# Combinatori

### Mattia Martelli

## Forma di Backus-Naur

$$T \coloneqq V \mid \lambda V. \, T \mid (T \, T)$$

## $\lambda$ calcolo

$$\begin{split} \mathbf{I} &\coloneqq \lambda x. \, x \\ \mathbf{K} &\coloneqq \lambda x. \, \lambda y. \, x \\ \mathbf{S} &\coloneqq \lambda xyz. \, x \, z \, (y \, z) \\ \mathbf{B} &\coloneqq \lambda xyz. \, x \, (y \, z) \\ \mathbf{C} &\coloneqq \lambda xyz. \, x \, z \, y \\ \mathbf{W} &\coloneqq \lambda xy. \, x \, y \, y \\ \boldsymbol{\omega} &\coloneqq \lambda x. \, x \, x \\ \boldsymbol{\Omega} &\coloneqq (\lambda x. \, x \, x) \, (\lambda x. \, x \, x) \\ \mathbf{Y} &\coloneqq \lambda f. \, (\lambda x. \, f \, (x \, x)) \, (\lambda x. \, f \, (x \, x)) \\ \boldsymbol{\Theta} &\coloneqq (\lambda xy. \, y \, (x \, x \, y)) \, (\lambda xy. \, y \, (x \, x \, y)) \end{split}$$

## SKI caclolo

$$\begin{split} \mathbf{I} &\coloneqq \mathbf{S} \, \mathbf{K} \, \mathbf{K} \\ \mathbf{Y} &\coloneqq \mathbf{S} \, (\mathbf{K} \, (\mathbf{S} \, \mathbf{I} \, \mathbf{I})) (\mathbf{S} \, (\mathbf{S} \, (\mathbf{K} \, \mathbf{S}) \, \mathbf{K}) \, (\mathbf{K} \, (\mathbf{S} \, \mathbf{I} \, \mathbf{I}))) \end{split}$$