

Identification and tagging of double  $b$ -hadron  
jets from gluon splitting with the ATLAS  
Detector

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**Identification and tagging of double  $b$ -hadron jets from  
gluon splitting with the ATLAS Detector**

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## Abstract

Esta tesis describe un método que permite la identificación de jets que contienen dos hadrones  $b$ , que se originan en la división de un gluon en un par  $b\bar{b}$ . La técnica desarrollada explota las diferencias cinemáticas entre los llamados jets “merged” y los genuinos jets  $b$ , usando variables que describen la estructura interna y la forma de los jets, construidas a partir de las trazas asociadas a los mismos. Las variables con mayor poder discriminador son combinadas en un análisis de multivariable. Poder identificar y remover jets  $b$  que provienen de la división de un gluon es importante para la estimación y la reducción del fondo a señales de física dentro del Modelo Estándar y en nueva física. El algoritmo diseñado rechaza, en eventos simulados, el 95% (50%) de los jets “merged”, mientras que retiene el 50% (90%) de los jets  $b$  genuinos.

***Palabras clave:*** Experimento ATLAS, Jets, Subestructura de Jets, Etiquetado de Jets  $b$ , *Gluon Splitting*.

## Abstract

This thesis describes a method that allows the identification of double  $B$ -hadron jets originating from gluon-splitting. The technique exploits the kinematic differences between the so called “merged” jets and single  $B$ -hadron jets using track-based jet shape and jet substructure variables combined in a multivariate likelihood analysis. The ability to reject  $b$ -jets from gluon splitting is important to reduce and to improve the estimation of the  $b$ -tag background in Standard Model analyses and in new physics searches involving  $b$ -jets in the final state. In the simulation, the algorithm rejects 95% (50%) of merged  $B$ -hadron jets while retaining 50% (90%) of the tagged  $b$ -jets, although the exact values depend on the jet  $p_T$ .

**Keywords:** ATLAS Experiment, Jets, Jet Substructure,  $b$ -tagging, Gluon Splitting.

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# Chapter 1

## Double $b$ -hadron jet identification

In this chapter we focus on the understanding of the internal structure of  $b$ -jets containing two  $b$ -hadrons by investigating the differences between these and single  $b$ -quark jets. These differences are expected to arise from the two-subjet structure of double  $b$ -hadron or “merged” jets, which would tend to be wider and with a larger number of constituents. Based on these envisaged characteristics, simulated QCD samples of  $b$ -tagged jets were used to explore properties with potential discrimination power. The Monte Carlo distributions were compared to data from the 2011 run for validation. We present results from these studies and discuss the choice of the observables selected to build the multivariable tool presented in Chapter ??.

### 1.1 Data Analysis

The tagging technique presented in this thesis relies on Monte Carlo predictions for the signal (single  $b$ ) or background (merged  $b$ ) hypotheses. The accuracy of the simulation is validated with data by comparing the distributions of the different variables studied.

The data samples employed correspond to proton-proton collisions at  $\sqrt{s} = 7$  TeV delivered by the LHC and recorded by ATLAS between May and November 2011, with the LHC running with 50 ns bunch spacing, and bunches organized in bunch trains. Only data collected during stable beam periods in which all sub-detectors were fully operational are used. After the application of the data quality selection, the surviving data corresponds to an integrated luminosity of  $4.7 \text{ fb}^{-1}$ . The LHC instantaneous luminosity steadily increased during 2011. As a result, the average number of minimum-bias pile-up events, originating from collisions of additional protons in the same bunch as the signal collision, grew from 3 to 20. This fact will be of importance when discussing the selection of discriminating variables.

The Monte Carlo event generators discussed in Section ?? are used here. Samples of dijet events from proton-proton collision processes were simulated with PYTHIA version 6.423 [1], used both for the simulation of the hard  $2 \rightarrow 2$  process as well as for the parton shower, underlying event, and hadronization models. The ATLAS AMBT2 tune of the soft model parameters was used [2]. In order to have sufficient statistics over the entire  $p_T$  spectrum, eight samples were generated with different thresholds of the hard-scattering partonic transverse momentum  $\hat{p}_T$ . Events from different samples were mixed taking into account their respective production cross sections. The simulated data sample used for the analysis gives an accurate description of the pile-up content and detector conditions for the full 2011 data-taking period.

### 1.1.1 Event selection

The event selection and quality criterion used to extract, from the data and Monte Carlo samples, the final set of jets for the analysis comprises different steps:



- **Trigger.** The event sample was collected using the ATLAS single jet triggers which select events with at least one jet with transverse energy above a given threshold. At the hardware Level 1 and local software Level 2 (see Section ??), cluster-based jet triggers are used to select events with high- $p_T$  jets. The Event Filter, in turn, runs the offline anti- $k_t$  jet finding algorithm with  $R = 0.4$  on topological clusters over the complete calorimeter. At this stage, the transverse energy thresholds, expressed in GeV, are: 20, 30, 40, 55, 75, 100, 135, 180. These triggers reach an efficiency of 99% for events having the leading jet with an offline energy higher than the corresponding trigger thresholds by a factor ranging between 1.5 and 2. The jet triggers with the lowest  $p_T$  thresholds were prescaled by up to five orders of magnitude.
- **Primary vertex.** The offline event selection requires at least one primary vertex candidate with 5 or more tracks. No requirements are placed on the longitudinal position (along the beam line) of the vertex as the beam spot is used as a constraint when fitting the vertex.
- **Primary jet algorithm.** The jet algorithm selected for the analysis was the ATLAS default anti- $k_t$  algorithm [3], with a distance parameter  $R = 0.4$ , using calorimeter topological clusters [4] as input.
- **Jet calibration.** The EM+JES calibration scheme, described in Section ??, was used to correct the jet energies for inhomogeneities and for the non-compensating nature of the calorimeter.
- **Jet quality.** Several quality criteria are applied to eliminate “fake” jets that are caused by noise bursts in the calorimeters and energy depositions belonging to a previous bunch crossing [5].

- **Jet tagging.** Only jets tagged as  $b$ -jets using the MV1  $b$ -tagging algorithm at the 60% efficiency working point were considered.
- **Isolation.**  $b$ -tagged jets with close-by jets ( $\Delta R < 0.8$ ) with  $p_T$  higher than 7 GeV at electromagnetic scale were not included in the analysis.

All jets, with transverse momentum between 40 and 480 GeV, the selected  $p_T$  range for the analysis, were required to be in a region with full tracking coverage,  $|\eta_{jet}| < 2.1$ , and they were classified in eight  $p_T$  bins chosen such as to match the jet trigger 99% efficiency thresholds (in GeV): 40, 60, 80, 110, 150, 200, 270, 360. An event is used if it satisfies the highest threshold trigger that is 99% efficient for the  $p_T$  bin that corresponds to the  $p_T$  of its leading jet.

In the case of MC, the reconstructed  $b$ -tagged jets were further classified into single and merged  $b$ -jets based on truth Monte Carlo information. A  $b$ -hadron is considered to be associated to a jet if the  $\Delta R$  distance in  $\eta - \phi$  space between the direction of the hadron and the jet axis is smaller than 0.4. Jets were labeled as merged (single)  $b$ -jets if they contain two (only one)  $b$ -hadron:

$$\text{single } b\text{-jets: } \Delta R(j, b_{1/2}) < 0.4 \quad (1.1)$$

$$\text{merged } b\text{-jets: } \Delta R(j, b_1) < 0.4 \ \& \ \Delta R(j, b_2) < 0.4 \quad (1.2)$$

where  $j$  is a jet in the event and  $b_{1/2}$  are the  $b$ -hadrons in the event. In the case another size parameter is used for jet finding, the definitions in equations 1.1 and 1.2 change accordingly.

