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% Author: Leon Tannenbaum
% Date: June 6th 2021
% Purpose: Analyze a simple swept wing, use this code as basis for transonic cruise analysis.
% Written for Aero 601 Fall 2020 Advanced Aerodynamics - 2020
% This edition of VLM code has some parallelization written into it so as to speed
% up execution time. Alone, a single run is fairly quick. However, when iterated
% >1000 times, integrated over time, execution can be fairly time intensive.
%_wp - with parallelization
% -- Constants ------CONSTANTS
errors on = 1;
sideslip = 0;
% errors on = 1 turn on, 0 off
if ~(errors_on == 0 || errors_on == 1)
   error("Error entry must = 1 or 0.");
end % if ~(errors on == 0 || errors on == 1)
% -- Get number of CPU cores ------CPU core amount
num_cpu = feature('numcores'); % number of available CPU cores
if isempty(gcp('nocreate')) == 1 % no parallel pool is running
   parpool('local', num_cpu);
end % if isempty
% ------CPU core amount
% if B_pg is = 1, then the PG transform isn't done, if <= 1, then PG transform is used.
B_pg = 1;
eps = 1.456619e-16;
Uinf = 1;
rho = 1; % density
gamma = 1; % circulation
     = 5;
     = 1; % wingspan normalized
lambda = .5; % taper
     = 64; % number of panels
c_root = (2*b) / (AR * (1+lambda)); % length
sweep = deg2rad(25); % sweep = deg2rad(25); % 25 degrees of sweep
                     % alfa = deg2rad(6); % angle of attack
alfa
       = deg2rad(6);
beta
      = deg2rad(0); % beta = deg2rad(0); % sideslip
Sref
      = (b^2)/AR;
washout = deg2rad(2); % washout = deg2rad(2);
% -- Input Check ------Input check
if lambda <= 0</pre>
   error(" lambda cannot be less than or equal to zero.");
end % lambda <= 0</pre>
if lambda > 1
   error("lambda cannot be greater than 1");
end % lambda > 1
if AR <=0
   error("AR can't be less than or equal to zero.");
end % AR <=0
```

```
if mod(N,num cpu) ~= 0
   error("N is NOT divisble by the # of available CPU cores, parallelization problem!!");
end % (mod(N,4) \sim = 0)
if (N \le 0) \mid (mod(N,2) == 1) \% check if N is \le 0 or is odd
   error("ERROR N can't be less than/equal to zero or odd.");
end % (N <= 0) \mid \mid (mod(N,2) == 1) % check if N is <= 0 or is odd
% ------Input check
len_y_pts = (N/2) + 1; % number of points (N/2) is number of panels
% ------CONSTANTS
% -- FIND Y POSITIONS AND CHORD LENGTH EDGES------YandCHORD
y_VEC = linspace(-b/2, b/2, len_y_pts);
chord_len_edges = zeros(1, len_y_pts);
for j =1:len_y_pts
   chord_len_edges(j) = chord_x(y_VEC(j), c_root, lambda,b);
   %fprintf("chord_len_edges(%d) = %e\n",j, chord_len_edges(j));
   if isnan(chord_len_edges(j)) == 1
       error("chord_len_edges(%d) = Nan\n", j);
   end % isnan(x_lead_vort_VEC(m)) == 1
end % for j = 1:len_y_pts
% check to make sure chord_len_edges is sym about y
for m = 1:N/2
   if chord_len_edges(m) ~= chord_len_edges(len_y_pts - m+1)
