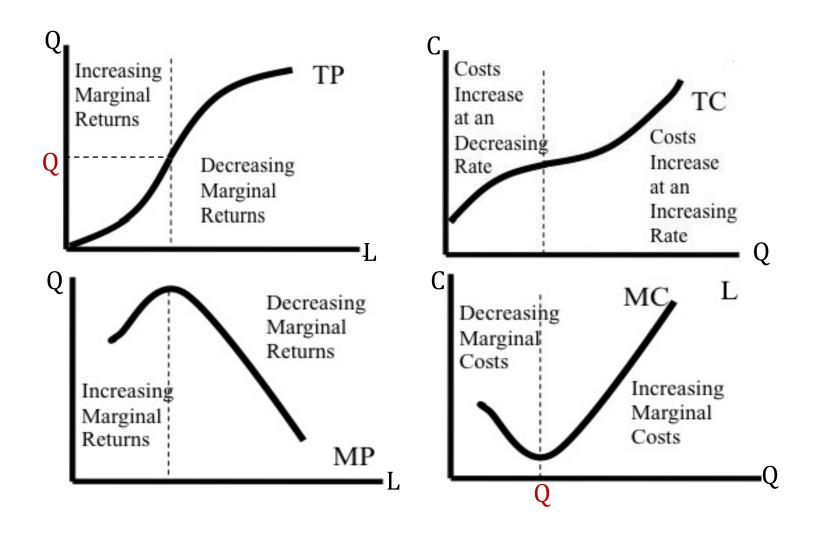
Introductory Microeconomics

Tutorial 8 Nhan La

Production functions



Production functions

Total Product: TP(L) = Q(L)

Marginal Product: $MP(L) = \frac{\partial Q(L)}{\partial L}$

Total cost: SRTC(Q) = FC + VC(Q)

Marginal cost: $SRMC(Q) = \frac{\partial SRTC(Q)}{\partial Q} = \frac{\partial VC(Q)}{\partial Q} = \frac{w}{MP(Q)}$

- Supply curve (SRMC > AVC)