### 1.1.2 Track selection

It is important to select genuine tracks belonging to jets. Only tracks located within a cone of radius  $\Delta R(j, \text{track}) \leq 0.4$  around the jet axis were consid-

ered. Cuts on  $p_T^{\text{trk}} > 1.0$  GeV and the  $\chi^2$  of the track fit,  $\chi^2/ndf < 3$ , are applied. In addition, tracks are required to have a total of at least seven precision hits (pixel or micro-strip) in order to guarantee at least 3  $z$ -measurements. Tracks are also required to fulfill cuts on the transverse and longitudinal impact parameters at the perigee to ensure that they arise from the primary vertex. As cutting on impact parameter (IP) significance might be detrimental for  $b$ -jets, where large IP values are expected, relaxed cuts were used,  $|d_0| < 2$  mm, and  $|z_0 \sin \theta| < 2$  mm, with  $\theta$  being the polar angle measured with respect to the beam axis. The track quality cuts are summarized in table 1.1.

Track parameter	Selection
$p_T$	$> 1$ GeV
$d_0^{PV}$	$< 2$ mm
$z_0^{PV} \sin \theta$	$< 2$ mm
$\chi^2/ndof$	$< 3$
Number of Pixel hits	$\geq 2$
Number of SCT hits	$\geq 4$
Number of Pixel+SCT hits	$\geq 7$

Table 1.1: Track selection criteria used for double  $b$ -hadron jet tagging, where  $d_0^{PV}$  and  $z_0^{PV}$  denote the transverse and longitudinal impact parameters derived with respect to the primary vertex. The  $\chi^2/ndof$  is that of the track fit.

## 1.2 Kinematic differences between single and double $b$ -hadron jets

The differences between genuine  $b$ -quark jets and double  $b$ -hadron jets, that in QCD originate mainly from gluon splitting, are expected to arise from the two-subjet structure of merged jets. In this section we present the study of a set of jet shape and substructure variables for the discrimination between single and merged  $b$ -jets. These variables are built from jet constituents either at calorimeter level (topological clusters) or tracks associated to the jet.

### *I. Jet track multiplicity*

The jet track multiplicity is a variable simple to calculate that carries important information of the jet inner structure. It is defined as the number of tracks with  $p_T$  above 1 GeV, satisfying the quality cuts described in section 1.1.2, and contained within a cone of radius  $R = 0.4$  around the jet axis. Figure 1.1 shows its distribution for two  $p_T$  bins, representative of the range covered in this study. It is observed that merged  $b$ -jets contain on average around two more tracks than single  $b$ -jets at low jet  $p_T$ , with a larger difference at higher  $p_T$  values.

The effect of the minimum track  $p_T$  requirement was examined by lowering the selection cut to  $p_T > 0.5$  GeV. On the one hand this could lead to an improvement in discrimination if it captured more information about the fragmentation process; on the other hand, a lower minimum track  $p_T$  can make the method more sensitive to pile-up with the addition of soft tracks incorrectly associated to the jets. It was observed that reducing the  $p_T$  cut of the tracks degrades the discrimination because it widens the distributions without increasing the separation between single and merged jets.

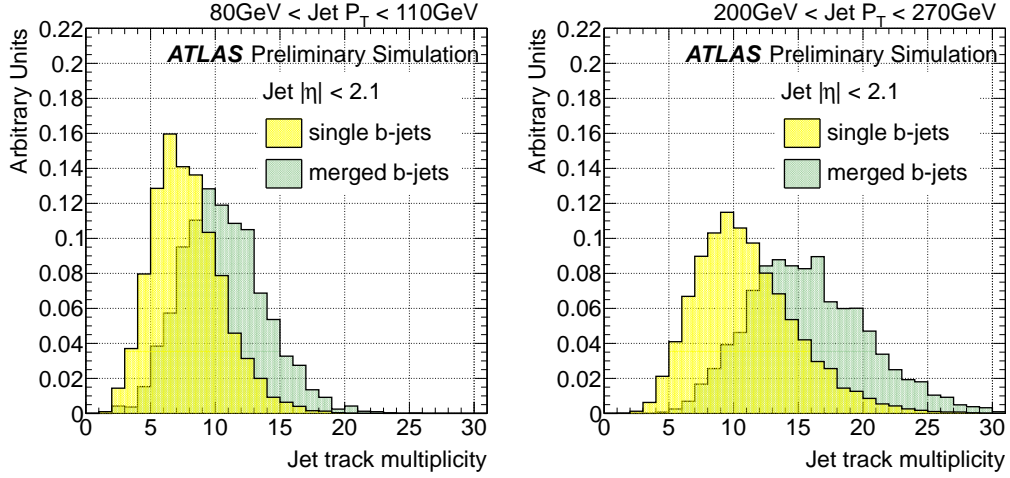


Figure 1.1: Distribution of the track multiplicity in jets for single and merged  $b$ -jets between 80 GeV to 110 GeV (left) and 200 GeV to 270 GeV (right).

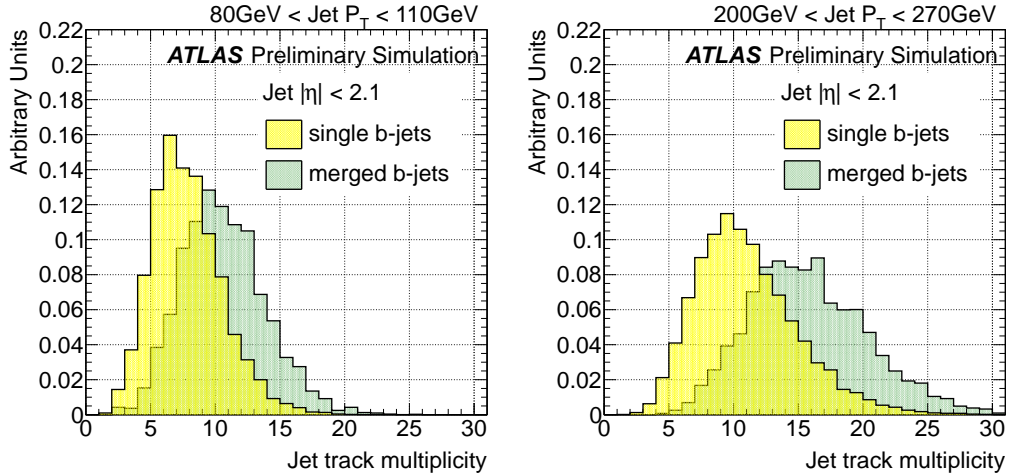


Figure 1.2: Distribution of the track multiplicity in jets for single ( $b$ ) and merged ( $bb$ ) jets between 80 GeV to 120 GeV in a sample of dijet events generated with PYTHIA AND NO DETECTOR SIMULATION. DISTRIBUTIONS ARE SHOWN USING ALL CHARGED PARTICLES (LEFT) AND USING ONLY CHARGED PARTICLES COMING FROM  $B$ -HADRON DECAY (RIGHT).