       error("Non Symmetry on chord_len_edges at %d and %d!\n", m, len_y_pts - m+1);
   end
end %
% -- GENERATE THE LEAD/TRAIL EDGE POINTS, LEAD/TRAIL VOR PTS -----LE/TE_LE/TE_VOR
x_leading_VEC = zeros(1, len_y_pts);
x_central_VEC = zeros(1, len_y_pts);
x_trail_VEC = zeros(1, len_y_pts);
x_lead_vort_VEC = zeros(1, len_y_pts);
x_trail_vort_VEC = zeros(1, len_y_pts);
for k = 1:len_y_pts
   h = (c_root - chord_len_edges(k))*.5;
   if isnan(h) == 1
       error("h at (%d) = Nan\n", k, h);
   end % isnan(x lead vort VEC(m)) == 1
   h = add_sweep(sweep, h, y_VEC(k));
   if isnan(h) == 1
       error("h at (%d) = Nan\n", k, h);
   end % isnan(x_lead_vort_VEC(m)) == 1
   x_leading_VEC(k) = h / B_pg;
   x_central_VEC(k) = (h + (chord_len_edges(k)*.5))/B_pg;
   x trail VEC (k) = (h + chord len edges(k))/B pg;
   x_{eq} = (h + (1/8)^* \text{ chord_len_edges(k))/B_pg};
   x_{\text{trail\_vort\_VEC}(k)} = (h + (5/8)* \text{ chord\_len\_edges}(k))/B_pg;
   if isnan(x_lead_vort_VEC(k)) == 1
       error("x_lead_vort_VEC(%d) = Nan\n", k);
   end % isnan(x_lead_vort_VEC(m)) == 1
```

```
end % for k = 1:len_y_pts
%------LE/TE_LE/TE_VOR
% -- GET CONTROL POINTS Y LOCATION IN THE CENTER OF EACH PANEL-----Y_ctrl
y_{ctrl_pts_VEC} = zeros(1, (N/2));
for j = 1:(len_y_pts -1)
   y_{ctrl_pts_vec(j)} = (y_{vec(j)} + y_{vec(j+1)})/2;
end %for i = 1:(length(Y_vec) -1)
% -- Freestream Vel w/ Washout ------Freestream/Washout
% Uinf_x = Uinf * cos(alfa);
% Uinf_y = Uinf * 0;
% Uinf_z = Uinf * sin(alfa);
% U_inf_vec = [Uinf_x Uinf_y Uinf_z];
alfa_VEC = ones(N/2, 1) .* alfa;
wash_f_VEC = zeros(N/2, 1);
parfor m = 1:N/2
   wash_f_VEC(m) = (-2*washout / b) *( abs(y_ctrl_pts_VEC(m)) - (b/2));
end % wash_f_VEC = zeros(N/2, 1);
alfa_w_wash_VEC_n2 = alfa_VEC + wash_f_VEC; % alfa for each panel
alfa_w_wash_VEC_n2(1) = alfa; alfa_w_wash_VEC_n2(N/2) = alfa; % correct numerical computation issues
alfa_wash_VEC_N = [alfa_w_wash_VEC_n2; alfa_w_wash_VEC_n2]; % full alfa vector
% set up matrix with freestream velocity values
U_inf_VEC = zeros(N, 3);
parfor m = 1:N
   Uinf_x = Uinf * cos(alfa_wash_VEC_N(m));
   Uinf_y = Uinf * 0;
   Uinf_z = Uinf * sin(alfa_wash_VEC_N(m));
   U_inf_VEC(m, :) = [Uinf_x Uinf_y Uinf_z];
end % m = 1:N
% ------Freestream/Washout
% -- GET X CONTROL POINTS LOCATION FOR LEADING AND TRAILING EDGE PANELS ---X ctrl
x_{ctrl_lead_VEC} = zeros(1, (N/2));
x_ctrl_trail_VEC = zeros(1, (N/2));
for m = 1:(N/2)
   chord = chord_x(y_ctrl_pts_VEC(m), c_root, lambda,b);
   h = (c_root - chord) * .5;
   h = add_sweep(sweep, h, y_ctrl_pts_VEC(m));
   x_{ctrl_lead_VEC(m)} = (h + (5/16)*chord)/B_pg;
  fprintf("chord = %e,\t m = %d,\th = %e\t x_ctrl_lead_VEC(%d) = %e\n", chord, m, h, m, x_ctrl_lead_VEC(m));
   x_{ctrl_trail_VEC(m)} = (h + (13/16)*chord)/B_pg;
end % m = 1:(N/2)
% ------X_ctrl
% -- Set up Z positions -----Z-ctrl/vort
