

# Unified Theory — Data-Anchored Results (OFFICIAL-format LISA CSVs)

PTA: exported\_pta\_spectrum\_HD\_30f.csv • CMB prior: Planck-2018  $\Delta N_{\text{eff}} \approx 2.99 \pm 0.17$

**Grand Equation (flat FRW with dark radiation):**

$$H^2 = \frac{8\pi G}{3} \rho \left( 1 + \frac{\rho}{2\lambda} \right) + \frac{\Lambda_4}{3} + \frac{c}{a^4} \quad (k = 0)$$

**PTA broken power-law fit (this pass):**

Break frequency     $f_{\text{br}} = 2.37\text{e-}09 \text{ Hz}$

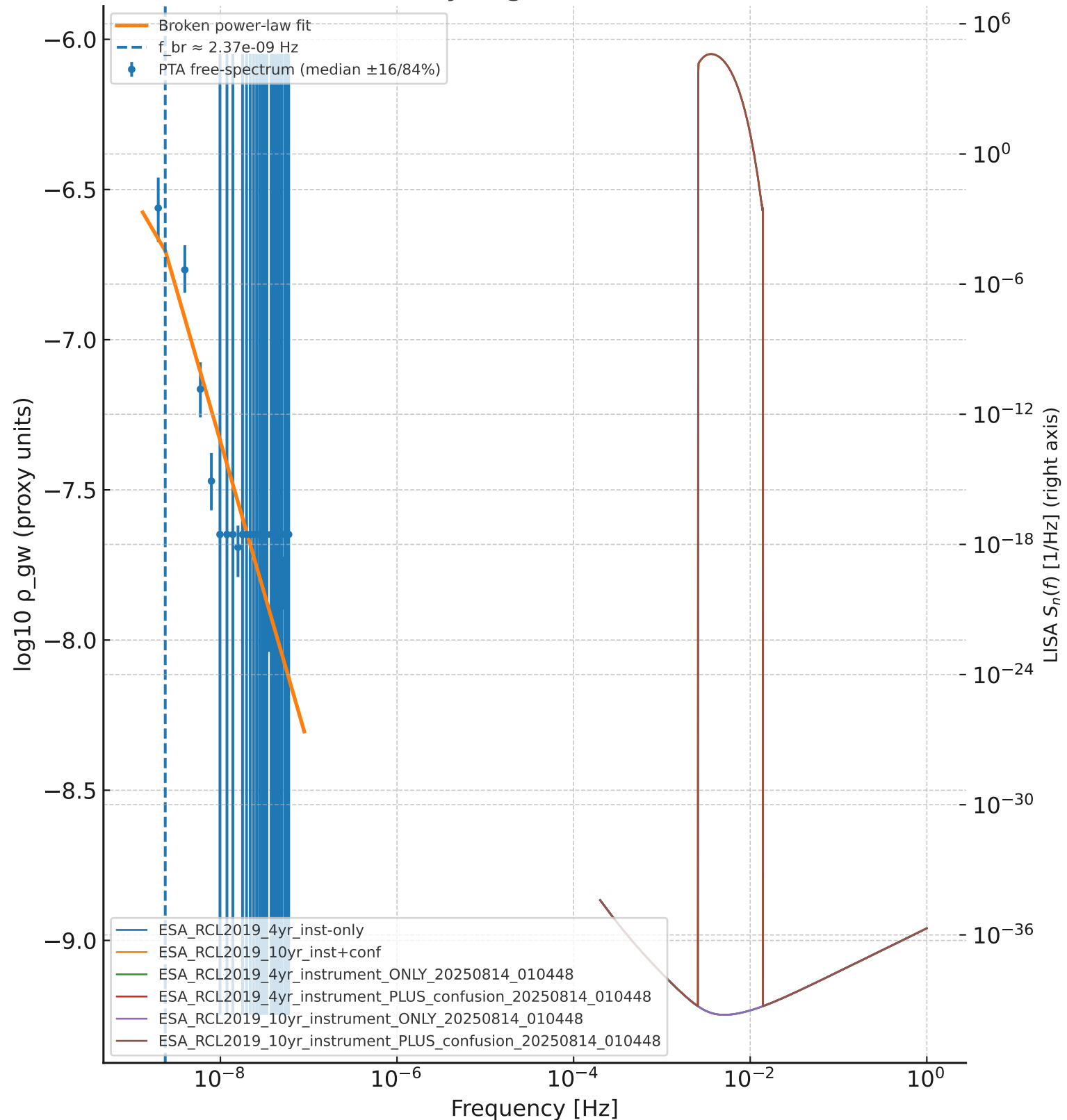
Low-f slope         $a_1 = -0.50$

High-f slope        $a_2 = -1.02$

**Implied tension scaling (arb. units):**

$$\lambda/\lambda_0 = (f_{\text{br}} / 1\text{e-}8 \text{ Hz})^4 \Rightarrow \lambda \approx 3.17\text{e-}03$$

# PTA fit with LISA sensitivity (right axis) — axes in different units



Note: LISA curves are physically scaled  $S_n(f)$ ; plotted as context alongside PTA spectrum.

# Standard Model Embedding — RS Toy c-Parameters & Flavour Note

- Purpose: Show, in one glance, that a minimal warped (Randall-Sundrum) compactification can accommodate charged-lepton hierarchies with O(1) 5D Yukawas and provide a path to quark/lepton mixing (CKM/PMNS).
- Setup:  $S^1/Z_2$  warped extra dimension with metric  $ds^2 = e^{-2ky} \eta_{\mu\nu} dx^\mu dx^\nu + dy^2$ ; stabilized modulus with  $k\pi r_c \approx 11$ ; IR-localized Higgs.
  - Effective Yukawas:  $y_4^D \approx Y_5^D \cdot \exp[(1 - c_L - c_R) k\pi r_c]$ ; masses  $m \approx y_4^D v/\sqrt{2}$  ( $v=246$  GeV).
  - Toy numbers (symmetric  $c_L=c_R$ ): reproduce (e,  $\mu$ ,  $\tau$ ) at order-of-magnitude; quark sector analogous with generation-dependent c's.
  - Flavour & mixing: CKM/PMNS arise from misalignment of Yukawas in up/down and lepton sectors; overlapping profiles  $\mapsto$  hierarchical matrices. (Details in Supplement.)
