

LOO_MRP Simulation Design document

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13/09/2021

This document will describe the simulations we plan to conduct and the expected results from using `loo` and `weighted_loo` (`wtd_loo`) to do model comparisons.

Description of variables

Say we want to explore having variables that are **strongly/weakly predictive of the outcome** and **strongly/weakly predictive of the response**. We will have 4 variables X_1 , X_2 , X_3 and X_4 , and an outcome Y . Lets suppose:

Variable type	Weakly predictive of the (svy) response	Strongly predictive of the (svy) response
Weakly predictive of the outcome	X_1	X_3
Strongly predictive of the outcome	X_2	X_4

All the X 's were sampled unevenly from the population, which gives us strong indication for incorporating inclusion probability in our models.

We expect $2^4 - 1 = 15$ different models for the combination of these variables. If we ran these models (in R syntax):

- 1) $Y \sim X_1 + X_2 + X_3 + X_4$
- 2) $Y \sim X_1 + X_2 + X_3$
- 3) $Y \sim X_1 + X_2 + X_4$
- 4) $Y \sim X_1 + X_3 + X_4$
- 5) $Y \sim X_2 + X_3 + X_4$
- 6) $Y \sim X_1 + X_2$
- 7) $Y \sim X_1 + X_3$
- 8) $Y \sim X_1 + X_4$
- 9) $Y \sim X_2 + X_3$
- 10) $Y \sim X_2 + X_4$
- 11) $Y \sim X_3 + X_4$
- 12) $Y \sim X_1$
- 13) $Y \sim X_2$

- 14) $Y \sim X_3$
- 15) $Y \sim X_4$
- 16) $Y \sim X_1$
- 17) $Y \sim X_2$
- 18) $Y \sim X_3$
- 19) $Y \sim X_4$
- 20) $Y \sim X_1 + X_2$
- 21) $Y \sim X_1 + X_3$
- 22) $Y \sim X_1 + X_4$
- 23) $Y \sim X_2 + X_3$
- 24) $Y \sim X_2 + X_4$
- 25) $Y \sim X_3 + X_4$
- 26) $Y \sim X_1 + X_2 + X_3$
- 27) $Y \sim X_1 + X_2 + X_4$
- 28) $Y \sim X_1 + X_3 + X_4$
- 29) $Y \sim X_2 + X_3 + X_4$
- 30) $Y \sim X_1 + X_2 + X_3 + X_4$

What should we expect?

If we only look at models #1-4, the expected performance is that using `loo` as comparison, it should pick out X_2 and X_4 as they are **strongly predictive of the outcome**. But if we use the `wtd_loo` as comparisons, it should pick out X_4 as we now take into account the survey design and weights accordingly, and X_4 is **strongly predictive of the survey response**.