z_edges_VEC = zeros(1, len_y_pts);
z_lead_vort_VEC = zeros(1, len_y_pts);
z_trail_vort_VEC = zeros(1, len_y_pts);
z_ctrl_lead_VEC = zeros(1, N/2);
z_ctrl_trail_VEC = zeros(1, N/2);
% == WARNING =======PANELS NO MORE VECTORS
```

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% == HERE VECTORS ARE DONE AND PANELS ARE CREATED ===================PANELS NO MORE VECTORS
% ===========PANELS NO MORE VECTORS
lead_vortex = zeros(len_y_pts, 3);
trail_vortex = zeros(len_y_pts, 3);
% set up lead/trail vortex pts
for m = 1:(len_y_pts)
   if isnan(x lead vort VEC(m)) == 1
       error("x lead vort VEC(%d) = Nan\n", m);
   end % isnan(x_lead_vort_VEC(m)) == 1
   if isnan(y_VEC(m)) == 1
       error("y_VEC(%d) = Nan\n", m);
   end % isnan(x_lead_vort_VEC(m)) == 1
   if isnan(z_lead_vort_VEC(m)) == 1
       error("z_lead_vort_VEC(%d) = Nan\n", m);
   end % isnan(z lead vort VEC(m)) == 1
   if isnan(x_trail_vort_VEC(m)) == 1
       error("x_trail_vort_VEC(%d) = Nan\n", m);
   end % isnan(x_lead_vort_VEC(m)) == 1
   if isnan(y_VEC(m)) == 1
       error("y_VEC(%d) = Nan\n", m);
   end % isnan(y_VEC(m)) == 1
   if isnan(z_lead_vort_VEC(m)) == 1
       error("z trail vort VEC(%d) = Nan\n", m);
   end % isnan(z_trail_vort_VEC(m)) == 1
   lead_vortex(m, :) = [x_lead_vort_VEC(m) y_VEC(m) z_lead_vort_VEC(m)];
   trail_vortex(m, :) = [x_trail_vort_VEC(m) y_VEC(m) z_trail_vort_VEC(m)];
end % m = 1:(len_y_pts)
lead_control = zeros(N/2, 3);
trail control = zeros(N/2, 3);
% set up control points
parfor m = 1:(N/2)
   lead_control(m, :) = [x_ctrl_lead_VEC(m) y_ctrl_pts_VEC(m) z_ctrl_lead_VEC(m)];
   trail_control(m, :) = [x_ctrl_trail_VEC(m) y_ctrl_pts_VEC(m) z_ctrl_trail_VEC(m)];
end % m = 1:(N/2)
control = [lead_control; trail_control];
                            -----Generate Vor / Control Vectors
% -- Generate Midpoints ------ Midpoint Matrix
lead mdpts ctl = zeros(N/2, 3);
trail_mdpts_ctl = zeros(N/2, 3);
for m = 1:(N/2)
   lead mdpts ctl(m, 1) = .5*(x \text{ lead vort VEC(m)} + x \text{ lead vort VEC(m+1)});
   lead_mdpts_ctl(m, 2) = .5*(y_VEC(m) + y_VEC(m+1));
   lead_mdpts_ctl(m, 3) = .5*(z_lead_vort_VEC(m) + z_lead_vort_VEC(m+1));
   trail_mdpts_ctl(m, 1) = .5*(x_trail_vort_VEC(m) + x_trail_vort_VEC(m+1));
   trail_mdpts_ctl(m, 2) = .5*(y_VEC(m)
                                            + y_VEC(m+1));
   trail_mdpts_ctl(m, 3) = .5*(z_trail_vort_VEC(m) + z_trail_vort_VEC(m+1));
end % m = 1:(N/2)
midpoint_control = [lead_mdpts_ctl; trail_mdpts_ctl];
                                          -----Generate - Midpoint Matrix
```

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% AT THIS POINT IN THE CODE THE GEOMETRY IS ACCURATE - CHECKED BY "Plots-Wingshape"
% CREATE PANELS TO STORE ALL RELEVANT POINTS: N PANELS, 4 POINTS PER PANEL,
% POINTS ARE ORGANIZED: XA, XB, XC (Control), XM (Midpoint)
% X,Y,Z will be the pages and the final component.
