λ —controls two independent observables: a broken-power-law stochastic gravitational-wave background with break frequency $f_{\text{br}} \propto \lambda^{1/4}$, and an early-universe radiation excess parameterized by ΔN_{eff} via C . Using the public NANOGrav 15-year KDE free-spectrum (HD, 30 frequencies) and a loose Planck-2018 prior on ΔN_{eff} , we demonstrate a data-anchored fit and provide a small reproducibility pack (CSV + script). The claim is falsifiable: one value of λ must simultaneously place the GW break and satisfy CMB/BBN bounds. We outline an explicit RS-type toy embedding of the Standard Model on the brane and show the GR/PPN limit for $\rho \ll \lambda$.

SM Description: Supplemental Material: (i) exported_pta_spectrum_HD_30f.csv (NANOGrav KDE-derived percentiles), (ii) reproduce_posteriors.py (fits broken power law; outputs best-fit JSON and plots), (iii) best_fit_REALDATA.json, and (iv) README_REPRO.txt with a 60-second rerun command.