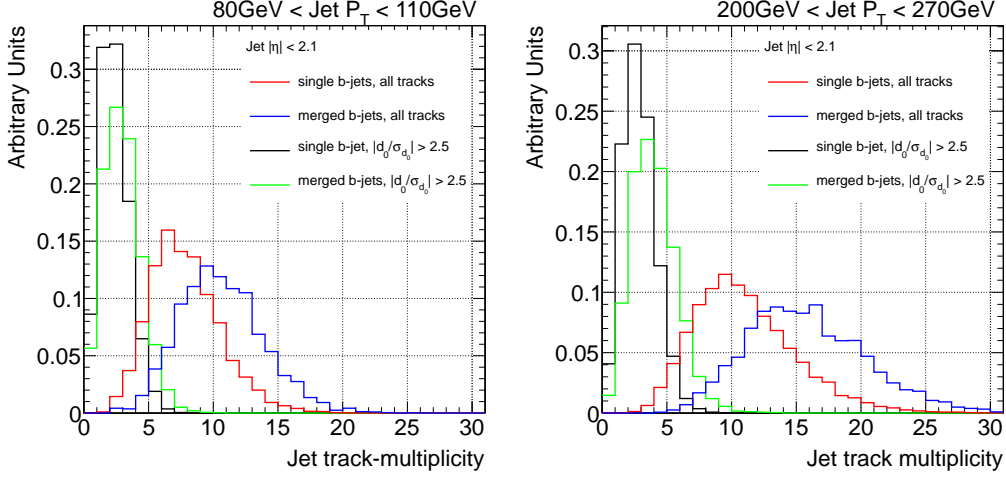


Figure 1.3: Distribution of the jet track multiplicity single and merged  $b$ -jets between 80 GeV to 110 GeV (left) and 200 GeV to 270 GeV (right), for all and displaced tracks only.

Results in PYTHIA standalone using all and “ $b$ -tracks” in Fig. ?? . COMPLETAR. No improvement was obtained either by circumscribing the selection to tracks with large impact parameter significance ( $> 2.5$ ). The potential sensitivity achieved by enriching the sample in tracks associated to the  $b$ -hadron is counterbalanced by the lower number of associated tracks. A comparison of track multiplicity distributions using all tracks and distributions built with displaced tracks is shown in Fig. 1.3.

## II. Jet width

The jet width is part of a set of continuous variables that try to distinguish individual particles/subjects within the jet by means of smooth functions  $(\Delta\eta, \Delta\phi)$  away from the jet axis, in order to form combinations like geometric moments. This particular combination is a linear moment which sums the distances between the jet constituents and its axes, weighted by the con-

stituent  $p_T$ , and then normalized to the total  $p_T$  of the jet. Its definition is,

$$Jet\ width = \frac{\sum_{i=1}^N p_T^{const_i} \Delta R(const_i, jet)}{\sum_{i=1}^N p_T^{const_i}} \quad (1.3)$$

where  $N$  is the total number of calorimeter or track constituents. This observable is also highly correlated to the mass of the jet.

Figure 1.4 shows the distributions for the track-jet width for which the sum in equation 1.3 runs over the  $N$  tracks associated to the jet, using the same criteria as for the jet track multiplicity. As expected, merged  $b$ -jets are wider than single  $b$ -jets.

The jet width can also be measured in terms of calorimeter variables, replacing tracks by topological clusters in the sum. Although it offers good separation, this variable is more sensitive to the amount of pile-up in the event than its track-based counterpart. This is illustrated in Fig. 1.5, which shows the distribution of calorimeter width and track-jet width for single  $b$ -jets in events with low and high number of primary vertices (NPV) in a low  $p_T$  region where the effect of pile-up is more important.

In general, all the studied calorimeter-based jet variables show similar dependences with NPV. For this reason the track-based versions are preferred as more robust discriminators.

### III. Jet Mass

The jet mass, like the linear radial moment, also depends on the radiation pattern of the event. It is the most basic observable for distinguishing massive boosted objects from jets originating from quarks or gluons. The latter are expected to be dominated by wide-angle emissions, with increase probability to see high mass jets initiated from gluons as opposed to quarks [6]. Figure 1.6 shows the distribution of the jet mass for single and merged  $b$ -jets.

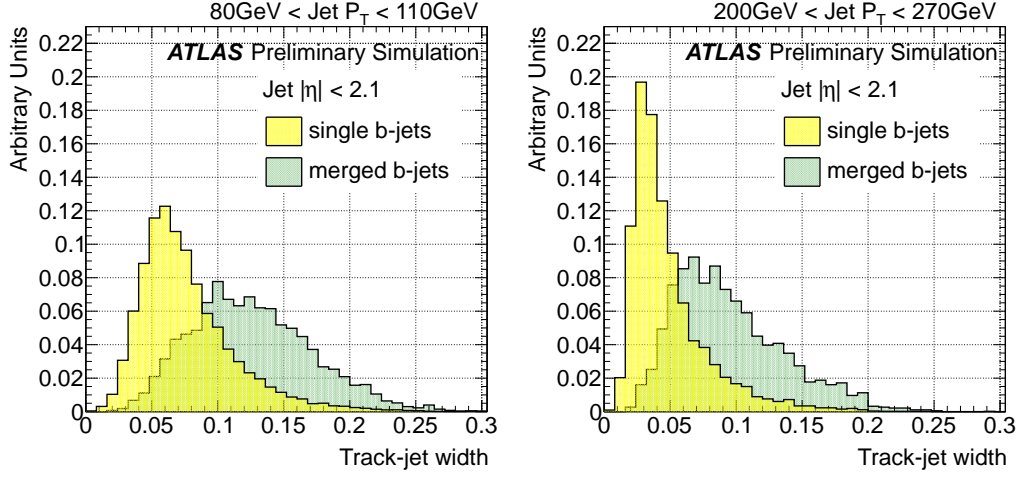


Figure 1.4: Distribution of track-jet width in jets for single and merged  $b$ -jets between 80 GeV to 110 GeV (left) and 200 GeV to 270 GeV (right).

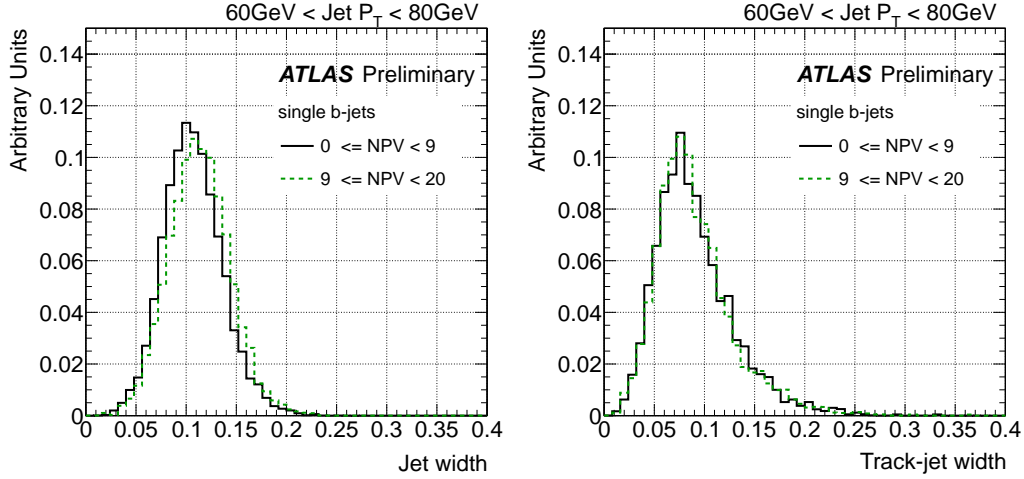


Figure 1.5: Distribution of jet width using topological clusters (left) and tracks (right) for single  $b$ -jets in two bins of number of primary vertices (NPV) for jets between 60 GeV to 80 GeV.