% -- Create Vortex Panels ------Vortex Panels
% N/2 panels, xa/xb, xyz depth
lead vor panels = zeros(N/2,2,3);
trail_vor_panels = zeros(N/2,2,3);
for m = 1:(N/2)
   % read in xa
   lead_vor_panels (m, 1, :) = lead_vortex(m, :);
   trail_vor_panels(m, 1, :) = trail_vortex(m, :);
   % read in xb
   lead_vor_panels (m, 2, :) = lead_vortex(m+1, :);
   trail_vor_panels(m, 2, :) = trail_vortex(m+1, :);
end % m = 1:(N/2)
vor_panels = [lead_vor_panels; trail_vor_panels];
% check for any value in vor_panels == NAN
for m = 1:N
   if isnan(vor_panels(m,1,1)) == 1
       error('vor_panels = NaN, @(%d,1,1)', m);
   end
   if isnan(vor_panels(m,1,2)) == 1
       error('vor_panels = NaN, @(%d,1,2)', m);
   end
   if isnan(vor_panels(m,1,3)) == 1
       error('vor_panels = NaN, @(%d,1,3)', m);
   end
   if isnan(vor panels(m,2,1)) == 1
       error('vor_panels = NaN, @(%d,2,1)', m);
   end
   if isnan(vor_panels(m,2,2)) == 1
       error('vor_panels = NaN, @(%d,2,2)', m);
   end
   if isnan(vor panels(m,2,3)) == 1
       error('vor_panels = NaN, @(%d,2,3)', m);
   end
end % m = 1:N
% check if xb(m) = xa(m+1) ow not set up right
for m = 1:(N-1)
   if vor_panels(m+1, 1, :) ~= vor_panels(m, 2, :)
       error("ERROR xb != xa\n");
   end % vor_panels(m+1, 1, :) ~= vor_panels(m, 2, :)
end % m = 1:(N-1)
% -- Generate g_hat and n_hat -----g_hat and n_hat
lead g = zeros((N/2), 3);
trail_g = zeros((N/2), 3);
```

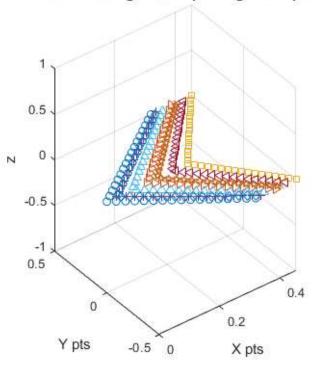
```
lead n hat = zeros((N/2), 3);
trail_n_hat = zeros((N/2), 3);
for m = 1:(N/2)
   % pattern: g_hat = (xb - xa) x (xc - xa)
   lead_g(m, :) = cross (lead_vortex (m+1, :) - lead_vortex (m, :), lead_control (m, :) - lead_vortex (m, :));
   trail_g(m,:) = cross (trail_vortex(m+1, :) - trail_vortex(m, :), trail_control(m, :) - trail_vortex(m, :));
   lead_n_hat (m, :) = lead_g (m, :)/norm(lead_g (m, :));
   trail n hat(m, :) = trail g(m, :)/norm(trail g(m, :));
    if (norm(lead_n_hat(m, :)) ~= 1) || (norm(trail_n_hat(m, :)) ~= 1)
       disp(norm(lead_g (m, :)));
       disp(norm(trail_g(m, :)));
       disp(lead_g(m,:));
       disp(trail_g(m,:));
       disp(lead_n_hat(m, :));
       disp(trail_n_hat(m,:));
       error("Norm vectors lead n hat and trail n hat have a norm != 1 !!!\n");
   end
end % m = 1:(N/2)
% -- Check for lead n hat and trail n hat norms all = 1 ------CHECK NORMS
for m = 1:(N/2)
   if (norm(lead_n_hat(m, :)) ~= 1) || (norm(trail_n_hat(m, :)) ~= 1)
       disp(lead_n_hat(m, :));
       disp(trail_n_hat(m,:));
       error("Norm vectors lead_n_hat and trail_n_hat have a norm != 1 !!!\n");
   end
end % m = 1:(N/2)
n_hat = [lead_n_hat; trail_n_hat];
% ------CHECK NORMS