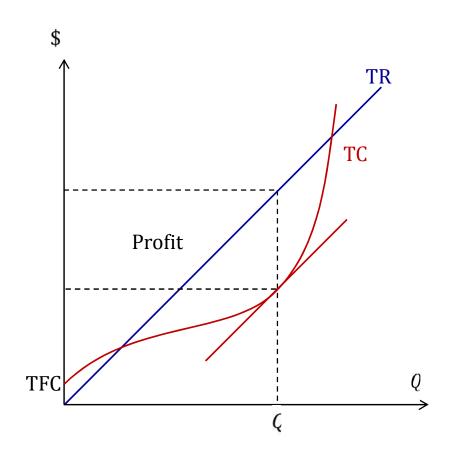
Total Revenue: $TR = P \times Q$

Marginal/Average revenue: $AR = MR = \frac{TR}{Q} = P$

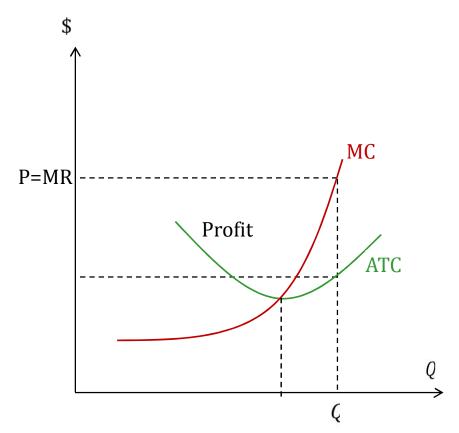
Demand curve

Profit maximisation

Total decision



Marginal decision



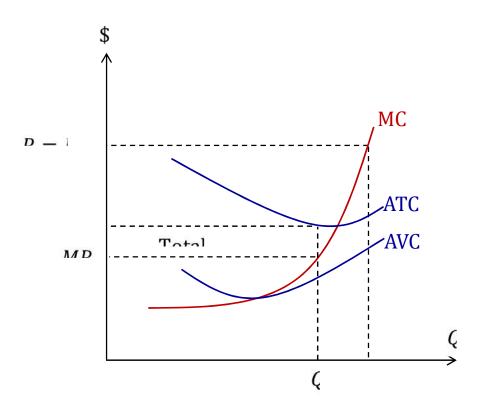
Short run decision

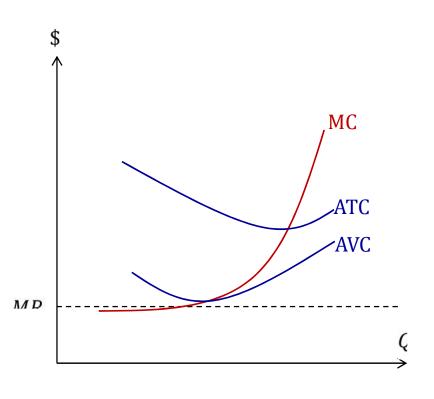
Operate

$$MR = P > AVC(Q)$$

Exit

$$MR = P < AVC(Q)$$





a/

Events	VC	SRMC	FC	SRTC		TC
		$(TC_{t+1} - TC_t)$		(VC + FC)		7 C'N
0	0	-	500	500+0=5 00	-	-
1	1000	1500- 500= 1000	500	1000+50 0= 1500	1000/1= 1000	1500/1= 1500
2	2400	1400	500	2900	1200	2900/2= 1450
3	4200	1800	500	4700	1400	1566.7
4	6400	2200	500	6900	1600	1725
5	9000	2600	500	9500	1800	1900

b/
$$P = AR = MR = 1,500$$

Events	VC	$\begin{array}{c} SRMC \\ (TC_{t+1} - TC_t) \end{array}$	FC	$\begin{array}{c} \mathbf{SRTC} \\ (VC + FC) \end{array}$		L
					1,	·
0	0	-	500	500	-	-
1	1000	1000	500	1500	1000	1500
2	2400	1400<1500	500	2900	1200	1450
3	4200	1800	500	4700	1400	1566.7
4	6400	2200	500	6900	1600	1725
5	9000	2600	500	9500	1800	1900

$$c/\Pi = TR - TC = P * Q - TC = 1500 \times 2 - 2900 = 100$$

Entry/exit: $TR \leq TVC \iff MR = AR = P \leq AVC$

Profit: $TR \leq TC \iff MR = AR = P \leq ATC$

$$a/TC(Q) > TR(Q)$$

 $\Rightarrow TFC + TVC(Q) > TR(Q)$

Need more information

b/
$$TVC(Q) > TR(Q)$$

 $\Rightarrow AVC > AR = MR = P$

Shut down

Entry/exit: $TR \leq TVC \Leftrightarrow MR = AR = P \leq AVC$

Profit: $TR \leq TC \iff MR = AR = P \leq ATC$

c/MR(Q) > MC(Q)

Need more information

d/TR(Q) > TFC

Need more information

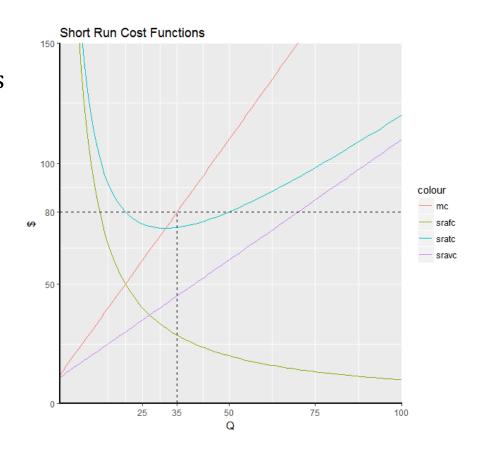
e/MR = AR = P > ATC

Produce

$$AR = MR = P = 80$$
; $FC = 1000$; $VC(Q) = 10Q + Q^{2}$
 $a/SRTC = FC + VC = 1000 + 10Q + Q^{2}$
 $SRAFC = \frac{FC}{Q} = \frac{1000}{Q}$
 $SRAVC = \frac{VC}{Q} = 10 + Q$
 $SRATC = \frac{SRTC}{Q} = \frac{1000}{Q} + 10 + Q$
 $MC = \frac{\partial SRTC}{\partial Q} = 10 + 2Q$

b/ As Q increases:

- SRAFC monotonically decreases
- SRAVC increases
- SRATC lies above SRAVC but these lines catch up
 - Why? SRAFC decreases
- MC goes through the minimum on SRAVC and SRATC



c/

$$MR = AR = P = 80$$

 $TC = 1000 + 10Q + Q^{2}$
 $MC = 10 + 2Q$

To maximise profit firm sets:

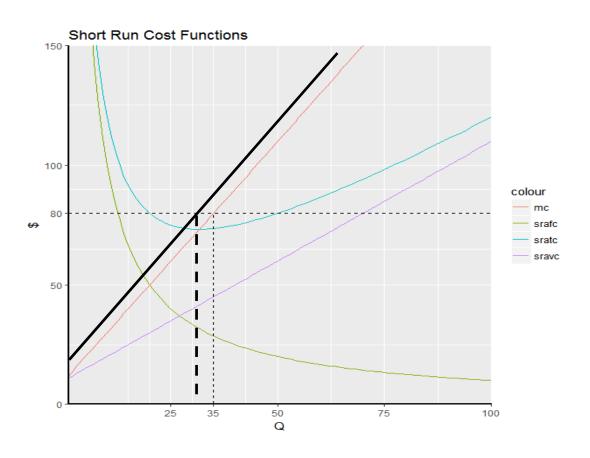
$$MR = P = MC \iff 80 = 10 + 2Q^* \iff Q^* = 35$$

$$TR = PQ^* = 80 \times 35 = 2800$$

 $TC = 1000 + 10 \times 35 + 35^2 = 2575$

$$\Pi = TR - TC = 2800 - 2575 = 225$$

d/ Tax on restaurant: Shift the supply curve (MC) upward



d/ Tax on restaurant:

$$VC = 4Q + 10Q + Q^2$$

$$VC = 14Q + Q^2$$

Supply: MC = 14 + 2Q (Compare with before tax: MC = 10 + 2Q)

Still, to maximise profit firm sets:

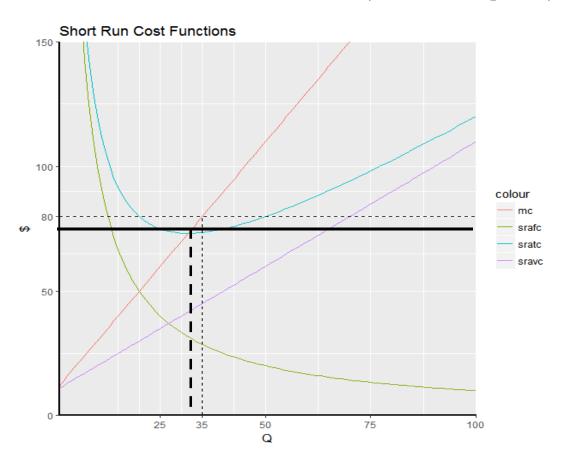
$$MR = P = MC \Leftrightarrow 80 = 14 + 2Q^* \Leftrightarrow Q^* = 33$$

$$TR = PQ^* = 80 \times 33 = 2640$$

$$TC = 1000 + 14 \times 33 + 33^2 = 2551$$

$$\Pi = TR - TC = 2640 - 2551 = 89$$

d/ Tax on customers: Shift the demand curve (or market price) downward



d/ Tax on customers:

Demand:
$$MR = P = 80 - 4 = 76$$

Supply:
$$MC = 10 + 2Q$$

Again, to maximise profit firm sets:

$$MR = P = MC \Leftrightarrow 76 = 10 + 2Q^* \Leftrightarrow Q^* = 33$$

$$TR = PQ^* = 76 \times 33 = 2508$$

$$TC = 1000 + 10 \times 33 + 33^2 = 2419$$

$$\Pi = TR - TC = 2508 - 2419 = 89$$