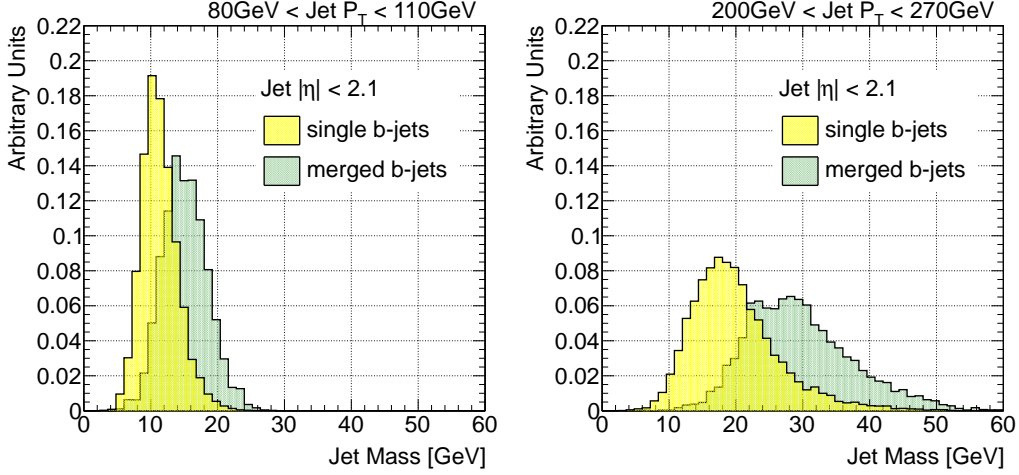


Figure 1.6: Distribution of jet mass in GeV for single and merged  $b$ -jets between 80 GeV to 110 GeV (left) and 200 GeV to 270 GeV (right).

Merged jets tend to have higher masses than single  $b$ -jets for the same  $p_T$  bin. Although it shows good separation, this calorimeter based variable is susceptible to the amount of pile-up in the event and for this it is not a robust discriminator.

#### IV. $\Delta R$ between leading tracks

An alternative approach to measuring the width is to use the angular separation of the two hardest constituents inside jets. This has the advantage of removing any dependence on the shower development within the calorimeter and focuses on the hard components of the jet. Figure 1.7 shows the distribution of the  $\Delta R$  between leading tracks in the jet for single and merged  $b$ -jets. The merged  $b$ -jet distributions are slightly broader than single  $b$ -jet distributions for medium  $p_T$ . The effect diminishes as we go to higher transverse momentum values, offering very poor discrimination.

#### V. Maximum $\Delta R$ between track pairs

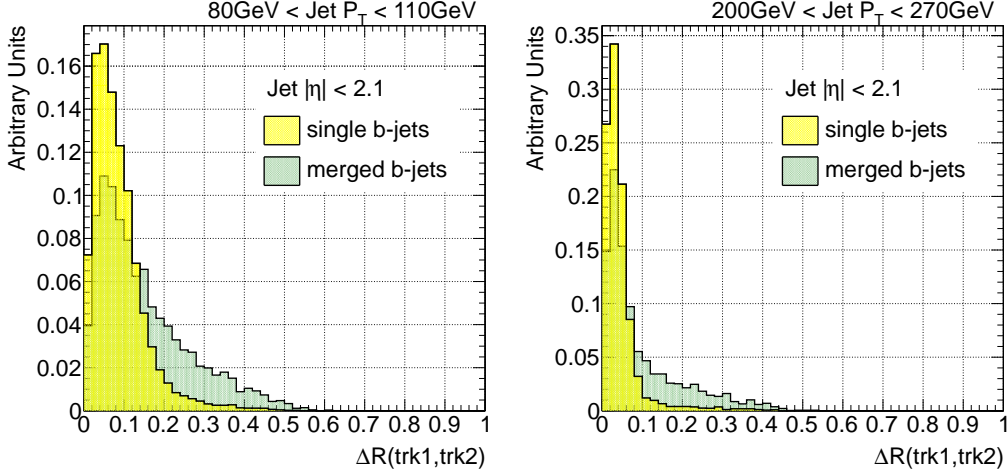


Figure 1.7: Distribution of  $\Delta R$  between leading tracks for single and merged  $b$ -jets between 80 GeV to 110 GeV (left) and 200 GeV to 270 GeV (right).

Several other variables, besides the jet width, were investigated to expose the expected two-subjet substructure of merged  $b$ -jets. The maximum  $\Delta R$  separation between pairs of tracks associated to the jet ( $\max\{\Delta R(trk, trk)\}$ ) was also evaluated as a discriminating variable. Its distribution is shown in Fig. 1.8, for single and double  $b$ -hadron jets. The latter shows significantly higher values for this variable over a broad range of jet  $p_T$ . The distinct characteristic of this variable is that the separation between single  $b$ -jets and merged does not depend on jet  $p_T$ . In spite of its good discrimination power, alternative characterising variables are desirable as  $\max\{\Delta R(trk, trk)\}$  is sensitive to soft tracks originating from pile-up.

#### VI. Number of $k_t$ subjets

The subjet multiplicity – the number of subjets within a jet – provides information on the distribution of energy and multiplicity of particles within a jet. For instance, in [7] the result of measuring this variable on quark- and

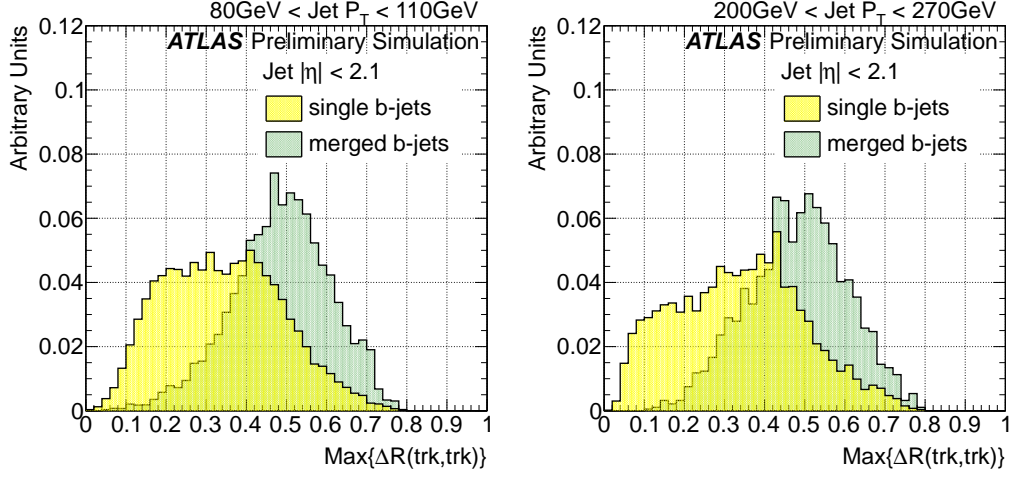


Figure 1.8: Distribution of the maximum  $\Delta R$  between pairs of tracks in jets for single and merged  $b$ -jets between 80 GeV to 110 GeV (left) and 200 GeV to 270 GeV (right).

gluon-initiated jets indicates that gluon-initiated jets tend to have on average higher subjet multiplicity. This result is consistent with the QCD prediction that gluons radiate more than quarks. In the case of this and different other analyses the  $k_t$  algorithm is rerun for subjet finding.

By using the sequential recombination algorithms introduced in Section ??, it is straightforward to define a “subjet algorithm” in which the structure of the jet’s constituents is resolved using either the same jet finder algorithm as used for jet reconstruction or a new one with a fixed (smaller) distance parameter. As an alternative to fixed distance parameter subjects, it is also possible to undo the last step in the recombination sequence [8] in order to identify the decay products of an object. This approach is used in several jet grooming procedures<sup>1</sup>, see for instance [10].

<sup>1</sup>Jet grooming comprises dedicated techniques to remove uncorrelated radiation within a jet. A review of these procedures can be found in [9].