% ------g_hat and n_hat
Q_influence = zeros(N,N,3); % N by N by xyz, page 1 is x, page 2 y, page 3 z
for i = 1:N
   for j = 1:N
        fprintf("%d, %d\n", i, j);
%
        disp(control(i, :));
%
        disp(vor_panels(j, 1, :));
%
        disp(vor_panels(j, 2, :));
%
       xa(:) = vor_panels(j, 1, :);
       xb(:) = vor_panels(j, 2, :);
       xc(:) = control(i, :);
       Q_influence(i,j, :) = horse(gamma, xc, xa, xb);
   end \% j = 1:N
end %for i = 1:N
% diagonal check
for m = 1:(N/2)
   for n = 1:(N/2)
       if (Q_influence(m,m,3) > Q_influence(m,n,3)) && m ~= n && (dihedral == 0)
          fprintf("Q_influence m = %d, n = %d\n", m, n);
          fprintf("Q_influence(%d,%d,3) = %f, ", m,m, Q_influence(m,m,3));
          fprintf("Q_influence(%d,%d,3) = %f\n ", m,n, Q_influence(m,n,3));
          error("something is fishy in Q influence!");
       end % if
```

```
end % n = 1:(N/2)
end %m = 1:(N/2)
% -- Solve A_mn*Circ_n = B_n, for Circ_n------Solve for Circ n
B_n = zeros(N,1);
parfor m = 1:N
 B_n(m) = dot(U_inf_VEC(m,:), n_hat(m,:));
end % m = 1:N
Amn = zeros(N,N);
q = [0 \ 0 \ 0];
for i = 1:N
   for j = 1:N
      q(1) = Q_{influence(i, j, 1)}; q(2) = Q_{influence(i, j, 2)}; q(3) = Q_{influence(i, j, 3)};
      Amn(i, j) = dot(q(:), n_hat(i, :));
   end % for j = 1:N
end % for i = 1:N
Circ n = Amn \setminus (-1*B n);
                    -----Solve for Circ n
% NOW WE WILL WORK ON THE VLM FLOW FIELD AND FORCES
Rn = zeros(N, 3);
for m = 1:N
   Rn(m, :) = vor_panels(m, 2, :) - vor_panels(m,1,:);
end % for m = 1:N
%disp(norm(Rn(1,:)));
Qinf mid = zeros(N, N, 3);
% create the Qinf matrix using midpoints as the xc input
for i = 1:N
   for j = 1:N
      xa(:) = vor_panels(j, 1, :);
      xb(:) = vor_panels(j, 2, :);
      xc(:) = midpoint_control(i, :);
      Qinf_mid(i,j, :) = horse(gamma, xc, xa, xb);
   end \% j = 1:N
end \% i = 1:N
% diagonal check
for m = 1:(N/2)
   for n = 1:(N/2)
       if (Qinf_mid(m,m,3) >= Qinf_mid(m,n,3)) \&\& m \sim= n
          fprintf("Qinf_mid m = %d, n = %d\n", m, n);
          fprintf("Qinf_mid(%d,%d,3) = %f, ", m,m, Qinf_mid(m,m,3));
          fprintf("Qinf_mid(%d,%d,3) = %f\n ", m,n, Qinf_mid(m,n,3));
          error("something is fishy in Qinf mid!");
      end % if
   end % n = 1:(N/2)
end %m = 1:(N/2)
% Vn hat
cQnm_x = Circ_n' * Qinf_mid(:,:, 1);
cQnm y = Circ n' * Qinf mid(:,:, 2);
cQnm_z = Circ_n' * Qinf_mid(:,:, 3);
```

```
% N*xyz
cQnm = [cQnm_x' cQnm_y' cQnm_z'];
Vel_mat_w_wash = U_inf_VEC + cQnm;
\% ------RN, Qmn w/ midpoint Vn
% Transformation matrix
% wf_bf_transform_mat = ...
    [cos(beta)*cos(alfa) sin(beta)*cos(alfa) -sin(alfa); ...
    -sin(beta) cos(beta) 0; ...