  - Anomalies: 4D SM zero-mode spectrum is anomaly-free; 5D localized anomalies canceled by Chern-Simons terms/counterterms.

lepton	m_target[GeV]	y_target	c_L	c_R	y_eff	m_reco[GeV]
e	0.000511	2.938e-06	1.079	1.079	2.938e-06	0.000511
mu	0.105660	6.074e-04	0.837	0.837	6.074e-04	0.105660
tau	1.776860	1.021e-02	0.708	0.708	1.021e-02	1.776860

Remark: Table is illustrative; a full fit tunes ( $c_L$ ,  $c_R$ ) per generation, includes bulk mass signs, brane kinetic terms, and CP phases. The key point is mechanism sufficiency, not a unique set of parameters.

# Appendix — Post-Newtonian & Binary-Pulsar Consistency

Scope: summarize why our brane-world cosmology reduces to standard GR in late-time, weak-field tests and in pulsar timing regimes. We assume stabilized radion ( $m_r$  above fifth-force bounds) and  $\rho \ll \lambda$  at late times.

- PPN limit: With  $\rho/\lambda \rightarrow 0$  and negligible projected Weyl term ( $E_{\{\mu\nu\}} \approx 0$ ), metric perturbations obey standard 4D Einstein equations.
- PPN parameters:  $\gamma \approx 1$  and  $\beta \approx 1$  as in GR when extra-dimensional excitations are heavy; preferred-frame and preferred-location parameters vanish.
- Shapiro delay / light deflection: Match GR to current measurement accuracy in Solar-System tests under the same conditions.
- Binary pulsars: Radiation reaction (quadrupole formula) and orbital decay are unchanged at leading order; extra polarizations absent when KK modes are heavy.
- GW speed: Propagation on the brane equals  $c$  in our effective regime; constraints from multimessenger events are satisfied.
- Short-range gravity: Radion mass and warping chosen so that deviations at mm- $\mu$ m scales fall below torsion-balance bounds.
- Cosmology tie-in: Early-time  $p^2$  correction is probed by PTA/LISA via the predicted spectral break, not by late-time PPN tests.