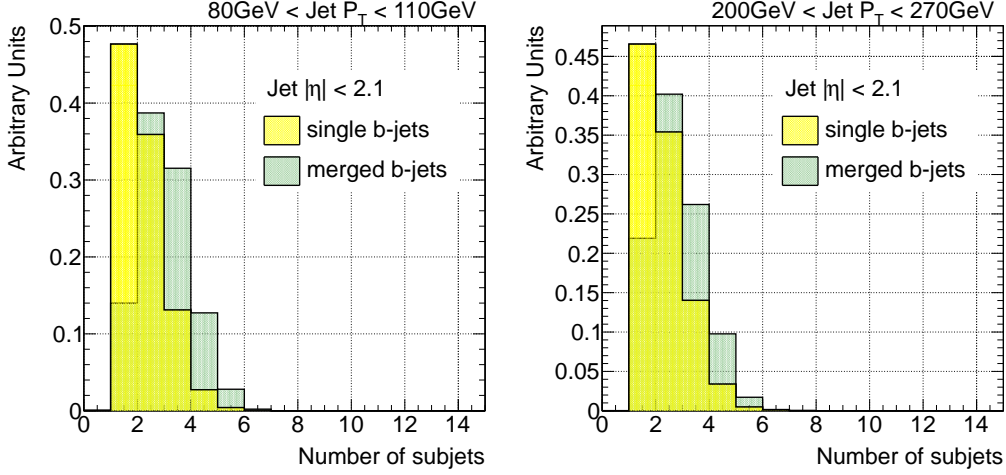


Figure 1.9: Distribution of the number of  $k_t$  sub-track-jets for single and merged  $b$ -jets between 80 GeV to 110 GeV (left) and 200 GeV to 270 GeV (right).

Figure 1.9 shows the distribution of the number of subjects for single and merged  $b$ -jets. The subjects in this case were built using the associated tracks as constituents, clustered by the inclusive  $k_t$  algorithm with distance parameter  $R = 0.2$ . The discrimination power of this variable, as it is defined, turned out to be very poor.

#### VII. $\Delta R$ between the axes of two $k_t$ subjects

The  $\Delta R$  between  $k_t$  subjects is obtained by applying the exclusive  $k_t$  algorithm [11] to the tracks associated to the jet using a large  $k_t$  distance parameter to ensure that all tracks get combined. The clustering is stopped once it reaches exactly two jets. The  $\Delta R$  between the axes of the two exclusive subjects is shown in Fig. 1.10. As expected, it is larger for merged than for single jets. We observe that this variable provides very good separation, with the advantage of infrared safety and insensitivity to pile-up as opposed

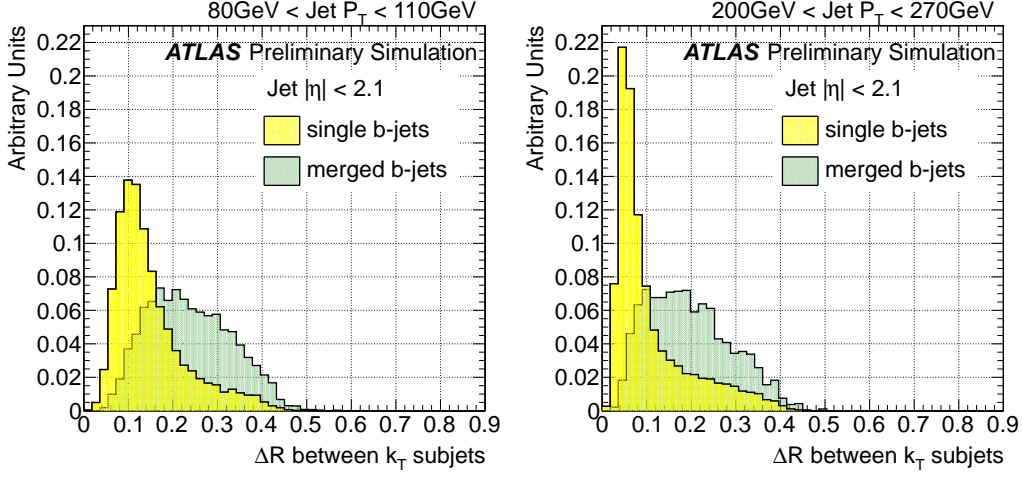


Figure 1.10: Distribution of the  $\Delta R$  between the axes of the two  $k_t$  subjects in the jet for single and merged  $b$ -jets between 80 GeV to 110 GeV (left) and 200 GeV to 270 GeV (right).

to  $\max\{\Delta R((trk, trk))\}$ .

#### VIII. $N$ -subjettiness variables

It is possible to extend the use of individual subjects in conjunction with more traditional jet shape variables. Using these tools, an inclusive jet shape based on the substructure topology of a single jet, “ $N$ -subjettiness” [12] is defined. This variable describes the energy flow within a jet, quantifying the degree to which radiation is aligned along specified subjet axes. This jet shape was adapted from the event shape  $N$ -jettiness [13].

Given candidate subjects directions determined by an external algorithm such as the exclusive  $k_t$  procedure, the variable is defined as,

$$\tau_N^{(\beta)} = \frac{1}{\sum_k p_{T_k} (R_0)^\beta} \sum_k p_{T_k} (\min\{\Delta R_{j1,k}, \Delta R_{j2,k}, \dots, \Delta R_{jN,k}\})^\beta. \quad (1.4)$$

The sum runs over the  $k$  constituent particles in a given jet where  $p_{T,k}$  are their transverse momenta, and  $\Delta R_{j1,k}$  is the distance between the candidate

subjet  $j_1$  and a constituent particle  $k$ .  $R_0$  is the characteristic jet radius used in the original jet clustering algorithm. The exponential weight,  $\beta$ , can optionally be applied to the angular distance computed between the subjets and the jet constituents. Since eq. 1.4 is linear in each of the constituent particle momenta, this variable is an infrared- and colliner-safe observable.

This jet shape was designed to separate boosted hadronic objects, like electroweak bosons and top quarks decaying into collimated showers of hadrons which a standard jet algorithm would reconstruct as single jets. A simple cut on the ratio  $\tau_N/\tau_{N-1}$  provides excellent discrimination power for  $N$ -prong hadronic objects[12]. In particular,  $\tau_2/\tau_1$  can identify boosted  $W/Z$  and Higgs bosons, with the angular weighting exponent  $\beta = 1$  providing the best discrimination.

The definition of  $N$ -subjettiness is not unique, and different choices can be used to give different weights to the emissions within a jet. The initial step of choosing candidate subjet axes is in fact unnecessary; the quantity in equation 1.4 can be minimised over the candidate subjet directions, further improving boosted object discrimination.

To avoid dependence on pile-up we consider track-based  $n$ -subjettiness, where the sum is over the tracks in the  $b$ -tagged jet. As seen for massive boosted objects, a jet with a two pronged structure, with all tracks clustered along two directions, is expected to have a smaller  $\tau_2$  value than a jet with a more uniform track distribution. The distributions of  $\tau_2$ , shown in Fig. 1.11, display good separation between single and merged jets, but with the latter showing larger values than single. This behavior can be traced to the level of correlation between  $\tau_2$  and track-jet width, displayed in Fig. 1.12a, to be compared to the much lower correlation presented, for instance, between track-jet width and the jet track multiplicity, shown in Fig. 1.12b.

