

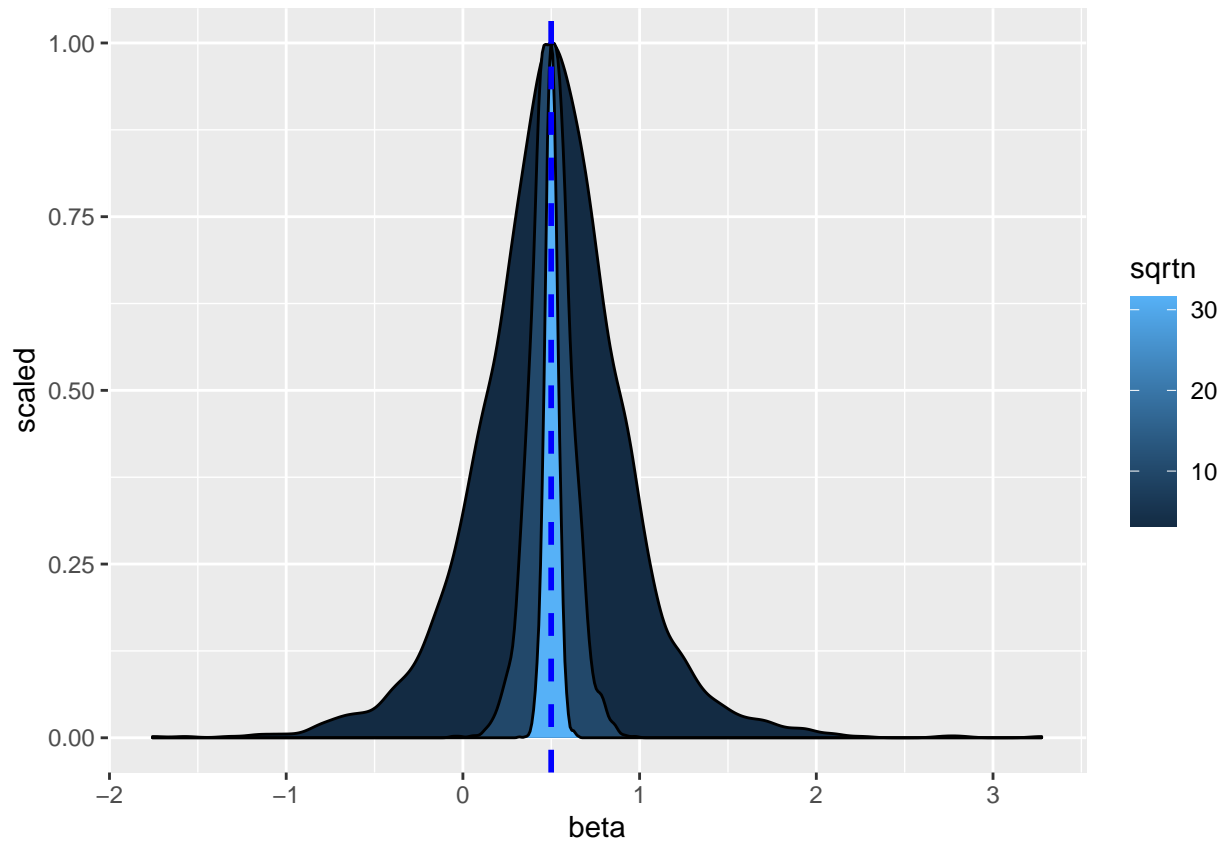
# Homework 3

## Corner Solutions

2/23/2022

1. We are asked to show that  $\hat{\beta}$  converges to both a constant and a normal distribution. This is a function of it being derived using the CLT. Recall that  $\hat{\beta} \sim N(\beta, \frac{V_{\beta}}{n})$ , and so as  $n \rightarrow \infty$  our variance goes to 0. Below we use show this graphically using non-normal errors and show that they not only approximate  $\beta$  but also have variance going to 0, which is exactly what we want.

