

Time complexity analysis of iterative programs

A l g o r i t h m s	
Iterative	Recursive
Looping	Calls itself

```
A() {
    l=1, s=1, n=99;
    while(s≤n) {
        i++;
        s=s+i;
        pf("print");
    }
}
```

S: 1, 3, 6, 10, 15, 21 >n

l: 1, 2, 3, 4, 5

$$k(k+1)/2 > n \Rightarrow k^2 = n \Rightarrow k = O(\sqrt{n})$$

```
A(){
    if(n>1)
        return A((n-1))
}
```

$$\Rightarrow T(n) = 1 + T(n-1)$$

By **Back substitution**

$$T(n-1) = 1 + T(n-2)$$

$$T(n-2) = 1 + T(n-3)$$

$$T(n-3) = 1 + T(n-4)$$

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Substitute $T(n-1)$ in $T(n)$

$$T(n) = 1 + 1 + T(n-2)$$

$$= 2 + T(n-2)$$

Substitute $T(n-2)$ in $T(n)$

$$= 2 + 1 + T(n-3)$$

$$= 3 + T(n-3)$$

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Hence, $T(n) = k + T(n-k)$

Alpha condition is $n > 1$; $n - k = 1 \Rightarrow k = n - 1$

$$T(n) = (n-1) + T(n-(n-1))$$

$$= (n-1) + T(1)$$

$$= (n-1) + 1$$

$$= n$$

Therefore, $O(n)$