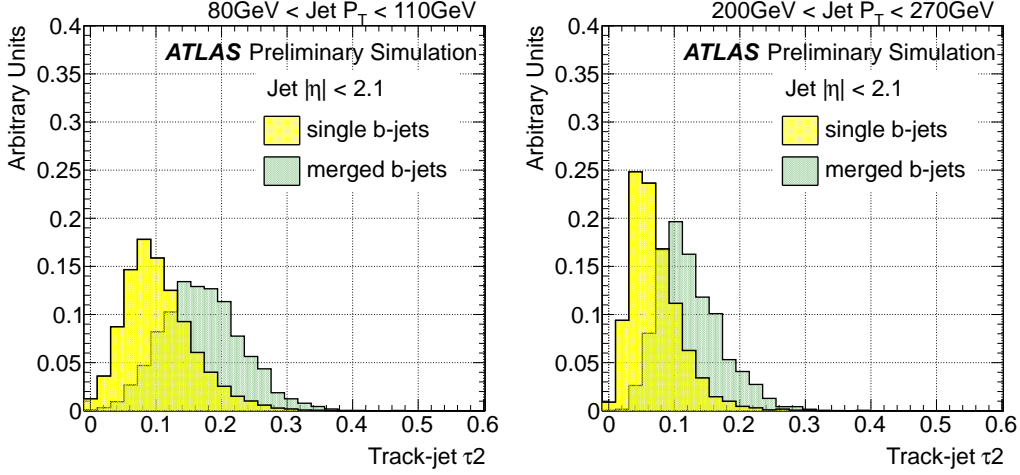


Figure 1.11: Distribution of  $\tau_2$  in jets for single and merged  $b$ -jets between 80 GeV to 110 GeV (left) and 200 GeV to 270 GeV (right).

The correlation observed suggests to switch from an absolute to a width-normalized  $\tau_2$ , and evaluate the ratio  $\tau_2/\tau_1$ . Fig. 1.13 thus shows the distributions for this observable. Somewhat larger values are obtained for single than for merged  $b$ -jets, specially at high  $p_T$ , however we decided not to use this variable as it offers only marginal discrimination.

### IX. Jet eccentricity

In defining a jet moment there are several ways to weight the momentum and define the center of the jet. We have defined the jet width as the first moment of the transverse energy with respect to the jet axis; another example of useful combination is the jet pull [14]. But it is also natural to look at higher moments, such as those contained in the  $2 \times 2$  matrix,

$$\begin{bmatrix} \sum E_i \eta_i^2 & -\sum E_i \eta_i \phi_i \\ -\sum E_i \eta_i \phi_i & \sum E_i \phi_i^2 \end{bmatrix} \quad (1.5)$$

Here,  $(E_i, \eta_i, \phi_i)$  are the jet constituent energy, pseudorapidity and azimuthal

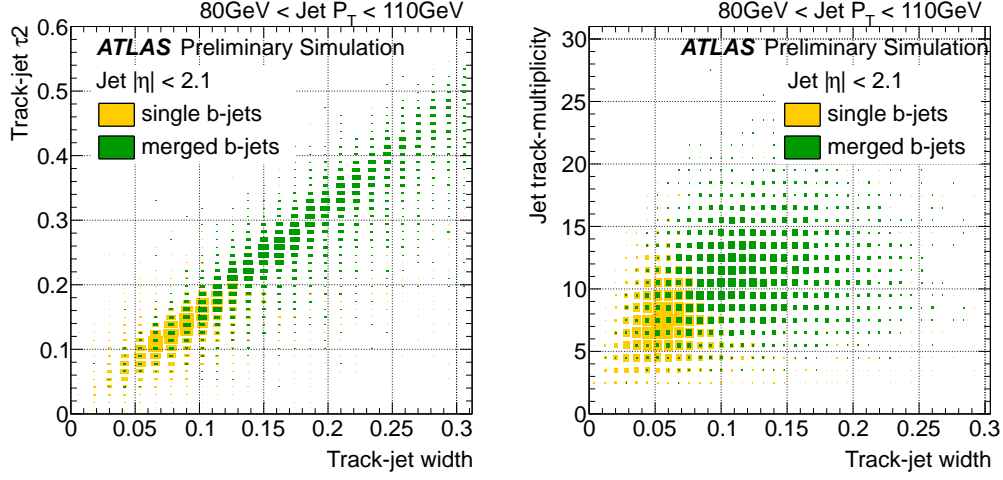


Figure 1.12: Correlation between  $\tau_2$  and track-jet width (left) and jet track multiplicity and track-jet width (right) for single and merged  $b$ -jets between 80 GeV to 110 GeV.

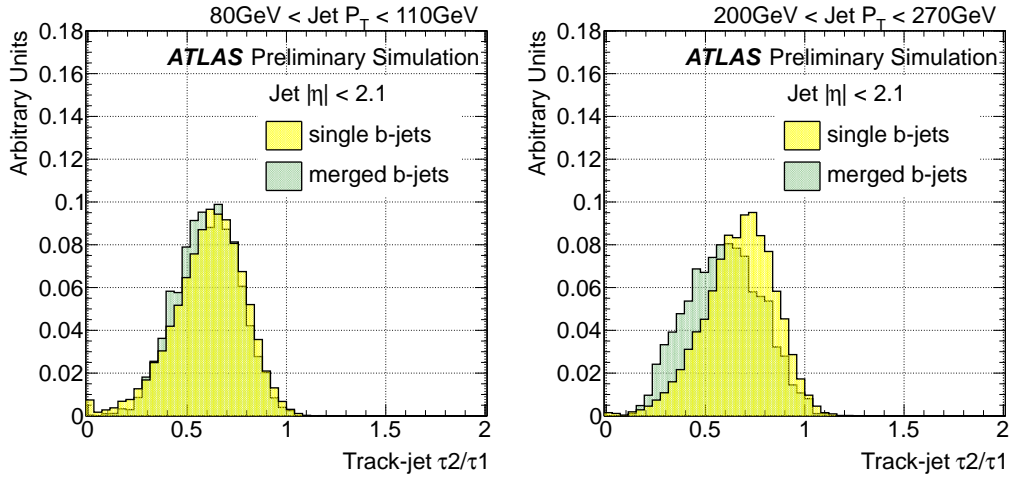


Figure 1.13: Distribution of  $\tau_2/\tau_1$  in jets for single and merged  $b$ -jets between 80 GeV to 110 GeV (left) and 200 GeV to 270 GeV (right).



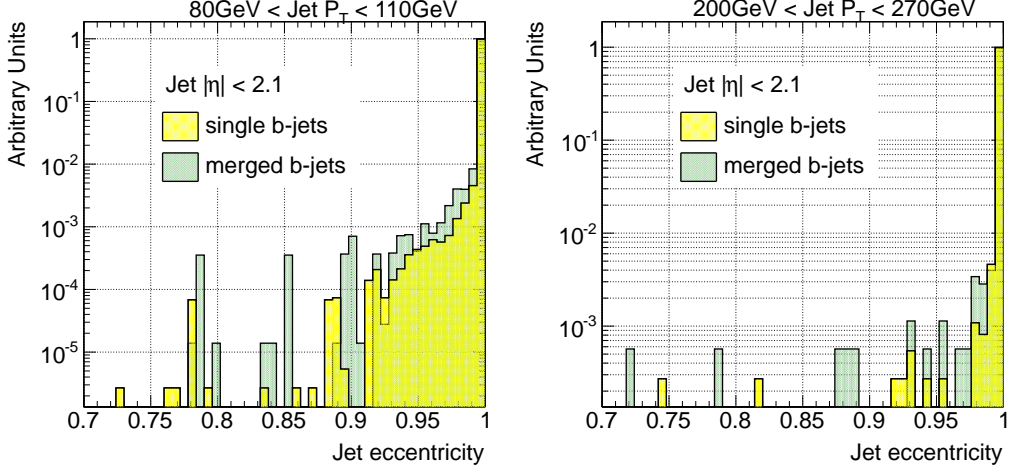


Figure 1.14: Distribution of the jet eccentricity for single and merged  $b$ -jets between 80 GeV to 110 GeV (left) and 200 GeV to 270 GeV (right).

angle, respectively. The eigenvalues  $\lambda_m \geq \lambda_p$  of this tensor are associated to the semiminor and semimajor axes of an elliptical jet, in the  $\eta - \phi$  plane. The jet eccentricity, defined below, is a combination of these eigenvalues, and it is a measure of how elongated is the area of a jet,

$$e = \sqrt{1 - r^2} \quad (1.6)$$

where the parameter  $r$  is defined as the ratio of the eigenvalues,

$$r = \frac{\lambda_m}{\lambda_p} = \frac{\sum E_i \eta_i^2 + \sum E_i \phi_i^2 - \sqrt{(\sum E_i \eta_i^2 - \sum E_i \phi_i^2)^2 + 4(\sum E_i \eta_i \phi_i)^2}}{\sum E_i \eta_i^2 + \sum E_i \phi_i^2 + \sqrt{(\sum E_i \eta_i^2 - \sum E_i \phi_i^2)^2 + 4(\sum E_i \eta_i \phi_i)^2}}. \quad (1.7)$$

Figure 1.14 shows the distribution of the jet eccentricity, built using track constituents. No significant difference in eccentricity was found between single and merged  $b$ -jets.