%
     cos(beta)*sin(alfa) sin(beta)*sin(alfa) cos(alfa)];
Wind_F_n = zeros(N,3);
parfor m = 1:N
  [bf_wf_transform_mat] = bf2wf(alfa_wash_VEC_N(m), beta);
   F_n = rho * Circ_n(m) * cross(Vel_mat_w_wash(m, :), Rn(m, :));
   Wind_F_n(m, :) = bf_wf_transform_mat\F_n';
end
Drag = sum(Wind_F_n(:,1)); Side = sum(Wind_F_n(:,2)); Lift = sum(Wind_F_n(:,3));
% fprintf("Lift = %f,\t Drag = %f\n", Lift, Drag);
% -- Solve for Variables, CL, CDi, e, a ------CL,CDi,e,a
CL = Lift/(Sref*.5*rho*Uinf^2);
CDi = Drag/(Sref*.5*rho*Uinf^2);
e = (CL)^2/(pi*AR*CDi);
if errors_on == 1
fprintf("CL = %f,\t CDi = %f\n", CL, CDi);
fprintf("e = %f\n", e);
if abs(CL) > .7 \mid\mid abs(CL) < .1
   fprintf("Not an error, but weird CL values.\n");
end % if CL > .6 \mid \mid CL < .3
if CDi <= 0
   error("CDi CANNOT be less than or equal to zero! Drag <= 0, & Axial < 0\n.");</pre>
end % Cdi < 0
if (e > 2) || (e < .4)
   error("e > 2 or e < .5. These are BAD e values.");</pre>
end % if (e > 2) || (e < .5)
end % if errors_on == 1
% ------CL,CDi,e,a
% -- Find Panel Areas -----Panel Areas
lead_panel_area = zeros(1,N/2);
trail_panel_area = zeros(1,N/2);
% get panel areas
for m = 1:N/2
   lead_vec = [x_leading_VEC(m) y_VEC(m) z_edges_VEC(m)] - ...
              [x_central_VEC(m) y_VEC(m) z_edges_VEC(m)];
   lead\_vec\_2 = [x\_leading\_VEC(m+1) \quad y\_VEC(m+1) \quad z\_edges\_VEC(m+1)] - \dots
              [x_central_VEC(m+1)  y_VEC(m+1)  z_edges_VEC(m+1)];
   center_vec = [x_central_VEC(m+1) y_VEC(m+1) z_edges_VEC(m+1)] - ...
              [x_central_VEC(m) y_VEC(m) z_edges_VEC(m)];
   trail_vec = [x_trail_VEC(m)  y_VEC(m) z_edges_VEC(m)] - ...
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```
[x_central_VEC(m) y_VEC(m) z_edges_VEC(m)];
   \label{eq:trail_vec_2} {\tt trail\_vec\_2} \ = \ [ x\_{\tt trail\_VEC(m+1)} \qquad y\_{\tt VEC(m+1)} \qquad z\_{\tt edges\_VEC(m+1)} ] \ - \ \dots
               [x_central_VEC(m+1)  y_VEC(m+1)  z_edges_VEC(m+1)];
   lead_panel_area(m) = norm(lead_vec + lead_vec_2) * norm(center_vec) * .5;
   trail_panel_area(m) = norm(trail_vec + trail_vec_2) * norm(center_vec) * .5;
end % m = 1:N/2
% ------Panel Areas
% -- PLOT1 ------Plot1-Wingshape
grid on
scatter3(x_leading_VEC, y_VEC, z_edges_VEC, 'o');
hold on
plot3(x_central_VEC, y_VEC, z_edges_VEC, '>');
plot3(x_trail_VEC, y_VEC, z_edges_VEC,
plot3(x_lead_vort_VEC, y_VEC, z_lead_vort_VEC, '+');
plot3(x_trail_vort_VEC, y_VEC, z_trail_vort_VEC, 'x');
plot3(x_ctrl_lead_VEC, y_ctrl_pts_VEC, z_ctrl_lead_VEC, '^');
plot3(x_ctrl_trail_VEC, y_ctrl_pts_VEC, z_ctrl_trail_VEC, '<');</pre>
plot3(lead_mdpts_ctl(:, 1), lead_mdpts_ctl(:, 2), lead_mdpts_ctl(:, 3), 'd');
plot3(trail_mdpts_ctl(:, 1), trail_mdpts_ctl(:, 2), trail_mdpts_ctl(:, 3), 'p');
legend('Leading Edge', 'Central Line', 'Trailing Edge',...
      'Leading vortex in/out Pts', 'Trailing vortex in/out Pts', ...
      'Leading Control Pts', 'Trailing Control Pts', ...
      'Leading Midpoints' , 'Trailing Midpoints');
xlabel('x');
ylabel('y');
zlabel('z');
title('Plot 1 Rectangular/Swept Wing with taper'); xlabel('X pts'); ylabel('Y pts');
% -- Profiling ------Profiling
s = profile('status');
disp(s);
% ------Profiling
```

Plot 1 Rectangular/Swept Wing with taper





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