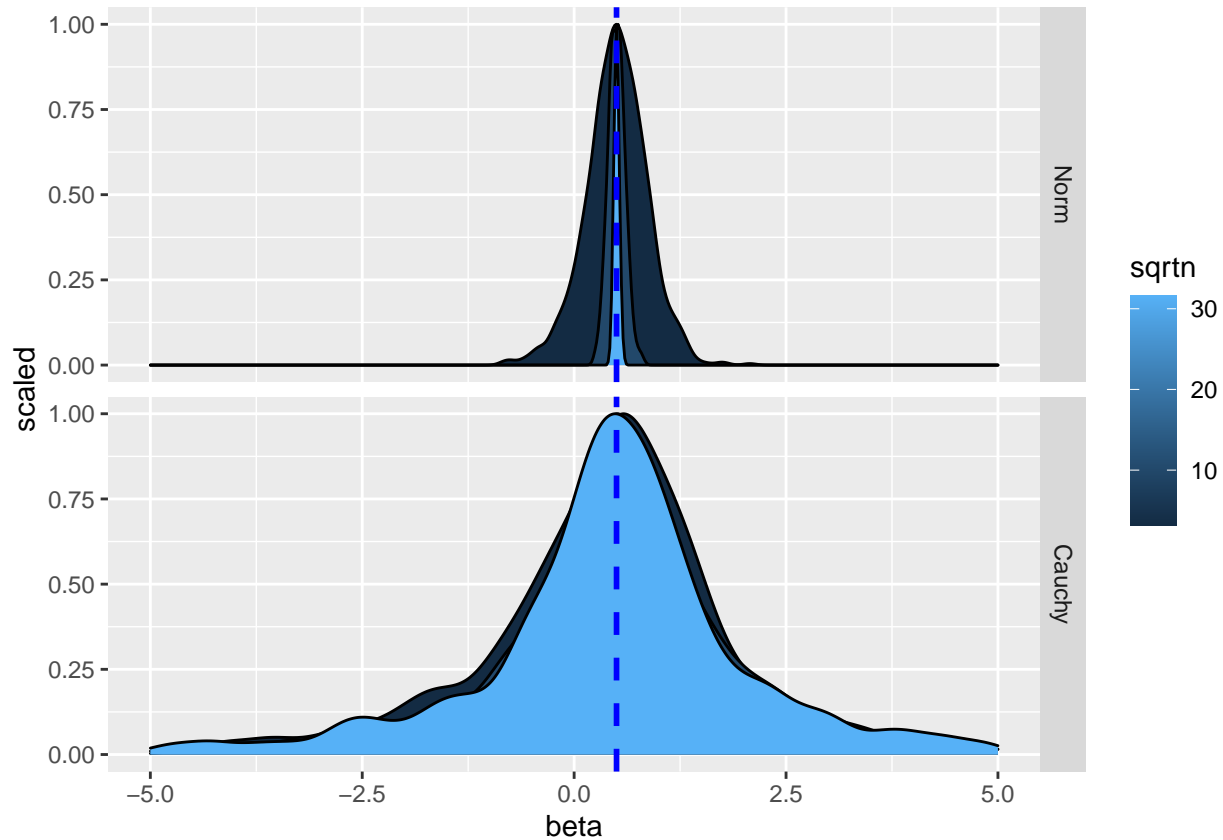
So as  $\sqrt{n} \rightarrow \infty$  our variance approaches 0 and we notice our  $\hat{\beta}_1 \rightarrow \beta$  which is a constant!