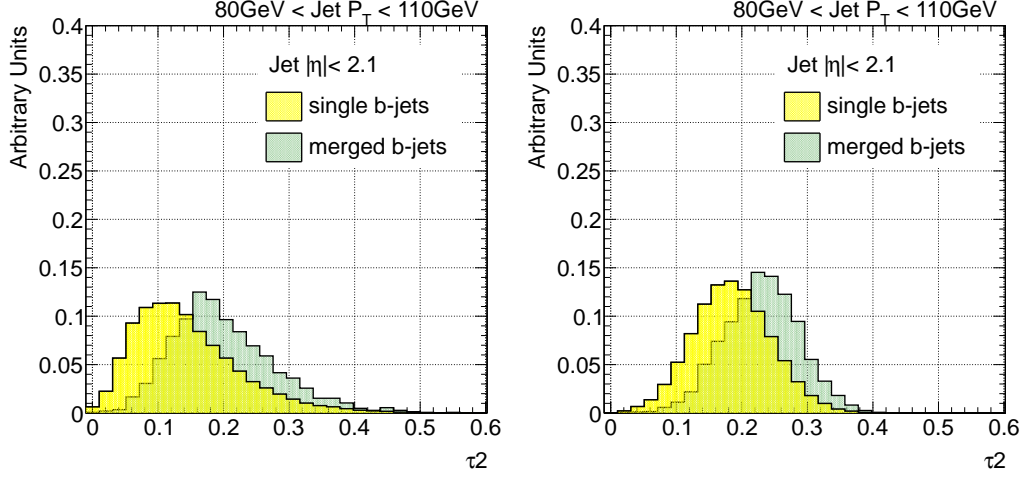


Figure 1.15: Distribution of  $\tau_2$  for single and merged  $b$ -jets between 80 GeV to 110 GeV in anti- $k_T$  0.6 jets using track constituents (left) and anti- $k_T$  0.4 jets using the active area of the jet, with calorimeter topoclusters as input.

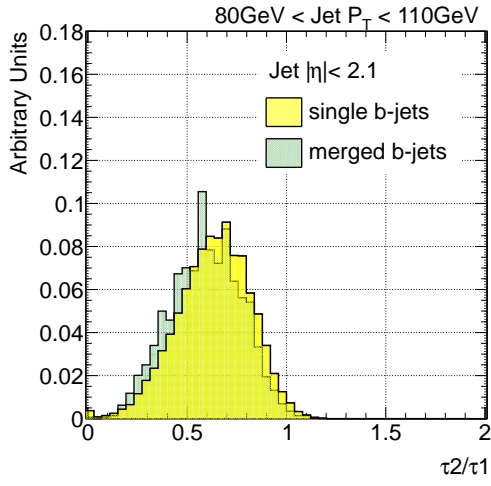
### Further studies

In order to better understand the behavior observed for  $\tau_2$ ,  $\tau_2/\tau_1$  and jet eccentricity in anti- $k_T$  0.4 jets, these variables were studied for other two different scenarios,

- using the active area of jets (with clusters used as input to jet reconstruction).
- using bigger 0.6 anti- $k_T$  jets

in order to enhance the efficiency to capture the decay products in gluon to  $b\bar{b}$ -jets.

Figures 1.16 to 1.17 show distributions of variables mentioned above for single and merged  $b$ -jets between 80 GeV to 110 GeV.



FIGS/TEMPFigs/GhostMatchingVarsClus/Tauratio2080

Figure 1.16: Distribution of  $\tau_2/\tau_1$  for single and merged  $b$ -jets between 80 GeV to 110 GeV in anti- $k_T$  0.6 jets using track constituents (left) and anti- $k_T$  0.4 jets using the active area of the jet, with calorimeter topoclusters as input.

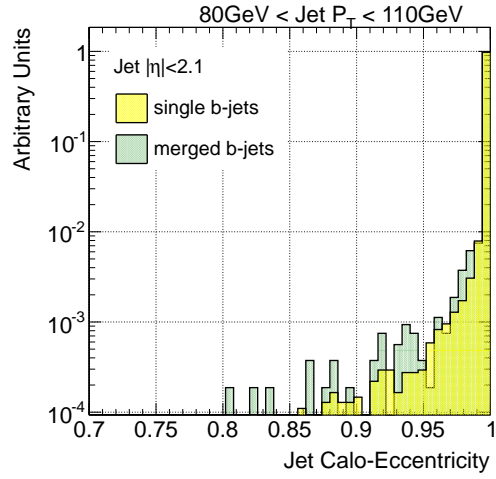
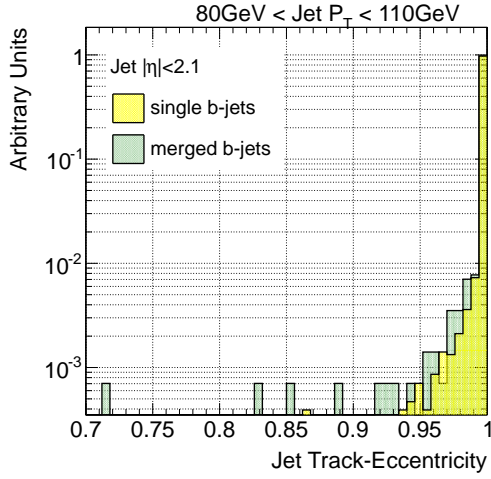


Figure 1.17: Distribution of the jet eccentricity for single and merged  $b$ -jets between 80 GeV to 110 GeV in anti- $k_T$  0.6 jets using track constituents (left) and anti- $k_T$  0.4 jets using the active area of the jet, with calorimeter topoclusters as input.

### 1.3 Validation of the jet variables in data

In order to study the extent to which the simulation reproduces the distributions observed in data for the different variables explored a set of comparison plots is presented. Figures 1.18 and 1.19 show distributions of jet track multiplicity, track-jet width,  $\Delta R$  between the axes of the two  $k_t$  subjets,  $\max\{\Delta R(trk, trk)\}$  and  $\tau_2$  in two different  $p_T$  bins for  $b$ -tagged jets in di-jet Monte Carlo and data events passing selection described in Section 1.1.1. The distributions are normalized to unit area to allow for shape comparisons. There is a good agreement between data and simulation.

It should be remarked that the observed agreement is actually not a direct validation of the description in the MC of the relevant variables, but its convolution with the simulated relative fractions of light-,  $c$ -,  $b$ - and  $bb$ -jets in the  $b$ -tagged generated jet sample. To some extent, there could be some level of compensation between these two effects, although the agreement evaluated in  $b$ -jets selected with a looser cut of MV1 tagger as well as with another  $b$ -tagging algorithm is still very good, suggesting that this compensation is not likely to occur in samples sufficiently enriched in  $b$ -jets.