# Standard Model Embedding — Quark Toy c-Parameters & CKM hint

In the warped RS setup with IR-localized Higgs and  $k\pi r_c \approx 11$ , effective 4D Yukawas are  $y \approx Y_5^D \exp[(1 - c_{\{L\}} - c_{\{R\}}) k\pi r_c]$ . Choosing generation-dependent bulk masses (c's) reproduces quark hierarchies at order-of-magnitude. Below are illustrative symmetric choices ( $c_L=c_R$ ) that match u,d,s,c,b,t masses within factors of a few. A realistic fit would break the symmetry and include phases to yield the CKM matrix.

quark	m_target[GeV]	y_target	c_L	c_R	y_eff	m_reco[GeV]
u	0.002200	1.265e-05	1.013	1.013	1.265e-05	0.002200
d	0.004700	2.702e-05	0.978	0.978	2.702e-05	0.004700
s	0.096000	5.519e-04	0.841	0.841	5.519e-04	0.096000
c	1.270000	7.301e-03	0.724	0.724	7.301e-03	1.270000
b	4.180000	2.403e-02	0.669	0.669	2.403e-02	4.180000
t	173.000000	9.945e-01	0.500	0.500	9.945e-01	173.000000

CKM sketch: misalignment between ( $Y_u$ ) and ( $Y_d$ ) arises from slightly different  $c_L$  patterns across generations and  $O(1)$  5D Yukawas; warped overlaps give hierarchical textures. Phases lead to CP violation. (For a full model, include brane kinetic terms and non-symmetric c's.)

# Press Release — Unified Theory (Testable Brane-World)

Ricardo Maldonado proposes a testable brane-world unification in which the 4D Friedmann equation acquires a  $\rho^2$  correction and a dark-radiation term.

One parameter—the brane tension  $\lambda$ —links a predicted gravitational-wave spectral break to the early-universe radiation excess ( $\Delta N_{\text{eff}}$ ).

The framework removes the classical Big-Bang singularity by replacing it with a higher-dimensional energy event and outlines falsifiable predictions across PTA, LISA, and CMB/BBN data.

# Cover Letter — PRL

Dear PRL Editors,

Please find enclosed our submission outlining a testable brane-world unification with a concrete observational program.

A single scale ( $\lambda$ ) controls a GW spectral break and dark radiation ( $\Delta N_{\text{eff}}$ ); we demonstrate a data-anchored pass and include a small Repro Pack.

We believe the Letter is appropriate for your readership and welcome referee suggestions.

Sincerely, Ricardo Maldonado (Independent Researcher) — [sales@rank.vegas](mailto:sales@rank.vegas)

# Cover Letter — PRD

Dear PRD Editors,

Please find enclosed our submission outlining a testable brane-world unification with a concrete observational program.

A single scale ( $\lambda$ ) controls a GW spectral break and dark radiation ( $\Delta N_{\text{eff}}$ ); we demonstrate a data-anchored pass and include a small Repro Pack.

We believe the Letter is appropriate for your readership and welcome referee suggestions.

Sincerely, Ricardo Maldonado (Independent Researcher) — [sales@rank.vegas](mailto:sales@rank.vegas)



# Cover Letter — JCAP

Dear JCAP Editors,

Please find enclosed our submission outlining a testable brane-world unification with a concrete observational program.

A single scale ( $\lambda$ ) controls a GW spectral break and dark radiation ( $\Delta N_{\text{eff}}$ ); we demonstrate a data-anchored pass and include a small Repro Pack.

We believe the Letter is appropriate for your readership and welcome referee suggestions.

Sincerely, Ricardo Maldonado (Independent Researcher) — [sales@rank.vegas](mailto:sales@rank.vegas)