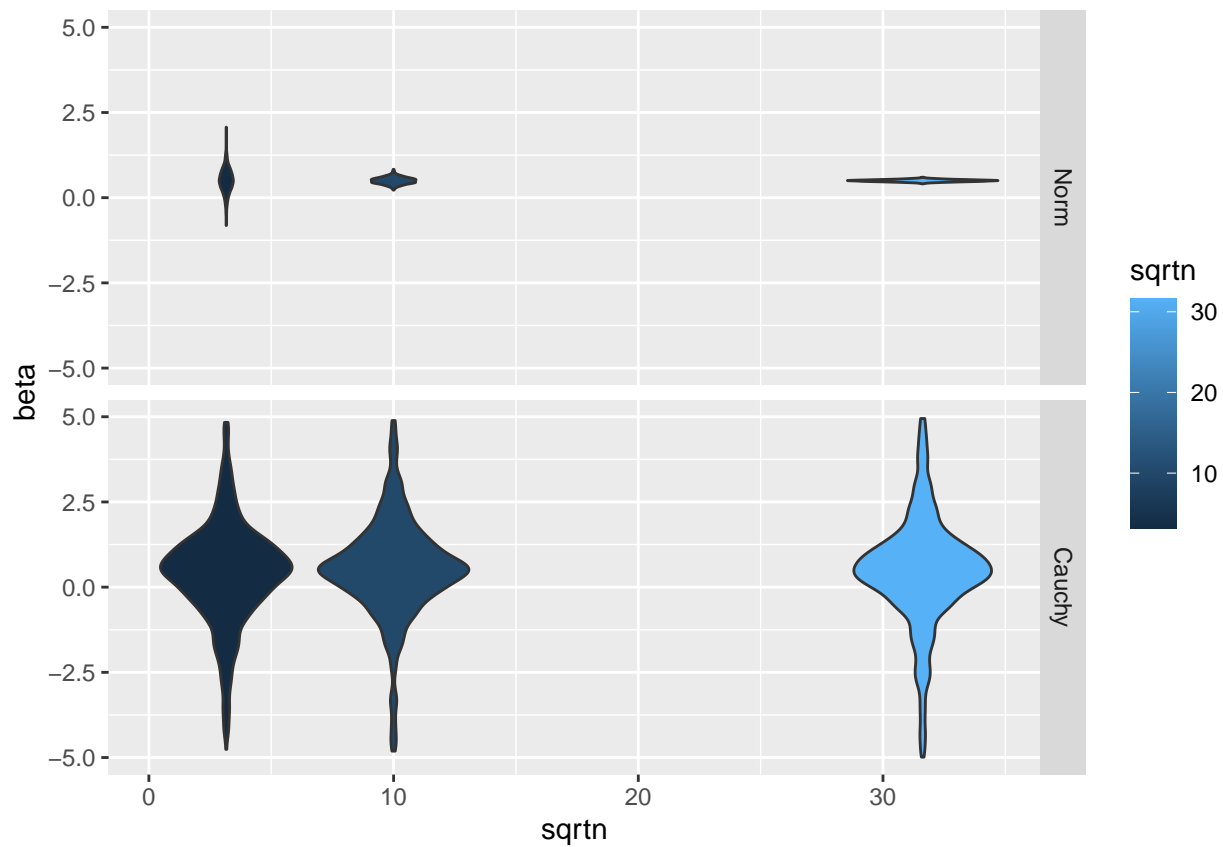
2. Here we are asked to explore the Cauchy distribution. I used the prescribed DGP in the previous problem for convenience, so I'm able to recycle some of the functions here.

```
## # A tibble: 3 x 5
##       n mean_beta_Norm mean_beta_Cauchy sd_beta_Norm sd_beta_Cauchy
##   <dbl>      <dbl>      <dbl>      <dbl>      <dbl>
## 1    10        0.500        0.601        0.362        18.4
## 2   100        0.501        0.905        0.0990         9.65
## 3  1000        0.501        0.728        0.0315        14.0

## Warning: Removed 317 rows containing non-finite values (stat_density).
```



```
## Warning: Removed 317 rows containing non-finite values (stat_ydensity).
```



2.3 Since the Cauchy distribution doesn't have finite moments we're not able to use the asymptotic properties that would apply under proper constraints to most distributions. That's why our errors never converge to 0 and we never achieve the convergence to  $\beta$  as we do when we have errors that follow distributions with finite moments.