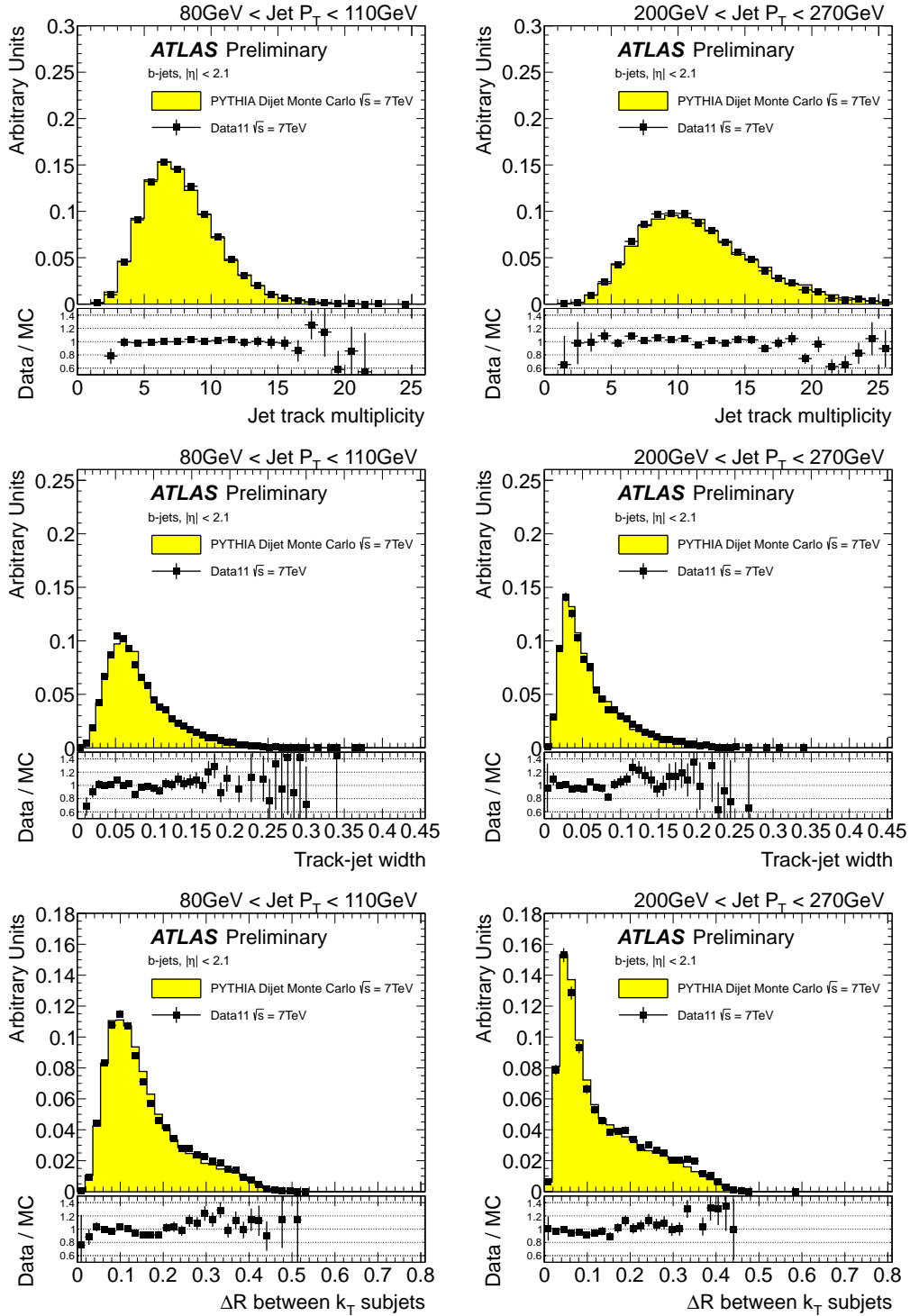


Figure 1.18: Distribution of three tracking variables in 2 different jet  $p_T$  bins, for experimental data collected by ATLAS during 2011 (solid black points), and simulated data (filled histograms)<sup>24</sup>. The ratio data over simulation is shown at the bottom of each plot.

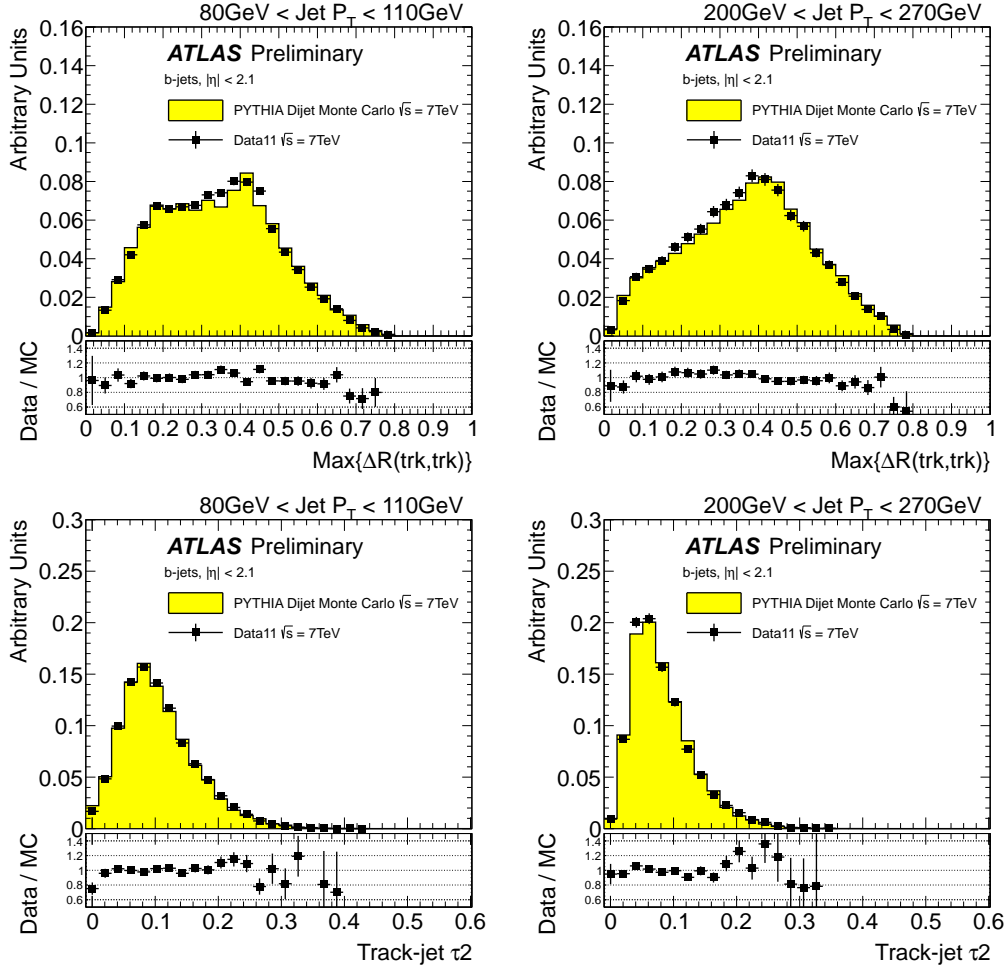


Figure 1.19: Distribution of two tracking variables in two different jet  $p_T$  bins, for experimental data collected by ATLAS during 2011 (solid black points), and simulated data (filled histograms). The ratio data over simulation is shown at the bottom of each plot.

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